

Shape Analysis of 3D Human Faces and Applications Boulbaba Ben Amor

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Mémoire présenté pour l'obtention de L'HABILITATION À DIRIGER DES RECHERCHES

Shape Analysis of 3D Human Faces and Applications

$\mathbf{P}\mathbf{A}\mathbf{R}$

Boulbaba BEN AMOR

December 2, 2014

Committee

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A cknowledgements

Thanks for reading...

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Bibliography

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Part I

Synthesis of Activities

Curriculum Vitae

Boulbaba BEN AMOR, 36 years, married, 1 child.

Associate Professor (Maître de conférences) with Institut Mines-Télécom/Télécom Lille, Member of Computer Science Laboratory of Lille (LIFL UMR CNRS/Lille1 8022), Cité scientifique - Rue Guglielmo Marconi, 59653 Villeneuve d'Ascq Cedex BP 20145 - FRANCE. Tél : + (33) 3 20 43 64 18 Fax : + (33) 3 20 33 55 99 E-mail : benamor@telecom-lille.fr Web : http://www.telecom-lille.fr/people/benamor/

Education —

| 2003-2006 | Ph.D. in Computer Science, with highest honor, |
|-------------|--|
| | École Centrale de Lyon – France. |
| | Laboratoire d'InfoRmatique en Image et Systèmes d'information (LIRIS UMR 5205 CNRS). |
| 2002-2003 | Master Degree in Computer Science, Images & Systems, |
| | École Centrale de Lyon – France. |
| | Laboratoire d'InfoRmatique en Image et Systèmes d'information (LIRIS UMR 5205 CNRS). |
| 1999-2002 | Engineer Degree in Computer Science, |
| | National Engineering School of Sfax (ENIS) – Tunisia. |
| 1997 - 1999 | Two-year classes to prepare for admission to Engineer Schools, |
| | Preparatory Institute for Engineering Studies of Sfax (IPEIS) – Tunisia. |
| 1997 | Baccalauréat in Mathematics – Tunisia. |

Positions —

| 2007-present | Associate Professor (Maître de conférences), Institut Mines-Télécom, |
|--------------|---|
| | Department of Computer Science & Networks, Télécom Lille. |
| | Laboratoire d'Informatique Fondamentale de Lille (LIFL UMR CNRS/Lille1 8022). |
| 2014 | Visiting Professor (January-August), Florida State University – USA, |
| | Supported conjointly by Institut Mines-Télécom and Florida State University. |
| | Statistical Shape Analysis and Modeling Group (SSAMG), Department of Statistics, FSU. |
| 2006-2007 | Assistant Professor (A.T.E.R), Ecole Centrale de Lyon – France, |
| | Department of Mathematics & Computer Science, École Centrale de Lyon. |
| 2005-2006 | Temporary Lecturer, EPSI de Lyon – France, |
| | École Privé des Sciences Informatique, Lyon. |

Research Grants

2010 - 2013 — ANR¹ blanc international 3D Face Analyzer, Partners: École Centrale de Lyon/LIRIS, Lille1/LIFL, Baihang University/IRIP, North China University of Technology (NCUT). Leader of work-package, co-supervision of two post-docs.

2008 - 2011 — ANR Face Analysis and Recognition using 3D (FAR-3D), Partners: Lille1/LIFL, École Centrale de Lyon/LIRIS, Eurecom, THALES R&T. Leader of work-package, co-supervision of one Ph.D. and one Master projects, development of the 3D Face Authentication demonstration.

2008 - 2013 — CPER-CIA (Contrat Plan État Région – Campus Intelligence Ambiante) contract funded by the Région Nord-Pas de Calais. Leader of the 3D acquisition platform.

2008 - 2011 — CMCU French-Tunisian project, Partners: Lille1/LIFL, École Centrale de Lyon/LIRIS, ENSI/CRISTAL, ENIS/REGIM . Supervision of one Ph.D. student.

2005 - 2007 — Techno-vision IV² (Identification par l'Iris et le Visage via la Vidéo) co-funded by Ministère de la Recherche and Ministère de la Défense, Partners: GET - INT, GET - ENST, IMEDIA - INRIA, Institut EURECOM, Let It Wave, LIRIS - École Centrale de Lyon, IBISC - Université d'Evry, THALES (TRT), URATEK . Design of acquisition settings and evaluation protocols of 3D face recognition algorithms.

Students Supervision —

Ph.D. thesis (5)

2008 - 2011 — Hassen Drira, Statistical Computing on Manifolds for 3D Face Analysis and Recognition, defense on July, 2011, University of Lille1, ANR funding, co-supervision with Prof. Mohamed Daoudi – rate 50%.

2009 - 2012 — Ahmed Maalej, 3D Facial Expressions Recognition using Shape Analysis and Machine Learning, defense on May 2012, University of Lille1, Funded by Institut Mines-Télécom/Région Nord-Pas de Calais, co-supervision with Prof. Mohamed Daoudi – rate 50%.

2009 - 2012 — Lahoucine Ballihi, 3D Facial Biometrics by learning Geometric Features, defense on May 2012, University of Lille1 & University Mohammed V-Agdal (Rabat, Morocco), Funded by STIC Morocco program, co-supervision with Prof. Mohamed Daoudi & Pr. Driss Aboutajdine (University Mohammed V-Agdal)– rate 40%.

2011 - present — **Baiqiang Xia**, Learning 3D Geometric Features for Soft Biometrics Recognition, defense planned for November 2014, **University of Lille1**, Funded by the China Scholarship Council (CSC), co-supervision with Prof. Mohamed Daoudi – rate 70%.

2012 - present — **Taleb Alashkar**, 3D Face Dynamic Sequences Analysis: Application to Face and Facial Expression Recognition, defense planned for October 2015, **University of Lille1**, Funded by the Future & Rupture program supported by Institut Mines-Télécom, co-supervision with Prof. Mohamed Daoudi & Prof. Stefano Berretti (University of Firenze, Italy) – rate 70%.

¹www.agence-nationale-recherche.fr/en/project-based-funding-to-advance-french-research/

Post-docs (2)

2012 - 2013 — Lahoucine Ballihi, Post-doc, University of Lille1, Funded by the ANR, cosupervision with Prof. Mohamed Daoudi – rate 50%.

2011 - 2012 — Hassen Drira, Post-doc, University of Lille1, Funded by the ANR, co-supervision with Prof. Mohamed Daoudi – rate 50%.

Masters (2)

2010 - 2011 — Rim Slama, Master, 3D Face Recognition under Occlusions, defense on July 2011, Ecole Nationale des Sciences de l'Informatique, Tunisie, co-supervision with Prof. Mohamed Daoudi – rate 50%.

2012 — Marion Detourmignies, final year study project at Telecom Lille, Expression Analysis from Depth-consumer 3D Sensors, defense on September 2012, Télécom Lille, co-supervision with Prof. Mohamed Daoudi & Prof. Ludovic Macaire (LAGIS Lab.)– rate 50%.

Collaborations

Statistical Shape Analysis and Modeling Group (SSAMG), Florida State University, USA, I visited the FSU for 8 months (December 2013 - August 2014) as a Visitor Scholar – My stay was supported conjointly by Institut Mines-Télécom and Florida State University. Collaboration with *Prof. Anuj Srivastava* giving rise to 6 common journal publications and several international conferences.

Media Integration and Communication Center (MICC), University of Firenze, Italy, collaboration with *Prof. Stefano Berretti*, resulted in 3 journal publications. Co-supervision of the thesis of Taleb Alashkar supported by the Future & Rupture program of Institut Mines-Télécom (2013-2015). Taleb Alashkar received financial help of DAI N11 from University of Lille1 for a 2-months staying at Media Integration and Communication Center (MICC), University of Firenze.

Laboratory of Intelligent Recognition and Image Processing (IRIP), Beihang University, China, collaboration with *Prof. Yunhong Wang* and *Dr. Di Huang*, since 2010. Collaboration part of the ANR-NSFC 3D Face Analyzer project. This collaboration have resulted in 2 conference papers. Baiquiang Xia, Ph.D. student at University of Lille1, spent 6 weeks with the IRIP Lab., in 2013.

Laboratoire d'InfoRmatique en Image et Systèmes d'information (LIRIS), Ecole Centrale de Lyon, France, collaboration with *Prof. Liming Chen* and *Dr. Mohsen Ardabilian*. We have participated together to the ANR FAR-3D and ANR blanc international 3D Face Analyzer projects. We co-wrote the first chapter of the book *3D Face Modeling and Recognition* [O1], published in 2013. I was invited to the Ph.D. committee of Wael Ben Soltana, the defense organized in December 2012.

Invited talks and Seminars

CAR, Center for Automation Research, University of Maryland College Park, USA, July 2014.

SSAMG Group, Florida State University, USA, January 2014.

IRIP Lab., Baihang University, China, April 2013 & July 2011.

VIVA Lab., University of Ottawa, Canada, July 2012.

Bell Labs, Belgium, March 2013.

Workshop « 3D Human Modeling », IMAGINA event, Monaco, February 2011²

Workshop « Essor du Nomadisme : une sécurité suffisante ? », International forum on Cybercriminality, Lille, January 2010.³

Services to the community –

Journal Review Committees

Reviewer for several journals as – IEEE Transactions on Image Processing – IEEE Transactions on Multimedia – IEEE Transactions on Information Forensics & Security – Image and Vision Computing – Pattern Recognition Letters – Computers & Graphics – EURASIP Journal on Image and Video Processing – International Journal of Pattern Recognition and Artificial Intelligence – IET Computer Vision.

Conferences Review Committees

Reviewer for several international conferences and workshops as IAPR International Conference on Pattern Recognition (ICPR) – IEEE International Conference on Image Processing (ICIP) – IEEE/RSJ International Conference on Intelligent Robots and Systems – EUSIPCO – SITIS – CORESA – Eurographics Workshop on 3D Object Retrieval (2010) – FG 3D Face Biometrics Workshop (FG'13) – and others.

Conference Program Committees

Member of technical committees of the following conferences and workshops 3D Face Biometrics Workshop (in conjunction with the Automatic Face and Gesture Recognition conference, 2013)– 3D Object Retrieval Workshop (in conjunction with ACM Multimedia 2010) – International Conference on Signal Image Technology & Internet Based Systems, SITIS – International Conference on Intelligent Machines, ICIM – CORESA (COmpression et REprésentation des Signaux Audiovisuels) – TAIMA (Ateliers de Travail sur le Traitement et l'Analyse de l'Information).

Conferences Organizing Committees

Member of the organization committee of 15th edition of CORESA (COmpression et REprésentation des Signaux Audiovisuels), Lille, 24-25 May 2012.

Member of the organization committee of the international conference Shape Modeling International (SMI), which will take place in Lille in 2015.

²http://www.imagina.mc/2011/content/Industry-speakers/industry_speakersUK.php

³https://cybercriminalite.wordpress.com/

Participation to Ph.D. committees

Member of the thesis committee of Wael Ben Soltana, École Centrale de Lyon, December 2012.

Member of the thesis committee (midterm) of François Lamare, Télécom SudParis, September 2014.

Awards —

Best Paper Award⁴ received for our paper titled – Can 3D Shape of the Face Reveal Your Age? – in the international conference on Computer Vision Theory and Applications (VISAPP) 2014, with *Baiqiang Xia (PhD student), Mohamed Daoudi and Hassen Drira.*

Affiliation to Scientific Societies

Member of IEEE (Institute of Electrical and Electronics Engineers).

Member of GDR-ISIS⁵, Image et Vision theme.

Member of AFRIF⁶ (Association Française de Reconnaissance et d'Interprétation des Formes).

Publications -

Articles in international peer-reviewed journals (7)

[J1] <u>Boulbaba Ben Amor</u>, Hassen Drira, Stefano Berretti, Mohamed Daoudi, Anuj Srivastava, 4D Facial Expression Recognition by Learning Geometric Deformations. Accepted for publication as regular paper in the IEEE Tran. on Cybernetics, 2014 (published online). (Impact Factor: 3.236).

[J2] Hassen Drira, **Boulbaba Ben Amor**, Anuj Srivastava, Mohamed Daoudi, Rim Slama, *3D Face Recognition under Expressions, Occlusions, and Pose Variations*. IEEE Trans. Pattern Anal. Mach. Intell. 35(9): 2270-2283, 2013. (Impact Factor: 4.795).

[J3] Lahoucine Ballihi, <u>Boulbaba Ben Amor</u>, Mohamed Daoudi, Anuj Srivastava, Driss Aboutajdine, Boosting 3-D-Geometric Features for Efficient Face Recognition and Gender Classification. IEEE Transactions on Information Forensics and Security 7(6): 1766-1779, 2012. (Impact Factor: 1.895).

[J4] Ahmed Maalej, <u>Boulbaba Ben Amor</u>, Mohamed Daoudi, Anuj Srivastava, Stefano Berretti, *Shape analysis of local facial patches for 3D facial expression recognition*. Pattern Recognition 44(8): 1581-1589, 2011.(Impact Factor: 2.632).

[J5] Stefano Berretti, <u>Boulbaba Ben Amor</u>, Mohamed Daoudi, Alberto Del Bimbo, 3D facial expression recognition using SIFT descriptors of automatically detected keypoints. The Visual Computer 27(11): 1021-1036, 2011. (Impact Factor: 0.91).

⁴visapp.visigrapp.org/PreviousAwards.aspx

⁵gdr-isis.fr/

⁶www.afrif.asso.fr/

[J6] <u>Boulbaba Ben Amor</u>, Hassen Drira, Lahoucine Ballihi, Anuj Srivastava, Mohamed Daoudi, An experimental illustration of 3D facial shape analysis under facial expressions. Annals of telecommunications 64(5-6): 369-379, 2009. (Impact Factor: 0.56).

[J1-s] Baiqiang Xia, <u>Boulbaba Ben Amor</u>, Mohamed Daoudi, *Combining Face Averageness and Symmetry for 3D-based Gender Classification*. <u>Accepted for publication</u> in Pattern Recognition, 2014 (Impact Factor: 2.584).

Articles under review, or in progress (3)

[J2-s] <u>Boulbaba Ben Amor</u>, Jingyong Su, Anuj Srivastava, Action Recognition Using Rate-Invariant Analysis of Skeletal Shape Trajectories. <u>Major Revisions</u> in IEEE Trans. Pattern Anal. Mach. Intell., 2014.

[J3-s] Baiqiang Xia, <u>Boulbaba Ben Amor</u>, Mohamed Daoudi, Joint Gender, Ethnicity and Age Estimation from 3D Faces - An Experimental Illustration of their Mutual Correlations. Submitted to International Journal of Computer Vision, 2014.

[J4-s] <u>Boulbaba Ben Amor</u> and Anuj Srivastava, Sequential Test of Skeletal Shape Trajectories for Early Action Recognition. (In preparation).

Book Chapters (4)

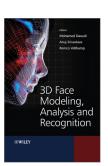
[O1] Contributor in three chapters of the book "3D Face Modeling, Analysis and Recognition"⁷, Editors Mohamed Daoudi, Anuj Srivastava, Remco Veltkamp, ISBN: 978-0-470-66641-8, Wiley, August 2013.

- Chapiter I, *3D Face Modeling*, **Boulbaba Ben Amor**, Mohsen Ardabilian and Liming Chen.
- Chapiter III, 3D Face Surface Analysis and Recognition Based on Facial Curves, Hassen Drira, Stefano Berretti, <u>Boulbaba Ben Amor</u>, Mohamed Daoudi, Anuj Srivastava, Alberto del Bimbo and Pietro Pala.
- Chapiter V, *Applications*, Stefano Berretti, <u>Boulbaba Ben Amor</u>, Hassen Drira, Mohamed Daoudi, Anuj Srivastava, Alberto del Bimbo and Pietro Pala.

[O2] Contributor in the chapter *Elastic Shape Analysis of Functions, Curves, and Trajectories* of the book "*Riemannian Computing in Computer Vision*"⁸, Editors Pavan Turaga, and Anuj Srivastava (In preparation).

Articles in selective international peer-reviewed conferences and workshops (24)

[C1] Baiqiang Xia, <u>Boulbaba Ben Amor</u>, Mohamed Daoudi, Hassen Drira: *Can 3D Shape of the Face Reveal your Age*? International Conference on Computer Vision Theory and Applications (VISAPP 2014), **Best Paper Award**⁹.



⁷http://www.wiley.com/WileyCDA/WileyTitle/productCd-0470666412.html

⁸http://www.public.asu.edu/~pturaga/RCCV/Welcome.html

⁹http://www.visapp.visigrapp.org/PreviousAwards.aspx

[C2] Baiqiang Xia, <u>Boulbaba Ben Amor</u>, Hassen Drira, Mohamed Daoudi, Lahoucine Ballihi: *Gender and 3D facial symmetry: What's the relationship?* 10th IEEE International Conference and Workshops on Automatic Face and Gesture Recognition (FG 2013).

[C3] Baiqiang Xia, <u>Boulbaba Ben Amor</u>, Huang Di, Daoudi Mohamed, Wang Yunhong, Drira Hassen: *Enhancing Gender Classification by Combining 3D and 2D Face Modalities*, 21th European Signal Processing Conference (EUSIPCO) (2013).

[C4] Mohamed Daoudi, Hassen Drira, <u>Boulbaba Ben Amor</u>, Stefano Berretti: A dynamic geometrybased approach for 4D facial expressions recognition. EUVIP 2013: 280-284.

[C5] Hassen Drira, <u>Boulbaba Ben Amor</u>, Mohamed Daoudi, Stefano Berretti: A Dense Deformation Field for Facial Expression Analysis in Dynamic Sequences of 3D Scans. HBU 2013: 148-159.

[C6] Lahoucine Ballihi, Anuj Srivastava, <u>Boulbaba Ben Amor</u>, Mohamed Daoudi, Driss Aboutajdine: Which 3D geometric facial features give up your identity? ICB 2012: 119-124.

[C7] Hassen Drira, <u>Boulbaba Ben Amor</u>, Mohamed Daoudi, Anuj Srivastava, Stefano Berretti: 3D dynamic expression recognition based on a novel Deformation Vector Field and Random Forest. ICPR 2012: 1104-1107.

[C8] Wael Ben Soltana, Mohsen Ardabilian, Pierre Lemaire, Di Huang, Przemysław Szeptycki, Liming Chen, Nesli Erdogmus, Lionel Daniel, Jean-Luc Dugelay, <u>Boulbaba Ben Amor</u>, Hassen Drira, Mohamed Daoudi, Joseph Colineau: *3D face recognition: A robust multi-matcher approach to data degradations.* ICB 2012: 103-110.

[C9] Remco C. Veltkamp, Stefan van Jole, Hassen Drira, <u>Boulbaba Ben Amor</u>, Mohamed Daoudi, Huibin Li, Liming Chen, Peter Claes, Dirk Smeets, Jeroen Hermans, Dirk Vandermeulen, Paul Suetens: SHREC '11 Track: 3D Face Models Retrieval. 3DOR 2011: 89-95.

[C10] Lahoucine Ballihi, <u>Boulbaba Ben Amor</u>, Mohamed Daoudi, Anuj Srivastava, Driss Aboutajdine: Selecting 3D Curves on the Nasal Surface using AdaBoost for Person Authentication. 3DOR 2011: 101-104.

[C11] Stefano Berretti, <u>Boulbaba Ben Amor</u>, Mohamed Daoudi, Alberto Del Bimbo: *Person Inde*pendent 3D Facial Expression Recognition by a Selected Ensemble of SIFT Descriptors. 3DOR 2010: 47-54.

[C12] Hassen Drira, <u>Boulbaba Ben Amor</u>, Mohamed Daoudi, Anuj Srivastava: *Pose and Expression-Invariant 3D Face Recognition using Elastic Radial Curves*. BMVC 2010: 1-11.

[C13] Stefano Berretti, Alberto Del Bimbo, Pietro Pala, <u>Boulbaba Ben Amor</u>, Mohamed Daoudi: A Set of Selected SIFT Features for 3D Facial Expression Recognition. ICPR 2010: 4125-4128.

[C14] Ahmed Maalej, <u>Boulbaba Ben Amor</u>, Mohamed Daoudi, Anuj Srivastava, Stefano Berretti: Local 3D Shape Analysis for Facial Expression Recognition. ICPR 2010: 4129-4132.

[C15] Hassen Drira, <u>Boulbaba Ben Amor</u>, Mohamed Daoudi, Anuj Srivastava: Nasal Region Contribution in 3D Face Biometrics Using Shape Analysis Framework. ICB 2009: 357-366.

[C16] Hassen Drira, <u>Boulbaba Ben Amor</u>, Anuj Srivastava, Mohamed Daoudi: A Riemannian analysis of 3D nose shapes for partial human biometrics. ICCV 2009: 2050-2057.

[C17] Salwa Said, <u>Boulbaba Ben Amor</u>, Mourad Zaied, Chokri Ben Amar, Mohamed Daoudi: *Fast and efficient 3D face recognition using wavelet networks*. ICIP 2009: 4153-4156.

[C18] Joseph Colineau, Johan D'Hose, <u>Boulbaba Ben Amor</u>, Mohsen Ardabilian, Liming Chen, Bernadette Dorizzi: 3D Face Recognition Evaluation on Expressive Faces Using the IV2 Database. ACIVS 2008: 1050-1061.

[C19] <u>Boulbaba Ben Amor</u>, Mohsen Ardabilian, Liming Chen: Toward a region-based 3D face recognition approach. ICME 2008: 101-104, 2008.

[C20] <u>Boulbaba Ben Amor</u>, Mohsen Ardabilian, Liming Chen: An Improved 3D Human Face Reconstruction Approach Based on Cubic Splines Models. 3DPVT 2006: 279-286.

[C21] <u>Boulbaba Ben Amor</u>, Mohsen Ardabilian, Liming Chen: New Experiments on ICP-Based 3D Face Recognition and Authentication. ICPR (3) 2006: 1195-1199.

[C22] <u>Boulbaba Ben Amor</u>, Mohsen Ardabilian, Liming Chen: *Enhancing 3D Face Recognition By Mimics Segmentation*. ISDA (3) 2006: 150-155, 2005.

[C23] <u>Boulbaba Ben Amor</u>, Mohsen Ardabilian, Liming Chen: 3D Face Modeling Based on Structured-Light Assisted Stereo Sensor. ICIAP 2005: 842-849.

[C24] <u>Boulbaba Ben Amor</u>, Mohsen Ardabilian, Liming Chen: *Efficient and low-cost 2.5D and 3D face photography for recognition*. SITIS 2005: 36-42.

National reviewed journals and conferences (7)

[J7] Lahoucine Ballihi, <u>Boulbaba Ben Amor</u>, Mohamed Daoudi, Anuj Srivastava, Driss Aboutajdine, Sélection de caractéristiques géométriques faciales 3D par boosting pour la reconnaissance des visages, Traitement du signal (Journal), volume 29, 3-5 - 2012 - pp.383-407.

[C25] Lahoucine Ballihi, <u>Boulbaba Ben Amor</u>, Mohamed Daoudi, Anuj Srivastava, Driss Aboutajdine, *Quelles caractéristiques géométriques faciales 3D donnent votre identité ?*, 18e congrès francophone AFRIF-AFIA Reconnaissance des Formes et Intelligence Artificielle (RFIA), Lyon, 2012.

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Software (1)

[S1] Mohsen Ardabilian, Liming Chen, Karima Ouji, **Boulbaba Ben Amor**, Procédé d'acquisition et de modélisation 3D sans contact et avec ajout de texture, École Centrale de Lyon, Janvier 2010.

Ph.D. Thesis (1)

[**T1**] <u>Boulbaba Ben Amor</u>, Contributions to 3D face Modeling and Recognition, Ph.D. Dissertation, co-supervised by *Prof. Liming Chen* and *Dr. Mohsen Ardabilian*, Ecole Centrale de Lyon, N 2006-39, December 2006.

Teaching Activities -

TELECOM Lille (2007 – Present)

Télécom Lille is a French public engineering school (grande école) founded by Université de Lille1 and Institut Mines-Télécom, in 1991. Open to holders of a French Baccalaureate, two-year degree students (roughly equivalent to a Bachelor's degree) and to professionals, Télécom Lille has broadened access to engineering degrees. Since my arrival in September 2007, I have designed new classes related to my research topics that are proposed to the last year students. In particular, I have targeted two topics: *Introduction to Biometrics* and 3D Acquisition, Modeling and Analysis. Since 2011, I'm the responsible and the coordinator (with another colleague in the same department) of the Systems & Networks Security module, proposed to the last year students.

2011 - present: Coordinator of the Systems & Networks Security module at Télécom Lille,

This module is proposed to the last year students. It provides a rich set of security topics, ranging from computer system security to network security and security of emerging ICT applications, and it is composed of lectures, conferences, and hands-on experiments, given by both guest lecturers from industry and researchers from academia, offering technical and scientific perspectives on dealing with security threats and attacks. The students are expected to gain insightful understanding on those significant security issues and the latest security technologies, as well as learning to solve practical security problems in creative and efficient ways. The module contains fundamental topics (Cryptography, Risk assessment, Dependability, Network Protocols, Intrusion Detection Techniques, etc.) and a second part which changes continuously according to the hot new topics in security (Cyber-criminality, Trust and Privacy, etc.).

2011 - present: Introduction to Biometrics,

Lectures and a practical project, proposed within the Systems & Networks Security module at Télécom Lille. My research activities in the field of face recognition pushed me to introduce this class. It is designed to first highlight the need of emerging biometrics and related applications. Then, it studied more deeply some of the technologies such as Iris, Fingerprint and Face following a pattern recognition methodology (preprocessing, feature extraction, pattern matching, datasets, evaluations, etc.). Usually, a seminar from a company (Morpho¹⁰, etc.) is proposed to give the industrial point-of-view, the systems constraints and the new applications.

2008 - present: 3D Acquisition and Analysis Techniques,

Lectures, practices and demonstrations, proposed to the Multimedia module at Télécom Lille. I have

 $^{^{10}}$ www.morpho.com/?lang=en

introduce this class to allow our students discover multiple technologies of 3D imaging (stereo-vision, structured-light, laser rangefinder, time-of-flight, etc.). Furthermore, I have introduced practices on 3D mesh processing and analysis using the Visualization Toolkit (VTK) library¹¹. With these practices, the students discover tools for 3D mesh processing and scientific visualization. They work with a class library entirely designed in an Object-Oriented fashion.

2007 - present: Algorithms and C/C++ programming,

Lectures, practices and project, proposed to the 1^{st} year students at Télécom Lille. First, with the Algorithms teaching, the students learn how to design solutions for a given problem and how to write an algorithm. Then, a translation to the C/C++ language which is built and executed, allow to touch on the whole process.

2007 - present: Data Structure (E-learning),

Distant lectures, proposed within the apprenticeship curriculum at Télécom Lille. Here, the students are apprentice and spend half of their time in a company and the other half at school for practices and exams. I note that Télécom Lille has developed a strong expertise in e-learning, since 2000.

