

Optimized and formally verified compilation for a VLIW processor

Cyril Six

▶ To cite this version:

Cyril Six. Optimized and formally verified compilation for a VLIW processor. Programming Languages [cs.PL]. Université Grenoble Alpes, 2021. English. NNT: . tel-03326923v1

$\begin{array}{c} {\rm HAL~Id:~tel\text{-}03326923} \\ {\rm https://hal.science/tel\text{-}03326923v1} \end{array}$

Submitted on 26 Aug 2021 (v1), last revised 10 Dec 2021 (v2)

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.



THÈSE

Pour obtenir le grade de

DOCTEUR DE L'UNIVERSITÉ GRENOBLE ALPES

Spécialité : Informatique Arrêté ministériel : 25 mai 2016

Présentée par

Cyril SIX

Thèse dirigée par **David MONNIAUX**, Université Grenoble Alpes et codirigée par **Sylvain BOULME**, Grenoble INP

préparée au sein du Laboratoire VERIMAG dans l'École Doctorale Mathématiques, Sciences et technologies de l'information, Informatique

Compilation optimisante et formellement prouvée pour un processeur VLIW

Optimized and formally-verified compilation for a VLIW processor

Thèse soutenue publiquement le **13 juillet 2021**, devant le jury composé de :

Monsieur David Monniaux

DIRECTEUR DE RECHERCHE, Université Grenoble Alpes, CNRS, Grenoble INP, Verimag, Directeur de thèse

Monsieur Adam Chlipala

MAITRE DE CONFERENCE, MIT, Rapporteur

Monsieur Xavier Leroy

PROFESSEUR, Collège de France, PSL Research University, Rapporteur

Madame Laure Gonnord

MAITRE DE CONFERENCE, Université Lyon1, LIP, Inria, Examinatrice

Madame Delphine Demange

MAITRE DE CONFERENCE, Université Rennes, Inria, CNRS, IRISA, Examinatrice

Monsieur Alain Girault

DIRECTEUR DE RECHERCHE, Inria, Université Grenoble Alpes, Examinateur



Abstract

Software programs are used for many critical roles. A bug in those can have a devastating cost, possibly leading to the loss of human lives. Such bugs are usually found at the source level (which can be ruled out with source-level verification methods), but they can also be inserted by the compiler unknowingly. CompCert is the first commercially available optimizing compiler with a formal proof of correctness: compiled programs are proven to behave the same as their source programs. However, because of the challenges involved in proving compiler optimizations, CompCert only has a limited number of them. As such, CompCert usually generates low-performance code compared to classical compilers such as GCC. While this may not significantly impact out-of-order architectures such as x86, on in-order architectures, particularly on VLIW processors, the slowness is significant (code running half as fast as GCC -O2). On VLIW processors, the intra-level parallelism is explicit and specified in the assembly code through "bundles" of instructions: the compiler must bundlize instructions to achieve good performance.

In this thesis, we identify, investigate, implement and formally verify several classical optimizations missing in CompCert. We start by introducing a formal model for VLIW bundles executing on an interlocked core and generate those bundles through a postpass (after register allocation) scheduling. Then, we introduce a prepass (before register allocation) superblock scheduling, implementing static branch prediction and tail-duplication along the way. Finally, we further increase the performance of our generated code by implementing loop unrolling, loop rotation and loop peeling – the latter being used for Loop-Invariant Code Motion. These transformations are verified by translation validation, some of them with hash-consing to achieve reasonable compilation time.

We evaluate each introduced optimization on benchmarks, including Polybench and TACleBench, on the KV3 VLIW core, ARM Cortex A53, and RISC-V "Rocket" core. Thanks to this work, our version of CompCert is now only 16% slower (respectively 12% slower and 30% slower) than GCC -O2 on the KV3 (respectively ARM and RISC-V), instead of 50% (respectively 38% and 45%).

Keywords: Embedded, Optimization, Formal Verification, VLIW, Compilation

Résumé

On utilise des logiciels pour différents rôles, parfois critiques. La présence d'un bogue dans un logiciel peut avoir un coût dévastateur, pouvant aller jusqu'à la perte de vies humaines dans les cas les plus extrêmes. Les bogues viennent en général du code source (ceux-là peuvent être détectés par des méthodes de vérification formelle sur le langage source), mais ils peuvent être également générés par le compilateur. CompCert est le premier compilateur optimisant commercialisé comportant une preuve formelle de correction : il est formellement prouvé que les programmes compilés avec cet outil ont le même comportement que leurs programmes sources originels. Cependant, comme prouver les optimisations d'un compilateur relève d'un défi considérable, CompCert n'en a qu'un nombre limité. Ainsi, en général CompCert génère du code moins performant comparé à d'autres compilateurs classiques tels que GCC. Bien que cela n'impacte peu les architectures à exécution dans le désordre telles que x86, sur des architectures à exécution dans l'ordre, et en particulier sur des processeurs VLIW, le ralentissement est important (le code résultant est deux fois plus lent que GCC -O2). Sur un processeur VLIW, le parallélisme d'instructions est explicite et spécifié dans le code assembleur par des bundles (paquets) d'instructions : le compilateur doit paquétiser les instructions pour obtenir une bonne performance.

Le but de cette thèse est d'identifier, d'enquêter, d'implémenter et de vérifier formellement plusieurs optimisations classiques manquantes dans CompCert. Tout d'abord, j'introduis un model formel d'exécution de *bundles* VLIW sur processeur à pipeline imbriqué. Nous génèrons ces *bundles* à partir d'un réordonnancement en *postpass* (après allocation de registres). Ensuite, j'introduis un réordonnancement de superblocks en *prepass* (avant allocation de registres). Ce travail implique aussi l'introduction d'une prédiction statique de branchements, et une duplication de queue. Enfin, pour continuer d'augmenter la performance du code généré, j'introduis du déroulage, rotation, et pelage de boucles – ce dernier étant utilisé dans du déplacement d'invariants de boucles. Ces transformations sont vérifiées par validation de translation, et certaines utilisent du partage maximal afin d'obtenir des temps de compilation raisonnables.

Nous avons évalué chacune de ces optimisations sur des tests de performance, dont Polybench et TACLeBench, sur le coeur VLIW KV3, l'ARM Cortex A53, et le coeur RISC-V "Rocket". Grâce à nos travaux, notre version de CompCert est maintenant seulement 16% plus lente (respectivement 12% et 30% plus lente) que GCC -O2 sur KV3 (respectivement ARM et RISC-V), au lieu de 50% (respectivement 38% et 45%).

Mots-clefs: Embarqué, Optimisations, Vérification Formelle, VLIW, Compilation

Acknowledgements

I deeply thank Adam Chlipala and Xavier Leroy for their detailed and insightful reviews. I also thank Laure Gonnord, Delphine Demange and Alain Girault for taking part in this thesis jury. It is an honor for me.

I started this thesis without any prior notion of formal proofs or functional programming and barely any practical experience in compilers. This adventure was quite interesting (but very rewarding), to say the least. I was glad to have Sylvain Boulmé by my side for helping me navigate through the jungle of formal proof engineering in Coq and formal concepts in general. I have learned a lot from him and his teachings; his deep knowledge of Coq and proof methods has been invaluable. Complementary to Sylvain, David Monniaux was also very helpful both for general thesis direction and for having excellent ideas that, more often than not, led to promising results. Last but not least, I want to thank Benoît Dupont de Dinechin for ensuring I have an excellent environment at Kalray for working on my thesis and for his helpful insights on optimizing compilers.

I want to thank the persons of the VERIMAG laboratory for providing me with a great work environment. I also want to thank the doctoral school EDMSTII for having been very understanding and amenable throughout the thesis. In particular, they participated in the opportunity for me to attend the DeepSpec Summer School of 2018 (DSSS'18) at the Princeton University. Thanks to their most excellent program and teachers, my knowledge level of Coq and formal proofs got boosted through the roof.

I want to thank two additional persons: Florent-Bouchez Tichadou and Fabrice Rastello. I believe that most of life is the result of lucky opportunities; these two persons introduced me to the CORSE research team and gave me the will to pave my own way into optimizing compilers studies. I sincerely thank both of them. I also want to thank my wonderful teacher Christophe Brouillard, who showed me the wonderful world of mathematics and gave me the first glimpse of what research looks like. Finally, I thank Duco Van Amstel for having such a pleasant and memorable discussion, after which I was sure to head towards doctoral studies!

I thank my lab and company student mates Amaury, Arthur, Bai, Clément, Maëva, Matheus, Rémy, Valentin, Vincent, Yanis. Many meals, funny discussions, and horoscopes were shared. I also thank my former lab (CORSE) student mates for all the interesting discussions about compilation, performance, or any other subject. Among them, I'm thinking of Antoine, Diogo, Emmanuelle, Fabian, Imma, Luis, Nicolas, Thomas; but there are others!

Three years (and a half) is a lot of time, during which I met many people who inspired me on a personal level and have encouraged me throughout this adventure. I want to thank the Rainbow Swingers chorus, particularly Andrea, Antoine (x2), Benjamin, Cécile, Charlotte,

Chloé, Clémentine, Cyrielle, Geoffroy, Juliette, Kevin, Marion, Maxime, Maximin, Raphaël, Solène, Sophia, Véronique (and many others!) with who I had such a wonderful time. Lastly, I want to thank my other wonderful friends who have inspired me on many occasions: Alex, Aurélien, Bastien, Clémentine, Corentin, Freddy, Guillaume, Hannah, Inès, Jean, Joseph, Julien, Laurie, Lucie, Marine, Maxime, Nicolas, Olga, Pierre, Virginie.

Lastly, I want to thank the three persons that are the most important to me.

My grandmother has always adored me and has been ever-loving since I was born.

My father taught me to always keep working for my goals and never give up.

My mother encouraged me to follow my dreams, whatever happens.

These persons have always been there to support me throughout my whole life.

Thank you immensely for being there and believing in me!

Remerciements

Je remercie profondément Adam Chlipala et Xavier Leroy qui ont pris le temps de lire cette thèse en tant que rapporteurs : leurs remarques détaillées ont été extrêmement utiles. Je remercie également Laure Gonnord, Delphine Demange et Alain Girault pour faire parti de ce jury. C'est un immense honneur pour moi.

Le démarrage de cette thèse fut une épopée. Je n'avais pratiquement aucune connaissance en matière de preuve formelle, programmation fonctionnelle, ou même de l'expérience pratique en compilation. Cette thèse a été une aventure fructueuse et formatrice, notamment grâce à mon encadrant Sylvain Boulmé. Sylvain était mon guide dans la jungle des preuves formelles en Coq et des formalismes en général. J'ai énormément appris de lui, autant de par sa personne que de par ses enseignements; sa connaissance de Coq et des méthodes formelles a été un atout indispensable pour ma thèse. Mon directeur de thèse, David Monniaux, a également été formidable, autant pour la direction de la thèse que pour ses idées qui ont quasiment toujours mené à des résultats prometteurs. Enfin, je remercie Benoît Dupont de Dinechin pour m'avoir instauré un cadre de travail idyllique à Kalray, en plus d'avoir été une référence en matière de compilation optimisante.

J'ai passé trois super années de thèse au sein de VERIMAG, et je remercie toutes les personnes de ce laboratoire pour cela. Je remercie également l'école doctorale EDMSTII : ça a toujours été un plaisir d'avoir affaire à eux sur le côté administratif, et ils m'ont donné l'opportunité de participer à des écoles d'été, en particulier l'école d'été DeepSpec Summer School 2018 (DSSS'18) à l'université de Princeton. Les cours exemplaires de DSSS'18 m'ont permis de relever de façon conséquente mon niveau de connaissances en preuves formelles, ce qui s'est révélé être un atout considérable pour ma thèse.

Je tiens également à remercier Florent-Bouchez Tichadou et Fabrice Rastello. Si je devais résumer ma vie, je dirais que c'est tout d'abord des rencontres — ces deux personnes en particulier m'ont introduit au sujet de la recherche en compilation, et m'ont donné l'envie de poursuivre dans cette voie! Je tiens également à remercier mon professeur de prépa Christophe Brouillard; il m'a montré la beauté des mathématiques, et m'a permis d'avoir un premier aperçu de la recherche. Enfin, je remercie Duco Van Amstel pour une discussion autour d'un verre qui a scellé mon envie de poursuivre en doctorat.

Je remercie mes camarades du laboratoire ou de Kalray : Amaury, Arthur, Bai, Clément, Maëva, Matheus, Rémy, Valentin, Vincent, Yanis. Avec eux j'ai passé beaucoup de repas partagés, de discussions intéressantes, et même d'horoscopes amusants. Je remercie aussi les collègues de mon ancienne équipe (CORSE) pour les discussions orientés performance, compilation, ou juste

tout autre sujet. Je pense à Antoine, Diogo, Emmanuelle, Fabian, Imma, Luis, Nicolas, Thomas; mais il y en a d'autres!

Trois ans (et un petit demi) c'est une sacré durée. J'ai eu l'occasion de rencontrer beaucoup d'autres personnes qui m'ont encouragé tout au long de ma thèse, et qui ont été source d'inspiration sur un plan personnel. Je remercie les personnes de la chorale des Rainbow Swingers, en particulier Andrea, Antoine (x2), Benjamin, Cécile, Charlotte, Chloé, Clémentine, Cyrielle, Geoffroy, Juliette, Kevin, Marion, Maxime, Maximin, Raphaël, Solène, Sophia, Véronique (et beaucoup d'autres!) avec qui j'ai passé des moments inoubliables. Je remercie également tous mes autres amis proches et adorables: Alex, Aurélien, Bastien, Clémentine, Corentin, Freddy, Guillaume, Hannah, Inès, Jean, Joseph, Julien, Laurie, Lucie, Marine, Martin, Maxime, Nicolas, Olga, Pierre, Virginie. Cela a été un réel plaisir de partager du temps avec vous tout au long de ma thèse!

Enfin, je veux remercier trois personnes qui ont été là tout au long de ma vie, et ont toujours cru en moi.

Mamie, tu as toujours été très aimante et une grande confidente depuis que je suis né.

Papa, tu m'as appris à ne jamais abandonner et à toujours viser plus haut.

Maman, tu as toujours été là pour m'encourager dans ma vie peu importe les situations.

Vous avez toujours été là pour me soutenir dans ma vie, et je suis fier de vous avoir comme parents et grand-parent.

Contents

Co	Contents						
I	Background						
1	Introduction						
	1.1	Gener	al motives	3			
		1.1.1	Software Verification	3			
		1.1.2	Compilation	4			
		1.1.3	The need for formally verified compilation	5			
		1.1.4	Verifying software with Coq	6			
		1.1.5	VLIW processors in the context of critical applications	7			
	1.2	The K	alray KV3 architecture	9			
	1.3	The C	OMPCERT formally-verified compiler as of today	11			
		1.3.1	Overview of CompCert	11			
		1.3.2	CompCert 's framework for proving transformation passes correctness .	13			
	1.4	Motiv	ations of this thesis and contributions	15			
2	Rela	ated W	ork	19			
	2.1	2.1 Compiler optimizations for VLIW processors					
		2.1.1	Instruction scheduling	19			
		2.1.2	Loop transformations	20			
		2.1.3	Other optimizations	21			
	2.2	Forma	ally proven compiler transformations	22			
		2.2.1	Advanced compiler optimizations in CompCert	22			
		2.2.2	Other related work	24			
II	Fo	rmally	y Verified Optimizations	25			
3	For	mal Ve	rification of Basic-Block Scheduling at Asm level	27			
	3 1	∆sm\/	I IW: semantics for a VI IW assembly language	30			

		3.1.1	Overview of CompCert's Asm IR	30
		3.1.2	Syntax of Bundles & Basic Blocks	31
		3.1.3	Parallel Semantics of AsmVLIW	32
		3.1.4	Sequential Semantics in Asmblock	34
	3.2	Retriev	ving the basic block structure with Machblock	35
		3.2.1	The Mach IR of CompCert	35
		3.2.2	Necessity of Constructing Basic Blocks at the Mach Level	37
		3.2.3	Machblock: generating basic blocks from Mach	37
	3.3	Asmbl	ock: adapting the Mach to Asm translation for basic blocks	38
		3.3.1	Translating and proving Mach code to Asm	39
		3.3.2	Translating Machblock to Asmblock	41
		3.3.3	Proof of Forward Simulation	46
	3.4	Forma	l verification of the basic block postpass scheduling	51
		3.4.1	AbstractBasicBlock IR	53
		3.4.2	Parallelizability Checker	54
		3.4.3	Verifying Intrablock Reordering	55
		3.4.4	Generic and Verified Hash-Consing	57
		3.4.5	Peephole Optimization	58
		3.4.6	Atomic Sequences of Assignments in AbstractBasicBlock	59
4	Gen	eral Co	oncepts of Superblock Scheduling	61
	4.1	Guidir	ng trace selection with branch prediction	62
		4.1.1	What we expect out of static branch prediction	63
			Storing the prediction	65
		4.1.2	Storing the prediction	05
		4.1.2 4.1.3	Acquiring prediction information	66
			Acquiring prediction information	
	4.2	4.1.3 4.1.4		66
	4.2	4.1.3 4.1.4	Acquiring prediction information	66 68
	4.2	4.1.3 4.1.4 Supert	Acquiring prediction information	66 68 70
	4.2	4.1.3 4.1.4 Superb 4.2.1 4.2.2	Acquiring prediction information	66 68 70 73
		4.1.3 4.1.4 Superb 4.2.1 4.2.2	Acquiring prediction information	66 68 70 73 73
		4.1.3 4.1.4 Superb 4.2.1 4.2.2 Superb	Acquiring prediction information	66 68 70 73 73 75
		4.1.3 4.1.4 Superb 4.2.1 4.2.2 Superb 4.3.1	Acquiring prediction information	66 68 70 73 73 75 77
		4.1.3 4.1.4 Supert 4.2.1 4.2.2 Supert 4.3.1 4.3.2 4.3.3	Acquiring prediction information	66 68 70 73 73 75 77
	4.3	4.1.3 4.1.4 Supert 4.2.1 4.2.2 Supert 4.3.1 4.3.2 4.3.3	Acquiring prediction information	66 68 70 73 73 75 77 79 80
	4.3	4.1.3 4.1.4 Superb 4.2.1 4.2.2 Superb 4.3.1 4.3.2 4.3.3 Superb	Acquiring prediction information	666 688 700 733 755 777 799 800 811
5	4.3	4.1.3 4.1.4 Superb 4.2.1 4.2.2 Superb 4.3.1 4.3.2 4.3.3 Superb 4.4.1 4.4.2	Acquiring prediction information	666 688 700 733 755 777 79 800 811 822

		5.1.1	Overview of RTL	86
		5.1.2	Modeling speculative loads in RTL	89
		5.1.3	Modeling branch prediction	91
	5.2	Repres	senting superblocks as execution paths in RTLpath	92
		5.2.1	RTLpath syntax and informal semantics	93
		5.2.2	RTLpath formal semantics	96
		5.2.3	Bisimulation between RTLpath and RTL semantics	98
	5.3	Genera	ating RTLpath paths from RTL	101
		5.3.1	RTLpath generation oracle	103
		5.3.2	Pathmap verifiers	107
		5.3.3	RTLpath state equality modulo liveness	109
6	Fori	nal Vei	rification of Code Duplication Transformations	111
	6.1	Proof	of correction through a forward simulation	112
	6.2	Verifie	r implementation	114
	6.3	Modul	e system	114
	6.4	Modifi	cations to support branch swapping	115
7	Fori	nal Vei	rification of Superblock Scheduling	117
	7.1	Abstra	ct Symbolic Execution for Superblocks	119
		7.1.1	Abstract symbolic states and execution semantics	121
		7.1.2	Superblock symbolic execution	129
		7.1.3	Bisimulation between RTLpath and symbolic execution semantics	130
	7.2	Provin	g Lockstep Simulation of Scheduling from Sufficient Conditions on Ab-	
		stract S	Symbolic Executions	134
		7.2.1	Simulation of superblocks	134
		7.2.2	Simulation Test Specification and Superblock Scheduling Lockstep Sim-	
			ulation	140
	7.3	Refine	d Simulation Test with Hash-Consing	143
		7.3.1	Refined Symbolic States and Refinement Relations	144
		7.3.2	Simulation test specifications and implementation	150
		7.3.3	Canonization of Refined Symbolic Values	155
Ш	Ex	perim	ents 1	159
8	Perf	Orman	ce Tuning of Superblock Formation, Selection, Linearization	161
J	8.1		selection and tail-duplication	161
	0.1	8.1.1	Trace partitioning	163
			Tail-duplication	165
		U. I. ∠	Tall Qui/IIVallVII	111

	8.2	Loop u	unrolling, peeling and rotation	168
		8.2.1	Innermost loop detection	170
		8.2.2	Loop unrolling	171
		8.2.3	Loop rotation	172
	8.3	Adapti	ng the Linearize oracle for superblocks	173
		8.3.1	Original Linearize heuristics from CompCert	175
		8.3.2	Modifications to the heuristics for superblocks	178
	8.4	Static 1	branch prediction	179
		8.4.1	Implementing Branch Prediction for Free	179
		8.4.2	A new heuristic for predicting branches inside loops	180
9	Imp	lement	ing the Scheduling Oracles	183
	9.1	Postpa	ss Scheduling Oracle	184
		9.1.1	Postpass frontend	185
		9.1.2	Postpass backend	188
	9.2	Prepas	s Scheduling Oracle	189
		9.2.1	Additional dependencies for conditional branches	190
		9.2.2	Prepass scheduling algorithms	191
10	Expe	erimen	tations	195
	10.1	Experi	mental setup	195
		10.1.1	Measured processors	196
		10.1.2	Measuring methods	197
		10.1.3	Benchmarks used	197
	10.2	Impact	t of postpass scheduling	199
		10.2.1	Performance	199
		10.2.2	Compilation times of postpass scheduling on KV3	201
	10.3	Impact	t of superblock scheduling related optimizations	202
		10.3.1	Evaluation of our static branch prediction	202
		10.3.2	Evaluation of our superblock linearizer	204
		10.3.3	Evaluation of loop unrolling, loop rotation and tail-duplication threshold	s 205
		10.3.4	Performance impact of each added optimization	208
		10.3.5	Evaluation of the different prepass scheduling strategies	209
		10.3.6	Gains of loop unrolling without prepass scheduling	210
	10.4	СомРС	CERT VS GCC in our current iteration	212
		10.4.1	COMPCERT VS GCC on the KV3 architecture	212
		10.4.2	COMPCERT VS GCC on AArch64 and RiscV architecture	217
11	Con	clusion	1	219
	111	Summ	0777	210

	11.2 Reflexions and Future Work	220
A	Non-exhaustive instruction listing of the KV3 core	A 1
Bi	ibliography	

Part I

Background

Introduction

1.1 General motives

1.1.1 Software Verification

In the past decades, our reliance on software to conduct repetitive and sensitive tasks has grown tremendously. Whether it be to fly a space rocket, manage bank deposits, or just ordering your next meal, software programs are now almost everywhere.

Due to their human manufacturing, software programs are prone to errors. A wrong design, a miscommunication within the development team, or just a faulty line inserted on a Friday afternoon: it suffices of a tiny error, a tiny misconception, to make a software program crash – or worst, behave erratically. These errors (called "bugs" ¹) may have varying effects based on the nature of the application.

If there is a bug on your meal ordering application, you could probably have the wrong meal ordered or have to order it a second time because the application crashed. A bug in your message delivery service and your message might not get sent at all. These represent classes of applications that are non-critical: a bug in these might make people lose time, or in general, have minor inconveniences.

Some other applications can have more nasty repercussions if there is a bug in them. In 2013, software defects were found in the United Kingdom's Post Office computer system: people were wrongly accused of stealing money, some of them even going to jail as a result, even though the actual cause was a false accounting within the software [68].

Software bugs in aerospace applications can have dire consequences. In 1996, the Ariane 5 space rocket physically exploded on its maiden flight because of miscasting a 64-bits floating-point variable into a 16-bits integer, causing the propulsion system to flip the rocket [59]. In 2009, four unfortunate passengers of an ES350 Toyota car died after their car's accelerator pedal got stuck and the brakes did not apply enough pressure to stop the car. Several investigations were led in the early 2010s to investigate this incident among others; software bugs were found to be the

¹The term "bug" became popular after an unfortunate moth caused a hardware error on the Mark II computer, though it has been part of the engineering jargon since the 1870s [60].

likely cause of this incident [45]. In 2021, a software bug from Orange made all urgency calls unreachable for several hours in France, resulting in at least five deaths [35].

The prevention and detection of software bugs have been an ongoing area of research for the past decades. Ensuring that critical software is bug-free (or at least free of any bug that could cause harm) may involve various techniques. Some involve executing the program to look for faulty behaviors, either through extensive testing (Parnas et al. [70]; Parnas et al. [69]) or runtime verification (Leucker and Schallhart [53]; Bartocci et al. [7]). Others rely on deriving properties based on the source code itself: this can be done through static analysis (Blanchet et al. [12]) or formal verification (Yoo et al. [101]).

1.1.2 Compilation

The execution of software programs on processors requires them to be encoded in binary machine code. Traditionally, this machine code is obtained by translating a textual representation called *assembly language*. Each separate code module, written in assembly, is translated into *object machine code* through an *assembler*. Then, a *linker* is used for gathering all objects code into one binary machine code, ready to be executed on a given machine.

One caveat of assembly language is that it is too close to the machine: it does not provide enough abstraction for developing software. As such, producing software directly in machine code is inefficient and error-prone.

To leverage this issue, high-level languages were invented to ease software development. Among them, the C language became one of the most popular for embedded systems primarily because of its portability (the same C code can be compiled on many different processor architectures) and its closeness to actual machine code, making it possible to fine-tune C code to get similar performance than with concrete machine code.

The process of translating C code to machine code is called *compilation* and is done through a *compiler*. The compilation process is usually split into several passes: a *frontend* that transforms C code into a given *intermediate representation* (*IR*) of the compiler, and finally a *backend* that gradually transforms this IR into an assembly code suitable for the target machine. Once this is done, the *assembler* and *linker* can then generate the final machine code.

During the compilation process, the compiler can optimize the code: performing transformations that aims to have a faster machine code, a smaller machine code, or sometimes both.

1.1.3 The need for formally verified compilation

The compiler, assembler and linker are all pieces of software: there may be bugs in those. In particular, compilers are considered one of the most complex pieces of software; they usually involve intricate transformation passes, especially when optimizing the code.

As such, properties that were proved at a source level might not be valid anymore if the compiler introduced a bug. Compilers are usually thoroughly tested to trim out any major bug. However, it is not physically possible to test all the possible cases because there are infinitely many of them: even with thorough testing, there might still be bugs hidden in corners.

While this is of little to no concern for most applications, it is concerning for critical applications. The probability of having a major accident happening one day because of a compiler bug is not null.

To tackle this potential issue, some classes of applications require traceability between the object code and the source code (for example, the DO-178B requirements for avionics [42]). Such traceability is generally challenging to get on compilers without relying on manual annotations [79]. It is also compromised by many compiler optimizations, though some recent research attempts at tackling this issue (Li et al. [54]). In some critical systems, traceability is ensured by turning off all optimizations of compilers [8].

Turning off all optimizations comes with a downside: the resulting code is usually bigger and takes more time to execute. This, in turn, increases the worst-case execution time (WCET) and the energy consumption (more cycles are spent for performing the same task).

One way to tackle these issues is to use a formally verified compiler.

The CompCert certified compiler (Leroy [50, 51]) is the first optimizing C compiler with a formal proof of correctness that is used in industry [8; 43]. In particular, it does not have the middle-end bugs usually found in compilers [100], thus making it a significant success story of software verification.

CompCert features several middle-end optimizations (constant propagation, inlining, common subexpression elimination, etc.) as well as some backend optimizations (register allocation using live ranges, clever instruction selection on some platforms).

Using CompCert allows to have both compiler optimizations and formal guarantees: it proves a property of semantic preservation between the source code and the generated assembly code. In other words, the proofs done on the C source code remain valid on the assembly code generated by CompCert. ²

²Small note: CompCert proof of semantic preservation only holds for executions free of undefined behaviours.

CompCert is used in several projects, among which:

- Vélus[18; 17], a formally-verified compiler for the Lustre dataflow language [39]. It consists of a Lustre frontend branched into the Clight IR of CompCert. Our version of CompCert is compatible with a modified version of Vélus [80].
- CertiKOS: an architecture for building formally-verified concurrent OS kernels [38]. They use CompCertX, a thread-safe version of CompCert [37].
- The Verified Software Toolchain [2], comprising tools to prove properties about the program's behavior at source level using a dialect of C (Verifiable C [3]). The program is then plugged into CompCert via the Clight intermediate representation.

1.1.4 Verifying software with Coo

Using Coq is one possible technique to verify software. [10] Coq is both a (functional) programming language and a proof description language. The typical workflow in Coq is to write code in Gallina (Coq's programming language) and then specify theorems about that code. Coq's code is then extracted to other languages, typically OCAML or Haskell.

Given a list sorting algorithm sort_list written in Gallina, an example of theorem could be "For each possible input list 1, (sort_list 1) is sorted".

To prove such theorems, one writes a list of tactics to apply, such as destructing the theorem into different cases, introducing variables from forall quantifiers, or using the result of another (previously proved) theorem.

The trusted computing base (TCB) of Coq is intentionally small: most of its datatypes are provided in the form of formally proven libraries instead of built-in types. For example, Coq does not natively support integers or even booleans: instead, several integer libraries exist, each supplying their definition of what integers (or booleans) are, the possible operations on them and their associated lemmas (such as the associativity of the addition).

Coo proofs give a high level of assurance; if there is a bug in code verified in Coo, it may come from either:

- The Coq extractor (the part of Coq that converts a Gallina program into OCAML (or Haskell), which can then be compiled); though recent work has been done towards a fully verified Coq extractor, such as Savary Bélanger et al. [84] or Forster and Kunze [34].
- The compiler of the language used after extraction (e.g. OCAML's compiler).
- A problem in the specification written in Coq: under-specification, wrong modeling, or axiomatizing wrong hypotheses.

Most of the time, bugs of programs written in Coo come from the latter.

A disadvantage of Coq is that some proofs can be very tedious to perform (it usually takes much more time to prove code than writing it). Proving code in Coq usually involves cutting each piece of code finely into smaller fragments, each of which can then be proven more easily and then patching all these fragments together into one bigger theorem. When the code can hardly be cut in such fragments, one must rely on finding proof invariants or other techniques. In particular, most of the time, the Coq proof must be changed when the Coq code is modified; though some automation tactics exist to remedy that, an overly-automated proof can be very tricky to untangle when it becomes invalid because of a change.

One way to avoid this caveat for some challenging problems, as has initially been explored by Tristan and Leroy [95], is to apply *a posteriori* verification: an untrusted oracle (e.g. written in OCAML) returns its result to a formally proven verifier written in Coq. The verifier then checks the oracle's result for correctness: if the verdict is positive, we have the formal proof that the result is correct.

With this approach, it is also much easier to modify the program transformation (performed by the oracle). Indeed, if it stays within a certain class of program transformations, and if the verifier is complete in regards to that class, then modifying the oracle does not require to modify the verifier or its proof. This is a major advantage, especially for complex optimizations that might require slight changes before reaching their full potential.

The other advantage is that it opens up the range of possible proofs: some problems that would be very hard to prove structurally may become much easier to prove through an a posteriori verifier.

In this thesis, we used a posteriori verification profusely: this allowed us to fine-tune our compiler optimizations without much need for proof modification.

1.1.5 VLIW processors in the context of critical applications

In most architectures, processors are synchronous entities that execute instructions under the beat of a clock. Executing an instruction involves a several-step process: fetching the instruction from memory, decoding the instruction, reading the registers indicated by the instruction, performing the instruction's operation, and finally writing back the result to the destination registers. As such, each instruction typically take several cycles to be completed.

Modern processors processors are organized so that several instructions are evaluated in parallel. Each step is assigned to a processor unit: while a given instruction is decoded, another instruction is getting fetched, and yet another instruction is being evaluated. This process is called *instruction*

pipelining, and the hardware responsible for that is the *processor pipeline*. Most processors have an *interlocked* pipeline: if an operand of an instruction to be executed is not yet ready, the processor inserts *stalls* in the pipeline, which halts the execution of that instruction until its data is ready.

Thanks to this method, as long as there is no starvation in the pipeline and no stall is inserted, processors can virtually execute one instruction per cycle. The process of feeding an instruction through the pipeline is called *issuing* an instruction.

In addition to instruction pipelining and the ever-going quest to get more performance, various techniques have emerged to have processors execute code faster. A first technique has historically been to increase the processors' frequencies; in just decades, the processor frequencies' order of magnitude increased from the MHz all the way to the GHz. However, this technological progress soon hit a wall, as increasing frequency further started to pose challenging issues in terms of miniaturization and temperature increase within the chips.

Another technique has been to issue several instructions per cycle instead of just one, either by allowing the pipeline to process two or more instructions per step or having different distinct pipelines.

In the most extreme case, some processors, including all current x86 architecture processors, can execute instructions ahead of time to fill idle units: these are categorized as *out-of-order* processors since the concrete order of execution might not be the same as the original order of the assembly code. Having such processors allows to have good performance without having to change the assembly code: they minimize the number of cases where instructions have to wait on each other in the pipeline.

However, this comes with a cost: their design is more complex (their hardware circuit requires more space), they are more susceptible to side-channel information leaks (especially when speculative execution is used to decrease the cost of control branches), and they tend to be less energy-efficient.

In contrast, *in-order* processors do not try to reorder instructions. Their design is then simpler, more energy-efficient, and they are also more predictable, which makes them a good fit for embedded systems. Indeed, reasonably tight bounds on worst-case execution time (in most safety-critical applications, the WCET must be estimated by a sound analysis [9]) are more easily obtained on in-order processors than on out-of-order processors. In addition, a simpler design may be more reliable. ³

In-order superscalar processors have hardware logic to detect code dependency at runtime and issue multiple independent instructions in the same cycle. VLIW (Very Large Instruction Word)

³For instance, Intel's Skylake processor had a bug that crashed programs under complex conditions [52].

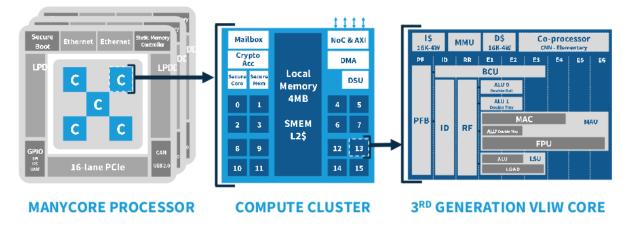


Figure 1.1.: The Coolidge architecture

processors can also issue several instructions in parallel [32], but unlike superscalar processors, the groups of instructions to be issued together (called *bundles*) are expressed directly in the assembly code: each bundle is syntactically separated by a ; ; token.

The caveat of these processors is that since they do not have any reordering at runtime, they rely on compilers' optimizations to produce adequate bundles, and more generally, to ensure good performance. In this thesis, we will mostly tackle two levels of performance issues for VLIW processors:

- The instruction ordering: a bad ordering could lead to either the processor spending most
 of its cycles stalling or having certain units to be idle while they could be executing an
 instruction. Modern out-of-order architectures do not suffer from that, thanks to their
 runtime reordering.
- The cost of branching: on such processors, taking a branch induces a penalty because the pipeline has to be refilled. This penalty is bigger for a conditional branch than for an unconditional branch. Again, modern out-of-order architectures suffer less from this, thanks to their speculative branch execution.

1.2 The Kalray KV3 architecture

The Kalray Coolidge is a manycore processor, as displayed in figure 1.1. It features 5 compute clusters interconnected by a Network-on-Chip. Each compute cluster runs its own code: to deploy an application to the Coolidge architecture, one uses the Kalray compilation tools to create a multi-binary file, which can then be deployed to the processor. External libraries handle the matters of spawning and communication between the clusters; the compiler does not have to worry about it: as such, in this thesis, we focus on programs running on a single cluster.

Each compute cluster contains 16 KV3 VLIW cores, sharing a local memory of 4 MB. Support for parallelism is provided either through libraries made available in a C API or through higher-level languages such as OpenCL combined with specific compiler support [90]. In our case, CompCert has no support for anything related to multi-threading, so we focus here on the execution on one single core (of a single compute cluster).

The Kalray KV3 core implements a 6-issue Fisher-style VLIW architecture [33] (partial predication, dismissible loads, no rotating registers), with an instruction pipeline of 8 stages. It has 64 general-purpose registers of 64-bits used for both integer and floating-point data (a given register can store an integer or a float). It sequentially executes blocks of instructions called *bundles*, with parallel execution within them.

Bundles A *bundle* is a block of instructions that are to be issued into the pipeline at the same cycle. They execute in parallel with the following semantics. If an instruction writes into a register that is read by another instruction of the same bundle, then the value that is read is the value of the register before executing the bundle. If two instructions of the same bundle write to the same register, then the behavior at runtime is non-deterministic. For example, the bundle written in pseudo-code " $R_1 := 1$; $R_1 := 2$ " assigns R_1 non-deterministically. On the contrary, " $R_1 := R_2$; $R_2 := R_1$ " is deterministic and swaps the contents of R_1 and R_2 registers in one atomic execution step. In assembly code, bundles are delimited by ; ; (Fig. 1.2). Compilers must ensure that each bundle does not require more resources than available—e.g., the KV3 has only one load/store unit, thus a bundle should contain at most one load/store instruction. The assembler refuses ill-formed bundles.

Execution Pipeline In the case of the KVX, bundles are executed through an 8-stage interlocked pipeline: the first stage prefetches the next bundle (PF stage), the second decodes it (ID stage), the third reads the registers (RR stage), then the last five stages (E1 through E5) perform the actual computation and write to the destination registers; depending on the instructions, the writes occur sooner or later (e.g., an addition takes fewer stages than a multiplication). If, during the RR stage⁴, one of the read registers of an instruction in the bundle is not available, the pipeline *stalls*: the bundle stops advancing through the pipeline until the register gets its result (Fig. 1.2).⁵

⁴Or the ID stage, for some instructions such as conditional branching.

⁵When a register is read before some prior instruction has written to it, *non-interlocked* VLIW processors use the old value. The compiler must then take instruction latencies and pipeline details into account to generate correct code, including across basic blocks. This is not the case for the KVX, where these aspects are just matters of code efficiency, not correctness.

Cycle	ID	RR	E1	E2	E3	E4+E5	$B1: R_1 := load(R_0 + 0);$
1	B1						• • • • • • • • • • • • • • • • • • • •
2	B2	B1					$B2: R_2 := load(R_0 + 4);;$
3	В3	B2	B1				$B3: R_3 := R_1 + R_2; R_4 := R_1 * R_2;;$
4	B4	В3	B2	B1			$B4: R_3 := R_3 + R_4;$
5	B4	В3	STALL	B2	B1		$B5: store(R_0, R_3);$;
6	B4	В3	STALL	STALL	B2		, , , , ,
7	B5	B4	В3	STALL	STALL		$B6: R_6 := R_7 + R_8;$;

Figure 1.2.: The pipeline stalls at cycles 5 and 6 because B3 is waiting for the results of R_1 and R_2 from bundles B1 and B2, which are completed at stage E3. Stage PF (not shown here) happens just before the ID stage.

1.3 The CompCert formally-verified compiler as of today

1.3.1 Overview of CompCert

Usual compilers (GCC, Clang/LLVM, ICC) split the compilation process into several components. In the case of CompCert, a *frontend* first parses the source code into an *intermediate representation* (IR)—called Cminor—that is independent of the target machine [13]. Then, a *backend* transforms the Cminor program into an assembly program for the target machine [51]. Each of these components introduces several IRs, which are linked by *compilation passes*. A compilation pass can either transform a program from an IR to another (transformation pass) or optimize within an IR (optimization pass). As illustrated in Fig. 1.3, CompCert introduces more IRs than usual compilers. This makes its whole proof more modular and manageable because each compilation pass comes with its own proof of *semantic preservation*.

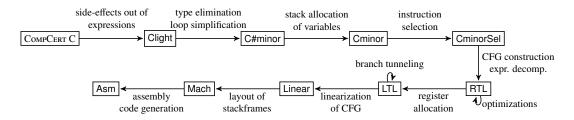


Figure 1.3.: The Intermediate Languages of CompCert

The CompCert compiler [41] executes an external C preprocessor then parses the result. It accepts a large subset of the C99 language [1], ⁶ as well as some C11 extensions.

⁶The main C99 features absent from CompCert C are variable-length arrays and certain forms of unstructured "switch" statements. On most platforms, the setjmp()/longjmp() system is not supported either.

In particular:

- The *backend* starts at the CminorSel level: we have at this level a precise abstract syntax tree of the C program.
- From CminorSel to RTL is the construction of the Control-Flow Graph, using an infinite amount of *pseudo-registers*. Most of the optimizations are done on the RTL level, such as constant propagation, common subexpression elimination, tail call elimination. Compared to more traditional compilers whose control-flow graph is organized in basic blocks, in RTL, each node of the control-flow graph is a single 3-address instruction. RTL will be detailed in chapter 5.
- The *register allocation* pass transforms an RTL program (infinite amount of registers) into an LTL program (finite amount of registers). Another difference between LTL and RTL: each node is a basic-block instead of a single instruction.
- The Linear language is a linearized (laid out) version of the control flow. A certain positioning is chosen for each basic block, then control-flow instructions (conditional or unconditional jumps, labels) are inserted to replicate the control-flow graph. The original CompCert heuristics used by this pass are detailed in chapter 8.
- The Mach language lays out the activation records. Mach is a language close to assembly that abstracts from the ABI (Application Binary Interface) and the ISA (Instruction Set Architecture). It is further detailed in chapter 3.
- The final language Asm models the concrete assembly's semantics, with all the necessary instructions, functionally modelled.

As detailed in Section 1.3.2, the semantics of each IR are specified using a Labeled Transition System (LTS)—a set of transitions between states, with a (possibly empty) execution trace assigned to each transition. While the intermediate languages of the frontend have a very rich state, with various environment variables, the intermediate languages of the backend have increasingly simple states, with the final language Asm featuring a very barebone state mainly containing the state of the registers (including Program Counter (PC) and Return Address (RA)) and the state of the memory.

These semantics (from Clight to the target assembly) are designed as deterministic. ⁷ Indeed, this design choice simplifies the correctness proof of the compiler. It reduces to prove the following: if the source code execution is valid (does not end in an invalid state) and produces an execution trace, then the execution of the compiled assembly code will also be valid and will produce the same execution trace. For instance, for a program containing just arithmetic computations and printf() calls, the execution of the assembly code should produce the same sequence of printf() calls as dictated by the semantics of the source program.

⁷Undefined behaviours [1, §3.4.3] are either defined to lead to an invalid execution or are assigned precise semantics. Unspecified behaviours [1, §3.4.4] are also given precise semantics.

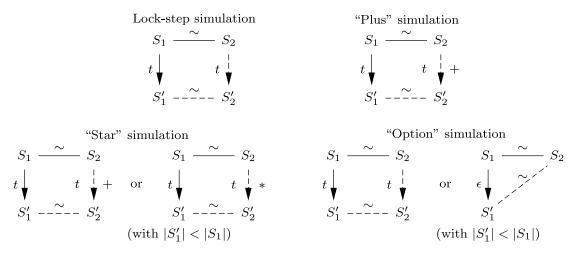


Figure 1.4.: Examples of Simulation Diagrams in CompCert, from Leroy [51]

Within the backend, compilers usually first introduce an unbounded number of *pseudo-registers*, which are then mapped to actual machine registers, with possible spills (saving on the stack, then reloading) when needed. This mapping is performed by the register allocation pass. Compiler backend passes can then be divided into two groups: those happening before register allocation (prepass) and those happening after (postpass).

As of today, the mainstream version of CompCert [26] does not have any reordering optimization, nor does it have any loop optimization such as loop unrolling, loop rotation or loop-invariant code motion. Because of that, CompCert's performance on in-order processors err on the low side compared to GCC, despite the already present optimizations.

1.3.2 CompCert 's framework for proving transformation passes correctness

In CompCert [51], the semantics of a program P consists of predicates for describing initial and final states, as well as a predicate $S \xrightarrow{t} S'$ (usually named step) indicating if *one* execution step can run from state S to state S' by generating a trace t—where t is either a single observable event (e.g. an external call or an access to a volatile variable) or ϵ (absence of observable event). The formal correctness property of CompCert expresses that, given a source program P_1 without undefined behavior (i.e. that can always run step from a non-final state), if the compilation of P_1 produces some assembly program P_2 , then the "observational behaviors" of P_2 are included in those of P_1 , as formalized by Leroy [50, 51]. In order to simplify correctness proofs of its successive passes (Fig. 1.3), CompCert uses an alternative definition for the correctness. One of them is the *forward simulation* applicable on passes between *deterministic* languages.

In its simplest form (*lockstep simulation*), given a relation (\sim) matching states between P_1 and P_2 , a forward simulation involves proving that:

- 1. the initial (resp. final) states of P_1 match those of P_2 ;
- 2. given two matching states, if P_1 steps to a state S'_1 , then P_2 steps to a state S'_2 matching S'_1 .

In the semantic model of CompCert, each external call, access to volatile variable and builtin will produce an *event*. An event is composed of a list of input values (e.g. the arguments to a function call), and a return value if any (e.g. the return value of the function call). A *trace* is then defined as a sequence of events. At last, CompCert classifies program *behaviors* in three categories:

- converges(r, t): the program eventually terminates, with a return code *r* and a finite trace *t*.
- diverges(t): the program never terminates, with a possibly infinite trace t.
- goeswrong(t): the program fails (e.g. division by zero or out-of-bound access), with a finite trace *t*.

Let S and C be respectively the source and compiled programs. The notation $S \Downarrow B$ denotes that B is an observed behavior of the source program S. Let S pec be a set of behaviors that do not go wrong (i.e. without undefined behaviors like invalid memory accesses). The notation $S \models S$ pec means that all the observed behaviors of S are in S pec:

$$S \models S \ pec \ iff \ \forall B, \ S \ \downarrow B \implies B \in S \ pec$$
 (1.1)

CompCert proves a property of semantic preservation: if S verifies a specification S pec, then so does C.

$$S \models S pec \implies C \models S pec$$
 (1.2)

The modular design of CompCert splits the compilation into different Intermediate Representations (IR), and proves the semantics preservation between each of these IR (Fig. 1.3). Actually, when languages at both sides of the pass are deterministic, CompCert proves the semantic preservation from an easier property known as forward simulation: it states that if S has an observable behavior B that does not go wrong, then C will observe the same behavior: [50; 51]

$$\forall B \notin Wrong, S \downarrow B \implies C \downarrow B \tag{1.3}$$

Given semantics of the source and target languages (that is, a mapping from a program to its observable behaviors), the property can be proven using structural induction on the predicate

 $S \downarrow B$. This is still not practical to prove directly, so CompCert uses specific schemes (e.g., lock-step simulation) that each imply the forward simulation.

A semantic of a language *L* in CompCert consists of:

- An inductive type State describing the states of execution of a program in a language L
- A predicate (step $L_1 S_1 t S_1'$) indicating if we can transition from state S_1 to state S_1' by generating a trace t in the language L_1
- A predicate (initial_state *prog S*) indicating if state *S* is an initial state of the program *prog*
- A predicate (final_state *S ret*) indicating if state *S* returning with value *ret* is a final state.

Let us assume we want to write a compilation pass from language L_1 to L_2 , and that we have a (match_state S_1 S_2) predicate indicating if the states S_1 from L_1 and S_2 from L_2 match. Let us also assume the following hypotheses:

- The public symbols are preserved across the transformation (not formalized here)
- The initial states match: $\forall S_1$, initial_state $L_1 S_1 \implies \exists S_2$, initial_state $L_2 S_2 \land$ match_state $S_1 S_2$
- The final states match: $\forall S_1 \ S_2 \ r$, match_state $S_1 \ S_2 \land$ final_state $L_1 \ S_1 \ r \implies$ final_state $L_2 \ S_2 \ r$

Lock-step simulation consists of: "if the source program can take a step, then the transformed program can take a matching step". It is expressed as:

$$\forall S_1 \ t \ S_1' \ S_2$$
, step $L_1 \ S_1 \ t \ S_1' \land \text{match_states} \ S_1 \ S_2$
 $\implies \exists S_2'$, step $L_2 \ S_2 \ t \ S_2' \land \text{match_states} \ S_1' \ S_2'$

Lock-step simulation can be visually represented as a diagram, along with other kinds of simulation that also imply a forward simulation (cf figure 1.4).

The "plus" simulation is like the lock-step one, but one may execute several instructions of the target program for one in the source program, instead of just one.

1.4 Motivations of this thesis and contributions

The motivations of this thesis have then been the following:

- To identify optimizations that would increase performance on in-order processors, and in particular on VLIW processors.
- Implement those optimizations and measure whether they were successful in improving the performance.
- Find efficient ways to formally verify these optimizations.

In this thesis, I focused on the KV3 interlocked VLIW processor from Kalray, though most of its results also extend to other in-order processors including non-VLIW processors such as ARM Cortex A53 and RiscV Rocket (for which our optimizations have been easily ported, with the help of Léo Gourdin).

With the help of David Monniaux and Sylvain Boulmé, I contributed the following:

- A port of CompCert on the KV3 architecture, inspired from the existing RiscV port and the partial port of Barany [5] on the prior KV2 architecture. ⁸
- A modelling of instruction bundles for the KV3 (chapter 3). This work could be adapted for any other interlocked VLIW processor.
- A postpass scheduling optimization: an instruction reordering pass happening after register allocation (see chapter 3). In our case, it happens directly at the assembly IR of Comp-Cert and transforms each basic block into a list of bundles that are then emitted by the assembly printer. The verification is done using a similar symbolic execution technique to that of Tristan and Leroy [95], but in Asm instead of Mach, and with hash-consing. To formally verify this optimization, we also had to define semantics for basic-block execution, reconstructing them at the Mach level and re-adapting the Mach to Asm translation accordingly (chapter 3). When designing this optimization, we kept in mind ease of adaptation to other architectures; Léo Gourdin, Sylvain Boulmé and David Monniaux later ported it to AArch64 with relative ease (a couple of person-months) [89].
- A superblock scheduling optimization: an instruction reordering pass before register allocation, on the scope of superblocks (a kind of extended basic-blocks). This work includes the implementation of a static branch prediction (chapter 8), the definition of new superblock execution semantics in RTL (chapter 5), a minor change of the Linearize oracle for laying out superblocks contiguously in memory (chapter 8), and the verified superblock scheduling transformation itself (chapter 7) with hash-consing.
- A series of more minor optimizations consisting of duplicating instructions to increase optimization opportunities (chapter 8): loop unrolling, tail-duplication, loop peeling and loop rotation. These transformations are all verified a posteriori within a lightweight

⁸Barany's backend generates only one instruction per bundle. He also faced the challenge of representing pairs of 32-bit registers in CompCert for handling 64-bit floating-point values on the KV2. The KV3 natively has 64-bit registers, so that has not been an issue for us.

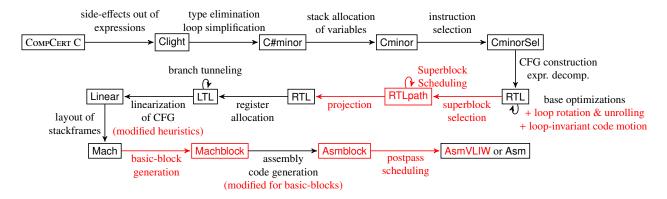


Figure 1.5.: CompCert compilation flow with our added optimizations in red

module described in chapter 6. In particular, when loop peeling is combined with the new CSE3 pass of David Monniaux, we achieve Loop Invariant Code Motion [63].

• An evaluation of CompCert on the Polybench and TACleBench benchmarks, with an evaluation of the performance gain induced by each introduced optimization, and some results obtained for other in-order processors (chapter 10). In addition to the Kalray KV3 core, with the further help of Léo Gourdin, we evaluated CompCert with our optimizations on an ARM Cortex A53 (on a Raspberry Pi 3) and a "Rocket" RiscV core (on FPGA).

I also participated in the following publications:

- Six et al. [88] describes the formally verified postpass basic-block scheduling with bundles semantics, published in OOPSLA'20.
- Monniaux and Six [63] describes a formally verified Loop Invariant Code Motion, using code duplication to hoist instructions outside of the loop (in particular, the loop-invariant instructions are hoisted), then CSE3 to eliminate loop-invariant computations within the loop. This was published in LCTES'21.
- Six et al. [89] describes the formally verified prepass superblock scheduling, submitted for publication.

Figure 1.5 shows the new compilation flow of CompCert with our new optimizations.

Thanks to this work, compared to GCC -O2, and for most of our benchmarks, code compiled with CompCert is now, on average, only 16% slower (instead of 50% slower) on KV3, 12% slower (instead of 38%) for the ARM Cortex A53, and 30% slower (instead of 45%) for the "Rocket" RiscV core.

The full source code of this work is available on https://gricad-gitlab.univ-grenoble-alpes.fr/certicompil/compcert-kvx.

During my thesis, I was an employee of Kalray under CIFRE (Convention Industrielle de Formation par la REcherche) agreement number 2018/0441.

Related Work

2.1 Compiler optimizations for VLIW processors

2.1.1 Instruction scheduling

Scheduling methods (for the *compaction* problem: how to parallelize a sequential micro-code) have been thoroughly studied by Fisher [30], Rau et al. [78], Chang and Hwu [20]. Some of these methods were implemented in the Multiplow compiler [55] for a VLIW architecture. Dupont de Dinechin [25] did a thorough study of adapting the machine scheduling algorithms from the litterature to VLIW processors.

Instruction scheduling for micro-code is a particular instance of scheduling with timing and resource constraints, which is a classical problem [62, §5.4].

In its simplest form, instruction scheduling is done in basic blocks; however, scheduling on super blocks (sequences of basic blocks where each basic block has a single predecessor, except the first) yields better results due to the bigger scheduling scope. The scheduling can be acyclic or cyclic if the scope is a whole inner loop. Lastly, it may run before (prepass scheduling) or after (postpass scheduling) register allocation.

If the scheduling happens before register allocation, then extra care must be given to not increase register pressure too much — that is, the register allocation should not generate more register spills as a result of the prior scheduling. On the other hand, if the scheduling happens after register allocation, the reuse of registers introduced by the register allocation may hamper the scheduling (*false dependencies*).

Ideally, having the register allocation and instruction scheduling in a single pass would solve this issue; however doing so is challenging, though there are existing work like Motwani et al. [65], or more recently Lozano et al. [57]. Instead, the approach usually taken by compilers is to have two separate scheduling passes: one before register allocation, and another after register allocation.

Pouzet [77] considered the scheduling of functional programs on VLIW architectures, including forms of software pipelining (for tail-recursive programs), with equivalence defined as term

equivalence, possibly up to rewriting. The work is similar to our scheduling transformations, however Pouzet did not investigate formal proofs of the transformation.

Schulte et al. apply constraint programming to instruction selection, register allocation, code motion and other optimizations [14; 58]. Their process can even be optimal (w.r.t. their cost model) on medium-sized functions. They consider a wider class of optimizations than we do, but they do not provide any machine-verified proof of correctness. The primary goal of their approach is to identify weak points in production compilers. The machine code programs generated by their experimental compiler based on constraint solving and the production compiler are compared; if the production compiler is clearly sub-optimal, compiler designers investigate and devise an optimization pattern that may eventually be integrated into the production compiler.

Though ample work exists on scheduling optimizations, none of what was mentioned above are used in the context of a formally verified compiler such as CompCert. Some of these transformations, although promising, might require significant work to prove. In CompCert, our choice of scheduling algorithm was then partly driven by proof constraints: we wanted to implement scheduling techniques that both were likely to give good results, but also who were affordable to verify given the time we had. We settled for a basic block scheduling in postpass, and a superblock scheduling in prepass.

2.1.2 Loop transformations

Most programs spend most of their time on a small part of the code; that code is usually made of loops. In particular, innermost loops can be decisive in terms of performance: small improvements of even one cycle can, in some cases, result in an unexpected overall performance improvement. [24] The first loop transformations were investigated early on with the introduction of dependence graphs [46]. Today, many classical loop transformations exist to improve program performance [74, §2.4.1]. More recently, the Polyhedral model was introduced to formalize the problem of finding the right sequence of loop transformations to apply to get optimal performance [99].

In this thesis, we experimented with simple classical loop transformations: loop unrolling, loop rotation and loop-invariant code motion.

Loop unrolling

Davidson and Jinturkar [24] did a thorough study of loop unrolling, including a classification of loops worthy to unroll, and how to determine how many times should a given loop be unrolled. As in our approach, loop unrolling is done at the backend level to not be reliant on loop counting

information. Our version is more minimalistic: we unroll one time any innermost loop whose instruction count is below a given threshold.

Loop rotation

We implemented in this thesis loop rotation, a method to push the conditional branch at the end of the loop instead of the start to induce a better postpass scheduling. This transformation is mentionned in Platzer [74, §2.5.3], though in this thesis we perform this transformation independently of loop-invariant code motion, and it is not required for loop-invariant code motion neither. Also, another difference is that our loop rotation is performed in RTL, an intermediate representation close to machine code. In particular, information such as loop counters (or the type of loop) is lost at that level.

Such work is probably subsumed by cyclic scheduling transformations such as rotation scheduling [21] or software pipelining [47]; but none of these methods are formally verified. Even though our approach is more limited, it has the advantage of requiring only minimal proof.

Loop-Invariant Code Motion

Traditionally, Loop-Invariant Code Motion is performed by identifying expressions whose value do not vary along successive iterations, then hoisting them before the identified loop [74].

Here, we followed a more modular approach to ease the proofs: first, we hoist an entire iteration of the loop (loop peeling), then the new common subexpression elimination pass of D. Monniaux [63] naturally removes in the loop body what was initially computed before.

2.1.3 Other optimizations

Static branch prediction

For some transformations such as superblock scheduling (or, more generally, trace scheduling), the compiler must have some knowledge of which part of the code will be executed the most [20]. Inserting profiling information and running the code on a "training" dataset (a dataset whose execution is representative of the dataset to run) is one way to get such information.

However, training datasets are not always available – also, their execution might not cover 100% of the code, leaving no choice to the compiler but to make guesses for the rest.

Ball and Larus [4] studied static branch prediction algorithms to have the compiler make fair guesses under the absence of such information. We inspired ourselves of this work to provide CompCert with static branch prediction.

Code positioning

Code positioning consists in laying out the code in memory in such a way that improves performance, typically by minimizing the penalty of branching. When having access to profile information, this problem was tackled by Pettis and Hansen [72]. One advantage here compared to scheduling transformations is that CompCert already has a verifier for code positioning; the heuristics giving the positioning can then be modified without changing the proof. However, their work requires to have exact branch profiling information.

We do not always have access to exact branch profiling information, so we did not use this work for positioning our superblocks; instead, we adapted the existing CompCert heuristics with a small modification.

2.2 Formally proven compiler transformations

2.2.1 Advanced compiler optimizations in CompCert

Translation validation, first introduced by Pnueli et al. [75], consists in feeding both the translated code and the original code through a verifier, which will check for semantic discrepancies between the two versions.

This verifier may use various techniques: from static analyzes (e.g. [81; 92]) to generation of verification conditions in SMT-solvers (e.g. [104; 28]). While SMT-solving has been successful to formally prove the correctness of the compilation of the SeL4 operating system [86; 85], this technique seems too much compute-intensive for being included in a general purpose compiler. Moreover, [67] and [94] established that *symbolic execution* combined with *rewriting* is effective enough in *validating* the code produced by state-of-the-art compilers applying various optimizations.

In particular, using translation validation to certify instruction scheduling was previously explored by Tristan and Leroy [96]. They extended CompCert with a certified postpass list-scheduler, split into

- 1. an untrusted oracle written in OCAML that computes a scheduling for each basic block¹ in order to minimize pipeline stalls
- 2. a checker—certified in Coo—that verifies the oracle results.

Compared to our postpass scheduler, their scheduling operates at the Mach level, simpler than Asm. Since some aspects (stack and control flow handling) are only detailed in the Mach to Asm pass, a model of latencies and pipeline use at the Mach level can only be less accurate. Furthermore, our postpass scheduling needed access to the concrete Asm instructions to construct well-formed bundles.

Also, their checker has exponential complexity w.r.t. the size of basic blocks, making it slow or even impractical as the number of instructions within a basic block grows [95, §7][93, §6.7.1]. This is problematic since certain programs, such as unrolled computational loops or some forms of cryptography, may have up to a thousand instructions within a block. We thus needed to devise new algorithms that scale much better but that can still be proved correct in Coq.

Compared to our superblock scheduling, trace scheduling (as introduced by Fisher [31]) is more general since code may be moved below or above side-entrances on a given trace. Moving code below a side-exit requires duplicating instructions (also called *bookkeeping*); this is very similar to the tail-duplication used in superblock scheduling. Moving code above a side-entrance, however, requires more complex bookkeeping. The trace scheduling of Tristan and Leroy [96] was implemented at the Mach level, as an extension to their prior list scheduling. Aside of the exponential blow-up, there are two further differences between our approach and theirs:

- Our approach is more modular. We dissociate tail-duplication (bookkeeping) from superblock scheduling. We can then apply optimizations such as common subexpression elimination or constant propagation between the bookkeeping and the scheduling.
- In the trace scheduling of Tristan and Leroy [96], the instructions are systematically duplicated when moving above a side-exit. On our end however, we are able to move instructions above side-exits without duplication under sufficient conditions expressed through a liveness analysis.

Tristan and Leroy [97] uses a mapping from RTL original nodes to transformed nodes to prove Lazy Code motion; we use a similar concept for the Duplicate verifier in chapter 6, and for the superblock scheduling verifier of chapter 7.

Lazy Code Motion subsumes Loop-Invariant Code Motion; the software pipelining Tristan and Leroy [98] probably subsumes loop rotation as well. One should note however that none of the above-cited work was integrated into CompCert due to excessive compilation times. Also, their work was implemented on a CompCert from 10 years ago: it is hard to say the effort that would

¹A basic block is defined as a sequence of instructions with a single entry point (possibly named by a label in front of the sequence) and a single exit point (e.g. a control-flow instruction at the end of the sequence).

involve a re-adaptation of their work today. Finally, their lack of evaluation of generated code efficiency or description of the underlying oracles makes it hard to compare their work to ours in terms of optimization gain.

In comparison, our approach has been more pragmatic: the goal of this thesis was to improve performance as much as possible, with minimal proof effort.

Inspired by their work, Barthe et al. [6] did the ambitious task of integrating a formally verified SSA-based middle-end within CompCert, using translation validation. This entails giving precise semantics to SSA, transforming from RTL to SSA, implementing Global Value Numbering (GVN) and sparse conditional constant propagation (SCCP) within SSA, then transforming SSA back into RTL. The proof effort is significant: approximately 15000 lines of Coq code. The CSE3 optimization of Monniaux and Six [63] achieves a similar gain in the generated code efficiency compared to SSA-GVN, but in a much lighter approach.

2.2.2 Other related work

Besides CompCert, there are other projects that generate low-level code in a formally verified fashion.

The CakeML system is very similar to CompCert, except that its source language is functional (a variant of ML) instead of imperative [91]. It features the same ideas as CompCert: splitting the translation into many smaller transformations, with 12 intermediate languages and some optimizations. Their formally verified backend can generate ARM, x86, or RISC-V code. To the best of our knowledge, it does not feature any scheduling optimization.

Pit-Claudel et al. [73] recently introduced a novel approach to rely on using the Coq extractor to generate assembly code instead of a compiler that is proven once and for all. High-level specifications are written in Gallina, then refined into non-deterministic functional programs in a Gallina DSL. These programs are then soundly extracted to an imperative intermediate language (Facade) with a new proof-generating extraction. The generated programs are then translated to Bedrock assembly [22] by a more traditional verified compiler approach. This comes with the drawback of having longer compilation times. However, compared to certified compilers, their approach is lighter, more easily extensible, and easier to prove.

Some other work on verifying compiler transformations include Vellvm, an ambitious project to formally verify the transformations done in the LLVM compiler [103] [102]. To the best of our knowledge, they did not formalize yet any of the optimizations introduced in this thesis.

Part II

Formally Verified Optimizations

Formal Verification of Basic-Block Scheduling at Asm level

Reordering instructions (which can include bundling in the case of VLIW architectures) was our first step in our quest to improve performance for the in-order VLIW KV3 processor. Indeed, CompCert does not attempt to reorder operations, which are issued in almost the same order as written in the source code. This may not be so important on processors with out-of-order or speculative execution (e.g., x86) since such hardware may dynamically find an efficient ordering on its own. Yet, it hinders performance on in-order processors, especially superscalar ones (multiple execution units can execute several instructions at once, in parallel).

The task of reordering instructions to minimize latencies is traditionally done by two different scheduling passes, one before register allocation (prepass) and one after (postpass). For VLIW architectures, traditionally, the postpass scheduling is also in charge of generating the bundles of instructions: two instructions are in the same bundle if they are scheduled in the same time slot.

Previous work by Tristan and Leroy [95] studied *a posteriori* verification of basic-block and trace scheduling at the Mach level. However, the Mach level is not a good fit for us: modeling bundles at the Mach level would have been challenging and imprecise. Indeed, the Asm generation pass can expand a Mach instruction in several Asm instructions. Instead, expressing our postpass scheduling at the Asm level allows us to have more precise latency and resource constraints information. In terms of scope, we chose to implement basic-block scheduling: it is much simpler than trace scheduling and is enough to get a substantial performance increase.

Implementing a formally verified basic-block scheduler in CompCert presents us with several challenges:

• *How to represent bundles in* CompCert? The existing Asm languages are all sequential. The key challenge for modeling bundle execution lies in defining semantics: on the concrete processor, each instruction within a bundle is executed in parallel! More precisely, the register reads are performed first, and then the register writes are done. Thus, it is

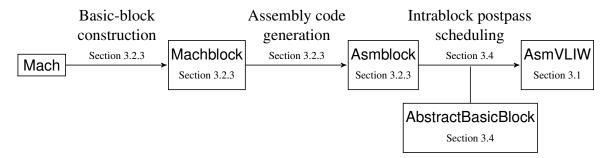


Figure 3.1.: Architecture of our postpass scheduling

possible to write and read from the same register in the same bundle. However, writing twice in the same register is not deterministic and should be avoided.

- How to formally verify a postpass scheduling in CompCert? For a VLIW architecture, the postpass scheduling performs two tasks: reordering the instructions according to a given schedule and packing the instructions of the same timeslot into the same bundle. The compiler must ensure that the transformations of the initial sequential code into a given sequence of bundles are correct and that each bundle does not exceed the available resources on the target processor. In CompCert, we do not need to verify formally that the bundles obey the resource constraints limits: if we emit bundles impossible to encode, the assembler will return an error. However, we still need to ensure formally that the generated sequence of bundles simulates the initial sequential basic block.
- How to recover the basic-block structure in Asm? We want our optimization to transform each basic block into a sequence of bundles: this raises the issue of modeling basic-block execution semantics (instead of instruction-per-instruction execution semantics).

To tackle these challenges, we adopted the code architecture figure 3.1. First, we created a new IR called Machblock, whose sole purpose is to recover the basic-block structure. Indeed, we found it easier to do that task at the Mach level, which features semantics easier to work with than Asm. The IR, as well as the transformation pass to recover this basic-block structure, is described in section 3.2.3.

We then introduce Asmblock: an Asm IR with basic-block execution semantics. Once the basic blocks are recovered in Machblock, each instruction inside is translated to an Asm instruction. The Machblock to Asmblock transformation is inspired by the existing Mach to Asm, but adapted to basic-block execution semantics — this is described in section 3.3.

Finally, our postpass scheduler (described section 3.4) takes each basic block from Asmblock and transforms them into sequences of bundles from the IR AsmVLIW, that I describe in section 3.1.

The AsmVLIW language is our final representation. It formalizes the assembly semantics of our VLIW target: the bundles are defined as basic blocks with a parallel execution inside.

Our postpass scheduler is formalized as a transformation on basic blocks. It takes as input our Asmblock IR, which shares its syntax with AsmVLIW, but with sequential execution inside basic blocks instead of a parallel one.

Our postpass scheduler from Asmblock to AsmVLIW takes each block from Asmblock, performs intra-block scheduling via an external untrusted oracle, and uses a certified, that is, formally verified checker to verify the generated AsmVLIW bundles.

The core of our scheduling checker—involving symbolic evaluation of basic blocks with hash-consing—operates on a new auxiliary IR, called AbstractBasicBlock.

Our certified scheduler is made of:

- An oracle, written in OCAML, producing a sequence of bundles for each basic block. We implemented a greedy list-scheduler with a priority heuristic based on latencies. More details on its implementation can be found in chapter 9.
- A generic certified scheduling checker, written in Coo, with a proof of semantic preservation, implementing two independent checks:
 - Verifying that, assuming sequential execution within each bundle, the reordered basic block preserves the sequential semantics of the original one. This is achieved by comparing the symbolic execution of two basic blocks, as did Tristan and Leroy [96]. The exponential complexity of their approach is avoided by introducing (verified) hash-consing.
 - 2. Verifying that, for each bundle, the sequential and parallel executions have the same semantics. This reduces to checking that each bundle never uses a register after writing to it.

Both the oracle and checker are *generic*; we instantiated them with the instruction set and (micro-)architecture of the Kalray KVX core.

These checks are performed on a new IR, called AbstractBasicBlock, which makes them easier to implement and prove, and which is moreover generic w.r.t the instruction set. The core of our certified scheduler is independent of the instruction set: it has been reused for the AArch64 architecture [89], though this is not detailed here.

3.1 AsmVLIW: semantics for a VLIW assembly language

The Asm language of our target processor introduces syntax and semantics for *bundles* of instructions. Bundles can be seen as a special case of *basic blocks*: zero or more labels giving (equivalent) names to the *entry-point* of the block; followed by zero or more *basic instructions* – i.e. instructions that do not branch, such as arithmetic instructions or load/store; and ended with at most one *control-flow instruction*, such as conditional branching to a label.

Semantically, basic blocks have a single entry-point and a single exit-point: branching from/to the middle of a basic block is impossible. Thus, it is possible to define semantics that step through each block atomically, sequentially executing the program block by block. We call such semantics *blockstep semantics*. The notion of basic blocks is interesting for scheduling optimizations: reordering the sequence of *basic instructions* in a basic block without changing its (local) blockstep does not change the (global) semantics of the surrounding program.

We provide two such blockstep semantics, which only differ on how they combine instructions within basic blocks: an IR with sequential semantics called Asmblock, and one with parallel semantics called AsmVLIW. Our backend first builds an Asmblock program from a Mach program by detecting syntactically its basic block structure (Section 3.2). Then, each basic block is split into bundles of the AsmVLIW IR (Section 3.4). Below, Section 3.1.1 gives an overview of the Asm IR of CompCert. Then Section 3.1.2 defines the syntax shared between AsmVLIW and Asmblock. Finally, Section 3.1.3 defines AsmVLIW, and Section 3.1.4 defines Asmblock.

3.1.1 Overview of COMPCERT'S ASM IR

CompCert defines one Asm language per target processor. An Asm program consists of functions, each with a function body. Asm states are of a single kind "State(rs, m)" where rs is the register state (a mapping from register names to values), and m is the memory state (a mapping from addresses to values). An initial state is one where the PC register points to the first instruction of the main function, and the memory is initialized with the program code. The instructions of Asm are those of the target processor, each with its associated semantics that specifies how the instruction modifies the registers and the memory.

In each CompCert backend the instruction semantics are modeled by an exec_instr function which takes as argument an instruction i, a register state rs and a memory state m, and returns the next state (rs', m') given by the execution of i; or the special state Stuck if the execution failed.

Here are some instructions that can be modeled in Asm:

- Pcall(s): calls the function from symbol s (saves PC into RA and then sets PC to the address of s);
- Paddw(rd, r1, r2): writes in rd the result of the addition of the lower 32-bits of r1 and r2:
- Pcb(bt, r, l): evaluates the test bt on register r—if it evaluates to true, PC jumps to the label l;
- Pigoto(r): PC jumps to the value of the register r.

Most of the instructions modelled in Asm directly correspond to the actual instructions of the processor. However, there can also be a few pseudo-instructions like Pallocframe or builtins, which are specified in Asm, then replaced by a sequence of instructions in a non-certified part of CompCert. Due to distinctions in immediate vs register operand, word vs doubleword operand size etc., there are as many as 193 instructions to be modelled in the KVX processor.

3.1.2 Syntax of Bundles & Basic Blocks

We first split the instructions into two main inductive types: basic for basic instructions and control for control flow ones. Then, a basic block (or a bundle) is syntactically defined as a record of type bblock with three fields: a list of labels, a list of basic instructions, and an optional control flow one.

In our AsmVLIW and Asmblock semantics, on a None exit, the PC is incremented by the number of instructions in the block. This convention makes reasoning easier when splitting a basic block into a sequence of smaller ones. To avoid infinite stuttering (due to incrementing PC by 0), we further require that a block should contain at least one instruction.

Sections 3.1.3 and 3.1.4 define, respectively, the parallel and the sequential blockstep semantics of this syntax. A state in AsmVLIW and Asmblock is expressed the same way as in Asm: it is either a pair (rs, m) where rs (register state) maps registers to values and m (memory) maps addresses to values, or a Stuck in case of failure (e.g. division by zero). Hence, executing a single instruction in our semantics gives an outcome defined as either a (Next rs m) state or a Stuck execution. Then, each blockstep takes as input an initial state (rs, m), fetches the block pointed by rs[PC] (the value of PC in rs), and executes the content of that block. Finally, that blockstep either returns the next state or propagates any encountered failure.

3.1.3 Parallel Semantics of AsmVLIW

A bundle is a group of instructions that are to be *issued* in the same cycle through the pipeline. The pipeline stages of our interlocked VLIW processor can be abstracted into:

- Reading Stage: the contents of the registers are fetched.
- **Computing Stages**: the output values are computed, which can take several cycles. Once an output is computed, it is *available* to other bundles waiting at the reading stage.
- Writing Stage: the results are written to the registers.¹

Our processor stalls at a reading stage whenever the result is not yet available. The exact number of cycles required to compute a value thus only impacts the performance: our formal semantics abstracts away the computing stages and only considers the reading and writing stages.

Reads are always deterministic: they happen at the start of the execution of our bundle. However, the order of writes is not necessarily deterministic, e.g. if the same register is written twice within the same bundle. We first introduce deterministic semantics where the writes are performed in the order in which they appear in the bundle. For instance, the bundle " $R_0 := 1$; $R_0 := 2$ " assigns 2 to R_0 , in our in-order semantics. The actual non-deterministic semantics is then defined by allowing the execution to apply an arbitrary permutation on the bundle before applying the in-order semantics.

In-Order Parallel Semantics

We model the reading stage by introducing an internal state containing a copy of the initial state (prior to executing the bundle). Such an internal state is thus of the form (rsr, rsw, mr, mw) where (rsr, mr) is the copy of the initial state, and (rsw, mw) is the running state where the values are written. Fig. 3.2 schematizes the semantics.

- The function (bstep *b rsr rsw mr mw*) executes the basic instruction *b*, fetching the values from *rsr* and *mr*, and performing the writes on *rsw* and *mw* to give an outcome.
- The function (estep *f ext sz rsr rsw mw*) does the same with the optional control flow instruction *ext*: if there is no instruction, then it just increments PC by *sz*, the size of the block; here, *f* is the current function—in which branching instructions look for labels, like in other Asm semantics.
- The function (parexec_wio ... rsr mr) is the composition of the basic and control steps.

For example, the bundle " $R_0 := R_1$; $R_1 := R_0$; jump@toto" runs over an initial register state $rsw_0 = rsr$ in 3 steps:

¹This includes the Program Counter register, which is updated at the end of each bundle execution.

$$\begin{pmatrix} rsr \\ mr \end{pmatrix} \Longrightarrow \begin{pmatrix} rsr, rsw_0 \\ mr, mw_0 \end{pmatrix} \xrightarrow{\text{bstep } b_1} \cdots \xrightarrow{\text{bstep } b_n} \begin{pmatrix} rsr, rsw_n \\ mr, mw_n \end{pmatrix} \xrightarrow{\text{estep } f \text{ ext } sz} \begin{pmatrix} rsw_{n+1} \\ mw_{n+1} \end{pmatrix}$$

$$\text{parexec_wio } f [b_1; b_2; \cdots; b_n] \text{ ext } sz$$

Figure 3.2.: Parallel In-Order Blockstep

```
1. "R_0 := R_1" leads to rsw_1 = rsw_0[R_0 \leftarrow rsr[R_1]]
```

2. "
$$R_1 := R_0$$
" leads to $rsw_2 = rsw_1[R_1 \leftarrow rsr[R_0]]$

3. "jump @toto" leads to
$$rsw_3 = rsw_2[PC \leftarrow @toto]$$

The final register state of the parallel in-order blockstep is

$$rsw_3 = rsr[R_0 \leftarrow rsr[R_1]; R_1 \leftarrow rsr[R_0]; PC \leftarrow @toto]$$

As expected, this bundle swaps the contents of R_0 and R_1 .

The in-order parallel execution of a list of basic instructions is formally defined in CoQ by the following function, where "NEXT $rs, m \leftarrow e_1$ IN e_2 " is a notation for:

```
"match e_1 with Next rs m \Rightarrow e_2 \mid \_ \Rightarrow Stuck end"
```

```
Fixpoint parexec_wio_body bdy rsr rsw mr mw : outcome :=

match bdy with nil \Rightarrow Next rsw mw

| bi::bdy' \Rightarrow NEXT rsw', mw' \Leftarrow bstep bi rsr rsw mr mw IN parexec_wio_body bdy' rsr rsw' mr mw'

end
```

The in-order parallel execution of a block (defined below) first performs a parallel in-order execution on the body (the list of basic instructions), and then performs a parallel execution with the optional control flow instruction. Here, f is the current function and sz is the offset by which PC is incremented in the absence of a control-flow instruction.

```
Definition parexec_wio f bdy ext sz rs m :=
NEXT rsw', mw' ← parexec_wio_body bdy rs rs m m IN estep f ext sz rs rsw' mw'
```

Deterministic Out-of-Order Parallel Semantics

The in-order parallel semantics defined above is not very representative of how a VLIW processor works, since concurrent writes may happen in any order. This issue is solved by relation (parexec_bblock f b rs m o), which holds if there exists a permutation of instructions such that the in-order parallel execution of block b with initial state (rs, m) gives the outcome o.

```
Definition parexec_bblock f b rs m o: Prop :=

| B bdy1 bdy2, Sorting.Permutation (bdy1++bdy2) b.(body)
```

Formally, the execution takes any permutation of the body and splits this permutation into two parts bdy1 and bdy2. It first executes bdy1, then the control flow instruction, then bdy2. While PC is possibly written before the end of the execution of the bundle, the effect on the control flow takes place when the next bundle is fetched, reflecting the behaviour detailed in Footnote 1.

This semantics gives a fair abstraction of the actual VLIW processor. However, the proof of semantic preservation of CompCert requires the target language to be deterministic. Consequently, we force our backend to emit bundles that have the same semantics irrespectively of the order of writes. This is formalized by the relation below:

```
Definition det_parexec f b rs m rs' m': Prop := \forall o, parexec_bblock f b rs m o \rightarrow o = Next rs' m
```

Given (rs', m'), the above holds only if all possible outcomes o satisfying (parexec_bblock f $b \, rs \, m \, o$) are exactly (Next $rs' \, m'$); that is, it only holds if (rs', m') is the only possible outcome. We then use the det_parexec relation to express the step of our AsmVLIW semantics: if det_parexec does not hold then it is not possible to construct a step.

3.1.4 Sequential Semantics in Asmblock

Asmblock is the IR just before AsmVLIW: instructions are grouped in basic blocks. These are not reordered and split into bundles yet: execution within a block is sequential.

The given sequential semantics of a basic block, called exec_bblock below, is similar to the semantics of a single instruction in other Asm representations of CompCert. Just like AsmVLIW, its execution first runs the body and then runs the control-flow instruction. Moreover, our sequential semantics of single instructions reuses bstep and estep by using the same state for reads and writes. Our semantics of single instructions is thus shared between the sequential Asmblock and the parallel AsmVLIW.

```
Fixpoint exec_body bdy rs m: outcome :=

match body with nil ⇒ Next rs m

| bi::bdy' ⇒ NEXT rs', m' ← bstep bi rs rs m m IN exec_body bdy' rs' m'

end

Definition exec_bblock f b rs m: outcome :=

NEXT rs', m' ← exec_body b.(body) rs m IN estep f b.(exit) (Ptrofs.repr (size b)) rs' rs' m'
```

3.2 Retrieving the basic block structure with Machblock

The preliminary stage of our backend constructs the Asmblock program from the Mach program. The basic block structure cannot be recovered from the usual Asm languages of CompCert. Thus, we recover it from Mach, through a new IR—called Machblock—whose syntax reflects the basic block structure of Mach programs, and then translates each basic block from Machblock to obtain an Asmblock program.

In this section, I motivate and present our solution to reconstruct basic blocks in CompCert, necessary for the later scheduling pass.

3.2.1 The Mach IR of COMPCERT

The Mach IR consists of a set of functions, each with a function body. Roughly speaking, Mach is a simplified assembly language (with 3-address code instructions handling the actual registers of the target processor, except for some special registers like the program counter PC) where:

- The ABI (Application Binary Interface) is abstracted into Mach instructions allowing access to the stack and function parameters Mgetstack, Msetstack and Mgetparam.
- Loads and stores stay generic and are not yet expanded into the "real" load/store instructions. The same applies to branching instructions.
- Calling instructions Mcall and Mtailcall can only branch either on a function symbol or a register on an address that must be the first address of a function.
- Branching instructions such as Mgoto branch to labels in the current function (like in LLVM).
- There is neither a PC (Program Counter) nor a RA (Return Address) register. The remaining code to be executed is an explicit part of the current state.

Mach states describe the register state rs, the global memory state m, and the stack state st. They are of three kinds, with the following meanings:

- (State st f c rs m): the first instruction of code c is about to be run in current function f;
- (Callstate st f rs m): function f is about to be run, the caller context has just been pushed on stack st;
- (Returnstate st rs m): a caller context is about to be restored from stack st.

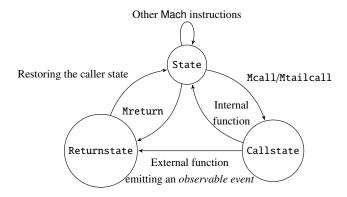


Figure 3.3.: Execution Steps between Mach States

The states of a Mach program are either of:

- State(stack, f, sp, c, rs, m): we are in the current function f, with a callstack stack, a stack pointer sp, a Mach register ² state rs, and a memory state m. The remaining code of f to execute is c.
- Callstate(stack, f, rs, m): like State, but this time we are about to call f. A transition between State and Callstate is typically done by a Mcall or Mtailcall instruction. From there, if it's an internal function, we go back to a State inside the designed function if it's an external function, we go directly to Returnstate and generate a trace (external event).
- Returnstate(stack, rs, m): the execution of the function is over, we have now to return to the latest function in the callstack stack. A transition from a State to a Returnstate is typically done by a Mreturn.

The instructions of the Mach IR are 3-address code, providing basic interactions between the register state, memory, the function arguments, and the actual stack where temporary variables can be stored.

- Mgetstack/Msetstack/Mgetparam: moves between stack/function parameters and registers
- Mop: arithmetic operations
- Mload/Mstore: moves between memory and registers
- Mlabel: pseudo instruction signaling a label, used by Mcond and Mgoto
- Mgoto/Mcond: respectively inconditional and conditional branching
- Mcall/Mtailcall/Mreturn: calling and returning. Tailcalls are distinguished from normal calls as a small optimization.
- Mbuiltin: builtin instruction, whose execution generate an external event

²a Mach register basically corresponds to a general purpose register of the target assembly

3.2.2 Necessity of Constructing Basic Blocks at the Mach Level

One major difference between Mach and Asm lies in their semantics: the "next" Mach instructions to be executed are directly in a Mach state (as a list of instructions), whereas the Asm instructions are stored in memory, accessed by the PC register. In such Asm semantics, the PC register can jump anywhere within the function body, not necessarily to a label.³ On the contrary, the Mach semantics ensures that jumps can only branch to particular points (labels, function entry points and return addresses). This property is not carried within the Asm IR. Unfortunately, this makes reconstructing basic blocks from Asm (in a hypothetical Asm to Asmblock pass) impossible: our AsmVLIW semantics requires that PC never jump inside a basic block.

Moreover, proving that a block-step semantics simulates an instruction-step semantics is not trivial. Hence, it seems interesting to capitalize this effort for a generic component w.r.t the processor.

Our solution is to construct the basic blocks earlier, at the Mach level, by introducing a new Machblock IR and an architecture-independent Mach to Machblock translation, and then adapting the former Mach to Asm pass to a new Machblock to Asmblock pass. Not only does introducing Machblock allows separating the proof of the basic block reconstruction from the proof of the Mach to Asm translation, but it also makes part of the process reusable for other backends.

3.2.3 Machblock: generating basic blocks from Mach

The basic blocks syntax in Machblock is similar to that of Asmblock, except that instructions are Mach instructions and that empty basic blocks are allowed (but not generated by our translation from Mach). We have only defined sequential semantics for Machblock, which is Mach one, except that a whole basic block is run in one step. This block-step is internally made up of several computation steps, one by basic or control-flow instruction.

```
Record bblock := { header: list label; body: list basic_inst; exit: option control_flow_inst }
```

The code of our translation from Mach to Machblock is straightforward: it groups successive Mach instructions into a sequence of "as-big-as-possible" basic blocks while preserving the initial order of instructions. Indeed, each Mach instruction corresponds syntactically to either a label, a basic instruction, or a control-flow instruction of Machblock.

Proving that this straightforward translation is a forward simulation is much less simple than naively expected. Our proof is based on a special case of "Option" simulation (Fig. 3.5).

³See the igoto instruction in Section 3.1.1.

Intuitively, the Machblock execution stutters until the Mach execution reaches the last execution of the current block, then while the Mach execution runs the last step of the current block, the Machblock execution runs the whole block in one step. Hence, the measure over Mach states—that indicates the number of Machblock successive stuttering steps—is simply the size of the block (including the number of labels) minus 1. Formally, we have introduced a dedicated simulation scheme, called "Block" simulation in order to simplify this simulation proof. This specialized scheme avoids defining the simulation relation—written " \sim " in Fig. 3.5—relating Mach and Machblock states in the stuttering case. In other words, our scheme only requires relating of Mach and Machblock states at the beginning of a block. Indeed, the "Block" simulation scheme of a Mach program P_1 by a Machblock program P_2 is defined by the two conditions below (where S_1 and S_1' are states of P_1 ; S_2 and S_2' are states of P_2 ; and t is a trace):

1. stuttering case of P_2 for one step of P_1 :

$$|S_1| > 0 \ \land \ S_1 \xrightarrow{t} S_1' \implies t = \epsilon \ \land \ |S_1| = |S_1'| + 1$$

2. one step of P_2 for $|S_1|+1$ steps of P_1 :

$$S_1 \sim S_2 \wedge S_1 \xrightarrow{t} S_1^{t+1} S_1' \implies \exists S_2', S_2 \xrightarrow{t} S_2' \wedge S_1' \sim S_2'$$

Naively, relation $S_1 \sim S_2$ would be defined as " $S_2 = \text{trans_state}(S_1)$ " where trans_state translates the Mach state in S_1 into a Machblock state, only by translating the Mach codes of S_1 into Machblock codes. However, this simple relation is not preserved by goto instructions on labels. Indeed, in Mach semantics, a goto branches to the instruction *following* the label. On the contrary, in Machblock semantics, a goto branches to the block *containing* the label. Hence, we define $S_1 \sim S_2$ as the following relation: "either $S_2 = \text{trans_state}(S_1)$, or the next Machblock step from S_2 reaches the same Machblock state as the next step from trans_state(S_1)". The condition (2) of the "Block" simulation is then proved according to the decomposition of Figure 3.4.

3.3 Asmblock: adapting the Mach to Asm translation for basic blocks

The Machblock to Asmblock pass is adapted from the Mach to Asm pass of other backends (see Section 3.3.1), but with a consequential change: instead of manipulating instructions (and reasoning on the execution of single instructions), we are now manipulating basic blocks of instructions, and must reason on the execution of an entire basic block (in one single step). I give

On the right-hand side, c and b::bl are, respectively, the initial Mach and Machblock codes where b is the basic block at the head of the Machblock code. Relation match state is the Coo name of the simulation relation (also noted "~" in the paper). The Machblock step from b::bl simulates the following |b| Mach steps from c. First, skip all labels: this leads to Mach code c0. Second, run all basic instructions: this leads to Mach code c1. Finally, run the optional control-flow: this leads to code c2. Each of these three subdiagrams is an independent lemma of our Coo proof.

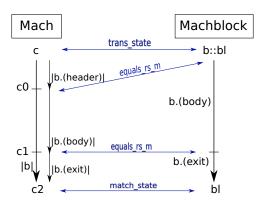


Figure 3.4.: Overview of our Proof for Condition (2) of the "Block" Simulation of Mach by Machblock

here details to hint the reader on the differences between the two approaches, particularly for the star simulation proof.

Translating and proving Mach code to Asm 3.3.1

The major difference between Mach and Asm lies in the execution semantics. In Mach, the remaining code to be executed is directly in the state, and Mach semantics provide a clean notion of internal function call: execution can only enter into an internal function by its syntactic entry-point. In Asm, the code to be executed resides in memory and is pointed to by the PC register. Through jumps into registers and a bit of pointer arithmetic, an Asm program can jump into the middle of a function, like in Return-Oriented-Programming (ROP) [19]. Thus, proving the code generation pass from Mach to Asm implies ensuring that the generated code does not have such a behaviour (assuming that the Mach program does not have any undefined behaviour): it simulates Mach execution where such behaviour does not exist. 4

Formally, it involves introducing a suitable "~" relation matching Mach states with Asm states. The gist of it consists of expressing a correspondence between the register states as well as the memory, in addition to the following properties depending on the Mach state: if it is a State, then the PC register points to the Asm code generated from Mach; if it is a Callstate, then the PC should point to the callee function, and the RA register to the return address (i.e. the address following the call instruction in the caller); otherwise, it is a Returnstate and the PC should point to the return address.

⁴Thus, ROP attacks on code generated by CompCert are only possible from undefined behaviours of the source code.

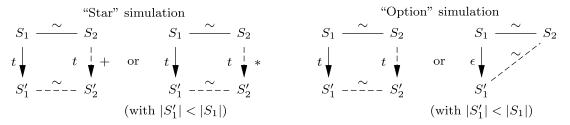


Figure 3.5.: Simulation Diagrams with Stuttering in COMPCERT

Then, the proof involves a "Star" simulation. Such a simulation of a program P_1 by a program P_2 is defined — for a relation $S_1 \sim S_2$ matching states S_1 from P_1 with states S_2 from P_2 — by the following conditions:

• The initial states match

$$\forall S_1, P_1.$$
istate $S_1 \implies \exists S_2, P_2.$ istate $S_2 \land S_1 \sim S_2$

• The final states match

$$\forall S_1 S_2 r, S_1 \sim S_2 \land P_1.$$
fstate $S_1 r \implies P_2.$ fstate $S_2 r$

• The execution steps match through the "Star" simulation diagram (also depicted in Figure 1.4)

$$\forall S_1 \ S_2 \ S_1' \ t, \ S_1 \sim S_2 \wedge S_1 \xrightarrow{t} S_1' \implies \exists S_2', \ S_1' \sim S_2' \wedge (S_2 \xrightarrow{t} S_2' \vee (S_2 \xrightarrow{t} S_2' \wedge |S_1'| < |S_1|))$$

The "Star" simulation diagram expresses that each single step of P_1 producing a trace t can be simulated by several steps of P_2 producing the same trace t. In particular, when P_1 performs an internal step (where $t = \epsilon$), P_2 can *stutter*, i.e. perform no computation step. But, if P_1 loops forever without producing any observable event, then P_2 cannot stutter infinitely.⁵ Indeed, stuttering is only allowed if the step of P_1 makes the state decrease for a well-founded order (hence, sequences of *successive* stutterings cannot be infinite).

The "Star" simulation from Mach to Asm thus corresponds to prove that one Mach step (i.e. one transition of Fig. 3.3) gives the same result as several Asm instructions. For instance, the Mach step from Callstate into State is simulated by the steps of the Asm function prologue that allocate the stack-frame and save it into registers FP (Frame Pointer) and RA. The Mach conditional branching step is simulated by the Asm steps that compute the result of the condition and then branch accordingly. Actually, the only stuttering step of Asm w.r.t Mach corresponds to the *Restoring* step from Returnstate.

⁵Otherwise an infinite silent loop P_1 could be compiled into a program P_2 returning in one step, and this would be incorrect.

3.3.2 Translating Machblock to Asmblock

Overview

Given a basic block from Machblock, the translation consists of emitting an Asmblock basic block that performs the same operation.

The Mach to Asm pass of other backends translates code function by function, then within each function, instruction by instruction.

Our translation goes through the Machblock code function by function, then basic block by basic block. Within each basic block, the labels, basic instructions, then the control-flow instruction are translated consecutively.

Label translation is straightforward. A label in CompCert is a positive identification number, so we translate a label from Machblock to Asmblock by applying the identity function.

The translation of Machblock basic instructions gives Asmblock basic instructions. Indeed, if a Machblock instruction does not modify the control, then there is no reason for the corresponding Asmblock instructions to do so. By "not modifying the control" we mean here: not taking any branch, and going to the "next" instruction in line instead. This is done by the transl_basic_code and transl_instr_basic with the following signatures (the Boolean is there for an optimization explained in the next section):

The translation of Machblock control-flow instructions is less trivial. It gives a list of Asmblock basic instructions (possibly empty), followed by a single Asmblock control-flow instruction.

For example, the translation of a MBreturn cannot be just a ret assembly instruction, because other operations such as restoring the stack pointer must be handled in the function epilogue.

Another example is the (MBcond cond args 1b1) instruction which evaluates the arguments args with the condition cond, and jumps to 1b1 if this evaluation is true. Evaluating a comparison of a register to 0 can be done in one instruction in the Kalray assembly. However, comparing two registers must be done by at least two instructions: one (compd rd rs1 rs2) instruction comparing the two registers rs1 and rs2, writing the Boolean result to rd, then a cb (Conditional Branch) instruction using the value of rd to decide of the branch.

The translation of control-flow instructions is done by a transl_instr_control function of signature:

If we note (L; lb; c) a Machblock basic block, the translation then consists in generating the Asmblock basic block $(L; t_b(lb) ++ l'; c')$ where t_b is transl_basic_code, and l', c' are defined such that $t_c(c) = l' ++ (c' :: nil)$, with t_c being transl_instr_control.

The Argument Pointer Code Optimization in COMPCERT

For handling the loading of function arguments into registers, CompCert's backends perform an optimization that I present here.

There are many possible ways to pass the arguments to a function in assembly code. To ensure compatibility between the different compilers and hand-written assembly code, each architecture defines an ABI (Application Binary Interface), a specification of how arguments should be handled.

The arguments are usually first passed into registers and then onto the stack if there isn't enough room in the registers. In the case of the Kalray Coolidge ABI (but it is also the case for some other ABIs like the Risc-V), when there are too many arguments to be contained by the registers, the caller pushes the extra arguments on the stack. Since each stack-frame is adjacent, the callee can then access the arguments directly via its SP (Stack Pointer) register. For instance, if the stack size of the callee is 24 bytes long, and the stack is in decreasing order (parents are in higher addresses), then the first extra argument will be at address (SP+32).

This poses an issue within the memory model of CompCert. A CompCert address is a couple (b, off), where b is an integer representing the memory block, and off is the offset within that memory block. In this model, memory blocks are not contiguous. Thus, if we take the above example, (SP+32) would be pointing to invalid memory. Consequently, in CompCert, function arguments cannot be accessed with the SP register directly.

The solution adopted by CompCert backends, is to keep the value of the "old SP" somewhere on the stack. It is then part of the specifications that the function prologue should be saving SP before modifying SP. This is done by the Pallocframe pseudo-instruction, for which we give below the specification:

```
1
        \mid Pallocframe sz pos \Rightarrow
2
            let (mw, stk) := Mem.alloc mr 0 sz in
3
            let sp := (Vptr stk Ptrofs.zero) in
4
            match Mem.storev Mptr mw (Val.offset_ptr sp pos) rsr#SP with
5
            | None ⇒ Stuck
6
            | Some mw \Rightarrow Next (rsw #FP \leftarrow (rsr SP) #SP \leftarrow sp #RTMP \leftarrow Vundef) mw
            end
```

This pseudo-instruction is doing two actions in regards to the old value of SP:

- Storing it at (Val.offset_ptr sp pos)
- Copying it at the register FP, a register is arbitrarily chosen among the general-purpose registers that can be used for any operation.

This pseudo-instruction does not correspond to any particular assembly instruction: it is expended into a sequence of assembly instructions by not-formally-verified (but trusted) part of Comp-Cert⁶.

The copy into FP is part of a small optimization done during code generation. Loading a value from memory is expensive in most architectures, and having to load this "old SP" for each access of a parameter would result in a particularly inefficient code. To alleviate this, CompCert backends remember during the code generation whether they previously loaded the old SP or not. Then, when translating a MBgetparam, additional code is inserted if the old SP isn't already loaded in FP. For instance, translating two consecutive MBgetparam writing a parameter in a different register than FP will result in at most one FP reload operation.

In order to remember whether FP is loaded, a Boolean value parameter ep is added to each translation function. The translation starts with ep=true (the prologue initially loads the old SP into FP), then throughout the translation sets ep to true if it has been reloaded, or to false if it might have been destroyed. For instance, ep is set to false every time a label is encountered, since it is not possible to know where did the control originate from.

More precisely, the next value of ep (outside of labels, handled separately) is given by this function (in the case of Kalray backend, but other backends also have a similar function):

```
Definition fp_is_parent (before: bool) (i: Machblock.basic_inst) : bool :=
2
      match i with
3
       | MBgetstack ofs ty dst \Rightarrow before && negb (mreg_eq dst MFP)
4
       \mid MBsetstack src ofs ty \Rightarrow before
5
       | MBgetparam ofs ty dst ⇒ negb (mreg_eq dst MFP)
6
       | MBop op args res ⇒ before && negb (mreg_eq res MFP)
7
       | MBload chunk addr args dst ⇒ before && negb (mreg_eq dst MFP)
8
      \mid MBstore chunk addr args res \Rightarrow before
```

⁶It can be a source of bugs to perform such a critical operation in the uncertified part of CompCert, especially when taking into account the complex support for variadic arguments. The solution is to perform careful testing to rule them out.

9

MFP stands for the Mach register corresponding to FP. In the case of an operation whose result is to be stored in FP, we must invalidate FP by setting ep to false, hence the (negb (mreg_eq dst MFP)) used in most cases of the match.

Constraints of an Asmblock Basic Block

There are two main constraints to verify when forming an Asmblock basic block. These are enforced by a wf_bblock predicate inside a bblock record.

The first constraint is that the bblock should never be empty. Indeed, by our semantics, PC is incremented by the size of the block at the end of its execution. If there are three instructions in the bblock, then, at the end of the bblock step, PC is incremented by three. If the bblock were allowed to be empty, then PC would not get modified; we would then execute the same bblock, which would cause infinite stuttering.

The second constraint comes from the Pbuiltin special instructions. A Pbuiltin instruction represents a *builtin* instruction, that is, an instruction that is inserted directly from the C code to the assembly code, without any translation from the compiler.

Here is an example of a C code containing such a builtin:

```
/* Invalidating data cache */
__builtin_k1_dinval();

int v = tab[40];
printf("%d\n", v+3);
```

The __builtin_k1_dinval builtin produces directly the instruction dinval, which is used to invalidate the data cache before accessing a value on the heap. Such instructions are specially handled by compilers.

In terms of CompCert assembly semantics, they are treated as external function calls (generating a trace). However, they pose the problem that, in assembly, we do not know exactly what they are made of. Indeed, their expansion lies in the uncertified part of CompCert, with the only restriction that a builtin cannot create new functions or sections. As a result, each builtin instruction could generate an entire block of code, with its own labels and more than one control-flow instructions.

We could treat them the same way we treat function call instructions, but then the uncertified scheduler could return us a schedule where the builtin is to be bundled with another basic

instruction, which could lead to absurd code if the builtin is eventually expanded to several instructions and labels.

To prevent the above case, we chose to isolate each builtin with one desired property: if an Asmblock basic block has a builtin instruction, then that instruction must be the only instruction of the basic block.

This ensures that the uncertified expansion should not affect the rest of the generated code though this is not proven formally by lack of precise builtin semantics. Like the function prologue and epilogue, test benchmarks remedy this lack of formal certification.

Let us also recall a third constraint, which is not specific to a bblock but rather a direct definition of our Asmblock semantics: we cannot branch in the middle of a bblock, i.e. a Stuck state is induced when the PC register does not point to the beginning of a bblock. This third constraint is necessary to define a blockstep semantics.

Function Prototypes for Implementation

I describe here the actual functions used for implementing the translation.

For each function, linearly, each basic block is translated via a transl_blocks function, starting with ep=true:

```
Definition transl_function (f: Machblock.function) :=
2
      do lb ← transl_blocks f f.(Machblock.fn_code) true;
3
      OK (mkfunction f.(Machblock.fn_sig) (make_prologue f lb))
```

The make_prologue consists in inserting the Pallocframe pseudo-instruction, as well as instructions making sure the return address is stored on the stack, to have a correct linking when executing the ret instruction of the function epilogue.

The transl_blocks goes through each basic block of the list, translates it, then propagates ep if the block does not have any label.

```
Fixpoint transl_blocks (f: Machblock.function) (lmb: list Machblock.bblock) (ep: bool) :=
2
       match 1mb with
3
       \mid nil \Rightarrow OK nil
       \mid mb :: 1mb \Rightarrow
5
           do lb ← transl_block f mb (if Machblock.header mb then ep else false);
6
           do lb' ← transl_blocks f lmb false;
7
           OK (1b @@ 1b')
       end
```

transl_block is split into three functions: transl_basic_code which translates linearly each basic instruction of the Machblock basic block, then transl_exit_code which translates the optional control-flow instruction, and finally, gen_bblocks which makes one or several basic blocks based on the results of the two last functions.

```
Definition transl_block f fb ep : res (list bblock) :=
do c ← transl_basic_code f fb.(Machblock.body) ep;
do ctl ← transl_instr_control f fb.(Machblock.exit);
OK (gen_bblocks fb.(Machblock.header) c ctl)
```

The gen_bblocks function ensures that we generate bblocks that satisfy the two earlier described constraints:

- a bblock cannot be empty: while we believe this should never happen, we must nevertheless tackle what happens in the case that it does to ensure a forward simulation. We have chosen to generate a bblock with a single nop instruction if we ever come across an empty Machblock basic block.
- a builtin instruction must be alone in its bblock. When we encounter one, we split the basic block into two bblocks.

```
Program Definition gen_bblocks (hd: list label) (c: list basic) (ctl: list instruction) :=
 2
      match (extract_ctl ctl) with
 3
      | None ⇒ match c with
 4
         | \text{ nil} \Rightarrow \{| \text{ header} := \text{hd}; \text{ body} := \text{Pnop}::\text{nil}; \text{ exit} := \text{None} |\} :: \text{nil}
 5
         | i::c \Rightarrow \{| header := hd; body := ((i::c) ++ extract_basic ctl); exit := None | \} :: nil
 6
 7
      | Some (PExpand (Pbuiltin ef args res)) \Rightarrow match c with
 8
       | \text{ nil} \Rightarrow \{| \text{ header} := \text{hd}; \text{ body} := \text{nil}; \text{ exit} := \text{Some (PExpand (Pbuiltin ef args res))} | \} :: \text{nil}
 9
         | \_ \Rightarrow \{ | \text{ header} := \text{hd}; \text{ body} := \text{c}; \text{ exit} := \text{None} | \} ::
10
                   {| header := nil; body := nil; exit := Some (PExpand (Pbuiltin ef args res)) |} :: nil
11
12
      | Some ex \Rightarrow {| header := hd; body := (c++extract_basic ctl); exit := Some ex |} :: nil
13
```

Finally, the extract_basic and extract_ctl functions (not detailed here) extract respectively the basic and the control-flow instructions of a list of instructions.

3.3.3 Proof of Forward Simulation

Issues of Using the Usual Mach to Asm Diagram

The usual diagram consists of starting from two states s_1 and s_2 for which a certain match_states relation holds, executing one Mach instruction, then executing the translated Asm instruction

and proving that the two obtained states s'_1 and s'_2 also verify the match_states relation that we give below for our backend: ⁷

```
Inductive match_states: Machblock.state → Asmvliw.state → Prop :=
2
       | match states intro:
3
           ∀ s fb sp c ep ms m m' rs f tf tc
4
             (STACKS: match_stack ge s)
5
              (FIND: Genv.find_funct_ptr ge fb = Some (Internal f))
6
             (MEXT: Mem.extends m m')
7
             (AT: transl_code_at_pc ge (rs PC) fb f c ep tf tc)
8
             (AG: agree ms sp rs)
9
             (DXP: ep = true \rightarrow rs#FP = parent_sp s),
10
           match_states (Machblock.State s fb sp c ms m)
11
                       (Asmvliw.State rs m')
```

This relation ensures several things, among which:

- AG and MEXT ensures the value of registers and memory match those of the Machblock state
- AT ensures that, in the memory pointed by PC register, the Machblock code c is translated into the Asmblock code tc with the Boolean parameter ep.
- DXP ensures that if ep is true, then FP must contain the value of the old SP.

In the other CompCert backends, the match_states relation holds between each execution of a Mach instruction. For each possible Mach instruction, lemmas are then proved to ensure that executing, on the one hand, the Mach instruction, on the other hand, the translated Asm instructions, lead to the same result.

In our case, using the above match_states directly is tricky: instead of executing one Mach instruction and reasoning on its translation, we execute an entire basic block of Machblock instructions and must reason on the translation of the whole block.

A possibility for us could be to define a finer grain step relation, which would execute a single instruction of a basic block on the Machblock part. In Machblock, executing one instruction could be as simple as executing its effects, then removing it from the current basic block. On the Asmblock side, one could suggest incrementing PC instruction by instruction instead of doing it all at the end of the bblock; however that would not be compatible with the constraint that we must not branch in the middle of a bblock.

A New Diagram to Prove Machblock to Asmblock

In the lights of this difficulty, we chose to introduce a new state definition used for reasoning at a finer grain. We call it a Codestate, and define it as follows:

⁷I am here only describing the particular case of executing code within an internal function

```
1
    Record codestate :=
2
       Codestate { pstate: state;
                                       (* projection to Asmblock.state *)
3
                  pheader: list label; (* list of label *)
4
                  pbody1: list basic; (* list of basics coming from the Machblock body *)
5
                  pbody2: list basic; (* list of basics coming from the Machblock exit *)
6
                  pctl: option control; (* exit instruction, coming from the Machblock exit *)
7
                  ep: bool;
                                      (* reflects the [ep] variable used in the translation *)
8
                  rem: list AB.bblock; (* remaining bblocks to execute *)
9
                  cur: bblock
                                      (* current bblock to execute - useful to increment PC *)
10
                }
```

A Codestate augments a state of Asmblock by including the instructions to execute, much like Machblock. It also includes the value of ep used when translating the first instruction of Codestate.

With this new Codestate, we can decompose the match_states relation into two relations.

The first of these two relations is match_codestate, which ensures an agreement between a Machblock state and a Codestate, namely: the code residing in the Codestate must have been a result of a translation of a Machblock code, the memory and register states should correspond, and also the ep value of the Codestate should match with the one used in the translation.

```
1
     Inductive match_codestate fb: Machblock.state \rightarrow codestate \rightarrow Prop :=
 2
        | match_codestate_intro:
 3
            ∀ s sp ms m rs0 m0 f tc ep c bb tbb tbc tbi
 4
              (STACKS: match_stack ge s)
 5
              (FIND: Genv.find_funct_ptr ge fb = Some (Internal f))
 6
              (MEXT: Mem.extends m m0)
 7
              (TBC: transl_basic_code f (MB.body bb) (if MB.header bb then ep else false) = OK tbc)
 8
              (TIC: transl_instr_control f (MB.exit bb) = OK tbi)
 9
              (TBLS: transl_blocks f c false = OK tc)
10
              (AG: agree ms sp rs0)
11
              (DXP: (if MB.header bb then ep else false) = true → rs0#FP = parent_sp s)
12
13
            match_codestate fb (Machblock.State s fb sp (bb::c) ms m)
14
              {| pstate := (Asmvliw.State rs0 m0);
15
                  pheader := (MB.header bb);
16
                  pbody1 := tbc;
17
                 pbody2 := extract_basic tbi;
18
                  pctl := extract_ctl tbi;
19
                  ep := ep;
20
                 rem := tc;
21
                 cur ≔ tbb
22
              |}
```

The second relation is match_asmstate between a Codestate and an Asmblock state, ensuring that the code present in a Codestate resides in memory of the Asmblock state, at the address pointed by the PC register.

```
1 Inductive match_asmstate fb: codestate → Asmvliw.state → Prop :=
```

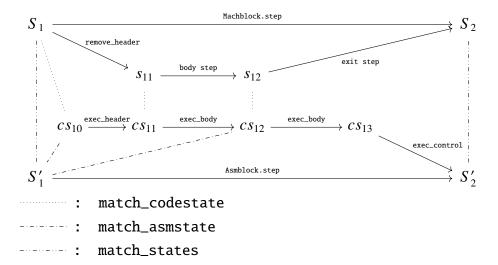


Figure 3.6.: Diagram of the Simulation Proof

```
2
        | match_asmstate_some:
 3
            V rs f tf tc m tbb ofs ep tbdy tex lhd
 4
              (FIND: Genv.find_funct_ptr ge fb = Some (Internal f))
 5
              (TRANSF: transf_function f = OK tf)
 6
              (PCeq: rs PC = Vptr fb ofs)
 7
              (TAIL: code_tail (Ptrofs.unsigned ofs) (fn_blocks tf) (tbb::tc))
 8
 9
            match_asmstate fb
10
              {| pstate := (Asmvliw.State rs m);
11
                  pheader := lhd;
12
                  pbody1 := tbdy;
13
                  pbody2 := extract_basic tex;
14
                  pctl := extract_ctl tex;
15
                  ep := ep;
16
                  rem := tc;
17
                  cur := tbb |}
18
              (Asmvliw.State rs m)
```

Both relations take an extra fb parameter, which is the function block, an integer value identifying the current function.

The details of proving the Machblock to Asmblock pass with these two new match relations are very cumbersome (it is, in general, the case for all of the Mach to Asm proofs of the various backends - there are a lot of details and corner cases to consider). In particular, we are not covering here the case of a builtin instruction. However, we are giving below the general idea of simulating a bblock without builtin, assuming we already have an existing Mach to Asm proof to base ourselves on.

Figure 3.6 depicts the diagram we went for. It can be decomposed in three theorems for simulating respectively the Machblock header, body, and exit. The exec_header is a predicate which removes the header from the bblock, and sets ep to false if there was a header:

```
Inductive exec_header: codestate → codestate → Prop :=

| exec_header_cons: ∀ cs1,

exec_header cs1 {| pstate := pstate cs1; pheader := nil; pbody1 := pbody1 cs1;

pbody2 := pbody2 cs1; pct1 := pct1 cs1;

ep := (if pheader cs1 then ep cs1 else false); rem := rem cs1;

cur := cur cs1 |}
```

We start by the theorem match_state_codestate, allowing us to decompose (match_states $S_1 S_1'$) into a (match_codestate $S_1 cs_{10}$) and a (match_asmstate $cs_{10} S_1'$) with a fitting cs_{10} :

```
1
      Theorem match_state_codestate:
 2
        \forall mbs abs s fb sp bb c ms m,
 3
        (\forall \text{ ef args res, MB.exit bb } <> \text{Some (MBbuiltin ef args res)}) \rightarrow
 4
        (MB.body bb \ll nil \vee MB.exit bb \ll None) \rightarrow
 5
       mbs = (Machblock.State s fb sp (bb::c) ms m) \rightarrow
 6
       match\_states mbs abs 	o
 7
       \exists cs fb f tbb tc ep,
 8
          match_codestate fb mbs cs \wedge match_asmstate fb cs abs
 9
         A Genv.find_funct_ptr ge fb = Some (Internal f)
10
          ^ transl_blocks f (bb::c) ep = OK (tbb::tc)
11
          ∧ body tbb = pbody1 cs ++ pbody2 cs
          ∧ exit tbb = pctl cs
12
13
          \wedge cur cs = tbb \wedge rem cs = tc
14
          \land pstate cs = abs
```

The Machblock header simulation is then straight forward, and is proven by the step_simu_header theorem below. After this theorem, the state s_{11} is free of any header.

```
Theorem step_simu_header:

V bb s fb sp c ms m rs1 m1 cs1,

pstate cs1 = (State rs1 m1) →

match_codestate fb (MB.State s fb sp (bb::c) ms m) cs1 →

(∃ cs1',

exec_header cs1 cs1'

∧ match_codestate fb (MB.State s fb sp (mb_remove_header bb::c) ms m) cs1')
```

The body simulation is then proven by induction on the list of basic instructions of s_{11} , each individual case is covered by adapting the old proofs of Mach to Asm for the basic instructions.

```
Theorem step_simu_body:
 2
       ∀ bb s fb sp c ms m rs1 m1 ms' cs1 m',
3
       MB.header bb = nil \rightarrow
       (\forall ef args res, MB.exit bb \iff Some (MBbuiltin ef args res)) \rightarrow
 5
       body_step ge s fb sp (MB.body bb) ms m ms' m' \rightarrow
6
       pstate cs1 = (State rs1 m1) \rightarrow
 7
       match_codestate fb (MB.State s fb sp (bb::c) ms m) cs1 \rightarrow
8
      (∃ rs2 m2 cs2 ep,
9
             cs2 = {| pstate := (State rs2 m2); pheader := nil; pbody1 := nil; pbody2 := pbody2 cs1;
10
                       pctl := pctl cs1; ep := ep; rem := rem cs1; cur := cur cs1 |}
11
         ∧ exec_body tge (pbody1 cs1) rs1 m1 = Next rs2 m2
     ∧ match_codestate fb (MB.State s fb sp
```

```
13 ({| MB.header := nil; MB.body := nil; MB.exit := MB.exit bb |}::c) ms' m') cs2)
```

This theorem gives a state s_{12} without any body anymore, just the exit instruction. We can then use the last theorem, step_simu_control:

```
Theorem step_simu_control:
2
        \forall bb' fb fn s sp c ms' m' rs2 m2 t S'' rs1 m1 tbb tbdy2 tex cs2,
3
        MB.body bb' = nil \rightarrow
 4
        (\forall ef args res, MB.exit bb' <> Some (MBbuiltin ef args res)) \rightarrow
5
        Genv.find_funct_ptr tge fb = Some (Internal fn) \rightarrow
 6
        pstate cs2 = (Asmvliw.State rs2 m2) \rightarrow
7
        pbody1 cs2 = nil \rightarrow pbody2 cs2 = tbdy2 \rightarrow pctl cs2 = tex \rightarrow
8
       cur cs2 = tbb \rightarrow
9
        match_codestate fb (MB.State s fb sp (bb'::c) ms' m') cs2 \rightarrow
10
        match\_asmstate fb cs2 (Asmvliw.State rs1 m1) \rightarrow
11
        exit_step return_address_offset ge (MB.exit bb') (MB.State s fb sp (bb'::c) ms' m') t S'' \rightarrow
12
       (∃ rs3 m3 rs4 m4,
13
            exec_body tge tbdy2 rs2 m2 = Next rs3 m3
14
       ∧ exec_control_rel tge fn tex tbb rs3 m3 rs4 m4
15
        natch_states S'' (State rs4 m4))
```

That last theorem gives us a match_states between a S'_2 and S_2 which is what we are looking for. The final theorem step_simulation_bblock then uses the four theorems to prove the plus simulation.

```
Theorem step_simulation_bblock:

V sf f sp bb ms m ms' m' S2 c,

body_step ge sf f sp (Machblock.body bb) ms m ms' m' \rightarrow

(V ef args res, MB.exit bb <> Some (MBbuiltin ef args res)) \rightarrow

exit_step return_address_offset ge (Machblock.exit bb)

(Machblock.State sf f sp (bb :: c) ms' m') E0 S2 \rightarrow

V S1', match_states (Machblock.State sf f sp (bb :: c) ms m) S1' \rightarrow

S2' : state, plus step tge S1' E0 S2' \rightarrow match_states S2 S2'
```

3.4 Formal verification of the basic block postpass scheduling

Our postpass scheduling takes place during the pass from Asmblock to AsmVLIW (Fig. 3.1). This pass has two goals:

- 1. reordering the instructions in each basic block to minimize the stalls;
- 2. grouping into bundles the instructions that can be executed in the same cycle.

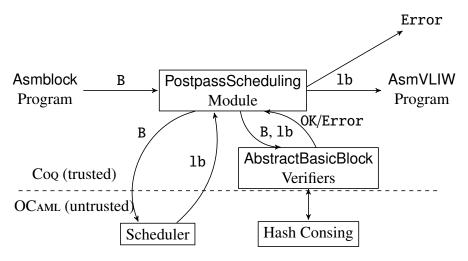


Figure 3.7.: Certified Scheduling from Untrusted Oracles

Similarly to Tristan and Leroy [96], our scheduling is computed by an untrusted oracle that produces a result which is checked by Coo-proved verifiers. A significant benefit of this design is the ability to change the untrusted oracle without modifying our Coo proofs.

The verifiers check semantic correctness only. If some generated bundle exceeds resource constraints, it will be rejected by the assembler.

Scheduling is performed block by block from the Asmblock program. As depicted in Fig. 3.7, it generates a list 1b of AsmVLIW bundles from each basic block B. More precisely, a basic block B from Asmblock enters the PostpassScheduling module. This module sends B to an external untrusted scheduler, which returns a list of bundles 1b, candidates to be added to the AsmVLIW program (scheduling is detailed in chapter 9). The PostpassScheduling module then checks that B and 1b are indeed semantically equivalent through dedicated verifiers. Then, PostpassScheduling either adds 1b to the AsmVLIW program or stops the compilation if the verifier returned an error.

In Coo, the scheduler is declared as a function⁸ splitting a basic block "B:bblock" into a value that is then transformed into a sequence of bundles "lb: list bblock".⁹

```
Axiom schedule: bblock \rightarrow (list (list basic))*(option control)
```

The proof of the pass uses a "*Plus*" *simulation* (Fig. 1.4): one step of the initial basic block B in the sequential Asmblock semantics is simulated by stepping sequentially all bundles of 1b for the parallel AsmVLIW semantics. This forward simulation results from the composition of these two ones:

⁸The scheduler is declared as a pure function like other CompCert oracles.