2007 - 2012: Multimedia Indexing and Retrieval,

Java development project, proposed to the last year students in the Multimedia module. With this project, the students design and implement a graphical user interface and a set of image descriptors for image retrieval. The project ends with an evaluation procedure using the appropriate criteria Recall/Precision, F1-score, etc. This project is proposed with the lectures on Multimedia Retrieval given by Prof. Mohamed Daoudi.

École Centrale de Lyon (2004 – 2007)

École centrale de Lyon, founded in 1857, is one of the oldest post-bachelor graduate schools (grande école) in France. During my Ph.D. graduation, I got the chance to work with the professors at École Centrale de Lyon and to be involved in some classes,

2004 - 2007: Algorithms and Data Structure,

Practices proposed to the 1st year students at École Centrale de Lyon (with Prof. Liming Chen).

2004 - 2007: Oriented Object Programming,

Practices proposed to the 2nd year students at École Centrale de Lyon (with Prof. Christian Vial).

2006 - 2007: Information System Architecture (Java language),

Practices proposed to the 3rd year students at École Centrale de Lyon (with Prof. Christian Vial).

EPSI Lyon (2005 – 2006)

EPSI (École Privée des Sciences Informatiques) is a French private school founded in 1961.

2005 - 2006: Software Engineering,

Lectures, practices and projects proposed to the engineer students at EPSI-Lyon. It was a nice experience at this private school. In fact, I was the responsible of the Software Engineering module to study modeling methodologies like UML (Unified Modeling Language) or MERISE. Several projects have been proposed to the students to practice and design applications.

¹¹http://www.vtk.org/

Part II

Research Activities

Notations

TABLE 1: List of symbols and their definitions used in this *habilitation*.

| Symbol | Definition /Explanation |
|---|--|
| X | $n \times 3$ matrix of landmarks coordinates in \mathbb{R}^3 . |
| $\ \cdot\ _F$ | the matrix Frobenius norm. |
| C | preshape space. |
| $\langle X, Y \rangle$ | Riemannian metric on \mathcal{C} |
| S | shape space. |
| $T_X(\mathcal{C})$ | tangent space to \mathcal{C} at $X \in \mathcal{C}$. |
| [X] | equivalence class of X (orbit of X). |
| $d_{\mathcal{C}}$ | distance on \mathcal{C} , $d_c(X, Y) = cos^{-1}(\langle X, Y \rangle)$. |
| $exp_X(V)$ | exponential map function $(exp: T_X(\mathcal{C}) \to \mathcal{C}).$ |
| $exp_X^{-1}(Y)$ | inverse exponential map function $(exp^{-1}: \mathcal{C} \to T_X(\mathcal{C})).$ |
| SO(3) | rotation group in \mathbb{R}^3 . |
| $\gamma(t)$ | a parametrized geodesic path on Kendall's shape space. |
| $L(\gamma)$ | the length of γ . |
| Ι | the unit interval [0, 1]. |
| \mathbb{L}^2 | (also $\mathbb{L}^2(I, \mathbb{R}^3)$) refer to the infinite-dimensional function space of \mathbb{R}^3 . |
| β | a parametrized continuous curve in \mathbb{R}^3 . |
| q | the SRV function, $q(t) = \dot{\beta}(t) / \sqrt{\ \dot{\beta}(t)\ }$. |
| | the standard Euclidean norm in \mathbb{R}^3 . |
| $\langle f_1, f_2 \rangle$ | the the standard \mathbb{L}^2 metric $\int_0^1 f_1(s) f_2(s) ds$ |
| . | the standard \mathbb{L}^2 norm. |
| $\psi(t)$ | a parametrized geodesic path on the shape space of continuous curves. |
| $L(\psi)$ | the length of ψ . |
| $\psi(t)$ | derivative of ψ with respect to t. |
| Γ | group of orientation-preserving re-parametrizations in $[0, 1]$. |
| [q] | equivalence class of SRVF under rotation and re-parametrization. |
| \mathcal{C}, \mathcal{S} | preshape space and shape space, respectively. |
| F | a facial surface represented as indexed collection of radial curves $\{\beta^{(\alpha)}\}_{\alpha \in [0,2\pi]}$. |
| \mathcal{M} | the manifold of facial surfaces $\mathcal{M} = \mathcal{S}^{[0,2\pi]}$. |
| $d_{\mathcal{C}}, d_{\mathcal{S}}, d_{\mathcal{M}}$ | metrics on \mathcal{C}, \mathcal{S} and \mathcal{M} , respectively. |
| Ψ | a geodesic path between elements of \mathcal{M} . |
| $\psi^{(\alpha)}$ | a geodesic path between curves of index α . |
| Ţ | a sample mean on \mathcal{M} of a set of facial shapes. |
| | the unit circle. |
| | a landmark of index l on the face. |
| $\begin{vmatrix} & n \\ & \lambda \end{vmatrix}$ | a variable for the value of the distance from the landmark r_l . |
| c_{λ} | a closed curve extracted around an arbitrary landmark r . |
| | metric on $\mathcal{S}^{[0,\lambda_0]}$ the manifold of facial patches. |
| $d_{\mathcal{S}^{[0,\lambda_0]}}$ | |

Chapter 1

Extended Summary

Over the last decade, I have directed my research towards the topic of 3D shape analysis and recognition with a particular focus on studying facial surfaces and their dynamics (deformations). I have targeted fundamental applications in pattern recognition – face recognition, facial expression classification and soft-biometrics (gender, age, etc.) estimation – based on three-dimensional data. With the emergence of modern shape theory and related approaches based on differential geometry, conducted mainly in 2D domain, I have been attracted by the elegant theory and relevant geometric and statistical tools that it offers. In particular, viewing shapes as elements of finite- or infinite-dimensional manifolds, the definition of Riemannian structures (or metrics) on these manifolds, and computing statistics on them (sample mean of shapes, sample covariance, etc.). These tools are suitable and computationally efficient to be applied to pattern recognition problems, as shown in the literature of 2D domain. Throughout this habilitation, my goal was to develop shape analysis frameworks for 3D faces and dynamic faces (4D faces), with the specific interrelated goals of (1) matching facial surfaces (i.e. dense registration of the shapes modulo rigid and non-rigid transformations); (2) comparing 3D shapes (i.e. define shape-preserving metrics); (3) measuring/quantifying the deformations between them; and (4) averaging a population of shapes to get representative shape, for instance. As I shall describe later on, the developed methodology is shown to be promising from both empirical and theoretical perspectives and illustrate how several applications can profit from the underlying mathematical framework.

Historically, I was among the first researchers focusing on 3D face modeling and recognition (Ben Amor et al., 2006a) by investigating the (rigid) registration approaches, such as the well-known *Iterative Closest Point* (ICP) algorithm and develop variants to perform region-oriented ICP to handle the facial expression variations. It is important to mention that despite the slight overlapping with my early research conducted within my Ph.D. project¹, the methodology that I adopted later presents in someway a scientific jump in several fronts. On the theoretical side, viewing the 3D facial shapes as elements of Riemannian manifolds and the use of tools from **Differential geometry** to interpolate between them and to quantify their

¹Refer to my earlier publications (Ben Amor et al., 2006a), (Ben Amor et al., 2006b), and (Ben Amor et al., 2008) for more details.

divergence, was my significant methodological evolution. Furthermore, modeling the shape variations by action of groups on shape representations, as previously formulated by D.G. KENDALL and ULF GRENANDER which leads to the **Group theory**, was my second methodological trend. This approach resulted in a registration-comparison (leaded jointly) solution of 3D facial shapes. With the use of appropriate mathematical representations and elastic shape analysis models, an efficient approach to register facial surfaces in presence of the variations cited above, has been proposed. The contributions of this *habilitation* are following:

- \hookrightarrow A mathematical representation of 3D faces through multiple curves suitable for shape analysis;
- \hookrightarrow An effective elastic model for 3D face registration and analysis leaded jointly;
- \hookrightarrow An efficient way to deform one surface into another which provides interpolation tools on the underlying manifolds;
- \hookrightarrow Robust face recognition solutions under expression, occlusion and pose variations, as shown through the extensive set of experiments conducted on publicly available Benchmarks;
- \hookrightarrow Relevant geometric tools to capture and learn deformations across 3D faces,
- \hookrightarrow Algorithms for facial expression recognition from static and dynamic 3D data;
- \hookrightarrow Morphology-inspired geometric features for soft-biometrics estimation.

In summary, this *habilitation* provides comprehensive frameworks for shape analysis of faces with applications to facial biometrics and facial expression analysis. Different pieces of the proposed computational framework, our contributions and the application perspectives are raised in the following items:

3D Faces, Elements of Infinite-dimensional Riemannian Manifolds – In *Pattern Recognition*, shapes are considered as one of the main cues for scene understanding, in addition to colors, textures and motions. Shapes are usually represented as sparse landmarks or continuous contours which delimit the external boundary of the objects. However, with the advancements of 3D scanning technologies, like laser rangefinder, structured-light and time-of-flight cameras, it is possible to capture depth-maps of the objects in the scene, which is a more complete description of the external boundary of shapes. These 3D images (depth-maps) could be often converted to 3D point clouds, 3D surfaces (meshes) or textured surfaces. Hence, there was an outstanding need for developing suitable tools and computational strategies for shape interpretation under many variablities of two kinds – (1) shape-preserving transformations such as the rigid transformations (scaling, translations and rotations), and (2) shape-changing transformations as the non-rigid deformations, which affect the shape. Because most of the geometric features (landmark configurations, curves, surfaces, deformations) do not belong to Euclidean spaces but rather to curved manifolds, a new methodology has emerged over the three last decades for studying shapes and model their variabilities. The emerging *school* of modern shape theory, promoted

by researchers as D.G. KANDELL and U. GRENANDER, consider the space of shapes representations as a geometrical object akin to a Riemannian manifold on which it is possible to resort conventional tools from Differential Geometry. Thus, shapes (or their mathematical representations) live on spaces on which one should impose Riemannian metrics required to quantify shape similarity/difference, as a first goal. There has been an increasing interest in using Riemannian frameworks for shape analysis of objects. One reason for its increasing popularity is the breadth of the tools that it offers. On one hand it allows to remove all shape-preserving transformations from the representation space, using the notion of quotient spaces and, on the other, it provides geometric tools and algorithms for computing statistics (sample means, covariances, etc.) of shapes useful in statistical modeling, for example. Our first contribution relay on this point, after a pre-processing step, trough a new mathematical representation, we map the

facial surfaces on an infinite dimensional Riemannian manifold. Then, we derive algorithms to quantify

shapes divergence and compute statistics on the underlying shape space.

According to several studies (including my earlier work (Ben Amor et al., 2006a)), the most important variability that we seek to filter out is the facial deformation. The scaling, the location and the rotations could be removed by introducing pre-processing steps and using previous solutions (Kendall, 1984). To tackle this issue, we have proposed to represent the facial surfaces as collections of radial curves emanating from the nose tip (as a reference point). This impose a first level of parameterization of the facial surfaces. The second level is to adopt an elastic model to pairwise register and compare the 3D curves through the faces. Recall that in practice the 3D faces subject of the study are presented as 3D meshes devoid of order (or parameterization) on them. Thus, representing facial surfaces as indexed collections of parametrized curves is a crucial step in our shape analysis methodology. Some previous works (including ours) have proposed similar representations through sets of curves (Samir et al., 2006, 2009) (Ben Amor et al., 2009, Drira et al., 2009a) (Berretti et al., 2011), however, the radial curves representation is more suitable to handle facial deformations (as we will discuss in Chapter 2, Section 2.4.1). The next step was to propose a mathematical representation of 3D faces which account for the stretching, shrinking and bending of the facial surfaces. We have adopted the Square Root Velocity Framework, proposed in (Joshi et al., 2007, Srivastava et al., 2011) to compare facial surfaces through their parametrized radial curves. Based on this representation, shapes (of 3D faces) are viewed as elements of an infinite-dimensional curved manifold. The shape space is a quotient space of a pre-shape space under the action of the groups of transformations. Tools from differential geometry are used to define a Riemannian metric on the shape space and compute geodesics (most efficient way to deform on shape to another) under the elastic metric.

Shape Analysis of Static Faces – Due to the increasing importance of shape analysis of objects in different applications, including 3D faces, a variety of mathematical representations and techniques have been suggested in the literature. The difficulty in analyzing shapes of objects comes from the fact that: (1) Shape representations, metrics, and models should be invariant to certain transformations. For instance, rigid motions and re-parameterization of facial surfaces do not change their shapes, and any shape analysis of faces should be invariant to these transformations. Several tools have been proposed in our framework including (1) interpolating between 3D facial shapes using geodesics on manifolds; (2) measuring distances between shapes (length of geodesics); (3) averaging a set of shapes to define sample means and statistical models on their tangent spaces. These ideas have been applied to 3D face recognition under challenging variations such as expressions, occlusions, and pose variations (Drira et al., 2010a, 2013a). Here, facial surfaces are parametrized as collections of curves are elements of an infinite-dimensional manifold as described earlier. This methodology have been also successfully applied to expression analysis from 3D static faces (Maalej et al., 2010, 2011). Here, shape analysis of local facial patches (local surfaces around pre-defined landmarks) is used to capture and learn deformation patterns for each class of expressions. Taking another direction, we have proposed in (Berretti et al., 2011) to use SIFT feature descriptors of depth images around keypoints to perform 3D facial expression recognition.

Shape Analysis of Dynamic (4D) Faces – With the advancement in 3D imaging technologies, it is possible nowadays to capture dynamic flows of objects for the purposes of merging them or making analysis of their dynamics (motions). To reach the latter goal, an accurate dense registration of meshes (frames) across time is important. One basic idea to capture facial deformations across 3D video sequences is to track mesh vertices densely along successive 3D frames. Specifically, in comparing shapes of faces, it is important that similar biological parts are registered to each other across different faces. Furthermore, it is important to use techniques that allow a joint registration and comparisons of surfaces in a comprehensive framework, rather than in two separate steps. These two issues – invariance and registration – are naturally handled using Riemannian methods where one can choose metrics that are invariant to certain transformations and form quotient spaces (termed shape spaces) by forming equivalence classes of objects that have the same shape. The elastic Riemannian metric that we used provides a nice physical interpretation of measuring deformations between facial curves using a combination of stretching and bending. We have introduced in (Drira et al., 2012, Ben Amor et al., 2014a) a novel method to capture densely and faithfully the facial deformations, grounding on Riemannian geometry, called Dense Scalar Fields (DSFs). The elastic deformations are accurately captured by the DSF features and used for expression classification. The main motivation of using a Riemannian approach is to perform registration that matches corresponding anatomical features, and obtain deformation fields that are physically interpretable.

Learning Geometric Features for Classification – In this part of our work, we utilize ideas from two growing but disparate fields in computer vision – shape analysis using tools from differential geometry and Machine Learning techniques – to learn the geometric features for classification tasks. For example, in (Ballihi et al., 2012a,b) we have used the Adaboost algorithm to select and highlight salient geometrical facial features that contribute most in 3D facial biometrics. Firstly, a large set of geometric features (curves) are extracted using level sets (circular curves) and streamlines (radial curves) of the Euclidean distance functions of the facial surface; together they approximate facial surfaces with arbitrarily high accuracy. Then, we used the shape analysis techniques in order to measure shapes difference and capture their deformations that are fed up to the Boosting step. A second idea was to derive from the geometric features Euclidean representations, then apply Machine Learning algorithms to perform face classification. For example, the Dense Scalar Fields are the magnitude of the shooting vectors (elements of different tangent spaces), which bring their initial representation to an Euclidean vector space. Thus, applying traditional classification algorithms (Random Forest, Hidden Markov Models, Support Vector Machines, etc.) for face classification become possible. These ideas have been tested in facial expression recognition (Maalej et al., 2011, Ben Amor et al., 2014a) and more recently in soft-biometrics estimation (Xia et al., 2013a, 2014a), such as gender classification and age estimation.

Manuscript Organization

After this executive summary of the *habilitation* contributions, Chapter 2 describes scientific challenges of 3D face analysis and provide a brief review of modern shape theory with an essential background of shape analysis of landmark-based representations and continuous parametrized curves. It also details our methodology for shape analysis of 3D faces and shows our practical and unified computing framework. Chapter 3 targets our first application, 3D face recognition under pose, expression and occlusion variations. In Chapter 4 we explore the role of shapes in facial expression analysis and recognition, from static or dynamic data. We present in Chapter 5 our third application related to soft-biometrics estimation using Morphology-inspired geometric descriptions. Finally Chapter 6 presents our current research and some perspectives for future directions.

Chapter 2

Shape Analysis on Riemannian Manifolds

The goal of this chapter is to provide a brief literature review and essential theoretical aspects required to introduce our contributions in 3D shape analysis. We will start by reviewing some pioneering work from the literature related to modern shape theory ranging from landmarks (a dataset of registered anchor points), in particular the Kendall's shape analysis methodology, to landmark-free geometrical representations, including 3D continuous curves. Then, we will introduce the geometrical shape analysis framework grounding on Riemannian geometry proposed in our research for 3D shape analysis. In particular, we will emphasize on two key ideas -(1) the mathematical representation of the studied shapes, and (2) the geometric tools defined on the space of these representations for the purposes to measure distances between shapes, interpolate between them, quantify their shape difference, estimate an average shape as well as estimate the shape variability within a class of shapes. One important difficulty to lead shape analysis is that the study of the representations involves non-linear spaces (i.e. not vector spaces), thus tools commonly used to process the shapes are not valid. For that reason, shape analysis often implies Differential Geometry to study curved spaces formed by shape representations and to develop appropriate tools to resolve the tasks above-cited. Another important fundamental aspect which has emerged is to consider the variabilities induced by the transformations such as rotations, translation, scaling, and deformations (diffeomorphisms) as actions of certain groups on the space of representations. Thus, the study of the groups and their actions which involves knowledge in *Group theory*, is required to conduct transformation(s)-invariant shape analysis. Later, through this *habilitation*, we will discuss the benefits of the geometric shape analysis methodology and will provide some illustrations involving 3D face analysis applications.

Recall that the aim of *shape analysis* is to develop mathematical descriptions of shapes, so that shapes of objects can also be measured and quantitatively compared. In particular, goals of shape analysis include:

- \hookrightarrow Quantifying similarity (or difference) between shapes The space of shape descriptors is equipped with a sort of distance function d. This function measures the difference between shapes, enabling us to make statements such as shape x is more similar to y than to z (formally, $d(x,y) \leq d(x,z)$).
- \hookrightarrow Finding the most efficient way to deform one shape into another By viewing shapes as elements of a given shape space, it is often possible to define paths (curves) on that shape space connecting two arbitrary shapes. Minimal curves (in term of length) provide the most efficient way to deform one shape into another and can be seen as an interpolation between these shapes. This needs first algorithms to produce dense correspondence between the shapes that seek to optimally register them.
- \hookrightarrow Defining a mean shape to represent a shape class Given a set of shapes, points of the shape space, one seek here to define a sample representative mean shape of that class. As shape spaces are curved spaces, we need to use appropriate approaches from differential geometry involving tangent spaces to design algorithms to estimate a sample mean.
- \hookrightarrow Shape classification Suppose we have a database of previously-observed shapes from each of several different classes. Given a test shape, we would like to determine which of these classes the test shape most likely belongs to. In classification tasks, it is often useful to define probability densities of shapes given a mean shape and a set of training samples.

Thanks to tools from Differential Geometry, achieving the goals above-mentioned become possible. In the following sections, I shall review essential concepts and related methods from state-of-the-art which offered elegant theories and computational algorithms for shape analysis. From this point-of-view, my research is indebted to the seminal work of D.G. KENDALL (Kendall, 1984) and his colleagues (Dryden and Mardia, 1998) on statistical shape analysis of landmark-based representations, the work of U. GRENANDER on shape theory formulation (Grenander, 1993), and the recent work of A. SRIVASTAVA and his group in elastic shape analysis of continuous curves in \mathbb{R}^n , in particular (Klassen et al., 2004), (Joshi et al., 2007), and (Srivastava et al., 2011). I should also cite the work conducted in M. DAOUDI's group in the field of 3D face recognition using iso-level curves (Samir et al., 2006, 2009), before I joined his group and get involved in the research on that topic. Next section will provide a brief literature review of 3D face analysis as a particular challenging case of 3D shape analysis.

2.1 3D Faces, Particular 3D Shapes

The exploitation of the 3D shape of the face rather than its appearance with definition of innovative algorithms for 3D face matching has been a growing field of research in recent years. In addition to face recognition, many applications have been targeted as facial expressions analysis and Action Units detection, and soft-biometrics estimation (gender, ethnicity and age). The up-to-date list of the solutions proposed can be derived from the survey of (Bowyer et al., 2006a) and the literature reviews of (Drira et al., 2013a)(Ben Amor et al., 2014a)(Xia et al., 2014b). A collection of 3D face data sets have also been made available, thus providing the opportunity to have fair comparison between different solutions. The Face Recognition Grand Challenge (FRGC) initiative, directed by NIST, provides common data sets to be used as a reference for training (FRGCv1) and evaluation (FRGCv2) ; a 3D face recognition contest was launched in 2005, with the final results published in 2006 (Phillips et al., 2005). Since then, several 3D face recognition approaches have been developed. In the same direction, some research groups are interested on performing facial expression recognition from 3D still images (Wang et al., 2006a)(Berretti et al., 2011)(Fang et al., 2011)(Gong et al., 2009a)(Le et al., 2011)(Mpiperis et al., 2008a)(Tang and Huang, 2008a) and very recently from 4D face sequences (Sun et al., 2010a) and (Sandbach et al., 2012a). Thanks to the publicly available databases such as BU-3DFE and Bosphorus for static analysis and BU-4DFE for dynamic analysis, many research groups have investigated the problem with the assumption that the 3D facial geometry could be more informative (in terms of deformations) that planar images, thus their use can achieve better performances as demonstrated in (Sandbach et al., 2012a).

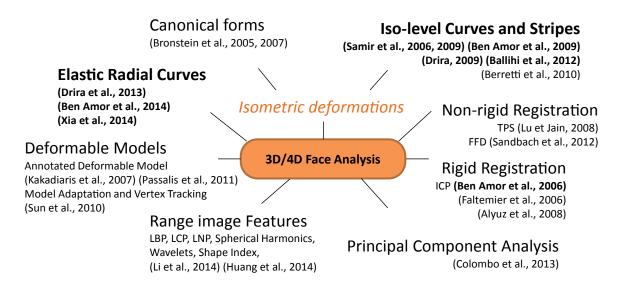


FIGURE 2.1: Literature review of 3D face analysis approaches for recognition, expression recognition and soft-biometrics estimation.

Show in figure 2.10 is an overview of related approaches used in different applications, in particular face and facial expression recognition. The fundamental ingredient of these approaches (performing on static or on dynamic 3D data) is the facial matching (or correspondence). For example in face recognition it is important to match accurately different anatomical parts of the face before using a defined metric to derive a dissimilarity measure between the face (Bronstein et al., 2005a, 2007a). This step is also very important to achieve dynamic analysis (Sun et al., 2010a) (Sandbach et al., 2012b). With the definition of an appropriate metric, this is the most important step in 3D facial shape analysis because of the multiple variabilities exhibited by the facial surface,



FIGURE 2.2: Different challenges of 3D face analysis: Pose variations, deformations caused by the expressions, occlusions, missing data, etc. (these examples are taken from the Bosphorus dataset).

- → Facial Expressions induce non-rigid (often elastic) transformations to the facial surfaces (center of Figure 2.2). One seek here to use metrics suitable to compare facial surfaces modulo such transformations. An assumption which states an approximation of the facial deformations to be isometric under the intrinsic surface metric has been first proposed in (Bronstein et al., 2005b)(Bronstein et al., 2007a) and considered by other groups (Samir et al., 2009)(Ben Amor et al., 2009) using iso-level curves and (Berretti et al., 2010a) based on iso-stripes, to handle the deformation problem. Another direction consists to use *Deformable Face Models* as illustrated in (Kakadiaris et al., 2007) (annotated deformable model) and (Sun et al., 2010a) (Model Adaptation and Vertex Tracking) to perform facial registration. The use of existing solution for non-rigid registration such as the Thin-Plate Splines (TPS) in (Lu et al., 2006a) and the Free-Form Deformation (FFD) in (Sandbach et al., 2012b) algorithms is explored to perform an accurate registration.
- ↔ External Occlusions result in external parts which will over the facial mesh (the right part of Figure 2.2). One seek here to first remove the external occlusions which results in missing data, then apply one of the following strategies, (1) tolerate the missing data using local approaches (Mian et al., 2008)(Huang et al., 2011) or region-based approaches (Faltemier et al., 2008), or (2) complete the missing data using generative statistical models (such as Gappy-PCA applied on range images, as proposed in (Colombo et al., 2009)) then perform the analysis.
- \hookrightarrow Head Pose Variations induce self-occlusions which results in missing data on the facial surface and luck of matching between the faces (left part of Figure 2.2). A rough registration step is necessary to perform face comparison (Ben Amor et al., 2006b)(Lu et al., 2006a).

Accordingly, several works have investigated the problem of face analysis using static and dynamic 3D data with fundamental problems of invariance and registration. From the description above, the proposed approaches tackle one of the challenging problems. Abundant works have been proposed for non-rigid registrations of facial surfaces, and others have been oriented to handle external occlusions or significant pose variations. In this *habilitation*, we propose a novel methodology which can handle the above-cited challenges under a unified Riemannian framework. As we will illustrate later, the – invariance and registration – problems are solved jointly (in the same step) using an elastic model suitable to handle the deformations. This framework allows also for formal statistical inferences, such as the estimation of

missing facial parts using Principal Component Analysis on tangent spaces and computing average shapes. These tools are useful in data completion and hierarchical clustering for efficient recognition. Facial deformations are captured using the shooting directions (elements of tangent spaces of the underlying manifold) computed between faces and serves to classify the facial expressions. Lastly, Morphology-inspired perspectives are extracted using the same Riemannian framework to perform soft-biometrics estimation and study the correlation between them. Although the ideas of using tools from Differential Geometry and Machine Learning are disjoint, and rarely used together, we have successfully used them to learn *geometric* features for *classification*.

2.2 Literature Review on Modern Shape Theory

Shapes of natural or man-made objects extracted from imaged scenes are important cues used in detection, recognition, retrieval, clustering and classification. It points out the external form of someone or something as produced by their outline and is usually viewed as a set of landmarks or continuous boundary. A formal and intuitive definition of shape has been introduced in (Kendall, 1984) then in (Dryden and Mardia, 1998) and considered later by many researchers in this field:

Shape is all the geometrical information that remains when location, scale and rotational effects are filtered out from an object (definition taken as is from (Dryden and Mardia, 1998)).

This topic is not new¹, that is, the biologist D'ARCY W. THOMPSON (Thompson, 1917) have proposed theories in geometric species warping, which have been presented in his book *On Growth and Form*. Thompson explored the degree to which differences in the forms of related animals could be described by means of relatively simple mathematical transformations (Thompson, 1917). Thompson essentially applied the idea of morphing to biological structures, whereby he plotted the contour landmarks of various like-species and generated deformed grids based on the results.

The seminal work of Kendall (Kendall, 1984) (and later of (Dryden and Mardia, 1998)) and Bookstein (Bookstein, 1986) resulted in elegant and comprehensive statistical shape analysis theory, that influenced the modern theory of shapes and inspired many researchers with the introduction of methods and techniques derived from differential geometry. Herein, shapes are represented by **sets of ordering land-mark points** and their statistical variability imposes to deal with a set of Euclidean shape-preserving transformations such us **scaling**, **translation**, and **rotation**. Starting with this space, Kendall methodically and rigorously proceed to remove variability due to translation, rotation, and (optionally) scaling to arrive at their space of shape representations, which is the space of orbits under the action of the rotation group. He also equipped this orbit space with a Riemannian metric, making possible to quantify

¹This review cannot claim to provide an exhaustive account of the subject. Related theory and references listed in this section mostly rely on the author's view of the field. We encourage the reader to refer to the nice and comprehensive survey written recently by L. YOUNES in (Younes, 2012) for a more complete picture.

shape divergences (geodesic distance) and to provide geodesics between shapes. The notion of *geodesic distance* is a basic tool for statistical shape analysis. Later, in (Dryden and Mardia, 1998) the authors have discussed planar Procrustes analysis to highlight the main components of shape analysis. They have defined tangent-space probability models to Kendall's shape manifolds.

From a similar point-of-view, Grenander's shape theory formulation (Grenander et al., 1991) viewed continuous shapes as points on an infinite-dimensional, differentiable manifold. The variations between shapes are modeled by actions of *Lie groups* on this manifold. Low-dimensional groups, such as rotation, translation and scaling, change the object instances keeping the shape unchanged, while high-dimensional groups (diffeomorphisms) smoothly change the object shapes (Younes, 1998). This theory proposed to view the set of shape representations (the shape space) as quotient of the pre-shape space, obtained by modding out shape-preserving transformations. The idea is to assume that there is a template object, which represents the reference shape. Then, the variability of the shape is analyzed through the deformations of this reference shape towards the actual observations: a shape difference is encoded by the transformation that deforms one to reach the other. In (Grenander et al., 1991), the authors used Markov models to represent the boundaries of non-rigid objects. They demonstrated how these models can be used to detect objects in noisy images. By using deformable templates (Grenander, 1993) with shape deformations modeled as action of diffeomorphisms, (Basri et al., 1998) described how to measure similarity between objects in terms of the amount of stretching and bending necessary to turn the shape of one object into the shape of another one. Work toward elastic shape analysis (using elastic models) has been carried out by L. YOUNES in (Younes, 1998) followed by (Michor and Mumford, 2003) and (Mio et al., 2007), where some shape descriptors and metrics were derived. The key idea in elastic analysis is that the mapping is nonlinear, i.e. points that are matched together are at unequal distances from their origins. Such a matching can be considered as an elastic matching, as one curve has to (locally) stretch, compress and bend to match the other.

Modern vision problems require a unifying framework for the statistical study of shapes and the development of computational algorithms. This demand has spawned numerous studies of shapes in recent years. For example, (Klassen et al., 2004) introduced a representation for planar curves parametrized by arc-length in which each curve is represented by its angle function $\theta(t)$, defined as the elevation angle of the tangent vector of the curve at t (values are chosen so that θ is continuous). This representation is invariant to translation and reparametrization, and can be made rotation-invariant by vertically shifting each angle function so that it has an average value of π . However, since all curves are required to be parametrized by arc-length, it is not possible to reparametrize curves to improve the registration between them. They applied this framework to statistical modeling and analysis using large collections of shapes (Srivastava et al., 2005). Other parametric shape analysis frameworks do allow the curves to be reparametrized; these are referred to elastic shape analysis frameworks, since they model deformations as combinations of bending and stretching. Mio et al. (Mio et al., 2007) used a parametric curve representation along with an **elastic metric** obtained as a weighted combination of stretching and bending energies. A general discussion of several classes of metrics on the space of smooth planar curves modulo reparametrization that can be introduced for this purpose can be found in (Michor and Mumford, 2007). More recently, (Joshi et al., 2007, Srivastava et al., 2011) presented a special representation of curves, called the Square-Root Velocity Function (SRVF), under which a specific elastic metric becomes an \mathbb{L}^2 metric and simplifies the shape analysis. The later family of approaches will be discussed in detail in Section 2.4. Before coming to them, I shall present in the Section 2.3 the Kendall shape analysis approach related to registered landmark representations.

When the state-of-the-art on shape analysis of landmarks configurations and curves (1D-functions, 2Dcurves (planar), ..) is now well established, there is nowadays a new trend to shape analysis of surfaces. The main difference with continuous curves is that when the arc-length parametrization is a natural choice to impose an "order" on curves, surfaces are completely devoid of order. So, one should first impose a parametrization then move to the shape analysis task. It is well-known that the main difficulty in 3D shape analysis is the registration of vertices across the 3D meshes before their comparisons. In addition, the analysis methods should achieve desired invariance (which is closely related to the chosen metric) to transformations such as rigid motions (rotations, translations and global scaling) and to reparameterizations (deformations). Some recent work studied shape spaces of parametrized surfaces and the invariance to rigid transformations and change of parametrization (Bauer and Michor, 2011) and (Kurtek et al., 2012).

Because of the difficulty of the over-mentioned problems, our focus was directed to facial surfaces and all the variabilities than are able to exhibit. We can cite the head pose variations which results in rigid transformations (mainly rotations) and missing data due to the self occlusions. Also, the facial expressions which non-rigidly deform the surface and some times change its topology (when the mouth is open for instance). When moving our faces in front of the 3D camera, it introduces translations, scaling and spatial resolution changes. All these changes makes the problem difficult and conventional tools are no more able to handle all the challenges in one step. For example, the well-known Iterative Closest Point algorithm (Besl and McKay, 1992) works only for rigid surfaces thus do not tolerate deformations.

Our idea is to represent the facial surfaces by collections of curves. The facial curves have a fixed ordering and only one-dimensional diffeomorphisms are needed for their registration. One can view our methodology as a natural transit from curves to 3D surfaces, with applications to 3D face analysis. In the following sections, we shall give a brief review of Kendall's approach for shape analysis, then move to continuous curves. We will close the chapter by presenting our methodology for shape analysis of 3D faces and the derived tools to register facial surfaces, compare and average them and quantify accurately their divergence. These tools will be applied in the next chapters for face recognition (Chapter 3), expression recognition (Chapter 4) and soft-biometrics estimation (Chapter 5).

2.3 Kendall's Shape Space and Procrustes Analysis

Kendall's Shape Analysis approach provides an elegant and comprehensive framework applied to discrete landmarks representation and provides tools derived from differential geometry which can be used to come to the shape analysis aims cited above. This framework is useful in many applications involving registered landmarks configurations, in medical images, animal anatomy understanding, etc. Let $X \in$ $\mathbb{R}^{n \times 3}$ represents a discrete points set or a configuration of n landmarks in \mathbb{R}^3 (here, we will restrict ideas to the landmarks in \mathbb{R}^3 , extension to \mathbb{R}^k is straightforward). Starting with this space, (Kendall, 1984) methodically and rigorously proceed to remove variability due to translation, rotation, and (optionally) scaling to arrive at their space of shape descriptors, which is the space of orbits under the action of the rotation group. They also equip this orbit space with a Riemannian metric, making it possible to compute distances and geodesics between shapes. More formally, they are interested in analyzing shapes of the set of configurations X, i.e analysis should be invariant to rotations, translations, and global scaling. The setup for this shape analysis is described next. To remove translation, a possible common way is to force X to satisfy: $\sum_{i=1}^{n} X_{i,j} = 0$, for j = 1, 2, 3, via translation. Similarly, to remove the scale we assume that $||X||_F = \sqrt{\sum_{i,j} X_{i,j}^2} = 1$. Let \mathcal{C}_0 be the set of all such centered configurations of n landmarks in \mathbb{R}^3 , i.e. $\mathcal{C}_0 = \{X \in \mathbb{R}^{n \times 3} | \sum_{i=1}^n X_{i,j} = 0 \text{ for } j = 1, 2, 3\}$. \mathcal{C}_0 is a 3(n-1) dimensional vector space and can be identified by $\mathbb{R}^{3(n-1)}$. Since in some applications it is required to filter out the scale variability, the *pre-shape* space can be defined to be:

$$\mathcal{C} = \{ X \in \mathcal{C}_0 | \| X \|_F = 1 \}$$

 \mathcal{C} is a unit sphere in $\mathbb{R}^{3(n-1)}$ and, thus, is (3n-4) dimensional. The tangent space at any pre-shape X is given by:

$$T_X(\mathcal{C}) = \{ V \in \mathcal{C}_0 | \operatorname{trace}(V^T X) = 0 \}$$
.

While the translation and scaling are removed from the representation, one still need to account for the rotation variability. For any $X \in C$, we define an equivalence class: $[X] = \{XO|O \in SO(3)\}$ that represents all rotations of a configuration X. The set of all such equivalence classes, $S = \{[X]|X \in C\} = C/SO(3)$, is called the *shape space* of configurations having n landmarks. The tangent space at any shape [X] is defined to be:

$$T_{[X]}(\mathcal{S}) = \{ V \in \mathcal{C}_0 | \operatorname{trace}(V^T X) = 0, \ \operatorname{trace}(V^T X S) = 0 \} ,$$

$$(2.1)$$

where S is any 3×3 skew-symmetric matrix. The first condition makes V tangent to C and the second makes V perpendicular to the rotation orbit and, together they force V to be tangent to the shape space S.

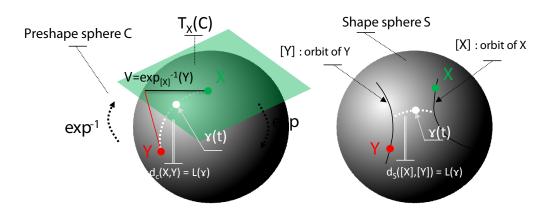


FIGURE 2.3: A pictorial of the spherical structure of the manifold \mathcal{C} , on the left panel, X (green) and Y (red) are elements of \mathcal{C} the geodesic γ connecting them (white path), $T_X(\mathcal{C})$ (green) is the velocity space of \mathcal{C} attached to X, and the shooting vector V obtained by $\exp_X^{-1}(Y)$. The right panel shows the Shape Sphere with two elements [X] and [Y] on it as well as the geodesic path γ (white path) and the distance between [X] and [Y] on \mathcal{S} defined as the length of γ , $L(\gamma)$.

In view of the spherical structure of C, the expressions for the exponential map and its inverse are well known, and can be easily adapted to S. Shown in Fig. 2.3 are the geometry of the *pre-shape* (left) and *shape* (right) spaces with notations that will be detailed by the following items:

1. Exponential Map: The exponential map is given by: for any $V \in T_{[X]}(S)$,

$$\exp_{[X]}(V) = \left[\cos(\theta)X + \frac{\sin(\theta)}{\theta}V\right],$$

$$\theta = \sqrt{\langle V, V \rangle} = \sqrt{\operatorname{trace}(VV^T)}.$$
(2.2)

2. Inverse Exponential: The inverse exponential map is given by:

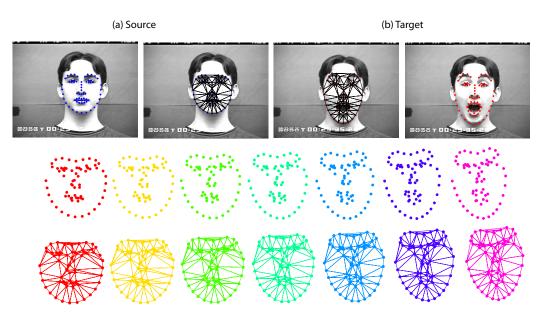
$$\exp_{[X]}^{-1}([Y]) = \frac{\theta}{\sin(\theta)}(YO^* - \cos(\theta)X), \qquad (2.3)$$
$$\theta = \cos^{-1}(\langle X, YO^* \rangle) = \cos^{-1}(\operatorname{trace}(X(YO^*)^T)) .$$

Here O^* is the optimal rotation of Y that aligns it with X: $O^* = \operatorname{argmin}_{O \in SO(3)} ||X - YO||_F^2$.

3. Geodesic Path: Also, assuming standard Riemannian metric on \mathcal{S} , the geodesic between any two configurations $[X], [Y] \in \mathcal{S}$ is given by $[\gamma(\tau)]$ where

$$\gamma(\tau) = \frac{1}{\sin(\theta)} (\sin((1-\tau)\theta)X + \sin(\tau\theta)YO^*)$$
(2.4)

$$\theta = \cos^{-1}(\langle X, YO^* \rangle) , \qquad (2.5)$$



(c) Geodesic path connecting shapes of (a) and (b)

FIGURE 2.4: An illustration of face landmarks interpolation under two different facial expressions (a) Neutral face with extracted 2D landmarks and (b) Surprised face with extracted landmarks. Part (c) gives the interpolation on the shape space between shapes from (a) and (b) called also geodesic connecting these shapes.

where O^* is the optimal rotation as stated in the previous item. To illustrate this idea, let's consider facial images given in (a) and (b) of figure 2.4 and the landmarks extracted on them. One can apply the interpolation formula given by Eq. 2.4 to these configurations and get the geodesic $\gamma(\tau)$ at discrete τ , given in panel (c).

4. **Procrustes Metric**: This θ given in Eq. 2.4 is also the geodesic distance separating [X] and [Y] (length of the shortest path connecting [X] and [Y]) in the shape space S, i.e.

$$d_s([X], [Y]) = \theta = \cos^{-1}(\langle X, YO^* \rangle) .$$

5. **Parallel Translation:** For shapes [X] and [Y], and a tangent vector $V \in T_{[X]}(S)$, the parallel transport of V to [Y], along a geodesic connecting [X] and [Y], is given by:

$$V_{[X]\to[Y]} = V - \frac{2\langle V, YO^* \rangle}{\|X + YO^*\|_F^2} (X + YO^*) .$$
(2.6)

6. Mean and Median Shape Estimation: Another important tool in shape analysis of landmarks configurations is computing their statistical summaries. Given a set of landmarks, one would like to compute their statistical mean as a template for that shape. In case of noisy observations and in the presence of outliers, one often uses a median instead of the mean to minimize the influence of outliers. Therefore, we need tools to compute mean and median of sets of shapes under the chosen

shape metric. For a set of given shapes $[X_1], \ldots, [X_k]$, the two quantities of interest are defined to be:

Mean
$$\hat{\mu}$$
 = argmin $\sum_{[X]\in\mathcal{S}}^{k} \sum_{i=1}^{k} d_s([X], [X_i])^2$,
Median \hat{m} = argmin $\sum_{[X]\in\mathcal{S}}^{k} \sum_{i=1}^{k} d_s([X], [X_i])$.

The formulas for computing the inverse exponential map (exp^{-1}) and the exponential map (exp) are given by Eqns. 2.3 and 2.2, respectively.

As stated earlier, the spherical structure of the manifold of interest keeps the methodology quite simple and computationally efficient. For example, the great circles on the *n*-sphere (unit sphere in \mathbb{R}^{n+1}) are geodesics of the *n*-sphere. A great circle is given by the intersection of the sphere with a 2-plane that pass through the origin in the Euclidean space \mathbb{R}^{n+1} and the ending points of the geodesic, which could be computed explicitly using Eq.2.4. Same comment for the remaining geometric tools as the Exponential map (exp) and Inverse Exponential map (exp^{-1}) given by Eq. 2.2 and Eq. 2.3, respectively. This elegant framework and the suite of geometric tools that it can provide can be applied in many applications where registered landmarks configurations are available.

Shape spaces of landmarks are still an active research topics and are used in large number of applications. Recently, based on Kendall's approach, we have proposed in [J1-s] (Major Revisions in PAMI) a set of geometric tools for shape analysis of skeletal data estimated from the depth information measured by depth sensors such as the Kinect. The proposed framework studies the problem of classifying actions of human subjects using depth movies generated by the Kinect or other depth sensors. Representing human body as dynamical skeletons, we study the evolution of their (skeletons') shapes as trajectories on Kendall's shape manifold. More details bout this work and some on-going research are given in the last chapter (Chapter 6) of this *habilitation* as one of our future research directions. The shape theory of Kendall and his school (Kendall, 1984)(Dryden and Mardia, 1998) meets many of the requirements of shape analysis, but the use of landmarks is a drawback. Additionally, while the simplicity of the shape representation is very attractive from a computational standpoint, it often leads to unsatisfactory interpolations. More recent shape analysis approaches have been introduced based on Kendall's achievements but oriented to continuous parametrized curves which will be the subject of the next section.

2.4 Shape Space of Parametrized Curves and Elastic Analysis

Several applications of shape analysis required modeling the objects of interest as continuous boundaries, planar curves from 2D imaging and 3D surfaces from 3D imaging, for instance, the contours extracted from imaged scenes of humans (in this case we talk about silhouettes) or animals or any other general object. In medical image analysis, boundaries of anatomical parts can be approximated by surfaces in \mathbb{R}^3 . More recently, in face analysis one can use rangefinder laser scanner to capture the external boundary of the frontal part of the human head, the face, and use it in tasks of surgery simulation, realistic face animation or recognition.

Among the last decades, there has been a considerable effort in shape analysis of continuous objects, in particular continuous curves. Consequently, an abundant literature on shape analysis of curves represented mathematically to be elements of infinite-dimensional Riemannian manifolds. (Ghorbel, 1992) proposed to use Fourier descriptors and moment features for global shape representation. This approach has been used in (Ghorbel et al., 1996, Daoudi et al., 1999) for motion analysis and in (Ghorbel, 1998) for image coding. An harmonic analysis (Fourier transform for separating the shape description and the transformations) allows them to derive the notions of shape, shape space and the invariant feature space as well as a metric to compare them. (Younes, 1999) defined shape space of planar curves and derive a Riemannian approach for interpolation and comparison. (Michor and Mumford, 2006) have studied different choices of Riemannian metrics for comparing shapes of closed planar curves. More recently, (Mio et al., 2007) have proposed a family of elastic metrics able that account for the stretching and bending to deform one shape into another. In particular the Fisher-Rao metric (Mio et al., 2007) allows to keep the distance between shapes unchanged when changing their parametrization. (Joshi et al., 2007) have introduced an interesting mathematical representation of curve shapes called SRVF (Square Root Velocity Function). Taking this representation, the elastic metric for comparing shapes of curves becomes the simple \mathbb{L}^2 -metric, as shown in (Srivastava et al., 2011). This point is very important as it simplifies the analysis of curves, under the elastic metric, to the standard functional analysis. As many contributions introduced in this *habilitation* build on the **Square Root Velocity (SRV)** framework, I shall briefly recall ideas and properties of such representation in shape analysis of curves. Then, in section 2.5, we will describe our 3D shape analysis methodology applied to facial surfaces.

2.4.1 The Square Root Velocity (SRV) Representation

Let $\beta : I \to \mathbb{R}^3$, represent a parameterized smooth curve, where I = [0, 1]. Note that the set of all such curves is the Hilbert space $\mathbb{L}^2(I, \mathbb{R}^3)$ or simply \mathbb{L}^2 . Given a function β , let $\|\beta\| = \sqrt{\int_I |\beta(t)|^2 dt}$ its \mathbb{L}^2 norm². If β_1 and β_2 are two arbitrary elements of \mathbb{L}^2 , then we can compute the distance between them given by $\|\beta_1 - \beta_2\|$. However, the distance value can vary with the parametrization function, so that $\|\beta_1 - \beta_2\| \neq \|\beta_1 \circ \gamma - \beta_2 \circ \gamma\|$ ($\gamma : I \to I$ is a re-parameterization function and let Γ be the set of all such functions), which has deep repercussions on shape analysis. To handle this issue, in stead of using β , (Joshi et al., 2007) proposed to represent it mathematically using the Square Root Velocity Function (SRVF) given by,

$$q(t) = \dot{\beta}(t) / \sqrt{|\dot{\beta}(t)|}, \qquad (2.7)$$

²From now, we will use $|\cdot|$ to denote the standard Euclidean norm in \mathbb{R}^3 and $||\cdot||$ to denote the \mathbb{L}^2 -norm.

q is a special function of β that simplifies computations under the elastic metric introduced in (Mio et al., 2007), as we will show later. More precisely, as shown in (Srivastava et al., 2011), the elastic metric for comparing shapes of curves becomes the simple \mathbb{L}^2 -metric under the SRVF representation. Furthermore, under the \mathbb{L}^2 -metric, the group of re-parametrization acts by isometries on the manifold of q functions, which is not the case for the original curve β , so that we have $||q_1 - q_2|| = ||q_1 \circ \gamma - q_2 \circ \gamma||$. Also note that if we are given $q \in \mathbb{L}^2(I, \mathbb{R}^3)$, there exists a curve β (unique up to a translation) such that the given q is the SRV function of that curve. This curve can be obtained using the equation: $\beta(t) = \int_0^t q(s)|q(s)|ds$.

2.4.2 *Pre-shape Space* of SRV Functions

Consider the space $C = \{q : I \to \mathbb{R}^3 | ||q|| = 1\} \subset \mathbb{L}^2(I, \mathbb{R}^3)$, be the pre-shape space of such representations. C is a space of shape descriptors which are invariant with respect to translations and scaling, that is, if two curves differ only by a scaling or a translation, then both of these curves will have the same representative in C. Because the q function involves the first derivative $(\dot{\beta})$, it is translation-invariant, but still varies under scaling, rotations, and reparametrizations. It is made scaling invariant by first scaling all the q functions to unit length $(||q|| = \sqrt{\int_I |q(t)|^2 dt} = \sqrt{\int_I |\dot{\beta}(t)| dt} = L(\beta) = 1)$. With the \mathbb{L}^2 metric on its tangent spaces, C becomes a Riemannian manifold. However, C is called a pre-shape space because curves that differ only by a rotation or a reparametrization will still have different representatives in C. Now, that we have identified the pre-shape space, C sub-manifold of \mathbb{L}^2 , the tangent space at a point $q \in C$ is the set of all vectors which are orthogonal to q, $T_q(C) = \{v \in \mathbb{L}^2(I, \mathbb{R}^3) | \langle q, v \rangle = 0\}$. Each tangent space is equipped with the usual \mathbb{L}^2 inner product, and the geodesics on C are the great circle paths (where a great circle path is the intersection of C with a two-dimensional subspace of \mathbb{L}^2). The geodesic path between any two points $p, q \in C$ is given analytically by, $\psi : [0, 1] \to C$, where

$$\psi(t) = \frac{1}{\sin(\theta)} \left(\sin((1-t)\theta)p + \sin(\theta t)q \right), \tag{2.8}$$

and the geodesic length (the geodesic distance) is given by,

$$d_{\mathcal{C}}(p,q) = L(\psi) = \theta = \cos^{-1}(\langle p,q \rangle).$$
(2.9)

Figure 2.5 illustrates the spherical structure of the preshape space C of the SRV functions. Given two elements q_1 and q_2 the geodesic connecting them is given explicitally by the parametrization of the minorarc of the great circle passing throw the center of the hyper-sphere, q_1 and q_2 . The shooting vector (or the initial velocity vector) v at q_1 pointing towards q_2 along the geodesic ψ connecting q_1 and q_2 is given by $\dot{\psi(t)}_{|t=0}$, the first derivative of ψ with respect to the parameter t taken at t = 0.

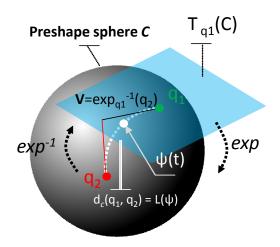


FIGURE 2.5: Geometry of the pre-shape space C, q_1 and q_2 are elements of C, $\psi(t)$ denote the geodesic connecting q_1 and q_2 and $T_{q_1}(C)$ is the tangent space to C on q_1 .

The exponential map $(exp: T_{q_1}(\mathcal{C}) \to \mathcal{C})$ and its inverse $(exp^{-1}: \mathcal{C} \to T_{q_1}(\mathcal{C}))$ are also given with explicit formulas (similarly to the Kendall's shape space of landmarks configurations, presented in Section 2.3) and could be easily extended to the shape space that will be presented in the next section.

2.4.3 Shape Space as Quotient Space and Elastic Metric

To study the *shapes* of parametrized curves in a rotation and reparametrization-invariant fashion, one should identify all rotations and re-parameterizations of a curve as an equivalence class which is,

$$[q] = \operatorname{closure}\{\sqrt{\dot{\gamma}(t)}Oq(\gamma(t))|O \in SO(3), \ \gamma \in \Gamma\}.$$
(2.10)

Here Γ denote the group of orientation-preserving diffeomorphisms of I to itself (representing reparametrizations), and SO(3) denote the group of orthogonal 3×3 real matrices with determinant +1 (representing rotations in \mathbb{R}^3). The set of such equivalence classes, denoted by $S \doteq \{[q] | q \in C\}$ is the *shape space* of SRV functions defined in \mathbb{R}^3 . S is a metric space with the metric inherited from the larger space C. To obtain geodesics and geodesic distances between elements of S, one needs to solve the optimization problem:

$$(O^*, \gamma^*) = \operatorname*{argmin}_{(O,\gamma) \in SO(3) \times \Gamma} d_{\mathcal{C}}(q_1, \sqrt{\dot{\gamma}}O(q_2 \circ \gamma)).$$
(2.11)

While for a fixed rotation $O \in SO(3)$, the optimization over Γ is done using the Dynamic Programming (DP) algorithm (Bellman, 1957), for a fixed $\gamma \in \Gamma$, the optimization over SO(3) is performed using SVD (Singular Value Decomposition). By iterating between these two steps, we can reach a solution for the

joint optimization problem. Let $q_2^*(t) = \sqrt{\dot{\gamma}^*(t)}O^*q_2(\gamma^*(t)))$ be the optimal element of $[q_2]$, associated with the optimal rotation O^* and the best re-parameterization γ^* of the second curve, then the geodesic distance between $[q_1]$ and $[q_2]$ in \mathcal{S} is given by (Eqn. 2.12):

$$d_{\mathcal{S}}([q_1], [q_2]) \doteq d_{\mathcal{C}}(q_1, q_2^*) \tag{2.12}$$

The geodesic path connecting $[q_1]$ and $[q_2]$ elements of S is given by (Eqn. 2.8), with a difference that q_2^* replace q_2 . Invariance to rotation and reparametrization is achieved by modding out the actions of SO(3)and the group Γ of orientation-preserving diffeomorphisms. Both of these group actions are isometric with respect to the \mathbb{L}^2 metric, which gives rise to a distance function on the space of orbits. Let us recall how the actions of the groups Γ and SO(3) (and $SO(3) \times \Gamma$) act on the preshape space. Details and proofs are given in (Srivastava et al., 2011) and (Robinson, 2012), we briefly recall some of them here for convenience.