⁹It would be unsound to declare schedule returning directly a value of type "list bblock", since the "correct" proof field of bblock does not exist for the OCAML oracle.

- 1. A plus simulation ensuring that executing B is the same as executing 1b in the sequential Asmblock semantics, which proves the reordering part of the postpass scheduling.
- 2. A lockstep simulation ensuring that executing each bundle of 1b with the Asmblock semantics gives the same result as executing this bundle with the parallel AsmVLIW semantics.

Each of these two forward simulations is derived from the correctness property of a dedicated verifier. In other words, we prove that if each of these two verifiers returns "OK", then the corresponding forward simulation holds. The following sections describe these two verifiers and their correctness proof. We first introduce AbstractBasicBlock, a helper IR that we use for both simulations. Then we describe the "parallelizability checker" ensuring a lockstep simulation (2). Finally, we describe the "simulation checker" ensuring a plus simulation (1).

3.4.1 AbstractBasicBlock IR

The core of our verifiers lies in the AbstractBasicBlock specific representation, designed by Sylvain Boulmé. AbstractBasicBlock provides a simplified syntax, in which the registers that are read or assigned by each instruction appear syntactically. The memory is encoded by a pseudo-register denoted by m. ¹⁰ We illustrate in Example 3.4.1 how we have translated some instructions into AbstractBasicBlock assignments.

Example 3.4.1 (Syntax of AbstractBasicBlock). *Examples of translations into AbstractBa*sicBlock:

- 1. the addition of two registers r_2 and r_3 into r_1 is written " $r_1 := add[r_2, r_3]$ ";
- 2. the load into register r_1 of memory address "ofs $[r_2]$ " (representing ofs + r_2 where ofs is an integer constant) is written " $r_1 := (load \ ofs)[m, r_2]$ ";
- 3. the store of register r_1 into memory address "ofs $[r_2]$ " is written " $m := (store\ ofs)[m, r_1, r_2]$ ".

AbstractBasicBlock is dedicated to intra-block analyses. In AbstractBasicBlock, a block is encoded as a list of assignments, meant to be executed either sequentially or in parallel depending on the semantics. Each assignment involves an expression composed of operations and registers.

The syntax and semantics of AbstractBasicBlock are generic and have to be instantiated with the right parameters for each backend. I did that task for the KV3 backend, though this is easily extendable to other backends such as AArch64 [89].

¹⁰This encoding should be refined in the future to introduce alias analysis

AbstractBasicBlock provides a convenient abstraction over assembly instructions like most IR of CompCert except Asm: it leverages the hundreds of AsmVLIW instructions into a single unified representation. Compared to the Mach IR—used in the initial approach of Tristan and Leroy [96]— AbstractBasicBlock is more low-level: it allows to represent instructions that are not present at the Mach level, like those presented in Section 3.4.6. It is also more abstract: there is no particular distinction between basic and control-flow instructions, the latter being represented as an assignment of a regular pseudo-register PC. The simplicity of its formal semantics is probably the key design point that allows us to program and prove the verifiers efficiently.

The following sections summarize how we used AbstractBasicBlock to certify the scheduling of Asmblock/AsmVLIW. A more detailed presentation of AbstractBasicBlock is available in Six et al. [88, Section 5 & Appendix C].

3.4.2 Parallelizability Checker

To check whether a certain bundle's sequential and parallel semantics give the same result, we translate the bundle into AbstractBasicBlock with a trans_block function, then we use the is_parallelizable function from AbstractBasicBlock.

Function is_parallelizable analyzes the sequence of AbstractBasicBlock assignments and checks that no pseudo-register is read or rewritten after being written once. For example, blocks " $r_1 := r_2$; $r_3 := r_2$ " and " $r_1 := r_2$; $r_2 := r_3$ " are accepted as parallelizable. However, " $r_1 := r_2$; $r_2 := r_1$ " and " $r_1 := r_2$; $r_2 := r_3$ " are rejected, because r_1 is used after being written.

When is_parallelizable returns true, the list of assignments has the same behaviour in both the sequential and the parallel semantics. This property at the AbstractBasicBlock level can be lifted back to the AsmVLIW/Asmblock level because the list of assignments returned by trans_block is proven to *bisimulate* the input block—both for the sequential and the parallel semantics. This bisimulation is also useful for the simulation checker described next section.

Proving the previously mentioned forward simulation (2) then relies on proving the following lemma bblock_para_check_correct which is proven by using the above bisimulation property.

```
Definition bblock_para_check bundle: bool := is_parallelizable (trans_block bundle)
Lemma bblock_para_check_correct ge f bundle rs m rs' m': bblock_para_check bundle = true ->
exec_bblock ge f bundle rs m = Next rs' m' -> det_parexec ge f bundle rs m rs' m'
```

The syntax of AbstractBasicBlock and its semantics are generic, in the sense that the IR is parametrized by the names of pseudo-registers and the syntax and semantics of operators. Thus,

as claimed in the introduction, it can be easily reused for other processors or other IRs of CompCert.

3.4.3 Verifying Intrablock Reordering

To reason on reordering, we define a concatenation predicate: "is_concat tb 1b" means that the bblock tb is the *concatenation* of the list of bundles 1b. Formally, 1b must be non-empty, only its head may have a non-empty header, only its tail may have a control flow instruction, tb.(body) must be the concatenation of all the bodies of 1b and the header (resp. exit) of the head (resp. tail) of 1b must correspond to the header (resp. exit) of tb.

We also define a *block simulation*: a block b is *simulated* by a block b' *if and only if* when the execution of b is not Stuck, executing b and b' from the same initial state gives the same result (using the sequential semantics). That is, b' preserves any non-Stuck outcome of b.

```
Definition bblock_simu ge f b b' := ∀ rs m,
exec_bblock ge f b rs m <> Stuck → exec_bblock ge f b rs m = exec_bblock ge f b' rs m
```

The forward simulation (1) reduces to proving the correctness of our verified_schedule function on each basic block, as formalized by this property:

```
1 Theorem verified_schedule_correct: ∀ ge f B lb,
2 (verified_schedule B) = (OK lb) → ∃ tb, is_concat tb lb ∧ bblock_simu ge f B tb
```

In detail, (verified_schedule B) calls our untrusted scheduler (schedule B) and then builds the sequence of bundles 1b as well as their concatenation tb. Then, it checks each bundle for parallelizability with the bblock_para_check function described in the previous section. Finally, it calls a function bblock_simub: $bblock \rightarrow bblock \rightarrow bool$ checking whether tb simulates B.¹¹

Function bblock_simub is composed of two steps. First, each basic block is compiled (through the trans_block function mentioned in Section 3.4.2) into a sequence of AbstractBasicBlock assignments. Second, like in [96], the simulation test symbolically executes each AbstractBasicBlock code and compares the resulting *symbolic memories* (Fig. 3.8). A symbolic memory roughly corresponds to a parallel assignment equivalent to the input block. More precisely, this symbolic execution computes a term for each pseudo-register assigned by the block: this term represents the final value of the pseudo-register in function of its initial value.

¹¹More precisely, if the result of "bblock_simub B tb" is true, then "bblock_simu ge f B tb" holds.

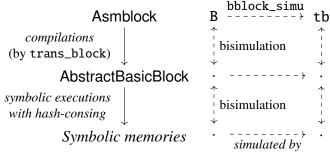


Figure 3.8.: Diagram of bblock_simub Correctness

Example 3.4.2 (Equivalence of symbolic memories). Let us consider the two blocks B_1 and B_2 below:

$$(B_1)$$
 $r_1 := r_1 + r_2$; $r_3 := load[m, r_2]$; $r_1 := r_1 + r_3$

$$(B_2)$$
 $r_3 := load[m, r_2]; r_1 := r_1 + r_2; r_1 := r_1 + r_3$

They are both equivalent to this parallel assignment:

$$r_1 := (r_1 + r_2) + load[m, r_2] \parallel r_3 := load[m, r_2]$$

Indeed, B_1 and B_2 bisimulate (they simulate each other).

Collecting only the final term associated with each pseudo-register is actually incorrect: an incorrect scheduling oracle could insert additional failures. Thus, the symbolic memory must also collect a list of all intermediate terms on which the sequential execution may fail and that have disappeared from the final parallel assignment. See Example 3.4.3 below. Formally, the symbolic memory and the input block must be bisimulable as pictured in Fig 3.8.

Example 3.4.3 (Simulation on symbolic memories). *Consider:*

$$(B_1)$$
 $r_1 := r_1 + r_2$; $r_3 := load[m, r_2]$; $r_3 := r_1$; $r_1 := r_1 + r_3$

$$(B_2)$$
 $r_3 := r_1 + r_2$; $r_1 := r_3 + r_3$

Both B_1 and B_2 lead to the same parallel assignment:

$$r_1 := (r_1 + r_2) + (r_1 + r_2) \parallel r_3 := r_1 + r_2$$

However, B_1 is simulated by B_2 , whereas the converse is not true. This is because the memory access in B_1 may cause its execution to fail, whereas this failure cannot occur in B_2 . Thus, the symbolic memory of B_1 should contain the term "load[m, r_2]" as a potential failure. We say that a symbolic memory d_1 is simulated by a symbolic memory d_2 if and only if their parallel assignments are equivalent, and the list of potential failures of d_2 is included in the list of potential failures of d_1 .

As illustrated in Examples 3.4.2 and 3.4.3, the computation of symbolic memories involves many duplications of terms. Thus, comparing symbolic memories with structural equalities of terms, as performed in [96], is exponential time in the worst case. To solve this issue, we have

developed a generic verified hash-consing factory for Coo. Hash-consing consists of memoizing the constructors of some inductive data-type to ensure that two structurally equal terms are allocated to the same object in memory. This enables us to replace (expensive) structural equalities with (constant-time) pointer equalities.

3.4.4 Generic and Verified Hash-Consing

Below is given a brief overview of the hash-consing mechanism.

Hash-consing a data-type simply consists of replacing the usual constructors of this data-type by smart constructors that perform the memoization of each constructor. This memoization is usually delegated to a dedicated function that can, in turn, be generated from a generic factory [29]. Our hash-consing technique follows this principle. However, whereas the memoization factory of Filliâtre and Conchon [29] (in OCAML) has no formal guarantee, ours satisfies a simple correctness property that is formally verified in Coq: each memoizing function observationally behaves like an identity.

Our Coo memoization function on terms invokes an external untrusted OCAML oracle that takes as input a given term and returns a memoized term (possibly memoizing the input term in the process). Then, our Coo memoization function dynamically checks that the memoized term and the input term are isomorphic or aborts the computation if it cannot ensure they are. This check is kept constant-time by using OCAML pointer equality to compare already memoized subterms: $f(t_1,\ldots,t_m)$ and $g(u_1,\ldots,u_n)$ are tested for isomorphism by checking that the head symbols f and g are identical, the numbers of arguments m and n are the same, and for all i, t_i and u_i are the same pointer. We have thus imported OCAML pointer equality into Coq.

Importing an OCAML function into Coq is carried out by declaring the type of this OCAML function through an axiom: the Coo axiom is replaced by the actual OCAML function at extraction. Using a pure function type in this Coq axiom implicitly assumes that the OCAML function is *logically* deterministic (like any Coq function): calling the function twice on equal inputs should give equal outputs—where equality is Coo equality: structural equality. In contrast, the OCAML pointer equality does not satisfy this property: two structurally equal values do not necessarily have the same pointer.¹²

We solve this issue by using the *pointer equality* from the IMPURE library of Boulmé [15], which embeds OCAML functions in Coq through a non-deterministic monad. In particular, it represents

¹²Hence, if we model pointer equality (OC_{AML}'s ==) as an infix function "phys_eq: $\forall \{A\}, A \rightarrow A \rightarrow bool$ ", then we are able to prove this wrong proposition (when x and y are structurally equals but are distinct pointers): $y=x \rightarrow (phys_eq x y)=false \rightarrow (phys_eq x x)=true \rightarrow false=true$

```
Axiom phys_eq: ∀ {A}, A → A → ??bool

Extract Constant phys_eq ⇒ "←⇒"

Axiom phys_eq_true: ∀ A (x y:A), phys_eq x y ~> true → x=y
```

OCAML *pointer equality* as a non-deterministic function.¹³ We then use the axiom from IMPURE stating that, if pointer equality returns true, then the two values are (structurally) equal.

Here, "??boo1" is logically interpreted as the type of all "subsets" of Booleans; phys_eq is the physical equality, later extracted as the OCAML (==); and " \leadsto " is the may-return relation of the IMPURE library: "phys_eq x y \leadsto true" means that "true" is a *possible* result of "phys_eq x y". In other words, even if "phys_eq x y \leadsto true" and "phys_eq x y \leadsto b", then we cannot conclude that "b=true" (we could also have "b=false"). The IMPURE library does not even assume that " \forall x, phys_eq x x \leadsto true".

These axioms are proved to be non-contradictory w.r.t. the Coo logic. They express a correctness property of OCAML physical equality, from which we derive efficient and formally verified hash-consing.

3.4.5 Peephole Optimization

We have expressed the semantics of assembly instructions by decomposing them into atomic operations, which we used to define the symbolic execution. This means that distinct groups of instructions that decompose into the same atomic operations are considered equivalent. We exploited this to implement *peephole optimization*: local replacement of groups of instructions by faster ones prior to scheduling. On Fig. 3.7, this untrusted optimization is performed by a preliminary pass of the "Scheduler" oracle, and thus dynamically checked by our bblock_simub trusted verifier.

Currently our only peephole optimizations are the replacement of two (respectively, four) store instructions from an aligned group of double-word (64-bit) registers (e.g. \$r18, \$r19) to a succession of offsets from the same base register (e.g. 8[\$r12], 16[\$r12]) by a single quadruple-word (respectively, octuple-word) store instruction; and the same with loads. In practice, this quickens register spilling and restoring sequences, such as those around function calls: CompCert spills and restores registers in ascending order, whereas in general, it would only be sheer chance that register allocation placed data that is consecutive in memory into an aligned group of consecutive registers. Léo Gourdin implemented a similar but slightly more complex optimization for the AArch64 architecture: loads and stores to consecutive memory

¹³In the Coq logic, two occurrences of variable "x" may correspond to two distinct objects in memory (e.g. after substituting y=x in "P x y"). This is why phys_eq must appear as "non-deterministic" to Coq's eyes.

locations, but not necessarily consecutive register indices, are searched for in the assembly code and grouped together.

3.4.6 Atomic Sequences of Assignments in AbstractBasicBlock

In the previous examples, each AsmVLIW instruction is translated to a single assignment of AbstractBasicBlock. However, in many cases (extended-word accesses of Sect. 3.4.5, control-flow instructions, frame-handling pseudo-instructions, etc), AsmVLIW instructions cannot correspond to a single assignment: they are rather translated to AbstractBasicBlock as an atomic sequence of assignments (ASA). A form of parallelism may occur in such a sequence through the special operator Old(e) where e is an expression, meaning that the evaluation of e occurs in the initial state of the ASA. And an AsmVLIW bundle (resp. an Asmblock basic-block) corresponds to the parallel (resp. sequential) composition of a list of such ASA.

For example, the parallel load from a 128-bit memory word involves two contiguous (and adequately aligned) destination registers d_0 and d_1 that are distinct from each other by construction but not necessarily from the base address register a. This parallel load is thus translated into the following ASA, that emulates a parallel assignment of d_0 and d_1 , even if $a = d_0$:

$$d_0 := (\operatorname{load} i)[m, a] ; d_1 := (\operatorname{load} (i + 8))[m, (\operatorname{old} a)]$$

General Concepts of Superblock Scheduling

We manipulated basic blocks within the postpass scheduling optimisation—sequences of instructions within a function, each with only one entry point and one exit point. Throughout the remaining chapters, we will study prepass scheduling, in RTL, at the level of superblocks: a generalisation of basic blocks where additional exit points (called *side exits*) are allowed. Compared to our previous work, superblocks are much like how we defined basicblocks (several *basic* instructions, followed by an optional *control-flow* instruction) except that this time, conditional branches are also allowed among the "basic" instructions. This chapter introduces the basic notions of superblocks: it informally describes the transformations we perform on superblocks and briefly discusses their correctness.

Superblock optimisation techniques originate from compiler literature — in particular, the papers Hwu et al. [40] and Lee et al. [49] describe the implementation of superblock scheduling in particular compilers, along with other superblock-related optimisations. Much like trace scheduling (introduced by Fisher [31]), superblock scheduling optimises a given path of the program by moving instructions before conditional branches¹. If the optimised path is frequently taken, the function execution will be faster. However, this is to the detriment of other paths, whose execution will be slower. Hence, while basicblock scheduling is an optimisation in the scope of a basic block, superblock scheduling has the more general scope of a trace (later turned into a superblock) within a function.

The first step to form superblocks is to identify an execution trace likely to be executed (section 4.1). That trace selection, driven mainly by *branch prediction*, outlines traces that have the potential to become superblocks of interest. To ensure a faster execution (rather than a slower), it is of great interest to have a sufficiently accurate branch prediction. Then, transformations are done on each interesting trace to superblockify them and increase the optimisation potential of certain superblocks (section 4.2). In particular, we perform *tail duplication* and *loop unrolling*. Finally, we schedule the resulting superblock (section 4.3): reordering the instructions, potentially moving them upwards across branches, aiming to get a faster resulting machine code.

¹The transformation also allows to move them below conditional branches, at the discretion of the scheduler

We depict in section 4.4 how our optimisations are inserted among the already existing RTL optimisations.

Similar work was done by Tristan and Leroy [95] to implement *trace scheduling* at the Mach level, in an older version of CompCert. *Trace scheduling* is more general than *superblock scheduling*: it also allows to move code below or above side-entrances. Moving code below *side exits* require to duplicate instructions (this is called *bookkeeping*), much like *tail duplication* for superblocks. However, moving code above or below *side entrances* requires more complex bookkeeping. For our prepass, we chose *superblock scheduling* instead of the *trace scheduling* technique from Tristan and Leroy [95] for the following reasons:

- In trace scheduling, bookkeeping and scheduling are done in the same pass. Superblock scheduling, on the other hand, allows us to dissociate tail duplication with the actual scheduling. In particular, we can apply optimisations such as CSE3, ² constant propagation or dead code elimination, between tail-duplication (which might introduce redundant computations) and the actual scheduling, which might improve the scheduling opportunities.
- On the contrary of the original trace scheduling from Fisher [31], the *trace scheduling* of Tristan and Leroy [95] systematically duplicates instructions when they are moved above a side-exit; our superblock scheduling, on the other end, can move instructions above side-exit without any duplication (under certain conditions expressed through a liveness analysis).

In this chapter, I will not detail the verificators or their proof of correctness, and I will not lay out the actual algorithms used either — this will be tackled in the later chapters. This chapter is, instead, a general picture overview of superblock scheduling and the new passes introduced.

In practice, the transformations detailed here happen at the RTL level of CompCert. However, to properly analyse the performance, we have to consider the other passes between RTL and the final assembly code. Thus, most of the examples shown in this chapter will be shown in assembly. In particular, I will briefly discuss how the transformations presented here relate to the further passes, particularly the Linearize, Postpass Scheduling and CSE3.

4.1 Guiding trace selection with branch prediction

Predicting which branch is likely to be taken is necessary to ensure that our optimisations result in a performance gain rather than a loss. Indeed, the superblock scheduling optimisation is only beneficial if the superblock is executed frequently in its entirety.

²CSE3 is a common subexpression elimination that analyses across branches.

Branch prediction affects:

- Trace selection: only the traces likely to be executed are selected.
- Tail duplication, as a direct consequence of trace selection being affected.
- Loop unrolling: we only unroll loops that cover a superblock, but also determining the direction of the loop (which condition leads to the loop body) is reliant on branch prediction.
- Superblock scheduling: the superblocks to be scheduled depend on branch prediction and the former passes.

If profiling information is available, we can use it to drive the above passes. However, it is still possible to "guess" which way the program is more likely to go if there is none. Our static branch prediction is based on Ball and Larus [4], with some additions and fine-tuning to their techniques. We then use predictions to select traces, using a technique inspired by Chang and Hwu [20].

4.1.1 What we expect out of static branch prediction

Let us consider a program consisting of two imbricated loops, like the kind shown in figure 4.1. The innermost loop is the one that interests us: this is usually where most of the computation time lies. Our goal is to apply loop transformations on that loop (such as loop unrolling) and then perform superblock scheduling. However, that loop has one other branch inside.

Ideally, we would like our static branch prediction to perform well in two aspects:

- The branch prediction should be able to predict the conditional branch correctly from the innermost loops. It should privilege the trace going within the loop instead of the one going out. Also, if there is a branch leading to exiting the loop, then that branch should be predicted to stay within the loop. This ensures that our later trace selection (followed by tail duplication) will indeed form a superblock encompassing the loop.
- In the given example (figure 4.1), the branch "in the middle" is a "may-exit" branch. However, there are other examples with branches for which both ends remain within the loop. This would happen if the body of the if does not have any return or break. In such a case, we should not try to wild guess it. Indeed, without profiling information, we might be lucky and guess right just like we might be wrong and end up decreasing performance, sometimes by a large margin. We have found it best to leave such examples untouched: the trace (superblock) would then stop at the branch instead of going through it (and consequently, we do not unroll such loops).

Generally speaking, a false negative (an unpredicted branch that could have been predicted) will just result in a lack of optimisation: it will not decrease the performance compared to the original

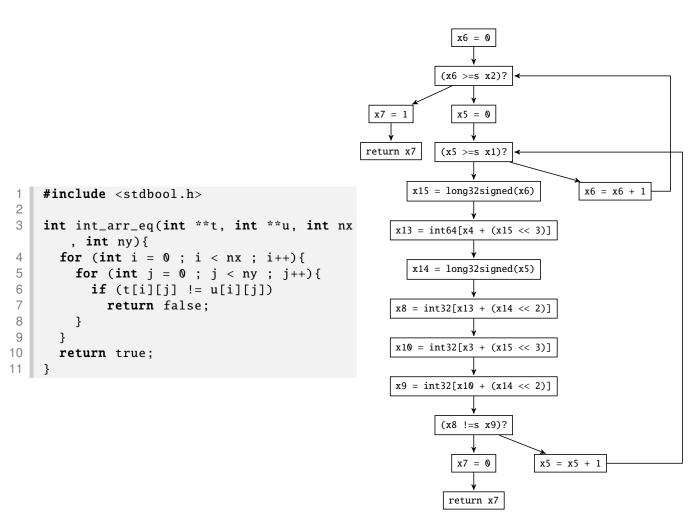


Figure 4.1.: Two imbricated loops

code. However, a false positive (a predicted branch with a wrong prediction) can be harmful to the performance.

As a result, we tried to tune the static branch prediction in such a way as to get a low number of false positives but still be able to identify most of the superblockification opportunities out of innermost loops. This work has been mostly empirical — involving a lot of trying out algorithms, witnessing the impact on performance, then analysing individual examples where we saw a decrease in performance, and iterating on the compiler code until we got to a satisfying state.

4.1.2 Storing the prediction

The compiler literature (such as Lee et al. [49]) usually advises storing the profiling information under one float number per branch edge, which indicates the probability to take that edge when branching. Then, for trace selection, path is dug following edges that have more than 50% probability.

In our case, our superblock transformations are scattered across several elementary passes. There is a need for each of these passes to get consistent information for knowing which branch is privileged. In particular, if we were annotating each conditional branch with such a probability number, then we would need each of our passes to interpret such a number consistently, to prevent cases where say a tail-duplication treated a particular set of instructions as a superblock, but the superblock scheduling treated another different set of instructions for scheduling.

Given our compiler architecture, we also think it is better not only to store which branch should be privileged but also to point out whether there are branches for which we are *unsure* of the privileged direction. To illustrate that, let us examine the program shown in figure 4.2. This program is fictional — each letter represents one instruction, with A and D being conditional branches. If each branch has say a 51% probability to take the privileged branch, and we move instruction E_1 to the top of instruction A (because the scheduler ruled that this would give a faster execution *under the assumption that we follow the trace* $A - B - D - E_1 - E_2 - H$), then we would only have 25% chance to get a faster execution. Indeed, on that particular example, three different paths are possible: $A - B - D - E_1 - E_2 - H$ (26%), A - B - D - F - H (25%) or A - C - G - H (49%). That move would be only beneficial for the first path and detrimental for the other two because of the waste of time executing E_1 (wrongly) speculatively. For that particular case, we would have labelled each branch to be of *unsure* direction and stop the trace, rather than identifying a *too big* trace whose scheduling results in a worse performance.

The two above points led us to adopt one Option bool prediction p_c per conditional branch c, with the following informal semantics:

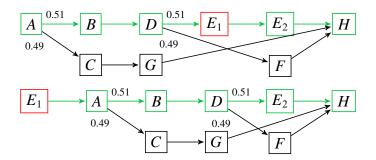


Figure 4.2.: Program with two branches. Top figure: original program. Bottom figure: the instruction E_1 is moved before A (under the non-trivial assumption that it is correct to do so). An identified trace (that could be turned into a superblock) is shown in green. Each conditional branch edge is annotated with its probability.

- p_c = None: no prediction attached for c. Either we are unsure of which way the branch goes, or the static/profiling prediction has not been run yet.
- p_c = Some true: the branch instruction c is predicted to be very likely to follow the ifso branch (condition evaluates to true).
- p_c = Some false: the branch instruction c is predicted to be very likely to follow the ifnot branch (condition evaluates to false).

4.1.3 Acquiring prediction information

Prediction information can be acquired through two means, the first of which is to use profiling. The code is instrumented to record profile information in the form of a file. Then, that file is used on the subsequent compilations to guide the prediction. In the absence of profiling information, static heuristics can be used. By exploiting specific patterns in the program, it is possible to make a fair, educated guess on the direction of most branches. In particular, innermost loops and their exit branches can be detected by static prediction: this paves the way for the later superblock optimisations.

With profiling

We use the profiling from our version of CompCert [16] (see modules Profiling and ProfilingExploit). This profiling system was developed by D. Monniaux. The profiling instrumentation is done through the addition of additional code on top of the existing CompCert code:

- Counters are inserted into each object file as local symbols.
- Right after each branch, a special CompCert builtin EF_profiling is inserted, which increments the appropriate counter.

• When the main function exits, all the counters are written to a file. This is done through additional linker code added to each compiled object file.

Once the profiling is recorded by executing the program one time, it is then possible to use that information to add prediction information to branches. For now, the profiler-based heuristic consists of simply assigning the prediction to None when the two branches counts are equal, or Some b if one branch is executed more than another (with b chosen accordingly). In the future, this could be refined to be less aggressive (say, by choosing None when the relative difference between the two branches counts is too small).

D. Monniaux also implemented support for __builtin_expect: a compiler built-in to be placed in branches to indicate the most likely branch direction.

With heuristics

If no profiling is available, we have certain heuristics to make an educated guess at the privileged direction. Most of these are heavily inspired from Ball and Larus [4]. The following heuristics are run in sequence until one of them decides a prediction. If none of them could decide a prediction, then the prediction information will remain None.

- We look at the comparison used in the conditional branch: a comparison such as (x < 0)? is seen as something likely to be an error-code check, so we predict that the check succeeds (that is, the condition is not taken). On the same line of thoughts, float equality checks are predicted to be false most of the time.
- If a given branch leads to a return, then that branch is unlikely to be taken.
- If a branch leads to a backedge (a looping edge), and if the other branch does not also lead to a backedge ³, then this is very likely to be a conditional branch from an innermost loop with one branch diving inside the loop and the other branch exiting the loop. We then predict that the looping branch should be privileged. This heuristic is critical for later identifying the superblock following that innermost loop.
- Finally, if a given branch leads to a call instruction and the other does not, then the branch without call is privileged.

Experimentally, these heuristics seem to be enough to detect most branches of interest. However, we still ran into one or two minor edge cases where the prediction failed (particularly for the first heuristic on conditions).

³In regards to CompCert RTL representation and how it generates loops, two imbricated loops usually lead to such a case where the two branches from the conditional branch lead to a backedge. This will be explained in more details in chapter 8

4.1.4 Driving the selection based on predictions

Once branch prediction has been done, several phases of selection are done:

- For tail-duplication, a trace selection for electing the traces that will be transformed into superblocks.
- For the loop unrolling optimisation, a superblock selection to elect the superblocks that encompass innermost loops.
- For the superblock scheduling, another superblock selection, which aims to partition the entire code into superblocks.
- Finally, for the Linearize phase (linearizing the code from LTL to Mach), yet another superblock selection, with the same goal as above: partitioning the code into superblocks.

Trace selection for tail-duplication

This phase is the most complex of the four mentioned above and ends up defining which parts of the code will be optimised. We mainly use the algorithm from Chang and Hwu [20], which consists of selecting a node that has the largest execution count, then growing a trace forward (by going through the "best successors" in regards to execution count), and then grow it backward. Then, the trace stops, and the next unvisited node is selected to grow a new trace.

A few key differences that our implementation has in regards to their algorithm:

- It is unclear whether their algorithm allows for traces crossing each other (the presence of nodes that would belong to strictly more than one trace). In any case, since we intend for our traces to become superblocks, we chose to prohibit the traces from crossing each other.
- They have access to precise execution counts for each node. However, in the most general case (when we have no profiling information), we would be unable to get any fair approximation of such execution count. In the case of the presence of profiling information, it could be possible to get them. A first method would be to compute an approximation of the execution count based on our profiler's edge information. Another method would be to add profiling counters to each RTL basic-block ⁴ and then use them to propagate the execution count on RTL nodes. We found that the effort required was non-negligible, for an unclear gain, so we focused on other aspects of the optimisations instead.

Our algorithm has then been adapted (compared to theirs) to take into account these two differences. We stop the trace if we encounter a node already visited to prevent getting traces from crossing each other. And then, instead of reasoning by execution count to decide the "best

⁴These would have to be manually reconstructed since each RTL node consists of a single instruction.

successor" or "best predecessor", we decide it based on the privileged nodes, as indicated by the branch prediction information, stopping the trace when that information is None.

Superblock selection for the other passes

The other phases are more straightforward since their goal is to identify superblocks, not traces. One issue here is the replication of the selection algorithms: we detect superblocks three times over each function (even if for loop unrolling, we only select superblocks that encompass an innermost loop). Ideally, one would like to have some way to store the superblock information somewhere once and for all, and then the selection would just be about looking up that current information. In terms of data structure, this information could be a list of RTL nodes used for each superblock.

However, introducing and maintaining such information would require two things:

- 1. To be able to pass that information along with the successive passes. We would either need to use some global pointer in an OCAML module, used by our oracles — but that would break the Coq assumption that OCAML functions are pure. To overcome this, we could use the Impure library again, but that might be adding significant proof efforts. ⁵ Alternatively, we could add other pieces of information to the existing RTL language, just like we did for storing branch information. However, we felt like it would be cumbersome to maintain for the existing passes, in particular, because of the second point below.
- 2. Updating such superblock information whenever any change is done to the code. Indeed, RTL transformations can potentially add new instructions, remove some others, or just change the whole structure of the program. Updating the branch prediction information is easy enough, and we do that already. ⁶ However, updating a list of instructions used by each superblock would be another story: it could potentially add significant effort to each RTL transformation pass, regardless of any proof, as well as adding maintenance burden.

This led us to recompute the superblock selection once per superblock optimisation pass. On the one hand, this can potentially lead to inconsistencies: one pass optimising a superblock a certain way, while another pass optimises it in a completely different way because the superblocks are not the same. On the other hand, our selection algorithms all rely on making superblocks as big as possible (following the preferred direction every time, if there is one). ⁷ So my personal belief

⁵Though it might be trivial to do so, we never know until we do try it. To quote the famous idiom: "The devil is in the details".

⁶Say if a branch is inverted: just negate the boolean stored in the prediction. For more complex transformations, one could always set it to None for particularly nasty cases.

⁷See algorithm 2 for an example.

```
// returns (t[0] * t[1]) + (t[2] * t[3]) + ...
2
    int sum_product (int *t, int n) {
3
      int S = 0;
4
      for (int i = 0; i < n; i += 2) {
5
        if (i == n-1)
6
          S += t[i]; // only remaining element
7
8
          S += t[i] * t[i+1];
9
10
      return S;
11 }
```

Figure 4.3.

is that this has no impact on the overall quality of the produced code — and, when examining the code structure on our benchmarks, we did not witness such oddity. ⁸

Consequently, each pass implements a variation of the following informal algorithm:

- We compute *join points*: those are nodes that are reached by more than one predecessor.
- We form superblocks starting from the unique *entrypoint*:
 - If the node has a *preferred successor*, and it is not a *join point*, we add it to the superblock and continue the formation through that successor.
 - Else, we stop the current superblock and start creating new superblocks from the exit
 nodes that were recorded while forming the former superblock by order of encounter.

This allows us to have (as far as we have observed) consistency between each pass regarding superblock selection.

4.2 Superblock transformations before scheduling

To illustrate the superblock transformations, let us analyse the C sample given by figure 4.3. In this piece of code, we perform the multiplication of each pair of consecutive elements, which we then sum together. If the array has an odd number of elements, the last element will be summed to the rest. One way to handle that is to get a if..else construct within the for loop, to take into account the edge case of the last iteration.

That example (disregarding any bundle) is translated into the following simplified assembly code on figure 4.4, after basicblock scheduling. ⁹ It is annotated with timings information.

⁸Except, of course, while debugging our introduced algorithms. Like any uncertified code, our oracles may be subject to implementation bugs.

⁹Note: the Linearize oracle of CompCert here chose to layout the ELSE branch before the IFSO. It uses heuristics such as the code length to decide. More details can be found in section 8.3.

Indeed, on the Kalray architecture, assuming the instruction and data caches never miss, it is possible to compute by hand the number of cycles that a piece of code takes: each bundle is issued in one cycle, to which penalties may have to be added — either data dependency penalties (e.g. using a register which has not been computed yet), or branch penalties (unconditional jumps give 1 cycle penalty, conditional branches give 2 cycles when the branch is taken). We annotated the assembly code with these timings information (assuming the ELSE branch is taken). An example of such penalties is on Line 22: the maddw instruction uses \$r5, which needs the lws.xs to complete before being used; the goto induces another cycle penalty on top of that.

This code is inefficient in two ways.

First, because of the presence of ELSE basicblock, the code has to execute two unconditional jumps (goto instructions) to loop: at the end of the ELSE block and then at the end of LOOPINCR block. This adds 1 cycle per loop iteration. On tiny loops such as this one, this represents 7% of the 14 cycles required to execute one iteration, which is not negligible.

Second, if we were able to move instructions atop conditional branches, then the sxwd and addw instructions from ELSE basicblock could be executed in the same bundle as compw.eq from SWITCH basicblock. This would make us gain another cycle.

The first issue could be tackled by transforming the code so that the basicblocks (LOOPCOND, SWITCH, ELSE and LOOPINCR) end up as one monolithic (without any branch taken, except for going out) trace. This could be done by moving the IFSO basicblock right after the LOOPINCR basicblock in the linearised code. The IFSO basicblock would then have to get an additional goto instruction; however, this would allow to remove the goto from the ELSE basicblock.

Our trace would then be executable with just one goto branch taken. However, we would still be unable to use superblock scheduling to tackle the second issue: since IFSO has LOOPINCR as a successor, our trace has two different entrypoints.

To solve these issues, we use the following techniques:

- First, we use *tail duplication*, detailed in section 4.2.1, to transform our identified trace into a superblock.
- Second, if our superblock is an innermost loop, we apply loop unrolling to make it more fruitful for scheduling. This is detailed in section 4.2.2.
- Then, we perform *superblock scheduling* to re-order instructions across the given superblock, detailed in section 4.3.
- Finally, we augmented the Linearize heuristic used by CompCert, to ensure that each superblock is laid out contiguously in memory. This part is detailed in section 8.3.

Our tail duplication and loop unrolling techniques are inspired by what is described in Lee et al. [49].

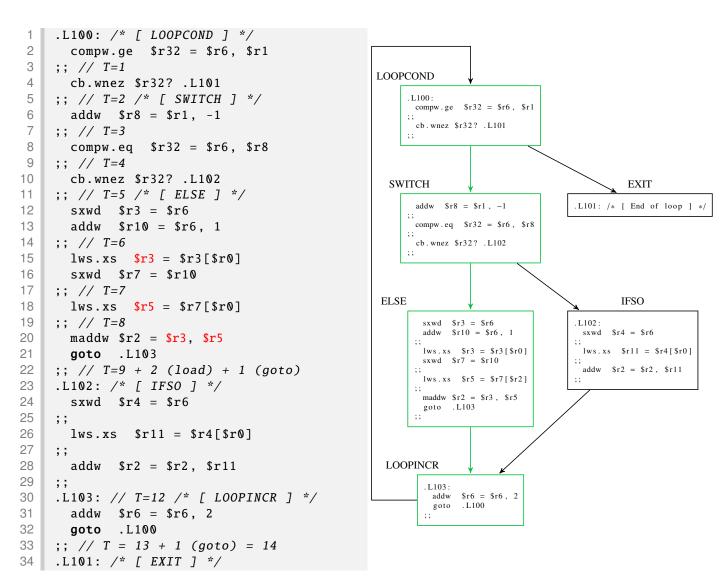


Figure 4.4.: On the left, the assembly generated code, annotated with timings information. On the right, its basicblock representation, with a trace of interest shown in green. In the assembly code, the registers targetted by load instructions along the trace are written in red. See appendix A for an instruction reference.

4.2.1 Tail duplication

As it stands, the trace (LOOPCOND, SWITCH, ELSE and LOOPINCR) is not a superblock yet: indeed, IFSO points within the trace, so it has a second entrypoint. Given a selected trace, tail-duplication consists of identifying the first additional entrypoint and then duplicating the tail of the trace starting from the identified entrypoint. Anything that would point to the tail is then modified to point to the duplicated tail instead. This thus transforms the original trace into a superblock.

Figure 4.5 shows the result of performing tail-duplication on our selected trace. We show both the RTL representation (in which we perform the translation) and the resulting assembly code, annotated with timing information just like the previous.

We duplicate the LOOPINCR block of code, and change IFSO to point to the new LOOPINCR' instead. Our trace is now a superblock: we will be able to perform superblock scheduling on it later on. We linearised the code in such a way that the resulting code of ELSE does not contain any goto instruction: our superblock is a contiguous block of code, which makes us win one cycle (we lose the latency from the goto that was present in the previous code). Furthermore, as a side effect of doing so, the ELSE and LOOPINCR blocks can now be fused into one basicblock: compared to our previous code, our postpass scheduling gains one additional cycle by mixing their instructions together.

In this particular example, the result of performing tail-duplication (and smartly linearising the code) is then to gain 2 cycles out of the initial 14 required to compute one iteration.

4.2.2 Loop unrolling

Loop unrolling consists of duplicating the body of a loop so that several iterations are run before looping back. We perform a specific kind of loop unrolling, which duplicates the conditional branch for going out of the loop. The result of such a transformation can be seen in figure 4.6.

This transformation is interesting because it preserves the superblock structure: the trace (LOOPCOND, SWITCH, ELSE, LOOPINCR, LOOPCOND2, SWITCH2, ELSE2, LOOPINCR2) is now a two times bigger superblock than the original. Without any prepass scheduling, this has two effects on the resulting code, in terms of performance:

- When executing two iterations, this removes one goto: we gain one cycle
- Laid out like this, the CSE optimization pass was able to determine that the x13 = x1 + x-1 instruction from SWITCH2 is redundant: indeed, x1 did not change. That instruction was then removed, which in fine made us win another cycle.

```
.L100: /* [ LOOPCOND ] */
 1
 2
        compw.ge $r32 = $r4, $r1
      ;; // T=1
 3
        cb.wnez $r32? .L101
 4
      ;; // T=2 /* [ SWITCH ] */
 5
 6
        addw $r8 = $r1, -1
 7
      ;; // T=3
 8
        compw.eq $r32 = $r4, $r8
                                                             LOOPCOND
      ;; // T=4
 9
        cb.wnez $r32? .L102
10
                                                          18: if (x3 \ge x1) goto 2 else goto 17
11
      ;; // T=5 /* [ ELSE+LOOPINCR ] */
        sxwd $r6 = $r4
12
                                                               SWITCH
                                                                                                  EXIT
13
        addw
                r7 = r4, 1
                                                          17: x13 = x1 + -1
16: if (x3 == s x13) goto 7 else goto 15
                                                                                                 x5 = x4
14
        addw $r4 = $r4, 2
                                                                                               1: return x5
15
      ;; // T=6
16
        lws.xs r10 = r6[r0]
                                                               ELSE
17
        sxwd $r5 = $r7
                                                                                                      IFSO
                                                             15: x12 = long32signed(x3)
14: x8 = int32[x2 + (x12 << 2)]
18
      ;; // T=7
                                                                                              x7 = long32signed(x3)

x6 = int32[x2 + (x7 << 2)]
                                                             14: x8 = int32[x2 + (x12 << 2)]

13: x11 = x3 + 1

12: x10 = long32signed(x11)

11: x9 = int32[x2 + (x10 << 2)]

10: x4 = x4 + x8 * x9
        lws.xs r3 = r5[r0]
19
                                                                                              x4 = x4 + x6
      ;; // T=8
20
21
        maddw $r2 = \frac{r10}{r3}
                                                                                          LOOPINCR'
22
        goto .L100
                                                             LOOPINCR
23
                                                                                                  4: \quad x3 = x3 + 2
      ;; // T=9 + 2 (1d) + 1 (goto) = 12
                                                                                                  3: goto 18
                                                                      x3 = x3 + 2
goto 18
      .L102: /* [ IFSO+LOOPINCR' ] */
24
25
        sxwd $r3 = $r4
26
        addw $r4 = $r4, 2
27
28
        29
30
        addw r2 = r2, r11
```

Figure 4.5.: Tail duplicating the identified trace.

31

32

;;

goto .L100

.L101: /* [EXIT] */

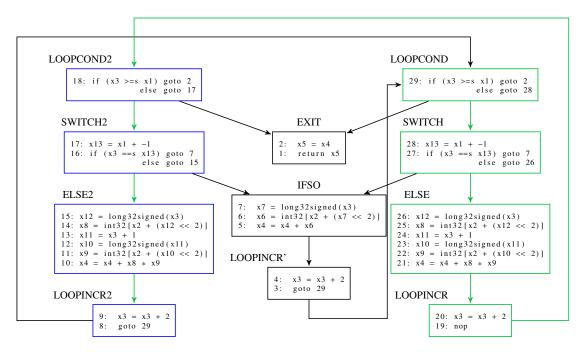


Figure 4.6.: Performing loop unrolling one time

In total, after loop unrolling, executing two iterations is now 20 cycles. On average, an iteration is then 10 cycles (instead of 12 before loop unrolling).

4.3 Superblock scheduling

Once a superblock has gone through tail-duplication and potentially unrolling, it is ready for being scheduled. Much like basicblock scheduling, the goal of superblock scheduling is to minimise an execution time: here, minimising those of the paths that go through the entire superblock, *i.e.* taking no branch (all conditional branches from that superblock must result in their *fallthrough* case).

Under such an assumption, it is possible to approximate the time it takes to execute a given superblock. Indeed, the only control-flow instructions allowed inside a superblock are conditional branches. They each supposedly go through their *fallthrough* case, which induces no cycle penalty on the Kalray architecture.

In terms of scheduling oracle, there are two major differences compared to the postpass scheduling oracle:

• We manipulate RTL instructions, which are not exactly assembly instructions (unlike postpass scheduling). However, we can use the translation functions from the later passes (in particular, the translation from Mach to Asm) and combine it with the timing functions

```
.L100: /* [ LOOPCOND ] */
                                       28
                                            ;; // T=12
2
      compw.ge $r32 = $r7, $r1
                                       29
                                             cb.wnez $r32? .L102
3
                                            ;; // T=13
    ;; // T=1
                                       30
4
      cb.wnez $r32? .L101
                                       31
                                            /* [ ELSE2 + LOOPINCR2 ] */
    ;; // T=2 /* [ SWITCH ] */
                                              sxwd $r34 = $r7
5
                                       32
                                             addw $r9 = $r7, 1
6
      addw $r8 = $r1, -1
                                       33
7
    ;; // T=3
                                       34
                                             addw r7 = r7, 2
      compw.eq $r32 = $r7, $r8
8
                                       35
                                            ;; // T=14
9
    ;; // T=4
                                       36
                                              lws.xs r11 = r34[r0]
10
      cb.wnez $r32? .L102
                                       37
                                             sxwd $r6 = $r9
                                            ;; // T=15
11
    ;; // T=5
                                       38
    /* [ELSE+LOOPINCR+LOOPCOND2] */
                                             lws.xs r3 = r6[r0]
12
                                       39
                                            ;; // T=16
13
      sxwd  $r33 = $r7
                                       40
      addw r4 = r7, 1
14
                                       41
                                             maddw $r2 = $r11, $r3
15
      addw $r7 = $r7, 2
                                       42
                                             goto .L100
16
    ;; // T=6
                                       43
                                            ;; // T=17 + 2 (1d) + 1 (goto) = 20
17
      lws.xs r15 = r33[r0]
                                       44
                                           /* [ IFSO ] */
      sxwd $r5 = $r4
                                       45
18
                                            .L102:
19
      compw.ge $r32 = $r7, $r1
                                       46
                                              sxwd
                                                   r10 = r7
20
                                       47
                                             addw $r7 = $r7, 2
    ;; // T=7
21
      48
    ;; // T=8
22
                                       49
                                             lws.xs  $r3 = $r10[$r0]
23
      maddw $r2 = $r15, $r17
                                       50
24
                                       51
      cb.wnez $r32? .L101
                                             addw $r2 = $r2, $r3
25
    ;; // T=9 + 2 (load)
                                       52
                                             goto .L100
    /* [ SWITCH2 ] */
26
                                       53
      compw.eq $r32 = $r7, $r8
                                            .L101: /* [ EXIT ] */
                                       54
```

Figure 4.7.: Final code after tail duplication and loop unrolling.

from the postpass scheduler oracle to make an educated guess at the RTL instructions latencies as well as their resource usage. This guess might be inexact: in particular, if the register allocator (RTL to LTL translation) introduces spills, then our scheduled time will be off. Further optimisations between LTL and Asm might also reduce the actual number of cycles for a given superblock, compared to our guess.

• Like the postpass scheduling, data dependencies between instructions have to be considered. In addition to that, some additional dependencies have to be inserted involving conditional branches: even though our oracle assumes (for the sake of computing timings) that each conditional branch is not taken, there is a possibility for a conditional branch to be taken, in which case the program should remain correct.

Once the dependencies and resource constraints are computed (the additional dependencies are described in 4.3.1), we can choose any scheduling oracle. Subsection 4.3.2 discusses informally two variants of list scheduling in regards to scheduling opportunities and register allocation. Then, I show the result of applying superblock scheduling to the example from section 4.2, in subsection 4.3.3.

4.3.1 Elements of superblocks scheduling correctness

Compared to basicblock scheduling, several new elements have to be checked to ensure correctness before deciding to execute an instruction speculatively. To illustrate that, figure 4.8 shows two examples of scheduling our tail-duplicated (but not unrolled, for simplicity) program from earlier.

The first schedule attempts to move all instructions from ELSE (conserving their own partial order) before the conditional branch (x3 == s x13)?. We mark them in red. In terms of data dependencies among the superblock, this is a correct move: the conditional branch instruction does not write to any register, so neither Write-After-Read nor Read-After-Write are possible. However, there is one issue: x4 is written to in the IFSO branch! By moving the instruction x4 = x4 + x8 * x9 before the conditional branch, we are actually introducing a new Write-after-Write dependency on the (SWITCH, IFSO) path that wasn't there before. This move is then incorrect.

The second schedule does the same, but only for instructions that do not introduce any additional *Read-after-Write* or *Write-after-Write* dependency. In terms of data writes, the program is correct. There is still one additional issue: the RTL int32[...] instructions represent load instructions, and these may trap if their address is incorrect. In a normal execution (one without speculation), this might happen if the program has undefined behaviours — but then it would be a problem lying in the application source code rather than a compiler bug. However, in the

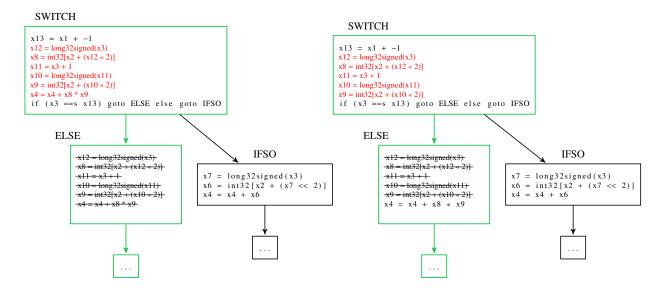


Figure 4.8.: Two scheduling examples — the moved instructions are in red. The left schedule is incorrect: an instruction assigning x4 was moved before a branch which later uses x4. The right schedule is correct.

case of speculative execution (moving an instruction before a branch), one might execute an instruction before a branch ensured that its operands would be valid. Such an example could be a C program containing "if (ptr != NULL) x = ptr->foo;": evaluating ptr->foo before the branch could trap if ptr == NULL, whereas the normal execution might not have trapped at all.

At the end of the day, in addition to the dependencies constraints we saw for basicblock scheduling, the following has to be checked to ensure that a given superblock scheduling is correct:

- The moved instructions (either above or below a side-exit) should not change the result of any instruction in the "exit" part of the conditional branch. This can be checked with a liveness analysis: the live registers at the time of branching should not be modified by the reordering.
- No trapping instruction should be moved before a conditional branch. ¹⁰ To remedy that, certain architectures like the KVX have support for *speculative* instructions which do not trap when their operands are invalid. Since the KVX supports *speculative* loads, we turn loads into speculative loads when they move before a conditional branch.

Certifying the superblock scheduling turned out to be challenging in terms of proof effort (contrary to tail-duplication and loop unrolling, who were easy to prove). The later chapters will describe the proofs involved, from designing an IR to execute superblocks to certifying the actual scheduling.

¹⁰More generally, moving an instruction before a side-exit should not add any additional undefined behaviour.

```
x5 = int32[x1 + 0]
                                                lws
                                                       r1 = 0[r0]
2
         x6 = int32[x1 + 4]
                                       2
                                                       r2 = 4[r0]
                                                lws
3
                                       3
                                                       r1 = r1, r2
         x3 = x5 + x6
                                                addw
4
         x4 = int32[x1 + 8]
                                       4
                                                lws
                                                       r2 = 8[r0]
                                       5
         x2 = x3 + x4
                                                addw
                                                       r1 = r1, r2
```

Figure 4.9.: Example illustrating the impact of register allocation on scheduling. Left: RTL code example; it is possible to move instruction 4 before instruction 3 to reduce stalls. Right: Assembly (before scheduling) example; that move is not possible because of a false dependency with \$r2.

4.3.2 Choosing an appropriate scheduling oracle

Doing superblock scheduling before register allocation has two advantages. First, as mentioned earlier, we profit from the more extensive scheduling scope (superblock instead of basicblock). However, since the registers are not allocated yet, there are no false dependencies in the code, unlike postpass scheduling. Figure 4.9 shows a simple RTL code computing t[0] + t[1] + t[2], before register allocation. One possible outcome of assembly generation (after register allocation and before postpass scheduling) is shown on the right. To prevent a stall in the x2 = x3 + x4 assignment, a valid scheduling could be to move the load assigning x4 before x3 = x5 + x6. However, such scheduling is not possible after register allocation because the register allocator was pressured to reuse the \$r2 register instead of introducing a new register \$r3. 11 Prepass scheduling does not have this issue.

The downside of scheduling before register allocation is that it may increase *register pressure*—that is, the number of registers that are *live* at a given time. Going back to the example in figure 4.9: in the unscheduled version, only x5 and x6 have to be live during the first addition. Moving the load assigning x4 before the addition would add x4 to the list of live registers, thus increasing the register pressure. When there is too much register pressure, the register allocator has no choice but to insert *spills*: saving a register to the stack, then reloading it later. In which case, prepass scheduling can worsen performance instead of improving speed.

The general problem of easing the interactions between the scheduler and register allocation is a tough one. There has been work to merge both optimisations into one, like Motwani et al. [65], and more recently Lozano et al. [57]. This is far beyond our scope: implementing such solutions would require rewriting the register allocator of CompCert and its proof and merging scheduling within: this would be a titanic task.

¹¹On this particular example, the CompCert register allocator would have chosen to allocate a new register. However, in large functions, it is common for the register allocator to reuse registers. Whether it reuses the "right" register (one that would not introduce false dependency) or not is then a matter of luck.

One possible solution for not having too much pressure on the register allocation is to do *backward list scheduling*, as described in Cooper et al. [23]. The core idea is to reverse all edges from the dependency graph and schedule the *finish times* instead of the *starting times*. Whereas forward list scheduling tends to cluster operations to the beginning of the scheduled block, backward scheduling tends to cluster operations to the bottom of it, which should ease the register pressure. ¹²

The code presented in this chapter uses this variant. Though we have found in our benchmarks that applying regular forward scheduling gives a better performance on average, which can be partly explained by the KVX architecture having many available registers, we rarely suffer the effects of increased register pressure. An alternative would be to make the scheduler sensitive to register pressure [36; 87]; this is left to future work.

4.3.3 Application to our example

The optimisations that we presented before scheduling were able to shave a few cycles off our example. However, that was just a side effect — their real goal was to increase the superblock's scheduling potential. At last, let us apply superblock scheduling to our example. Figure 4.10 shows the new processor code obtained after activation of the prepass scheduler. We can notice significant progress compared to the code that was presented in figure 4.7.

- Many instructions were able to be moved before conditional branches, which allowed to "fill the gaps" in the bundles. If we take the first line from the code after unrolling, there was a single instruction compw.ge in the bundle. In the code with superblock scheduling, that instruction is executed alongside sxwd and addw. Having such a denser packing contributes to having fewer bundles executed: for the identified trace, we went from 15 bundles (unrolled version) down to 13. *A priori*, this can make us save 2 cycles.
- The most significant result is the lack of any stall, thanks to the use of speculative loads. All the load instructions were able to be scheduled in such a way as to not induce any stall. This makes us save 4 cycles compared to the unrolled version.

In fine, it takes 14 cycles to execute our new code, so 7 cycles per iteration. Compared to the unrolled version of 10 cycles per iteration, that is 30% fewer cycles. Compared to the original version (without any of the optimisations presented in this chapter: no tail-duplication, no loop unrolling, no superblock scheduling), which was at 14 cycles, that is 50% fewer cycles. This results in twice faster execution, on the privileged path, for this particular example.

¹²A variant of this technique is used in Sarkar et al. [83] to decrease register pressure.

```
.L100: /* [ SUPERBLOCK ] */
1
                                            lws.s.xs r3 = r5[r0]
2
                                      26
      sxwd $r9 = $r34
                                            sxwd $r5 = $r33
3
      addw r6 = r34, 1
                                      27
                                          ;; // T=9
4
      compw.ge $r32 = $r34, $r1
                                      28
                                            lws.s.xs r15 = r5[r0]
                                            cb.wnez $r32? .L101
5
                                      29
    ;; // T=1
6
                                      30
     lws.s.xs r7 = r9[r0]
                                          ;; // T=10
7
      sxwd $r8 = $r6
                                      31
                                            compw.eq
                                                     r32 = r34, r4
8
    ;; // T=2
                                          ;; // T=11
                                      32
9
     cb.wnez $r32? .L101
                                      33
                                            cb.wnez $r32? .L102
                                          ;; // T=12
10
    ;; // T=3
                                      34
11
      addw r4 = r1, -1
                                      35
                                            maddw $r2 = $r3, $r15
      lws.s.xs r11 = r8[$r0]
                                            addw
12
                                      36
                                                  r34 = r34, 2
13
                                      37
                                            goto
                                                  .L100
    ;; // T=4
14
      compw.eq $r32 = $r34, $r4
                                      38
                                          ;; // T=13 + 1 (goto)
15
    ;; // T=5
                                      39
                                          /* [ IFSO ] */
     cb.wnez $r32? .L102
16
                                      40
                                          .L102:
17
    ;; // T=6
                                      41
                                                 r17 = r34
                                            sxwd
                                      42
18
      addw $r34 = $r34, 2
                                            addw $r34 = $r34, 2
19
      maddw $r2 = $r7, $r11
                                      43
20
                                      44
                                            ;; // T=7
21
                                      45
      sxwd $r5 = $r34
22
      addw $r33 = $r34, 1
                                      46
                                            addw r2 = r2, r10
                                      47
                                                 .L100
23
      compw.ge $r32 = $r34, $r1
                                            goto
24 ;; // T=8
                                      48
                                      49
                                          .L101: /* [ EXIT ] */
```

Figure 4.10.: Our example, with prepass scheduling activated. It is annotated with timings information.

4.4 Superblock transformations and RTL

Each code optimisation is supposed to, on its own, induce an improvement in the resulting program. Still, a specific order has to be chosen for each code optimisation to be run sequentially.

In the case of superblock transformations, we already have a straightforward partial order. First, branch prediction (either through profiling or heuristics) should annotate the conditional branches since all the other superblock passes rely on that. Tail-duplication allows turning the body of specific innermost loops into superblocks, making it logical to do it after branch prediction and before the other superblock transformations. The same goes for loop unrolling: except that by applying tail-duplication before, we have more chance to find innermost loops eligible for unrolling (they must follow a superblock structure for the unrolling to do any benefit). Finally, superblock scheduling should be the last of all superblock transformations since the former transformations aim at increasing the scheduling potential.

However, it is a bit more unclear how should these passes fit into existing (and future) RTL transformations of CompCert. The superblock transformations might result in better optimisation opportunities for later passes — on the other hand, optimisations might result in a better trace selection or tail-duplication. In subsection 4.4.1, we give an overview of each RTL optimisation

and discuss its impact on superblock transformation passes. Then, in subsection 4.4.2, we layout the actual used order.

4.4.1 Existing RTL transformations in regards to superblock transformations

Let us analyse each RTL transformation and discuss how it affects our superblocks passes — or perhaps, how our superblock passes may affect it.

Tailcall generation

This optimisation detects functions that end with calling another function. It allows for the called function to reuse the stack frame of the (tail) caller instead of creating its own new stackframe, thus reducing stack memory consumption. In practice, this optimization just transforms certain Icall instructions into Itailcall.

This has no impact on any of our superblock transformations. Furthermore, our superblock transformations would not have any positive impact on this transformation. So it is safer for this transformation to be placed before our superblock optimisations.

Function inlining

Function inlining consists of identifying small functions and replacing some calls to such functions by their entire code.

Our superblock transformations can harm this transformation since we might make functions bigger by tail-duplication or loop unrolling, making them uneligible for inlining. Also, this transformation can help a great deal with our transformations by replacing calls, thus extending the number of instructions to schedule. A natural choice is then to perform this optimisation before ours.

Common Subexpression Elimination

This optimisation aims to detect expressions that are computed more than once: the additional computations are then replaced by the appropriate register containing the result of the computation. Informally, code such as x0 = x3 + x4; x1 = x2 * (x3 + x4) would become

x0 = x3 + x4; x1 = x2 * x0. In our version of CompCert, we have two variants of this optimization:

- The original CSE optimization, from mainstream CompCert. That optimisation performs the above optimisation on *extended basicblocks*: groups of basicblocks with only one predecessor (except the first). In practice, this optimisation stops at *join points*. In particular, it does not traverse loops (since a loop header has two predecessors: the node dominating the loop and the last node of the loop).
- A new CSE3 optimization from D. Monniaux [63], which propagates the analysis across *join points*.

In our compilation flow we perform two common subexpression elimination: one before static branch prediction, since it might have an influence in the prediction heuristics, and both CSE and CSE3 version after the instruction duplication passes.