• Action of SO(3) on C – the rotation group SO(3) acts from the left on C by multiplication. This action is isometric; for any $q_1, q_2 \in C$ and any $O \in SO(3)$, we have

$$\langle Oq_1, Oq_2 \rangle = \int_I \langle Oq_1(t), Oq_2(t) \rangle dt$$
 (2.13)

$$= \int_{I} \langle q_1(t), q_2(t) \rangle dt$$

$$= \langle q_1, q_2 \rangle$$
(2.14)

The second equality comes from the fact that SO(3) acts by isometry on \mathbb{R}^3 . The following equality is trivial: $||Oq_1 - Oq_2|| = ||q_1 - q_2||$.

• Action of Γ on C – The reparametrization group Γ acts on C from the right as follows: for $\gamma \in \Gamma$ and $q \in C$,

$$(q,\gamma) = \sqrt{\dot{\gamma}}(q \circ \gamma) \tag{2.15}$$

The action is defined in this way so that acting on an SRVF is equivalent to reparametrizing the corresponding curve. Now, to see that Γ acts by isometries, let $q_1, q_2 \in C$, and let $\gamma \in \Gamma$. Then

$$\langle (q_1, \gamma), (q_2, \gamma) \rangle = \int_I \left\langle \sqrt{\dot{\gamma}} q_1(\gamma(t), \sqrt{\dot{\gamma}} q_2(\gamma(t)) \right\rangle dt$$
(2.16)

$$= \int_{I} \langle q_{1}(\gamma(t), q_{2}(\gamma(t)) \rangle \sqrt{\dot{\gamma}} dt \qquad (2.17)$$
$$= \int_{I} \langle q_{1}(t), q_{2}(t) \rangle dt$$
$$= \langle q_{1}, q_{2} \rangle$$

Here also, we can derive the following equality $||(q_1, \gamma) - (q_2, \gamma)| = ||q_1 - q_2||$. Another useful fact is that these two actions commute: reparametrizing and then rotating gives the same result as rotating and then reparametrizing. Let $q \in \mathcal{C}$, $O \in SO(3)$, and $\gamma \in \Gamma$, then,

$$O(q,\gamma) = O(\sqrt{\dot{\gamma}}(q \circ \gamma)) = \sqrt{\dot{\gamma}}((Oq \circ \gamma)) = (Oq,\gamma)$$
(2.18)

If q_1 and q_2 are SRVFs of two curves β_1 and β_2 , respectively, then it is easy to show that under the \mathbb{L}^2 norm, $||q_1 - q_2|| = ||\sqrt{\dot{\gamma}}(q_1 \circ \gamma) - \sqrt{\dot{\gamma}}(q_2 \circ \gamma)||$, for all $\gamma \in \Gamma$, while $||\beta_1 - \beta_2|| \neq ||(\beta_1 \circ \gamma) - (\beta_2 \circ \gamma)||$, in general. This is one important reason why SRVF q is a suitable representation of curves than β for shape analysis.

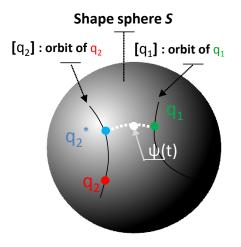


FIGURE 2.6: Shape space $S = C/SO(3) \times \Gamma$ with $[q_1]$ and $[q_2]$ elements of S (orbits of shapes on C). $q_2^* = \sqrt{\dot{\gamma^*}}O^*q_2 \circ \gamma^*$ where $O^* \in SO(3)$, $\gamma^* \in \Gamma$ are the optimal rotation and the best reparametrization, respectively. $\psi(t)$ denote a geodesic connecting $[q_1]$ and $[q_2]$.

The Shape Space S – The feature space of shape representations will be a sort of quotient of C under the actions of SO(3) and Γ. We then define the shape space as the set of all such closed-up orbits (as defined previously in Eqn. 2.10) by S = {[q]|q ∈ C} = C/SO(3) × Γ. Shown in Figure 2.6 a pictorial illustrating the space space S, two orbits [q₁] and [q₂], a geodesic connecting them ψ.

• Metric on the Shape Space S – To define a distance between two closed-up orbits $[q_1], [q_2] \in S$, one simply take the smallest distance between any pair of representatives. Formally, let $[q_1], [q_2] \in S$, the metric d_S is given by Eqn. 2.19:

$$d_{\mathcal{S}}([q_{1}], [q_{2}]) = \underset{v \in [q_{1}], w \in [q_{2}]}{\operatorname{arginf}} d_{\mathcal{C}}(v, w)$$

=
$$\underset{O_{1}, O_{2} \in SO(3), \gamma_{1}, \gamma_{2} \in \Gamma}{\operatorname{arginf}} d_{\mathcal{C}}(O_{1}(q_{1}, \gamma_{1}), O_{1}(q_{2}, \gamma_{2}))$$

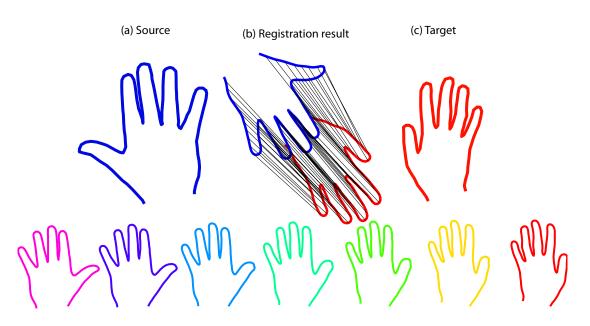
=
$$\underset{O \in SO(3), \gamma \in \Gamma}{\operatorname{arginf}} d_{\mathcal{C}}(q_{1}, O(q_{2}, \gamma))$$
(2.19)

The last equality follows from the fact that both group actions are isometric. Recall that our elastic matching problem is that of finding a pair $(\hat{\gamma}, \hat{O})$ subject to,

$$(\hat{\gamma}, \hat{O}) = \operatorname*{arginf}_{\gamma \in \Gamma, O \in SO(3)} \int_{I} ||q_1(t) - O\sqrt{\dot{\gamma}(t)}q_2(\gamma(t))||^2 dt$$

$$(2.20)$$

• Optimal Matching – Find an optimal re-parametrization between q functions, when scaling, translation and rotations are filtered out, can be viewed as an optimal matching between the corresponding parametrized curves β throw their SRV functions. In other worlds, the problem of matching β_1 and β_2 is turned out to find an optimal re-parametrization between $[q_1]$ and $[q_2]$, respectively their SRVF which will realize the minimum distance between the orbits.



(d) Geodesic path connecting shapes of (a) and (b)

FIGURE 2.7: An example of optimal matching of two parametrized curves of hands under deformations. One needs a combination of bending and stretching to match anatomical parts as the tips of the fingers and the valleys between them. To illustrate the key idea behind the theoretical framework, presented above, for shape analysis of parametrized curves (in \mathbb{R}^2), we consider in figure 2.7, two hands boundaries ((a) and (c)) extracted from images. Panel (b) illustrates a dense registration of their shapes, and panel (d) draws a geodesic path connecting them. One should note that this result is important as it allows to (jointly) compute the optimal registration and the distance between shapes.

As stated previously, shape analysis of continuous curves is now rich and one can develop techniques which achieve invariance to the standard transformations (rigid and re-parametrization). In many other applications involving 3D imaging technologies, an outstanding need is observable for developing suitable tools and computational strategies for 3D shape interpretation. Nowadays, this need is growing in computer vision due to the huge advancements in cost-effective 3D sensors. In stead of curves, the output data is three-dimensional and are represented as depth-maps, point clouds or 3D meshes. In the following section, I shall describe our contributions to 3D face shape analysis through a multiple curves approximation. Thus our contributions could be viewed as a transit step to 3D shape analysis which provide a comprehensive framework to compute geodesics and distances, achieve accurate registration between facial surfaces, develop statistical models for 3D face shape completion, etc.

2.5 Shape Analysis of Facial Surfaces

Understanding human faces by computers is still an active research area and find its application in many applications ranging from face detection to emotion interpretation. Classical approaches are based on the face appearance extracted from 2D still images (and videos). As 2D images are the result of the camera projection of the scene, the 3D geometry of the face is lost. Few works emphasize on the role of 2D face geometry based on the Active Appearance Model or the Active Shape Models. With the advancement in 3D imaging systems (mainly optical), there has been an increasing effort (since 2005-2006) to 3D faces. This has been marked by the release of the Face Recognition Grand Challenge dataset (phi) accompanied with a well-defined evaluation protocol, and the publication of first results using this dataset and other in-house datasets (Heseltine et al., 2004)(Lu et al., 2004)(Bronstein et al., 2005c)(Ben Amor et al., 2006a) (Samir et al., 2006) (Berretti et al., 2006) (Bowyer et al., 2006a)³. The aim of the research that we present here is to introduce relevant tools and computational algorithms for the purpose of shape analysis of facial surfaces (both static, 3D, and dynamic, 4D) with applications to face recognition, facial expression recognition and soft-biometrics estimation. In this section, I shall discuss the main challenges of facial shape analysis and introduce many facets of our contributions to handle these challenges. The details related to each of the above mentioned applications will be discussed in the next chapters. To do so, I shall refer to the mathematical background presented in the previous sections to describe the proposed Riemannian framework for 3D face analysis and its relevant geometric tools used in our target applications.

³We refer the reader to the next three chapters for a more complete state-of-the-art in each application

2.5.1 Motivation for Elastic Radial Curves

The changes in facial expressions affect different regions of a facial surface differently. For example, during a smile, the top half of the face is relatively unchanged while the lip area changes a lot, and when a person is surprised the effect is often the opposite. If chosen appropriately, curves have the potential to capture regional shapes and that is why their role becomes important. The locality of shapes represented by facial curves is an important reason for their selection. The next question is: Which facial curves are suitable for recognizing people? Curves on a surface can, in general, be defined either as the level curves of a function or as the streamlines of a gradient field. Ideally, one would like curves that maximally separate inter-class variability from the intra-class variability (typically due to expression changes). The past usage of the level curves (Samir et al., 2006, 2009) (of the surface distance function) has the limitation that each curve goes through different facial regions and that makes it difficult to isolate local variability.



FIGURE 2.8: A smile (see middle) changes the shapes of the curves in the lower part of a the face while the act of surprise changes shapes of curves in the upper part of the face.

In contrast, the radial curves with the nose tip as origin, that we propose here, have a tremendous potential. This is because: (i) the nose is in many ways the focal point of a face. It is relatively easy and efficient to detect the nose tip (compared to other facial parts) and to extract radial curves, with nose tip as the center, in a completely automated fashion. It is much more difficult to automatically extract other types of curves, e.g. those used by sketch artists (cheek contours, forehead profiles, eye boundaries, etc); (ii) Different radial curves pass through different regions and, hence, can be associated with different facial expressions. For instance, differences in the shapes of radial curves in the upper-half of the face can be loosely attributed to the inter-class variability while those for curves passing through the lips and cheeks can largely be due to changes in expressions. This is illustrated in Fig. 2.8 which shows a neutral face (left), a smiling face (middle), and a surprised face (right). The main difference in the middle face, relative to the left face, lies in the lower part of the face, while for the right face the main differences lie in the top half; (iii) Radial curves have a more universal applicability. The curves used in the past have worked well for some specific tasks, e.g., lip contours in detecting certain expressions, but they have not been as efficient for some other tasks, such as face recognition. In contrast, radial curves capture the full geometry and are applicable to a variety of applications, including facial expression recognition; (iv) In the case of the missing parts and partial occlusion, at least some part of every radial curve is usually

available. It is rare to miss a full radial curve. In contrast, it is more common to miss an eye due to occlusion by glasses, the forehead due to hair, or parts of cheeks due to a bad angle for laser reflection. This issue is important in handling the missing data via reconstruction, as shall be described in chapter 3; (v) Natural face deformations are largely (although not exactly) symmetric and, to a limited extent, are radial around the nose. Based on these arguments, we present here a novel geometrical representation of facial surfaces using radial curves that start from the nose tip.

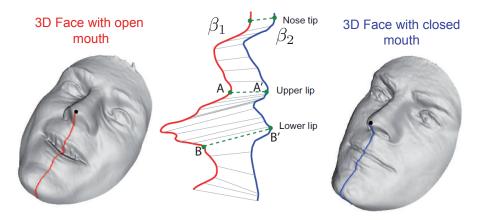


FIGURE 2.9: An example of matching radial curves extracted from two 3D faces of the same person: a curve with an open mouth (on the left) and a curve with a closed mouth (on the right). One needs a combination of stretching and shrinking to match similar points (upper lips, lower lips, etc)

Consider the two parameterized curves shown in Fig. 2.9; call them β_1 and β_2 . Our task is to automatically match points on these radial curves associated with two different facial expressions. The expression on the left has the mouth open whereas the expression on the right has the mouth closed. In order to compare their shapes, we need to register points across those curves. One would like the correspondence to be such that geometric features match across the curves as well as possible. In other words, the lips should match the lips and the chin should match the chin. Clearly, if we force an arc-length parameterization and match points that are at the same distance from the starting point, then the resulting matching will not be optimal. The points A and B on β_1 will not match the points A' and B' on β_2 as they are not placed at the same distances along the curves. For curves, the problem of optimal registration is actually the same as that of optimal re-parameterization. This means that we need to find a re-parameterization function $\gamma(t)$ such that the point $\beta_1(t)$ is registered with the point $\beta_2(\gamma(t))$, for all t. The question is how to find an optimal γ for an arbitrary β_1 and β_2 ? Keep in mind that the space of all such γ is infinite dimensional because it is a space of functions. As described in section 2.4, this registration is accomplished by solving an optimizing problem using the dynamic programming algorithm, but with an objective function that is developed from a Riemannian metric. The chosen metric, termed an **elastic** metric, has a special property that the same re-parameterization of two curves does not change the distance between them. This, in turn, enables us to fix the parameterization of one curve arbitrarily and to optimize over the parameterization of the other. This optimization leads to a proper distance

(geodesic distance) and an optimal deformation (geodesic) between the shapes of curves. In other words, it results in their elastic comparisons (refer to section 2.4 for details).

2.5.2 Mathematical Representation of Facial Shape

A facial surface S will be represented by a collection of radial curves that are defined as follows. Although S is a triangulated mesh, we start the discussion by assuming that it is a continuous surface. Let $\{\beta^{(\alpha)}\}^{\alpha \in [0,2\pi]}$ denote the collection of radial curves on S which makes angles α with a reference radial curve. The reference curve on S is chosen to be the vertical curve after the face has been rotated to the upright position ($\alpha = 0$). Figure 2.10 illustrates the 3D facial surface approximation by collections of radial curves and their pairwise correspondence.

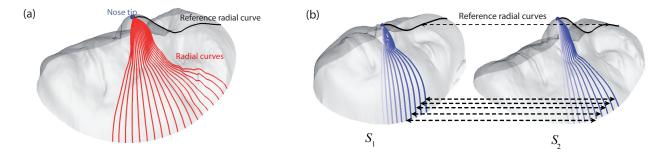


FIGURE 2.10: (a) 3D face approximation by a collection of radial curves; (b) pairwise correspondence of the facial curves.

We will use the elastic shape analysis of parametrized curves described in section 2.4 because it is particularly appropriate in our shape analysis of facial surfaces. This is because (1) such analysis uses the Square-Root Velocity Function (Joshi et al., 2007) representation which allows us to compare local facial shapes in presence of elastic deformations, (2) this method uses a representation under which the elastic metric (Mio et al., 2007) reduces to the standard \mathbb{L}^2 metric and thus simplifies the analysis, (3) under this metric the Riemannian distance between curves is invariant to the re-parametrization. To analyze the shape of $S = \{\beta^{(\alpha)}\}^{[0,2\pi]}$, we shall represent each curves $\beta^{(\alpha)}$ mathematically using the square-root representation (presented in section 2.4) such as $q^{(\alpha)}(t) \doteq \beta^{(\alpha)}(t)/\sqrt{|\beta^{(\alpha)}(t)|}$). Here t is a parameter $\in I$ and $|\cdot|$ is the standard Euclidean norm in \mathbb{R}^3 . Following the over-mentioned shape representation $\mathcal{F} = \{q^{(\alpha)}\}^{[0,2\pi]}$, facial shapes could be viewed as elements of the Riemannian manifold $\mathcal{M} \doteq \mathcal{S}^{[0,2\pi]}$. Hence, all the geometric tools defined on \mathcal{S} are straightforward in \mathcal{M} , as we will describe later.

2.5.3 Joint Shape Registration and Comparison

• **Dense Shape Registration** – The difficulty in analyzing shapes of objects comes from the fact that: (1) Shape representations, metrics, and models should be invariant to certain transformations

that are termed *shape preserving*. For instance, rigid motions and re-parameterizations of facial surfaces do not change their shapes, and any shape analysis of faces should be invariant to these transformations. (2) Registration of points across objects is an important ingredient in shape analysis. Specifically, in comparing shapes of faces, it makes sense that similar biological parts are registered to each other across different faces. Furthermore, it is important to use techniques that allow a joint registration and comparisons of surfaces in a comprehensive framework, rather than in two separate steps. These two issues— invariance and registration—are naturally handled using Riemannian methods where one can choose metrics that are invariant to certain transformations and form quotient spaces (termed shape spaces) by forming equivalence classes of objects that have the same shape. The elastic Riemannian metric used in this work provides a nice physical interpretation of measuring deformations between facial surfaces, through the radial curves representation, using a combination of stretching and bending. Figure 2.11 gives four examples of facial curves matching under facial expression variations using the elastic model.

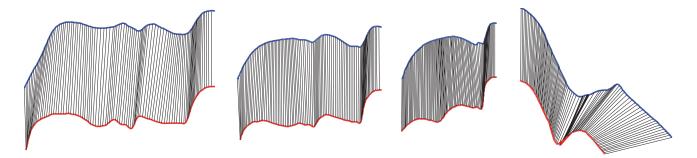


FIGURE 2.11: Four examples of facial curves matching results using the elastic Riemannian method.

Figure 2.12 provides an example of facial shapes registration through the radial curves representation. For better visibility, four different resolutions of the registration result are shown.

• Metric on the Manifold \mathcal{M} – To define a distance between two facial shapes $\mathcal{F}_1, \mathcal{F}_2 \in \mathcal{M}$, one simply integrate over all α the distance between pairwise-corresponded SRVFs of the curves on the faces \mathcal{F}_1 and \mathcal{F}_2 , given by :

$$d_{\mathcal{M}}(\mathcal{F}_1, \mathcal{F}_2) = \int_0^{2\pi} d_{\mathcal{S}}([q_1^{(\alpha)}], [q_2^{(\alpha)}]) \ d\alpha \tag{2.21}$$

where $\mathcal{F}_i = \{[q_i^{(\alpha)}]^{\alpha \in [0,2\pi]}\}$, the set of SRV functions on the face when varying the parameter α .

2.5.4 Geodesics and Shapes Interpolation

Since we have deformations (geodesic paths) between corresponding curves, we can combine these deformations to obtain deformations between full facial surfaces. In fact, these full deformations can be shown to be formal geodesic paths between faces, when represented as elements of $\mathcal{M} \doteq \mathcal{S}^{[0,2\pi]}$. According to the *Theorem* provided in (Samir et al., 2009) (page 94) adapted to our case, if we are given a path in \mathcal{M}

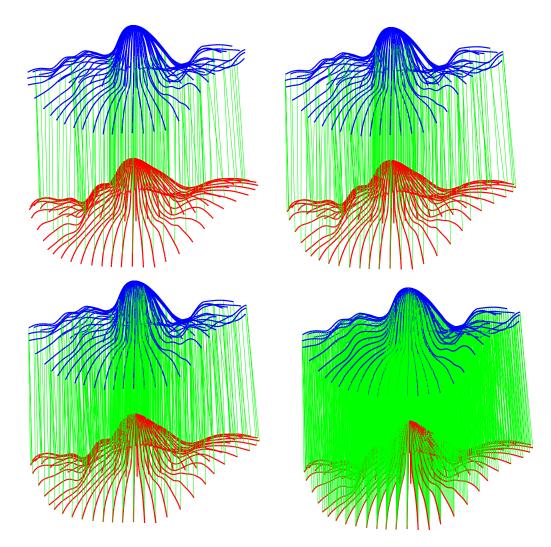


FIGURE 2.12: Results of the optimal matching (dense registrations) of two facial surfaces of same subject with different expressions viewed at different resolutions for better visibility.

represented as $\Psi : [0, 2\pi] \times I \to \mathcal{M}$. For each $\alpha \in [0, 2\pi]$, define $\psi^{(\alpha)} : I \to \mathcal{S}$ by $\psi^{(\alpha)} = \Psi(\alpha, t)$. Then Ψ is a geodesic in \mathcal{M} if $\forall \alpha \in [0, 2\pi]$, $\psi^{(\alpha)}$ is a geodesic in \mathcal{S} . Thus, the geodesic path between any two points $\mathcal{F}_1, \mathcal{F}_2 \in \mathcal{M}$ is given by, $\Psi : [0, 1] \to \mathcal{M}$, where

$$\psi^{(\alpha)}(\tau) = \frac{1}{\sin(\theta^{(\alpha)})} \left(\sin((1-\tau)\theta^{(\alpha)})q_1^{(\alpha)} + \sin(\theta\tau)q_2^{(\alpha)*} \right)$$
(2.22)

and the length of the geodesic is $\theta^{(\alpha)} = d_{\mathcal{C}}(q_1^{(\alpha)}, q_2^{(\alpha)*}) = \cos^{-1}(\langle q_1^{(\alpha)}, q_2^{(\alpha)*} \rangle)$. These geodesics provide a tangible benefit, beyond the current algorithms that provide some kind of a similarity score for analyzing faces. In addition to their interpretation as optimal deformations under the chosen metric, the geodesics can also be used for computing the mean shape and measuring the shape covariance of a set of faces, as illustrated later. Figure 2.13 illustrates an example of geodesic path between faces through their radial curves representations viewed under different view angles for better visibility.

The figure 2.14 illustrates the benefit of use of the elastic model (in the *shape space*) over the non-elastic

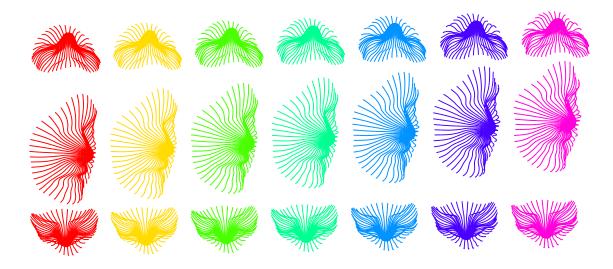


FIGURE 2.13: An example of geodesic path connecting shapes of 3D faces through the radial curves representation. The figure shows three different views of the same geodesic.

model (in the *pre-shape space*) and an Euclidean model (using the ICP algorithm). While, the top panel (a) shows the shape interpolation for an intra-class example (expressive and neutral faces of the same person), the second panel shows an inter-class example (faces of different persons). In both examples, it is clear to note the most natural deformations are exhibited by the intermediate faces (equally spaces points from the geodesic) of the first path performed in the shape space, using the elastic model. The remaining paths in the pre-shape space and in the Euclidean space presents less-natural deformations. Due to the accurate dense correspondence achieved by the elastic model, the first path showed in the panel (b) of this figure represents the most efficient way to deform the source face to the target face when keeping the anatomical parts of the faces in the intermediate faces. The application of these ideas will be shown in Chapter 3 dedicated to 3D face recognition, in which a definition of a metric to compare faces, is a crucial step in designing face recognition algorithms.

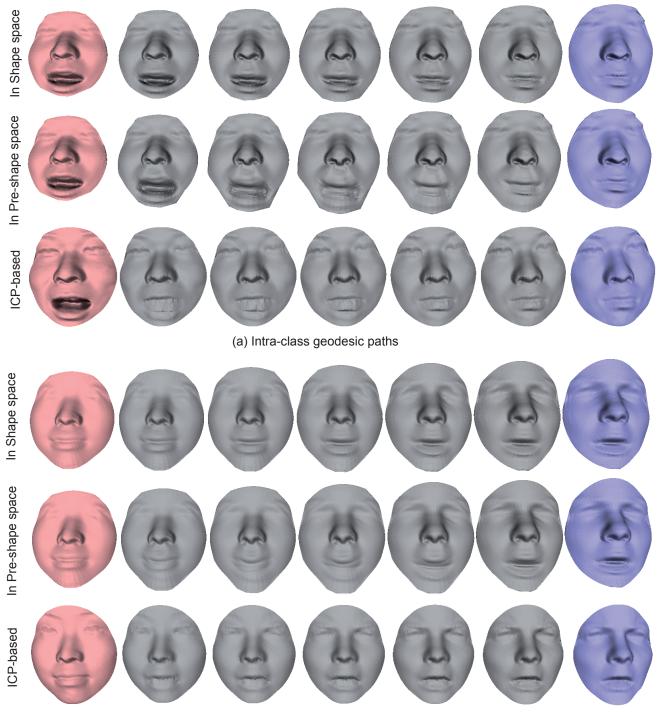
2.5.5 Sample Mean of 3D Faces

As mentioned above, an important advantage of our Riemannian approach over many past work on 3D face analysis is its ability to compute summary statistics of a set of faces. For example, one can use the notion of Karcher mean (Karcher, 1977) to define an average face that can serve as a representative face of a group of faces. To calculate a Karcher mean of facial surfaces $\{\mathcal{F}^1, ..., \mathcal{F}^k\}$ in \mathcal{M} , we define an objective function:

$$\mathcal{V}: \mathcal{M} \to \mathbb{R}, \mathcal{V}(\mathcal{F}) = \sum_{i=1}^{k} d_{\mathcal{M}}(\mathcal{F}^{i}, \mathcal{F})^{2}$$

The Karcher mean is then defined by:

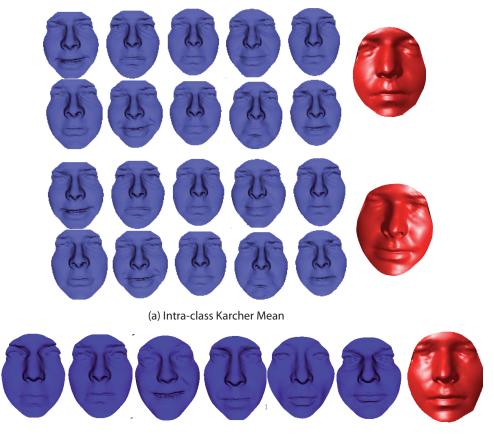
$$\overline{\mathcal{F}} = \arg\min_{\mathcal{F}\in\mathcal{M}}\mathcal{V}(\mathcal{F}).$$



(b) Inter-class geodesic paths

FIGURE 2.14: (a) Intra-class deformations achieved from top-to-bottom in the shape space (using the elastic model); in the preshape space (using an non-elastic model); and in \mathbb{R}^3 using the iterative closest point algorithm (Besl and McKay, 1992) to align the faces and to establish a dense correspondence using the closest-point criteria. (b) Inter-class deformations using the three over-mentioned methods.

The algorithm for computing Karcher mean is a standard one, see e.g. (Dryden and Mardia, 1998) and successfully used in (Drira et al., 2009b) to compute the mean of 3D nasal shapes.



(b) Inter-class Karcher Mean

FIGURE 2.15: Three examples of Karcher means (in red), the first two computes the mean shape of faces within the same class, the third example shows the result for a set shapes comping from different classes.

This minimizer may not be unique and, in practice, one can pick any one of those solutions as the mean face. This mean has a nice geometrical interpretation: $\overline{\mathcal{F}}$ is an element of \mathcal{M} that has the smallest total (squared) deformation from all given facial surfaces $\{\mathcal{F}^1, ..., \mathcal{F}^k\}$. Three examples of Karcher sample means for sets faces are given in figure 2.15. On the left the set of faces to be averaged and on the right (in red) the mean sample shape. When the two first examples illustrate the means of faces taken from a single class of person but with expression variations, the third example average a set of shapes from different classes of different age, different gender and different ethnic group.

We shall use this tool in Chapter 3 in 3D face recognition in two tasks (1) Hierarchical clustering of the gallery for efficient face recognition and (2) design a statistical model for partially-obscured face completion.

2.5.6 Optimal Deformations (Dense Scalar Fields)

In some applications, it is also interesting to capture accurately the deformations exhibited by the 3D faces in order to analyze locally the deformations or to track the facial motions. In order to capture and model the deformations of the face induced by facial movements, we propose to use the same facial

representation by radial curves and to use tools from differential geometry to effectively capture the deformations between two arbitrary faces or along a video of dynamic faces. To this end, we propose to exploit the notion of **shooting vector** along a geodesic to capture the facial deformations between facial shapes, end points of a geodesic on \mathcal{M} , and derive our **Dense Scalar Fields** (Drira et al., 2012, Ben Amor et al., 2014a).

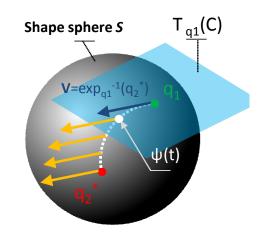


FIGURE 2.16: The tangent vector field (in yellow) along a geodesic ψ and the shooting vector V (arrow in black) element of $T_{q_1}(\mathcal{C})$ at the source point of the same geodesic ψ one $[q_1]$ pointing towards $[q_2]$ (or q_1 pointing towards q_2^*).

More formally, for each SRV representation $q^{(\alpha)}$ of a given original curve $\beta^{(\alpha)}$, the tangent vector field on this geodesic is then written as $\frac{d\psi^{(\alpha)}}{d\tau}: [0,1] \to T_{\psi^{(\alpha)}}(\mathcal{S})$, and is obtained by the Eqn. 2.23:

$$\frac{d\psi^{(\alpha)}}{d\tau} = \frac{-\theta}{\sin(\theta)} \left(\cos((1-\tau)\theta)q_1^{(\alpha)} - \cos(\theta\tau)q_2^{(\alpha)*} \right).$$
(2.23)

The tangent vector field along a geodesic path ψ connecting q_1 to q_2 is illustrated in Figure 2.16 by yellow arrows. Knowing that on geodesics, the covariant derivative of its tangent vector field is equal to $0, \frac{d\psi^{(\alpha)}}{d\tau}$ is parallel along the geodesic $\psi^{(\alpha)}$ and one can represent it with $\frac{d\psi^{(\alpha)}}{d\tau}|_{\tau=0}$ without any loss of information. Accordingly, Eqn. (2.23) becomes at the source point q_1 ($\tau = 0$), Eqn. (2.24):

$$\frac{d\psi^{(\alpha)}}{d\tau}|_{\tau=0} = \frac{\theta^{(\alpha)}}{\sin(\theta^{(\alpha)})} \left(q_2^{(\alpha)*} - \cos(\theta^{(\alpha)})q_1^{(\alpha)}\right) \ (\theta^{(\alpha)} \neq 0).$$
(2.24)

Figure 2.16 illustrates the idea to map the two radial curves on the Hyper-sphere C in the Hilbert space through their SRVFs q_1 and q_2 , and shows the geodesic path connecting these two points ψ . The tangent vectors of this geodesic path represent a vector field whose covariant derivative is zero. According to this, $\frac{d\psi^*}{d\tau}|_{\tau=0}$ becomes sufficient to represent this vector field, with the remaining vectors obtained by parallel transport of $\frac{d\psi^*}{d\tau}|_{\tau=0}$ along the geodesic ψ^* . In this way, the vector $\frac{d\psi^*}{d\tau}|_{\tau=0}$ represents the dense deformation field between two given SRVF q^1_{α} and q^2_{α} . Based on the above representation, we define the **Dense Scalar Fields** capable to capture deformations between two 3D faces through their radial multiple radial curves representation and using the elastic model for shape analysis.

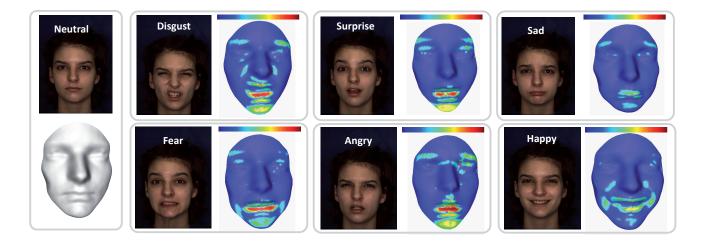


FIGURE 2.17: Deformation Scalar Fields computed between a neutral face of a given subject and the apex frames of the sequences of the six prototypical expressions of the same subject. The neutral scan is shown on the left. Corresponding texture images are also illustrated with each DSFs colormap.

A graphical interpretation of this mathematical representation is given in Figure 2.17. This figure provides the Dense Scalar Fields computed between a neutral face and expressive faces of the same person exhibiting the six universal facial expressions. The amount of deformation between them can be appreciated in this figure, as each facial expression shows different pattern of deformations. This representation will be used in Chapter 4 for facial expression classification from dynamic flows of 3D faces.

2.6 Conclusion

In this chapter, we have provided essential theoretical aspects and related literature to our research. We have started by the Kandall's shape analysis framework and we have presented Differential geometry and Group theory tools to remove shape-preserving transformations (scaling, location, rotation and re-parameterization). Although, the Kendall's approach is applicable only on shapes with registered landmarks representation, it provides a comprehensive framework. When moving to continuous (non-registered) shapes, an additional challenge appears, which is the re-parametrisation. Recent methods, inspired from the seminal Granender's shape theory, view the set of shape descriptors (the shape space) as quotient of the pre-shape space, obtained by modding out shape-preserving transformations. Thus, viewing smooth changes in shapes as action of diffeomorphisms (or the group of) is the key idea to to measure similarity between shapes in terms of the amount of stretching and bending necessary to turn one shape into another. This latter idea presents the foundations of our research on shape analysis and comparison of 3D facial shapes. Find jointly an accurate facial surfaces registration trough representation

by collections of elastic radial curves and return a distance between shapes in terms of the amount of stretching and bending is one of main contributions of our research.

Chapter 3

3D Face Recognition

In this chapter¹ I shall describe our contributions to 3D shape analysis with application to a fundamental problem in computer vision, **Face Recognition**. In fact, the head pose variations and the presence of external occlusions which lead to unregistered and obscured data, as well as the intra-class variations due to facial expressions, cause enormous variability, making the problem highly challenging. Throughout this part of the *habilitation*, I shall describe the application of our comprehensive and unified computational Riemannian framework (presented in Chapter 2) and its ability to cover many facets of 3D shape analysis where the robustness to the aforementioned variations is our central goal. We propose a mathematical representation of 3D facial shapes through collections of curves and use elastic shape analysis to develop a Riemannian framework for analyzing their full shapes. Thus, shapes of 3D faces are viewed as points on some Riemannian manifolds, and one should define appropriate metrics for shape interpolation, distance measurement, and so on. I have benefited to conduct this research from many exemplary efforts and development of elegant and mature methodologies of shape analysis of parametrized curves developed so far². From this point of view, my research is indebted to some of these seminal previous works (cf. (Dryden and Mardia, 1998) or the Kendall's school, (Klassen et al., 2004), (Srivastava et al., 2011), and (Samir et al., 2006, 2009)).

I shall emphasize, in particular, on how our facial surfaces representation, along with the defined elastic Riemannian metric, seems natural for performing, jointly, accurate dense registration (or matching) and comparison of 3D facial surfaces. Both the robustness (invariance) to variations in shape comparison and registration are naturally handled using Riemannian methods where the proposed metric is invariant to certain transformations and form quotient spaces (termed shape spaces) by forming equivalence classes of faces that share the same shape under shape-preserving transformations. We have adopted an elastic Riemannian metric which provides a nice physical interpretation of measuring deformations between facial curves using a combination of **stretching and bending** (Drira et al., 2013a, 2010b). This latter property

¹The content of this chapter is based on our published papers (Ballihi et al., 2012b), (Drira et al., 2013a) and (Drira et al., 2009b).

 $^{^{2}}$ Refer to the previous chapter for an historical review of this school of shape analysis.

makes the registration of facial surfaces accurate by matching corresponding anatomical features on the facial surfaces. We have targeted the 3D face recognition problem as first application of the theoretical and computational framework (Drira et al., 2013a, 2010b), for which interpolation between 3D shapes through accurate registration, averaging a set of 3D shapes and completion of partially obscured shape are possible. It is shown to be promising from both – empirical and theoretical – perspectives. In terms of the empirical evaluation, our results match or improve the state-of-the-art methods on several prominent databases, each posing a different type of challenge. From a theoretical perspective, this framework allows for formal statistical inferences, such as the estimation of missing facial parts using PCA on tangent spaces and average shapes computation. Because of the importance of efficiency when designing face recognition solutions, we have also introduced two solutions, (1) a feature selection step using Adaboost algorithm, to select and highlight salient geometrical facial features that contribute most in 3D face recognition (Ballihi et al., 2012a,b)and (2) an hierarchical organization, a tree-like Gallery organization of 3D faces. This latter imply comparisons performed only at the nodes of the tree. It has been explored on 3D facial shapes (Drira et al., 2010c) and 3D nasal shapes (Drira et al., 2009b) for partial biometrics. To construct such a shape tree one need to be able to cluster similar shapes.

3.1 Motivation and Related Work

Due to the natural, non-intrusive, and high throughput nature of face data acquisition, automatic face recognition has many benefits when compared to other biometrics. Accordingly, automated face recognition has received a growing attention within the computer vision community over the past three decades. Among different modalities available for face imaging, 3D scanning has a major advantage over 2D color imaging in that nuisance variables, such as illumination and small pose changes, have a relatively smaller influence on the observations. However, 3D scans often suffer from the problem of missing parts due to self occlusions or external occlusions, or some imperfections in the scanning technology. Additionally, variations in face scans due to changes in facial expressions can also degrade face recognition performance. In order to be useful in real-world applications, a 3D face recognition approach should be able to handle these challenges, i.e., it should recognize people despite large facial expressions, occlusions and large pose variations.

Some examples of face scans highlighting these issues are illustrated in Fig. 3.1. We note that most recent research on 3D face analysis has been directed towards tackling changes in facial expressions while only a relatively modest effort has been spent on handling occlusions and missing parts. Although a few approaches and corresponding results dealing with missing parts have been presented, none, to our knowledge, has been applied systematically to a full real database containing scans with missing parts. In this chapter, we adopt the Riemannian framework introduced in Chapter 2, in the process dealing with large expressions, occlusions and missing parts. Additionally, we provide some basic tools for statistical



FIGURE 3.1: Challenges of 3D face recognition: expressions, obscured data, pose variations (self-occlusion) and external occlusions.

shape analysis of facial surfaces. These tools help us to compute a typical or average shape and measure the intra-class variability of shapes, and will even lead to face atlases in the future.

The task of recognizing 3D face scans has been approached in many ways, leading to varying levels of successes. We refer the reader to one of many extensive surveys on the topic, e.g. see (Bowyer et al., 2006b). Below we summarize a smaller subset that is more relevant to our work. Deformable template**based approaches** – There have been several approaches in recent years that rely on deforming facial surfaces from one into another, under some chosen criteria, and use quantifications of these deformations as metrics for face recognition. Among these, the ones using non-linear deformations facilitate the local stretching, compression, and bending of surfaces to match each other and are referred to as elastic methods. For instance, Kakadiaris et al. (Kakadiaris et al., 2007) utilize an annotated face model to study geometrical variability across faces. The annotated face model is deformed elastically to fit each face, thus matching different anatomical areas such as the nose, eyes and mouth. In (Passalis et al., 2011), Passalis et al. use automatic landmarking to estimate the pose and to detect occluded areas. The facial symmetry is used to overcome the challenges of missing data here. Similar approaches, but using manually annotated models, are presented in (ter Haar and Velkamp, 2010, Lu and Jain, 2008). For example, (Lu and Jain, 2008) uses manual landmarks to develop a thin-plate-spline based matching of facial surfaces. A strong limitation of these approaches is that the extraction of fiducial landmarks needed during learning is either manual or semi-automated, except in (Kakadiaris et al., 2007) where it is fully automated. Local regions and features approaches – Another common framework, especially for handling expression variability, is based on matching only parts or regions rather than matching full faces. Lee et al. (Lee et al., 2005) use ratios of distances and angles between eight fiducial points, followed by a SVM classifier. Similarly, Gupta et al. (Gupta et al., 2007) use Euclidean/geodesic distances between anthropometric fiducial points, in conjunction with linear classifiers. As stated earlier, the problem of automated detection of fiducial points is non-trivial and hinders automation of these methods. Gordon (Gordan, 1992) argues that curvature descriptors have the potential for higher accuracy in describing surface features and are better suited to describe the properties of faces in areas such as the cheeks, forehead, and chin. These descriptors are also invariant to viewing angles. Li et al. (Li et al., 2009) design a feature pooling and ranking scheme in order to collect various types of low-level geometric features, such as curvatures, and rank them according to their sensitivity to facial expressions. Along

similar lines, Wang et al. (Wang et al., 2010) use a signed shape-difference map between two aligned 3D faces as an intermediate representation for shape comparison. McKeon and Russ (McKeon and Russ, 2010) use a region ensemble approach that is based on Fisherfaces, i.e., face representations are learned using Fisher's discriminant analysis. In (Huang et al., 2010), Huang et al. use a multi-scale Local Binary Pattern (LBP) for a 3D face jointly with shape index. Similarly, Moorthy et al. (Moorthy et al., 2010) use Gabor features around automatically detected fiducial points. To avoid passing over deformable parts of faces encompassing discriminative information, Faltemier et al. (Faltemier et al., 2008) use 38 face regions that densely cover the face, and fuse scores and decisions after performing ICP on each region. A similar idea is proposed in (Spreeuwers, 2011) that uses PCA-LDA for feature extraction, treating the likelihood ratio as a matching score and using the majority voting for face identification. Queirolo et al. (Queirolo et al., 2010) use Surface Inter-penetration Measure (SIM) as a similarity measure to match two face images. The authentication score is obtained by combining the SIM values corresponding to the matching of four different face regions: circular and elliptical areas around the nose, forehead, and the entire face region. In (Alyuz et al., 2008), the authors use Average Region Models (ARMs) locally to handle the challenges of missing data and expression-related deformations. They manually divide the facial area into several meaningful components and the registration of faces is carried out by separate dense alignments to the corresponding ARMs. A strong limitation of this approach is the need for manual segmentation of a face into parts that can then be analyzed separately. Surface distance **based approaches** – There are several papers that utilize distances between points on facial surfaces to define features that are eventually used in recognition. (Some papers call it *geodesic distance* but, in order to distinguish it from our later use of *qeodesics* on shape spaces of curves and surfaces, we shall call it surface distance.) These papers assume that surface distances are relatively invariant to small changes in facial expressions and, therefore, help generate features that are robust to facial expressions. Bronstein et al. (Bronstein et al., 2005a) provide a limited experimental illustration of this invariance by comparing changes in surface distances with the Euclidean distances between corresponding points on a canonical face surface. To handle the open mouth problem, they first detect and remove the lip region, and then compute the surface distance in presence of a hole corresponding to the removed part (Bronstein et al., 2007b). The assumption of preservation of surface distances under facial expressions motivates several authors to define distance-based features for facial recognition. Samir et al. (Samir et al., 2009) use the level curves of the surface distance function (from the tip of the nose) as features for face recognition. Since an open mouth affects the shape of some level curves, this method is not able to handle the problem of missing data due to occlusion or pose variations. A similar polar parametrization of the facial surface is proposed in (Mpiperis et al., 2008b) where the authors study local geometric attributes under this parameterization. To deal with the open mouth problem, they modify the parametrization by disconnecting the top and bottom lips. The main limitation of this approach is the need for detecting the lips, as proposed in (Bronstein et al., 2007b). Berretti et al. (Berretti et al., 2010b) use surface distances to define facial stripes which, in turn, is used as nodes in a graph-based recognition algorithm.

The main limitation of these approaches, apart from the issues resulting from open mouths, is that they

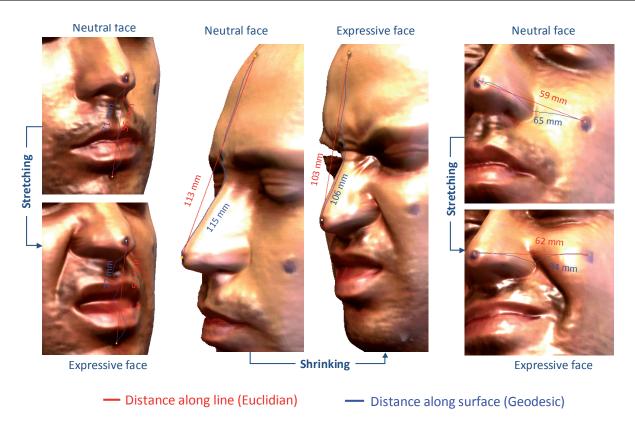


FIGURE 3.2: Significant changes in both Euclidean and surface distances under large facial expressions.

assume that surface distances between facial points are preserved within face classes. This is not valid in the case of large expressions. Actually, face expressions result from the stretching or the shrinking of underlying muscles and, consequently, the facial skin is deformed in a non-isometric manner. In other words, facial surfaces are also stretched or compressed locally, beyond a simple bending of parts. In order to demonstrate this assertion, we placed four markers on a face and tracked the changes in the surface and Euclidean (straight line) distances between the markers under large expressions. Fig. 3.2 shows some facial expressions leading to a significant shrinking or stretching of the skin surface and, thus, causing both Euclidean and surface distances between these points to change. In one case these distances decrease (from 113 mm to 103 mm for the Euclidean distance, and from 115 mm to 106 mm for the surface distance) while in the other two cases they increase. This clearly shows that large expressions can cause stretching and shrinking of facial surfaces, i.e., the facial deformation is elastic in nature. Hence, the assumption of an isometric deformation of the shape of the face is not strictly valid, especially for large expressions. This also motivates the use of elastic shape analysis in 3D face recognition.

3.2 Data Pre-processing and Representation

To analyze facial surfaces (or their shapes), one should first preprocess them and provide the way to represent them as multiple curves. This will be the subject of this section wich will introduce the pipeline of 3D scans pre-processing to denoise the data and to extract the informative part of the face (the facial surface) and the procedure to extract the radial curves, our approximation (or parametrization) of the 3D facial meshes.

3.2.1 3D Face pre-processing

Since the raw data contains a number of imperfections, such as holes, spikes, and include some undesired parts, such as clothes, neck, ears and hair, the data pre-processing step is very important and non-trivial.

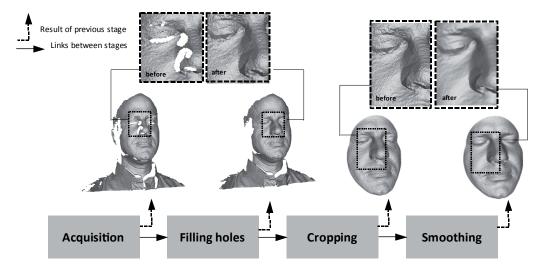


FIGURE 3.3: The different steps of preprocessing: acquisition, filling holes, cropping and smoothing

As illustrated in Fig. 3.3, this step includes the following items:

- \hookrightarrow The hole-filling filter identifies and fills holes in input meshes. The holes are created either because of the absorption of laser in dark areas, such as eyebrows and mustaches, or self-occlusion or open mouths. They are identified in the input mesh by locating boundary edges, linking them together into loops, and then triangulating the resulting loops.
- \hookrightarrow A cropping filter cuts and returns parts of the mesh inside an Euclidean sphere of constant radius centered at the nose tip, in order to discard as much hair as possible. The nose tip is automatically detected for frontal scans and manually annotated for scans with occlusions and large pose variation.
- \hookrightarrow A smoothing filter reduces high frequency components (spikes) in the mesh, improves the shapes of cells, and evenly distributes the vertices on a facial mesh.

The output of the pre-processing step will be a 3D facial mask with the nose tip coordinates, detected automatically. Holes of limited size are filled and the noise filtered out, in addition, only the informative part of the face is kept for the analyze. We have used existing filters from the open source Vizualisation toolkit library³ to design the outlined pipeline.

³http://www.vtk.org/

3.2.2 3D Face Representation by Elastic Radial Curves

Each facial surface is represented by an indexed collection of radial curves that are defined and extracted as follows. Let S be a facial surface obtained as an output of the preprocessing step. The reference curve on S is chosen to be the vertical curve after the face has been rotated to the upright position. Then, a radial curve $\beta^{(\alpha)}$ is obtained by slicing the facial surface by a plane $P^{(\alpha)}$ that has the nose tip as its origin and makes an angle α with the plane containing the reference curve. That is, the intersection of $P^{(\alpha)}$ with S gives the radial curve $\beta^{(\alpha)}$. We repeat this step to extract radial curves from S at equallyseparated angles, resulting in a set of curves that are indexed by the angle α . Fig. 3.4 shows an example of this process. If needed, we can approximately reconstruct S from these radial curves according to $S \approx \cup_{\alpha} \beta^{(\alpha)} = \bigcup_{\alpha} \{S \cap P^{(\alpha)}\}$. Using these curves, we will demonstrate that the elastic framework is well suited to modeling of deformations associated with changes in facial expressions and for handling missing data.

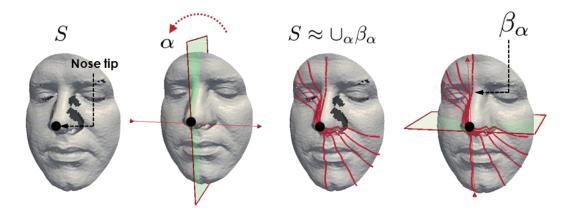


FIGURE 3.4: Extraction of radial curves: images in the middle illustrate the intersection between the face surface and planes to form two radial curves. The collection of radial curves is illustrated in the rightmost image.

In this application (Face Recognition), the probe face is first rigidly aligned to the gallery face using the ICP algorithm. In this step, it is useful but not critical to accurately find the nose tip on the probe face. As long as there is a sufficient number of distinct regions available on the probe face, this alignment can be performed. Next, after the alignment, the radial curves on the probe model are extracted using the plane P_{α} passing through the nose tip of the **gallery** model at an angle α with the vertical. This is an important point in that only the nose tip of the gallery and a good alignment between gallery-probe is needed to extract good quality curves.

3.3 Tools on the Manifold of 3D Faces

In this section we will use the framework described in Chapter 2, in particular the tools designed to interpolate between shapes (geodesics) and the length of these paths, under the defined elastic metric.

Recall that the central goal is given two facial surfaces how to quantify their difference under deformations (caused by expressions), missing data, occlusions and pose variations. Recall also that throw the representation by elastic radial curves, we view the shapes of 3D faces as element of an infinte-dimentional manifold termed \mathcal{M} equipped with a Riemannian elastic metric $(d_{\mathcal{M}})$. We have demonstrated the benefits of the Riemannian approach which allows jointly accurate dense correspondence between 3D surfaces (when counting for the elastic deformations that exhibit the expressive faces). These properties are suitable in face recognition as stated in Section 3.1 to handle the facial deformations.

3.3.1 Shape Interpolation – *Geodesics* on the Shape Space

Given two 3D shapes, since we have deformations (geodesic paths) between their pairwise radial curves, we can spatially interpolate these deformations to obtain deformations between full facial surfaces. In fact, these full deformations can be shown to be formal geodesic paths between faces, when represented as elements of $\mathcal{M} = \mathcal{S}^{[0,2\pi]}$. Shown in Fig. 3.5 are examples of some geodesic paths between source and target faces. It illustrates geodesic paths between faces of different subjects, and are termed *inter-class geodesics*. One can note that the shape located at the center of each path correspond to the average shape between the source ans the target. As illustrated, it has an intermediate-smooth morphology between the shapes of the ending points of each geodesic. In other worlds, when considering two facial shapes of different age, different gender or different ethnicity on could generate with our method a typical average face between them, in a mathematical way!



FIGURE 3.5: Three examples of inter-class geodesic paths. In each row, the first and the last 3D shapes represent respectively the source and the target faces, the intermediate shapes are equally-spaces points from the geodesic gerenated by our algorithm.

Shown in Fig. 3.6 are examples geodesic paths between faces of the same person conveying different expressions, and are termed *intra-class geodesics*. In the same way, we can note that the central shape

on each of these paths represent the middle intermediate deformation from the source and the target shapes.



FIGURE 3.6: Three examples of intra-class geodesic paths. In each row, the first and the last 3D shapes represent respectively the source and the target faces, the intermediate shapes are equally-spaces points from the geodesic gerenated by our algorithm.

These geodesics provide a tangible benefit, beyond the current algorithms that provide some kind of a similarity score for analyzing faces. These geodesic paths illustrate the most efficient way to deform one shape into another. The accurate dense correspondence, one of the essential ingredients of shape analysis, plays an important role to get these natural-like deformations (or morphing). In fact, matching accurately different anatomical parts of the faces yields with accurate deformations, hence the importance of use elastic models in shape analysis of facial surfaces. In addition to their interpretation as optimal deformations under the chosen metric, the geodesics can also be used for computing the mean shape and measuring the shape covariance of a set of faces, as illustrated later.