CSE combined with loop unrolling can increase performance from naturally replacing loop-invariant expressions by their assigned register (see the example of section 4.2.2). As an extension, CSE3 combined with loop peeling ¹³ achieves Loop-Invariant Code Motion [63].

Constant propagation

Constant propagation consists of pre-computing the operations whose results can be known at compile time. For example, x0 = 42; x1 = x0 + 3 could be turned into x0 = 42; x1 = 45. It might probably help static branch prediction if constant propagation is done before. Like CSE, a good fit would probably be to do it before and after the instruction duplication passes. In our experiments, we do it only once, after instruction duplication.

Deadcode elimination

Dead code elimination consists of eliminating the computations that are, in fact, never used. So, in a program such as x0 = x4 * x5; return x2, the x0 = x4 * x5 could be removed, since that result is discarded when returning x2. It should not matter whether we perform this optimisation before or after ours — we do it among the last optimizations, just before superblock scheduling.

¹³Loop peeling copies one iteration out of the loop body, see section 8.2.

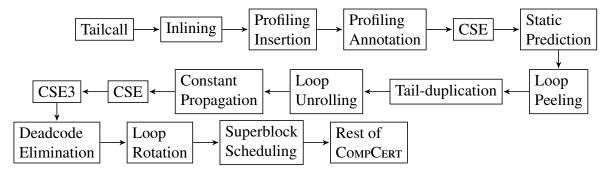


Figure 4.11.: Our order of RTL optimizations

4.4.2 Order of transformations

Figure 4.11 shows the order of each RTL transformation, including those that we introduced:

- 1. Tailcall optimization
- Inlining, before our superblock optimizations. Indeed, our instruction duplication oracles
 make the decision of duplicating based on the number of instructions that would be
 duplicated. Inlining functions after that decision is made could invalidate it, because of the
 increase in instruction count.
- 3. Profiling insertion, then, annotating branches based on profiling information if they exist.
- 4. The CSE pass just before static prediction, to possibly improve the branch prediction heuristics.
- 5. The static branch prediction pass, which annotates the branches that were not annotated from profiling.
- 6. Loop peeling: duplicating one iteration of loops, with the prospect that the loop-invariant expressions will be later eliminated with CSE3.
- 7. Tail-duplication, to transform relevant traces into superblocks.
- 8. Loop Unrolling, to increase scheduling opportunities and also reduce branching penalties due to looping (see section 10.3.6 for more details on the impact of reducing branch penalties).
- 9. Constant Propagation and CSE for eliminating potential redundancies introduced by instruction duplication.
- 10. CSE3, for simplifying the loop-invariant expressions within the loop body, that were copied out of the loop via loop peeling. This achieves loop-invariant code motion [63].
- 11. Redundancy elimination
- 12. Loop rotation, to improve the later postpass scheduling.

Introducing Superblock Execution Semantics with RTLpath

Chapter 4 introduced what superblock scheduling is, how do we generate and modify superblocks, and the impact of these transformations on performance. We touched briefly some elements of correctness for superblock scheduling, though we did not dive into any formalism. In particular, we saw that load instructions must be turned into *speculative loads* when they are scheduled ahead of a side-exit.

In this chapter, we will study the first step in certifying superblock scheduling: introducing a semantics for executing a program with steps covering whole superblocks. I first introduce the RTL representation in more details, along with our modifications to model *speculative loads* in CompCert, as well as keeping track of branch prediction throughout RTL (section 5.1). Then we define a new IR based on RTL, named RTLpath, which acts as an anchor point to perform the prepass scheduling (from RTLpath to RTLpath) discussed in the later chapter 7. After describing its formal semantics, I detail a bisimulation between RTL and RTLpath, which allows us to go back and forth from RTL to RTLpath (section 5.2). Finally, I detail its code generation, which involves selecting the superblock and computing their liveness information by an oracle, then verifying the oracle result for correctness (section 5.3).

The work of designing RTLpath has been mostly done by S. Boulmé, with D. Monniaux implementing support for *speculative loads* in RTL, and me filling the gaps: finishing the RTL to RTLpath proof stub, supporting *speculative loads* in RTLpath, and then implementing the superblock selection (the RTLpathLivegen oracle, described later).

5.1 Modifying CompCert RTL representation

RTL (Register Transfer Language) is the IR right after CminorSel, featuring 3-address code. Its control-flow graph structure, combined with its unbounded number of registers, makes it a

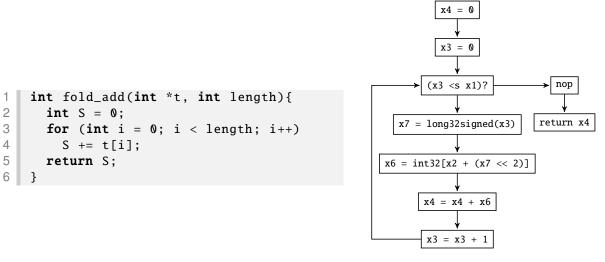


Figure 5.1.: C code, and RTL representation of fold_add as a control-flow graph

natural choice to implement optimizations such as constant propagation, deadcode elimination, common subexpression elimination.

5.1.1 Overview of RTL

Much like the other IRs of CompCert, a RTL program is composed of several functions. In RTL, each instruction is identified by a positive integer, called a *node*. Each RTL instruction has its successor nodes encoded within the syntax. In order to retrieve the instruction pointed by a node, there is a mapping from the nodes to the (syntactic) instructions. This mapping is called a RTL *code*. In addition to that, the *entrypoint* is the first node of the function to be executed.

A RTL function is then made of: a signature, a list of parameters (input registers), a stack size, some code, and an entrypoint.

Control-flow graph structure

RTL implements a control-flow graph structure, where each node is made of one single instruction, and there is an edge from i_1 to i_2 if the positive integer identifying i_2 is among the successors of i_1 .

Figure 5.1 shows an RTL function code with a single loop, represented as such a graph.

```
9 \mapsto Iop
             (0intconst 0) [] x4 8
8 → Iop
             (0intconst 0) [] x3 7
7 → Icond
             (Ccomp Clt [x3; x1]) 6 4
6 \mapsto Iop
             Ocast32signed [x3] x7 5
5 \mapsto Iload
             Mint32 (Aindexed2XS 2) [x2; x7] x6 4
4 → Iop
             Oadd [x4; x6] x4 3
3 \mapsto Iop
             (Oaddimm 1) [x3] x3 7
2 \mapsto Inop
1 \mapsto Ireturn x4
```

Figure 5.2.: The RTL code of **fold_add**, represented syntactically. The instruction nodes are represented in red. The entrypoint of that code is 9. For clarity, I represent registers as "x" followed by their number – though in the actual syntax, registers are just positive integers.

Syntax

The RTL representation is composed of 10 instructions:

- Inop pc': this is a no-operation instruction. It can be generated by some optimizations like common subexpression elimination. ¹ Branches to the instruction indicated by pc'.
- Iop op lr r pc': performs the operation op on the list of source registers *lr*, writes the result in the destination register r, branches to pc'.
- Iload chunk addr lr r pc': loads a chunk quantity, from the address computed by the addressing mode addr and a list of registers lr, writes to the destination register r, branches to pc'.
- Istore chunk addr lr r pc': same as Iload, but stores the register r to memory instead of loading it.
- Icall sig ros lr r pc': calls a function of signature sig, pointed by ros which represents either a register or a symbol. The list of arguments is lr, the destination register for the returned value is r. Finally, after the call, branches to pc'.
- Itailcall sig ros lr: same as Icall, but for a *tailcall*.
- Ibuiltin ef args dest pc': calls the external function ef, with arguments args. The return value is stored in dest, then it branches to pc'.
- Icond cond lr ifso ifnot: evaluates the condition cond on the values of lr. If the condition evaluation is true, branches to ifso. Otherwise, it branches to ifnot.
- Ijumptable r lpc: selects a value of the list lpc based on the register value r, then branches to this selected value.
- Ireturn or: ends the execution of the function, returning the value given by the optional register or. If or is None, then it returns an undefined value Vundef. ²

¹In terms of formal correctness, it is much easier to replace a useless expression by a Inop rather than removing an entire node from the control-flow graph. The Inop can then be removed by a dedicated pass.

²This is the case for a void function.

Figure 5.2 shows the same example as 5.1, but not pretty-printed (the actual syntax of each instruction is shown).

Compared to an Asm language, RTL has much fewer instructions. Much like Mach, it abstracts most of the architecture-specifics parts, which allows for simpler proofs (less cases to handle).

Semantics

The semantics of RTL are a lot like Mach semantics, but for two major differences. First, RTL fetches the next instruction differently than Mach: the PC value (equal to the next instruction node) is stored within a State, and remains internal to a function execution. Second, there is no variable stored on the stack. ³ Each variable lies in a register. Since there can be infinitely many registers, it is not possible to run out of registers: RTL optimizations are free to introduce any amount of fresh registers.

A RTL state is either:

- State stack f sp pc rs m: we are inside the function f, the callstack is stack, the stack pointer is sp, 4 and we are about to execute the instruction whose node is pc with register state rs and memory state m.
- Callstate stack f args m: we are about to call f with arguments args, the callstack is stack, and the memory state m.
- Returnstate stack v m: the callstack is stack, the memory state is m, and we are returning the value v from a function.

Figure 5.3 gives an overview of the *smallstep* relation defining the execution of a given RTL instruction.

Like Mach, the failure of an instruction execution (such as a division by zero) is encoded by an absence of transition in the *smallstep* relation. Listing 5.1 gives the Coq code defining the execution of Iop and Iload. For Iop, if the operation evaluations fails, then eval_operation will return None, thus the predicate required by the constructor exec_Iop will not be fullfilled. As for Iload, this instruction can fail in two distinct parts: the computing of the address might fail (if eval_addressing returns None), or the computed address might lie in an invalid memory region (if Mem.loadv returns None).

```
Inductive step: state → trace → state → Prop :=
(*...*)
| exec_Iload:
```

³The stacksize, which is part of a RTL function, is only there to be used by the later passes.

⁴Here, this is not the same stack pointer as in Asm. This is just the identifier of the memory block (the stack) allocated for the function.

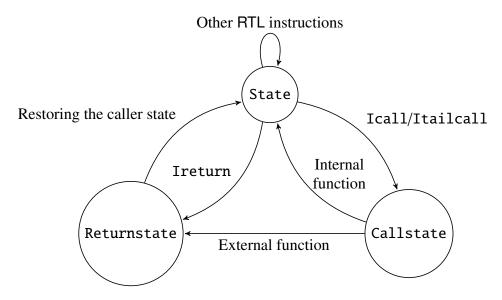


Figure 5.3.: Execution steps between RTL states

```
∀ s f sp pc rs m chunk addr args dst pc' a v,
5
             (fn\_code f)!pc = Some(Iload chunk addr args dst pc') \rightarrow
6
             eval_addressing ge sp addr rs##args = Some a \rightarrow
 7
             Mem.loadv chunk m a = Some v \rightarrow
8
             step (State s f sp pc rs m)
9
               E0 (State s f sp pc' (rs#dst \leftarrow v) m)
10
        | exec_Iop:
11
             ∀ s f sp pc rs m op args res pc' v,
12
             (fn\_code f)!pc = Some(Iop op args res pc') \rightarrow
13
             eval_operation ge sp op rs##args m = Some v \rightarrow
14
             step (State s f sp pc rs m)
15
               E0 (State s f sp pc' (rs#res \leftarrow v) m)
```

Listing 5.1.: Execution of Iop and Iload in RTL

5.1.2 Modeling speculative loads in RTL

As was mentioned in chapter 4, some architectures like the Kalray core support *speculative loads* — that is, load instructions that do not fail in the case of invalid addressing. ⁵

Modeling such instructions require us to add a new field to the syntax of Iload, to be able to distinguish between the speculative and non-speculative variants of the instruction. We thus included a trap field in the Iload syntax (listing 5.2).

```
1 Inductive trapping_mode : Type := TRAP | NOTRAP
```

⁵There exists older architectures with more general *speculative execution* for most of the integer operations, such as in Lee et al. [49]. Speculative execution as described in that paper is only relevant for in-order architectures supporting those, since modern out-of-order architectures support speculative memory accesses right away, without the need to change the instruction into a speculative variant.

```
2 Inductive instruction: Type :=
3    (* ... *)
4    | Iload: trapping_mode → memory_chunk → addressing
5     → list reg → reg → node → instruction
```

Listing 5.2.: Introducing trapping modes in Iload

Then, we added semantics to the execution of a non-trapping load with two new relations: exec_Iload_notrap1 and exec_Iload_notrap2 (listing 5.3).

```
1
     Inductive step: state → trace → state → Prop :=
2
       (* ... *)
3
       | exec_Iload_notrap1:
4
            ∀ s f sp pc rs m chunk addr args dst pc',
 5
            (fn_code f)!pc = Some(Iload NOTRAP chunk addr args dst pc') \rightarrow
6
            eval_addressing ge sp addr rs##args = None \rightarrow
7
           step (State s f sp pc rs m)
8
             E0 (State s f sp pc' (rs#dst ← Vundef) m)
9
      | exec_Iload_notrap2:
10
           \forall s f sp pc rs m chunk addr args dst pc'a,
11
            (fn\_code f)!pc = Some(Iload NOTRAP chunk addr args dst pc') \rightarrow
12
           eval_addressing ge sp addr rs##args = Some a \rightarrow
13
           Mem.loadv chunk m a = None→
            step (State s f sp pc rs m)
14
15
              E0 (State s f sp pc' (rs#dst ← Vundef) m)
```

Listing 5.3.: Trapping load semantics in RTL

Informally, if eval_addressing evaluates to None, then we write a Vundef value in the destination register. This is different from the concrete processor execution, which returns 0 when a speculative load reaches an invalid address. However, replacing this Vundef value by 0 would be an incorrect specification since a load instruction in RTL might fail more than its concrete counterpart on the processor. A typical example would be an out-of-bounds access on the stack. Since the function stacks are not contiguous in the memory model of CompCert, such a load instruction would fail in RTL (the load would return 0), whereas on the concrete processor, it would succeed and return the value in the given address. Using Vundef instead of 0 ensures that the result will never be read in the remaining of the execution (in CompCert semantics, an instruction reading Vundef automatically fails).

We do the same if eval_addressing returned a value, but Mem.loadv returned None. In practice though, only the latter case is possible, because it is guaranteed within the Mach to Asm code generation that eval_addressing never fails (but we must still take it into account in our semantics).

Correctness of making an Iload speculative

Compared to a non-speculative load, the only change in the semantics is in the case of failure: a speculative load does not fail, while a regular load does. Since CompCert proof of correctness only holds for programs that do not fail, we can deduce that transforming a non-speculative Iload into a speculative Iload is correct: nothing changes in terms of semantics (if the step relation from the code before transformation was constructed with an exec_Iload, then we can apply this same exec_Iload on the speculative version of the Iload).

It is thus possible to implement a dedicated pass like listing 5.4, which would make each Iload speculative, and prove it correct by a lockstep simulation.

```
Definition transf_instr (pc: node) (instr: instruction) :=
   match instr with
   | Iload trap chunk addr args dst s ⇒ Iload NOTRAP chunk addr args dst s
   | _ ⇒ instr
   end
```

Listing 5.4.: Turning each Iload into a non-trapping version

However, in terms of application development, although correct, this might not be desirable. Application-level bugs would indeed be much harder to find, since any load could potentially fail silently, producing wrong values instead of signaling a trap to the underlying operating system.

In practice, in our superblock scheduling (described in chapter 7) we only make our loads speculative when necessary — that is, when they move ahead of a side-exit, as described informally in section 4.3.1.

5.1.3 Modeling branch prediction

Branch prediction information is used by our newly introduced passes that we introduced in chapter 4, and by our modified version of Linearize, which uses this information to retrieve the superblock structure and emit a Linear code in which each identified superblock is contiguous in memory.

This branch prediction is stored through an additional blank field in each Icond instruction (listing 5.5).

```
Inductive instruction: Type :=
(*...*)
Icond: condition → list reg → node → node
→ option bool → instruction
```

Listing 5.5.: Definition of Icond in our version of RTL

This new field is ignored by all the certified passes. It is only used by the external uncertified oracles to guide their heuristics. For these oracles, this option bool field has the following meaning based on its value:

- None indicates a lack of prediction for the given Icond. Either the prediction pass has not yet been performed, or the heuristics were unable to devise a preferred branch.
- Some true indicates that the *if so* branch is privileged. According to the heuristics, the program should spend more time diving in *if so* than in *if not*.
- Vice-versa, Some false indicates that the *if not* branch is privileged.

Since we need to preserve this information until Linear, we did the same change for LTL.

This choice is motivated by the previous section 4.1.2 — there are other possible alternatives. In the future, changing that data format would only imply little effort on proof maintenance. Most of the effort would be on adapting the heuristics to cope with the change.

5.2 Representing superblocks as execution paths in RTLpath

To reason about superblock scheduling, we first need to provide semantics for executing superblocks. This is, in a way, similar to the work we did in chapter 3 for the Machblock representation: we would like an RTL-like IR within which we can execute whole superblocks. However, compared to Mach, we have several differences to cope with:

- Mach code is linear: executing Mach code is simply executing a list of instructions, and possibly re-loading the instruction list by jumping to Mlabel instructions. RTL code, on the other hand, follows a control-flow graph structure in which the next instruction to execute must be computed from the current instruction execution.
- In Machblock we were very interested in keeping that basicblock structure, to translate it to Asmblock (assembly code generation), and then to AsmVLIW (scheduling + formation of bundles). For our prepass optimization, we need to output a RTL program (empty of any superblock structure) for the later register allocation pass to happen. This implies that we would rather make the transition back to RTL as painless as possible.
- We intend to give semantics for a structure more complex than a basicblock. In particular, for the later certification of superblock scheduling, we require to access liveness information for each side exit of a superblock.

We present in this section RTLpath, an IR dedicated to outlining the superblock structure from the input RTL program. This IR acts as a supplementary semantics augmenting the RTL program — translating a RTL program to RTLpath does not involve any change within the RTL syntax, so the RTL program (and semantics) can be retrieved very easily from RTLpath.

5.2.1 RTLpath syntax and informal semantics

Schedulable and non-schedulable instructions

In Machblock, we split the Mach instructions into two groups: those that alter the control-flow, and those that do not. For RTLpath, we also split the RTL instructions in two groups:

- Those that have a preferred successor, and which we would be able to reorder. Inop, Iop, Iload, Istore belong naturally to that group: they have only one possible successor, and do not generate any trace.
- The rest, who will always be sitting at the end of a superblock: Icall, Itailcall, Ibuiltin, Ireturn, Ijumptable.

The case of Icond requires a bit of discussion. We are able to devise a preferred successor on Icond in most cases, but not always. If we lack branch prediction, or if the branch prediction fails to deliver a verdict, then there is no way to tell which Icond branch to prefer. We could be looking at the option bool field of Icond, and decide based on the value of that field whether a given Icond belongs inside a superblock (is schedulable), or should remain at the end. However, that would make the semantics and proofs of RTLpath harder. So we chose that Icond always has one privileged successor, the fallthrough case (ifnot field). ⁶ To ensure that this is actually the case, we do two things:

- Before RTLpath, during the branch prediction RTL pass, we invert the conditions of the Icond that would have their ifso branch as privileged. This makes them privilege ifnot instead.
- In order to respect the None prediction (no branch is preferred), we will rely on the RTLpath and scheduler oracles to ensure these Icond are placed at the end of a superblock, and remain that way.

As for those that we excluded: since Itailcall and Ireturn finish the execution of a function, it would break the semantic to reorder them. Icall and Ibuiltin only have one successor, but since their semantic involve going out of the current function, it would be complex to include

⁶This choice is completely arbitrary. One could argue that choosing ifnot instead of ifso results in a better performance, since executing the fallthrough case of a conditional branch induces 0 penalty (compared to 2 cycles otherwise) — but such issue would be corrected by the later Linearize pass anyway.

it in our reordering, for unclear benefits. Finally, Ijumptable is more complex than Icond to handle, since there are more than one possible side-exit. Also, we found its presence to be very rare in our benchmarks, the associated tail-duplication could involve duplicating much more code than if it was an Icond, and Ijumptable are always translated into unconditional jumps (1 cycle penalty). The benefit of including it in our scheduling is unclear, and would require potentially more cumbersome proofs, so we decided not to include it.

Paths and pathmaps

The notion of *path* that we will present here is very close to the notion of *trace* in the compiler litterature; but since CompCert already has a notion of trace completely unrelated ⁷, to prevent confusion, we name them *paths*. An *execution path* is a group of instructions with the following semantics:

- Each path has an entry node, from which the path execution starts.
- During the path execution, it is possible to step out of the path if an *early exit* instruction is met. Here, the only early exit instructions are Icond.
- The number of instructions to execute for a path is bounded, and annotated to the entry node. If no early exit is triggered, the path execution stops as soon as this number is reached.

The information of the maximum number of instructions to execute, along with liveness information, is stored in a path_info data structure. We define a *pathmap* as a partial mapping from RTL nodes to such data structure: path entries are those for which the mapping has a path_info. Listing 5.6 shows our code listing defining these notions. One tiny detail should be noted: we took the convention to keep track of the "number of instructions to execute before the last instruction", so a value psize=0 indicates there is only one instruction to execute in the path.

```
Record path_info := {
    psize: nat; (* number minus 1 of instructions in the path *)
    input_regs: Regset.t;
    output_regs: Regset.t; (* not yet used by proofs *)
}

Definition path_map: Type := PTree.t path_info

Definition path_entry (pm: path_map) (n: node): Prop := pm!n <> None
```

⁷In CompCert, a trace is a (possibly infinite) sequence of observational events (*e.g.* external function calls) emitted by the execution of a given piece of code.

⁸On the contrary of psize, the liveness information has no impact on the actual RTLpath semantics. It is, however, verified for correctness (but not for completeness).

Listing 5.6.: Definitions of path_info, path_map and path_entry. psize details the number of instructions to execute in the path. input_regs are the live registers at the start of the path. output_regs is a field used by the scheduler oracle, without any impact on the proofs.

A RTLpath function is a RTL function, augmented with a pathmap. To be able to execute a whole function with such a pathmap, we need to have certain guarantees:

- The entrypoint of the function must be a path entry.
- Each successor of a given path must be a path entry.

If these two requirements are not met, the semantics will not be able to derive an execution (the execution will be invalid). These requirements are defined as predicates of well-formedness in listing 5.7: a path is *wellformed* if each of its successor is a path entry; a pathmap is *wellformed* if each path is *wellformed*; a RTLpath function is *wellformed* if its entrypoint is a path entry, and its pathmap is *wellformed*.

```
Inductive wellformed_path (c:code) (pm: path_map): nat \rightarrow node \rightarrow Prop :=
 2
        | wf_last_node i pc:
 3
             c!pc = Some i \rightarrow
 4
             (\forall n, List.In n (successors\_instr i) \rightarrow path\_entry pm n) \rightarrow
 5
             wellformed_path c pm 0 pc
 6
        | wf_internal_node path i pc pc':
 7
             c!pc = Some i \rightarrow
 8
             default\_succ i = Some pc' \rightarrow
 9
             (\forall n, early_exit i = Some n \rightarrow path_entry pm n) \rightarrow
10
             wellformed_path c pm path pc' \rightarrow
11
             wellformed_path c pm (S path) pc
12
13
      (* all paths defined from the path_map are wellformed *)
14
      Definition wellformed_path_map (c:code) (pm: path_map): Prop :=
15
        \forall n path, pm!n = Some path \rightarrow wellformed_path c pm path.(psize) n
16
17
     Record function : Type :=
18
      { fn_RTL:> RTL.function;
19
         fn_path: path_map;
20
         (* condition 1 below: the entry-point of the code is an entry-point of a path *)
21
         fn_entry_point_wf: path_entry fn_path fn_RTL.(fn_entrypoint);
22
         (* condition 2 below: the path_map is well-formed *)
23
         fn_path_wf: wellformed_path_map fn_RTL.(fn_code) fn_path
24
```

Listing 5.7.: Definitions of well-formedness for paths, pathmaps and functions.

Figure 5.4 shows three different examples of pathmaps for the example that was introduced in figure 5.1. The pathmap A is not well-formed: 7 is not a path entry, so the unconditional jump from 3 to 7 would result in an invalid execution. The pathmap B is well-formed, however the path from 9 to 3 does not constitute a superblock, since there is a side-entrance at instruction 7.

The pathmap C is well-formed, and each path forms a superblock: this is the kind of pathmap that we desire. ⁹

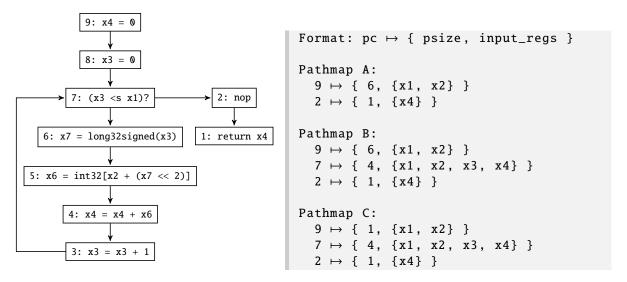


Figure 5.4.: Three examples of pathmaps for the RTL code on the left. We omit the output_regs field. Pathmap A would lead to an incorrect execution. Pathmap B is correct, but undesirable because the path starting at 9 is not a superblock. Pathmap C is correct, and desirable.

5.2.2 RTLpath formal semantics

A RTLpath state is the exact same as a RTL state, with one exception: instead of having RTL functions in the stackframes and other fields, we have RTLpath functions. As such, a RTLpath state is either a State (an execution inside the current function), a Returnstate (returning from a function), or a Callstate (about to call a function).

The only significant change is in the step semantics. Instead of executing a single RTL instruction, we execute an entire path (listing 5.8): the pc value of a RTLpath state has to point to a path entry, from which the path information path is retrieved.

```
Inductive step ge pge: state → trace → state → Prop :=
| exec_path path stack f sp rs m pc t s:
(fn_path f)!pc = Some path →
path_step ge pge path.(psize) stack f sp rs m pc t s →
step ge pge (State stack f sp pc rs m) t s
```

Listing 5.8.: Executing an entire path in one step

⁹In terms of formal correctness, only the A case will be ruled out by our verifier. The B case is a valid choice in terms of RTLpath semantics. However, the B case would later fail during the superblock scheduling verification. More details in chapter 7.

To model the path execution, we introduce a notion of internal state (listing 5.9). This state has four components: icontinue dictates whether a side-exit is taken (if a conditional branch got triggered), ipc points to the next instruction to execute within the path, irs and imem are the internal states of the registers and memory.

```
Record istate := mk_istate { icontinue: bool; ipc: node; irs: regset; imem: mem }
```

Listing 5.9.: RTLpath internal state

This internal state is transformed by the istep function, which evaluates the new irs, imem and ipc, as well as updating icontinue. I detail two examples in listing 5.10. For most of the schedulable instructions (like Iop), istep is mostly just a computational variant of the RTL (single) step semantics. For Icond, it requires in addition to set icontinue according to the condition evaluation.

```
Definition istep (ge: RTL.genv) (i: instruction) (sp: val) (rs: regset) (m: mem):
 2
            option istate ≔
 3
         match i with
         | Iop op args res pc' \Rightarrow
 5
               \texttt{SOME} \ v \leftarrow \texttt{eval\_operation} \ \texttt{ge} \ \texttt{sp} \ \texttt{op} \ \texttt{rs\#args} \ \texttt{m} \ \texttt{IN}
 6
               Some (mk_istate true pc' (rs#res \leftarrow v) m)
 7
         \mid Icond cond args ifso ifnot \_\Rightarrow
 8
               SOME b \leftarrow eval\_condition cond rs\#args m IN
 9
               Some (mk_istate (negb b) (if b then ifso else ifnot) rs m)
10
          | (* ... *)
11
         |  |  |  |  |  None
12
         end
```

Listing 5.10.: Internal execution of Iop and Iload

With istep defined, we can then code the isteps function which executes successively each instruction until there is no more instruction to execute but one (we reached the bounded end of the path), or until icontinue equals false. This isteps is guided by path, a natural number defining how many instructions to execute at maximum within the path. If path is 0, nothing is executed and isteps returns the current state.

```
1
       Fixpoint isteps ge (path:nat) (f: function) sp rs m pc: option istate :=
 2
          match path with
 3
          \mid 0 \Rightarrow Some (mk_istate true pc rs m)
          | S p \Rightarrow
 5
             SOME i \leftarrow (fn\_code \ f)!pc \ IN
 6
             \texttt{SOME} \ \texttt{st} \leftarrow \texttt{istep} \ \texttt{ge} \ \texttt{i} \ \texttt{sp} \ \texttt{rs} \ \texttt{m} \ \texttt{IN}
 7
             if (icontinue st) then
 8
                isteps ge p f sp (irs st) (imem st) (ipc st)
 9
             else
10
                Some st
11
```

Listing 5.11.: Executing several instructions along a path with isteps

The last instruction is executed by a path_last_step relation, which mimics the step relation from RTL. The path_step relation (listing 5.12) bridges it all together: either icontinue is false, in which case there is no more instruction to execute, or icontinue is true, implying that we execute the final instruction with path_last_step.

```
1
     Inductive path_step ge pge (path:nat) stack f sp rs m pc: trace \rightarrow state \rightarrow Prop :=
2
       | exec_early_exit st:
3
          isteps ge path f sp rs m pc = Some st \rightarrow
4
          (icontinue st) = false \rightarrow
 5
           path_step ge pge path stack f sp rs m pc E0
6
             (State stack f sp (ipc st) (irs st) (imem st))
7
      | exec_normal_exit st t s:
8
          isteps ge path f sp rs m pc = Some st \rightarrow
9
          (icontinue st) = true \rightarrow
10
           path_last_step ge pge stack f sp (ipc st) (irs st) (imem st) t s \rightarrow
11
           path_step ge pge path stack f sp rs m pc t s
```

Listing 5.12.: Executing an entire path

Figure 5.5 gives a summary of these semantics. The starting point is a RTLpath State, from which we capture rs, m and pc into an internal state. We then distinguish two cases: either we execute the whole path, in which case we get an internal state (ipc_1 , irs_1 , im_1 , true) and we perform one final step with path_last_step to get the state s'_1 (which can be a Callstate, a Returnstate, or just a State). Or, after n instructions, the execution reaches a conditional branch whose condition evaluates to true, in which case icontinue is set to false, and the final state is constructed with ipc_2 , irs_2 and im_2 .

5.2.3 Bisimulation between RTLpath and RTL semantics

To plug RTLpath in the compilation flow of CompCert, we have to prove a bisimulation between RTL and RTLpath semantics: this will make it possible and certified to use RTLpath instead of RTL, and vice-versa. This comes in two steps: proving a simulation from RTLpath to RTL, then doing the same for RTL to RTLpath.

Simulation from RTLpath to RTL

Proving that we can go back to RTL semantics from RTLpath is the easiest part of the bisimulation. The gist of the proof lies in exhibiting that all internal transitions from RTLpath can be seen as RTL transitions.

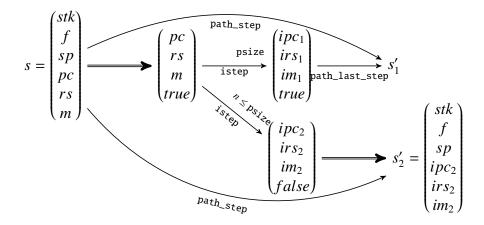


Figure 5.5.: Executing a path from s (a RTLpath.State). Two possible executions are shown. One executes an entire path by computing istep psize times, finishing by a path_last_step which gives the final state s'_1 . The other computes istep only n times, then reaches a point where icontinue = false: it exits the path and returns a State s'_2 . The entire execution is a path_step.

To begin, we prove by case analysis that the istep function simulates the RTL.step relation.

Listing 5.13.: Simulation from istep to RTL.step

Then, by induction, we can prove a simulation between isteps and RTL.step. In the most general case, this simulation is of the *star* type, since isteps can be run with a path=0 argument. However, if an early exit is taken (if icontinue of the final internal state is false), then we can prove that this is a *plus* (instead of a *star*) simulation, since we would have executed at least one conditional branch instruction. Similarly, we can prove a step simulation between path_last_step and RTL.step.

Using the above, we can prove a plus simulation from RTLpath to RTL by a case analysis on path_step: either the path_step was constructed with the exec_early_exit constructor, then we have directly a plus simulation — or it was constructed with the exec_normal_exit constructor, we then have a star simulation for isteps combined with a step simulation for path_last_step, so *in fine* a plus simulation.

Simulation from RTL to RTLpath

This part is more complex. On the one hand, we have an instruction-per-instruction execution semantics. On the other hand, we execute a whole path at each step. Proving the simulation requires then to introduce a notion of *stuttering*, much like the Mach to Machblock proof: we must have a match_states relation which allows for the RTL program to advance one step, while the RTLpath stutters (but with progression in the internal state).

We call this new relation match_inst_states_goal, with the following definition:

```
Inductive match_inst_states_goal (idx: nat) (s1:RTL.state): RTLpath.state → Prop :=

| State_match path stack f sp pc rs m is2:

(fn_path f)!pc = Some path →

(idx ≤ path.(psize))%nat →

isteps ge (path.(psize)-idx) f sp rs m pc = Some is2 →

s1 = State stack f sp is2.(ipc) is2.(irs) is2.(imem) →

match_inst_states_goal idx s1 (State stack f sp pc rs m)
```

Listing 5.14.: match_inst_states_goal definition

Informally, match_inst_states_goal idx s1 s2 holds if a certain number of instructions have already been executed in the path indicated by the pc from s2, there remains idx instructions to execute before the syntactic end of the path, and the current internal execution state is2 matches structurally with the RTL state s1. I give a more graphical representation of this relation in figure 5.6: several states from RTL match to the same state from RTLpath, but with a different idx value. Once this value reaches 0, or when an early-exit is taken, the RTLpath state changes with a path_step.

The actual match_step relation combines match_inst_states_goal with a more classical structural equality for Callstates and Returnstates. wf_stackframe is a necessary predicate to ensure that pc points to a valid path after exiting another.

```
Definition is_inst (s: RTL.state): bool :=

match s with RTL.State stack f sp pc rs m ⇒ true | _ ⇒ false end

Definition match_inst_states (idx: nat) (s1:RTL.state) (s2:state): Prop :=

if is_inst s1 then match_inst_states_goal idx s1 s2 else s1 = state_RTL s2

Definition match_states (idx: nat) (s1:RTL.state) (s2:state): Prop :=

match_inst_states idx s1 s2 ∧ wf_stackframe (stack_of s2)
```

Listing 5.15.: match_states definition for RTL to RTLpath simulation

Proving the forward simulation from RTL to RTLpath relies then on a case analysis based on the initial RTL transition. The possible cases are the following (referring to figure 5.6 for illustration):

- 1. Either the RTL step corresponds to a RTLpath stuttering within a path. This is the case of the olive transition from the left subfigure, from S_{11} to S_{12} . We have then a *local stuttering* with idx as decreasing measure.
- 2. Or, the RTL step corresponds to the last instruction of a given path. This is the case of the red transition from the left subfigure, from S_{1n} to S'_1 . We have then a *local lockstep*, with the transition from S_2 to S'_2 .
- 3. Finally, the RTL step could be right after an early exit was taken. We have a match_inst_states_goal (n-i) between S_{1n} and S_2 , and we also know that icontinue from s_{1i} is false by case analysis (if it was true, we would be in either case 1 or case 2). We can then construct a path_step from S_2 to S'_2 . To analyze what happens next, we perform a case analysis on the length of the new path, n':
 - Either n' = 0 (not shown in the figure) in which case we get one additional path_step (the RTL step actually corresponds to the one and only instruction from the new path). In total, we have then two RTLpath transitions.
 - Or n' > 0 (case shown in the figure), in which case we have a stuttering after the RTLpath transition.

In both cases, we have a *local plus simulation*.

We were able to construct in Coq a forward simulation with the combination of these three possible cases, which certifies the use of RTLpath semantics instead of RTL.

5.3 Generating RTLpath paths from RTL

Now that we have a semantic for executing paths, and two forward simulations between RTL and RTLpath, the only missing piece for a complete RTL to RTLpath pass is the generation of the pathmap.

This pathmap is generated by an oracle, described in subsection 5.3.1.

Then, its result is verified for two purposes:

- 1. The pathmap has to satisfy the well-foundedness predicate. In other words, the pathmap must have a valid entry for the RTL entrypoint, and each successor of each path must be valid entries. This is necessary to prove the RTL to RTLpath forward simulation from the previous section. This verification is described in subsection 5.3.2.
- 2. Even though our forward simulation does not involve any property about the correctness of the liveness information provided in our path_info structure, it is required later on for the superblock scheduling correctness. So we include within the pass a liveness verificator,

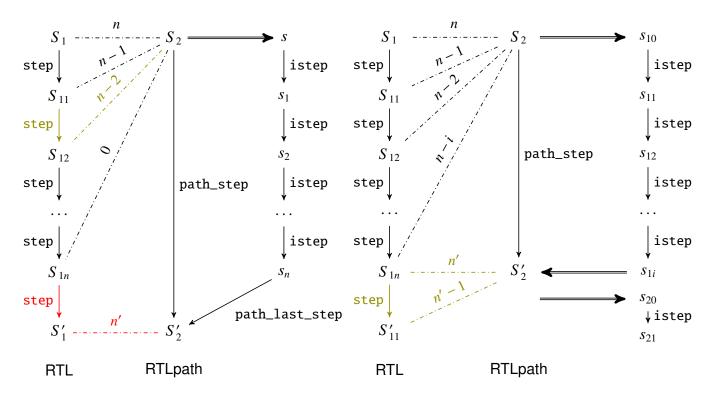


Figure 5.6.: Bridging RTL and RTLpath execution. The left figure shows an execution through a whole path, the right figure shows an execution with the path ending before the end because of an early exit. The red transition outlines the RTL execution of the last instruction from the path; the olive transitions outline RTL executions corresponding to RTLpath stutterings. Dotted edges correspond to match_inst_states_goal idx with idx value displayed on top of the edge.

which checks that the liveness information returned by the oracle is correct. This is described in subsection 5.3.2.

5.3.1 RTLpath generation oracle

Our oracle performs two main tasks: identifying the superblocks to schedule, and generating liveness information for each superblock.

Superblock identification

As was described in chapter 4, superblocks are contiguous units of code with only one entrance. In the RTL to RTLpath pass, we suppose that all the pre-scheduling superblock-related passes (tail-duplication, loop unrolling) have already been done. We then just have to identify the superblocks to schedule: given a RTL control-flow graph (CFG) and its entrypoint, we want to partition that graph into paths that are superblocks.

We want those superblocks to be non-overlapping. Indeed, if we were to create a pathmap containing overlapping superblocks, the scheduling pass could fail. Let's imagine a superblock containing the instructions [i1; i2] and the other containing [i1; i2; i3]. One possible transformation would be to schedule the first into [i1; i2] and the second into [i3; i1; i2]. The latter superblock scheduling would be correct; however the former would not be correct, since a new instruction would have been added to the superblock.

To identify the superblocks, we can start by identifying the *join points* among RTL nodes. The join points are the nodes in the CFG that have more than one predecessors. These cannot be included in a superblock (unless they are the first instruction of the superblock) because that would create side-entrances.

We compute the join points by a graph DFS (Depth-First Search) traversal starting from the entrypoint. The core idea of this traversal is to memorize whether a node was visited or not. If, during a branch traversal, we come accross a node that was already visited, then that node is a join point, and we stop the search for that branch. Algorithm 1 shows pseudo-code for computing them. It should be noted that this algorithm is the same as the one used in mainstream CompCert for the Linearize pass. 10

Once the join points are identified, we start from the entrypoint and grow a superblock from there, with the following rules:

¹⁰Computing join points is of interest for figuring out a good linearized layout, that is, one that minimizes the impact of jump penalties. More details can be found in section 8.3.

Algorithm 1. Identifying join points in RTL code

```
1: function GET_JOIN_POINTS(code, entry)
         visited \leftarrow { all \mapsto false }
 2:
 3:
         join\_points \leftarrow \{ all \mapsto false \}
         function TRAVERSE(pc)
 4:
              if visited[pc] then
 5:
                   join_points[pc] := true
 6:
 7:
              else
                   visited[pc] := true
 8:
                   traverse_all(successors(code[pc]))
 9:
         function Traverse_all(1)
10:
              match 1 with
11:
                   case []
12:
13:
                        pass
14:
                   case pc :: 1
15:
                        traverse(pc)
                        traverse_all(l)
16:
17:
         traverse(entry)
         return join_points
18:
```

- If we encounter an Icond with a privileged direction, we continue growing in that direction, and keep track of the early-exit. Encountering an unpredicted Icond results in stopping the superblock growth.
- If the next instruction is a join point, we stop the growth.
- If we encounter an instruction that does not have exactly one successor, and which is not an Icond, we include that instruction in the superblock and stop the growth.

Once we are done growing a superblock, we grow another one from one of its successor nodes (either an early-exit or a successor from the last instruction). We also keep track of which node was visited in order to prevent infinite loops from CFG cycles.

I write below our algorithm for identifying superblocks. This algorithm does not update the liveness information — this is done later.

Computing liveness information

Given a set of instructions to execute, it is possible to compute the set of registers whose initial values may alter the execution of a RTL code. For example, in the code below:

```
1 1: x0 = x1 + x2;
2 2: x3 = x1 * x0;
3 3: ret x3
```

Algorithm 2. Identifying superblocks in RTL code

```
1: function GET_PATH_MAP(code, entry, join_points)
         visited \leftarrow { all \mapsto false }
         pathmap \leftarrow \{\}
 3:
         to\_visit \leftarrow \{ entry \}
 4:
         while to_visit \neq \emptyset do
 5:
 6:
              e \leftarrow to\_visit.pop()
 7:
              if visited[e] then
 8:
                    continue
 9:
              visited[e] := true
              psize \leftarrow -1
10:
              pc \leftarrow e
11:
12:
              loop
13:
                    inst \leftarrow code[pc]
                    ps ← predicted_successor(inst)
14:
                    to_visit += non_predicted_successors(inst)
15:
16:
                    psize += 1
                    match ps with
17:
                         case None
18:
19:
                              break
20:
                         case Some s
                              if join_points[s] then
21:
22:
                                   break
23:
                              pc := s
                                                                                     ▶ The path is finished
              pathmap[e] := { psize = psize; input_regs = 0; output_regs = 0 }
24:
25:
         return pathmap
```

This set would be $\{x1, x2\}$: changing the initial value of x1 or x2 changes the value returned by the function. In compiler litterature, such an analysis is called *liveness analysis*.

This analysis is already done by the Liveness pass of CompCert but in a slightly different fashion. The Liveness module of CompCert assumes that the instructions that compute a useless result (a result that isn't live) will be later removed, so it ignores these instructions. In our case, we want a complete analysis, since we will not be removing any instruction.

Since the Liveness module of CompCert was not a perfect fit for us, and implementing a verifier was not that costly to do in terms of implementation and proof effort, we implemented our own, re-using most of the definitions of the Liveness module in our oracle.

For a branchless code, a liveness analysis can be done with a backward approach: given a set of live registers after a given instruction, it is possible to compute the set of live registers before that instruction. In the above example, the set of live registers would be: before 3, $\{x3\}$; before 2, $\{x1, x0\}$ (x3 is removed because it was assigned); before 1, $\{x1, x2\}$ (x0 is removed because it was computed — x2 is added since it's in the input operands of 1). The function which performs this operation of adding/removing registers is called the *transfer function*. We give below an example of transfer function for three instructions.

Algorithm 3. Transfer function for liveness analysis

```
1: function TRANSFER(code, pc, live_after)
       match code[pc] with
2:
3:
            case Inop _
4:
                 return live after
5:
            case Iop _ args res _
                 return live_after - { res } + args
6:
7:
            case Istore _ _ args src _
                 return live_after + { res } + args
8:
9:
```

For code containing branches but without loop, it is possible to perform this same backward analysis, except that when a *split* is encountered (a *join point* under the perspective of a backward analysis), the set of live registers before the split is $S_1 \cup S_2$ with S_1 and S_2 the respective sets of live registers before each branch of the split.

For code containing loops, we need to use a more refined algorithm such as Kildall (Kildall [44]). This algorithm allows, given a transfer function and a semi-lattice (a partially ordered set equipped with a least upper bound function), to propagate the analysis to graphs containing cycles. In our case, we manipulate sets of integers, they are partially ordered by the inclusion operator, and the least upper bound function is the union operator.

We run this analysis using CompCert Kildall module on the RTL code with our own transfer function — then, extracting the input_regs field of a given path is as simple as fetching the set of live registers before the entry of the path.

The output_regs field, used by the scheduling oracle, represents the registers that are live after the last instruction of the path. It is computed as the union of all the input_regs from the successors of the last instruction of the path. This field is used only by the scheduling oracle, and has no impact on correctness.

5.3.2 Pathmap verifiers

Since the pathmaps are generated by external oracles, their information needs to be verifier.

We have two distinct cases of pathmap generation: right before superblock scheduling (during the RTL to RTLpath pass), and within the superblock scheduling pass. In both cases, we need to verify the well-foundedness of the pathmap. The liveness information, however, only needs to be verified for the former: the superblock scheduling will rely on that information, so it must be correct; but this information is of no use once the scheduling is actually done.

The next subsections will detail how do we verify the well-foundedness and the liveness for the RTL to RTLpath pass.

Well-foundedness verification

The correctness of the RTL to RTLpath transformation partly resides in the guarantee that all paths are wellfounded; that is, each successor of a path must be a valid path entry.

First of all, to verify that a given path is well-founded, we go through each instruction of a path: if this instruction is an Icond, then we check that the exit branch is a path entry. Finally, we do the same for the successors of the final instruction of the path.

Once we have this verification in place, verifying the well-foundedness of our pathmap is done by checking that the RTL entrypoint is a valid path entry, and that each path from the pathmap is well-founded (listing 5.16). We have then formally proven the two theorems in listing 5.17, which ensure that our verifier is correct.

```
Definition function_checker (f: RTL.function) pm: bool :=
  pm!(f.(fn_entrypoint)) &&& list_path_checker f pm (PTree.elements pm)
```

Listing 5.16.: Well-foundedness verifier

```
Lemma function_checker_wellformed_path_map f pm:
function_checker f pm = true → wellformed_path_map f.(fn_code) pm

Lemma function_checker_path_entry f pm:
function_checker f pm = true → path_entry pm (f.(fn_entrypoint))
```

Listing 5.17.: Correctness theorems for the well-foundedness verifier

Liveness analysis verification

Since the liveness information is computed by an oracle, we also need to verify its correctness. This is done by taking the input_regs field of each path, and perform a simple forward analysis: go through each instruction of the path in order, check that each read register is in the set of currently live registers, and add the written register to the set of live registers. For each encountered side-exit, we also verify that the set of alive registers match the liveness information of the side-exit path. This is summarized by the below algorithm. ¹¹

Algorithm 4. Verifying liveness information

```
1: function PATH_CHECKER(path, entry, code)
 2:
         live ← path.input_regs
         psize ← path.psize
 3:
         pc \leftarrow entry
 4:
 5:
         loop
 6:
              inst \leftarrow code[pc]
              read \leftarrow read\_regs(inst)
 7:
              written \leftarrow written reg(inst)
 8:
 9:
              assert(read \subseteq live)
              live := live + written
10:
              if psize == 0 then
11:
12:
                   break
13:
              succ \leftarrow successors(inst)
              pc := preferred_successor(inst)
14:
              foreach side_exit \in succ \a {pc}
15:
                    assert(f.fn_path[side_exit].input_regs \subseteq live)
16:
17:
         return OK
```

This check is done during the RTL to RTLpath generation. To remember that it succeeded for the later scheduling pass, we define the following predicate:

```
Definition liveness_ok_function (f: function): Prop :=

V pc path, f.(fn_path)!pc = Some path \rightarrow path_checker f f.(fn_path) pc path = Some tt
```

¹¹The actual Coq implementation is a bit more complex since it is done through recursion and with several separate individual functions, but the gist of it is the same.

Finally, instead of just generating a RTLpath function, we generate a habitant from the set of RTLpath functions fulfilling the predicate liveness_ok_function $f' \wedge f'$.(fn_RTL) = fwhere f' is the new RTLpath function and f is the original RTL function.

```
Program Definition transf_function (f: RTL.function):
2
      { r: res function | \forall f', r = 0K f' \rightarrow liveness_ok_function f' \land f'.(fn_RTL) = f } :=
3
      let pm := build_path_map f in
4
      match function_checker f pm with
5
       | true \Rightarrow OK {| fn_RTL := f; fn_path := pm |}
6
       | false ⇒ Error(msg "RTLpathGen: function_checker failed")
```

5.3.3 RTLpath state equality modulo liveness

As was described briefly in section 4.3.1, scheduling an instruction above an early-exit requires to check whether the instruction writes in a register that is live in the other branch. In order to reason on that, we introduce a notion of state equality modulo liveness.

Given an live predicate stating whether a given register is live, eqlive_reg_live_rs1_rs2 holds if rs1 and rs2 have the same values for each live register.

```
Definition eqlive_reg (live: Regset.elt → Prop) (rs1 rs2: regset): Prop :=
  \forall r, (live r) \rightarrow rs1#r = rs2#r
```

Listing 5.18.: Definition of regset equality modulo liveness

We can then build a notion of state equality eqlive_states using this definition (I show only the definition for a RTLpath State). ext live is a shorthand for writing $r \mapsto r \in \text{live}$.

```
Inductive eqlive_states: state \rightarrow state \rightarrow Prop :=
2
      | eqlive_states_intro
3
           path st1 st2 f sp pc rs1 rs2 m
4
           (STACKS: list_∀2 eqlive_stackframes st1 st2)
5
           (LIVE: liveness_ok_function f)
6
           (PATH: f.(fn_path)!pc = Some path)
7
           (EQUIV: eqlive_reg (ext path.(input_regs)) rs1 rs2):
8
           eqlive_states (State st1 f sp pc rs1 m) (State st2 f sp pc rs2 m)
      (* ... *)
```

Listing 5.19.: State equality modulo liveness

This definition of regset equality is weaker than the complete regset equality we used until now. In particular, this definition alone may be too weak to be able to simulate a RTLpath program. Indeed, if we were to prove a step simulation from a given code to itself (a "self simulation"), and if for one particular path we had an incorrect input_regs field (say, one

where input_regs = \emptyset), then the eqlive_reg predicate would not be giving any meaningful information (since no register is in \emptyset , this predicate automatically holds). For instance, let's consider the code if (x1) then f() else g(), with f and g being two external functions. Without any information about what the value of x1 could possibly be, there is no way to know which of f or g will end up being executed: we might get a different trace, which prevents any forward simulation. In fact, if the liveness oracle had returned a correct result, then we would have had $x1 \in live$, which would have implied an equality rs1[x1] = rs2[x1], and thus the same trace.

So we need to combine this definition with the liveness verifier of subsection 5.3.2 to prove such a self simulation. I write below the self simulation that we prove:

```
Lemma path_step_eqlive path stk1 f sp rs1 m pc t s1 stk2 rs2:

path_step ge pge (psize path) stk1 f sp rs1 m pc t s1 →

list_∀2 eqlive_stackframes stk1 stk2 →

eqlive_reg (ext (input_regs path)) rs1 rs2 →

liveness_ok_function f →

(fn_path f) ! pc = Some path →

∃ s2, path_step ge pge (psize path) stk2 f sp rs2 m pc t s2 ∧ eqlive_states s1 s2
```

Listing 5.20.: Self simulation of RTLpath with state equality modulo liveness

The above lemma is a step simulation within the same function f, using eqlive_states. It states that if we execute a path with a given input_regs field (by a RTLpath step), and we have an initial state equality modulo input_regs, and that field was indeed verified by our liveness verifier, then we can execute that path and the next path will start with another eqlive_states binding the registers from its input_regs. Proving such a lemma involves a case analysis on which RTLpath step is taken (an early-exit or going through the entire path), as well as breaking it into smaller lemmas guaranteeing the same kind of property, but applied to each internal step function or relation (such as istep) instead.

The path_step_eqlive lemma will be very useful for proving our superblock scheduling in chapter 7.

Formal Verification of Code Duplication Transformations

Chapter 5 explained how the superblocks are selected, the superblock execution semantics, as well as an introduction to the RTL language. Chapter 4 introduced certain transformations done before superblock scheduling: tail-duplication and loop unrolling, but without giving much detail about those. These transformations feature a common point: they do not change the instructions; they just duplicate those and update their node pointers.

In this chapter, we introduce Duplicate, a module used to verify any transformation that duplicates instructions while preserving the control-flow structure within RTL. The module itself is very light: the coqwc tool indicates 350 lines of specifications and 300 lines of proof.

This module can be instanced for potentially any number of fitting optimizations, which allows to easily add or remove any such optimization with barely any modification of the underlying Coo proofs. In our case, we use it for tail-duplication, loop unrolling and loop rotation; with a slight modification, we also support branch swapping. ¹

A Duplicate module instance is made of an untrusted OCAML oracle and a common verifier. We typically create one instance per different OCAML oracle optimization. ²

The untrusted oracles have the following type in Coq:

```
Parameter duplicate_aux: function → code * node * (PTree.t node)
```

Given a function to perform a transformation (defined by the oracle) on, it returns:

- The new code on which the transformation was applied.
- The new entrypoint of the function (on the new code).
- A mapping from nodes of the new code to the nodes of the original code. We call this mapping a *reverse map*: its information will guide the verifier.

¹This is a necessary transformation for RTLpath, where the predicted branch of Icond instructions is supposed to be in the ifnot field. More details in section 5.2.1.

²The actual oracle implementations are detailed in chapter 8

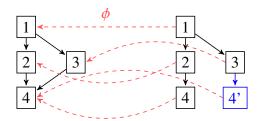


Figure 6.1.: Example of code duplication, with its reverse mapping. To the left, the original code. To the right, the transformed code. The reverse mapping is shown in red.

I give in figure 6.1 an example of code duplication. The nodes 1, 2, 3 and 4 are unchanged. However, a new node 4, named 4' in the figure, is introduced: it is a duplication from node 4. The node 3 is then modified so that its successor becomes 4'. The reverse mapping ϕ indicates which node originated from where. Thanks to ϕ , we will be able to ensure formally that the transformation is correct.

In section 6.1 I detail the forward simulation used for the formal proof of the underlying pass. Next, in section 6.2, I give some details of the verifier implementation. Then, in section 6.3, I detail a bit of the Coo engineering that makes it possible to share efficiently (in terms of proof effort) a common verifier with many different OCAML external oracles. Finally, I give in section 6.4 the modifications done to support branch swapping.

Details about each actual transformation oracle will be given in the remaining sections.

6.1 Proof of correction through a forward simulation

Let us note an original function f and a transformed function f' acquired through replacing the code and entrypoint with those given by the oracle, and a reverse mapping ϕ given by the oracle. The gist of the forward simulation lies in exhibiting that the execution of a node n from f always corresponds to an execution of a node n' from f', with n' verifying $\phi(n') = n$. Each element of the mapping ϕ will be verified to ensure the following property: $\phi(n') = n \implies n \equiv n' \cap \phi(succ(n')) = succ(n)$, where succ(n) denotes the successors of n, and n is the match_inst relation defined below. The mapping ϕ is actually named dm or dupmap in the code (for "duplication map"). The dm n' = Some n notation stands for: "There is a mapping in n' associated to n', and it points to n."

```
Inductive match_inst (dupmap: PTree.t node): instruction → instruction → Prop :=
| match_inst_op: ∀ n n' op lr r,
dupmap!n' = (Some n) → match_inst dupmap (Iop op lr r n) (Iop op lr r n')
| match_inst_cond: ∀ ifso ifso' ifnot ifnot' c lr i i',
dupmap!ifso' = (Some ifso) → dupmap!ifnot' = (Some ifnot) →
```

```
match_inst dupmap (Icond c lr ifso ifnot i) (Icond c lr ifso' ifnot' i')

(* ... *)
```

I give two examples for this relation: Iop and Icond. There can be a match_inst between (Iop op lr r n) and (Iop op' lr' r' n') only if op = op', lr = lr', r = r' and $\phi(n') = n$. The Icond instructions must follow a similar property, with the exception that there are two nodes to check for the reverse mapping (ifso and ifnot), and the branch prediction field is unchecked (since it does not have formal semantics). In a way, this relation is a structural equality, but modulo the pointers of successors, that must verify the mapping ϕ instead.

Given two functions (original and transformed) f and f', we then define a match_function relation:

This relation ensures the following:

- The entrypoints obey the reverse mapping: this ensures that executing a function starts in the same point for both the original and the transformed code (modulo duplication).
- The dupmap_correct relation ensures that the associated instructions of each pair (n', n) from the reverse mapping follow a match_inst relation.
- The rest of the premises ensure that only the code and entrypoint differs, the remaining of the data defining a RTL function are the same.

We then use a lockstep simulation to prove the transformation pass, with the following match_states relation (shown only for the case of a State; the other cases for Returnstate and Callstate are straightforward).

```
Inductive match_states: state → state → Prop :=
| match_states_intro
| dupmap st f sp pc rs m st' f' pc'
| (STACKS: list_V2 match_stackframes st st')
| (TRANSF: match_function dupmap f f')
| (DUPLIC: dupmap!pc' = Some pc):
| match_states (State st f sp pc rs m) (State st' f' sp pc' rs m)
| (* ... *)
```

This denotes a simulation where the register and memory states are structurally the same, but only the program counters pc and pc' change: they must verify $\phi(pc') = pc$.

6.2 Verifier implementation

The core of the verifier is implemented through a simple function comparing two instructions, returning 0K if each field is structurally the same, except for the successor pointers (and the branch prediction field of Icond instructions). Here is the implementation for Iop:

```
Definition verify_match_inst dupmap inst tinst :=
2
       | Iop op lr r n \Rightarrow match tinst with
3
           Iop op' lr' r' n' \Rightarrow
               do u \leftarrow verify_is_copy dupmap n n';
5
               if (eq_operation op op') then
6
                  if (list_eq_dec Pos.eq_dec lr lr') then
7
                    if (Pos.eq_dec r r') then
8
                      OK tt
9
                    else Error (msg "Different r in Iop")
10
                  else Error (msg "Different lr in Iop")
11
                else Error(msg "Different operations in Iop")
12
            | _ ⇒ Error(msg "verify_match_inst Inop") end
```

We use decidable equality functions to compute the verdict. These tests should run fast. We have not concluded detailed measurements, but we have not noticed any odd timings when using these new duplication passes. The function $verify_is_copy$ verifies that the pair (n', n) is indeed a binding of the reverse mapping dupmap.

We prove the correctness of the above function by the theorem verify_match_inst_correct:

The verify_match_inst function is run for each binding found in the reverse mapping. Along with an additional reverse map check on the entrypoints, we can prove that verifying both functions in such a way ensures a match_function relation, from which the forward simulation is then proven.

6.3 Module system

The Duplicate verifier is embedded into a Coq module system, parametrized by the untrusted OCAML oracle. The duplicate_aux function from earlier is actually embedded in a DuplicateOracle module type.

```
Module Type DuplicateOracle
Parameter duplicate_aux: function → code * node * (PTree.t node)
DuplicateOracle
```

We then use two modules that are parametrized by a DuplicateOracle, following the CompCert way of structuring passes. The Duplicate module contains the implementation of the actual pass (the Coq code that calls the OCAML oracle and checks its result), and the Duplicateproof module contains the proofs of the former.

```
Module Duplicate (D: DuplicateOracle)

Export D

(*...*)

End Duplicate

Module Duplicateproof (D: DuplicateOracle)

Include Duplicate D

(*...*)

End Duplicateproof
```

Once these two modules are implemented following the content of the previous subsections, we just have to instantiate them with particular OCAML code to define formally verified transformation passes. We give below the instantiation of the tail-duplicate transformation as an example (the other transformations described in this chapter are instantiated the same way).

```
Module TailDuplicateOracle <: DuplicateOracle

Axiom duplicate_aux : function → code * node * (PTree.t node)

(* Duplicateaux.tail_duplicate is the actual name of the OCaml function *)

Extract Constant duplicate_aux ⇒ "Duplicateaux.tail_duplicate"

End TailDuplicateOracle

Module Tailduplicateproof := DuplicateProof TailDuplicateOracle

Module Tailduplicate := Tailduplicateproof
```

The resulting modules can then be integrated into the standard CompCert RTL compilation flow.

6.4 Modifications to support branch swapping

Branch swapping is the action of negating a condition and inverting the two branches from a conditional branch instruction. In essence, it turns a (Icond c lr ifso ifnot p) into a (Icond (negate c) lr ifnot ifso p), where negate is a function negating a condition (already present in CompCert). The Linearize pass of CompCert already performs this kind of

transformation to minimize branch penalties in the generated program ³, but here we need it at the RTL level for RTLpath.

In our case, branch swapping is done by the static prediction oracle: it inserts prediction information in each Icond, and it also swaps branches accordingly. Verifying code duplication is then not enough to tackle this: we need to add support to the existing Duplicate module. Thankfully though, this is relatively easy and straightforward.

To start, we add a new inductive rule for the match_inst relation:

```
Inductive match_inst (dupmap: PTree.t node): instruction → instruction → Prop :=

(*...*)
| match_inst_revcond: ∀ ifso ifso' ifnot ifnot' c lr i i',
| dupmap!ifso' = (Some ifso) → dupmap!ifnot' = (Some ifnot) →
| match_inst dupmap (Icond c lr ifso ifnot i)
| (Icond (negate_condition c) lr ifnot' ifso' i')
```

We then modify the proof of the forward simulation to account for this new rule. The gist of the forward simulation remains unchanged: we have a simulation modulo the program counters. However, given identical register values, the execution of the original Icond and the modified Icond must lead to the same branch. This is ensured through using the eval_negate_condition lemma from upstream CompCert (given below), and exploiting the RTL semantics of Icond instructions.

Finally, we modify our verifier by checking two possible cases on conditions c and c' respectively from the original and transformed Icond:

- Either c = c', in which case we check that $\phi(ifso') = ifso$ and $\phi(ifnot') = ifnot$.
- Or c = negate(c'): we then check that $\phi(ifso') = ifnot$ and $\phi(ifnot') = ifso$.
- Or neither of the two cases: we reject the program.

³More details in section 8.3.

Formal Verification of Superblock Scheduling

In chapter 4 we saw the basic principles of superblock scheduling. In chapter 5 we defined the RTLpath semantics, based on RTL, for executing whole superblocks.

In this chapter, we use the RTLpath semantics to write a formally proven superblock scheduling verifier. Much like chapter 3, the pass consists of an external untrusted oracle returning a modified superblock and a verifier comparing the modified superblock with the original through symbolic execution.

In the case of superblock scheduling, the scheduling oracle is defined as such:

```
Axiom untrusted_scheduler: RTLpath.function → code * node * path_map * (PTree.t node)
```

Given an original function from RTLpath, the oracle devises a schedule for each superblock (each path from the function). It returns a tuple (tc, te, tpm, dm) where:

- tc is the modified code obtained by devising and applying a schedule on each superblock.
- *te* is the new node representing the entrypoint. Indeed, the untrusted scheduler can move the instruction pointed by the entrypoint further down, so the entrypoint might differ on the scheduled function. ¹
- *tpm* is the new pathmap: for the same reason as above, each path might have a different entry node.
- Finally, *dm* is the reverse mapping: much like chapter 8, we use this reverse mapping to ensure the successors of each superblock still point to the right paths and also to guide the verifier.

Each pair (sb', sb) of superblocks from the reverse mapping dm will be examined and compared through symbolic execution, explained below.

The goal of symbolic execution is to be able to derive a piece of data (a symbolic state) that can be used in conjunction with any initial state (before execution) to deduce its final state

¹In practice, for debugging purposes, we chose that our untrusted scheduler should not modify the existing node values: we change the node content without changing the nodes themselves.

(after execution). We name the rules used to deduce the final state from the initial state (given a symbolic state) *symbolic execution semantics*. These have to be in bisimulation with the RTLpath semantics to ensure correctness. The big picture is then to compute the symbolic state of the original unscheduled superblock, do the same for the scheduled superblock, and compare them. If the scheduled block simulates (according to some simulation relation to be defined later) the input block, then, since their semantics are in bisimulation with the RTLpath semantics, the simulation should also hold in RTLpath semantics.

Compared to our previous work in chapter 3 for basicblock scheduling, there are several additional difficulties:

- For basicblock symbolic execution, the control flow has only one possible direction: through the basicblock. For superblock execution, if we have *n* conditional branches within the superblock, then the control flow has *n* different outcomes. This will need to be reflected within the definition of the symbolic state.
- The notion of RTL state is more complex than that of Asm. In particular, in Asm, we only needed to take into account the registers and memory. In RTL, we also have to take into account whether the final state should be a State, a Returnstate, or a Callstate; along with additional information such as the RTL program counter and the stack.
- Hoisting instructions above conditional branches requires to check that they do not write a register which is live in the other branch. This requires reasoning about liveness.

In our proof architecture, symbolic execution is split into two versions: an abstract symbolic execution, used to facilitate the bisimulation between this symbolic execution and RTLpath semantics; and a concrete symbolic execution, using refined symbolic states (with hash-consing) that can be compared with decidable functions. The link between abstract and concrete (refined) symbolic states is expressed through refinement relations.

First, I define in 7.1 the abstract symbolic execution for superblocks, along with its semantics and the necessary bisimulation required for correctness. Then, I describe in 7.2 the notion of symbolic simulation we use for comparing superblocks and outline a property of the simulation test sufficient to prove a forward simulation on the scheduling pass. Finally, I show the hash-consed implementation of the simulation test, along with the proof that this implementation meets the above property, in section 7.3. This implementation works on refined symbolic states.

The implementation of the scheduling oracle will be described in chapter 8; this chapter only contains the elements of correctness of our formally proven verifier. The work presented in this chapter was done in collaboration with Sylvain Boulmé for the design and some parts of the implementation.

7.1 Abstract Symbolic Execution for Superblocks

I introduce in this section abstract symbolic execution. I avoid repeating the "abstract" word: in the text that will follow, "symbolic value" means "abstract symbolic value", and likewise for the other related terms. Concrete (refined) symbolic execution will be introduced in a later section.

The notions of symbolic value and symbolic memory form the building blocks of symbolic execution. A symbolic value is an expression, possibly including input registers or symbolic memory. These are defined below with mutual induction:

```
Inductive sval :=
2
      | Sinput (r: reg)
3
       | Sop (op:operation) (lsv: list_sval) (sm: smem)
4
       | Sload (sm: smem) (trap: trapping_mode) (chunk:memory_chunk) (addr:addressing)
5
           (lsv:list_sval)
6
    with list_sval :=
7
      | Snil
8
       | Scons (sv: sval) (lsv: list_sval)
9
    with smem :=
10
      | Sinit
11
       | Sstore (sm: smem) (chunk:memory_chunk) (addr:addressing) (lsv:list_sval) (srce: sval)
```

Listing 7.1.: Symbolic value definition

The core idea of symbolic execution is to produce a symbolic state which maps registers and memory to symbolic values. The final values can then be deduced out of symbolic values and initial values by the evaluation functions seval_sval and seval_smem, whose types are given below.

```
seval_sval : RTL.genv → val → sval → regset → mem → option val seval_smem : RTL.genv → val → smem → regset → mem → option mem
```

Figure 7.1 shows a simplified example on a small branchless code. The code contains one addition and one store. The symbolic execution gives a mapping associating the registers and memory to their symbolic value. Here, only the mapping of r_0 , r_1 , r_2 and m are represented. r_0 and r_1 are not changed, so their symbolic value are simply (Sinput r_i). r_2 and r_3 are changed: r_2 contains the symbolic value constructed by a Sop, and the symbolic value of r_3 is constructed with a Sstore, represented here by a "mem[address r_3 value]" notation, where address and value are symbolic values and mem is a symbolic value of memory. We can note that r_3 does not appear anywhere within the symbolic value of memory: the final memory is a

²Since RTL states contain an infinite amount of registers, the mapping also has to account for an infinite amount of registers. In our case, this is handled by having a default mapping: by convention, any unmentioned register *r* has the associated symbolic value (Sinput r).

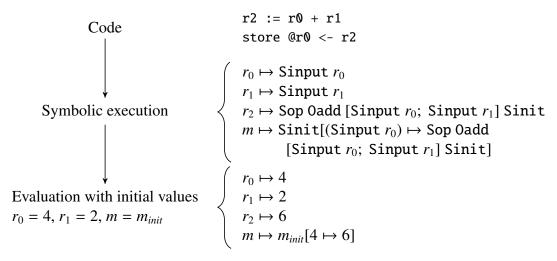


Figure 7.1.: Example of symbolic execution, then evaluation of the symbolic states

function of just the initial values of r_0 , r_1 and m. Symbolic execution computes a kind of parallel assignment – called a symbolic state – that is equivalent to the sequential code. The semantics of this symbolic state evaluates it with the given initial values to deduce the final values of the registers and memory.

Another vital information to store, aside from the final values, is whether there could be a failure (such as a division by zero or an invalid load) during the execution of the block of code. The main theorem of semantic preservation of CompCert assumes behaviours that do not fail. This property is then propagated through the forward simulations, so we have the guarantee that the original code will never fail. However, we do have to guarantee that the transformed code will not fail either. One way to handle this is to remember all the computed symbolic values (including the intermediate ones) and to test whether the scheduled block does not introduce any additional symbolic value that was not present in the original block. If that is the case, we have the guarantee that if the original block does not fail, then the scheduled block should not fail either.

Along with storing the symbolic values of registers and memory, this would be enough to reason about the execution of a branchless basicblock. However, for superblocks, we need to store more information. In subsection 7.1.1, I describe a model of symbolic states for a superblock and its associated semantics. Then, I exhibit in 7.1.2 the process of performing the symbolic execution. Finally, I describe in 7.1.3 the main theorems ensuring a bisimulation between RTLpath and the presented symbolic execution semantics.

7.1.1 Abstract symbolic states and execution semantics

To execute a superblock symbolically, we need to have information on both the case where the whole superblock is executed (all the conditions from the conditional branches evaluated to false), and any case where the superblock exits at a given conditional branch (whose condition evaluation was true). Since we do not know at compile time which it will be, we need a symbolic data structure storing all the possibilities.

I present this data structure by following a bottom-up presentation:

- First, I present sistate_local, which is a symbolic internal state staying local to the superblock. This structure does not encode anything regarding exiting the superblock—it just stores the symbolic values of registers and memory.
- Then, I present sistate_exit: this structure holds both the symbolic state achieved when exiting the superblock, as well as the symbolic value of the condition, to later evaluate whether the condition is taken.
- The next step is to define a sistate, using the two above definitions: a sistate_local to keep track of the current register/memory symbolic values, and a list of sistate_exit to account for all the possible early exits of the superblock.
- Finally, we define a sstate, the actual symbolic execution structure. It combines a sistate with a sfval, a symbolic final value of the superblock. This sfval allows us to store symbolic information for the final instruction of the superblock, which could be either of Icall, Ireturn, Ibuiltin, Itailcall or Ijumptable.

Figure 7.2 shows a tree representation of our data structure. The following subsections will explain the technical details behind these choices.

Model of local internal symbolic states

A sistate_local is defined like this:

```
1
Record sistate_local := { si_pre: RTL.genv → val → regset → mem → Prop;
2 si_sreg: reg → sval; si_smem: smem }
```

si_sreg and si_smem hold the symbolic values of respectively the registers and the memory. si_pre is a precondition on the initial values that must hold for the superblock execution to succeed.

Semantically, (ssem_local ge sp st rs0 m0 rs m) holds if, given initial registers/memory values rs_0 and m_0 , evaluating the local internal symbolic state st would give the new register and memory states rs and m, and the si_pre precondition is met.

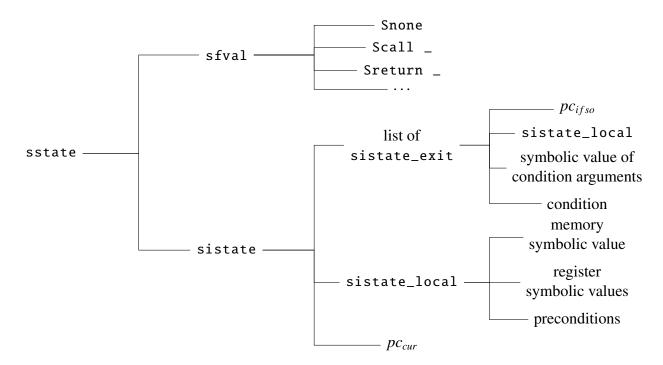


Figure 7.2.: Tree representation of a sstate

```
Definition ssem_local (ge: RTL.genv) (sp:val) (st: sistate_local) (rs0: regset) (m0: mem)

(rs: regset) (m: mem): Prop :=

st.(si_pre) ge sp rs0 m0

^ seval_smem ge sp st.(si_smem) rs0 m0 = Some m

^ \forall (r:reg), seval_sval ge sp (st.(si_sreg) r) rs0 m0 = Some (rs#r)
```

To later reason on whether the superblock execution succeeded or not, we also need to define a relation defining whether the local symbolic state's evaluation is a success. Below is a predicate that holds if one of the evaluations of ssem_local failed: either the precondition was not met, or the memory evaluation failed, or one of the register evaluations failed.

Throughout the rest of this chapter, I will refer to such relations as abort semantics.

Exit internal symbolic state

A sistate_exit encodes what happens if the condition of the early exit evaluates to true, as well as the symbolic value of the condition:

```
Record sistate_exit := mk_sistate_exit
2
      { si_cond: condition; si_scondargs: list_sval; si_elocal: sistate_local;
3
        si_ifso: node }
```

si_cond is the condition to evaluate (could be "greater than" or "lower or equal" for instance), si_scondargs are the arguments of that condition stored as symbolic values, si_elocal is the local symbolic state (of registers and memory) when exiting the superblock, and si_ifso is a pointer to the next superblock to execute when the condition evaluates to true.

It is essential to store the local symbolic state of the early exit and to store under which terms the early exit is taken: for the scheduled superblock to simulate the original, given the same initial values, their execution paths must go through the same early exit. Storing (and then comparing) the symbolic values of the condition arguments is one way to ensure this.

Semantically speaking, (ssem_exit ge sp ext rs m rs' m' pc') holds if, given initial registers/memory values (rs, m), an exit symbolic state ext, and given that the condition of extevaluates to true ³, then evaluating the local symbolic state of ext would give the register and memory states (rs, m), and the early exit ext points to pc' (to be later interpreted as the entry of the next superblock to execute).

```
Definition ssem_exit (ge: RTL.genv) (sp: val) (ext: sistate_exit) (rs: regset) (m: mem)
2
      rs' m' (pc': node) : Prop :=
3
        seval_condition ge sp (si_cond ext) (si_scondargs ext) ext.(si_elocal).(si_smem) rs m
4
          = Some true
5
     ^ ssem_local ge sp (si_elocal ext) rs m rs' m'
     \ (si_ifso ext) = pc'
```

Regarding the abort semantics of the early exit, the first step to consider is the evaluation of the condition arguments. If the condition evaluation fails, then the early-exit evaluation fails. If the condition is evaluated to true, then the early-exit evaluation only fails if the evaluation of its associated local symbolic state fails. Otherwise, if the condition is evaluated to false, then the associated local symbolic state is discarded: there is thus no failure on the early-exit evaluation. This results in the definition below:

```
1
    Definition sabort_exit (ge: RTL.genv) (sp: val) (ext: sistate_exit) (rs: regset) (m: mem)
2
3
      let sev_cond := seval_condition ge sp (si_cond ext) (si_scondargs ext)
4
        ext.(si_elocal).(si_smem) rs m in
5
      sev_cond = None
      ∨ (sev_cond = Some true ∧ sabort_local ge sp ext.(si_elocal) rs m)
```

³One technical remark here is how seval_condition requires the memory for the evaluation. In CompCert, the memory data structure is required to evaluate a pointer comparison: they must point to valid memory blocks. This information is only available within the memory data structure.

Internal symbolic state

We can now define the actual internal symbolic state. This is our running state when executing the superblock symbolically: it holds information about a partial execution of the superblock up to a certain point (named si_pc below).

```
Record sistate := { si_pc: node; si_exits: list sistate_exit; si_local: sistate_local }
```

si_pc is a pointer to the next node to execute in the superblock. si_local is the local symbolic state, holding the symbolic values of registers and memory. Finally, si_exits is the list of all symbolic exit states encountered so far. For technical reasons, this list is stored in reverse order: the first element of the list is the last exit state of the superblock.

When executing a superblock, it should be noted that at most one exit state condition of si_exits will evaluate to true. Indeed, as soon as such condition evaluates to true, the current superblock execution stops to then start the execution of another superblock. Also, another noteworthy point is that if a given exit state condition evaluates to true, then we have the guarantee that all the exit conditions before it evaluated to false. To express these properties, we introduce the following definitions all_fallthrough and all_fallthrough_upto_exit:

```
Definition all_fallthrough ge sp (lx: list sistate_exit) rs0 m0: Prop :=

∀ ext, List.In ext lx →

seval_condition ge sp ext.(si_cond) ext.(si_scondargs)

ext.(si_elocal).(si_smem) rs0 m0 = Some false

Definition all_fallthrough_upto_exit ge sp ext lx' lx rs m : Prop :=

is_tail (ext::lx') lx ∧ all_fallthrough ge sp lx' rs m
```

(all_fallthrough ge sp lx rs0 m0) holds if, given initial (rs0, m0), each exit condition of lx evaluates to false. (all_fallthrough_upto_exit ge sp ext lx' lx rs m) holds if, given initial (rs, m), all the exit conditions of lx' evaluated to false, and lx' represents all the exit conditions up to ext within lx. This last part is ensured through a is_tail relation.

Figure 7.3 depicts a graphical representation of the all_fallthrough_upto_exit relation: from right to left (the last element of si_exits is the first exit state of the superblock), all the conditions up to *ext* evaluated to false, and the relation gives no information about the other conditions.

Now that we have these two definitions, we define the semantics of an internal symbolic state. ($ssem_internal$ ge sp st rs m is) holds if, given initial (rs, m), evaluating the internal symbolic state st would lead to the RTLpath istate is. This reflects a partial evaluation of the superblock: we are evaluating all the past instructions since the superblock entry, all at once.

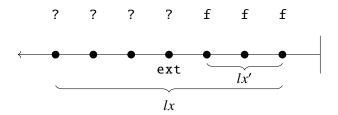


Figure 7.3.: Graphical representation of all_fallthrough_upto_exit relation. The superblock is executed from right to left; all conditions up to ext have been evaluated to false (f in the drawing). The other conditions remain to be evaluated.

```
Definition ssem_internal (ge: RTL.genv) (sp:val) (st: sistate) (rs: regset) (m: mem)
2
      (is: istate): Prop :=
3
      if (is.(icontinue)) then
4
         ssem_local ge sp st.(si_local) rs m is.(irs) is.(imem)
5
        \wedge st.(si_pc) = is.(ipc)
6
        ∧ all_fallthrough ge sp st.(si_exits) rs m
7
      else ∃ ext lx,
8
        ssem_exit ge sp ext rs m is.(irs) is.(imem) is.(ipc)
        A all_fallthrough_upto_exit ge sp ext lx st.(si_exits) rs m
```

The relation is defined based on the value of (icontinue **is**) which represents (according to RTLpath semantics) whether an early branch was taken or not.

- Either no early branch was taken (icontinue is true): the relation holds only if the local symbolic state evaluates to the registers and memory values from *is*, the identifier of the next instruction to execute is equal to the pc of *is*, and all the conditions of the early exits evaluated to false.
- Or an early branch was taken. The relation then only holds if there exists an exit symbolic state such that:
 - All the branches prior to it evaluated to false.
 - The registers, memory and PC of the istate obey the ssem_exit relation with that exit symbolic state.

I schematize in figure 7.4 the ssem_internal relation. Both left and right parts feature the same superblock. On the left, none of the symbolic exit state conditions was evaluated to true, and the local state evaluates to (*irs*, *imem*): there is then a ssem_internal relation to the internal state (*irs*, *imem*, *pc*, *true*). On the right, the two first symbolic exit state conditions were evaluated to false, but not the third, which presented a ssem_exit relation to (*irs*, *imem*, *pc*). There is then a ssem_internal relation to (*irs*, *imem*, *pc*, *false*): according to RTLpath semantics, the superblock execution is about to stop (to move on to another superblock).

The abort semantics for the internal symbolic state follows the same kind of reasoning as for the exit state: either all conditions evaluated to false, but the evaluation of the local symbolic state

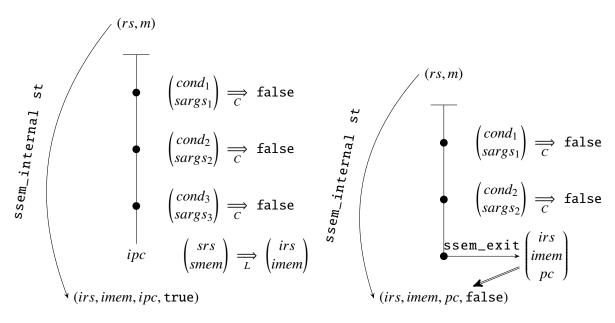


Figure 7.4.: Summary of ssem_internal semantics. The same superblock is presented in two scenarios: on the left, no early exit was triggered so far, so we continue to execute the superblock. On the right, one early exit was encountered: the next internal state will then have icontinue to false. The symbols \Longrightarrow and \Longrightarrow respectively denotate the condition and local (registers and memory) evaluation functions (over symbolic values).

aborted, or only a certain number of exit state conditions evaluated to false, but there was an abort during the evaluation of the following exit state.

```
Definition sabort (ge: RTL.genv) (sp: val) (st: sistate) (rs: regset) (m: mem): Prop :=

(* No early exit was met but we aborted on the si_local *)

(all_fallthrough ge sp st.(si_exits) rs m \( \) sabort_local ge sp st.(si_local) rs m)

(* OR we aborted on an evaluation of one of the early exits *)

V (\( \) ext lx, all_fallthrough_upto_exit ge sp ext lx st.(si_exits) rs m

\( \) sabort_exit ge sp ext rs m)
```

Abstract symbolic final state

As was described in section 5.2.1, in RTLpath, we partition the instructions between those that are schedulable and those that are not—in the context of scheduling, we call the latter *final instructions*. These final instructions can be either Icall, Itailcall, Ibuiltin, Ijumptable or Ireturn.

Since they have arguments whose value might depend on the execution, we have to consider them in our symbolic execution. This is handled by the sfval definition below:

```
1 Inductive sfval :=
```

```
| Snone | Scall (sig:signature) (svos: sval + ident) (lsv:list_sval) (res:reg) (pc:node) | Stailcall: signature → sval + ident → list_sval → sfval | Sbuiltin (ef:external_function) (sargs: list (builtin_arg sval)) | (res: builtin_res reg) (pc:node) | Sjumptable (sv: sval) (tbl: list node) | Sreturn: option sval → sfval
```

A symbolic final value is either Snone (which indicates that no such final instruction was found), or it represents the final instruction of the superblock directly. The arguments are encoded as variants of the type of symbolic values sval, mostly following the definitions of their RTL variant.

The evaluation semantics of symbolic final values are a bit special. I will start by illustrating the example of the Scall evaluation.

```
1  | exec_Scall rs m sig svos lsv args res pc fd:
2         sfind_function pge ge sp svos rs0 m0 = Some fd →
3         funsig fd = sig →
4         seval_list_sval ge sp lsv rs0 m0 = Some args →
5         ssem_final pge ge sp npc stack f rs0 m0 (Scall sig svos lsv res pc) rs m
6         (Callstate (Stackframe res f sp pc rs :: stack) fd args m)
```

The first part of Scall evaluation involves finding the function to be called: this is done through the svos argument, which is of the union type sval + ident. Either the function symbol is directly encoded as an identifier, or the function's address resides in a symbolic value (this would be the case when generating a program with function pointers). If this is the latter, then the symbolic value must be evaluated with the initial (rs0, m0) values, which is what $sfind_function$ does.

In RTL, the semantics of making a call involves creating a new stack frame containing, in particular, the state of registers when the call was made. ⁴ We must then have access to the register state right before the call was made: here, this is represented by the *rs* parameter.

In general, most symbolic final values require having access to both the initial register and memory states to evaluate the symbolic values of their arguments and the register and memory states from the superblock execution up to the final instruction. Their semantics is then represented by the relation (ssem_final pge ge sp npc stk f rs0 m0 sfv rs m t s) which holds if, given npc the PC of the next superblock (only matters if the symbolic final value is Snone), (rs0, m0) the initial register and memory states, (rs, m) the register and memory states reached right before the final instruction of the superblock, evaluating sfv would lead to the RTLpath state s, and would emit the trace t. ⁵

⁴In a sense, this is RTL's way of ensuring that all registers are saved when performing a call.

⁵The other parameters of the relation, such as pge or stk are there to forward information about the execution environment. These mainly reflect RTL semantics.

We illustrated this relation for Scall, but the other symbolic final values go through a similar treatment.

It should be noted that since these instructions are not scheduled, and since the register/memory states before their execution will be evaluated (see the following subsection), there is no need to exhibit abort semantics.

Abstract symbolic state

Now that we have all the building bricks, a symbolic state sstate is simply a symbolic final value combined with the symbolic internal state from right before the final instruction.

```
Record sstate := { internal:> sistate; final: sfval }
```

In terms of semantics, the relation (ssem pge ge sp st stk f rs0 m0 t s) holds if, given initial memory and register states (rs0, m0), evaluating the symbolic state st leads to the RTLpath state st, and emits a trace t.

```
Inductive ssem pge (ge: RTL.genv) (sp:val) (st: sstate) stack f
2
        (rs0: regset) (m0: mem): trace \rightarrow state \rightarrow Prop :=
3
        | ssem_early is:
 4
           is.(icontinue) = false \rightarrow
5
           ssem_internal ge sp st rs0 m0 is \rightarrow
6
           ssem pge ge sp st stack f rs0 m0 E0 (State stack f sp is.(ipc)
7
            is.(irs) is.(imem))
8
      | ssem_normal is t s:
9
           is.(icontinue) = true \rightarrow
10
           ssem_internal ge sp st rs0 m0 is \rightarrow
11
           ssem_final pge ge sp st.(si_pc) stack f rs0 m0 st.(final)
12
            is.(irs) is.(imem) t s \rightarrow
13
           ssem pge ge sp st stack f rs0 m0 t s
```

I schematize this relation in figure 7.5. The ssem relation is a lot like the path_step relation: either an early exit was encountered, or we went through the whole superblock, in which case we only have to execute the final instruction.

Since the generalization from internal symbolic state to symbolic state does not introduce additional abort semantics, we do not introduce any abort semantics for a symbolic state: the later proofs only reason on whether an internal symbolic state evaluation aborted or not.

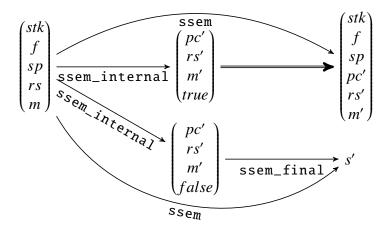


Figure 7.5.: Evaluating a symbolic state with the ssem relation.

7.1.2 Superblock symbolic execution

Now that we have a data structure to hold symbolic information about superblocks, with associated evaluation semantics, we need to devise a way to generate such data. This is done by going through each instruction from the superblock, one by one, accumulating and updating the information of a symbolic internal state as we go.

Internal symbolic execution

Our internal symbolic execution function, siexec_inst, has the type instruction -> sistate -> option sistate: given an instruction, and a current internal symbolic state, it returns either the internal symbolic state after execution, or None in the case that the instruction to be executed is actually a final instruction.

The new internal symbolic state is constructed as such:

- If the instruction sets a register, update the register state by its new symbolic value sv, and add the precondition (in the local symbolic state) that its evaluation (given an initial (rs, m)) should not fail.
- Do the same if an instruction changes the memory: the evaluation of the new memory should not fail.
- If a conditional branch is encountered, create a new symbolic exit state by recording the symbolic value of the condition arguments ⁶ and the local symbolic state.

⁶The condition arguments of a **Icond** are registers, so this just entails recording their symbolic values.

Abstract symbolic execution of the final instruction

This is done through the function <code>sexec_final</code>, of type <code>instruction -> sistate_local -> sfval</code>. It requires the current local internal symbolic state to capture the symbolic value of the potential arguments of the final instruction. Its implementation is mechanical; it follows directly the <code>sfval</code> definition.

Abstract symbolic execution of a superblock

Executing a superblock symbolically simply amounts to executing all of its instructions but the final, and then executing the final instruction. Since the final instruction might be schedulable, the None return value of siexec_inst rules out whether sexec_final should be used instead.

This is done by the function sexec below. (siexec_path size) is a function that executes symbolically a number *size* of instructions with siexec_inst.

```
Definition sexec (f: function) (pc:node): option sstate :=

SOME path ← (fn_path f)!pc IN

SOME st ← siexec_path path.(psize) f (init_sistate pc) IN

SOME i ← (fn_code f)!(st.(si_pc)) IN

Some (match siexec_inst i st with

| Some st' ⇒ {| internal := st'; final := Snone |}

| None ⇒ {| internal := st; final := sexec_final i st.(si_local) |}

end)
```

First, the superblock information is retrieved from the pathmap. Then, we execute symbolically a number path.(psize) of instructions: this gives an internal symbolic state st which contains, in particular, the PC of the final instruction. That final instruction is then executed: first, we try to execute it as if it was schedulable with siexec_inst. If it succeeds, we update the symbolic internal state accordingly and set the final symbolic value to Snone. If it fails, we keep the old symbolic internal state, and we use sexec_final to compute the symbolic final value.

This gives us a superblock symbolic state, representing the execution of a whole superblock.

7.1.3 Bisimulation between RTLpath and symbolic execution semantics

An important intermediate theorem of our formalization states that the RTLpath semantics (path_step) are bisimulated by the semantics of symbolic states (ssem), the latter being computed by symbolic execution (sexec).

We formulate the bisimulation as the observational equivalence between RTLpath semantics and symbolic execution semantics and prove it in two parts. First, we prove that, if there is a path_step, then we can execute the superblock symbolically and evaluate the result with ssem to get the same final state. This proves that the symbolic execution semantics are faithful to the RTLpath semantics. Then, we prove the reverse: if we executed a superblock symbolically, and evaluated it to a certain final state, then we should be able to construct a path_step leading to the same state, thus proving that the symbolic execution semantics is complete in regards to RTLpath semantics.

In both directions of the simulation, we have two subcases: the case where the superblock execution (or evaluation) succeeds and the case where it fails (aborts execution). Not only do we have to prove that a successful execution on one part (RTLpath or symbolic) leads to the same successful execution on the other part, but we also have to prove that failures are adequately reflected.

We will start by describing some key lemmas used for ensuring a kind of bisimulation at the internal level of a superblock. Then we will describe the two theorems that, together, ensure a bisimulation between RTLpath and symbolic execution.

Bisimulation at the internal level

In order to express lemmas reasoning on both the success and abort cases, we introduce two helper definitions: ssem_internal_opt2 and ssem_internal_opt.

```
Definition ssem_internal_opt ge sp (st: sistate) rs0 m0
 2
       (ois: option istate): Prop :=
3
       match ois with
 4
       | Some is ⇒ ssem_internal ge sp st rs0 m0 is
 5
       | None \Rightarrow sabort ge sp st rs0 m0
6
 7
8
     Definition ssem_internal_opt2 ge sp (ost: option sistate) rs0 m0
9
       (ois: option istate) : Prop :=
10
       match ost with
       \mid Some st \Rightarrow ssem_internal_opt ge sp st rs0 m0 ois
11
12
       None ⇒ ois=None
13
       end
```

I recall that istep is a function which returns an option istate: it may return None either if the execution of the instruction failed (an error was encountered) or if we tried to execute a final instruction. *ois* is here to be interpreted as the result of an istep. Similarly, siexec_inst returns None if it attempted to execute symbolically a final instruction; *ost* is to be interpreted as the result of a siexec_inst.

We then express the following lemma, which gives a kind of bisimulation at the level of internal instructions:

```
Lemma siexec_inst_correct ge sp i st rs0 m0 rs m:

ssem_local ge sp st.(si_local) rs0 m0 rs m →

all_fallthrough ge sp st.(si_exits) rs0 m0 →

ssem_internal_opt2 ge sp (siexec_inst i st) rs0 m0 (istep ge i sp rs m)
```

In the context of this lemma, we are executing symbolically a superblock instruction-perinstruction. To an existing internal symbolic state st, we are about to add the result of the symbolic execution of instruction i. We have two premises, ensuring that evaluating the internal symbolic state st indeed would bring us to the point of executing i:

- Evaluating the local symbolic state must succeed and lead to a certain register/memory state (rs, m).
- All the symbolic exit state conditions encountered so far have to evaluate to false.

Under these two conditions, ssem_internal_opt2 bridges siexec_inst with istep in the following way:

- If siexec_inst returned None (because it attempted to execute a final instruction), then istep must also have returned None.
- Or else, if istep returned None (because of an execution failure), then the symbolic state must satisfy sabort (the superblock evaluation must fail as well).
- Or else, then the symbolic state must satisfy a ssem_internal relation: both the istep execution and the evaluation of the symbolic state augmented by siexec_inst must lead to the same internal state.

This lemma is proved by case analysis on the instruction i to be executed symbolically. The proof is mechanical for most instructions. In the case of a conditional branch, if the istep is successful, we have to prove that the symbolic condition evaluation will reflect the execution flow of istep on the register/memory state (rs, m). But since we have the first premise in the lemma, we know that evaluating the superblock up to instruction i with initial states (rs0, m0) gives the same register/memory state (rs, m). So we can deduce that the symbolic values of the condition arguments will evaluate to the same result as the concrete (in RTLpath) condition evaluation, thus guaranteeing that the execution flow will be the same between the RTLpath execution and the superblock evaluation.

This lemma is then used for proving the more general lemma below, reasoning on the execution of all instructions but the last one:

```
1 Lemma siexec_path_correct_true ge sp n (f:function) rs0 m0: ∀ st is,
2 is.(icontinue)=true →
```

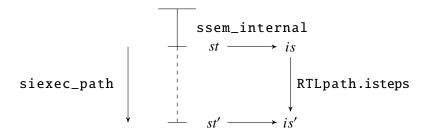


Figure 7.6.: Graphical representation of siexec_path_correct lemma. The superblock is symbolically executed up to a certain point, giving an internal symbolic state *st*. The evaluation of this internal symbolic state succeeds and gives an internal state *is*. The lemma proves then a correspondence between the remaining symbolic execution via siexec_path, and isteps.

This lemma states that, given an initial symbolic internal state st, and its successful evaluation is (assuming the icontinue field is true: all the conditions evaluated to false), and if the n-th default successor of st exists (this can be deduced from the property that each path from RTLpath is well-founded), then evaluating the n next instructions (in addition to the existing internal symbolic state st) should lead to the same result as the actual RTLpath execution. This is summarized in figure 7.6 for a more graphical representation of the lemma.

Bisimulation at the superblock level

With the above lemmas, we can deduce the sexec_correct and sexec_exact theorems below:

```
1
     Theorem sexec_correct f pc pge ge sp path stack rs m t s:
 2
       (fn_path f)!pc = Some path \rightarrow
3
        path_step ge pge path.(psize) stack f sp rs m pc t s \rightarrow
4
       \exists st, sexec f pc = Some st \land ssem pge ge sp st stack f rs m t s
 5
6
     Theorem sexec_exact f pc pge ge sp path stack st rs m t s1:
 7
       (fn_path f)!pc = Some path \rightarrow
8
        sexec f pc = Some st \rightarrow
9
        ssem pge ge sp st stack f rs m t s1 \rightarrow
10
        \exists s2, path_step ge pge path.(psize) stack f sp rs m pc t s2 \land
11
                     equiv_state s1 s2
```

These theorems, together, express a bisimulation between RTLpath and symbolic execution. The siexec_path_correct lemma gives a similar property for the execution of the superblock up to the last instruction, so the remaining part to prove is what happens for the execution of the last

instruction. This is proven by case analysis—some parts of the proof are non-trivial and a bit tedious due to some corner cases, so I will not detail them here. I refer the reader to the available source code for more information.

One thing to note is that, for the sexec_exact theorem, the states s2 (result of the actual execution) and s1 (result of the superblock evaluation) are not structurally the same: indeed, if we take an original code r0 := 1; r0 := 2, the value of the regset after RTLpath execution would look like $rs_{init}[0 \mapsto 1][0 \mapsto 2]$, while its symbolic execution semantics would rather be just $rs_{init}[0 \mapsto 2]$. We then defined a relation equiv_state that is a structural equality, except for the regset where only functional equality is required to satisfy the relation.

7.2 Proving Lockstep Simulation of Scheduling from Sufficient Conditions on Abstract Symbolic Executions

Now that we have a symbolic execution for superblocks and bisimulation properties with RTLpath, the only missing bricks are how to compare two symbolic states and which properties need to be verified to prove a lockstep simulation for the scheduling.

In this section, I present the latter: this will give a simulation property that will have to be fulfilled by the simulation test; the actual hash-consed simulation test is described in the next section. First, I detail in 7.2.1 the definitions of symbolic simulation that we use to reason semantically on whether one superblock simulates the other. Then, I use these definitions in 7.2.2 to outline properties that the verifier must fulfil to ensure a forward simulation from RTLpath to itself, to formally prove the correction of superblock scheduling.

7.2.1 Simulation of superblocks

To prove a lockstep simulation between the original code and the scheduled code, we would like to split the work in two: first, we want to find some properties such that, when fulfilled, a lockstep simulation can be deduced; second, we want to implement a verifier such that its success would imply the verification of the simulation properties. These properties need to be complete and verifiable.

First, we will introduce a notion of simulation at the RTLpath istate level: under which conditions can we say that two istates are equivalent, for the sake of verifying superblock

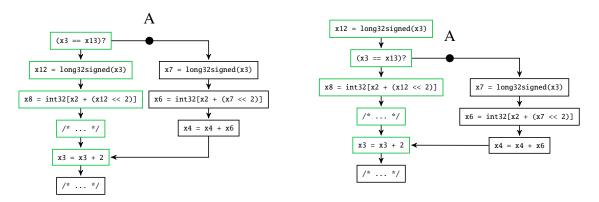


Figure 7.7.: Two semantically equivalent superblocks (in green), but who reach a different state when taking the branch A.

scheduling. Then, we will use this notion to choose a symbolic simulation definition for two symbolic states (the original and the scheduled code, executed symbolically).

Simulation at the RTLpath level

A first issue to consider when designing a simulation property at the RTLpath level is that the entry node value (the index from which we get the RTLpath superblock) might change between the original and the scheduled code. Indeed, if a superblock comprised of instructions [1; 2; 3] is rescheduled into [2; 1; 3], then the path entry of the scheduled superblock will be 2 instead of 1. So we need a way to keep track of which is the original entry of the scheduled superblock. Much like for verifying code duplication (see chapter 8), we use a reverse mapping that is returned by the scheduling oracle. This reverse mapping also guides the verification effort and ensures that each superblock from the pathmap is verified.

Another difficulty is that scheduling an instruction before a conditional branch does not give the same istate when executing the superblock if the branch is taken. For instance, the two superblocks shown in figure 7.7 are semantically equivalent: no matter which path is taken, the result after execution will be the same. However, the states achieved when taking branch A will not be the same: the right superblock will have an additional assignment for x12.

We already have introduced a notion of state simulation at the RTLpath level that allows for certain registers to have different values between the original and the scheduled code: this is the eqlive_states definition from section 5.3.3. We have proven the path_step_eqlive lemma (from that section), which states that, supposing a given early exit is executed, then only the live registers from the exit branch need to have the same value to ensure the same execution.

First, we define istate_simulive as a structural equality modulo liveness between two internal states:

Then, we extend this definition to include: the liveness information to use when taking an early exit; and also the required property that the exit branches from the scheduled and the original code must obey the reverse mapping (named dm in the definition below).

```
Definition istate_simu f (dm: PTree.t node) is1 is2: Prop :=

if is1.(icontinue) then
    istate_simulive (fun _ ⇒ True) is1 is2

else

∃ path, f.(fn_path)!(is1.(ipc)) = Some path
    ∧ istate_simulive (fun r ⇒ Regset.In r path.(input_regs)) is1 is2
    ∧ dm!(is2.(ipc)) = Some is1.(ipc)
```

Two cases are distinguished, based on the value of icontinue from is1:

- Either the superblock continues the execution: in that case, we must have a strict structural equality between is1 and is2.
- Or we are taking (right now) an early exit: in that case, there must be a valid next superblock to execute chosen by *is1.ipc*, both *is2.ipc* and *is1.ipc* must obey the reverse map, and *is1* and *is2* must be equal modulo the liveness of the superblock to be executed in the original code.

This brings a definition of semantic simulation for partial execution of a superblock for concrete RTLpath executions.

Simulation for symbolic states

I will follow a bottom-up presentation to describe our simulation definition for symbolic states, starting from the actual symbolic superblock simulation and then crawling upwards to the underlying definitions.

⁷Actually, it does not have to be strict: verifying it modulo liveness of the current superblock would be enough. For superblock scheduling, making it strict made the proof easier. Recently, Léo Gourdin and Sylvain Boulmé modified it to be verified modulo liveness, which enabled them to implement rewriting rules within superblock scheduling [89].

Given a reverse mapping dm, two RTLpath functions f1 and f2 (the original and the scheduled function), and two entry nodes pc1 and pc2 from which we extract the superblocks to compare, we define a simulation as such:

```
Definition sexec_simu dm (f1 f2: RTLpath.function) pc1 pc2: Prop :=

V st1, sexec f1 pc1 = Some st1 →

3 st2, sexec f2 pc2 = Some st2

∧ ∀ ctx, sstate_simu dm f1 st1 st2 ctx
```

The superblock starting at node pc2 simulates the one starting at pc1 if, given a successful symbolic execution of the first, there exists a successful symbolic execution of the second, such that for any environment context (detailed later), the second symbolic state simulates the first one. In a way, this defines a property of lockstep simulation: the intent is that, when combined with the bisimulation property of RTLpath with regards to symbolic execution, this should imply the forward simulation for the whole transformation.

The environment context contains all the elements that are necessary to evaluate a superblock symbolic state, ensure that the global environments (used to deduce a function out of a symbol) of the scheduled and the original function match, and record that the liveness information of the original pathmap is correct:

```
Record simu_proof_context {f1: RTLpath.function} := {
2
       liveness_hyps: liveness_ok_function f1;
3
       the_ge1: RTL.genv;
4
       the_ge2: RTL.genv;
5
       genv_match: \forall s, Genv.find_symbol the_ge1 s = Genv.find_symbol the_ge2 s;
       the sp: val:
7
       the_rs0: regset;
8
       the_m0: mem
9
    }
```

Now, I recall that a symbolic state contains a symbolic final state (which only matters if no early-exit is taken during the concrete execution) and an internal symbolic state which is used to rule out whether we exit early (and in which state) or we continue through the final instruction. So we take both into account for the definition of a symbolic state simulation, sstate_simu:

This can be read as: given a reverse mapping dm, an original function f, and an execution context ctx, a symbolic state s2 simulates s1 if the simulation holds on their internal symbolic states, and,

if no early-exit was taken (ensured through lines 4 and 5 of the definition), then the simulation also holds on their final symbolic values.

The line 4 is quite lengthy because it involves calling the the_ge1 projection (and others) on ctx—since many of the further definitions will share this syntax cumbersomeness, I will write ctx.ge1 instead of (the_ge1 ctx) and so on.

For the final symbolic state simulation, since the final instructions (call, return, etc...) are not scheduled, we just have to check that they are of the same nature and that their argument evaluations are the same. Here is an example for Sreturn and Snone—the other final instructions are expressed similarly.

```
Inductive sfval_simu (dm: PTree.t node) (f: RTLpath.function) (opc1 opc2: node)
2
       (ctx: simu_proof_context f): sfval \rightarrow sfval \rightarrow Prop :=
3
       | Snone_simu:
4
           dm!opc2 = Some opc1 \rightarrow
5
           sfval_simu dm f opc1 opc2 ctx Snone Snone
      | Sreturn_simu_none: sfval_simu dm f opc1 opc2 ctx (Sreturn None) (Sreturn None)
7
      | Sreturn simu some sv1 sv2:
8
            (seval_sval ctx.ge1 ctx.sp sv1 ctx.rs0 ctx.m0)
9
           = (seval_sval ctx.ge2 ctx.sp sv2 ctx.rs0 ctx.m0) \rightarrow
10
            sfval_simu dm f opc1 opc2 ctx (Sreturn (Some sv1)) (Sreturn (Some sv2))
```

It should be noted that, for Snone, we also check that the nodes indicating the next superblock to execute obey the reverse map, much like the code verifier for code duplication transformations from chapter 8.

Finally, the simulation for internal symbolic states is defined like this:

```
Definition sistate_simu (dm: PTree.t node) (f: RTLpath.function) (st1 st2: sistate)

(ctx: simu_proof_context f): Prop :=

∀ is1, ssem_internal ctx.ge1 ctx.sp st1 ctx.rs0 ctx.m0 is1 →

∃ is2, ssem_internal ctx.ge2 ctx.sp st2 ctx.rs0 ctx.m0 is2

∧ istate_simu f dm is1 is2
```

st2 simulates st1 if, given a successful evaluation of st1 into the internal state is1, then the evaluation of st2 is also successful into an internal state is2, and is2 simulates is1 under the istate_simu relation (equality modulo liveness or just structural equality).

Lockstep simulation on symbolic states

We have defined simulation properties on symbolic states—but we still must prove they are sufficient to ensure a lockstep simulation within the symbolic execution semantics.

First of all, we define a notion of $match_function$: an original function f and a scheduled function f' match if the following holds:

```
Record match_function (dm: PTree.t node) (f1 f2: RTLpath.function): Prop := {
    preserv_fnsig: fn_sig f1 = fn_sig f2;
    preserv_fnparams: fn_params f1 = fn_params f2;
    preserv_fnstacksize: fn_stacksize f1 = fn_stacksize f2;
    preserv_entrypoint: dm!(f2.(fn_entrypoint)) = Some f1.(fn_entrypoint);
    dupmap_path_entry1: ∀ pc1 pc2, dm!pc2 = Some pc1 → path_entry (fn_path f1) pc1;
    dupmap_path_entry2: ∀ pc1 pc2, dm!pc2 = Some pc1 → path_entry (fn_path f2) pc2;
    dupmap_correct: ∀ pc1 pc2, dm!pc2 = Some pc1 → sexec_simu dm f1 f2 pc1 pc2;
}
```

This match_function ensures the following properties binding f and f':

- The signature, parameters, and stack size must be the same.
- Their respective entrypoints should obey the reverse map.
- Each pair (pc2, pc1) of the reverse map should correspond to two path entries: one in the original function, one in the scheduled function.
- Each pair (pc2, pc1) must follow a sexec_simu simulation—this is a way to say that each such pair must have gone through the verifier.

Another necessary definition that we need before expressing our simulation theorem, is a notion of match_states:

```
Inductive match states: state \rightarrow state \rightarrow Prop :=
 2
       | match_states_intro dupmap st f sp pc rs1 rs2 m st' f' pc' path
 3
            (STACKS: list_\forall 2 match_stackframes st st')
 4
            (TRANSF: match_function dupmap f f')
 5
            (DUPLIC: dupmap!pc' = Some pc)
 6
            (LIVE: liveness_ok_function f)
 7
            (PATH: f.(fn_path)!pc = Some path)
 8
            (EQUIV: eqlive_reg (ext path.(input_regs)) rs1 rs2):
 9
            match_states (State st f sp pc rs1 m) (State st' f' sp pc' rs2 m)
10
       | match_states_call st st' f f' args m
11
            (STACKS: list_\forall 2 match_stackframes st st')
12
            (TRANSF: match_fundef f f')
13
            (LIVE: liveness_ok_fundef f):
14
           match_states (Callstate st f args m) (Callstate st' f' args m)
15
       | match_states_return st st' v m
16
            (STACKS: list_\day{2} match_stackframes st st'):
17
            match_states (Returnstate st v m) (Returnstate st' v m)
```

This definition follows a typical match_states you would find for RTL, except for the following points:

• The match_function defined above must hold between the original and translated functions.

- Each time we execute a path from a State of RTLpath, the PC of the scheduled version must obey the reverse map with the PC of the original version.
- The original function must have had its liveness information verified for all of its paths.
- The stack pointer and memory must be structurally equal; however, the registers must only coincide modulo the liveness of the path about to be executed.

We have also defined a match_stackframes with similar conditions.

We can then express below the main theorem of symbolic state simulation, ssem_state_simu:

```
Theorem ssem_sstate_simu dm f f' stk stk' sp st st' rs m t s:

match_function dm f f' →

liveness_ok_function f →

list_∀2 match_stackframes stk stk' →

ssem pge ge sp st stk f rs m t s →

(∀ ctx: simu_proof_context f, sstate_simu dm f st st' ctx) →

∃ s', ssem tpge tge sp st' stk' f' rs m t s' ∧ match_states s s'
```

This theorem states that, given some premises about the context, if we evaluate successfully a symbolic state st into a state s, and that the symbolic states st and st' are in simulation (according to $sstate_simu$, and independently of the execution context), then evaluating the symbolic state st' will be successful and lead to a state s' that will be in match with the original state s. This ensures a lockstep simulation within the symbolic execution semantics.

This theorem is proven directly by using the simulation properties, with several undetailed helper lemmas.

7.2.2 Simulation Test Specification and Superblock Scheduling Lockstep Simulation

Given two superblocks to compare, we defined in the last subsection a simulation property sexec_simu, as well as a theorem ssem_state_simu outlining a forward simulation within symbolic execution.

The sexec_simu property is actually acquired with the following lemma, simu_check_correct:

```
Lemma simu_check_correct dm f tf:
simu_check dm f tf = OK tt →

y pc1 pc2, dm ! pc2 = Some pc1 →
sexec_simu dm f tf pc1 pc2
```

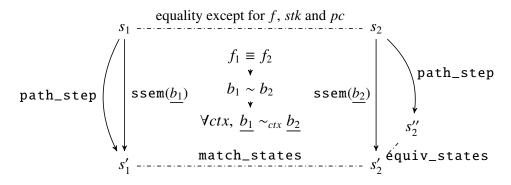


Figure 7.8.: Diagram used for proving the simulation in superblock scheduling. s_1 is actually the state made of $(f, sp, stk_1, rs, m, pc_1)$, and s_2 is made of $(f', sp, stk_2, rs, m, pc_2)$. $\underline{b_i}$ is the symbolic execution of the superblock from pc_i .

simu_check is the hash-consed simulation test (described section 7.3). The lemma states that if the original function f was compared (superblock per superblock) with the scheduled function tf, then, for each pair (pc2, pc1) of the reverse mapping, we have the sexec_simu simulation. This lemma represents the required property from the simulation test to prove the forward simulation.

The forward simulation is itself mostly expressed by the following theorem.

```
Lemma exec_path_simulation dupmap path stk1 stk2 f1 f2 sp rs m pc1 pc2 t s1':
2
       (fn_path f1)!pc1 = Some path \rightarrow
3
       path_step ge pge path.(psize) stk1 f1 sp rs m pc1 t s1' →
      list_∀2 match_stackframes stk1 stk2 →
 5
      dupmap ! pc2 = Some pc1 \rightarrow
 6
       match_function dupmap f1 f2 \rightarrow
7
       liveness_ok_function f1 \rightarrow
8
      \exists path' s2', (fn_path f2)!pc2 = Some path'
9
         ∧ path_step tge tpge path'.(psize) stk2 f2 sp rs m pc2 t s2'
10
         ∧ match_states s1' s2'
```

To prove this theorem, we use the past theorems <code>sexec_correct</code> (simulation of RTLpath by symbolic execution), <code>sexec_exact</code> (simulation of symbolic execution by RTLpath), <code>simu_check_correct</code> (correctness of the verifier) and <code>ssem_state_simu</code> (forward simulation within symbolic execution). I expose in figure 7.8 the simulation diagram involved.

An attentive eye will notice that we consider the regsets from s_1 and s_2 to be structurally equal. In practice, they are only equal modulo liveness: we will see right after the theorem explanation that it does not matter for the proof.

Since there is a path_step from s_1 to s'_1 , we can apply the theorem sexec_correct and deduce the following: the symbolic execution of the superblock pointed by pc is successful and gives a symbolic state b_1 whose evaluation results in the same state s'_1 .

Using the properties from the match_function, we can deduce that pc_2 is a valid path entry of f_2 , and we have a simulation sexec_simu between pc_1 and pc_2 : this implies that the symbolic execution of the superblock pointed by pc_2 is successful and gives a symbolic state $\underline{b_2}$. We also get the property of a sstate_simu simulation between $\underline{b_1}$ and $\underline{b_2}$.

We have then all the premises required to use the theorem $ssem_state_simu$, and deduce that the evaluation of $\underline{b_2}$ will be successful, and result in a state s'_2 which is in a match_states relation with s'_1 (modulo liveness).

The final part is then to apply the theorem sexec_exact: since pc_2 was successfully symbolically executed to $\underline{b_2}$, and that $\underline{b_2}$ was itself successfully evaluated to s_2' , then there is a state s_2'' in equiv_state relation with s_2' .

The actual theorem is then deduced from the use of one last small lemma, match_states_equiv, that states a transitivity between match_states and equiv_states:

```
Lemma match_states_equiv s1 s2 s3:
match_states s1 s2 → equiv_state s2 s3 →
match_states s1 s3
```

This proves the theorem exec_path_simulation. However, this is not exactly a forward simulation yet: we would like to reason on any initial s_1 and s_2 that are in match_states, not just those that are structurally equal.

This is where the lemma path_step_eqlive from chapter 5 comes in handy.

```
Lemma path_step_eqlive path stk1 f sp rs1 m pc t s1 stk2 rs2:

path_step ge pge (psize path) stk1 f sp rs1 m pc t s1 →

list_∀2 eqlive_stackframes stk1 stk2 →

eqlive_reg (ext (input_regs path)) rs1 rs2 →

liveness_ok_function f →

(fn_path f) ! pc = Some path →

∃ s2, path_step ge pge (psize path) stk2 f sp rs2 m pc t s2 ∧ eqlive_states s1 s2
```

This lemma allows to transform a path_step with initial regset rs1 into a path_step with initial regset rs2 such that rs2 and rs1 are in structural equality modulo liveness. This can be used to generalize the lemma above for the more general case where the two states s_1 and s_2 are equivalent modulo liveness (following a match_states instead of structural equality).

The generalization is then used to prove a forward simulation for superblock scheduling, thus ensuring its correctness.

7.3 Refined Simulation Test with Hash-Consing

The previous section outlined a simulation property, sexec_simu, used for proving the forward simulation. We would like now to implement a test such that its success would imply the simulation. This test should take two symbolic states and deliver a boolean value: either true or false based on whether the two symbolic states are equivalent.

Using the abstraction level provided by our model of symbolic states allowed us to prove the bisimulation more easily; however, now we need to refine them to give an efficient implementation of their comparison. Indeed, a sstate contains terms whose values cannot be compared with any terminating executable function. For example, the si_pre component of a sistate_local cannot be compared with another si_pre: it requires to have the execution context, that we do not have at compile-time. si_sreg is also another field we cannot compare: we cannot check in finite time an infinite number of register values.

Some fields, however, like si_smem, could be compared. But we have an additional issue, first discovered by Tristan and Leroy [95]: in the worst case, we have an exponential blow-up due to the tree structure of the memory representation (we could end up comparing identical subtrees several times in different places of the tree). Also, our symbolic states do not allow trapping loads to be turned into non-trapping loads: they will not be structurally the same. Finally, in COMPCERT, some operations like pointer comparison depend on memory: they need to know which memory blocks were allocated. We remove this dependency in our refined values by exploiting the property that the instructions inside superblocks never modify the memory allocation.

The refined version should have comparable data structures. Still, it should also include hashconsing to prevent the exponential blow-up and also provide a way to canonize values (such as trapping loads) to accept certain transformations on the level of symbolic values. We do not want to define whole new semantics for these new types, so we will define projections and refinement relations that will link a refined symbolic state hst and its semantically equivalent symbolic state st.

The hash-consing method used is the same as the one from chapter 3, so we will not describe it again here. However, we will detail the refined symbolic state definitions, explain how we compare those, and then outline lemmas showing that the refined states we introduced are equivalent to the symbolic states from earlier.

7.3.1 Refined Symbolic States and Refinement Relations

The concrete (refined) symbolic states mimic the symbolic states in terms of organization: a refined sistate_local will be called hsistate_local, a refined sstate will be called hsstate, and so on.

For each of them, we will present their definition and their refinement relation, that is, how do they relate to their non-refined variant in terms of semantics. Then we will describe the main theorem ensuring that the refined symbolic execution is correct regarding symbolic execution semantics.

Refined symbolic values and final symbolic values

Their definition is very close to the definition of symbolic values:

```
1
     Inductive hsval :=
2
      | HSinput (r: reg) (hid: hashcode)
3
       | HSop (op: operation) (lhsv: list_hsval) (hid: hashcode)
4
      | HSload (hsm: hsmem) (trap: trapping_mode) (chunk: memory_chunk) (addr: addressing)
5
        (lhsv: list_hsval) (hid: hashcode)
6
    with list_hsval :=
7
      | HSnil (hid: hashcode)
8
      | HScons (hsv: hsval) (lhsv: list_hsval) (hid: hashcode)
9
    with hsmem :=
10
      | HSinit (hid: hashcode)
11
     | HSstore (hsm: hsmem) (chunk: memory_chunk) (addr: addressing) (lhsv: list_hsval)
12
          (srce: hsval) (hid:hashcode)
```

Each constructor is exactly like a symbolic value, except that it also has a hashcode, used for hash-consing. Although one key difference is for HSop: this one does not depend on (symbolic) memory, while Sop does. This is a simplification to allow for operational instructions to be intermingled with memory stores. Then, when translating a refined symbolic value into a symbolic value (thus giving it a semantic), we reintroduce the symbolic memory as Sinit (which evaluates to the initial memory right before executing the superblock). This simplification is correct because the few operations requiring the memory (mostly pointer comparison operations) do not depend on the values stored in memory: they rely on other information (that do not change through a superblock) such as memory block allocation. This only adds a few lines of proof, while tackling this issue directly in the abstract symbolic execution model would have been more challenging.