3.3.2 Expression-Robust 3D Face Recognition

We will show in this section the benefits of using our **elastic model** in comparing facial surfaces exhibiting different facial expressions. The goal here is the robustness to the deformations introduced by the expressions. We should note here that in case of open mouth which often results in a hole, the preprocessing algorithm presented in section 3.2.1 will fill the hole by locating the edges and interpolating between them. An other important step is to discrete the shape representation both by indexed collections of radial curves and finite-points representations of each curve, starting from the nose tip. To this end, facial surface S is represented by an indexed collection of radial curves, indexed by the n uniform angles $\mathcal{A} = \{0, \frac{2\pi}{n}, \frac{4\pi}{n}, \dots, 2\pi \frac{(n-1)}{n}\}$. Thus, the shape of a facial surface can been represented

as an element of the set $S^n \approx \mathcal{M}$. The indexing provides a correspondence between curves across faces. For example, the curve at an angle α on a probe face is compared with the curve at the same angle on a gallery face. Thus, the distance between two facial surfaces is $d_{\mathcal{M}} : S^n \times S^n \to \mathbb{R}_{\geq 0}$, given by $d_{\mathcal{M}}(\mathcal{F}^1, \mathcal{F}^2) \doteq \frac{1}{n} \sum_{\alpha \in \mathcal{A}} d_{\mathcal{S}}([q_1^{(\alpha)}], [q_2^{(\alpha)}])$. Here, $[q_i^{(\alpha)}]$ denotes the SRVF of the radial curve $\beta_i^{(\alpha)}$ on the i^{th} facial surface, $i \in 1, 2$.

To explore experimentally the ability of our elastic model to be robust the facial excessions, we conducted our experiments on the FRGC2.0 dataset (Face Recognition Grand Challenge) (Phillips et al., 2005). The dataset contains 4007 3D scans of 466 subjects with near-frontal pose. About 40% of the scans are expressive. In our experiment we will consider the manual clustering of the 3D scans into three categories: neutral expression, small expression, and large expression as illustrated in Figure 3.7.

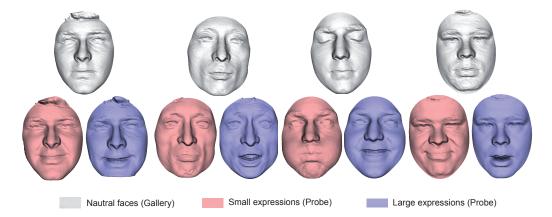


FIGURE 3.7: Examples of 3D preprocessed scans from the FRGC2.0 dataset. The Gallery faces are almost neutral as shown by the top row. The set of probe faces includes small expressions (in red) and large expressions (in blue) as shown in the second row.

As shown in Figure 3.7, the facial surfaces output of the pre-processing step are of good quality. Now, we will report experimental results both under the identification and verification scenarios, using the commonly used evaluation criteria in biometrics.

I. Identification Scenario: The gallery consists of the first scans for each subject in the database, and the remaining scans make up the probe faces. This dataset was automatically preprocessed as described in the Section 3.2.1. The left panel of Figure 3.8 shows the Cumulative Matching Curves (CMCs) of our method under this protocol for the three cases: neutral vs. neutral, neutral vs. non-neutral and neutral vs. all. Note that our method results in 97.7% rank-1 recognition rate in the case of neutral vs. all. In the difficult scenario of neutral vs. expressions, the rank-1 recognition rate is 96.8%, which represents a high performance, while in the simpler case of neutral vs. neutral the rate is 99.2%. As shown in these CMC curves the recognition rates reaches quickly 100% (at rank 5).

A comparison of recognition performance of our method with several state-of-the-art results is presented in Table 3.1. This time, in order to keep the comparisons fair, we kept all the 466 scans in the gallery. Notice that our method achieved a 97% rank-1 recognition which is close to the highest published results

| Method | Rank-1 Recognition Rate (%) |
|------------------------------|-----------------------------|
| (Spreeuwers, 2011) | 99% |
| (Wang et al., 2010) | 98.3% |
| (ter Haar and Velkamp, 2010) | 97% |
| (Berretti et al., 2010b) | 94.1% |
| (Queirolo et al., 2010) | 98.4% |
| (Faltemier et al., 2008) | 97.2% |
| (Kakadiaris et al., 2007) | 97% |
| (Drira et al., 2013a) | 97% |

TABLE 3.1: Comparison of rank-1 scores on the FRGCv2 dataset with the state-of-the-art results.

on this dataset (Faltemier et al., 2008, Spreeuwers, 2011, Queirolo et al., 2010). Since the scans in FRGCv2 are all frontal, the ability of region-based algorithms, such as (Faltemier et al., 2008, Queirolo et al., 2010), to deal with the missing parts is not tested in this dataset. For that end, one would need a systematic evaluation on a dataset with the missing data issues, e.g. the GavabDB. The best recognition score on FRGCv2 is reported by Spreeuwers (Spreeuwers, 2011) which uses an intrinsic coordinate system based on the vertical symmetry plane through the nose. The missing data due to pose variation and occlusion challenges will be a challenge there as well.

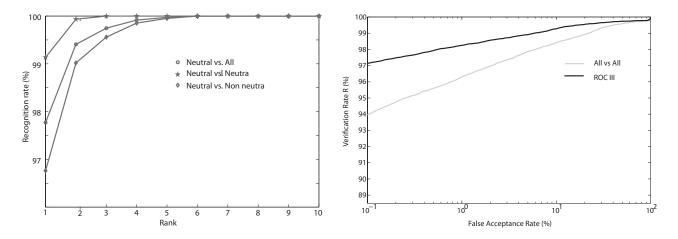


FIGURE 3.8: Left: Cumulative Matching Curves for the Neutral vs. Neutral, Neural vs. Small expressions and Neutral vs. Large expressions on FRGC2.0. Right: ROC curves for the All vs. All and ROC III evaluation protocols.

I. Verification Scenario: In order to evaluate the performance of the proposed approach in the verification scenario, the Receiver Operating Characteristic (ROC) curves for the ROC III mask of FRGCv2 and "all-versus-all" are plotted in the right part of Fig. 3.8. For comparison, Table 3.2 shows the verification results at false acceptance rate (FAR) of 0.1 percent for several methods. For the standard protocol testings, the ROC III mask of FRGC v2, we obtain the verification rates of around 97%, which is comparable to the best published results. In the all-versus-all experiment, our method provides 93.96% VR

at 0.1% FAR, which is among the best rates in the table (Wang et al., 2010, Spreeuwers, 2011, Queirolo et al., 2010).

| Method | ROC III | All vs. All |
|---------------------------|---------|-------------|
| (Kakadiaris et al., 2007) | 97% | — |
| (Faltemier et al., 2008) | 94.8% | 93.2% |
| (Berretti et al., 2010b) | _ | 81.2% |
| (Queirolo et al., 2010) | 96.6% | 96.5% |
| (Spreeuwers, 2011) | 94.6% | 94.6% |
| (Wang et al., 2010) | 98.4% | 98.1% |
| (Drira et al., 2013a) | 97.1% | 93.9% |

TABLE 3.2: Comparison of verification rates at FAR=0.1% on the FRGCv2 dataset with state-of-the-art results (the ROC III mask and the All vs. All scenario).

Note that these approaches are applied to FRGCv2 only. Since scans in FRGCv2 are mostly frontal and have high quality, many methods are able to provide good performance. It is, thus, important to evaluate a method in other situations where the data quality is not as good. In the next two sections, we will consider those situations with the GavabDB involving the pose variation and the Bosphorus dataset involving the occlusion challenge.

3.3.3 3D Face Recognition under Large Pose Variations

In situations involving non-frontal 3D scans, some curves may be partially hidden due to self occlusion. The use of these curves in face recognition can severely degrade the recognition performance and, therefore, they should be identified and discarded.

I. Curve Quality Filter: We introduce here a quality filter that uses the continuity and the length of a curve to detect such curves. To pass the quality filter, a curve should be one continuous piece and have a certain minimum length, say of, 70mm. The discontinuity or the shortness of a curve results either from missing data or large noise. We show two examples of this idea in Fig. 3.9 where we display the original scans, the extracted curves, and then the action of the quality filter on these curves. Once the quality filter is applied and the high-quality curves retained, we can perform face recognition procedure using only the remaining curves. That is, the comparison is based only on curves that have passed the quality filter. Let β denotes a facial curve, we define the boolean function quality: $(quality(\beta) = 1)$ if β passes the quality filter and $(quality(\beta) = 0)$ otherwise. Recall that during the pre-processing step, there is a provision for filling holes. Sometimes the missing parts are too large to be faithfully filled using linear interpolation. For this reason, we need the quality filter that will isolate and remove curves associated with those parts.

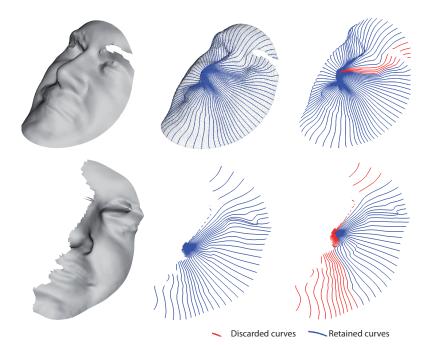


FIGURE 3.9: Curve quality filter: examples of detection of broken and short curves (in red) and complete curves (in blue). The first example show missing data due to bad reflection of the laser by the eyebrow. The second example shows a profile scan with only half of the data available.

II. Experiments on the GavabDB dataset: Since GavabDB (Moreno and Sanchez, 2004) has many noisy 3D face scans under large facial expressions, we will use that database to help evaluate our framework. This database consists of the Minolta Vi-700 laser range scans from 61 subjects – 45 male and 16 female – all of them Caucasian. Each subject was scanned nine times from different angles and under different facial expressions (six with the neutral expression and three with non-neutral expressions). The neutral scans include several frontal scans – one scan while looking up (+35 degree), one scan while looking down (-35 degree), one scan from the right side (+90 degree), and one from the left side (-90 degree). The non-neutral scans include cases of a smile, a laugh, and an arbitrary expression chosen freely by the subject. Figure 3.10 shows the nine scans of one subject from the GavabDB.



FIGURE 3.10: Scans of one subject of the GavabDB dataset under different variations.

One of the two frontal scans with the neutral expression for each person is taken as a gallery model, and the remaining are used as probes. Table 3.3 compares the results of our method with the previously published results following the same protocol. As noted, our approach provides the highest recognition rate for faces with non-neutral expressions (94.54%). This robustness comes from the use of radial, elastic

| Method | (N) | (E) | (N)+(E) | (LD) | (LU) | (RS) | (LS) |
|------------------------|-------|-------|---------|-------|-------|-------|-------|
| (Li et al., 2009) | 96.6% | 93.3% | 94.6% | _ | — | _ | — |
| (Moreno et al., 2005) | 90.1% | 77.9% | — | _ | _ | _ | — |
| (Mahoor and Abdel- | _ | 72% | 78% | 85.3% | 88.6% | _ | — |
| Mottaleb, 2009) | | | | | | | |
| (ter Haar and | _ | _ | - | _ | _ | _ | — |
| Velkamp, 2010) | | | | | | | |
| (Mousavi et al., 2008) | _ | _ | 91% | _ | _ | _ | — |
| (Drira et al., 2013a) | 100% | 94.5% | 95.9% | 100% | 98.3% | 70.4% | 86.8% |

TABLE 3.3: Recognition results comparison of the different methods on the GavabDB.

curves since: (1) each curve represents a feature that characterizes local geometry and, (2) the elastic matching is able to establish a correspondence with the correct alignment of anatomical facial features across curves. Table 3.3 provides an exhaustive summary of results obtained using GavabDB; our method outperforms the majority of other approaches in terms of the recognition rate. Note that there is no prior result in the literature on 3D face recognition using sideway-scans from this database. Although our method works well on common faces with a range of pose variations within 35 degrees, it can potentially fail when a large part of the nose is missing, as it can cause an incorrect alignment between the probe and the gallery. This situation occurs if the face is partially occluded by external objects such as glasses, hair, etc. To solve this problem, we first restore the data missing due to occlusion.

3.3.4 3D Face Recognition under External occlusions

In this section we target the problem of occlusions by external parts like glasses, hands, hair, etc. We will consider two components, (1) external occlusion detection and removal and (2) missing data recovery.

I. Occlusion Removal: The first problem we encounter in externally-occluded faces is the detection of the external object parts. We accomplish this by comparing the given scan with a template scan, where a template scan is developed using an average of training scans that are complete, frontal and have neutral expressions. The basic matching procedure between a template and a given scan is recursive ICP, which is implemented as follows. In each iteration, we match the current face scan with the template using ICP and remove those points on the scan that are more than a certain threshold away from the corresponding points on the template. This threshold has been determined using experimentation and is fixed for all faces. In each iteration, additional points that are considered extraneous are incrementally removed and the alignment (with the template) based on the remaining points is further refined.

Fig. 3.11 shows an example of this implementation. From left to right, each face shows an increasing alignment of the test face with the template, with the aligned parts shown in magenta, and also an increasing set of points labeled as extraneous, drawn in pink. The final result, the original scan minus the extraneous parts, is shown in green at the end. In the case of faces with external occlusion, we first

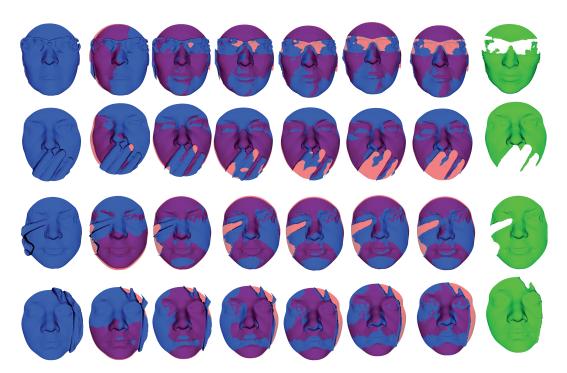


FIGURE 3.11: Gradual removal of occluding parts in a face scan using Recursive-ICP.

restore them and then apply the recognition procedure. That is, we detect and remove the occluded part, and recover the missing part resulting in a full face that can be compared with a gallery face using the metric $d_{\mathcal{S}}$. The recovery is performed using the tangent PCA analysis and Gaussian models, as described in Section 3.4. In order to evaluate our approach, we perform this automatic procedure on the Bosphorus database (Alyuz et al., 2008).

II. Completion of Partially-Obscured Curves: Earlier we have introduced a filtering step that finds and removes curves with missing parts. Although this step is effective in handling some missing parts, it may not be sufficient when parts of a face are missing due to external occlusions, such as glasses and hair. In the case of external occlusions, the majority of radial curves could have hidden parts that should be predicted before using these curves. This problem is more challenging than self-occlusion because, in addition to the missing parts, we can also have parts of the occluding object(s) in the scan. In a non-cooperative situation, where the acquisition is unconstrained, there is a high probability for this kind of occlusion to occur. Once we detect points that belong to the face and points that belong to the occluding object, we first remove the occluding object and use a statistical model in the shape space of radial curves to complete the broken curves. This replaces the parts of face that have been occluded using information from the visible part and the training data.

The core of this problem, in our representation of facial surfaces by curves, is to take a partial facial curve and predict its completion. The sources of information available for this prediction are: (1) the current (partially observed) curve and (2) several (complete) training curves at the same angle that are extracted from full faces. The basic idea is to develop a sparse model for the curve from the training curves and use that to complete the observed curve. To keep the model simple, we use the PCA of the training data, in an appropriate vector space, to form an orthogonal basis representing training shapes. Then, this basis is used to estimate the coefficients of the observed curve and the coefficients help reconstruct the full curve. Since the shape space of curve S is a nonlinear space, we use the tangent space $T_{\mu}(S)$, where μ is the mean of the training shapes, to perform PCA. Let α denote the angular index of the observed curve, and let $q_{\alpha}^1, q_{\alpha}^2, \ldots, q_{\alpha}^k$ be the SRVFs of the curves taken from the training faces at that angle. As described earlier, we can compute the sample Karcher mean of their shapes $\{[q_{\alpha}^i] \in S\}$, denoted by μ_{α} . Then, using the geometry of S we can map these training shapes in the tangent space using the inverse exponential map. We obtain $v_{i,\alpha} = \exp_{\mu_{\alpha}}^{-1}(q_{\alpha}^i)$, where

$$\exp_{q_1}^{-1}(q_2) = \frac{\theta}{\sin(\theta)}(q_2^* - \cos(\theta)q_1), \quad \theta = \cos^{-1}(\langle q_1, q_2^* \rangle) ,$$

and where q_2^* is the optimal rotation and re-parameterization of q_2 to be aligned with q_1 , as discussed earlier. A PCA of the tangent vectors $\{v_i\}$ leads to the principal basis vectors $u_{1,\alpha}$, $u_{2,\alpha}$, ..., $u_{J,\alpha}$, where J represents the number of significant basis elements.

Now returning to the problem of completing a partially-occluded curve, let us assume that this curve is observed for parameter value t in $[0, \tau] \subset [0, 1]$. In other words, the SRVF of this curve q(t) is known for $t \in [0, \tau]$ and unknown for $t > \tau$. Then, we can estimate the coefficients of q under the chosen basis according to $c_{j,\alpha} = \langle q, u_{j,\alpha} \rangle \approx \int_0^\tau \langle q(t), u_{j,\alpha}(t) \rangle dt$, and estimate the SRVF of the full curve according to

$$\hat{q}_{\alpha}(t) = \sum_{j=1}^{J} c_{j,\alpha} u_{j,\alpha}(t) , \ t \in [0,1] .$$

We present three examples of this procedure in Fig. 3.12, with each face corrupted by an external occlusion as shown in column (a). The detection and removal of occluded parts is performed as described in the previous section, and the result of that step is shown in column (b). Finally, the curves passing through the missing parts are restored and shown in (c).

In order to evaluate this reconstruction step, we have compared the restored surface (shown in the top row of Fig. 3.12) with the complete neutral face of that class, as shown in Fig. 3.13. The small values of both absolute deviation and signed deviation, between the restored face and the corresponding face in the gallery, demonstrate the success of the restoration process.

III. Experiments on Bosphorus Dataset: The Bosphorus database is suitable for this evaluation as it contains scans of 60 men and 45 women, 105 subjects in total, in various poses, expressions and in the presence of external occlusions (eyeglasses, hand, hair). The majority of the subjects are aged between 25 and 35. The number of total face scans is 4652; at least 54 scans each are available for most of the subjects, while there are only 31 scans each for 34 of them. The interesting part is that for each subject there are four scans with occluded parts. These occlusions refer to (i) mouth occlusion by hand, (ii) eyeglasses, (iii) occlusion of the face with hair, and (iv) occlusion of the left eye and forehead regions by

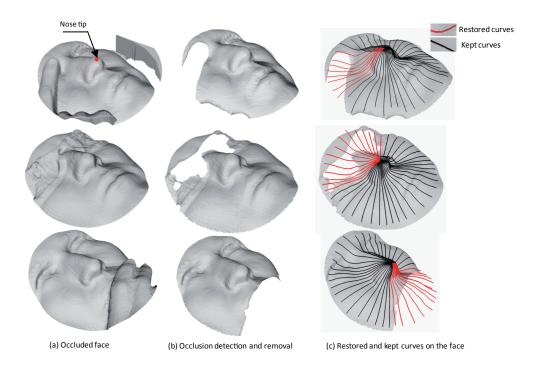


FIGURE 3.12: (a) Faces with external occlusion, (b) faces after the detection and removal of occluding parts and (c) the estimation of the occluded parts using a statistical model on the shape spaces of curves.

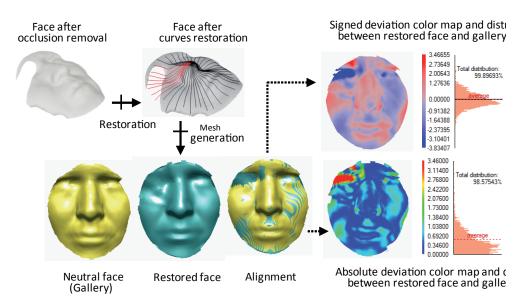


FIGURE 3.13: Illustration of a face with missing data (after occlusion removal) and its restoration. The deviation between the restored face and the corresponding neutral face is also illustrated.

hands. Fig. 3.14 shows sample images from the Bosphorus 3D database illustrating a full scan on the left and the remaining scans with typical occlusions.

We pursued the same evaluation protocol used in the previously published papers: a neutral scan for each person is taken to form a gallery dataset of size 105 and the probe set contains 381 scans that have occlusions. The training is performed using other sessions so that the training and test data are disjoint.



FIGURE 3.14: Examples of faces from the Bosphorus database. The un-occluded face on the left and the different types of occlusions are illustrated.

The rank-1 recognition rate is reported in Fig. 3.15 for different approaches depending upon the type of occlusion. As these results show the process of restoring occluded parts significantly increases the accuracy of recognition. The rank-1 recognition rate is 78.63% when we remove the occluded parts and apply the recognition algorithm using the remaining parts, as described in Section 2.4. However, if we perform restoration, the recognition rate is improved to 87.06%. Clearly, this improvement in performance is due to the estimation of missing parts on curves. These parts, that include important shape data, were not considered by the algorithm described earlier. Even if the part added with restoration introduces some error, it still allows us to use the shapes of the partially observed curves. Furthermore, during restoration, the shape of the partially observed curve is conserved as much as possible.

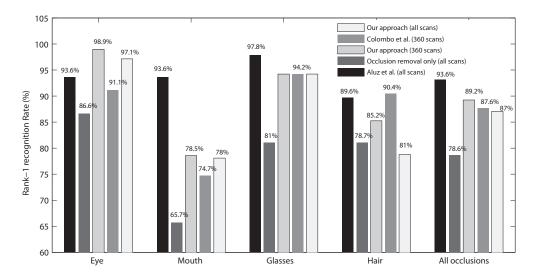


FIGURE 3.15: Recognition results on the Bosphorus database and comparison with state-of-the-art approaches.

Examples of 3D faces recognized by our approach are shown in Fig. 3.12, along with different steps of the algorithm. The faces in the two bottom rows are examples of incorrectly recognized faces by our algorithm without restoration (as described earlier), but after the restoration step, they are correctly recognized. (Alyuz et al., 2008) reported a 93.69% rank-1 recognition rate overall for this database using the same protocol that we have described above. While this reported performance is very good, their processing has some manual components. Actually, the authors partition the face manually and fuse the scores for matching different parts of the face together. In order to compare with (Colombo et al., 2011),

we reduce the probe dataset to 360 by discarding bad quality scans as (Colombo et al., 2011) did. Our method outperforms their approach with an overall performance of 89.25%, although individually our performance is worse in the case of occlusion by hair. It is difficult, in this case, to completely overcome face occlusion. Therefore, during the restoration step, our algorithm tries to keep majority of parts. This leads to a deformation in the shape of curves and, hence, affects the recognition accuracy.

3.4 Towards Efficient Face Recognition Solution

In this section, we explore two complementary ideas to make the recognition scenario more efficient. It is well stated that, compared to 2D-face recognition approaches, the 3D-based approaches required more computational time for several reasons. The most important one is the data representation itself, where the data in 2D are images (ordered pixels), in the second case the data is 3D meshes without any order. We target here the one-to-many matching scenario (identification scenario). To handle these issues, we propose first (1) a tree-like organization of the facial surfaces in the Gallery, and (2) introduce a boosting step to highlight and select the most relevant curves on the face. Thus, a gain on time will happen when parsing the branches of the tree instead of an exhaustive comparison, and use only the relevant curves to compare the probe face to the gallery face.

3.4.1 Hierarchical Gallery Organization

One of the main goals for studying shapes of faces is to conduct biometric identification where query is often compared to a set of gallery shapes. This comparison can be made more efficient if we can organize the gallery elements in form of a hierarchical database, i.e. a tree, where the comparisons are performed only at the nodes of that tree. To construct such a shape tree we need to be able to cluster similar shapes, and that is the problem we study next.

I. Clustering of 3D Faces: Consider the problem of clustering n faces (in \mathcal{M}) into k clusters. A general approach is to form clusters in such a way that they minimize total "within-cluster" variance. Let a configuration \mathcal{F} consists of clusters denoted by $\mathcal{F}_1, \mathcal{F}_2, \ldots, \mathcal{F}_k$, and let μ_i s be the mean shapes in \mathcal{F}_i s and n_i s be the sizes of \mathcal{F}_i s. There are several cost functions used for clustering, e.g the sum of traces of covariances within clusters. However, the computation of means μ_i s of large shape clusters, and therefore their variances, is computationally expensive, especially when they are updated at every iteration. As a solution, one often uses a variation, called *pairwise clustering* (Hofmann and Buhmann, 1998), where the variance of a cluster is replaced by a scaled sum of distances (squared) between its elements:

$$Q(\mathcal{F}) = \sum_{i=1}^{k} \frac{2}{n_i} \left(\sum_{\mathcal{F}^a \in \mathcal{F}_i} \sum_{b < a, \mathcal{F}^b \in \mathcal{F}_i} d_{\mathcal{M}}(\mathcal{F}^a, \mathcal{F}^b)^2 \right).$$
(3.1)

We seek configurations that minimize Q, i.e., $\mathcal{F}^* = \operatorname{argmin} Q(\mathcal{F})$. Notice that the metric used is the arithmetic mean $d_{\mathcal{M}}$. We will minimize the clustering cost using a Markov chain search process on the configuration space. The basic idea is to start with a configuration of k clusters and reduce Q by rearranging shapes among the clusters. The re-arrangement is performed in a stochastic fashion using two kinds of moves. These moves are performed with probability proportional to the negative exponential of the Q-value of the resulting configuration. The two types of moves are following. (1) **Move a shape**: Here we select a shape randomly and re-assign it to another cluster. Let $Q_j^{(i)}$ be the clustering cost when a shape N_j is re-assigned to the cluster C_i keeping all other clusters fixed. If N_j is not a singleton, i.e. not the only element in its cluster, then the transfer of N_j to cluster C_i is performed with probability: $P_M(j, i; T) = \frac{\exp(-Q_j^{(i)}/T)}{\sum_{i=1}^{k} \exp(-Q_j^{(i)}/T)}$ $i = 1, 2, \ldots, k$. Here T plays a role similar to temperature in simulated annealing. If N_j is a singleton, then moving it is not allowed in order to fix the number of clusters at k. (2) **Swap two shapes**: Here we select two shapes randomly from two different clusters and swap them. Let $Q^{(1)}$ and $Q^{(2)}$ be the Q-values of the original configuration (before swapping) and the new configuration (after swapping), respectively. Then, swapping is performed with probability: $P_S(T) = \frac{\exp(-Q^{(2)}/T)}{\sum_{i=1}^{k} \exp(-Q^{(i)}/T)}$. In order to seek global optimization, we have adopted a simulated annealing approach. Although simulated annealing and the random nature of the search help in avoiding local minima, the convergence to a global minimum is difficult to establish.