The translation from refined symbolic values to symbolic values (that we call projection) is defined below. Aside of the HSop specific case, the rest is quite straightforward.

```
1
     Fixpoint hsval_proj hsv :=
2
       match hsv with
3
       \mid HSinput r \_ \Rightarrow Sinput r
4
       | HSop op hl _ ⇒ Sop op (hsval_list_proj hl) Sinit
5
       | HSload hm t chk addr hl _ ⇒ Sload (hsmem_proj hm) t chk addr (hsval_list_proj hl)
6
       end
7
     with hsval_list_proj hl :=
8
     match hl with
9
       | HSnil _{-} \Rightarrow Snil
10
      | HScons hv hl _ ⇒ Scons (hsval_proj hv) (hsval_list_proj hl)
11
12 with hsmem_proj hm :=
13
      match hm with
14
       | HSinit _ ⇒ Sinit
15
       | HSstore hm chk addr hl hv _ ⇒ Sstore (hsmem_proj hm) chk addr (hsval_list_proj hl)
16
         (hsval_proj hv)
17
       end
```

The refined symbolic final values, of type hsfval, are constructed in much the same way as a sfval, except that they use refined symbolic values instead of symbolic values.

```
Inductive hsfval :=
2
      | HSnone
3
      | HScall (sig: signature) (svos: hsval + ident) (lsv: list_hsval) (res: reg)
4
        (pc: node)
5
      | HStailcall (sig: signature) (svos: hsval + ident) (lsv: list_hsval)
6
      | HSbuiltin (ef: external_function) (sargs: list (builtin_arg hsval))
7
        (res: builtin_res reg) (pc: node)
8
      | HSjumptable (sv: hsval) (tbl: list node)
      | HSreturn (res: option hsval)
```

Their projection is implemented in much the same way. It should be noted that we do not hash-cons them. Since they are only found at the end of a superblock, and there is only one of them per superblock, hash-consing would not reduce the number of equality tests performed to check the simulation of final symbolic values.

Refined local symbolic state

We have modelled local symbolic state with registers and memory symbolic values (stored as functions acting as mappings, like $reg \rightarrow sval$), and a function on register and memory values to express a required precondition to evaluate the symbolic state. These types were great to reason semantically—but now we need to define types that can be compared. This is done through hsistate_local:

```
1
    Record hsistate_local :=
2
      {
3
        hsi_smem:> hsmem;
        hsi_ok_lsval: list hsval;
```

```
5     hsi_sreg:> PTree.t hsval
6    }
```

First of all, to represent register values, we use a PTree.t positive map, a type introduced by CompCert. Internally, this positive map is a tree encoded so that each leaf from the tree is assigned a positive index.

This positive map will store all the refined symbolic values of the registers that are not identity: so there is only a finite number to check, those that are explicitly stored in hsi_sreg. The semantic of the positive map is actually implemented in the hsi_sreg_proj function below:

```
Definition hsi_sreg_proj (hst: PTree.t hsval) r: sval :=

match PTree.get r hst with

None ⇒ Sinput r

Some hsv ⇒ hsval_proj hsv
end
```

If the mapping does not have a corresponding register entry, it is assumed that the register was not touched (its symbolic value is identity).

To remember which values were computed (necessary to ensure that scheduling does not introduce additional failures), we store them in the list hsi_ok_lsval. We only store them if they might incur failure.

Finally, storing the memory is just done through a simple has mem type. Since the refined memory has the history of all the memory assignments (we do not perform any rewriting rule within the refined symbolic memory), there is no need to store them in a separate list.

We define a property hsok_local ensuring that, given a refined local symbolic state, its evaluation will be successful. We also define a sok_local property to better reason whether a non-refined local symbolic state would fail.

```
Definition sok_local (ge: RTL.genv) (sp:val) (rs0: regset) (m0: mem) (st: sistate_local):

Prop :=

(st.(si_pre) ge sp rs0 m0)

seval_smem ge sp st.(si_smem) rs0 m0 <> None

V(r: reg), seval_sval ge sp (si_sreg st r) rs0 m0 <> None

Definition hsok_local ge sp rs0 m0 (hst: hsistate_local) : Prop :=

(V hsv, List.In hsv (hsi_ok_lsval hst) → seval_hsval ge sp hsv rs0 m0 <> None)

(seval_hsmem ge sp (hst.(hsi_smem)) rs0 m0 <> None)
```

The refinement relation between local refined symbolic state *hst* and non-refined symbolic state *st* is then defined as the conjunction of four properties:

```
1
     Definition hsilocal_refines ge sp rs0 m0 (hst: hsistate_local) (st: sistate_local) :=
2
            (sok\_local \ ge \ sp \ rs0 \ m0 \ st \leftrightarrow hsok\_local \ ge \ sp \ rs0 \ m0 \ hst)
3
       \wedge (hsok_local ge sp rs0 m0 hst \rightarrow
4
         smem_refines ge sp rs0 m0 (hsi_smem hst) (st.(si_smem)))
5
       \land (hsok_local ge sp rs0 m0 hst \rightarrow \forall r, hsi_sreg_eval ge sp hst r rs0 m0
6
         = seval_sval ge sp (si_sreg st r) rs0 m0)
7
       \land (\forall m b ofs, seval_smem ge sp st.(si_smem) rs0 m0 = Some m \rightarrow
          Mem.valid_pointer m b ofs = Mem.valid_pointer m0 b ofs)
```

The first property ensures a simulation, in terms of success, between the refined and non-refined variants. If the evaluation of one fails, then the evaluation of the other must also fail. This simulation is necessary: we need to forward the information that the evaluation succeeded, from a symbolic state to its refined state, then from the refined state to the scheduled refined state, and finally from the scheduled refined state back to the scheduled symbolic state.

The second and third properties ensure that the evaluation of the refined memory/registers states (through projection) coincide with the non-refined version, but only if the evaluation succeeds. If the evaluation of the refined state does not succeed, the property does not give any information; however, we don't need to have this kind of information in such a case. Lastly, the fourth property is there to act as an invariant necessary to have the right to remove the memory dependency on HSop. These ensure a bisimulation between refined and abstract symbolic states.

We can note that the execution context (the initial values of registers and memory) must rule out whether there is such a refinement or not because the refinement is expressed in terms of symbolic execution semantics.

Refined symbolic exit state

The refined symbolic exit state is like its non-refined counterpart, except that it uses the refined version of the local symbolic state, and the symbolic condition values.

```
Record hsistate_exit := mk_hsistate_exit
2
      { hsi_cond: condition; hsi_scondargs: list_hsval; hsi_elocal: hsistate_local;
3
        hsi_ifso: node }
```

Because of a technical issue I will point out in the next subsection, we have to split the refinement of exit states into two parts: a static part, independent of the execution context, and a dynamic part:

```
1
    Definition hsiexit_refines_stat (hext: hsistate_exit) (ext: sistate_exit): Prop :=
2
      hsi_ifso hext = si_ifso ext
3
4
    Definition hsiexit_refines_dyn ge sp rs0 m0 (hext: hsistate_exit) (ext: sistate_exit):
```

```
hsilocal_refines ge sp rs0 m0 (hsi_elocal hext) (si_elocal ext)

(hsok_local ge sp rs0 m0 (hsi_elocal hext) →

hseval_condition ge sp (hsi_cond hext) (hsi_scondargs hext)

(hsi_smem (hsi_elocal hext)) rs0 m0

= seval_condition ge sp (si_cond ext) (si_scondargs ext)

(si_smem (si_elocal ext)) rs0 m0)
```

The static part is straightforward: it just checks that the node values for ifso are the same. The dynamic part is a bit more intricate. First of all, we must have a refinement within the local state of the early exit. I recall that this local state is a snapshot of the state we had right before executing the conditional branch.

We must also refine the condition arguments, but this is only required if the local state succeeded. It is a valid weakification of the premise: the condition evaluation refinement is only necessary if we did not fail earlier in the superblock.

These two definitions are generalized to a list of refined symbolic exit states by the definitions below:

```
Definition hsiexits_refines_stat lhse lse :=
list_V2 hsiexit_refines_stat lhse lse

Definition hsiexits_refines_dyn ge sp rs0 m0 lhse se :=
list_V2 (hsiexit_refines_dyn ge sp rs0 m0) lhse se
```

Each pair of exit states from both lists must verify the above predicate for the generalized predicate to hold.

Refined internal symbolic state

A refined internal symbolic state is like an internal symbolic state, but with refined types.

```
1 Record hsistate := { hsi_pc: node; hsi_exits: list hsistate_exit;
2 hsi_local: hsistate_local }
```

The refinement definitions are as such:

```
Definition hsistate_refines_stat (hst: hsistate) (st:sistate): Prop :=

hsi_pc hst = si_pc st

hsiexits_refines_stat (hsi_exits hst) (si_exits st)

Definition hsistate_refines_dyn ge sp rs0 m0 (hst: hsistate) (st:sistate): Prop :=

hsiexits_refines_dyn ge sp rs0 m0 (hsi_exits hst) (si_exits st)

hsilocal_refines ge sp rs0 m0 (hsi_local hst) (si_local st)

nested_sok ge sp rs0 m0 (si_local st) (si_exits st)
```

They are mostly straightforward, except for the third premise of the dynamic refinement: this one is an invariant ensuring that if a local state somewhere in the superblock (either at the end or an exit state) evaluates successfully, then each of the upwards local states also evaluate successfully. This is a necessary property to have to later reason on the condition evaluation of each exit state since they each require a hsok_local property.

More precisely, here is the definition of the predicate nested_sok:

```
Inductive nested_sok ge sp rs0 m0: sistate_local → list sistate_exit → Prop :=
2
        nsok_nil st: nested_sok ge sp rs0 m0 st nil
3
      | nsok_cons st se lse:
4
         (sok_local ge sp rs0 m0 st \rightarrow sok_local ge sp rs0 m0 (si_elocal se)) \rightarrow
5
         nested_sok ge sp rs0 m0 (si_elocal se) lse \rightarrow
         nested_sok ge sp rs0 m0 st (se::lse)
```

Refined symbolic state

At last, a refined symbolic state is defined below. It is comprised of a refined symbolic internal state and a refined symbolic final value.

```
Record hsstate := { hinternal:> hsistate; hfinal: hsfval }
```

Here is its refinement property:

```
Definition hsstate_refines (hst: hsstate) (st:sstate): Prop :=
2
       hsistate_refines_stat (hinternal hst) (internal st)
3
      \land (V ge sp rs0 m0, hsistate_refines_dyn ge sp rs0 m0 (hinternal hst) (internal st))
4
      \land (\forall ge sp rs0 m0, hsok_local ge sp rs0 m0 (hsi_local (hinternal hst)) \rightarrow
         hfinal_refines ge sp rs0 m0 (hfinal hst) (final st))
```

We have the static, context-independent part, which involves checking out the static parts from the internal state refinement. And then we have the dynamic part, but this time, valid for any value of the original context: refinement over the internal state, and then refinement over the final values, but only if the local state (from the internal state) evaluation is successful.

Refined symbolic execution and correction property

The refined symbolic execution function hsexec is coded in much the same way as sexec, except that it uses and updates refined types. We will not detail it, except for one different aspect that we will describe in subsection 7.3.3: hsexec also performs a kind of canonization of hash-consed terms, e.g. to turn trapping loads into non-trapping loads.

Its correctness theorem, hsexec_correct, is a variation of the following (the actual theorem includes hash-consing specifics that makes it harder to read):

```
Lemma hsexec_correct_aux f pc:
WHEN hsexec f pc → hst THEN
3 st, sexec f pc = Some st ∧ hsstate_refines hst st
```

Given a successful refined symbolic execution of a path starting at pc giving hst, it ensures that the non-refined symbolic execution would also be successful and return st, and that hst is a refinement of st based on the definitions above.

We will see in the following subsection how do we use hsexec_correct, the refinement definitions, and some simulation test specifications that we will define to prove the sexec_simu relation required for the whole forward simulation.

7.3.2 Simulation test specifications and implementation

In the last subsection, we saw refined symbolic states and projection functions for refined symbolic values.

Prior to that, we saw that in order to achieve a forward simulation for the superblock pass, we need to prove that if the simulation test succeeds, then we must have a siexec_simu relation, that I recall below:

```
Definition sexec_simu dm (f1 f2: RTLpath.function) pc1 pc2: Prop :=

V st1, sexec f1 pc1 = Some st1 →

3 st2, sexec f2 pc2 = Some st2 ∧ ∀ ctx, sstate_simu dm f1 st1 st2 ctx
```

To construct this relation, we first exhibit specifications that the simulation test must follow; then, we outline a theorem ensuring that these specifications indeed allow us to deduce the sexec_simu simulation. As we have done before, we will follow the structure of refined symbolic states to guide our description.

Simulation test of refined local symbolic states

To begin with, the specification for the simulation test on local symbolic states is given as follows:

```
1
    Definition hsilocal_simu_spec (oalive: option Regset.t) (hst1 hst2: hsistate_local) :=
2
          List.incl (hsi_ok_lsval hst2) (hsi_ok_lsval hst1)
3
       \land (\forall r, (match oalive with Some alive \Rightarrow Regset.In r alive \mid \_ \Rightarrow True end)
4
           \rightarrow PTree.get r hst2 = PTree.get r hst1)
5
       hsi_smem hst1 = hsi_smem hst2
```

Given an original refined local symbolic state hst1 and a scheduled one hst2, the simulation test should make sure that:

- hst2 does not introduce additional trapping computations compared to hst1
- They have the same (structurally) refined symbolic values for the registers in the given set of registers (this set is to be interpreted as the set of live registers)
- They have the same refined symbolic memory.

The actual test is done through two functions based on whether we would like to perform the test modulo liveness or not:

```
Definition hsilocal_simu_check hst1 hst2 : ?? unit :=
2
      phys_check (hsi_smem hst2) (hsi_smem hst1);;
3
      PTree_eq_check (hsi_sreg hst1) (hsi_sreg hst2);;
4
      Sets.assert_list_incl mk_hash_params (hsi_ok_lsval hst2) (hsi_ok_lsval hst1)
5
    Definition hsilocal_frame_simu_check frame hst1 hst2 : ?? unit :=
7
      phys_check (hsi_smem hst2) (hsi_smem hst1);;
8
      PTree_frame_eq_check frame (hsi_sreg hst1) (hsi_sreg hst2);;
      Sets.assert_list_incl mk_hash_params (hsi_ok_lsval hst2) (hsi_ok_lsval hst1)
```

In the actual code, we also have debugging information that can be toggled 8; for clarity, we omit them here.

We use the Impure library from Boulmé [15], upon which hash-consing was added (see appendix C.4.3 of Six et al. [88]). Since we use hash-consing, checking the structural equality of two hash-consed terms amounts to check the physical (pointer) equality. More details can be found in chapter 3: we apply the same mechanisms here. In addition to that, Impure also implements an efficient function for testing the inclusion of two lists of hash-consed terms, Sets.assert_list_incl.

Finally, PTree_eq_check is a function that checks the structural equality of each tree, the leaves being checked through phys_check. PTree_eq_check_frame does the same check, but only for the concerned registers, by iterating through the frame list.

The correctness of these functions are then proven through lemmas such as this one:

⁸Debugging such a verifier can be tricky: without debugging information, we know that it fails, but we do not know where. In our development, we used a mix of debugging information, ocamldebug tool, and sometimes even manually instrumenting the generated OCAML code.

```
Lemma hsilocal_frame_simu_check_correct hst1 hst2 alive:

WHEN hsilocal_frame_simu_check (Regset.elements alive) hst1 hst2 → _ THEN

hsilocal_simu_spec (Some alive) hst1 hst2
```

Since hsilocal_frame_simu_check involves calling OCAML oracles through the Impure framework, the termination is not guaranteed—moreover, the Impure library does not guarantee that two executions of the same function would give the same result. The WHEN term \rightarrow x THEN P syntax from Impure means: if the computation of term finishes, and gives a value x, then the property P holds.

This lemma certifies that the actual simulation test obeys its specification.

Simulation test of refined exit symbolic states

We define the specification of simulation for exit states:

Two refined symbolic exit states are semantically equivalent if:

- Their conditions and condition refined symbolic arguments are structurally equal.
- Their respective if so branches obey the reverse mapping
- The ifso path from the first exit state exists, and their local states are equivalent modulo liveness of the path.

The simulation test follows closely this specification:

```
Definition hsiexit_simu_check (dm: PTree.t node) (f: RTLpath.function)
(hse1 hse2: hsistate_exit): ?? unit :=
struct_check (hsi_cond hse1) (hsi_cond hse2);;
phys_check (hsi_scondargs hse1) (hsi_scondargs hse2);;
revmap_check_single dm (hsi_ifso hse1) (hsi_ifso hse2);;
DO path & some_or_fail ((fn_path f) ! (hsi_ifso hse1));;
hsilocal_frame_simu_check (Regset.elements path.(input_regs))
(hsi_elocal hse1) (hsi_elocal hse2)
```

To ensure a check modulo liveness, the input_regs field is taken from the ifso path.

We also define and prove a correctness theorem in much the same way we did for local states.

Simulation test of refined symbolic internal states

Almost last, we define the simulation of two refined symbolic internal states:

```
Definition hsistate_simu_spec dm f (hse1 hse2: hsistate) :=
list_\( \forall \) (hsiexit_simu_spec dm f) (hsi_exits hse1) (hsi_exits hse2)
hsilocal_simu_spec None (hsi_local hse1) (hsi_local hse2)
```

This amounts to checking the simulation of each exit state two by two and then checking the simulation of the local state for all registers.

The simulation test implementation is straightforward.

Simulation test of refined symbolic final values

The simulation of final symbolic values is defined as structural equality on the symbolic final projections (final_simu_spec, not shown here, is more or less structural equality, but with some checks on the reverse mapping):

```
Definition hfinal_simu_spec (dm: PTree.t node) (f: RTLpath.function) (pc1 pc2: node)
(hf1 hf2: hsfval): Prop :=
final_simu_spec dm f pc1 pc2 (hfinal_proj hf1) (hfinal_proj hf2)
```

The implementation of the simulation test is a bit more lengthy (we have to give special care for builtins that have their own definitions) but still relatively straightforward.

Simulation test of refined symbolic state

Finally, the simulation of two refined symbolic states is expressed by combining the above definitions:

```
Definition hsstate_simu_spec (dm: PTree.t node) (f: RTLpath.function) (hst1 hst2: hsstate) :=
    hsistate_simu_spec dm f (hinternal hst1) (hinternal hst2)
    hfinal_simu_spec dm f (hsi_pc (hinternal hst1)) (hsi_pc (hinternal hst2))
    (hfinal hst1) (hfinal hst2)
```

Its implementation hsstate_simu_check is also straightforward, using the implementation of the underlying smaller structures.

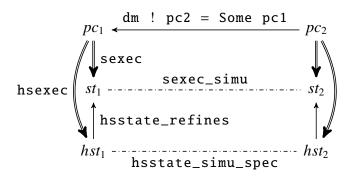


Figure 7.9.: Diagram used for proving the refinement simulation.

Refinement Simulation from simulation test

We define a notion of simulation between two refined symbolic states:

```
Definition hsstate_simu dm f (hst1 hst2: hsstate) ctx: Prop :=

V st1 st2,

hsstate_refines hst1 st1 →
hsstate_refines hst2 st2 → sstate_simu dm f st1 st2 ctx
```

Two refined states *hst*1 and *hst*2 simulate each other if their non-refined counterparts simulate each other.

We can prove that the specification given above indeed imply this notion of simulation (though we will not detail the proof here):

```
Theorem hsstate_simu_spec_correct dm f ctx hst1 hst2:

hsstate_simu_spec dm f hst1 hst2 →
hsstate_simu dm f hst1 hst2 ctx
```

Let's now combine what we have so far to prove the simu_check_correct theorem, which proves the necessary property for the forward simulation of the scheduling pass. I write the theorem below, with sexec_simu unfolded to get a clearer view.

```
Lemma simu_check_correct dm f tf:
simu_check dm f tf = OK tt →

y pc1 pc2, dm ! pc2 = Some pc1 →

st1, sexec f1 pc1 = Some st1 →

st2, sexec f2 pc2 = Some st2

A y ctx, sstate_simu dm f1 st1 st2 ctx
```

To help in the description of the proof of this theorem, I drew the diagram in figure 7.9. The terms that I will write below are present in the diagram.

From the premises, we know that $simu_check$ succeeded, so each pair (pc2, pc1) of the reverse mapping was checked through refined symbolic execution (which all succeeded) and simulation test of each pair of refined symbolic states. Thus, for the particular pc1 and pc2 from the theorem, we know that their refined symbolic execution succeeded and gave the refined symbolic states hst_1 and hst_2 .

By using hsexec_correct on these refined symbolic executions, we deduce that the non-refined symbolic executions would also have been successful 9 , and they would have given respectively the non-refined symbolic states st_1^{10} and st_2 , from which hst_1 and hst_2 are refinements.

Since hst_1 and hst_2 were checked by the verifier, we know they meet the hsstate_simu_spec relation; since this relation is correct (by the lemma hsstate_simu_spec_correct), we deduce that they follow the hsstate_simu simulation.

We have the two refinements: between hst_1 and st_1 , and between hst_2 and st_2 . So we have a sstate_simu relation between st_1 and st_2 . Which proves the theorem.

7.3.3 Canonization of Refined Symbolic Values

The previous subsections showed how we defined a refined symbolic execution and implemented a simulation test from which we deduce a forward simulation. However, we have not discussed how we can perform small transformations within superblock scheduling, such as transforming trapping loads into non-trapping loads. Indeed, without any change, a trapping load refined symbolic value and a non-trapping load value are structurally different.

We solve this problem by introducing a mechanism of canonization. By simplifying certain symbolic terms into semantically equivalent terms (in the case of loads, we simplify all loads into non-trapping loads), our modified refined symbolic values become comparable again.

Generalized Operations and Refinement Preservation

To reason about simplifications, we introduce the type root_sval:

⁹I employ the conditional tense here because during the compilation, we never actually execute the non-refined versions! They are only here to reason semantically.

¹⁰Formally, the st_1 described above (let's name it st'_1) and st_1 from the theorem are two different states. However, since there are both equal to sexec f1 pc1, they are actually the same by transitivity of structural equality: $st'_1 = st_1$.

```
Inductive root_sval: Type :=
| Rop (op: operation)
| Rload (trap: trapping_mode) (chunk: memory_chunk) (addr: addressing)
```

In a way, this represents the "root" of a symbolic value: it abstracts the operations to perform on the symbolic arguments of Sop and Sload. Here, we will call it a *generalized operation*: it's like an operation, except that memory loads are also taken in this abstraction.

The semantics of generalized operators is given by the root_apply function below.

```
Definition root_apply (rsv: root_sval) (lr: list reg) (st: sistate_local): sval :=
let lsv := list_sval_inj (List.map (si_sreg st) lr) in
let sm := si_smem st in
match rsv with
| Rop op ⇒ Sop op lsv sm
| Rload trap chunk addr ⇒ Sload sm trap chunk addr lsv
end
```

Given a generalized operator, a list of registers, and a local symbolic state, we fetch the symbolic value of the arguments; then, we insert these in the generalized operator to give a symbolic value.

We also define the same function, but for refined states:

```
Definition root_happly (rsv: root_sval) (lr: list reg) (hst: hsistate_local) : ?? hsval :=

DO lhsv ← hlist_args hst lr;;

match rsv with

Rop op ⇒ hSop op lhsv

Rload trap chunk addr ⇒ hSload hst trap chunk addr lhsv
end
```

The correction of root_happly is ensured through a lemma of refinement preservation (given below): if two local symbolic states refine each other, then applying root_apply on one and root_happly on the other preserves the refinement.

```
Lemma root_happly_correct (rsv: root_sval) lr hst:

WHEN root_happly rsv lr hst → hv' THEN ∀ ge sp rs0 m0 st

(REF:hsilocal_refines ge sp rs0 m0 hst st)

(OK:hsok_local ge sp rs0 m0 hst),

sval_refines ge sp rs0 m0 hv' (rsv lr st)
```

Generalized Operators Simplification

The actual canonization is done through the function simplify below:

```
1
     Definition simplify (rsv: root_sval) (lr: list reg) (hst: hsistate_local): ?? hsval :=
2
       match rsv with
3
       | Rop op \Rightarrow
4
         match is_move_operation op lr with
5
         | Some arg ⇒ hsi_sreg_get hst arg
6
          | None ⇒
7
           DO lhsv ← hlist_args hst lr;;
8
            hSop op lhsv
9
          end
10
      | Rload _ chunk addr ⇒
11
           DO lhsv ← hlist_args hst lr;;
12
           hSload hst NOTRAP chunk addr lhsv
13
```

Right now, this function has two purposes:

- It simplifies any memory load into a non-trapping memory load, which is correct if there is no failure (see section 5.1.2).
- It simplifies any move operation (operations that affect the content of a register to another register) into copying the symbolic value of the register directly. For instance, (Sop Omove [sv] Sinit) will be simplified to just sv. This is also a correct simplification.

The correctness is proven through a lemma of refinement preservation, much like root_happly_correct, that we prove by case analysis:

```
Lemma simplify_correct rsv lr hst:
2
      WHEN simplify rsv lr hst \sim hv THEN \forall ge sp rs0 m0 st
3
        (REF: hsilocal_refines ge sp rs0 m0 hst st)
4
        (OKO: hsok_local ge sp rs0 m0 hst)
5
        (OK1: seval_sval ge sp (rsv lr st) rs0 m0 <> None),
        sval_refines ge sp rs0 m0 hv (rsv lr st)
```

This mechanism thus allows us to replace memory loads with their speculative versions and perform some other small optimization on the size of the symbolic state without breaking the model on which we prove the superblock scheduling.

Optimizing the size of the refined symbolic states

I will present now two optimizations that decrease the simulation test execution time by further reducing the size of the refined symbolic state under certain specific conditions.

The first optimization consists of removing from the PTree of the registers: the bindings of the form $r \mapsto (HSinput r _)$. Indeed, in the absence of binding for a given register of a refined local symbolic state, the refined evaluation semantics consider the register symbolic value to

be an identity. The optimization is done through using the function red_PTree_set below whenever we would like to set such a register value ¹¹:

```
Definition red_PTree_set (r: reg) (hsv: hsval) (hst: PTree.t hsval): PTree.t hsval :=

match hsv with

HSinput r' _ ⇒

if Pos.eq_dec r r'

then PTree.remove r' hst

else PTree.set r hsv hst

| _ ⇒ PTree.set r hsv hst
end
```

In terms of RTL semantics, this optimization amounts to replacing $rs[r \mapsto rs[r]]$ by rs, where rs is a regset.

Another optimization consists of limiting the number of symbolic values present in the hsi_ok_lsval field of a refined symbolic local state. Indeed, out of all the computed symbolic values, we only need to store those that might incur a failure. If we can prove that a given refined symbolic value would never have any failure, then we can safely remove it from the list of computed symbolic values. For instance, speculative loads never fail, so there would be no need to include them.

This is done during the refined symbolic execution: before changing the refined local state, the generalized operator is checked by the function may_trap below (||| is here a lazy boolean OR operator):

```
Definition may_trap (rsv: root_sval) (lr: list reg): bool :=

match rsv with

Rop op ⇒ is_trapping_op op ||| negb (Nat.eqb (length lr) (args_of_operation op))

Rload TRAP _ _ ⇒ true

Rload NOTRAP _ _ ⇒ false

end
```

If may_trap returns false, then we know that it is impossible for any evaluation of the refined symbolic value to fail, so we do not add the value to the list hs_ok_lsval. This allows the simulation test to work on smaller sets when performing the inclusion test.

These optimizations should improve the execution time of the simulation test.

¹¹This function also enables to accept rewriting rules. For instance, r1 := r2; r2 := r1 is simulated by r1 := r2. Though we do not use this feature in superblock scheduling.

Part III

Experiments

Performance Tuning of Superblock Formation, Selection, Linearization

In the previous chapters I outlined a number of formally proven verifiers related to superblock scheduling: the RTL to RTLpath pathmap and liveness verifiers from chapter 5, the generic Duplicate verifier from chapter 6 and finally the superblock scheduling verifier from chapter 7. In the two following chapters, I will detail the implementation of the underlying oracles (except the RTLpath liveness oracle): even though their implementation does not affect the correctness of the passes thanks to the verifiers, they are in control of the performance aspect of each pass. A bug in the implementation of any of those will result in either a compilation failure (the oracle returns an incorrect result: the verifier rejects the compilation) or bad performance (the oracle did detrimental transformations).

This chapter is dedicated to the oracles of tail-duplication (section 8.1), loop unrolling and rotation (section 8.2), branch prediction (section 8.4) and linearization (section 8.3). If you have not already, before reading this chapter, I encourage the reader to read chapter 4 which introduces the general concepts of superblocks: it gives a quick and graphical overview of the various transformations described here.

8.1 Trace selection and tail-duplication

Once branch prediction is performed (either statically via section 8.4, through __builtin_expect user annotations, or through profiling), the next step is to form up execution traces that follow the likely paths of execution and then possibly transform the traces that are not superblocks into superblocks.

I do this combined work in two distinct steps:

• I partition the RTL CFG in a set of traces (subsection 8.1.1)

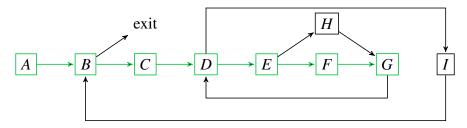


Figure 8.1.: RTL code for two nested loops. The identified trace is shown in green.

• Each trace is tail-duplicated as long as the amount of duplicated nodes does not go over a certain threshold to prevent duplicating too much (subsection 8.1.2).

These two steps are done in a single pass, called TailDuplicate. That pass is an instance of the Duplicate module from chapter 6: in particular, we must be careful in the OCAML oracle to exhibit a reverse mapping to help the correctness verifier.

The pass does not perform the actual superblock selection: this is done later, through the RTL to RTLpath oracle. The emphasis here is to transform the CFG so that the later actual superblock selection will be as fruitful as possible in terms of performance gain; however, there is no exact correspondence between a selected trace and a future superblock.

To give a practical example, figure 8.1 shows the typical example of two nested loops, as generated by CompCert. Each conditional branch from the loops is assumed to be predicted correctly (the static prediction ruled that the execution will remain within the loop most of the time), and let's assume there is a conditional branch within the innermost loop that was predicted.

An obvious trace for that code would be A - B - C - D - E - F - G: it surely regroups the most executed nodes from that code. That trace is not a superblock because there are side-entrances: the two loop edges $I \to B$ and $G \to D$, plus the edge $H \to G$, most likely coming from an if-then-else construct.

Applying naively tail-duplication would involve duplicating instructions starting from the first side-entrance, so starting at node *B*. Figure 8.2 shows the result of applying such a tail-duplication. This would create a superblock following the first execution of the outermost and innermost loops, but as soon as the second iteration of the innermost loop would be reached, the execution would go back to the duplicated (non-superblock) code.

On the other hand, tail-duplicating only from G node (shown figure 8.3) would provide just what we want: a superblock encompassing the innermost loop.

There are two ways to tackle this issue. Either we cut the trace so that only the innermost loop from the trace is selected for tail-duplication. Or we skip the loop headers when going through

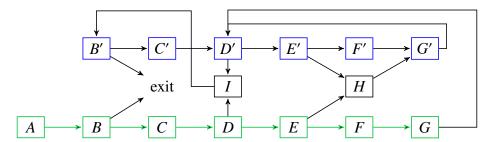


Figure 8.2.: RTL code for two nested loops, with a tail-duplication starting at B. The identified trace shown in green is now a superblock, although unwanted. The duplicated nodes as a result of tail-duplication are shown in blue.

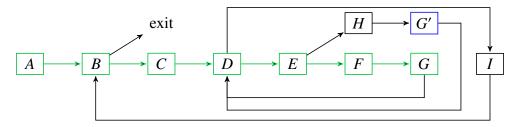


Figure 8.3.: RTL code for two nested loops, with an interesting tail-duplication done on the green trace. The duplicated node is in blue.

the trace. I found the latter to be more practical to implement, but the former could also have been a possibility and would have required a similar amount of effort.

The remaining subsections explain the exact algorithms performing trace partitioning and tailduplication.

8.1.1 Trace partitioning

Given a RTL control-flow graph annotated with prediction information, we would like to partition it so that each node will belong to only one trace: we would not want to apply tail-duplication to a set of nodes that already went through tail-duplication. We are particularly interested in traces that follow the most used execution flow, potentially entering loops (our tail-duplication will not duplicate the whole loop), and, whenever predicted, following the predicted branch of a conditional branch. Needless to say, having a fair branch prediction is necessary to prevent this pass from selecting "bad traces".

As was summarized in section 4.1.4, I largely base my algorithm on the one from Chang and Hwu [20], except that I forbid traces from crossing each other, and I rely only on the prediction information from conditional branch instructions. I recall that these are of ternary nature (either None, Some true or Some false). 1

¹See section 5.1.3 for more details on prediction information.

First of all, I define in algorithms 5 and 6 the functions best_successor_of and best_predecessor_of that return respectively a node that is picked to grow the trace either forward or backward.

Our representation of branch prediction makes it straightforward to select the best_successor: we just have to follow the predicted branch in the case of a predicted conditional branch or follow the only possible branch for the nodes that only have one successor. For the other cases, None is returned: this will then be interpreted as stopping to grow the trace. It also returns None when the predicted successor is already visited to prevent creating overlapping traces.

The implementation of best_predecessor_of, which selects a predecessor to grow the trace backwards, is a bit less strict. We only have the notion of "predicted successor" in our representation; we do not have any notion of "predicted predecessor". Furthermore, since we store branch prediction in a ternary way, we do not have enough information to rule out which predecessor is more likely to have been crossed by the execution. The function (best_predecessor_of n) then simply returns a node n' for which the predicted successor of n' is n, and n' is not visited. If there are several of them, the algorithm chooses based on the DFS order of the graph.

Algorithm 5. Choosing privileged successor for trace selection.

```
1: function BEST_SUCCESSOR_OF(node, code, visited)
 2:
        function select(node)
             match code[node] with
 3:
 4:
                 case Icond _ _ ifso ifnot pred
                     match pred with
 5:
                          case None
 6:
 7:
                              return None
                          case Some true
 8:
                              return Some ifso
 9:
                          case Some false
10:
                              return Some ifnot
11:
                 case Ijumptable _
12:
13:
                      return None
14:
                 case i
                      return either None or (Some s) based on the presence of a successor
15:
        chosen \leftarrow select(node)
16:
        if visited[chosen] then
17:
             return None
18:
        else
19:
             return Some chosen
20:
```

The set of successors of a given node is straightforward to obtain (just extract them from the RTL instruction syntax). The set of predecessors is trickier and requires to go through the whole graph. I abstracted this detail in the algorithm, but in practice, I pre-compute the set of predecessors for

Algorithm 6. Choosing privileged predecessor for trace selection.

```
1: function BEST_PREDECESSOR_OF(node, code, visited)
2:
        foreach pred ∈ predecessors[node] in DFS order
            if visited[pred] then
3:
                continue
4:
 5:
            match code[pred] with
                case Icond _ _ ifso ifnot pred
 6:
                     if (pred = Some true && node = ifso) || (pred = Some false && node =
    ifnot) then
8:
                         return Some pred
                     else
9:
                         continue
10:
                 case Ijumptable _
11:
                     continue
12:
13:
                case
                     return Some pred
                                              ▶ Other instructions have either 1 or 0 successor.
14:
        return None
15:
```

each node by a simple DFS graph traversal before running the actual trace selection algorithm. Another detail I abstracted is that computing a DFS graph traversal order requires knowing which node is the entrypoint. In the implementation, the DFS order is pre-computed, then given as a parameter to the functions.

Once we have these two functions to select a successor/predecessor to grow a trace, we can perform the actual trace selection (algorithm 7). The trace selection algorithm starts from an unvisited node (selected by DFS order). It tries to grow the trace forward through the successors; then, it tries to expand it backwards through the predecessors when it cannot grow further in the forward direction. The algorithm marks nodes as visited as they are added to a trace. Once the trace is finished (impossible to grow the trace in both forward and backwards directions), the trace is stored, and start a new one from an unvisited node, by DFS order.

8.1.2 Tail-duplication

Once the traces are selected, tail-duplication is applied to them, but in such a way that whole loops will not be tail-duplicated. The tail-duplication is written in algorithm 8. It takes as input the code to modify, the current reverse mapping (since each trace is tail-duplicated one by one, the current reverse mapping needs to be updated accordingly), and the trace to perform tail-duplication on.

The gist of the algorithm is to go through each node, starting from the first node of the trace, then analyze if that node has any other predecessor than the previous node of the trace: ignoring loop

Algorithm 7. Trace selection algorithm based on Chang and Hwu [20]

```
1: function select_traces(code)
         visited \leftarrow { all \mapsto false }
 3:
         traces \leftarrow []
         while \exists n \in \text{code s.t. visited}[n] = \text{false do}
 4:
 5:
              seed \leftarrow first node n of DFS order s.t. visited[n] = false
              current \leftarrow seed
 6:
              add_to_trace(trace, current)
 7:
              while true do
 8:
 9:
                   match best_successor_of(current, visited) with
10:
                        case None
                             break
11:
                        case Some s
12:
                             trace := trace + node
13:
                             visited[node] := true
14:
15:
                             current \leftarrow s
16:
              current ← seed
                                                             ▶ Resetting to grow the trace backwards
17:
              while true do
                   match best_predecessor_of(current, visited) with
18:
                        case None
19:
                             break
20:
                        case Some p
21:
                             trace := node + trace
22:
23:
                             visited[node] := true
24:
                             current \leftarrow p
                                                                        ▶ The trace is finished growing
25:
              traces += trace
         return traces
26:
```

Algorithm 8. Tail-duplication algorithm

```
1: function TAIL_DUPLICATE(code, revmap, trace)
 2:
          counter \leftarrow 0
          code \leftarrow copy(code)
 3:
          npc \leftarrow next\_free\_pc(code)
 4:
 5:
          is first \leftarrow true
          foreach n \in \text{trace}
 6:
 7:
               if is first then
                                                ▶ Special case for the trace entry: it is never duplicated.
                    is first \leftarrow false
 8:
 9:
                    prev \leftarrow n
10:
                    continue
               lp \leftarrow predecessors(n) - prev - backedges(n)
11:
               if lp \neq \emptyset then
12:
13:
                    code[npc] := copy(code[n])
14:
                    reroute_nodes(code, lp, n \mapsto npc)
15:
                    revmap := revmap [npc \mapsto n]
                    if code[n] is not a Inop then
16:
                          counter += 1
17:
18:
               prev \leftarrow n
          return (code, revmap, counter)
19:
```

edges (whole loops must not be tail-duplicated), if there is any predecessor, then it duplicates the node, and points the predecessors into that duplicated node instead. In the algorithm, backedges(n) return the nodes having a backedge with n, reroute_nodes is a function that changes the pointers of each node from a list to make them point to another node instead, and copy is an abstract function symbolizing a deep copy.

The algorithm returns a triple of: the modified code, the reverse mapping (useful for the verificator), and also a counter keeping track of the number of duplicated nodes (not counting Inop instructions: these are eliminated later on in CompCert anyway, so they are not counted). If the counter reaches a certain threshold, the returned code is ignored: the transformation is an identity (no tail-duplication is performed).

This is to prevent cases where the code size penalty due to tail-duplication would be too big compared to the performance gain. Right now, this is a very simple heuristic. Probably some smarter heuristics could be implemented in the future.

At the end of the algorithm, we should have a trace where any side-entrance (except loop backedges) is redirected to duplicated nodes, which should, in the case of a trace going inside an innermost loop, transform the innermost loop body into a superblock. I iterate the algorithm for each trace found in the RTL function by the select_traces function from earlier.

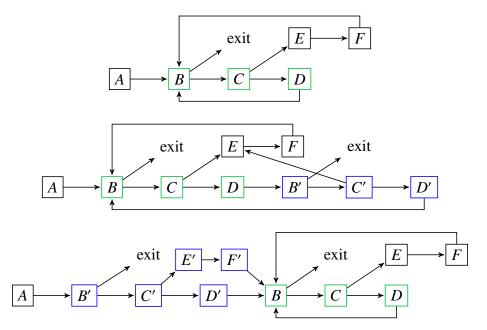


Figure 8.4.: Example of loop unrolling and loop peeling: above is the original code, in the middle is the unrolled code, at the bottom is the code with loop peeling. The nodes that are part of the original superblock are shown in green. The duplicated nodes are shown in blue.

We have hand tested our implementation on many examples to ensure that it behaves correctly, though a bug in there would not compromise correctness, thanks to our Duplicate verifier.

8.2 Loop unrolling, peeling and rotation

Loop unrolling and rotation are two transformations that do not do much on their own but when combined with prepass and postpass scheduling, can have some performance impact. Much like tail-duplication, these two transformations passes are instances from the generic Duplicate module.

Figure 8.4 shows an example of loop unrolling on a simple innermost loop, which went through a tail-duplication (it's a similar code than in figure 8.3, but simplified). Interestingly, this unrolling can be done just by duplicating nodes and changing node pointers: this makes it an excellent fit for our Duplicate verifier. Also, such an unrolling preserves the superblock structure: this then increases the scheduling potential of a superblock.

We also perform loop peeling: we duplicate the loop body once, outside of the loop (see figure 8.4). Loop peeling allows to copy in particular loop-invariant expressions outside of the loop, in order for CSE3 to remove these expressions from the main loop body [63]. Loop peeling is very similar to loop unrolling; it relies on duplicationg the relevant nodes, then adjusting the successor pointers. I do not detail its algorithm here.

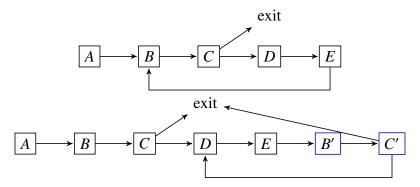


Figure 8.5.: Example of loop rotation: above is the original code, below is the rotated code, with the duplicated nodes shown in blue.

Finally, loop rotation is another optimization of interest, illustrated by figure 8.5. This optimization does not have much impact on the prepass scheduling; however, it may impact the postpass scheduling for a technical reason inherent to the architecture-specific CompCert backends.

In RTL, a conditional branch instruction is a single instruction that performs both the comparison computation and the actual branching. In most ISAs, however, this is done in two different instructions: one that performs the comparison, setting a specific register to the result of that comparison; then another that uses that result to branch accordingly. ²

As a result, for an innermost loop whose condition would require a separate instruction, the generated code from Mach to Asm consists of the code performing the comparison, then the conditional branch, and finally the actual loop body. The later basic block scheduling will then be unable to schedule the comparison code with the rest of the loop body since there is a conditional branch between. The prepass scheduling also will not be able to do much with the comparison code: it cannot move the comparison code below the conditional branch (it would conflict with the register used for comparison), and in some cases, it cannot move instructions above the branch either (if these would trap).

A solution consists of rotating the loop in the way of figure 8.5: enough instructions are duplicated for the first iteration to be correct; then, the loop is shifted in such a way that the conditional branch instruction is last in the loop body. This allows both basicblock and superblock schedulings to potentially schedule the comparison instructions with the rest of the loop body.

Both algorithms rely on a prior innermost loop detection, which outlines innermost loops and valuable information for the later passes. I first describe our innermost loop detection in subsection 8.2.1, then I describe the two algorithms: loop unrolling in subsection 8.2.2, loop rotation in subsection 8.2.3.

²This is the case for the KVX ISA, but also more mainstream ones like the Risc-V instruction set.

8.2.1 Innermost loop detection

Much like tail-duplication required to have traces to perform the optimization, our loop unrolling and rotation transformations need us to know beforehand where the innermost loops are.

For that, I use the innermost loop detection implemented by David Monniaux for the Loop Invariant Code Motion optimization [63]: given a set of loop headers to investigate (these are computed with a graph traversal), it returns a mapping where to each loop header is associated the list of nodes composing the innermost loop (if it is indeed an innermost loop). This is done by using a dominator dataflow analysis.

For each innermost loop identified, the following data structure is then generated by using simple graph traversal analysis (not detailed here).

```
type innerLoop = {
  preds: P.t list;
  body: P.t list;
  head: P.t;
  finals: P.t list;
  sb_body: P.t list option;
}
```

- preds contains the predecessors of the loop, that is, which nodes have pointers to the loop entry.
- head is the first instruction of the loop (the entry).
- body is the list of instructions (including the head) of the loop.
- finals is the list of the instructions that loop back to the head. There can be more than one such instruction: for example, a tail-duplicated loop will have at least two final instructions.
- If the innermost loop wraps a whole superblock, then sb_body are its instructions. Acquiring sb_body involves starting from the head of the loop, then following the predicted path until it either reaches back the head or stops because of a None prediction.

For example, if we examine the original code from figure 8.4: preds is [A], head is B, body is the whole loop, so [B, C, D, E, F], and finals is [E, F]. However, we are not interested in unrolling the whole loop since E and F are not part of any superblock; so, in addition to this information, we also have sb_body = [B, C, D] that contains the actual superblock we are interested in.

Once this structure is acquired, the loop unrolling and loop rotation transformations below are executed.

8.2.2 Loop unrolling

To unroll loops, I first define a function clone(code, revmap, ln) whose goal is to duplicate the instructions from the list ln, on the original code code; and with the original reverse mapping revmap as parameter to update it. The function is defined in algorithm 9. bindings(ln, ln') is an abstract function returning a mapping that binds two-by-two each element of ln with the corresponding element of ln'.

Algorithm 9. Algorithm to clone a list of instructions

```
1: function clone(code, revmap, ln)
         head' \leftarrow next_free_pc(code)
2:
3:
         \ln' \leftarrow \text{map}(\ln, n \mapsto n + \text{head'})
4:
         fwmap \leftarrow bindings(ln, ln')
         revmap' \leftarrow revmap[bindings(ln', ln)]
 5:
         code' ← code
 6:
         foreach n \in ln
7:
              n' \leftarrow fwmap[n]
8:
              code'[n'] := copy(code[n])
9:
10:
               reroute_nodes(code', [n'], fwmap)
11:
         return (code', revmap', ln', fwmap)
```

In a way, when ln is a contiguous set of nodes from the RTL graph, the algorithm duplicates both the nodes and the edges within that set. The nodes are first copied structurally (including their pointers), then the pointers are changed through applying a forward mapping fwmap: the pointers that initially pointed to nodes from the set now point to the duplicated nodes instead.

To ensure there is no collision (the new node integers used for the duplicated instructions do not collide with existing nodes), I use a trick: the next available integer is computed (the next free PC), then added to the node from the instruction to duplicate. The result of that addition is the new node. Doing it this way also ensures a certain consistency between the original code structure (in terms of used integers) and the modified code, which makes the transformation pass slightly easier to debug or analyze.

The loop unrolling, described in algorithm 10, then consists of the following steps:

- 1. The superblock body sb_body is cloned into new instructions sb_body'.
- 2. The last instruction of sb_body is modified to point to the head of sb_body' (instead of looping back).
- 3. The last instruction of sb_body' is modified to loop back to the head.

Like tail-duplication, if too many instructions to duplicate are counted (except Inop instructions), the loop is left without change.

Algorithm 10. Algorithm to unroll the body of a loop

```
1: function UNROLL_BODY(code, revmap, iloop)
2:
        match iloop.sb_body with
3:
             case None
                 return (code, revmap)
4:
             case Some sb_body
 5:
                 if too_many_instructions(sb_body) then
 6:
 7:
                      return (code, revmap)
                 sb\_final \leftarrow last(sb\_body)
8:
                 (code', revmap', sb_body', fwmap) ← clone(code, revmap, sb_body)
9:
                 head' ← fwmap[iloop.head]
10:
                 sb\_final' \leftarrow fwmap[sb\_final]
11:
                 reroute_nodes(code', [sb_final], iloop.head → head')
12:
                 reroute_nodes(code', [sb_final'], head' \mapsto iloop.head)
13:
14:
                 return (code', revmap')
```

8.2.3 Loop rotation

The loop rotation is done similarly: first, a group of nodes to duplicate is identified - then, they are duplicated, and the pointers are changed to make a loop rotation. In the case of loop rotation, the group of nodes to duplicate is all the nodes from the head to the conditional branch.

I define a function extract_upto_icond, not detailed here. Given a head, this function attempts to follow the execution path until it reaches a conditional branch. If the function finds an instruction that does not have exactly one successor, it returns None. Similarly, if the function reaches back the head, it also returns None (this might happen in the case of an infinite loop in the C source program: a loop without any conditional branch).

I write in algorithm 11 the loop rotation algorithm.

Algorithm 11. Algorithm to rotate a loop

```
1: function ROTATE_LOOP(code, revmap, iloop)
2:
       match extract_upto_icond(code, iloop.head) with
            case None
3:
4:
                return (code, revmap)
5:
            case Some header
                if too_many_instructions(header) then
6:
7:
                    return (code, revmap)
                (code', revmap', header', fwmap) ← clone code revmap header
8:
9:
                head' ← fwmap[iloop.head]
                reroute_nodes(code', iloop.preds, iloop.head → head')
10:
                return (code', revmap')
11:
```

Exactly like tail-duplication and loop unrolling, no modification is performed if too many nodes would be duplicated.

8.3 Adapting the Linearize oracle for superblocks

Chapter 1 gave an overview of each transformation pass and intermediate representation. In particular, the Linearize transformation pass generates a Linear code out of a LTL code. The LTL representation is like RTL, except for three major differences:

- Whereas a RTL code is a graph of instructions, a LTL code is a graph of basicblocks, each basicblock being represented as a list of instructions: the instructions within the basicblock do not have any successor pointer, except for the final instruction. Unconditional jumps are represented by a Lbranch instruction.
- The registers are allocated, so the registers appearing in LTL directly correspond to machine registers (there is only a finite number of them).
- To handle spilling registers into the stack, two new instructions Lgetstack and Lsetstack are introduced, which respectively get a value from the stack and set a value on the stack, at a given position.

The Linear representation is like LTL, except that this time, the control-flow graph has been flattened. A Linear code is a list of instructions, with the same instructions as LTL, except for two new instructions that are added to keep the control-flow intact: Llabel, defining a label (an additional entrypoint), and Lgoto, defining an unconditional jump to one of the defined labels. The semantic of Linear is then much like Mach: the list of instructions composing the function is executed, instruction by instruction, until a Lgoto is encountered — the list of instructions is then refreshed to contain the list of instructions starting from the corresponding Llabel instruction. If a Lcond is encountered, and the condition evaluates to false, the semantic of the Lcond is to simply ignore the instruction and execute the rest of the list.

One way to translate a LTL code into Linear is to concatenate the list of instructions of each basicblock together (along a certain order), and then inserting Lcond, Lgoto and Llabel instructions accordingly to preserve the control-flow structure of the original graph.

However, one must be careful to give a "good order": being careless could lead to bad performance. Indeed, in most architectures, unconditional jumps are not free to execute: not only do they incur a cycle penalty for some architectures (due to introducing a gap in the processor pipeline), they also might invalidate parts of the instruction cache if the jump bridges two memory addresses too far apart. In the case of the KVX, an unconditional jump induces a penalty of 1 cycle in the best-case scenario.

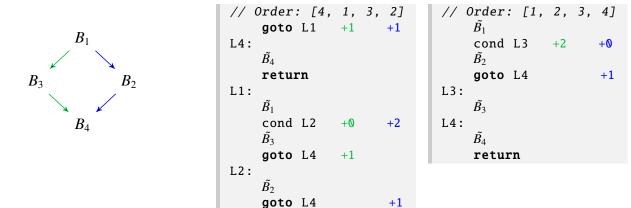


Figure 8.6.: Two possible code layouts for the LTL code shown on the left. Each code layout is annotated with branching penalties from two possible executions: either through B_3 (green) or through B_2 (blue). On average, the layout on the right has less branching penalties than the layout on the left.

Another thing to consider is that in most architectures, conditional branches work the following way: either the condition is evaluated to true, in which case a jump is performed to a particular label; or the condition is evaluated to false, then the next instruction is executed (as if the conditional branch instruction was a nop instruction). For the KVX, if the conditional jump is taken, a 2 cycles penalty is suffered in the best-case scenario. No penalty is induced if the conditional jump is not taken. The positioning of code can then significantly impact the performance speedup, especially when considering hot loops (loops in which the program spends a significant amount of time) that have only a few cycles of execution time.

I give in figure 8.6 an example of possible orders for basicblocks, on a simple code composed of four basicblocks B_1 , B_2 , B_3 and B_4 . I denote \tilde{B}_i as B_i without its final instruction (\tilde{B}_i can be possibly empty). The presented code could typically be the result of a if/then/else construct. The execution flow goes either through B_3 , or B_2 , but there is no way to know which, at compile time. I annotated the Linear code with the branch penalties, distinguishing between the two execution cases: the first column indicates the penalty induced by the path through B_3 , the second indicates the penalty caused by the path through B_2 . The Linear code from the left would lead to either 2 cycles of penalty when going through B_3 or 4 cycles of penalty when going through B_2 . On the other hand, the code on the right would lead to either 2 cycles of penalty when going through B_3 , or 1 cycle when going through B_2 : in average, much fewer cycles would be spent jumping!

In CompCert, the Linearize pass is separated into two parts: an untrusted oracle in OCAML that returns the order in which the basicblocks should be laid out, and the actual transformation that takes the order from the oracle and inserts Lgoto, Llabel and Lcond accordingly to preserve the LTL control-flow.

The untrusted oracle has the following type:

```
Parameter enumerate_aux: LTL.function → PMap.t bool → list node
```

Given a function from LTL (which contains, in particular, the LTL code and entrypoint), and also given a node to bool mapping indicating whether a given node is reachable ³, the oracle should return an order encoded by a list of nodes.

The only constraint of the order returned by the oracle (verified *a posteriori*) is that each reachable node from LTL must appear once in the order.

In subsection 8.3.1 I describe the original heuristics used by CompCert; then in subsection 8.3.2 I detail why the original heuristics might not be a good fit for superblocks, and my modifications to make them better for superblocks.

8.3.1 Original Linearize heuristics from CompCert

The original Linearize heuristics used by CompCert builds up chains of basicblocks that each have only one predecessor and one successor (except for the first basicblock of the chain). Each basicblock of the chain is then laid out contiguously in the returned order. When a join point (a basicblock with more than one predecessor) is met, the chain is broken, and a new chain starts. When a basicblock with more than one successor (such as a conditional branch) is met, the chain ends; new chains start from each of the successors.

Much like RTL, in a LTL code, each basicblock has an associated integer (the node): the LTL code is then a mapping from integers (nodes) to their content (basicblocks). When constructing a chain, the lowest node (by integer order) of its basicblocks is recorded. The final order is then computed by laying out each chain by decreasing order of their respective lowest nodes.

I represent the original heuristics of CompCert by the algorithm 12 below. The actual implementation is different, as it is written in a recursive way instead of iterative, but the core idea remains the same.

The function build_chain bridges together as many basicblocks as it can, stopping before a join point is reached or when a basicblock with more than one successor is met. Then, the successors of the last basicblock are added to the nodes to visit, and the building of another chain starts. While building a chain, the node's minimum value is stored: the chain is then annotated

³The Linearize oracle from CompCert does not actually use this parameter: unreachable nodes are naturally left out by the underlying algorithm from the oracle.

Algorithm 12. Original Linearize oracle ("enumerate_aux" in the Coq source)

```
1: function ENUMERATE(f)
 2:
         visited \leftarrow \emptyset
 3:
         join\_points \leftarrow compute\_join\_points(f)
         function GET_NEXT_PC(pc)
 4:
              match last_instruction_of(pc) with
 5:
                   case Lbranch s
 6:
 7:
                        return (Some s, [])
 8:
                   case i
 9:
                        return (None, successors(i))
         function Build_chain(pc)
10:
              chain \leftarrow []
11:
              minpc \leftarrow pc
12:
              while true do
13:
                   chain += pc
14:
15:
                   visited \leftarrow visited \cup pc
16:
                   if minpc > pc then
17:
                        minpc \leftarrow pc
                   (npc, nexts) \leftarrow get\_next\_pc(pc)
18:
                   match npc with
19:
                        case None
20:
21:
                             break
22:
                        case Some npc
                             if n \in join\_points then
23:
                                  break
24:
25:
                             pc \leftarrow npc
              return (chain, minpc, nexts)
26:
         to_visit ← [ entrypoint ]
27:
         while to_visit \neq \emptyset do
28:
29:
              pc \leftarrow to\_visit.pop()
              if pc \in visited then
30:
                   continue
31:
              (chain, minpc, nexts) \leftarrow build\_chain(pc)
32:
              to_visit += nexts
33:
              chains += (minpc, chain)
34:
         chains ← chains sorted by decreasing order of minpc
35:
                                                                  ▶ Concatenating each chain together
36:
         return flatten(map(snd, chains))
```

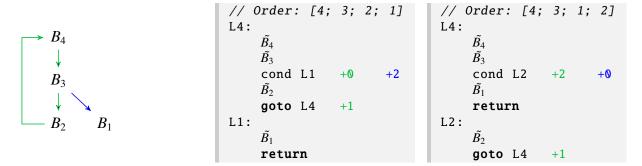


Figure 8.7.: Two possible code layouts for the LTL looping code shown on the left. The left layout is from the original CompCert heuristics, while the right layout is from a hypothetical heuristics where the chains are laid out in increasing order.

with this value. The chains are then ordered by this minpc value (by decreasing value), and then, they are flattened into one list of nodes.

The following is my best guess as to why this algorithm works well (and is a good fit, in general, for CompCert).

I believe this algorithm works reasonably well for CompCert, mainly because the nodes are generated so that the body of a loop will always have node identifiers greater than those of the exit branch of a loop. More formally, I think these heuristics work in numerotations such that each pair (A, B) of strongly-connected components verify the property: "if a successor of A is in B, then each node of A has an identifier greater than the nodes of B".

The RTLgen pass generates such a well-structured code by initiating code generation for loop exits before handling the loop body. The Renumber pass is then careful to preserve this structure.

To illustrate these heuristics, I give a simple loop in figure 8.7, where I note B_i the basicblock of node i. I give two possible code layouts: on the left, the one given by the original CompCerr heuristics; on the right, what would have happened if the heuristics had selected an increasing order instead of decreasing (in both cases, the basicblocks B_4 and B_3 are in the same chain, so they are laid out contiguously).

Without any branch prediction information, CompCert heuristics chose to privilege the basicblocks within the loop on their own: this was the right choice since it only incurs 1 cycle of penalty when looping (assuming the code does take the loop most of the time). The other solution, consisting of laying out the exit branch first, would incur 3 cycles of penalty when looping, which would be very detrimental.

8.3.2 Modifications to the heuristics for superblocks

CompCert already naturally makes the right call for laying out code from loops. However, there are two issues when taking into consideration superblocks:

- Even though we are lucky to have a fair Linearize for loops, this is only the case if the code indeed follows a numbering where the loop body nodes have a greater value than the nodes of the exit branch. This property could be potentially undermined by future optimizations.
- The issue remains when considering non-looping branches that were predicted: the original Linearize heuristics, clueless for such branches, may get a wrong guess and layout the wrong branch first.

Some work exists to solve the general of code positioning, such as Pettis and Hansen [72], that rely on branching edge frequencies to devise a good positioning. Since we do not have exact frequencies in our representation, I settled for a much simpler solution that would extend the existing heuristics for superblocks without incurring any performance downgrade compared to the original heuristics when no branch prediction is provided.

The solution consists in modifying what I named get_next_pc in algorithm 12. The new function is in algorithm 13.

Algorithm 13. Modified get_next_pc for superblocks

```
1: function GET_NEXT_PC(pc)
2:
        match last_instruction_of(pc) with
3:
             case Lbranch s
4:
                 return (Some s, [])
             case Lcond c _ ifso ifnot prediction
5:
                 match prediction with
 6:
                     case None
 7:
                          return (None, [ifso, ifnot])
 8:
                      case Some true
9:
10:
                          return (Some ifso, [ifnot])
                     case Some false
11:
                          return (Some ifnot, [ifso])
12:
13:
             case i
                 return (None, successors(i))
14:
```

Another modification: instead of recording the minimum PC of the chain, the PC of the first block of the chain is recorded. I have measured a slightly better performance in some instances, though it's mostly negligible for most of the benchmarks.