It is important to note that once the pairwise distances are computed, they are not computed again in the iterations. Secondly, unlike k-mean clustering, the mean shapes are never calculated in this clustering. The algorithms for computing Karcher mean and clustering can be applied repeatedly for organizing a large database of human faces into a hierarchy that allows efficient searches during identification process. As an illustration of this idea, we consider the 466 face scans corresponding of distinct subjects of FRGC2.0 dataset. These shapes form the bottom layer of the hierarchy, called level D in Figure 3.16. Then, we compute Karcher mean shapes (representative shapes) for each person to obtain shapes at level C. These shapes are further clustered together and a Karcher mean is computed for each cluster. These mean shapes form the level B of the hierarchy. Repeating this idea a few times, we reach the top of the tree with only one shape. We obtain so the final tree shown in Figure 3.16. If we follow a path from top to bottom of the tree, we see the shapes getting more particularized to groups and then to individuals as illustrated in Figure 3.17.

II. Hierarchical Shape Identification: Once the tree is formed, one can use this representation of data to conduct biometric search in order to reduce time computation. Specially in identification scenario, which needs a comparison of the query shape to the whole gallery dataset. In view of this structure, a natural way is to start at the top, compare the query with the shapes at each level, and proceed down the branch that leads to the closest shape. At any level of the tree, there is a number, say h, of possible shapes and our goal is to find the shape that matches the query best.

III. Experiments on FRGC2.0: We have tested this idea on the FRGC2.0 dataset where the Gallery subset is organized as describes in I and the query scans are matched against the faces in a single branch

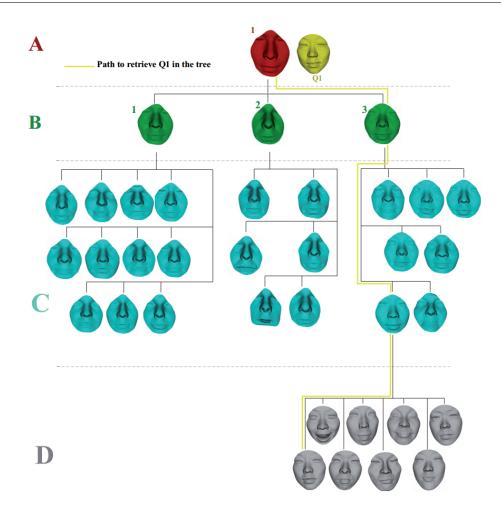


FIGURE 3.16: The tree resulting on hierarchical clustering on the 466 earliest scans of FRGC2.0 dataset (the Gallery).

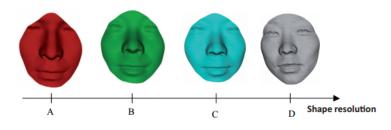


FIGURE 3.17: Paths from top to bottom in the tree show increasing shape resolutions

of the tree, according to the retrieval procedure described in II. The rank on recognition rate is 92.4% compared to 97% without clustering (by performing exhaustive search along the gallery). The time concuming is reduced from 52 minutes to 3 minutes in average which is 15 times less.

3.4.2 Boosting Geometric Facial Features

In this part, we combine ideas from *shape analysis* using tools from differential geometry and *feature selection* derived from Machine Learning to select and highlight salient 3D geometrical facial features. Notice that we introduce in addition to the radial curves presented above, iso-level curves extracted on the face with a reference point the nose tip and the Euclidean distance as the set function, as shown if Figure 3.19. Our previous studies on iso-level curves on facial surfaces as complete biometrics (Ben Amor et al., 2009) an on the nose (Drira et al., 2009a,b) as partial biometrics, demonstrated their relevance to conduct shape statistics. However, their use assume that surface distances are relatively robust to changes in facial expressions and, therefore, help generate features that are robust to facial expressions. The assumption of preservation of surface distances under facial expressions is no more true when large expressions are conveyed which result in stretching and shrinking of the facial surface. In addition, since an open mouth affects the shape of some level curves, this method is not able to handle the problem of missing data.

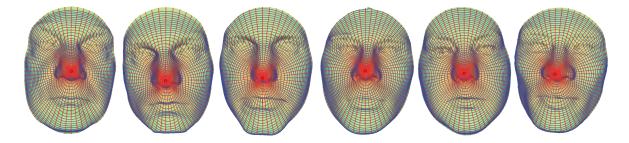


FIGURE 3.18: Radial and iso-level curves extracted on some faces fron FRGC2.0 dataset.

After preprocessing the 3D scans, we represent obtained facial surfaces by finite indexed collections of circular and radial curves. The comparison of pairwise curves, extracted from faces, is based on shape analysis of parameterized curves using differential geometry tools (as described in Chapter 2). The extracted features are trained as weak classifiers and the most discriminative features are selected optimally by adaptive boosting. Accordingly, it consists on the following steps:

- The *Off-line training step*, learns the most salient circular and radial curves from the sets of extracted ones, in a supervised fashion. In face recognition, construct feature vectors by comparing pairwise curves extracted from facial surfaces. Next, feed these examples, together with labels indicating if they are inter-class or not. Thus, the adaptive boosting selects and learns alliteratively the weak classifiers and adding them to a final strong classifier, with suitable weights. As a result of this step, we keep the *T*-earliest selected features (with highest weights) for the testing step.
- The **On-line test step**, performs classification of a given test face. In the recognition problem, a probe face is compared to the gallery faces using only individual scores computed based on selected features using the $d_{\mathcal{S}}$ metric.

Here, we introduce the feature selection step to highlight (or localize) the most stable and most discriminatory curves. To this end, we use the well-known machine learning algorithm AdaBoost introduced by Freund and Schapire in (Freund and Schapire, 1995). Recall that, boosting is based on iterative selection of weak classifiers by using a distribution of training samples. At each iteration, the best weak classifier is provided and weighted by the quality of its classification. In practice, the individual level curves and radial curves are used as weak classifiers. After M iterations, the most relevant T (T < M) facial curves are returned by the algorithm. The set of selected curves returned by Adaboost is shown in Fig. 3.19. The first row of the figure shows the locations of the subset of curves selected by Adaboost on different sessions of the same person with different expressions, whereas, the second row gives curves locations on different subjects. We notice that the boosting algorithm selects the level curves located on the nasal region, which is stable under expressions and radial curves in the way that it avoid two parts, the first one is the lower part of the face since its shape is affected by expressions, particularly when the mouth is open. The second area corresponds to the eye/eyebrow regions. Shapes of radial curves passing throw these regions change when conveying expressions. In contrast, the most stable area cover the nasal/forehead/cheeks regions. As expected and studied in our previous papers (Drira et al., 2009a,b), the use of level curves on the nose is relevant to perform expression-robust partial face analysis.

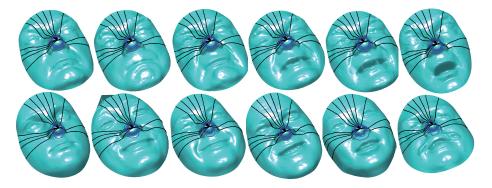


FIGURE 3.19: The most discriminating radial and circular curves selected by Boosting for face recognition, given on different faces.

This approach has been trained and tested on the FRGC2.0 dataset and reported 98.02% as rank-one recognition rate using only a subset of of radial and iso-level curves.

| Performance | All curves | | Selected curves | | |
|---------------|------------|---------|-----------------|---------|--|
| 1 enformance | Rank-1 RR | Time(s) | Rank-1 RR | Time(s) | |
| Radial curves | 88.65% | 1.6 | 89.04% | 0.48 | |
| Level curves | 66.51% | 1.04 | 85.65% | 0.20 | |
| Fusion | 91.81% | 2.64 | 98.02% | 0.68 | |

TABLE 3.4: Rank-1/Computation cost (in sec) for different configurations.

Table 3.4 reports the rank-one recognition rates of the radial and the level curves taken individually as well as their fusion. Also, it reports the recognition rates achieved using only the salient features. We notice that the fusion of selected radial and level features achieved the highest performance (98.02%), we can see also an important gain in the computational time (0.68 seconds) to match two facial surfaces.

These ideas (a) hierarchical clustering of the gallery and (b) boosting the geometric curves are presented disjoint. We expect that their use, in the same system, can improve the computational time in a one-to-many matching scenario and keep high recognition performance.

3.5 Conclusion

In this chapter we have demonstrated the application of our Riemannian approach in statistical shape analysis of facial surfaces with the final goal of face recognition. Several problems have been tackled using the unified framework – (1) face comparisons under shape-preserving transformations, (2) shape matching and comparison of 3D shapes robust to deformations caused by the expressions, (3) averaging facial shapes to represent classes/clusters and its use in organizing hierarchically the Gallery for efficient one-to-many matching (4) partially-obscured data completion then shape analysis using statistical models to recover missing data, and (5) Combine ideas from differential geometry and feature selection to select salient curves for more efficient recognition. We have presented results on the mostly used 3D Face datasets (FRGC2.0, Gavab and Bosphorus) designed to develop and test solutions working under variations of facial expression, pose variations and occlusions between gallery and probe scans.

Chapter 4

3D Facial Expression Recognition

In this chapter¹ we introduce two major contributions in the field of facial expression analysis and recognition from static and dynamic 3D data. In particular, we show how to capture facial movements using geometric shape analysis tools introduced in Chapter 2.

Hence, instead of the deformation-robust shape analysis, developed in Chapter 3 oriented to 3D face recognition, we focus here on two relevant questions — How effectively capture the facial deformations resulted from the facial expressions? and how establish facial deformation patterns for successful classification? — To answer these questions, we adopt two approaches : (1) A Landmark-dependent approach is first introduced in (Maalej et al., 2010, 2011) which uses 3D static scans. Herein, we propose a new facial representation using Local Facial Patches extracted around the landmarks, suitable for expression analysis; then (2) A Landmark-free approach (Drira et al., 2012, Ben Amor et al., 2014a) operating on dynamic data is developed based on a Global Facial Representation of 4D data. In both approaches, the issue of shape correspondence is a key point to achieve accurate measurements of the deformations. These deformations which characterize the facial expressions, such as happy or surprise, are executed by facial muscles and they are more prominent in 3D (geometry) than 2D (appearance or texture), which motivates this choice to this shift in the very recent literature. In both approaches that we have introduced, adapted Riemannian shape analysis frameworks are applied to derive statistical analysis of facial shapes. The classification task is resolved using conventional Machine Learning techniques, as Random Forest (RF), Support Vector Machine (SVM), Adaboost and Hidden Markov Model (HMM).

After introducing the problem, sections 4.2 and 4.2 describe our contributions in facial expression from static and dynamic data, respectively.

¹The content of this chapter is related to our published papers in the field of facial expression recognition, (Maalej et al., 2011) and (Ben Amor et al., 2014a).

4.1 Introduction

Over the last two decades, automatic recognition of facial expressions emerged as a field of active research, with applications in several different areas, such as HMI (Human-Machine Interaction), psychology, computer graphics, transport security (by detecting driver fatigue, for example), and so on. The importance of facial expressions was first realized and investigated by psychologists, among others. In a seminal work by Mehrabian et al. (Mehrabian and Wiener, 1967) the relative importance of verbal and nonverbal messages in communicating feelings and attitude is described. In particular, they provided evidence that face-to-face communication is governed by the 7%-38%-55% rule, that balances the relevance of verbal, vocal and visual elements, respectively, in communications. Despite this rigid quantification has since been refuted in later studies, it still provides an indication that the words and tone of the voice form only a part of human communication. The non-verbal elements related to the body language (e.g., gestures, posture, facial expressions) also play an important role. Starting from a different point of view, Ekman (Ekman, 1972) conducted the first systematic studies on facial expressions in the late 70s. Ekman also showed that facial expressions can be coded through the movement of face points as described by a set of action units (Ekman and Friesen, 1977). Through his experiments, it is demonstrated that there are six prototypical facial expressions, representing anger, disgust, fear, happiness, sadness and surprise, plus the *neutral* one that are universally recognized and remain consistent across different ethnicities and cultures. The presence of these prototypical facial expressions is now widely accepted for scientific analysis. These results, in turn, inspired many researchers to analyze facial expressions in video data, by tracking facial features and measuring the amount of facial movements in video frames (Zeng et al., 2009). This body of work demonstrates a collective knowledge that facial expressions are highly dynamical processes, and looking at sequences of face instances can help to improve the recognition performance. We further emphasize that, rather than being just a static or dynamic 2D image analysis, it is more natural to analyze expressions as spatio-temporal deformations of 3D faces, caused by the actions of facial muscles. In this approach, the facial expressions can be studied comprehensively by analyzing temporal dynamics of 3D face scans (3D plus time is often regarded as 4D data). From this perspective the relative immunity of 3D scans to lighting conditions and pose variations give support for the use of 3D and 4D data. Motivated by these considerations, there has been a progressive shift from 2D to 3D in performing facial shape analysis for recognition and expression recognition. In particular, this latter research subject is gaining momentum thanks to the recent availability of public 3D datasets, like the Binghamton University 3D Facial Expression database (BU-3DFE) (Yin et al., 2006a), and the Bosphorus 3D Face Database (Savran et al., 2008). At the same time, advances in 3D imaging technology (Di3D, 2006, 3DMD, 2010) have permitted collections of large datasets that include temporal sequences of 3D scans (i.e., 4D datasets), such as the *Binghamton University* 4D Facial Expression database (BU-4DFE) (Yin et al., 2008), the 4D dataset constructed at University of Central Lancashire (Hi4D-ADSIP) (Matuszewski et al., 2011, 2012), and the dynamic 3D FACS dataset (D3DFACS) for facial expression research (Cosker et al., 2011), which also includes fully coded FACS. This trend has been strengthened further by the

introduction of inexpensive acquisition devices, such as the consumer 3D cameras like Kinect or Asus (Kinect, 2010, Point grey, 2010, Asus, 2010), that provide fast albeit low-resolution streams of 3D data to a large number of users, thus opening new opportunities and challenges in 3D face recognition and facial expression recognition (Berretti et al., 2012, Li et al., 2013).

4.2 Expression Classification from *Static* (3D) Faces

Facial expression recognition has been extensively studied over the past decades especially in 2D domain (e.g., images and videos) resulting in a valuable enhancement. Existing approaches that address facial expression recognition can be divided into three categories: (1) *static* vs. *dynamic*; (2) *global* vs. *local*; (3) 2D vs. 3D. Most of the approaches are based on feature extraction/detection as a mean to represent and understand facial expressions. Pantic and Rothkrantz (Pantic and Rothkrantz, 2000) and Samal and Iyengar (Samal and Iyengar, 1992) presented a survey where they explored and compared different approaches that were proposed, since the mid 1970s, for facial expression analysis from either static facial images or image sequences. Whitehill and Omlin (Whitehill and Omlin, 2006) investigated on the Local versus Global segmentation for facial expression recognition. In particular, their study is based on the classification of action units (AUs), defined in the well-known Facial Action Coding System (FACS) manual by Ekman and Friesen (Ekman and Friesen, 1978), and designating the elementary muscle movements involved in the bio-mechanical of facial expressions. They reported, in their study on face images, that the local expression analysis showed no consistent improvement in recognition accuracy compared to the global analysis.

4.2.1 Related Work

As for 3D facial expression recognition, the first work related to this issue was presented by Wang et al. (Wang et al., 2006b). They proposed a novel geometric feature based facial expression descriptor, derived from an estimation of primitive surface feature distribution. A labeling scheme was associated with their extracted features, and they constructed samples that have been used to train and test several classifiers. They reported that the highest average recognition rate they obtained was 83%. They evaluated their approach not only on frontal-view facial expressions of the BU-3DFE database, but they also tested its robustness to non-frontal views. A second work was reported by Soyel and Demirel (Soyel and Demirel, 2007) on the same database. They extracted six characteristic distances between eleven facial landmarks, and using Neural Network architecture that analysis the calculated distances, they classified the BU-3DFE facial scans into 7 facial expressions including neutral expression. The average recognition rate they achieved was 91.3%. Mpiperis et al. (Mpiperis et al., 2008b) proposed a joint 3D face and facial expression recognition using bilinear model. They fitted both formulations, using symmetric and asymmetric bilinear models to encode both identity and expression. They reported an average recognition rate of 90.5%. They also reported that the facial expressions of disgust and surprise

were well identified with an accuracy of 100%. Tang and Huang (Tang and Huang, 2008b) proposed an automatic feature selection computed from the normalized Euclidean distances between two picked landmarks from 83 possible ones. Using regularized multi-class AdaBoost classification algorithm.

In this first approach, we further investigate the problem of 3D identity-independent facial expression recognition. The main contributions of our approach are the following: (1) We propose a new process for representing and extracting patches on the facial surface scan that cover multiple regions of the face; (2) We apply a framework to derive 3D shape analysis to quantify similarity measure between corresponding patches on different 3D facial scans. Thus, we combine a local geometric-based shape analysis approach of 3D faces and several machine learning techniques to perform such classification.

4.2.2 Shape Analysis of Local Patches

Most of the earlier work in 3D shape analysis use shape descriptors such as curvature, crest lines, shape index (e.g., ridge, saddle, rut, dome, etc.). These descriptors are defined based on the geometric and topological properties of the 3D object, and are used as features to simplify the representation and thus the comparison for 3D shape matching and recognition tasks. Despite their rigorous definition, such features are computed based on numerical approximation that involves second derivatives and can be sensitive to noisy data. In case of 3D facial range models, the facial surface labeling is a critical step to describe the facial behavior or expression, and a robust facial surface representation is needed. In Samir et al. (Samir et al., 2006) the authors proposed to represent facial surfaces by an indexed collections of 3D closed curves on faces. These curves are level curves of a surface distance function (i.e., geodesic distance) defined to be the length of the shortest path between a fixed reference point (taken to be the nose tip) and a point of the extracted curve along the facial surface. This being motivated by the robustness of the geodesic distance to facial expressions and rigid motions. Using this approach they were able to compare 3D shapes by comparing facial curves rather than comparing corresponding shape descriptors.

In this approach, we intend to further investigate on local shapes of the facial surface. We are especially interested in capturing deformations of local facial regions caused by facial expressions. Using a different solution, we compute iso-level curves using the Euclidean distance function (which is sensitive to deformations and thus can better capture differences related to variant expressions). To this end, we choose to consider N reference points (landmarks) $\{r_l\}_{1 \leq l \leq N}$ (Figure 4.1 (a)) and associated sets of level curves $\{c_{\lambda}^l\}_{1 \leq \lambda \leq \lambda_0}$ (Figure 4.1 (b)). These curves are extracted over the patches centered at these points. Here λ stands for the value of the distance function between the reference point r_l and the point belonging to the curve c_{λ}^l , and λ_0 stands for the maximum value taken by λ . Accompanying each facial model there are 83 manually picked landmarks, these landmarks are practically similar to the MPEG-4 feature points and are selected based on the facial anatomy structure. Given these points the feature region on the face can be easily determined and extracted. We were interested in a subset of 68 landmarks laying

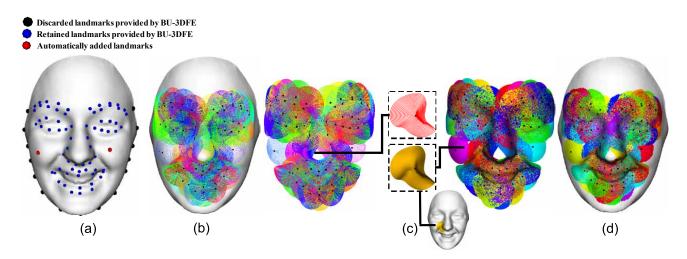


FIGURE 4.1: (a) 3D annotated facial shape model (70 landmarks); (b) 3D closed curves extracted around the landmarks; (c) 3D curve-based patches composed of 20 level curves with a size fixed by a radius $\lambda_0 = 20mm$; (d) Extracted patches on the face.

within the face area, discarding those marked on the face border. Contrary to the MPEG-4 feature points specification that annotates the cheeks center and bone, in BU-3DFE there were no landmarks associated with the cheek regions. Thus, we add two extra landmarks at both cheeks, obtained by extracting the middle point along the geodesic path between the mouth corner and the outside eye corner. We propose to represent each facial scan by a number of patches centered on the considered points. Let r_l be the reference point and P_l a given patch centered on this point and localized on the facial surface denoted by S. Each patch will be represented by an indexed collection of level curves. To extract these curves, we use the Euclidean distance function $||r_l - p||$ to characterize the length between r_l and any point p on S. Indeed, unlike the geodesic distance, the Euclidean distance is sensitive to deformations, and besides, it permits to derive curve extraction in a fast and simple way. Using this function we defined the curves as level sets of:

$$||r_l - .|| : c_{\lambda}^l = \{ p \in S \mid ||r_l - p|| = \lambda \} \subset S, \ \lambda \in [0, \lambda_0].$$
(4.1)

Each c_{λ}^{l} is a closed curve, consisting of a collection of points situated at an equal distance λ from r_{l} . The Fig. 4.1 resumes the scheme of patches extraction.

Once the patches are extracted, we aim at studying their shape and design a similarity measure between corresponding ones on different scans under different expressions. This is motivated by the common belief that people smile, or convey any other expression, the same way, or more appropriately certain regions taking part in a specific expression undergo practically the same dynamical deformation process. We expect that certain corresponding patches associated with the same given expression will be deformed in a similar way, while those associated with two different expressions will deform differently. The following sections describe the shape analysis of closed curves in \mathbb{R}^3 , initially introduced in (Joshi et al., 2007), and its extension to analyze shape of local patches on facial surfaces. We notice here that the shape analysis approach applied for curves here is different to the one described in Chapter 2, because of the closure constraint. For this reason, we shall describe in details in the following sections the shape analysis approach for closed curves and the extension to facial patches.

4.2.2.1 Shape Analysis of 3D Closed Curves

We start by considering a closed curve β in \mathbb{R}^3 . While there are several ways to analyze shapes of closed curves, an elastic analysis of the parametrized curves is particularly appropriate in 3D curves analysis. This is because (1) such analysis uses a square-root velocity function representation which allows us to compare local facial shapes in presence of elastic deformations, (2) this method uses a square-root representation under which the elastic metric reduces to the standard \mathbb{L}^2 metric and thus simplifies the analysis, (3) under this metric the Riemannian distance between curves is invariant to the re-parametrization. To analyze the shape of β , we shall represent it mathematically using a square-root representation of β (as described in Chapter 2) as follows ; for an interval I = [0, 1], let $\beta : I \longrightarrow \mathbb{R}^3$ be a curve and define $q : I \longrightarrow \mathbb{R}^3$ to be its square-root velocity function (SRVF), given by:

$$q(t) \doteq \dot{\beta}(t) / \sqrt{\|\dot{\beta}(t)\|} . \tag{4.2}$$

Here t is a parameter $\in I$ and $\|.\|$ is the Euclidean norm in \mathbb{R}^3 . We note that q(t) is a special function that captures the shape of β and is particularly convenient for shape analysis, as we describe next. The classical elastic metric for comparing shapes of curves becomes the \mathbb{L}^2 -metric under the SRVF representation (Srivastava et al., 2011). This point is very important as it simplifies the calculus of elastic metric to the well-known calculus of functional analysis under the \mathbb{L}^2 -metric. Also, the squared \mathbb{L}^2 -norm of q, given by: $\|q\|^2 = \int_{\mathbb{S}^1} \langle q(t), q(t) \rangle dt = \int_{\mathbb{S}^1} \|\dot{\beta}(t)\| dt$, which is the length of β . In order to restrict our shape analysis to closed curves, we define the set: $\mathcal{C} = \{q : \mathbb{S}^1 \longrightarrow \mathbb{R}^3 | \int_{\mathbb{S}^1} q(t) || q(t) || dt = 0\} \subset \mathbb{L}^2(\mathbb{S}^1, \mathbb{R}^3)$. Notice that the elements of \mathcal{C} are allowed to have different lengths. Due to a non-linear (closure) constraint on its elements, \mathcal{C} is a non-linear manifold. We can make it a Riemannian manifold by using the metric: for any $u, v \in T_q(\mathcal{C})$, we define:

$$\langle u, v \rangle = \int_{\mathbb{S}^1} \langle u(t), v(t) \rangle dt$$
 (4.3)

So far we have described a set of closed curves and have endowed it with a Riemannian structure. Next we consider the issue of representing the *shapes* of these curves. It is easy to see that several elements of C can represent curves with the same shape. For example, if we rotate a curve in \mathbb{R}^3 , we get a different SRVF but its shape remains unchanged. Another similar situation arises when a curve is re-parametrized; a re-parameterization changes the SRVF of curve but not its shape. In order to handle this variability, we define orbits of the rotation group SO(3) and the re-parameterization group Γ as the equivalence classes in C. Here, Γ is the set of all orientation-preserving diffeomorphisms of \mathbb{S}^1 (to itself) and the elements of Γ are viewed as re-parameterization functions. For example, for a curve $\beta : \mathbb{S}^1 \to \mathbb{R}^3$ and a function $\gamma : \mathbb{S}^1 \to \mathbb{S}^1, \ \gamma \in \Gamma$, the curve $\beta \circ \gamma$ is a re-parameterization of β . The corresponding SRVF changes according to $q(t) \mapsto \sqrt{\dot{\gamma}(t)}q(\gamma(t))$. We set the elements of the orbit:

$$[q] = \{\sqrt{\dot{\gamma}(t)} Oq(\gamma(t)) | O \in SO(3), \quad \gamma \in \Gamma\} , \qquad (4.4)$$

to be equivalent from the perspective of shape analysis. The set of such equivalence classes, denoted by $S \doteq C/(SO(3) \times \Gamma)$ is called the *shape space* of closed curves in \mathbb{R}^3 . S inherits a Riemannian metric from the larger space C due to the quotient structure.

The main ingredient in comparing and analysing shapes of curves is the construction of a geodesic between any two elements of S, under the Riemannian metric given in Eq.(4.3). Given any two curves β_1 and β_2 , represented by their SRVFs q_1 and q_2 , we want to compute a geodesic path between the orbits $[q_1]$ and $[q_2]$ in the shape space S. This task is accomplished using a *path-straightening approach* which was introduced in (Klassen and Srivastava, 2006). The basic idea here is to connect the two points $[q_1]$ and $[q_2]$ by an arbitrary initial path α and to iteratively update this path using the negative gradient of an energy function $E[\alpha] = \frac{1}{2} \int_{S} \langle \dot{\alpha}(s), \dot{\alpha}(s) \rangle ds$. The interesting part is that the gradient of E has been derived analytically and can be used directly for updating α . As shown in (Klassen and Srivastava, 2006), the critical points of E are actually geodesic paths in S. Thus, this gradient-based update leads to a critical point of E which, in turn, is a geodesic path between the given points. In the remainder of this section, we will use the notation $d_{S}(\beta_1, \beta_2)$ to denote the length of the geodesic in the *shape space* S between the orbits q_1 and q_2 , to reduce the notation.