Through experiments (see chapter 10), I ensured that this new version indeed provides only slightly worse performance in the worst case. ⁴

8.4 Static branch prediction

Static branch prediction (in the absence of profiling information) is the most critical heuristics of those presented in this chapter: an inaccuracy in branch prediction could result in a significant loss of performance due to the above heuristics taking wrong decisions.

In our case, we want a branch prediction that is both reasonably accurate (as few false positive as possible) and yet permissive enough to allow for certain straightforward formations (such as loops) to be detected correctly. In particular, detecting the conditional branches of innermost loops is of great importance to us: this is where our optimizations will have a more significant impact. A bad prediction on an innermost loop conditional branch would imply an impossibility to unroll it, or rotate it, or schedule it properly (since the header would then be on a different superblock than the body).

I based my work on Ball and Larus [4], in which several heuristics are given to infer the preferred direction of a given branch. I first briefly describe in 8.4.1 my implementation of the heuristics presented in Ball and Larus [4], then I introduce a new heuristic that I use for conditional branches within loops in 8.4.2.

8.4.1 Implementing Branch Prediction for Free

The heuristics of Ball and Larus [4] are described assuming an intermediate representation consisting of a control-flow graph of basicblocks. Then, a lot of their heuristics involve checking the instructions of the basicblock for specific properties. In our case, this would be more directly suited to the LTL representation. Still, we can adapt it to RTL easily. Instead of iterating through the instructions of a basicblock to check a property, we can traverse the control-flow graph node by node until we encounter an instruction with multiple successors.

For each conditional branch instruction encountered, we can then check each of its edges to look for the properties used by the original paper. The first (and perhaps most important) property is for loop conditional branches: if a conditional branch has a backedge and a forward edge, they predict the backedge. Indeed, the backedge will be the edge used for looping; also, in general, and for a given loop, we loop more often than we exit the loop.

⁴A funny note: it is through debugging the new Linearize oracle performance that I was able to rule out many bugs related to faulty branch prediction. Performance bugs are rarely where you would expect them to be.

Some others of these properties involve checking the branch for the presence of certain classes of instructions like a return, a call, or a store. There is also a heuristic based on the comparison of the conditional branch: e.g. if it's a "less than 0" comparison, one might assume it is an error-checking branch and that the condition will not be taken most of the time.

Each heuristic is applied following a specific order - if no heuristic is successful, the branch is randomly predicted.

I have a certain number of differences compared to the original paper:

- I do not perform any random prediction when no heuristic applied: trying to over-predict proved experimentally detrimental to the performance, compared to just leaving the branch as unpredicted.
- Similarly, I found that the store heuristic was giving too many false positives: the average performance across our benchmarks was better with the store heuristic deactivated.
- I modified the recommended order of heuristics: doing the heuristics in the order [opcode, return, loop, call] proved to be more performant.
- I did not implement the guard and pointer comparison heuristics for time reasons (they are more complex to implement). However, implementing them in the future could improve a bit the performance.

Another difference is that I modified the loop heuristic (checking whether the branch is a backedge) because it was unfit for CompCert. Indeed, in CompCert, the conditional branches are placed at the beginning of the loop, not at the end: both of their branches are then forward edges (not backedges). The actual backedge happens on the last instruction of the loop. So the loop heuristic, as described in the original paper, would have no impact on our case.

In the following subsection, I describe my modification for loop branches prediction to account for this issue.

8.4.2 A new heuristic for predicting branches inside loops

In CompCert, loops consist of the loop header, then the conditional branch (possibly exiting the loop), then the actual loop body, which then jumps back to the loop header. In our case, the loop heuristic of Ball and Larus [4] would only work for simple innermost loops containing a single basicblock. As soon as there would be branches within the loop (such as a if (cond) break; construct, or nested loops), both the loop conditional branch and the other branches would not be predicted.

To tackle this issue, my new heuristics rely on computing the body of a given loop (computing the instructions that are part of the loop). This is done by first computing the backedges, then

applying an algorithm to deduce the natural loop spawned by the backedge (I use the Nat_Loop algorithm from figure 7.21, page 192, of Muchnick et al. [66]). The list of all loop bodies is computed by the get_loop_bodies function, not detailed here.

The new heuristic is then implemented through the get_loop_info function (algorithm 14): it outputs a loop_info mapping from nodes to predictions, which is then directly consulted by my new loop heuristic.

Algorithm 14. Predicting conditional branches inside loops

```
1: function GET_LOOP_INFO(code, entrypoint)
 2:
         loop_bodies ← get_loop_bodies(code, entrypoint)
         loop\_info \leftarrow \{ all \mapsto None \}
 3:
         foreach body ∈ loop_bodies
 4:
              foreach n \in body
 5:
 6:
                  match code[n] with
 7:
                       case Icond _ _ ifso ifnot _
                            if loop_info[n] \neq None then
 8:
 9:
                                 continue
                            b1 \leftarrow (ifso \in body)
10:
                            b2 \leftarrow (ifnot \in body)
11:
                            if b1 && b2 then
12:
13:
                                 continue
14:
                            else if b1 then
                                 loop_info[n] := Some true
15:
                            else if b2 then
16:
                                 loop_info[n] := Some false
17:
18:
                       case _
                            continue
19:
20:
         return loop_info
```

I verified on most of our benchmarks that the loops were indeed correctly predicted and that if (...) break constructs did not break the prediction.

Implementing the Scheduling Oracles

Chapters 3 and 7 indicated how we formally verify a scheduling respectively for basic blocks (at Asm level) and superblocks (at RTLpath level). In this chapter, I briefly describe the inner workings of our scheduling oracles.

For this thesis, we are interested in scheduling an in-order VLIW pipelined processor (though the scheduling can also be applied to other pipelined in-order processors, not necessarily VLIW). I refer the reader to chapter 1 for a description of the KVX core pipeline and the definition of VLIW and in-order processors.

Given a set of n instructions to be executed sequentially, scheduling is the problem of finding an execution order which minimizes the execution time without making the code incorrect. Formally, we want to compute a function $t:0...n-1 \to \mathbb{N}$ assigning a time slot to each instruction. These time slots are used to reorder instructions accordingly; or, in the case of basic block scheduling, producing bundles: the first bundle has all instructions j such that t(j) = 0, the next bundle has all those such that t(j) = 1 etc.

This schedule must satisfy several classes of constraints, given below.

• Semantic and Latency Dependencies

Read and write dependencies are examined for each processor register, as well as memory. In both schedulings, we consider that a store always invalidates the whole memory (not just the address of the store) since our verifiers do not have any memory alias analysis yet. For the sake of expressing the dependencies below, the memory is treated like a register.

- Read after write: If instruction j writes to register r and this is the last write to r before an instruction j' reading from r, then the schedule should respect $t(j') - t(j) \ge c(j, j')$, where c(j, j') is the latency (in number of cycles) it takes for j' to be able to read the content of register r. Since certain instructions read their registers at different stages of the pipeline, and since some instructions take longer to compute their result than others, this latency depends on both j and j'. We computed those latencies by reading the KVX microarchitecture documentation. Since the KVX processor is interlocked, a wrong latency value will only incur a worse performance; it will not

- affect the architectural semantics (the processor will stall if the operand is not ready to be read yet).
- Write after write: If instruction j writes to register r and this is the last write to r before an instruction j' writing to r, then the schedule should respect $t(j') t(j) \ge c(j, j')$, with c(j, j') described above.
- Write after read: If instruction j reads from r, the next write to r is instruction j', then $t(j') t(j) \ge 0$. Consequently, in the case of the KVX core, it is possible to have both a register read from r, and a register write to r in the same bundle.

• Resource Usage Constraints

The processor has a limited number of processing units. Therefore, a bundle of instructions must not request more processing units of a given kind than available. Also, there is a limit on the number of instruction words ("syllables") inside a bundle. The assembler rejects bundles that do not abide by these rules.

The architecture documentation describes these limitations as a constant vector of available resources $\mathbf{r} \in \mathbb{N}^m$ and, for each instruction kind k, a vector $\mathbf{u}(k) \in \mathbb{N}^m$. The constraint is that the sum of all $\mathbf{u}(K(j))$ for all instructions j scheduled within the same bundle i should be coordinate-wise less than or equal to \mathbf{r} .

These constraints are computed by a *scheduler frontend*, dependent on the IR level used for scheduling (namely, RTLpath or Asmblock), and given to a *scheduler backend*, independent on the IR used. This allows reusing the scheduling algorithms between the postpass and prepass. Also, most of the prepass scheduler frontend is independent of the target architecture to be reused for others, such as Arm or Risc-V.

First of all, I describe in section 9.1 the postpass scheduling: the frontend, then which backend algorithm we use. Then, I describe in section 9.2 the prepass scheduling: the frontend and which backend algorithms are available.

A significant portion of the work presented in this chapter was done by David Monniaux: the scheduling backend used by both schedulings and part of the frontend for superblock scheduling. I developed the frontend for basic block scheduling, part of the frontend for superblock scheduling, and conducted experiments to analyze the performance of the scheduled code (in chapter 10).

9.1 Postpass Scheduling Oracle

For basic block scheduling (whose formal verification is shown chapter 3), the scheduling oracle has the following CoQ type:

```
Axiom schedule: bblock \rightarrow (list (list basic)) * option control
```

Given a basic block, the scheduling should return a list of bundles (a bundle is a list of instruction), and optionally a control-flow instruction that is to be attached to the last bundle (the last bundle can be possibly empty to emulate a control-flow instruction being alone in its bundle if that is the wish of the scheduler).

To get this result, first, the bblock is analyzed to extract the instruction dependencies and the resource vectors of each instruction, as well as possibly separating builtins from the basic block (subsection 9.1.1). Then, the backend operates through an algorithm that can be changed through the compiler options (subsection 9.1.2). Finally, the frontend interprets the result of the backend to pack it into the type required by the Coo module PostpassScheduling (not detailed here).

This work was initially done only for the KVX architecture, but it is possible to adapt the postpass scheduling verifiers and oracles to other architectures. Recently, this work has been ported to AArch64 by Léo Gourdin, Sylvain Boulmé and David Monniaux (see section 2.2 of Six et al. [89]), which provided non-negligible performance improvements (performance gain of about 10%).

9.1.1 Postpass frontend

The frontend is in charge of giving correct information to the scheduler about the following:

- The resource vectors. These should not be under-specified, and it's better if they are exact. Suppose the resource vectors are under-specified (too few resources is allocated to a given instruction, whereas in reality, the instruction consumes more). In that case, it might incur a compilation failure from the assembler because of a bundle using too many resources. If, on the contrary, the resource vectors are over-specified, this would result in an under-optimized code because of missed scheduling opportunities.
- The latency dependencies. These should be enough to output a correct code, and it's better if they are exact. If too few latency dependencies are given, the output code might have a different execution result: our scheduling verifier would return an error. If, on the contrary, too many latency dependencies are given, the output code might be underperforming because some instructions would not be packed into bundles as they should.

I show in figure 9.1 an example of a basic block, along with the resource vectors (on a simplified model of the KVX), and the dependency graph:

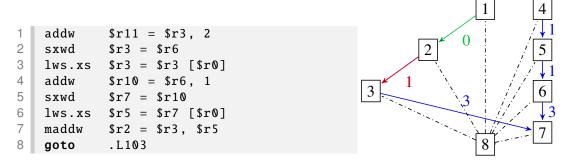


Figure 9.1.: Example of dependency graph. The Read-After-Write dependencies are in black; the Write-After-Write are in red. The dashed edges represent a dependency of latency 0.

- The instruction 2 has a write in \$r3 while the instruction 1 makes a read to \$r3: this incurs a Write-After-Read dependency, of latency 0. As a result, instructions 1 and 2 might be in the same bundle, but instruction 2 should never be scheduled before instruction 1.
- The instruction 3 has both a Write-After-Write and a Read-After-Write with instruction 2, regarding register \$r3. In that case, instruction 3 has to be scheduled at least one cycle after instruction 2: the duration of one cycle corresponds here to the time required for \$r3 to be available for the lws.xs instruction.
- The memory load instructions (3 and 6) each incurs a Read-After-Write dependency of 3 cycles: this is the duration required for a value to be fetched from memory, assuming that value is in the cache.
- The instruction 8 is a particular case: since it changes the control flow, it might not be scheduled before any other instruction. But it is still possible to schedule it simultaneously as a given other "basic" instruction. We model it by a dependency edge of latency 0.

The frontend computes these dependencies using a simple dependency analysis described in algorithm 15. Each instruction is examined in turn: their read and written registers are checked for RAW/WAW/WAR dependencies in regards to the previous accesses of the registers in read or write. These previous accesses are stored in the variables written and read, which are updated after each instruction is done analyzing. During this update, a write invalidates all the reads of a given register (if instruction 1 reads a given register, and instruction 2 writes to that same register, there is no need to keep track of the read of instruction 1). Finally, pseudo-WAR latencies are added from any basic instruction to the control-flow instruction to ensure the control-flow instruction remains at the end.

The frontend also computes the resources required by each instruction: for the KVX, the tables are available in its internal documentation.

Algorithm 15. Computing dependencies on the basic block

```
1: function GET_ACCESSES(source_of, locations)
 2:
         accesses \leftarrow []
 3:
         foreach loc \in locations
 4:
              accesses += source_of[loc]
 5:
         return accesses
 6: function GET_DEPENDENCIES(instructions)
         edges \leftarrow []
 7:
 8:
         written \leftarrow \{ \}
 9:
         read \leftarrow \{ \}
         foreach i \in instructions
10:
              raw \leftarrow get\_accesses(written, i.read\_locs)
11:
12:
              waw ← get_accesses(written, i.write_locs)
              war \leftarrow get\_accesses(read, i.write\_locs)
13:
14:
              foreach j \in raw + waw
                   edges += (j, i, latency(j, i))
15:
16:
              foreach j \in war
                   edges += (i, i, 0)
17:
              if is_control(i) then
18:
19:
                   foreach j \in instructions - [i] edges += (j, i, 0)
              foreach loc ∈ i.write_locs
20:
                   written[loc] := [i]
21:
                   read[loc] := []
22:
23:
              foreach loc \in i.read locs
24:
                   read[loc] += [i]
         return edges
25:
```

```
1
    type latency_constraint = {
2
      instr_from : int;
3
      instr_to : int;
4
      latency : int;
5
6
7
    type problem = {
        max_latency : int;
9
        resource_bounds : int array;
10
        instruction_usages: int array array;
11
        latency_constraints : latency_constraint list
      };;
```

Listing 9.1.: Definition of a scheduling problem

Finally, once the dependencies and resources are computed, it calls the backend, which returns a schedule, and translates that schedule into a list of bundles (two instructions scheduled at the same cycle are bundled together), which is returned back to the Coo verifier.

9.1.2 Postpass backend

The scheduler backend operates on a type abstracting only the necessary information, named problem (listing 9.1).

A scheduling problem is encoded with:

- A vector of available resources of the processor. If no such information is available, it is possible to give an empty array so that the scheduler will disregard resource constraints.
- An array of resource vectors. The array represents the list of instructions to schedule: to each instruction corresponds the resource vector required by the instruction.
- The latency constraints, encoded as a list of (from, to, lat) tuples where an instruction to must wait at least lat cycles after from in the schedule. This encodes a graph of dependencies where the nodes are the instructions to be scheduled (the indices of instruction_usages), and the edges are the latency dependencies. If there is a constraint of latency 0 between f and t, this means that the instruction t cannot be scheduled before instruction f (but they may be scheduled at the same time, to be in the same bundle).

Our default solver is based on a variant of Coffman-Graham list scheduling (see Dupont de Dinechin [25] and §5.4 of Micheli [62]) with one heuristic: instructions with the longest latency path to the exit get priority. This is fast (quasi linear-time) and computes an optimal schedule in almost all practical cases.

To analyze the impact of list scheduling, we conducted the following experiments:

- David Monniaux implemented the reduction of the scheduling problem to Integer Linear Programming, or pseudo-Boolean linear optimization, solved by an external tool (e.g. Gurobi). This showed that linear scheduling indeed returns an optimal schedule across almost all of our benchmarks for the scheduling model that we use. More details can be found in Six et al. [88], appendix D.
- I compared the performance results with a greedy scheduler that packs instructions into bundles without reordering them and with a trivial scheduler returning one instruction per bundle, without any reordering. The results of this comparison are in chapter 10.

9.2 Prepass Scheduling Oracle

The prepass oracle has the following Coq type:

```
Axiom untrusted_scheduler: RTLpath.function → code * node * path_map * (PTree.t node)
```

There are several differences compared to the postpass oracle type:

- The oracle performs scheduling of a whole RTLpath function, instead of just one block. However, the oracle does not have to recompute the blocks to schedule: these are taken directly from the pathmap of the RTLpath function.
- The scheduling is done on the scope of a superblock, instead of a basic block: there will be additional latencies compared to a basicblock.
- The list of instructions to schedule has to be computed from the RTL control-flow graph.
- Unlike Asm, we do not know the exact resources and latencies of each RTL instruction. We have to make educated guesses.

To tackle these differences but still reuse the backend of postpass scheduling, we used the code architecture given figure 9.2.

- InstructionScheduler is the postpass backend that also serves as the backend for the prepass. In addition to list scheduling, David Monniaux added reverse list scheduling and zigzag scheduling, which I informally describe in subsection 9.2.2.
- PostpassSchedulingOracle is the postpass frontend, that was described in section 9.1.2.
- Opweights is a new module for prepass written by David Monniaux that gives an educated guess of the resources and latency of each operation, condition, load and store. It uses some functions of the Asmblockgen module (part of the assembly backend for KVX) for getting an approximate translation of the concerned RTL instructions. Then, part of the

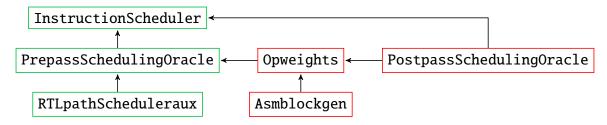


Figure 9.2.: Our code architecture for implementing the schedulers. The architecture-dependent parts are in red, the architecture-independent parts are in green.

PostpassSchedulingOracle module is used for getting the used resources and underlying latency. When a given operation would be translated into several assembly instructions, only the first instruction is taken into account. This gives an under-approximation of the actual latency and resource cost. In the future, this could be probably more finely tuned to give more accurate approximations.

- Since we work on whole CFGs instead of instruction lists, the RTLpathScheduleraux module does the junction of translating CFGs into lists of instructions to schedule and then modifying the CFG based on the schedule returned by the scheduler. It also turns trapping loads into non-trapping loads as necessary, based on whether they were scheduled before a given conditional branch.
- PrepassSchedulingOracle, implemented by David Monniaux, computes the dependencies and latencies in much the same way as our postpass frontend, except that it uses the approximated resources and latencies from Opweights, and adds additional dependencies for the conditional branches (see subsection 9.2.1). It also introduces zigzag scheduling as the combination of a forward and a backward list scheduling (see subsection 9.2.2).

Out of these newly introduced modules for prepass, only Opweights is target-dependent and needs to be readapted for each architecture. Compared to postpass, this allows having a prepass scheduling almost "for free" for any architecture supported by CompCert, as long as the approximated latencies/resources are entered in an Opweights module. David Monniaux, in particular, implemented an Opweights for RiscV and Aarch64, so our prepass superblock optimization can also be used on these architectures.

9.2.1 Additional dependencies for conditional branches

The scheduler should be careful to not schedule instructions that might trap on top of conditional branches. If the instruction may trap (this is the case for non-speculative memory loads, memory stores, and certain operations such as integer division or modulo), then an additional dependency of latency 1 is added between the instruction and the last conditional branch above the instruction.

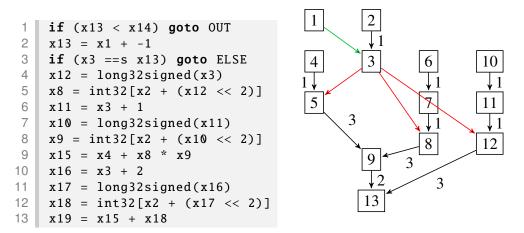


Figure 9.3.: Example of dependency graph of a superblock, for architectures that do not have speculative loads. The usual RAW dependencies are in black, the extra conditional branches dependencies coming from trapping instructions are in red, the additional dependencies between the conditional branches are in green.

Also, since our superblock verifier compares each exit states two-by-two, the scheduler must keep the conditional branches in the same order: a conditional branch might not be scheduled on top of another. This is handled by adding additional dependencies of latency 1 between each successive conditional branch.

I give in figure 9.3 an example of linearized RTL code with two conditional branches. Compared to a typical code from Asm, there is barely any Write-After-Read or Write-After-Write dependencies, thanks to the infinite amount of registers available. This makes less constraint for scheduling. To account for the conditional branches, two constraints are added: an edge of latency 1 between instructions 1 and 3, to conserve the order of conditional branches; and an edge of latency 1 between 3 and the load instructions, to ensure these are not scheduled before (though, in the case of the KVX, these edges are not added: instead, we make the memory loads speculative).

9.2.2 Prepass scheduling algorithms

We have three possible prepass scheduling algorithms available:

- Forward list scheduling: the same algorithm from the postpass scheduling, filling the time slots greedily, with the heuristic of privileging the longest execution path when given the choice.
- Backward list scheduling: forward list scheduling, but applied on a reverse problem where
 the edges from the dependency graph have been inverted, and the timeslots are allocated

- backwards. As was briefly presented in 4.3.2, the advantage of backward list scheduling compared to forward scheduling is to decrease register pressure.
- Zigzag scheduling: it uses forward scheduling to place the conditional branches, then locks
 them on particular timeslots by using special dependencies, and runs backward scheduling.
 This was an attempt at implementing a mix between forward scheduling, which tends to
 deliver better schedules when register allocation is not taken into account, and backward
 scheduling, which balances it out.

Compared to postpass scheduling, there is no bundling here: and yet, an order has to be chosen for instructions scheduled at the same time slot. We arbitrarily keep the instructions within the same time slot in the same order as they originally appeared in the superblock. ¹

To illustrate these different schedules, I give in figure 9.4 the result of the three schedules on the code given earlier in figure 9.3, for the KVX architecture (supporting speculative loads: so the extra conditional branch dependencies are ignored).

Since we only have few dependencies, the list scheduling can schedule many instructions from the first timeslot (instructions 1, 4, 6 and 10). The stalls from the load instructions 5 and 8 are partly mitigated (no stall for 5, one stall for 8). In this example, and according to our approximated latencies, list scheduling would result in the last instruction being scheduled at timeslot 7. This is a good time. However, a disadvantage of list scheduling can be seen: a lot of registers are alive at each given time. For instance, the register x12, x11, x16 and x13 are both alive at timeslot 0.

Reverse list scheduling gives a schedule with a similar final timeslot (the last instruction is also scheduled at timeslot 7), but fewer registers are alive at a given time: for the timeslot 0, only the registers x12 and x11 are live. However, since the schedule was done in reverse, the conditional branches that are usually at the beginning of the block find themselves at the end, so if our predictions end up incorrect, we will get a significant performance penalty (a lot of instructions executed that end up being discarded).

Zigzag scheduling fixed the conditional branches to the timeslots that were predicted in forward scheduling and then tried backward scheduling with these additional constraints. With zigzag scheduling, we have fewer instructions scheduled before conditional branches. Still, we pay the tradeoff with a higher latency: the final instruction is scheduled at timeslot 8 (instead of timeslot 7 for the other two scheduling).

We measured the impact of each of these three scheduling on the KVX and other architectures in chapter 10: for the KVX architecture, list scheduling gives slightly better results than reverse

¹This could be slightly improved by ordering the basic instructions before a conditional branch (as long as it respects the WAR dependencies) when they all are affected to the same timeslot: the postpass scheduling would then be able to bundle the instructions with the conditional branch.

```
// List: [0 \mapsto \{1, 4, 6, 10\};
                                              // Rev: [0 \mapsto \{4, 6\}; 1 \mapsto \{5, 7\};
      1 \mapsto \{2, 5, 7, 11\}; 2 \mapsto \{3, 8\}
                                                     2 \mapsto \{8, 10\}; 3 \mapsto \{11\};
                                               //
      3 \mapsto \{12\}; 5 \mapsto \{9\}; 7 \mapsto \{5\}]
                                                     4 \mapsto \{12\}; 5 \mapsto \{9\};
                                               //
1: if (x13 < x14) goto OUT
                                               //
                                                     6 \mapsto \{1, 2\}; 7 \mapsto \{3, 13\}]
    x12 = long32signed(x3)
                                                   x12 = long32signed(x3)
                                               4:
    x11 = x3 + 1
                                                   x11 = x3 + 1
6:
10: x16 = x3 + 2
                                                  x8 = int32.s[x2 + (x12 < 2)]
2: x13 = x1 + -1
                                               7:
                                                  x10 = long32signed(x11)
  x8 = int32.s[x2 + (x12 < 2)]
                                               8: x9 = int32.s[x2 + (x10 \ll 2)]
7: x10 = long32signed(x11)
                                               10: x16 = x3 + 2
11: x17 = long32signed(x16)
                                               11: x17 = long32signed(x16)
3: if (x3 == s x13) goto ELSE
                                              12: x18 = int32.s[x2 + (x17 < 2)]
8: x9 = int32[x2 + (x10 \ll 2)]
                                                   x15 = x4 + x8 * x9
12: x18 = int32[x2 + (x17 < 2)]
                                               1:
                                                  if (x13 < x14) goto OUT
9: x15 = x4 + x8 * x9
                                               2:
                                                   x13 = x1 + -1
13: x19 = x15 + x18
                                               3: if (x3 == s x13) goto ELSE
                                              13: x19 = x15 + x18
// Zigzag: [0 \mapsto \{1\}; 1 \mapsto \{2, 4, 6\}; 2 \mapsto \{3, 5, 7\}; 3 \mapsto \{8, 10\};
      4 \mapsto \{11\}; \ 5 \mapsto \{12\}]; \ 6 \mapsto \{9\}; \ 8 \mapsto \{13\}]
   if (x13 < x14) goto OUT
2:
    x13 = x1 + -1
    x12 = long32signed(x3)
    x11 = x3 + 1
  if (x3 == s x13) goto ELSE
5: x8 = int32[x2 + (x12 \ll 2)]
7:
   x10 = long32signed(x11)
8: x9 = int32[x2 + (x10 \ll 2)]
10: x16 = x3 + 2
11: x17 = long32signed(x16)
12: x18 = int32[x2 + (x17 < 2)]
9: x15 = x4 + x8 * x9
13: x19 = x15 + x18
```

Figure 9.4.: Our three possible prepass scheduling on the previous example. The code is annotated with the initial position of each line of code for clarity. I also show the "time → instructions" mapping of each schedule. The conditional branches are outlined in red. The load instructions are marked in green, and the conditional branches in red, for easier recognition.

list scheduling; for the other architectures, reverse list scheduling tends to provide better results, although it is very dependent on the benchmarks.

10

Experimentations

I introduced in the previous chapters formally verified techniques to optimize the generated code from CompCert: the basicblock scheduling from chapters 3 and 9, the loop unrolling and loop rotation from chapters 6 and 8, the superblock linearizer from chapter 8, and finally, the superblock scheduling from chapters 7 and 9.

In this chapter, I evaluate the impact of each of these optimizations, mainly on the KV3 architecture and other architectures such as AArch64 and RiscV, thanks to the porting efforts of Léo Gourdin, Sylvain Boulmé, and David Monniaux (see Six et al. [89]). Throughout my thesis, I focused only on the KV3 architecture.

I first present the benchmarks used and the means of measuring performance in section 10.1. Secondly, I study the impact of the postpass scheduling on KV3 and its experimental time complexity in section 10.2. Then, I look in section 10.3 the impact of all optimizations related to superblock scheduling: superblock linearization, the effect of loop unrolling, rotation; I also study the impact of Loop Invariant Code Motion, introduced by D. Monniaux [63]. Finally, I do a performance breakup of our best version of CompCert compared to GCC in section 10.4.

10.1 Experimental setup

Evaluating the performance of a given optimization has a certain number of challenges.

A given optimization might affect the performance impact of another optimization. A typical example: when developing the first iteration of superblock scheduling, I found that the performance was overall not as good as I would have imagined it. In some cases, it was even detrimental. My first thought was that probably there were bugs in the scheduler or some wrong latencies. But the actual reason was just that there had been a bug gone unnoticed in the static branch prediction. As a result, some loops were mispredicted, resulting in a superblock crossing the loop instead of staying within. As a result, instructions that did not belong to the loop found themselves inside it: we had achieved reverse loop-invariant code motion, in a way. Because of this issue, it is essential to have a way to easily examine the assembly generated by any benchmark so that the assembly code might be easily looked up on any benchmark producing abnormal performance.

For specific optimizations, it is not clear which "way" is better. For instance, both list scheduling, reverse list scheduling and zigzag scheduling have their strengths and weaknesses, but it is impossible to know before experimenting. This experimentation has to be done on a significant number of benchmarks because a given scheduling method might be biased for a specific source code pattern. Also, there must be a way to easily compare different sets of flags.

Finally, throughout my thesis, we asked ourselves the following question: "which optimizations can we implement to bridge the gap as best as we can, within the time and resources that we have". In some cases, looking at the code generated by the other compilers (GCC and LLVM) has been a way to try to infer what was missing from our version of CompCert and then try to close the gap a little bit further. For this reason, it was essential to have our benchmarks also compiled with GCC and LLVM.

David Monniaux and I implemented a benchmark harness (not detailed here) working with "flattened" benchmarks (transformed in such a way that they can be compiled with simple rules). We implemented a standardized way of compiling, running and measuring all benchmarks, keeping track of all intermediate files (assembly, binary, standard output log files) from different compilers and different sets of flags. This facilitated our production of results, as well as our subsequent analysis.

I detail in this section the settings of our measurements: subsection 10.1.1 detail the processors used, subsection 10.1.2 points our method of measuring performance, and subsection 10.1.3 describes the benchmarks that we used.

10.1.1 Measured processors

Within the duration of this thesis, I measured the benchmarks on the KV3 processor which was presented in chapter 1. I recall the main characteristics here: it features a 6-issue VLIW architecture with an instruction pipeline of 8 stages. It has 64 general-purpose registers of 64-bits used for both integer and floating-point data (a given register can store an integer or a float). It also features support for scalar vectors and SIMD instructions. Still, we do not take advantage of that, except for some memory loads that we group into octuple and quadruple loads when it is fit, thanks to a peephole optimization coded by David Monniaux verified at the same time as basicblock scheduling. The instruction cache capacity is 16 kB, the data cache also has 16 kB. When performing a memory load, if the value is in the cache, only 3 cycles are required. ¹

¹If there is a cache miss, the data cache needs to perform a line refill: a refill stops any request to/from the data cache for approximately 20 cycles in most cases.

David Monniaux and Léo Gourdin also experimented on an ARM Cortex A53 (AArch64) inside a Raspberry Pi 3 and a Rocket RiscV core [56] running on an FPGA. Both run under a Linux operating system which produces some noise on the performance measures.

10.1.2 Measuring methods

For the benchmarks executed on the KV3 processor, we use the hardware performance counter of the number of cycles. Similar counters are used for AArch64 and RiscV. To prevent timing IO system calls (such as sending a message to the standard output), which can be very costly on the KV3, we isolate the computing part and measure only that part.

The KV3 is a predictable architecture as long as the execution remains within a compute cluster: in our case, executing several times one of our benchmarks gives the same result in the number of cycles. There is then no need to have multiple executions. However, for RiscV and AArch64, the benchmarks were executed 20 times each and averaged to reduce the measuring noise.

In some figures, I show the compilation time: these are either obtained through time counters added by instrumenting the generated OCAML code or using the already present time counters of COMPCERT.

I also provide some metrics to measure the validity of our static branch prediction: this was obtained by instrumenting the code to force a static prediction pass even when profiling was present and increment relevant counters based on the results from static branch prediction.

Finally, to study the impact of instruction cache misses for certain optimizations, I measured the number of cycles spent waiting for the instruction cache to deliver data to the prefetch buffer. This is done through a specific counter of the KV3 named "Prefetch Buffer Starvation Cycle", whose description in the manual is "+1 at every cycle during which a PFB (Prefetch Buffer) fetch request to the ICache is not granted by the latter".

10.1.3 Benchmarks used

We evaluated CompCert on approximately 90 different benchmarks. On AArch64 and RiscV, about a fourth of them were removed because their execution time was too low; they were too sensitive to the external environment (operating system). In particular, on RiscV, the experimental noise is significant. On KV3, we do not have this issue since there is no variation in the number of cycles across several executions, so they are all evaluated.

Polybench

The Polybench benchmarks include computational kernels, originally meant for benchmarking polyhedral optimizations [76]. I chose to port this benchmark to our harness because they are easy to benchmark and analyze. Thanks to their minimalistic structure, the computational part is clearly identified in all benchmarks and usually small length codes. Any performance issue is then relatively easy to track on the C source code to trace back the cause to our optimizations.

Polybench code typically includes one or several nested loops, with little to no branching within them.

TACLeBench

TACLeBench is a collection of benchmarks used for worst-case execution time research[27]. Compared to Polybench, they have a wider variety of code patterns. In particular, most of them feature branches within their hot computational part. Like Polybench, they feature several extracted kernels that are easy to analyze. Léo Gourdin recently ported this benchmark to our harness.

Handpicked benchmarks

David Monniaux originally started by gathering particular benchmarks of interest relevant to the Kalray KV3 core: critical embedded systems and computational benchmarks.

Among them, we have:

- radiotrans, convertible and heater-control: these are benchmarks compiled from synchronous dataflow programming languages (respectively Heptagon, Lustre v6 and Lustre v4). For instance, such languages are used to specify and implement fly-by-wire aircraft controls [9].
- lift: directly taken from TACLeBench
- *bitsliced-aes* and *sha-256*: cryptography primitives taken from Mosnier [64] and Patrick [71].
- *glpk* runs GLPK (GNU Linear Programming Kit [61]) on an example.
- picosat is an optimized SAT solver [11] ran over a Sudoku example.
- float-mat is a textbook implementation of floating-point matrix multiplication
- *float-mat-v2* is a version with loop unrolling done at the source level. Comparing *float-mat* and *float-mat-v2* typically gave us a first clue to the performance we could gain on a similar code, before implementing the optimizations.

• *jpeg-6b* is from the Libjpeg [48].

I denote these benchmarks as the **handpicked** benchmark.

10.2 Impact of postpass scheduling

In this section, we study the impact of our postpass scheduling optimization from chapter 3, both in performance and compilation times.

10.2.1 Performance

On KV3 core

Instruction Level Parallelism (ILP) is achieved through two means:

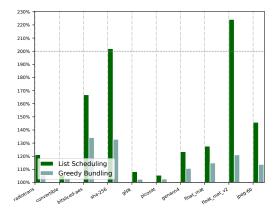
- Instruction pipelining: the KV3 has a pipeline of 8 stages (though in practice, only the first 4-6 stages are used most of the time). This many instructions can be processed simultaneously, given there is enough to feed the pipeline, and no stall (due to an interlock) is introduced.
- Issuing multiple instructions simultaneously: this is done through the VLIW design of the architecture. Up to 6 instructions can be issued together.

Unscheduled code, with only one instruction per bundle, can be expected to run quite poorly: not only is there only one instruction issued at a given time, but also, the code is likely to run into stalls, typically because of an instruction using the result of a memory load right away.

Postpass scheduling is the first step in fixing this performance issue by reordering code to minimize stalls and bundling together instructions.

In figure 10.1, I measure the impact of bundling alone (without any reordering: just packing together instructions into bundles, greedily), and of our actual postpass scheduling (who performs both reordering and bundling).

A first result: for most benchmarks, on the KV3, postpass scheduling gives a performance increase of at least 30%. Some benchmarks such as *convertible*, however, are not affected much: the main loop features around 800 different variables in the same scope, which do not fit into the 64 registers of the KV3. Register spills are thus generated, which prevents scheduling since we consider memory to be invalidated entirely by a store instruction. We would require an alias analysis to solve this issue: then, certain memory accesses could be reordered.



	KV3			
Setup	Q1	Med	Q3	
Greedy Bundling	+6.28%	+13.03%	+18.57%	
List Scheduling	+13.96%	+31.25%	+46.62%	

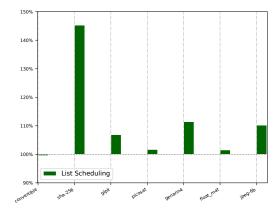
Figure 10.1.: Performance gain of postpass scheduling and "greedy bundling" on KV3. The left figure shows each of our handpicked benchmarks. The right figure shows the results across all the benchmarks.

A second result is that reordering has a much more significant impact than just bundling instructions together. On the KV3 architecture, stalls have a substantial effect on performance.

Another interesting result: though greedy bundling did not affect much of our float_mat_v2 benchmark, the list scheduling dramatically improved its performance. This gave us a glimpse that loop unrolling can have a significant impact on performance.

On AArch64 core

Léo Gourdin and David Monniaux ported the KV3 postpass scheduling module to AArch64 by using latencies information from the LLVM. I display the results in figure 10.2.



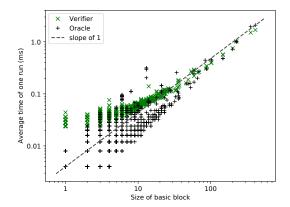
	AArch64				
Setup	Q1	Med	Q3		
Postpass Scheduling	+8.42%	+17.08%	+23.71%		

Figure 10.2.: Performance gain of postpass scheduling on AArch64. The left figure shows each of our handpicked benchmarks. The right figure shows the results across all the benchmarks.

Certain benchmarks can profit significantly from the postpass scheduling on AArch64. However, it is less potent than on the KV3 architecture and less consistent: a bit more than a quarter of the benchmarks are barely affected (+5% gain on the first quantile). However, a quarter of the benchmarks have a performance gain of at least 20%, thanks to postpass scheduling.

10.2.2 Compilation times of postpass scheduling on KV3

To ensure that hash-consing works as intended for reducing the execution cost of the optimization, I instrumented the OCAML generated code to include timers and basicblock size counters. I also measured the execution timings on the particular benchmark *bitsliced-aes*, which contains basicblocks with more than 100 instructions. The results are displayed in figure 10.3.



	Compiling bitsliced-aes				
Time	Transformation pass				
0.02s	Parsing				
0.01s	Elaboration				
0.04s	Common Subexpression Elimination				
0.02s	Constant Propagation				
0.02s	Redundancy Elimination				
0.08s	Register Allocation				
0.01s	Postpass Scheduling				

Figure 10.3.: On the left, compilation times based on the basicblock size for all our benchmarks (except TACLeBench, which was added recently) in logarithmic scales. On the right, the timings of compiling *bitsliced-aes* (showing only the passes with non-negligible computational time).

Each point in the left figure corresponds to an actual basic block from our benchmarks, verified and scheduled (for the list-scheduling) 1000 times. The verifier is generally a little slower than the oracle, but both are experimentally of linear complexity. The biggest basic block we came across, of around 500 instructions, was scheduled and verified in approximately 4 ms, which is the same time required for other CompCert optimizations such as constant propagation or common subexpression elimination. The timings of the *bitsliced-aes* benchmark show that the compile times are in line with other optimization passes of CompCert.

10.3 Impact of superblock scheduling related optimizations

In this section, we study the impact of most of the optimizations introduced in chapters 7, 8 and 9:

- Ensuring that our static branch prediction is not detrimental (because of wrong predictions).
- Testing the performance of our modified linearizer compared to the original one.
- Evaluating different threshold values for our loop unrolling and loop rotation optimizations.
- Evaluating the different prepass strategies: list scheduling, reverse list scheduling, zigzag scheduling.
- Evaluating the performance gain of each optimization individually

10.3.1 Evaluation of our static branch prediction

To evaluate our static branch prediction, we conducted several experiments.

First of all, we measured the number of wrong predictions experimentally by cross-referencing the guesses with those of the profiling. Our static branch prediction returns, for each conditional branch, either None if no prediction could be made or Some true (resp. Some false) if the condition was predicted to be evaluated to true (resp. Some false). Our profiler outputs the same kind of information, based on the execution count of each branch: None if both branches were executed an equal amount of times each, or Some b with b a boolean indicating which branch got executed more. I then distinguish four different cases to evaluate our static branch prediction:

- Correct predictions: the static prediction guessed a branch that was indeed taken more often in the concrete execution.
- Mispredictions: the static prediction guessed the branch that was taken the least often (it should have either guessed the other one instead or not guessed anything)
- Missed opportunities: the static prediction did not guess anything, and yet there was a privileged branch in the execution.
- No verdict: the profiler did not give any verdict. This could happen either because both branches were executed equally or because the code was not reached during profiling. In these cases, we can not evaluate the static prediction.

In addition, we also counted the number of right and wrong predictions for each used heuristic: opcode (automatic prediction for certain classes of comparisons), return (predicting the branch

that does not lead to a return instruction), loop (testing if the branch remains within the loop) and call (predicting the branch that does not have a call instruction) heuristics.

Correct Predictions	3551
Wrong Predictions	926
Missed Opportunitie	s 2605
No verdict	27234

Heuristics	Right Predictions	Wrong Predictions
Opcode	319	108
Return	882	223
Loop	1284	125
Call	1066	470

Figure 10.4.: On the left, statistics of the static branch prediction, evaluated in regards to profiling. On the right, details for each heuristic.

We show the results in figure 10.4. Ideally, we would like as few wrong predictions as possible since these may compromise our scheduling optimization by scheduling the "wrong" superblocks. In our benchmarks, among the conditional branches for which profiling could give a verdict, about 13% of them were mispredicted, and roughly 50% were predicted correctly. Missed predictions are numerous (36%) but not harmful: they will just result in a lack of optimization.

A significant number of conditional branches could not be evaluated by the profiler: we believe this is because we have a low code coverage on our benchmarks for the datasets we use.

Another way to evaluate our static branch prediction is to replace it by profiling and look at the performance difference. The setup is the following: we run our best version of CompCert (with all the optimizations presented in this thesis activated, and on their best version) with static prediction, then we run our best version of CompCert, but with profiling information instead of static branch prediction, then we compare them. The results are given in figure 10.5.

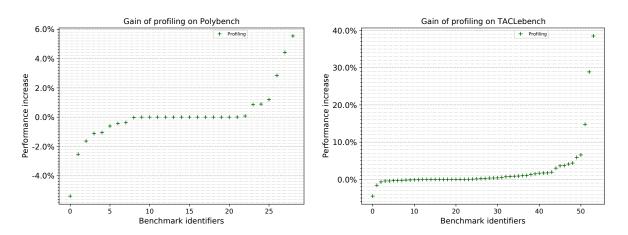


Figure 10.5.: Gain of using profiling instead of branch prediction. On the left, we evaluate this gain on the Polybench benchmarks. On the right, we evaluate it on the Taclebench benchmarks.

All of the Polybench benchmarks except one are untouched by using profiling: this is because their code is simple enough that the implemented heuristics were able to guess correctly. One benchmark suffers a 4% penalty, probably because our profiling got too sure of itself, inferring

the same behaviour as was described in section 4.1.2: right now, our profiling gives a verdict if $n_{ifso} > n_{ifnot}$ with n_{ifso} and n_{ifnot} being the execution counts of each branch. This can lead to a performance penalty if an instruction is scheduled ahead of two consecutive branches for which the execution counts are very close.

The gain of profiling is much more prominent on TACLeBench, because of the code being overall more complex. In the general case, the gain is negligible, except for a fifth of the benchmarks where the gain is between 2% and 10%. One benchmark, in particular, has a very high gain when using profiling (a bench implementing Djikstra's algorithm): 35% performance is gained, most probably because of a static branch prediction heuristic failing in a hot part of the code.

These performance results combined with our measures of predictions give us an informal guarantee that our static branch prediction performs well enough for most of the encountered cases.

10.3.2 Evaluation of our superblock linearizer

I evaluate here the superblock linearizer's performance in regards to the base linearizer from CompCert, on two setups.

The first setup is the baseline CompCert with just postpass scheduling activated, the other is the same setup but with branch prediction and superblock linearization activated. Evaluating this without prepass is a way to isolate the effect of linearization away from prepass scheduling to assert whether this linearizer version is (in the absence of prepass) better or worse than the base version.

The second setup is like the first, except that we include the prepass and instruction duplication optimizations (loop rotation, loop unrolling, tail-duplication). This setup evaluates the real impact of linearization when combined with all the passes introduced in this thesis.

The graphs from figure 10.6 show the impact of adding superblock linearization for these two scenarios.

In the case where we only run postpass scheduling and static branch prediction: for a few benchmarks, our linearization performs slightly worse, though it is mostly negligible: only 2% in the worst case. This can be explained by the presence of certain wrong predictions. A couple of benchmarks see an improvement from using our modified linearizer, though the gain is small.

For the case where all optimizations are run, our linearization has a slightly more significant impact, though it barely ever goes beyond 4% performance improvement. On the other hand, it also incurs a slightly worse performance on a couple of benchmarks, probably because the various

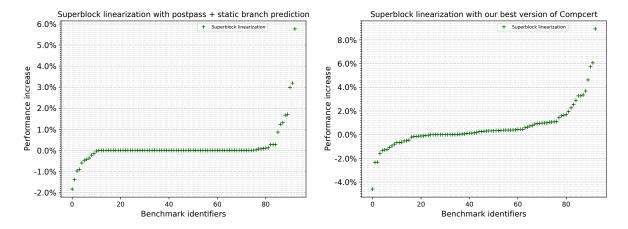


Figure 10.6.: Gain of using superblock linearization instead of base linearization. On the left, the setup includes just postpass scheduling and static branch prediction. On the right, it includes the best version of our optimizations.

instruction duplication passes aggravated the cases where superblocks were not representative enough of the actual execution flow.

10.3.3 Evaluation of loop unrolling, loop rotation and tail-duplication thresholds

Our heuristic for deciding whether to loop unroll, loop rotate or tail-duplicate right now is very barebones: we count the number of instructions that would be duplicated (except *nop* instructions), and if it is below a certain threshold, we unroll, rotate or tail-duplicate accordingly.

More is not necessarily better in this case: a too big threshold would imply too many duplicated nodes. This could then impact performance if the instruction cache is refilled too often due to the increased code size.

I measured the impact of different levels of threshold on instruction cache misses and performance as a whole for the KV3 architecture. I measure in figure 10.7 four different optimizations: loop rotation, loop unrolling, tail-duplication, but also a form of loop peeling that we use for loop invariant code motion. For each optimization, the other 3 are deactivated. So, for instance, to measure the effect of loop rotation, I deactivate loop unrolling, tail-duplication and loop peeling.

The figure is produced in the following way:

• For each benchmark and each threshold level (three of them), the relative performance increase is computed compared to the reference (the setup where the optimization is

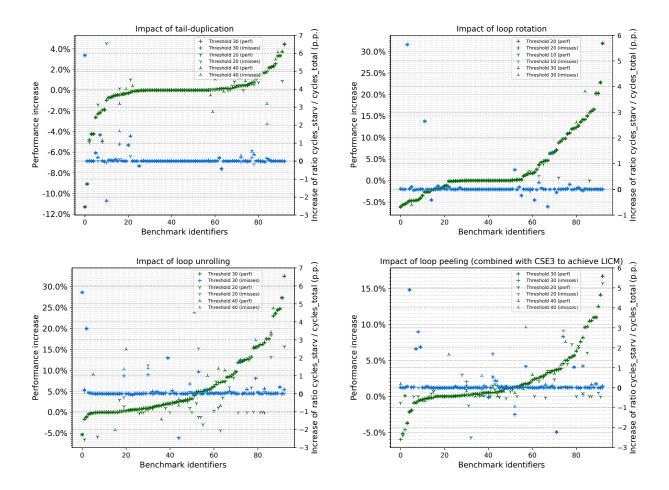


Figure 10.7.: Impact of the four instruction duplication optimizations on performance and pipeline stalls from instruction cache misses.

absent). To ease reading, the middle threshold level is represented by a cross, the upper threshold is a trio pointing upwards, and the lower threshold is a trio pointing downwards.

- We then order the benchmarks in increasing order of this relative performance boost, according to the *topmost threshold* in the legend. This topmost threshold is the middle threshold. This allows having a graph easier to read and forms a baseline to evaluate the lower and higher thresholds. For instance, for loop rotation, we order the benchmarks based on the performance of loop rotation with a threshold of 20: this allows then to compare the thresholds of 10 (lower) and 30 (higher) relatively to this threshold of 20.
- In parallel, from the measure of the number of cycles spent waiting for the instruction cache, I compute the percentage of time spent waiting (because of an instruction cache miss), i.e. the ratio $n_{PFB_starvation_cycles}/n_{total_cycles}$. I display the increase of this ratio compared to the reference, expressed in percentage points (p.p.).

Tail-duplication

Tail-duplication is the least game-changer of all optimizations, both in terms of performance and cache misses penalties, across most benchmarks.

The benchmarks getting a performance increase (or decrease, for some cases) are those having one or more branches in a hot loop that were able to be decided with static prediction.

The reason for bad performance on tail-duplication does not seem to come from instruction cache misses since their impact is minimal. Instead, I believe it comes from wrong predictions: the prepass scheduling is activated for these measures, so a bigger superblock that got the wrong prediction can be harmful to performance. For the best benchmark on tail-duplication, the benefit of tail-duplication seems to outweigh the drawback from having more instruction cache misses.

In some rare cases, tail-duplication induces fewer instruction cache misses. This could be a luck effect: adding instructions change the memory alignment of the other instructions.

At a glance, for tail-duplication, increasing the threshold looks to be beneficial, except for a couple of benchmarks.

Loop Rotation

Loop rotation has a much more significant impact. A third of the benchmarks have their performance increased by more than 5%, some of them are in the range of +10% to +20%. However, some other benchmarks have a slightly decreased performance (-5%), though they are very few. This performance decrease does not seem to be correlated with the number of instruction cache misses: this makes sense since the duplication caused by loop rotation does not add any instruction to the loop core, only outside the loop.

Much like tail-duplication, we also have a couple of benchmarks for which loop rotation induces fewer instruction cache misses.

Increasing the threshold does not seem to has much impact on instruction cache misses. It should be noted that it is rare for an innermost loop to have more than 10 RTL instructions before the conditional branch, which is why increasing the threshold only improves the performance of two benchmarks.

An unfortunate drawback of loop rotation is that since the conditional branch is placed at the end of the loop, one must be taking the conditional branch (and not the fallthrough case) to loop. This incurs a penalty of 1 more cycle (compared to a jump). Thankfully, the benefits of loop rotation (improving the postpass scheduling) outweigh the drawbacks for most benchmarks.

	AArch64			KV3		RiscV			
Setup	Q1	Med	Q3	Q1	Med	Q3	Q1	Med	Q3
+Postpass	+5.03%	+13.93%	+21.98%	+13.96%	+31.25%	+46.62%	-	-	-
+Inlining	-	-	-	+21.67%	+44.03%	+58.28%	-	-	-
+LICM	+11.49%	+29.22%	+45.73%	+27.37%	+51.47%	+74.32%	-0.92%	+1.26%	+5.83%
+Prepass	+14.03%	+32.06%	+58.01%	+28.15%	+51.53%	+75.23%	+0.57%	+9.02%	+15.72%
+Loop unroll.	+18.47%	+40.82%	+75.45%	+28.82%	+58.76%	+86.75%	+2.46%	+12.76%	+16.92%
+Loop rotate	+20.73%	+40.85%	+76.34%	+31.01%	+62.37%	+96.87%	+3.50%	+14.63%	+20.88%

Table 10.1.: Improvement of Cumulated Optimizations w.r.t. mainstream CompCert

Loop Unrolling

Loop-unrolling has a significant impact on performance for most of the benchmarks (between +5% and +20%). It sometimes increases cache misses, though only rarely.

Increasing the threshold seems to be overall more beneficial, except for one benchmark.

I will detail why loop unrolling produces such an impact in subsection 10.3.6.

Loop Peeling

Loop peeling allows the CSE3 pass to perform Loop Invariant Code Motion.

Increasing the threshold seems to be more beneficial since it allows for more loops to be considered, except for a couple of cases.

This optimization seems to have the most significant impact on the instruction cache, with some benchmarks spending between 2 and 5 more p.p. on pipeline starvation. This is generally correlated with worse performance.

10.3.4 Performance impact of each added optimization

In this subsection, I evaluate the performance of each optimization gradually introduced compared to mainstream CompCert 3.8, including the results from the measurements performed by Léo Gourdin and David Monniaux on the AArch64 and RiscV cores. The measures are displayed in table 10.1. Tail-duplication (with threshold 40) is included in the prepass line. For Loop Invariant Code Motion, a loop peeling of threshold 30 was used. The thresholds of loop unrolling and loop rotation were set to respectively 30 and 20. When unavailable, the measures are displayed as a "-". Each setup is evaluated with regards to the mainstream CompCert.

• For both the AArch64 and KV3 cores, postpass scheduling has a significant impact. For the KV3, this impact is more prominent, as expected on a VLIW architecture.

- CompCert can inline functions; however, it is very timid at doing so, unless the function is explicitly marked as "inline". David Monniaux implemented a more aggressive inlining heuristic relying on function code size (in the number of RTL instructions) to choose to inline or not; the +Inlining I show here is with this added heuristic, at threshold 50. This was only tested on KV3. The performance boost is significant on a non-negligible number of benchmarks, from +8% up to +17%.
- LICM is another meaningful optimization, producing a gain of 15% on some benchmarks.
- Prepass scheduling ² (without any loop unrolling) also helps, increasing performance by 5-10% for the AArch64 and RiscV cores. This is mainly due to removing the false dependencies (compared to the postpass scheduling). The KV3 core, on the other hand, is not affected much since it features 64 user registers.
- Loop unrolling increases performance by another 5-10%.
- Loop rotation used alone has a small impact on AArch64 and RiscV (about +3% on the latter). Still, the postpass (on AArch64) benefits from it as the rotation may provide more scheduling opportunities. It shines mostly for the KV3 architecture since it results in a more efficient bundling of the loop header in postpass.

In total, the gain of using our optimizations compared to the original CompCert is significant. On KV3, more than half of the benchmarks gain a performance boost of 60%, and a fourth of the benches have a performance increase of at least a factor 2.

This number is a bit less significant on AArch64, though still substantial: 40% more performance for half of the benchmarks, +75% for a quarter of the benches.

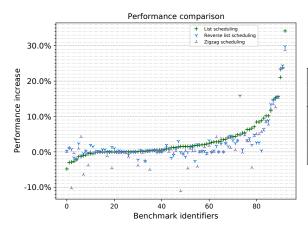
The results on RiscV are less significant: +15% for half of the benchmarks, +20% for a quarter of the benches. Less tuning work was done on RiscV compared to KV3 and AArch64. The performance boost is, however, non-negligible.

10.3.5 Evaluation of the different prepass scheduling strategies

For prepass scheduling, we have three different strategies: forward list scheduling, reverse list scheduling, and zigzag scheduling. I first evaluate these 3 different strategies in figure 10.8. For this experiment, all optimizations are activated.

From the results, no scheduling is absolutely superior: some benchmarks prefer zigzag scheduling, while some others prefer reverse list scheduling, and yet other benches prefer list scheduling. However, for most of the benchmarks we have tested, (forward) list scheduling seems to be

²On the KV3, due to a temporary technical issue not related to CompCert, we disabled the support for non-trapping loads.



		KV3	
Setup	Q1	Med	Q3
List Scheduling	+0.00%	+1.22%	+4.18%
Reverse List Scheduling	+0.00%	+0.39%	+2.38%
Zigzag Scheduling	-0.18%	+0.08%	+2.74%

Figure 10.8.: Performance gain of prepass scheduling on KV3. The left figure shows each benchmark individually. The right figure shows statistics across all the benchmarks.

the better choice, probably because the KV3 has 64 user registers available, so the chance of suffering from register spilling during register allocation is slim.

In general, the gain of using a prepass scheduling on the KV3 is relatively low for 2/3 of the benchmarks, though it can be exceptional for some benches. Indeed, there are occasions where the postpass scheduling cannot find a good schedule because of register dependencies introduced by the register allocator — prepass scheduling helps a lot in those cases.

The performance of zigzag scheduling is non-negligibly detrimental for approximately 10 benchmarks out of 90.

10.3.6 Gains of loop unrolling without prepass scheduling

One oddity that struck me compared to what I was initially expecting is that loop unrolling seems to gain a lot of performance across many benchmarks on the KV3, regardless of the presence of prepass scheduling. To illustrate that, let's deactivate prepass scheduling and focus only on the absence or not of loop unrolling. All the other optimizations are activated. The result is shown figure 10.9.

The performance gain of 20% was particularly impressive and unexpected. Let's dive down the rabbit hole to figure out what happened. This gain corresponds to the benchmark *matrix1* from TACLeBench, whose code is shown below.

```
void matrix1_main( void ) {
  register int *p_a = &matrix1_A[ 0 ];
  register int *p_b = &matrix1_B[ 0 ];
  register int *p_c = &matrix1_C[ 0 ];
```

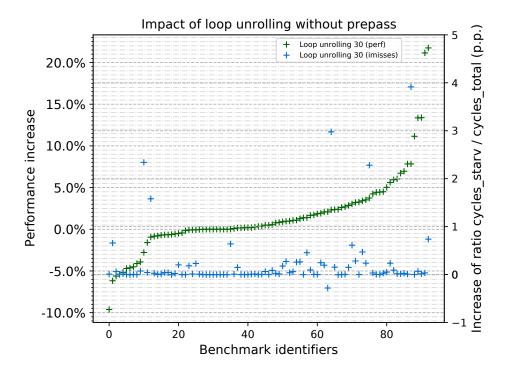


Figure 10.9.: Impact of loop unrolling, without prepass, with a threshold of 30.

```
5
6
      register int f, i, k;
7
8
      for (k = 0; k < Z; k++) {
        p_a = matrix1_A[0]; /* point to the beginning of array A */
9
10
11
        for (i = 0; i < X; i++) {
12
          p_b = &matrix1_B[ k * Y ]; /* take next column */
13
14
          *p_c = 0;
          for ( f = 0; f < Y; f++ ) /* do multiply */</pre>
15
16
             p_c += p_a++ p_b++;
17
18
          p_c++; } } }
```

On that code, most of the performance comes from the innermost loop. It is a very short innermost loop, so its code is relatively easy to analyze. I give in figure 10.10 two versions of the assembly code implementing this innermost loop: one without loop unrolling and one with loop unrolling.

The first version spends a total of 10 cycles per iteration: 5 cycles for issuing the bundles (5 bundles), 2 for the branch penalty (the conditional branch at the end), 2 for the stall on \$r39, and 1 cycle for the stall on \$r1 (2 cycles are required for the maddw instruction).

The second version spends a total of 17 cycles for two iterations: 9 cycles for the bundles (9 bundles), 2 for the branch penalty (last conditional branch), and 6 cycles for stalls (the same stalls as above, but duplicated). On average, the second version spends 8.5 cycles per iteration, hence a 15% performance boost.

So, where does this performance boost come from, and how did loop unrolling affect it? First of all, on the second version, we have one less instruction: the lws \$r45 that was line 11 does not appear anywhere in the second iteration. This was taken off by the base CSE optimization from CompCert, ³ thus saving us half a cycle per iteration. Finally, the biggest gain comes from the absorption of the conditional branch penalty. There is no branch penalty in one iteration out of two because the next iteration is laid out right next to the conditional branch (see line 16). This makes us gain two cycles per couple of iterations, so one cycle per iteration on average.

This case is particularly fruitful because the loop was rotated, so the branch penalty was 2 cycles. However, even if the loop were not rotated, there would still be a penalty of 1 cycle (penalty of unconditional jump): loop unrolling would have saved half a cycle per iteration (instead of 1).

In conclusion, loop unrolling alone can have a significant impact on small loops, regardless of any other optimization. CSE and prepass scheduling can help further on top of it.

10.4 COMPCERT VS GCC in our current iteration

In this section, I evaluate our version of CompCert with all enabled optimizations versus GCC, for KV3 (subsection 10.4.1), and for AArch64 and RiscV (subsection 10.4.2).

10.4.1 COMPCERT VS GCC on the KV3 architecture

Figure 10.11 shows GCC with four different optimization levels, compared to CompCert.

First of all, for all the benchmarks we have run, CompCert is always better than GCC -O0: for safety-critical applications that require traceability (e.g. DO178 level-A avionics), CompCert is a better choice in terms of performance (and the preservation proof of CompCert makes it also possible to have traceability, see Bedin França et al. [8]). On the KV3, GCC -O0 delivers particularly inefficient code because it does not use the 64 available registers (retrieving stack values through load/store rather than assigning registers to them), and postpass scheduling is deactivated: bundles contain only a single instruction. As a result, using CompCert instead of GCC -O0 results in 250% more performance for half of the benchmarks.

³CSE3 is also able to do this substitution, but CSE is executed before CSE3.

```
1
   .L106:
                                       .L110:
2
     addd $r3 = $r2, 0
                                    2
                                          addd $r3 = $r2, 0
      addd $r8 = $r7.0
                                    3
                                          addd $r9 = $r6, 4
3
4
     lws $r1 = 0[$r35]
                                    4
                                          lws $r5 = 0[$r43]
5
                                    5
     addw $r10 = $r10, 1
                                         addw $r37 = $r42, 1
6
                                    6
                                       ;;
   ;;
7
                                   7
     addd r2 = r3, 4
                                         addd r2 = r3, 4
8
     addd r7 = r8, 4
                                   8
                                        lws $r10 = 0[$r3]
9
     lws $r41 = 0[$r3]
                                   9
                                         compw.ge $r32 = $r37, 10
     compw.lt $r32 = $r10, 10
                                   10 ;;
10
11
                                   11
                                         lws $r45 = 0[$r6]
12
     lws $r39 = 0[$r8]
                                   12
                                       ;;
13
                                   13
                                         maddw $r5 = $r10, $r45
   ;;
14
    maddw $r1 = $r41, $r39
                                   14
15 ;;
                                   15
                                        sw 0[$r43] = $r5
   sw 0[$r35] = $r1
                                   16
16
                                          cb.wnez $r32? .L111
17
     cb.wnez $r32? .L106
                                   17
                                   18
                                          addd r8 = r2, 0
18 ;;
                                          addd r6 = r9, 4
                                    19
                                    20
                                         lws $r38 = 0[$r9]
                                    21
                                         addw $r42 = $r37, 1
                                    22 ;;
                                    23
                                         addd r2 = r8, 4
                                        lws $r15 = 0[$r8]
                                    25
                                         compw.lt $r32 = $r42, 10
                                    26 ;;
                                    27
                                         maddw $r5 = $r15, $r38
                                    28
                                    29
                                         sw 0[$r43] = $r5
                                    30
                                          cb.wnez $r32? .L110
                                    31 ;;
```

Figure 10.10.: Two versions of the innermost loop from *matrix1*: non-unrolled on the left, unrolled on the right. See appendix A for an instruction reference.

COMPCERT is also slightly better than GCC -O1 for the majority of the benchmarks, thanks to our additional introduced optimizations. Also, GCC -O1 does not perform any bundling nor any reordering. However, in some cases, we still have poorer performance than GCC, even in -O1.

Compared to GCC -O2, on the KV3 architecture, we still have a fair margin of progression ahead, although there are some benchmarks where we are very close: in a fourth of the benches, we are only 4% worse than GCC -O2. Also, GCC -O3 beats us by a large margin.

I will explain further below some elements that are missing either in CompCert or, more generally, in our KV3 port.

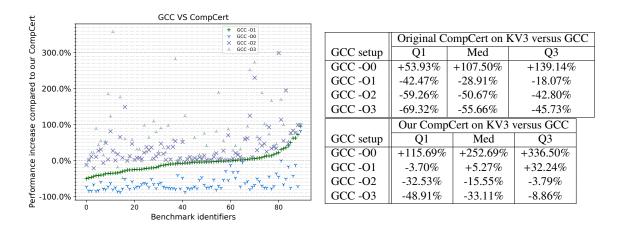


Figure 10.11.: Comparing the performance of CompCert and GCC on KV3. The left figure shows GCC compared relatively to CompCert across all the benchmarks. The right figure shows the reverse: the gain of using CompCert instead of GCC, for the original version of CompCert and the version with our included optimizations.

Elements missing in COMPCERT compared to GCC -O1

To get a glance at the missing elements, I picked the worst benchmark for CompCert VS GCC -O1: this is *rad2deg* from TACLeBench. The core of the source code is straightforward:

```
#define rad2deg(r) ((r)*180/PI)
float rad2deg_X, rad2deg_Y;

void rad2deg_main( void )

for ( rad2deg_X = 0.0f; rad2deg_X <= ( 2 * PI + 1e-6f ); rad2deg_X += ( PI / 180 ) )
            rad2deg_Y += rad2deg( rad2deg_X );
}</pre>
```

It features floating-point multiplications and divisions primarily. The KV3 does not have any floating-point division, so both GCC and CompCert have to rely on an external function provided as a library for performing the floating-point division. I give in figure 10.12 the code generated for GCC and CompCert. I turned off loop unrolling to make it easier to analyze – it decreases a bit the performance, but this is negligible compared to the issues I will outline. ___divsf3 is the library function providing floating-point division for 32-bits floats.

First of all, one may notice that on the CompCert code, two calls to __divsf3 are done, compared to just one for GCC. This is because we have no constant propagation for division with floats in our port, so CompCert has to recompute the constant (PI/180) every time. ⁴ Since

⁴We do not have any constant propagation for float division because the division is inserted as a builtin before constant propagation occurs. It might be possible to solve this technical issue in the future with the improved builtin support of CompCert 3.6.

this is done through a call to an external function, this is not caught by the Loop Invariant Code Motion of D. Monniaux [63].

Another point: the handling of global variables. GCC was smart enough to figure that during the loop execution, the global variable rad2deg_Y would only be accessed by the loop; all functions called in that particular loop will not access or modify rad2deg_Y. As a result, the global variable is loaded from the heap before the loop, then stored after the loop. In COMPCERT, the global variable value is stored or reloaded after each access, resulting in extra load and store instructions. Although the CSE pass is able to eliminate redundant load and stores, it does not traverse loops, and also the presence of a builtin can compromise the optimization (since builtins might modify the program memory). This, in turn, introduces extra stalls that were not present in the original code: in total, 6 additional cycles of stalls are introduced (from the two faddw instructions that each require 4 cycles to complete).

Finally, on some particular benchmarks, we noticed that GCC can expand an aggregate (such as an array or a structure) into independent scalar variables, which can then be allocated to registers. In other words, the values are first loaded from the aggregate to the registers; then, the computation is done with the allocated registers; finally, the values are stored back to the aggregate. On the affected benchmarks, the performance difference can be significant since doing so removes store and load instructions from the main loop.

There are some subtler differences, such as GCC having simpler prologues and epilogues for leaf functions that use no stack variables or GCC having better instruction selection in some instances.

Additional elements of GCC -O2 compared to us

There are several things that GCC -O2 does more or better than us, in addition to the relevant points from GCC -O1:

- GCC -O2 is able when the number of iterations is known at compile-time to unroll completely a given loop (if the number of iterations is small), which removes any conditional branching and allows to reorder the whole unrolled loop body. In certain cases, the performance gained is quite significant: at least one cycle is gained from removing the loop branch, and a couple more cycles per iterations can be gained with the finer scheduling that follows.
- GCC has memory alias analysis: it can reorder store and loads when it can rule out that they will never cross each other (when their accesses never overlap). On the other hand, we do not use any alias analysis yet; memory is seen as a single resource, invalidated by any store. An alias analysis already exist in RTL, though we have not looked yet into

```
1
      make $r0 = rad2deg_Y
                                              make $r20 = rad2deg_Y
                                              make $r21 = rad2deg_X
2
                                        2
      ;;
3
                                        3
                                              /* ... */
      lwz $r19 = 0[$r0]
4
                                        4
                                            .L102:
      ;;
5
                                        5
      make $r18 = 360
                                              lws $r23 = 0[$r20]
6
                                        6
                                              fmulw $r0 = $r0, $r18
7
                                        7
      /* ... */
                                              addd $r1 = $r19, 0
8
                                       8
                                              call __divsf3
    .L4:
9
      copyw $r1 = $r21
                                       9
10
                                       10
                                              faddw $r3 = $r23, $r0
                                              addd $r1 = $r18, 0
11
      fmulw $r0 = $r14, $r22
                                       11
12
                                       12
                                              addd r0 = r19, 0
13
      call __divsf3
                                       13
                                           ;;
14
                                       14
                                              sw 0[$r20] = $r3
      ::
15
                                       15
      faddw $r19 = $r19, $r0
                                       16
                                              lws $r23 = 0[$r21]
16
17
      faddw $r14 = $r14, $r20
                                       17
                                              call __divsf3
                                       18
18
      ;;
19
      addw $r18 = $r18, -1
                                       19
                                              faddw $r0 = $r23, $r0
                                       20
20
      ;;
                                            ;;
21
      cb.dnez $r18? .L4
                                       21
                                              sw 0[$r21] = $r0
                                       22
22
      /* ... */
                                           ;;
23
                                       23
                                              fcompw.oge $r32 = $r22, $r0
24
                                       24
      make $r0 = rad2deg_Y
25
                                       25
                                              cb.wnez $r32? .L102
26
      sw 0[$r0] = $r19
                                       26
```

Figure 10.12.: Compiled codes of rad2deg_main: on the left, the code from GCC -O1; on the right, the code from CompCert without loop unrolling. See appendix A for an instruction reference.

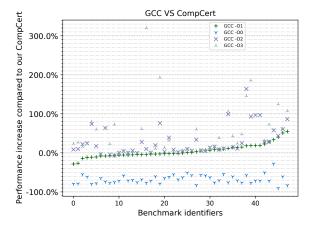
integarting it in our prepass scheduler. Propagating this alias analysis to Asm could prove challenging. Alternatively, a more limited form could be added in the postpass scheduler to reorder memory stores from the same base register but with different offsets; however, the verifier would need to be enhanced for this.

- The KV3 architecture features hardware loops: it is possible to set up special registers pointing to the beginning and end of a loop and a counter register; then the given section is repeated as many times as specified by the register counter.
- GCC is generally more aggressive than us when it comes to unrolling loops: so far, we only unroll loops once, but we could probably try to unroll them several times. In general, there is room for improvement in our current heuristics.
- GCC can perform loop strength reduction: instead of incrementing the loop index by 1, then multiplying by a loop-invariant constant c, it increments the loop index by c directly. This saves up one dependency and a multiplication, usually resulting in at least one gained cycle.

Bringing CompCert up to speed with GCC -O2 would require implementing the above optimizations.

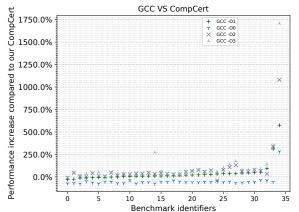
10.4.2 COMPCERT VS GCC on AArch64 and RiscV architecture

We also evaluated CompCert with regards to AArch64 and RiscV with our new optimizations. The results can be found in figures 10.13 and 10.14.



	Original C	Original CompCert on AArch64 versus GCo				
GCC setup	Q1	Med	Q3			
GCC -O0	+87.36%	+117.09%	+161.23%			
GCC -O1	-43.74%	-28.22%	-22.17%			
GCC -O2	-55.08%	-38.39%	-29.01%			
GCC -O3	-63.94%	-43.94%	-32.00%			
	Our Comp	Cert on AArc	h64 versus GCC			
GCC setup	Q1	Med	Q3			
GCC -O0	+153.98%	+242.55%	+323.93%			
GCC -O1	-12.38%	+0.89%	+5.83%			
GCC -O2	-29.24%	-12.25%	-4.68%			
GCC -O3	-40.39%	-20.23%	-5.67%			

Figure 10.13.: Comparing the performance of CompCert and GCC on AArch64. The left figure shows GCC compared relatively to CompCert across all the benchmarks. The right figure shows the reverse: the gain of using CompCert instead of GCC, for the original version of CompCert and the version with our included optimizations.



	Original Co	ompCert on I	disc v versus GCC
GCC setup	Q1	Med	Q3
GCC -O0	+78.62%	+102.16%	+124.77%
GCC -O1	-39.86%	-32.69%	-16.05%
GCC -O2	-52.23%	-45.42%	-24.87%
GCC -O3	-54.12%	-47.91%	-41.32%
	Our Comp	Cert on Risc\	V versus GCC
GCC setup	Q1	Med	Q3
GCC -O0	+114.84%	+133.14%	+184.17%
GCC -O1	-27.92%	-13.72%	-4.04%
GCC -O2	-40.96%	-30.90%	-22.48%
GCC -O3	-45.65%	-36.36%	-25.34%

Figure 10.14.: Comparing the performance of CompCert and GCC on Risc V. The left figure shows GCC compared relatively to CompCert across all the benchmarks. The right figure shows the reverse: the gain of using CompCert instead of GCC, for the original version of CompCert and the version with our included optimizations.

For AArch64, the results are less pronounced than for the KV3; however, the same trends as for KV3 can be observed. While GCC -O1 is for most benchmarks faster than our version of CompCert, our optimizations bring CompCert closer to GCC -O1.

Results for RiscV are not as good as on AArch64, though still noteworthy compared to the original CompCert. For one benchmark in particular (*audiobeam* from TACLeBench), CompCert

produces particularly inefficient code: CompCert is almost 3 times slower than GCC -O0 for that bench. Excluding that particular benchmark, the lack of postpass scheduling is likely to be a reason for the worse performance. Also, less work went on the RiscV prepass backend compared to AArch64 and KV3; this remains a work in progress.

11

Conclusion

11.1 Summary

We also recovered the basic block structure, introducing two new IRs: Machblock and Asmblock, which are identical to Mach and Asm, except that the code is organized in basic blocks, run in one semantic step, that we call block-step. The difference between Asmblock and AsmVLIW lies only in the execution semantics: basic blocks have sequential execution semantics, while AsmVLIW bundles have parallel execution semantics.

We introduced a postpass scheduling on basic blocks to generate bundles, formally verified by translation validation with hash-consing. The scheduler and verifier are independent in our approach: the scheduler is implemented through an untrusted oracle (in OCAML), while the verifier is implemented in Coq and is formally proved. To tackle the considerable number of instructions in the KV3 backend, we used a new IR, AbstractBasicBlock. It abstracts the details of each instruction to focus on which resources are being read or written and which operations are performed. The AbstractBasicBlock IR is equipped with two semantics (sequential and parallel) and symbolic evaluation. By writing a translation between Asmblock and AbstractBasicBlock, and by proving a bisimulation between the two IRs, we were able to prove the postpass scheduler verifier in two steps: first, checking that the concatenation of the bundles (returned by the scheduler oracle) is equivalent to the original basic block; then checking that each bundle has the same sequential and parallel semantics.

We then explored a prepass scheduling, at the RTL level, on superblocks. Forming superblocks requires having knowledge of the execution flow tendencies. We implemented static branch prediction with profiling and user-annotation support (via the builtin __builtin_expect) and modified RTL to include such information. Before superblock scheduling, we implemented tail-duplication to transform relevant traces into superblocks. Tail-duplication is formally verified through a generic and lightweight checker (Duplicate) that specializes in transformations that duplicate instructions without changing the semantics.

We introduced a new IR, RTLpath, with block-step semantics executing whole superblocks. This IR is just RTL augmented with block-step semantics and with a "pathmap" giving the partitioning of the control-flow graph into superblocks. In particular, RTL and RTLpath bisimulate each

other. Within this IR, we integrated a liveness checker and a new simulation modulo liveness. An external oracle creates the superblocks (and their associated liveness information); the RTLpath checker then checks the liveness. We adapted the linearizing heuristics of CompCert to ensure our superblocks are laid out contiguously in memory.

We used this RTLpath to construct a superblock scheduling checker. For that, we introduced an extension of symbolic execution for superblocks and a refined symbolic execution with hash-consed terms. Through adequate properties of bisimulation between RTLpath and superblock symbolic execution, and the simulation modulo liveness of RTLpath, we were able to formally verify the checker.

We also used the Duplicate verifier for transformations that further increases performance: loop unrolling, loop rotation, loop peeling. In particular, the latter was used in conjunction with a new common subexpression pass of D. Monniaux to achieve loop-invariant code motion; this was published in Monniaux and Six [63].

Finally, we evaluated each of our optimizations on a set of benchmarks, including Polybench and TACLeBench. Our optimizations give a significant performance increase to CompCert: on the KV3 VLIW core, our optimizations increase the performance of most benchmarks by 62%.

Although our version of CompCert is beating GCC -O1 for most benchmarks, we are still 12% worse than GCC -O2. We made a detailed analysis in section 10.4 and gave starting points for future work.

11.2 Reflexions and Future Work

The goal of this thesis was to bring CompCert closer to modern compilers such as GCC in terms of the performance of the generated code. This thesis was focused on the KV3 processor, a VLIW architecture with an interlocked pipeline. However, most of our optimizations can be used for other targets as well:

- Loop unrolling, loop rotation and loop-invariant code motion can be directly plugged in the other backends. Prepass superblock scheduling can also be plugged, though some backend-specific code needs to be written for encoding the resources and latencies of each Asm instruction.
- Our postpass scheduling can be adapted to other architectures: it was recently ported to AArch64 after three person-months of development [89].

In particular, we chose an approach where most optimizations are performed in smaller and easier to prove passes:

- Instead of proving loop-invariant code motion directly, we split it into two passes: a common-subexpression pass that goes through control-flow merges and a code duplication pass that replicates an entire loop body.
- Tail-duplication, superblock selection and superblock scheduling are three independent passes; compared to the heavier trace scheduling, this allowed us to ease the proof effort.
- Postpass scheduling is split into the generation of basic blocks at Mach level, translation
 of basic blocks from Machblock to Asmblock, and finally AsmVLIW bundles generation
 from Asmblock.

This approach was fruitful in our development and allowed us to tackle optimizations that would have probably been tougher to prove otherwise.

We also showed in this thesis that the concept of *a posteriori verification*, initially studied within CompCert by Tristan and Leroy [95], can be coupled with hash-consing to provide reasonable compilation times and can be used for a wide range of optimizations providing a significant increase in performance. On the KV3 processor, these optimizations bring CompCert close to GCC -O2. There is still progress to be done; we gave in section 10.4 a non-exhaustive list of the reasons why CompCert remains behind GCC.

Among the possible directions for progression, the following points could be studied:

- We unroll each loop only once; it could be interesting to try unrolling a given loop several times. Ideally, the code size of a loop (in bytes) should never be larger than the instruction cache. Davidson and Jinturkar [24] points that the loop unrolling pass should be positioned after traditional optimizations that modify the code size to have a fair approximation of the size of the unrolled loop.
- We do not perform any register renaming when unrolling the loop: this leads to false dependencies in scheduling and could be one reason why our prepass scheduling does not gain much from unrolling. A register renaming transformation (using fresh registers) could be introduced by an oracle and verified *a posteriori* by symbolic superblock execution (with a verification modulo liveness).
- It could be possible to implement induction variable expansion, as described in Hwu et al. [40]. In terms of verification, this would require adding more rewriting rules (e.g. for the addition operation) in superblock symbolic evaluation semantics. Loop strength reduction could probably be supported as well.
- None of our schedulers support alias analysis. At the RTL level, we could probably reuse
 the results of the alias analysis pass from Robert and Leroy [82]. It would probably be
 more challenging to forward these results to the Asm IR for the postpass scheduler.
- Our prepass scheduling does not pay much attention to the register pressure: while backward list scheduling tends to ease the register pressure compared to forward list scheduling, there is no guarantee that the pressure never exceeds a given threshold.

• It could be interesting to support hardware loops in CompCert, though it would be challenging: the exact number of iterations would need to be inferred down the intermediate representations. Also, one would need to prove some invariant that the special loop registers will never be modified outside of the given loop.

The above lays the ground for potential future work to bring CompCert even closer to production compilers in terms of the performance of the generated code.



Non-exhaustive instruction listing of the KV3 core

The KV3 processor features 64-bit registers that can be used for storing either floating-point or integer values.

I write below the instructions that were mentioned in the manuscript, with their assembly semantics. I use registers for most operands, however it is possible most of the time to use immediate values instead. This usually results in a bigger instruction depending on the size of the immediate: it will take more slots in the VLIW bundle.

- "addw \$r0 = \$r1, \$r2" performs \$r1 + \$r2, then clears the 32 upper bits and stores the result in \$r0.
- "addd \$r0 = \$r1, \$r2" performs \$r1 + \$r2, and stores the result in \$r0.
- "call symbol" performs a call to symbol. In practice, this is done by copying the current value of PC (Program Counter) into RA (Return Address), then setting PC to the address of symbol.
- "cb.dnez \$r0? .L1" evaluates a unary condition on \$r0, based on the modifier. If the comparison succeeds, PC jumps to the .L1 label. In this example, the modifier is .dnez which stands for "Double word Not Equal to Zero": it triggers the branch if \$r0 is not equal to 0. On the KV3, the branch penalty is 2 cycles if the branch is taken, 0 cycle if the branch is not taken.
- "compw.ge \$r0 = \$r1, \$r2" evaluates a binary condition on the 32 lower bits of registers \$r1 and \$r2, then stores the boolean result in \$r0. The modifier expresses the condition: here, .ge stands for "Greater Than or Equal".
- "copyw \$r0 = \$r1" copies the 32 lower bits of \$r1 into \$r0. The 32 higher bits of \$r0 are cleared.
- "faddw \$r0 = \$r1, \$r2" stores in \$r0 the addition of \$r1 and \$r2, interpreted as 32-bits floating-point values. The result is rounded to a 32-bits floating-point value according to a rounding mode set in the CS register. It is also possible to override the rounding mode via a modifier.
- "fcompw.oge \$r0 = \$r1, \$r2" is the same as compw, but for floating-point values.

 It also features different modifiers since comparing two floating-point values is more

- complex than comparing two integers values. In this example, .oge stands for "Ordered and Greater Than or Equal".
- "fmulw \$r0 = \$r1, \$r2" is the same as faddw, but for multiplication.
- "goto .L1" makes PC jump to the .L1 label.
- "lws \$r0 = \$r1[\$r2]" loads the 32-bits memory value at address \$r1 + \$r2 into \$r0, and performs sign extension to the result. There are also variants for loading 64-bits, or even 128-bits and 256-bits. There are modifiers to add scaling to the offset: for instance, lws.xs loads the value of 4 * \$r1 + \$r2. This is extremely helpful for array accesses. The optional .s modifier turns the instruction into a speculative load, i.e., one that does not trap if an incorrect address is given.
- "maddw \$r0 = \$r1, \$r2" performs a multiply-add on the least significant words: \$r0 += \$r1 * \$r2 The resulting word is zero-extended.
- "make \$r0 = imm" sets \$r0 to the immediate value imm (up to 64 bits).
- "sxwd \$r0 = \$r1" performs sign-extension on \$r1 (from 32-bits to 64-bits) and stores the result in \$r0.
- "sw \$r0[\$r1] = \$r2" stores the 32 lower bits of \$r2 into the memory address \$r0 + \$r1. It also has the .xs modifier. However, it does not have the .s: memory stores are never speculative on the KV3 architecture.

List of Figures

1.1	The Coolidge architecture	9
1.2	The pipeline stalls at cycles 5 and 6 because B3 is waiting for the results of R_1	
	and R_2 from bundles B1 and B2, which are completed at stage E3. Stage PF (not	
	shown here) happens just before the ID stage	11
1.3	The Intermediate Languages of CompCert	11
1.4	Examples of Simulation Diagrams in CompCert, from Leroy [51]	13
1.5	CompCert compilation flow with our added optimizations in red	17
3.1	Architecture of our postpass scheduling	28
3.2	Parallel In-Order Blockstep	33
3.3	Execution Steps between Mach States	36
3.4	Overview of our Proof for Condition (2) of the "Block" Simulation of Mach by	
	Machblock	39
3.5	Simulation Diagrams with Stuttering in CompCert	40
3.6	Diagram of the Simulation Proof	49
3.7	Certified Scheduling from Untrusted Oracles	52
3.8	Diagram of bblock_simub Correctness	56
4.1	Two imbricated loops	64
4.2	Program with two branches. Top figure: original program. Bottom figure: the	
	instruction E_1 is moved before A (under the non-trivial assumption that it is correct	
	to do so). An identified trace (that could be turned into a superblock) is shown in	
	green. Each conditional branch edge is annotated with its probability	66
4.3		70
4.4	On the left, the assembly generated code, annotated with timings information. On	
	the right, its basicblock representation, with a trace of interest shown in green. In	
	the assembly code, the registers targetted by load instructions along the trace are	
	written in red. See appendix A for an instruction reference	72
4.5	Tail duplicating the identified trace	74
4.6	Performing loop unrolling one time	75
4.7	Final code after tail duplication and loop unrolling	76

4.0	is incorrect: an instruction assigning x4 was moved before a branch which later uses x4. The right schedule is correct	78
4.9	Example illustrating the impact of register allocation on scheduling. Left: RTL code example; it is possible to move instruction 4 before instruction 3 to reduce stalls. Right: Assembly (before scheduling) example; that move is not possible because of a false dependency with \$r2	79
4.10	Our example, with prepass scheduling activated. It is annotated with timings information	81
4.11	Our order of RTL optimizations	84
5.1 5.2	C code, and RTL representation of fold_add as a control-flow graph The RTL code of fold_add, represented syntactically. The instruction nodes are represented in red. The entrypoint of that code is 9. For clarity, I represent registers as "x" followed by their number – though in the actual syntax, registers are just	86
	positive integers	87
5.3	Execution steps between RTL states	89
5.4	Three examples of pathmaps for the RTL code on the left. We omit the output_regs field. Pathmap A would lead to an incorrect execution. Pathmap B is correct, but undesirable because the path starting at 9 is not a superblock. Pathmap C is correct, and desirable	96
5.5	Executing a path from s (a RTLpath.State). Two possible executions are shown. One executes an entire path by computing istep psize times, finishing by a path_last_step which gives the final state s'_1 . The other computes istep only n times, then reaches a point where icontinue = false: it exits the path and returns a State s'_2 . The entire execution is a path_step	99
5.6	Bridging RTL and RTLpath execution. The left figure shows an execution through a whole path, the right figure shows an execution with the path ending before the end because of an early exit. The red transition outlines the RTL execution of the last instruction from the path; the olive transitions outline RTL executions corresponding to RTLpath stutterings. Dotted edges correspond to match_inst_states_goal idx with idx value displayed on top of the edge	102
6.1	Example of code duplication, with its reverse mapping. To the left, the original code. To the right, the transformed code. The reverse mapping is shown in red	112
7.1	Example of symbolic execution, then evaluation of the symbolic states	120
7.2	Tree representation of a sstate	122

7.3	Graphical representation of all_fallthrough_upto_exit relation. The superblock is executed from right to left; all conditions up to ext have been evaluated to false (f in the drawing). The other conditions remain to be evaluated	125
7.4	Summary of ssem_internal semantics. The same superblock is presented in two scenarios: on the left, no early exit was triggered so far, so we continue to execute the superblock. On the right, one early exit was encountered: the next internal state will then have icontinue to false. The symbols \Longrightarrow_C and \Longrightarrow_L respectively denotate the condition and local (registers and memory) evaluation functions (over symbolic values)	
7.5	Evaluating a symbolic state with the ssem relation	129
7.6	Graphical representation of siexec_path_correct lemma. The superblock is symbolically executed up to a certain point, giving an internal symbolic state st . The evaluation of this internal symbolic state succeeds and gives an internal state is . The lemma proves then a correspondence between the remaining symbolic execution via siexec_path, and isteps	
7.7	Two semantically equivalent superblocks (in green), but who reach a different state when taking the branch A	
7.8	Diagram used for proving the simulation in superblock scheduling. s_1 is actually the state made of $(f, sp, stk_1, rs, m, pc_1)$, and s_2 is made of $(f', sp, stk_2, rs, m, pc_2)$. $\underline{b_i}$ is the symbolic execution of the superblock from pc_i	141
7.9	Diagram used for proving the refinement simulation	154
8.1	RTL code for two nested loops. The identified trace is shown in green	162
8.2	RTL code for two nested loops, with a tail-duplication starting at <i>B</i> . The identified trace shown in green is now a superblock, although unwanted. The duplicated nodes as a result of tail-duplication are shown in blue	162
8.3	RTL code for two nested loops, with an interesting tail-duplication done on the	
8.4	green trace. The duplicated node is in blue	163
	are shown in blue	168
8.5	Example of loop rotation: above is the original code, below is the rotated code, with the duplicated nodes shown in blue	169
8.6	Two possible code layouts for the LTL code shown on the left. Each code layout is annotated with branching penalties from two possible executions: either through B_3 (green) or through B_2 (blue). On average, the layout on the right has less branching	
	penalties than the layout on the left	174

0.7	layout is from the original CompCert heuristics, while the right layout is from a hypothetical heuristics where the chains are laid out in increasing order	177
9.1	Example of dependency graph. The Read-After-Write dependencies are in black; the Write-After-Read are in green; the Write-After-Write are in red. The dashed edges represent a dependency of latency 0	186
9.2	Our code architecture for implementing the schedulers. The architecture-dependent parts are in red, the architecture-independent parts are in green	
9.3	Example of dependency graph of a superblock, for architectures that do not have speculative loads. The usual RAW dependencies are in black, the extra conditional	
	branches dependencies coming from trapping instructions are in red, the additional dependencies between the conditional branches are in green	191
9.4	Our three possible prepass scheduling on the previous example. The code is annotated with the initial position of each line of code for clarity. I also show the "time → instructions" mapping of each schedule. The conditional branches are outlined in red. The load instructions are marked in green, and the conditional branches in red, for easier recognition	
10.1		170
10.1	Performance gain of postpass scheduling and "greedy bundling" on KV3. The left figure shows each of our handpicked benchmarks. The right figure shows the results across all the benchmarks	200
10.2	Performance gain of postpass scheduling on AArch64. The left figure shows each of our handpicked benchmarks. The right figure shows the results across all the	
10.3	benchmarks	200
10.1	negligible computational time).	201
10.4	On the left, statistics of the static branch prediction, evaluated in regards to profiling. On the right, details for each heuristic	203
10.5	Gain of using profiling instead of branch prediction. On the left, we evaluate this gain on the Polybench benchmarks. On the right, we evaluate it on the Taclebench	
10.6	benchmarks	203
10.6	Gain of using superblock linearization instead of base linearization. On the left, the setup includes just postpass scheduling and static branch prediction. On the	
10.5	right, it includes the best version of our optimizations	205
10.7	Impact of the four instruction duplication optimizations on performance and pipeline stalls from instruction cache misses.	206

10.8	Performance gain of prepass scheduling on KV3. The left figure shows each	
	benchmark individually. The right figure shows statistics across all the benchmarks.	210
10.9	Impact of loop unrolling, without prepass, with a threshold of 30	211
10.10	Two versions of the innermost loop from <i>matrix1</i> : non-unrolled on the left, unrolled	
	on the right. See appendix A for an instruction reference	213
10.11	Comparing the performance of CompCert and GCC on KV3. The left figure shows	
	GCC compared relatively to CompCert across all the benchmarks. The right figure	
	shows the reverse: the gain of using CompCert instead of GCC, for the original	
	version of CompCert and the version with our included optimizations	214
10.12	Compiled codes of rad2deg_main: on the left, the code from GCC -O1; on the	
	right, the code from CompCert without loop unrolling. See appendix A for an	
	instruction reference	216
10.13	Comparing the performance of COMPCERT and GCC on AArch64. The left figure	
	shows GCC compared relatively to CompCert across all the benchmarks. The	
	right figure shows the reverse: the gain of using CompCert instead of GCC, for the	
	original version of CompCert and the version with our included optimizations	217
10.14	Comparing the performance of CompCert and GCC on RiscV. The left figure	
	shows GCC compared relatively to CompCert across all the benchmarks. The	
	right figure shows the reverse: the gain of using CompCert instead of GCC, for the	
	original version of CompCert and the version with our included optimizations	217
Lie	t of Tables	
∟ 13	of tables	

Improvement of Cumulated Optimizations w.r.t. mainstream CompCert 208

10.1

Bibliography

- [1] 9899:1999. *International standard—Programming languages—C.* Technical Report. ISO/IEC.
- [2] Andrew W. Appel. 2011. Verified Software Toolchain. In *Programming Languages and Systems*, Gilles Barthe (Ed.). Springer Berlin Heidelberg, Berlin, Heidelberg, 1–17.
- [3] Andrew W Appel. 2016. Verifiable C.
- [4] Thomas Ball and James R. Larus. 1993. Branch Prediction for Free. In *Proceedings of the ACM SIGPLAN 1993 Conference on Programming Language Design and Implementation (PLDI '93)*. Association for Computing Machinery, New York, NY, USA, 300–313. https://doi.org/10.1145/155090.155119
- [5] Gergö Barany. 2018. A more precise, more correct stack and register model for CompCert. In *LOLA 2018 Syntax and Semantics of Low-Level Languages 2018*. Oxford, United Kingdom. https://hal.inria.fr/hal-01799629
- [6] Gilles Barthe, Delphine Demange, and David Pichardie. 2014. Formal Verification of an SSA-Based Middle-End for CompCert. *ACM Trans. Program. Lang. Syst.* 36, 1, Article 4 (March 2014), 35 pages. https://doi.org/10.1145/2579080
- [7] Ezio Bartocci, Yliès Falcone, Adrian Francalanza, and Giles Reger. 2018. *Introduction to Runtime Verification*. Springer International Publishing, Cham, 1–33. https://doi.org/10.1007/978-3-319-75632-5_1
- [8] Ricardo Bedin França, Sandrine Blazy, Denis Favre-Felix, Xavier Leroy, Marc Pantel, and Jean Souyris. 2012. Formally verified optimizing compilation in ACG-based flight control software. In *ERTS2 2012: Embedded Real Time Software and Systems*. AAAF, SEE, Toulouse, France. https://hal.inria.fr/hal-00653367
- [9] Ricardo Bedin França, Denis Favre-Felix, Xavier Leroy, Marc Pantel, and Jean Souyris. 2011. Towards Formally Verified Optimizing Compilation in Flight Control Software. In *PPES 2011: Predictability and Performance in Embedded Systems (OpenAccess Series in Informatics)*, Vol. 18. Schloss Dagstuhl, Leibniz-Zentrum fuer Informatik, Grenoble, France, 59–68. https://doi.org/10.4230/0ASIcs.PPES.2011.59

- [10] Yves Bertot and Pierre Castéran. 2013. *Interactive theorem proving and program development: Coq'Art: the calculus of inductive constructions*. Springer Science & Business Media.
- [11] Armin Biere. 2008. PicoSAT essentials. *Journal on Satisfiability, Boolean Modeling and Computation* 4, 2-4 (2008), 75–97.
- [12] Bruno Blanchet, Patrick Cousot, Radhia Cousot, Jérôme Feret, Laurent Mauborgne, Antoine Miné, David Monniaux, and Xavier Rival. 2002. *Design and Implementation of a Special-Purpose Static Program Analyzer for Safety-Critical Real-Time Embedded Software*. Springer Berlin Heidelberg, Berlin, Heidelberg, 85–108. https://doi.org/10.1007/3-540-36377-7_5
- [13] Sandrine Blazy, Zaynah Dargaye, and Xavier Leroy. 2006. Formal Verification of a C Compiler Front-End. In *FM 2006: Formal Methods*, Jayadev Misra, Tobias Nipkow, and Emil Sekerinski (Eds.). Springer Berlin Heidelberg, Berlin, Heidelberg, 460–475.
- [14] Gabriel Hjort Blindell, Mats Carlsson, Roberto Castañeda Lozano, and Christian Schulte. 2017. Complete and Practical Universal Instruction Selection. ACM Trans. Embed. Comput. Syst. 16, 5s, Article 119 (Sept. 2017), 18 pages. https://doi.org/10.1145/ 3126528
- [15] Sylvain Boulmé. 2021. Draft of Habilitation. (2021).
- [16] Sylvain Boulmé, David Monniaux, and Cyril Six. 2021. Our version of CompCert for KVX architecture. https://gricad-gitlab.univ-grenoble-alpes.fr/certicompil/compcert-kvx
- [17] Timothy Bourke, Lélio Brun, Pierre-Évariste Dagand, Xavier Leroy, Marc Pouzet, and Lionel Rieg. 2017. A Formally Verified Compiler for Lustre. In *Proceedings of the 38th ACM SIGPLAN Conference on Programming Language Design and Implementation (PLDI 2017)*. Association for Computing Machinery, New York, NY, USA, 586–601. https://doi.org/10.1145/3062341.3062358
- [18] Timothy Bourke, Lélio Brun, and Marc Pouzet. 2018. Towards a Verified Lustre Compiler with Modular Reset. In *Proceedings of the 21st International Workshop on Software and Compilers for Embedded Systems (SCOPES '18)*. Association for Computing Machinery, New York, NY, USA, 14–17. https://doi.org/10.1145/3207719.3207732
- [19] Erik Buchanan, Ryan Roemer, Hovav Shacham, and Stefan Savage. 2008. When Good Instructions Go Bad: Generalizing Return-Oriented Programming to RISC. In *Proceedings of the 15th ACM Conference on Computer and Communications Security (CCS '08)*.

- Association for Computing Machinery, New York, NY, USA, 27–38. https://doi.org/10.1145/1455770.1455776
- [20] P. P. Chang and W. W. Hwu. 1988. Trace Selection for Compiling Large C Application Programs to Microcode. In *Proceedings of the 21st Annual Workshop on Microprogramming and Microarchitecture (MICRO 21)*. IEEE Computer Society Press, Washington, DC, USA, 21–29.
- [21] Liang-Fang Chao, A.S. LaPaugh, and E.H.-M. Sha. 1997. Rotation scheduling: a loop pipelining algorithm. *IEEE Transactions on Computer-Aided Design of Integrated Circuits and Systems* 16, 3 (1997), 229–239. https://doi.org/10.1109/43.594829
- [22] Adam Chlipala. 2013. The Bedrock Structured Programming System: Combining Generative Metaprogramming and Hoare Logic in an Extensible Program Verifier. In *Proceedings of the 18th ACM SIGPLAN International Conference on Functional Programming (ICFP '13)*. Association for Computing Machinery, New York, NY, USA, 391–402. https://doi.org/10.1145/2500365.2500592
- [23] Keith D Cooper, Philip J Schielke, and Devika Subramanian. 1998. An experimental evaluation of list scheduling. *TR98* 326 (1998).
- [24] Jack W Davidson and Sanjay Jinturkar. 1995. *An aggressive approach to loop unrolling*. Technical Report. Citeseer.
- [25] Benoît Dupont de Dinechin. 2004. From Machine Scheduling to VLIW Instrution Scheduling. ST Journal of Research 1, 2 (Sept. 2004), 1–35. https://www.cri.ensmp.fr/classement/doc/A-352.ps Also as Mines ParisTech research article A/352/CRI.
- [26] Xavier Leroy et al. 2021. The CompCert verified C compiler. https://github.com/ AbsInt/CompCert
- [27] Heiko Falk, Sebastian Altmeyer, Peter Hellinckx, Björn Lisper, Wolfgang Puffitsch, Christine Rochange, Martin Schoeberl, Rasmus Bo Sørensen, Peter Wägemann, and Simon Wegener. 2016. TACLeBench: A Benchmark Collection to Support Worst-Case Execution Time Research. In 16th International Workshop on Worst-Case Execution Time Analysis. Toulouse, France. https://doi.org/10.4230/0ASIcs.WCET.2016.2
- [28] Yi Fang and Lenore D. Zuck. 2007. Improved Invariant Generation for Tvoc. *Electronic Notes in Theoretical Computer Science* 176, 3 (2007), 21–35. https://doi.org/10.1016/j.entcs.2006.06.016 Proceedings of the 5th International Workshop on Compiler Optimization meets Compiler Verification (COCV 2006).

- [29] Jean-Christophe Filliâtre and Sylvain Conchon. 2006. Type-Safe Modular Hash-Consing. In *Proceedings of the 2006 Workshop on ML (ML '06)*. Association for Computing Machinery, New York, NY, USA, 12–19. https://doi.org/10.1145/1159876.1159880
- [30] Fisher. 1981. Trace Scheduling: A Technique for Global Microcode Compaction. *IEEE Trans. Comput.* C-30, 7 (1981), 478–490. https://doi.org/10.1109/TC.1981. 1675827
- [31] Fisher. 1981. Trace Scheduling: A Technique for Global Microcode Compaction. *IEEE Trans. Comput.* C-30, 7 (1981), 478–490. https://doi.org/10.1109/TC.1981. 1675827
- [32] Joseph A. Fisher. 1983. Very Long Instruction Word Architectures and the ELI-512. In *Proceedings of the 10th Annual International Symposium on Computer Architecture* (*ISCA '83*). Association for Computing Machinery, New York, NY, USA, 140–150. https://doi.org/10.1145/800046.801649
- [33] Joseph A. Fisher, Paolo Faraboschi, and Cliff Young. 2005. *Embedded Computing: A VLIW Approach to Architecture, Compilers and Tools*. Morgan Kaufmann Publishers Inc., San Francisco, CA, USA.
- [34] Yannick Forster and Fabian Kunze. 2016. Verified extraction from Coq to a lambda-calculus. In *Coq Workshop*, Vol. 2016.
- [35] France24. 2021. La panne des numéros d'urgence due à un "bug", selon l'enquête d'Orange. https://www.france24.com/fr/france/20210611-la-panne-des-num%C3%A9ros-d-urgence-due-%C3% A0-un-bug-selon-l-enqu%C3%AAte-d-orange
- [36] J. R. Goodman and W.-C. Hsu. 1988. Code Scheduling and Register Allocation in Large Basic Blocks. In *Proceedings of the 2nd International Conference on Supercomputing (ICS '88)*. Association for Computing Machinery, New York, NY, USA, 442–452. https://doi.org/10.1145/55364.55407
- [37] Ronghui Gu, Jérémie Koenig, Tahina Ramananadro, Zhong Shao, Xiongnan (Newman) Wu, Shu-Chun Weng, Haozhong Zhang, and Yu Guo. 2015. Deep Specifications and Certified Abstraction Layers. In *Proceedings of the 42nd Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages (POPL '15)*. Association for Computing Machinery, New York, NY, USA, 595–608. https://doi.org/10.1145/2676726.2676975

- [38] Ronghui Gu, Zhong Shao, Hao Chen, Xiongnan (Newman) Wu, Jieung Kim, Vilhelm Sjöberg, and David Costanzo. 2016. CertiKOS: An Extensible Architecture for Building Certified Concurrent OS Kernels. In *12th USENIX Symposium on Operating Systems Design and Implementation (OSDI 16)*. USENIX Association, Savannah, GA, 653–669. https://www.usenix.org/conference/osdi16/technical-sessions/presentation/gu
- [39] N. Halbwachs, P. Caspi, P. Raymond, and D. Pilaud. 1991. The synchronous data flow programming language LUSTRE. *Proc. IEEE* 79, 9 (1991), 1305–1320. https://doi.org/10.1109/5.97300
- [40] Wen-Mei W. Hwu, Scott A. Mahlke, William Y. Chen, Pohua P. Chang, Nancy J. Warter, Roger A. Bringmann, Roland G. Ouellette, Richard E. Hank, Tokuzo Kiyohara, Grant E. Haab, John G. Holm, and Daniel M. Lavery. 1993. *The Superblock: An Effective Technique for VLIW and Superscalar Compilation*. Springer US, Boston, MA, 229–248. https://doi.org/10.1007/978-1-4615-3200-2_7
- [41] INRIA 2019. The CompCert C verified compiler—Documentation and user's manual (version 3.5 ed.). INRIA.
- [42] Leslie A Johnson et al. 1998. DO-178B: Software considerations in airborne systems and equipment certification. *Crosstalk, October* 199 (1998), 11–20.
- [43] Daniel Kästner, Jörg Barrho, Ulrich Wünsche, Marc Schlickling, Bernhard Schommer, Michael Schmidt, Christian Ferdinand, Xavier Leroy, and Sandrine Blazy. 2018. CompCert: Practical Experience on Integrating and Qualifying a Formally Verified Optimizing Compiler. In *ERTS2 2018 9th European Congress Embedded Real-Time Software and Systems*. 3AF, SEE, SIE, Toulouse, France, 1–9. https://hal.inria.fr/hal-01643290
- [44] Gary A. Kildall. 1973. A Unified Approach to Global Program Optimization. In *Proceedings of the 1st Annual ACM SIGACT-SIGPLAN Symposium on Principles of Programming Languages (POPL '73)*. Association for Computing Machinery, New York, NY, USA, 194–206. https://doi.org/10.1145/512927.512945
- [45] Phil Koopman. 2014. A Case Study of Toyota Unintended Acceleration and Software Safety. https://users.ece.cmu.edu/~koopman/pubs/koopman14_toyota_ua_slides.pdf
- [46] D. J. Kuck, R. H. Kuhn, D. A. Padua, B. Leasure, and M. Wolfe. 1981. Dependence Graphs and Compiler Optimizations. In *Proceedings of the 8th ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages (POPL '81)*. Association for Computing

- Machinery, New York, NY, USA, 207–218. https://doi.org/10.1145/567532.567555
- [47] Monica S Lam. 1989. Software pipelining. In *A Systolic Array Optimizing Compiler*. Springer, 83–124.
- [48] Tom Lane and the Independent JPEG Group (IJG). 1998. Libjpeg. http://libjpeg.sourceforge.net/
- [49] M. Lee, P. Tirumalai, and T.-F. Ngai. 1993. Software pipelining and superblock scheduling: compilation techniques for VLIW machines. In [1993] Proceedings of the Twenty-sixth Hawaii International Conference on System Sciences, Vol. i. 202–213 vol.1. https://doi.org/10.1109/HICSS.1993.270744
- [50] Xavier Leroy. 2009. Formal Verification of a Realistic Compiler. *Commun. ACM* 52, 7 (July 2009), 107–115. https://doi.org/10.1145/1538788.1538814
- [51] Xavier Leroy. 2009. A formally verified compiler back-end. *Journal of Automated Reasoning* 43, 4 (2009), 363–446. http://xavierleroy.org/publi/compcert-backend.pdf
- [52] Xavier Leroy. 2017. How I found a crash bug with hyperthreading in Intel's Skylake processors. https://thenextweb.com/contributors/2017/07/05/found-crash-bug-hyperthreading-intels-skylake-processors/
- [53] Martin Leucker and Christian Schallhart. 2009. A brief account of runtime verification. *The Journal of Logic and Algebraic Programming* 78, 5 (2009), 293–303. https://doi.org/10.1016/j.jlap.2008.08.004 The 1st Workshop on Formal Languages and Analysis of Contract-Oriented Software (FLACOS'07).
- [54] Hanbing Li, Isabelle Puaut, and Erven Rohou. 2014. Traceability of Flow Information: Reconciling Compiler Optimizations and WCET Estimation. In *Proceedings of the 22nd International Conference on Real-Time Networks and Systems (RTNS '14)*. Association for Computing Machinery, New York, NY, USA, 97–106. https://doi.org/10.1145/2659787.2659805
- [55] P. Geoffrey Lowney, Stefan M. Freudenberger, Thomas J. Karzes, W. D. Lichtenstein, Robert P. Nix, John S. O'Donnell, and John C. Ruttenberg. 1993. *The Multiflow Trace Scheduling Compiler*. Springer US, Boston, MA, 51–142. https://doi.org/10. 1007/978-1-4615-3200-2_4
- [56] lowRISC. 2021. Rocket core overview. https://www.cl.cam.ac.uk/~jrrk2/docs/tagged-memory-v0.1/rocket-core/

- [57] Roberto Castañeda Lozano, Mats Carlsson, Gabriel Hjort Blindell, and Christian Schulte. 2019. Combinatorial Register Allocation and Instruction Scheduling. ACM Trans. Program. Lang. Syst. 41, 3, Article 17 (July 2019), 53 pages. https://doi.org/10.1145/3332373
- [58] Roberto Castañeda Lozano, Mats Carlsson, Gabriel Hjort Blindell, and Christian Schulte. 2019. Combinatorial Register Allocation and Instruction Scheduling. ACM Trans. Program. Lang. Syst. 41, 3, Article 17 (July 2019), 53 pages. https://doi.org/10.1145/3332373
- [59] Jamie Lynch. 2017. The Worst Computer Bugs in History: The Ariane 5 Disaster. https://www.bugsnag.com/blog/bug-day-ariane-5-disaster
- [60] Alexander B. Magoun and Paul Israel. 2013. Did you Know? Edison Coined the Term "Bug". https://spectrum.ieee.org/the-institute/ieee-history/did-you-know-edison-coined-the-term-bug
- [61] Andrey Makhorin. 2012. GNU Linear Programming Kit. https://www.gnu.org/software/glpk/
- [62] Giovanni De Micheli. 1994. Synthesis and Optimization of Digital Circuits. McGraw-Hill.
- [63] David Monniaux and Cyril Six. 2021. Simple, Light, Yet Formally Verified, Global Common Subexpression Elimination and Loop-Invariant Code Motion. (2021).
- [64] Alain Mosnier. 2019. SHA-256 implementation. https://github.com/amosnier/sha-2
- [65] Rajeev Motwani, Krishna V Palem, Vivek Sarkar, and Salem Reyen. 1995. Combining register allocation and instruction scheduling. *Courant Institute, New York University* (1995).
- [66] Steven Muchnick et al. 1997. Advanced compiler design implementation. Morgan kaufmann.
- [67] George C. Necula. 2000. Translation Validation for an Optimizing Compiler. In *Proceedings of the ACM SIGPLAN 2000 Conference on Programming Language Design and Implementation (PLDI '00)*. Association for Computing Machinery, New York, NY, USA, 83–94. https://doi.org/10.1145/349299.349314
- [68] BBC News. 2013. Bug found in Post Office row computer system. https://www.bbc.com/news/uk-23233573

- [69] David Lorge Parnas, GJK Asmis, and Jan Madey. 1991. Assessment of safety-critical software in nuclear power plants. *Nuclear safety* 32, 2 (1991), 189–198.
- [70] David L. Parnas, A. John van Schouwen, and Shu Po Kwan. 1990. Evaluation of Safety-Critical Software. *Commun. ACM* 33, 6 (June 1990), 636–648. https://doi.org/10.1145/78973.78974
- [71] Conor Patrick. 2015. Bitsliced AES implementation. https://github.com/conorpp/bitsliced-aes
- [72] Karl Pettis and Robert C. Hansen. 1990. Profile Guided Code Positioning. In Proceedings of the ACM SIGPLAN 1990 Conference on Programming Language Design and Implementation (PLDI '90). Association for Computing Machinery, New York, NY, USA, 16–27. https://doi.org/10.1145/93542.93550
- [73] Clément Pit-Claudel, Peng Wang, Benjamin Delaware, Jason Gross, and Adam Chlipala. 2020. Extensible Extraction of Efficient Imperative Programs with Foreign Functions, Manually Managed Memory, and Proofs. In *Automated Reasoning*, Nicolas Peltier and Viorica Sofronie-Stokkermans (Eds.). Springer International Publishing, Cham, 119–137.
- [74] André Platzer. 2010. Lecture Notes on Loop-Invariant Code Motion. (2010).
- [75] A. Pnueli, M. Siegel, and E. Singerman. 1998. Translation validation. In *Tools and Algorithms for the Construction and Analysis of Systems*, Bernhard Steffen (Ed.). Springer Berlin Heidelberg, Berlin, Heidelberg, 151–166.
- [76] Louis-Noël Pouchet. 2012. The Polyhedral Benchmark suite. http://web.cs.ucla.edu/~pouchet/software/polybench/
- [77] Marc Pouzet. 1994. *Compaction des langages fonctionnels*. Ph.D. Dissertation. Université Paris VII.
- [78] B. Ramakrishna Rau, Christopher D. Glaeser, and Raymond L. Picard. 1982. Efficient Code Generation for Horizontal Architectures: Compiler Techniques and Architectural Support. In *Proceedings of the 9th Annual Symposium on Computer Architecture (ISCA* '82). IEEE Computer Society Press, Washington, DC, USA, 131–139.
- [79] J. Richardson and J. Green. 2004. Automating traceability for generated software artifacts. In *Proceedings*. 19th International Conference on Automated Software Engineering, 2004. 24–33. https://doi.org/10.1109/ASE.2004.1342721
- [80] Lionel Rieg and David Monniaux. 2021. Modified version of Vélus for compatibility. https://gricad-gitlab.univ-grenoble-alpes.fr/certicompil/velus

- [81] Xavier Rival. 2004. Symbolic Transfer Function-Based Approaches to Certified Compilation. In *Proceedings of the 31st ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages (POPL '04)*. Association for Computing Machinery, New York, NY, USA, 1–13. https://doi.org/10.1145/964001.964002
- [82] Valentin Robert and Xavier Leroy. 2012. A Formally-Verified Alias Analysis. In *Certified Programs and Proofs*, Chris Hawblitzel and Dale Miller (Eds.). Springer Berlin Heidelberg, Berlin, Heidelberg, 11–26.
- [83] Vivek Sarkar, Mauricio J. Serrano, and Barbara B. Simons. 2001. Register-Sensitive Selection, Duplication, and Sequencing of Instructions. In *Proceedings of the 15th International Conference on Supercomputing (ICS '01)*. Association for Computing Machinery, New York, NY, USA, 277–288. https://doi.org/10.1145/377792.377849
- [84] Olivier Savary Bélanger et al. 2019. Verified Extraction for Coq. (2019).
- [85] Thomas Sewell. 2017. *Translation validation for verified, efficient and timely operating systems*. Ph.D. Dissertation. University of New South Wales, Sydney, Australia. http://handle.unsw.edu.au/1959.4/58861
- [86] Thomas Arthur Leck Sewell, Magnus O. Myreen, and Gerwin Klein. 2013. Translation validation for a verified OS kernel. In *ACM SIGPLAN Conference on Programming Language Design and Implementation*, *PLDI '13*, *Seattle*, *WA*, *USA*, *June 16-19*, 2013, Hans-Juergen Boehm and Cormac Flanagan (Eds.). ACM, 471–482. https://doi.org/10.1145/2491956.2462183
- [87] Ghassan Shobaki, Maxim Shawabkeh, and Najm Eldeen Abu Rmaileh. 2013. Preallocation Instruction Scheduling with Register Pressure Minimization Using a Combinatorial Optimization Approach. *ACM Trans. Archit. Code Optim.* 10, 3, Article 14 (Sept. 2013), 31 pages. https://doi.org/10.1145/2512432
- [88] Cyril Six, Sylvain Boulmé, and David Monniaux. 2020. Certified and Efficient Instruction Scheduling: Application to Interlocked VLIW Processors. *Proc. ACM Program. Lang.* 4, OOPSLA, Article 129 (Nov. 2020), 29 pages. https://doi.org/10.1145/3428197
- [89] Cyril Six, Léo Gourdin, Sylvain Boulmé, and David Monniaux. 2021. Verified Superblock Scheduling with Related Optimizations. (April 2021). https://hal.archives-ouvertes.fr/hal-03200774 preprint.
- [90] Stéphane Strahm. 2021. High Performance Programming: Offloading on Manycore Architecture.

- [91] Yong Kiam Tan, Magnus O. Myreen, Ramana Kumar, Anthony Fox, Scott Owens, and Michael Norrish. 2019. The Verified CakeML Compiler Backend. *Journal of Functional Programming* 29 (February 2019). https://kar.kent.ac.uk/71304/
- [92] Ross Tate, Michael Stepp, Zachary Tatlock, and Sorin Lerner. 2009. Equality Saturation: A New Approach to Optimization. In *Proceedings of the 36th Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages (POPL '09)*. Association for Computing Machinery, New York, NY, USA, 264–276. https://doi.org/10.1145/1480881.1480915
- [93] Jean-Baptise Tristan. 2009. *Formal verification of translation validators*. Ph.D. Dissertation. Université Paris 7 Diderot.
- [94] Jean-Baptiste Tristan, Paul Govereau, and Greg Morrisett. 2011. Evaluating Value-Graph Translation Validation for LLVM. In *Proceedings of the 32nd ACM SIGPLAN Conference on Programming Language Design and Implementation (PLDI '11)*. Association for Computing Machinery, New York, NY, USA, 295–305. https://doi.org/10.1145/1993498.1993533
- [95] Jean-Baptiste Tristan and Xavier Leroy. 2008. Formal Verification of Translation Validators: A Case Study on Instruction Scheduling Optimizations. In *Proceedings of the 35th Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages (POPL '08)*. Association for Computing Machinery, New York, NY, USA, 17–27. https://doi.org/10.1145/1328438.1328444
- [96] Jean-Baptiste Tristan and Xavier Leroy. 2008. Formal Verification of Translation Validators: A Case Study on Instruction Scheduling Optimizations. In *Proceedings of the 35th Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages (POPL '08)*. Association for Computing Machinery, New York, NY, USA, 17–27. https://doi.org/10.1145/1328438.1328444
- [97] Jean-Baptiste Tristan and Xavier Leroy. 2009. Verified Validation of Lazy Code Motion. In *Proceedings of the 30th ACM SIGPLAN Conference on Programming Language Design and Implementation (PLDI '09)*. Association for Computing Machinery, New York, NY, USA, 316–326. https://doi.org/10.1145/1542476.1542512
- [98] Jean-Baptiste Tristan and Xavier Leroy. 2010. A Simple, Verified Validator for Software Pipelining. In *Proceedings of the 37th Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages (POPL '10)*. Association for Computing Machinery, New York, NY, USA, 83–92. https://doi.org/10.1145/1706299.1706311
- [99] Sven Verdoolaege. 2016. Presburger formulas and polyhedral compilation. (2016).

- [100] Xuejun Yang, Yang Chen, Eric Eide, and John Regehr. 2011. Finding and Understanding Bugs in C Compilers. In *Proceedings of the 32nd ACM SIGPLAN Conference on Programming Language Design and Implementation (PLDI '11)*. Association for Computing Machinery, New York, NY, USA, 283–294. https://doi.org/10.1145/1993498. 1993532
- [101] Junbeom Yoo, Eunkyoung Jee, and Sungdeok Cha. 2009. Formal Modeling and Verification of Safety-Critical Software. *IEEE Software* 26, 3 (2009), 42–49. https://doi.org/10.1109/MS.2009.67
- [102] Yiji Zhang and Lenore D. Zuck. 2018. Formal Verification of Optimizing Compilers. In *Distributed Computing and Internet Technology*, Atul Negi, Raj Bhatnagar, and Laxmi Parida (Eds.). Springer International Publishing, Cham, 50–65.
- [103] Jianzhou Zhao, Santosh Nagarakatte, Milo M.K. Martin, and Steve Zdancewic. 2012. Formalizing the LLVM Intermediate Representation for Verified Program Transformations. In *Proceedings of the 39th Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages (POPL '12)*. Association for Computing Machinery, New York, NY, USA, 427–440. https://doi.org/10.1145/2103656.2103709
- [104] Lenore D. Zuck, Amir Pnueli, and Benjamin Goldberg. 2003. VOC: A Methodology for the Translation Validation of Optimizing Compilers. *J. UCS* 9, 3 (2003), 223–247. https://doi.org/10.3217/jucs-009-03-0223