4.2.2.2 Shape Analysis of 3D Facial Patches

Now, we extend ideas developed in the previous section from analyzing shapes of curves to the shapes of patches. As mentioned earlier, we are going to represent a number of l patches of a facial surface S with an indexed collection of the level curves of the $||r_l - .||$ function (Euclidean distance from the reference point r_l). That is, $P_l \leftrightarrow \{c_{\lambda}^l, \lambda \in [0, \lambda_0]\}$, where c_{λ}^l is the level set associated with $||r_l - .|| = \lambda$. Through this relation, each patch has been represented as an element of the set $S^{[0,\lambda_0]}$. In our framework, the shapes of any two patches are compared by comparing their corresponding level curves. Given any two patches P_1 and P_2 , and their level curves $\{c_{\lambda}^1, \lambda \in [0, \lambda_0]\}$ and $\{c_{\lambda}^2, \lambda \in [0, \lambda_0]\}$, respectively, our idea is to compare the patches curves c_{λ}^1 and c_{λ}^2 , and to accumulate these differences over all λ . More formally, we define a distance $d_{S^{[0,\lambda_0]}}$ given by:

$$d_{\mathcal{S}^{[0,\lambda_0]}}(P_1, P_2) = \int_0^L d_{\mathcal{S}}(c_\lambda^1, c_\lambda^2) d\lambda .$$

$$(4.5)$$

In addition to the distance $d_{\mathcal{S}^{[0,\lambda_0]}}(P_1, P_2)$, which is useful in biometry and other classification experiments, we also have a geodesic path in $\mathcal{S}^{[0,\lambda_0]}$ between the two points represented by P_1 and P_2 . This



FIGURE 4.2: Examples of intra-class (same expression) geodesic paths with shape and mean curvature mapping between corresponding patches.

geodesic corresponds to the optimal elastic deformations of facial curves and, thus, facial surfaces from one to another. Figure 4.2 shows some examples of geodesic paths that are computed between corresponding patches associated with shape models sharing the same expression, and termed *intra-class geodesics*. In the first column we illustrate the source, which represents scan models of the same subject, but under different expressions. The third column represents the targets as scan models of different subjects. As for the middle column, it shows the geodesic paths. In each row we have both the shape and the mean curvature mapping representations of the patches along the geodesic path from the source to the target. The mean curvature representation is added to identify concave/convex areas on the source and target patches and equally-spaced steps of geodesics. This figure shows that certain patches, belonging to the same class of expression, are deformed in a similar way. In contrast, Figure 4.3 shows geodesic paths between patches of different facial expressions. These geodesics are termed *inter-class geodesics*. Unlike the intra-class geodesics shown in Figure 4.2, these patches deform in a different way.

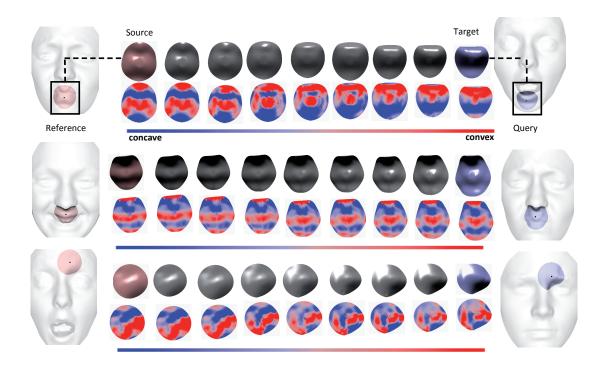


FIGURE 4.3: Examples of inter-class (different expressions) geodesic paths between source and target patches.

4.2.3 Facial Expression Classification

In order to classify expressions, we build a feature vector for each facial scan. Given a candidate facial scan of a person j, facial patches are extracted around facial landmarks. For a facial patch P_{j}^{i} , a set of level curves $\{c_{\lambda}\}_{j}^{i}$ are extracted centered on the i^{th} landmark. Similarly, a patch P_{ref}^{i} is extracted in correspondence to landmarks of a reference scans ref. The length of the geodesic path between each level curve and its corresponding curve on the reference scan are computed using a Riemannian framework for shape analysis of 3D curves (see Sections 4.2.2.1 and 4.2.2.2). The shortest path between two patches at landmark i, one in a candidate scan and the other in the reference scan, is defined as the sum of the distances between all pairs of corresponding curves in the two patches as indicated in Eq. (4.5). The feature vector is then formed by the distances computed on all the patches and its dimension is equal to the number of used landmarks N = 70 (i.e., 68 landmarks are used out of the 83 provided by BU-3DFED and the two additional check points). The i^{th} element of this vector represents the length of the geodesic path that separates the relative patch to the corresponding one on the reference face scan. All feature vectors computed on the overall dataset will be labeled and used as input data to machine learning algorithms such as Multi-boosting and SVM, where Multi-boosting is an extension of the successful Adadoost technique for forming decision committees.

4.2.4 Experimental Results

To investigate facial expression recognition, we have applied our proposed approach on a dataset that is appropriate for this task. In this Section, we describe the experiments, obtained results and comparisons with related work.

I. Database Description and Experimental Setting: BU-3DFE is one of the very few publicly available databases of annotated 3D facial expressions, collected by Yin et al. (Yin et al., 2006b) at Binghamton University. It was designed for research on 3D human face and facial expression and to develop a general understanding of the human behavior. Thus the BU-3DFE database is beneficial for several fields and applications dealing with human computer interaction, security, communication, psychology, etc. There are a total of 100 subjects in the database, 56 females and 44 males. A neutral scan was captured for each subject, then they were asked to perform six expressions namely: Happiness (HA), Anger (AN), Fear (FE), Disgust (DI), Sad (SA) and Surprise (SU). The expressions vary according to four levels of intensity (low, middle, high and highest or 01-04). Thus, there are 25 3D facial expression models per subject in the database. A set of 83 manually annotated facial landmarks is associated to each model. These landmarks are used to define the regions of the face that undergo to specific deformations due to single muscles movements when conveying facial expression (Ekman and Friesen, 1978). In Figure 4.4, we illustrate examples of the six universal facial expressions 3D models including the highest intensity level.

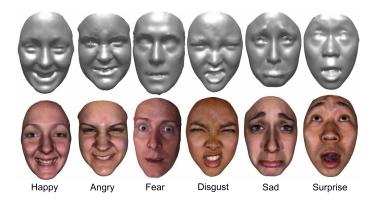


FIGURE 4.4: Examples of 3D facial expression models (first row 3D shape models, second row 3D textured models) of the BU-3DFE database.

For the goal of performing identity-independent facial expression recognition, the experiments were conducted on the BU-3DFE static database. A dataset captured from 60 subjects were used, half (30) of them were female and the other half (30) were male, corresponding to the high and highest intensity levels 3D expressive models (03-04). These data are assumed to be scaled to the true physical dimensions of the captured human faces. Following a similar setup as in (Gong et al., 2009b), we randomly divided the 60 subjects into two sets, the training set containing 54 subjects (648 samples), and the test set containing 6 subjects (72 samples). To drive the classification experiments, we arbitrarily choose a set of six reference subjects with its six basic facial expressions. We point out that the selected reference scans do not appear neither in the training nor in the testing set.

II. Discussions of the Results: Using the Waikato Environment for Knowledge Analysis (Weka) (Hall et al., 2009), we applied the Multiboost algorithm with three weak classifiers, namely, Linear Discriminant Analysis (LDA), Naive Bayes (NB), and Nearest Neighbor (NN), to the extracted features, and we achieved average recognition rates of 98.81%, 98.76% and 98.07%, respectively. We applied the SVM linear classifier as well, and we achieved an average recognition rate of 97.75%. We summarize the resulting recognition rates in Table 4.1.

TABLE 4.1: Classification results using local shape analysis and several classifiers.

| Classifier | Multiboost-LDA | Multiboost-NB | Multiboost-NN | SVM-Linear |
|------------------|------------------------|---------------|---------------|------------|
| Recognition rate | $\boldsymbol{98.81\%}$ | 98.76% | 98.07% | 97.75% |

We note that these rates are obtained by averaging the results of the 10 independent and arbitrarily run experiments (10-fold cross validation) and their respective recognition rate obtained using the Multiboost-LDA classifier. We note that different selections of the reference scans do not affect significantly the recognition results and there is no large variations in recognition rates values. The reported results represent the average over the six runned experiments. The Multiboost-LDA classifier achieves the highest recognition rate and shows a better performance in terms of accuracy than the other classifiers. This is mainly due to the capability of the LDA-based classifier to transform the features into a more discriminative space and, consequently, result in a better linear separation between facial expression classes.

The average confusion matrix relative to the best performing classification using Multiboost-LDA is given in Table 4.2.

| % | AN | DI | \mathbf{FE} | HA | SA | SU |
|----|-------|-------|---------------|-------|-------|-------|
| AN | 97.92 | 1.11 | 0.14 | 0.14 | 0.69 | 0.0 |
| DI | 0.56 | 99.16 | 0.14 | 0.0 | 0.14 | 0.0 |
| FE | 0.14 | 0.14 | 99.72 | 0.0 | 0.0 | 0.0 |
| HA | 0.56 | 0.14 | 0.0 | 98.60 | 0.56 | 0.14 |
| SA | 0.28 | 0.14 | 0.0 | 0.0 | 99.30 | 0.28 |
| SU | 0.14 | 0.56 | 0.0 | 0.0 | 1.11 | 98.19 |

TABLE 4.2: Average confusion matrix given by Multiboost-LDA classifier.

In order to better understand and explain the results mentioned above, we apply the Multiboost algorithm on feature vectors built from distances between patches for each class of expression. In this case, we consider these features as weak classifiers. Then, we look at the early iterations of the Multiboost algorithm and the selected patches in each iteration.

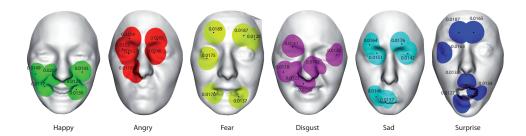


FIGURE 4.5: Selected patches at the early few iterations of Multiboost classifier for the six facial expressions (Angry, Disgust, Fear, Happy, Sadness, Surprise) with their associated weights.

Figure 4.5 illustrates for each class of expression the most relevant patches. Notice that, for example, for the Happy expression the selected patches are localized in the lower part of the face, around the mouth and the chin. As for the Surprise expression, we can see that most relevant patches are localized around the eyebrows and the mouth region. It can be seen that patches selected for each expression lie on facial muscles that contribute to this expression.

III. Comparison with Related Work: In Table 4.3 results of our approach are compared against those reported in (Tang and Huang, 2008b), (Soyel and Demirel, 2007), and (Wang et al., 2006b), on the same experimental setting (54-versus-6-subject partitions) of the BU-3DFE database. The differences between approaches should be noted: Tang et al. (Tang and Huang, 2008b) performed automatic feature selection using normalized Euclidean distances between 83 landmarks, Soyel et al. (Soyel and Demirel, 2007) calculated six distances using a distribution of 11 landmarks, while Wang et al. (Wang et al., 2006b) derived curvature estimation by locally approximating the 3D surface with a smooth polynomial function. In comparison, our approach capture the 3D shape information of local facial patches to derive shape analysis. For assessing how the results of their statistical analysis will generalize to an independent dataset, in (Wang et al., 2006b) a 20-fold cross-validation technique was used, while in (Tang and Huang, 2008b) and (Soyel and Demirel, 2007) the authors used 10-fold cross-validation to validate their approach.

| Method | 10-fold Average Recognition Rate $(\%)$ | 20-fold ARR (%) |
|---------------------------|---|-----------------|
| (Wang et al., 2006b) | | 83.6% |
| (Tang and Huang, 2008b) | 95.1% | |
| (Tang and Huang, 2008b) | 95.1% | |
| (Soyel and Demirel, 2007) | 91.3% | |
| (Maalej et al., 2011) | 98.81% | 92.75% |

TABLE 4.3: Comparison of this work with respect to previous work (Tang and Huang, 2008b), (Soyel and Demirel, 2007) and (Wang et al., 2006b).

IV. Impact of Head Pose Variation: In real world situations, frontal view facial scans may not be always available. Thus, non-frontal view facial expression recognition is a challenging issue that needs to be treated. We were interested in evaluating our approach on facial scan under large pose variations. By rotating the 3D shape models in the y-direction, we generate facial scans under six different non-frontal views corresponding to 15° , 30° , 45° , 60° , 75° and 90° rotation. We assume that shape information is

unavailable for the occluded facial regions due to the face pose. For each view, we perform facial patches extraction around the visible landmarks in the given scan. In cases where a landmark is occluded, or where the landmark is visible, but the region nearby is partially occluded, we treat it as a missing data problem for all faces sharing this view. In these cases, we are not able to compute the geodesic path between corresponding patches. The corresponding entries in the distance matrix are blank and we fill them using an imputation technique (Batista and Monard, 2003). In our experiments we employed the mean imputation method, which consists of replacing the missing values by the means of values already calculated in frontal-view scenario obtained from the training set. Let $d_{ijk} = d_{S^{[0,\lambda_0]}}(P_i^k, P_j^k)$ be the geodesic distance between the k^{th} patch belonging to subjects *i* and *j* ($i \neq j$). In case of frontal view (*fv*), the set of instances X_i^{fv} relative to the subject *i* need to be labeled and is given by:

$$\mathbf{X}_{\mathbf{i}}^{\mathbf{fv}} = \begin{pmatrix} d_{i11} & \dots & d_{i1k} & \dots & d_{i1N} \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ d_{ij1} & \dots & d_{ijk} & \vdots & d_{ijN} \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ d_{iJ1} & \dots & d_{iJk} & \dots & d_{iJN} \end{pmatrix}$$

where N is the number of attributes. In case of non-frontal view (nfv), if an attribute k is missing, we replace the k^{th} column vector in the distance matrix X_i^{nfv} by the mean of geodesic distances computed in the frontal-view case, with respect to the k^{th} attribute and given by: $m_k^{fv} = \frac{\sum_{j=1}^J d_{ijk}}{J}$, where J is the total number of instances.

$$\mathbf{X_{i}^{nfv}} = \begin{pmatrix} d_{i11} & \dots & m_{k}^{fv} & \dots & d_{i1N} \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ d_{ij1} & \dots & m_{k}^{fv} & \vdots & d_{ijN} \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ d_{iJ1} & \dots & m_{k}^{fv} & \dots & d_{iJN} \end{pmatrix}$$

To evaluate the robustness of our approach in a context of non-frontal views, we derive a view-independent facial expression recognition. Error recognition rates are evaluated throughout different testing facial views using the four classifiers trained only on frontal-view facial scans. Figure 4.6 shows the average error rates of the four classification methods. The Multiboost-LDA shows the best performance for facial expression classification on the chosen database. From the figure, it can be observed that the average error rates increase with the rotation angle (values from 0 to 90 degrees of rotation are considered), and the Multiboost-LDA is the best performing methods also in the case of pose variations. As shown in this figure, recognition accuracy remains acceptable, even only 50% of data (half face) are available when we rotate the 3D face by 45 degree in y-direction.

In this section we presented a novel approach for identity-independent facial expression recognition from 3D facial shapes. Our idea was to describe the change in facial expression as a deformation in the vicinity of facial patches in 3D shape scan. An automatic extraction of local curve based patches

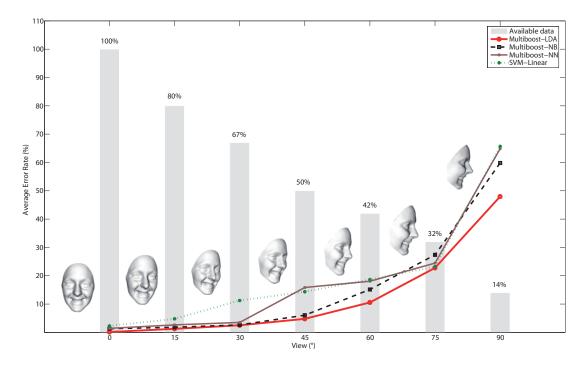


FIGURE 4.6: The average error rates of six expressions with different choice of views corresponding to the best reference and using different classifiers.

within the 3D facial surfaces was proposed. These patches were used as local shape descriptors for facial expression representation. A Riemannian framework was applied to compute the geodesic path between corresponding patches. Qualitative (inter and intra-geodesic paths) and quantitative (geodesic distances) measures of the geodesic path were explored to derive shape analysis. The geodesic distances between patches were labeled with respect to the six prototypical expressions and used as samples to train and test machine learning algorithms. Using Multiboost algorithm for multi-class classification, we achieved a 98.81% average recognition rate for six prototypical facial expressions on the BU-3DFE database. We demonstrated the robustness of the proposed method to pose variations. In fact, the obtained recognition rate remain acceptable (over 93%) even half of the facial scan is missed.

The major limitation of the approach presented in this section is that the 68 landmarks we used to define the facial patches were manually labeled. Several studies were interested detecting and tracking facial feature points, as proposed in (Gupta et al., 2010), (Sun et al., 2010b), for automatic 3D facial expression recognition. We will adopt a different approach (landmark-free) for the analysis of dynamic flows of facial surfaces.

4.3 Expression Classification from 3D Dynamic (4D) Faces

In his study, Ekman also showed that facial expressions can be coded through the movement of face points (temporal evolution of the face) as described by a set of **action units** (Ekman and Friesen, 1977).

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These results, in turn, inspired many researchers to analyze facial expressions in video data, by tracking facial features and measuring the amount of facial movements in video frames (Zeng et al., 2009). This body of work demonstrates a collective knowledge that facial expressions are highly dynamical processes, and looking at sequences of face instances can help to improve the recognition performance. We further emphasize that, rather than being just a static or dynamic 2D image analysis, it is more natural to analyze expressions as spatio-temporal deformations of 3D faces, caused by the actions of facial muscles. In this approach, the facial expressions can be studied comprehensively by analyzing temporal dynamics of 3D face scans (3D plus time is often regarded as 4D data). From this perspective the relative immunity of 3D scans to lighting conditions and pose variations give support for the use of 3D and 4D data. Motivated by these considerations, there has been a progressive shift from 2D to 3D in performing facial shape analysis for recognition (Chapter 3), and expression recognition as described in Section 4.2. In particular, this latter research subject is gaining momentum thanks to the recent availability of public 3D datasets, like the *Binghamton University* 3D Facial Expression database (BU-3DFE) (Yin et al., 2006a), and the *Bosphorus* 3D Face Database (Savran et al., 2008).

At the same time, advances in 3D imaging technology (Di3D, 2006, 3DMD, 2010) have permitted collections of large datasets that include temporal sequences of 3D scans (i.e., 4D datasets), such as the Binghamton University 4D Facial Expression database (BU-4DFE) (Yin et al., 2008), the 4D dataset constructed at University of Central Lancashire (Hi4D-ADSIP) (Matuszewski et al., 2011, 2012), and the dynamic 3D FACS dataset (D3DFACS) for facial expression research (Cosker et al., 2011), which also includes fully coded FACS. This trend has been strengthened further by the introduction of inexpensive acquisition devices, such as the consumer 3D cameras like Kinect or Asus (Kinect, 2010, Point grey, 2010, Asus, 2010), that provide fast albeit low-resolution streams of 3D data to a large number of users, thus opening new opportunities and challenges in 3D face recognition and facial expression recognition (Berretti et al., 2012, Li et al., 2013). Motivated by these facts, we focus in this section on the problem of expression recognition from dynamic sequences of 3D facial scans. We propose a new framework for temporal analysis of 3D faces that combines scalar fields modeling of face deformations with effective classifiers. To motivate our solution and to relate it to the state of the art, next we provide an overview of existing methods for 4D facial expression recognition (see also the recent work in (Sandbach et al., 2012b) for a comprehensive survey on this subject), then we give a general overview of our approach.

4.3.1 Related Work

The use of 4D data for face analysis is still at the beginning, with just a few works performing face recognition from sequences of 3D face scans (Li et al., 2013, Benedikt et al., 2008, 2010), and some works focussing on facial expression recognition. In particular, the first approach addressing the problem of facial expression recognition from dynamic sequences of 3D scans was proposed by Sun et al. (Sun et al., 2010a, Sun and Yin, 2008). Their approach basically relies on the use of a generic deformable 3D model

whose changes are tracked both in space and time in order to extract a spatio-temporal description of the face. In the temporal analysis, a vertex flow tracking technique is applied to adapt the 3D deformable model to each frame of a 3D face sequence, and the vertex flow estimation is derived by establishing pointto-point correspondences between 3D meshes based on a conformal mapping approach. Correspondences between vertices across the 3D dynamic facial sequences provide a set of motion trajectories (vertex flow) of 3D face scans. Consequently, the vertex flow can be depicted on the adapted generic model (tracking model) through the estimation of the displacement vector from the tracked points of the current frame to the corresponding points of the first frame (assumed to have a neutral expression). A facial motion vector is then obtained to describe the dynamics of facial expression across a 3D frame sequence. In the spatial analysis, an automatic surface labelling approach is applied on the tracked locations of the depth models in order to classify the 3D primitive surface features into eight basic categories. As a result, each depth scan in the sequence can be represented by a spatio-temporal feature vector that describes both shape and motion information and provides a robust facial surface representation. Once spatio-temporal features are extracted, a two-dimensional Hidden Markov Model (HMM) is used for classification. In particular, a spatial HMM and a temporal HMM were used to model the spatial and temporal relationships between the extracted features. Exhaustive analysis was performed on the BU-4DFE database. The main limit of this solution resides in the use of the 83 manually annotated landmarks of the BU-4DFE that are not released for public use. The approach proposed by (Sandbach et al., 2011) exploits the dynamics of 3D facial movements to analyze expressions. This is obtained by first capturing motion between frames using Free-Form Deformations and extracting motion features using a quad-tree decomposition of several motion fields. GentleBoost classifiers are used in order to simultaneously select the best features to use and perform the training using two classifiers for each expression: one for the onset temporal segment, and the other for the offset segment. Then, HMMs are used for temporal modeling of the full expression sequence, which is represented as the composition of four temporal segments, namely, neutral, onset, apex, offset. These model a sequence with an initial neutral segment followed by the activation of the expression, the maximum intensity of the expression, deactivation of the expression and closing of the sequence again with a neutral expression. Experiments were reported for three prototypical expressions (i.e., happy, angry and surprise) of the BU-4DFE database. An extension of this work has been presented in (Sandbach et al., 2012b), where results on the BU-4DFE database using the six universal facial expressions are reported. In (Le et al., 2011) a level curve based approach is proposed to capture the shape of 3D facial models. The level curves are parameterized using the arclength function. The Chamfer distance is applied to measure the distances between the corresponding normalized segments, partitioned from these level curves of two 3D facial shapes. These features are then used as spatio-temporal features to train HMM, and since the training data were not sufficient for learning HMM, the authors proposed to apply the universal background modeling to overcome the over-fitting problem. Results were reported for the happy, sad and surprise sequences of the BU-4DFE database. Fang et al. (Fang et al., 2011) propose a fully automatic 4D facial expression recognition approach with a particular emphasis on 4D data registration and dense correspondence between 3D meshes along the temporal line. The variant of the Local Binary Patterns (LBP) descriptor proposed in (Zhao and Pietikäinen, 2007), which computes

LBP on three orthogonal planes is used as face descriptor along the sequence. Results are provided on the BU-4DFE database for all expressions and for the subsets of expressions used in (Sandbach et al., 2011) and (Le et al., 2011), showing improved results with respect to competing solutions. In (fan, 2012), the same authors propose a similar methodology for facial expression recognition from dynamic sequences of 3D scans, with an extended analysis and comparison of different 4D registration algorithms, including ICP and more sophisticated mesh matching algorithms, as Spin Images and MeshHOG. However, 12 manually annotated landmarks were used in this study. Recently, Reale et al. (Reale et al., 2013) have proposed a new 4D spatio-temporal feature named *Nebula* for facial expressions and movement analysis from a volume of 3D data. After fitting the volume data to a cubic polynomial, a histogram is built for different facial regions using geometric features, as curvatures and polar angles. They have conducted several recognition experiments on the BU-4DFE database for posing expressions, and on a new database published in (Zhang et al., 2013) for spontaneous expressions. However, manual intervention is used to detect the onset frame and just 15 frames from the onset one are used for classification, and these frames correspond to the most intense expression.

From the discussion above, it becomes clear that solutions specifically tailored for 4D facial expression recognition from dynamic sequences are still preliminary, being semi-automatic, or are capable of discriminating between only a subset of expressions.

4.3.2 Geometric Facial Deformation

The elastic Riemannian metric used in our methodology provides a physical interpretation of measuring deformations between facial curves using a combination of stretching and bending. These elastic deformations are captured by the Dense Scalar Fields used for expression classifications.

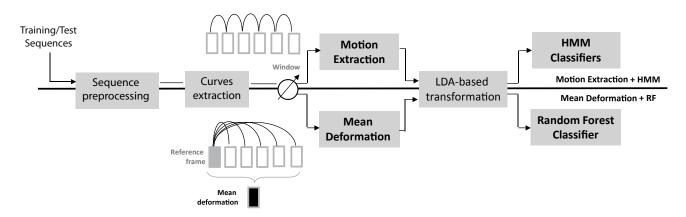


FIGURE 4.7: Overview of the proposed approach. Four main steps are shown: Sequence preprocessing and extraction of the radial curves; Motion extraction and Mean deformation computation; Dimensionality reduction with LDA; HMM- and Random-Forest-based classification. Note that both train and test sequences can go through the upper and lower path in the block-diagram.

Based on these premises, in this work we propose an automatic approach for facial expression recognition that exploits the facial deformations extracted from 3D facial videos. An overview of the proposed approach is given in Figure 4.7. In the preprocessing step, the 3D mesh in each frame is first aligned to the previous one and then cropped. From the obtained subsequence, the 3D deformation is captured based on a Dense Scalar Fields (DSFs) that represents the 3D deformation between two frames. Linear Discriminant Analysis (LDA) is used to transform derived feature space to an optimal compact space to better separate different expressions. Finally, the expression classification is performed in two ways: (1) using the HMM models for temporal evolution; and (2) using mean deformation along a window with Random Forest classifier. Experimental results show that the proposed approaches are capable of improving the state of art performance on the BU-4DFE database. There are three main contributions in this work,

- ↔ Novel Dense Scalar Fields (DSFs) defined on radial curves of 3D faces using Riemannian analysis in shape spaces of curves. These scalar fields accurately capture deformations occurring between 3D faces represented as collections of radial curves;
- ↔ A new approach for facial expression recognition from 3D dynamic sequences, that combines the high descriptiveness of DSFs extracted from successive 3D scans of a sequence with the discriminant power of LDA features using HMM and multi-class Random Forest;
- \hookrightarrow An extensive experimental evaluation that compares the proposed solution with the state of the art methods using a common dataset and testing protocols. Results show that our approach outperforms the published state of the art results.

One basic idea to capture facial deformations across 3D video sequences is to track mesh vertices densely along successive 3D frames. Since, as the resolution of the meshes varies across 3D video frames, establishing a dense matching on consecutive frames is necessary. For this purpose, (Sun and Yin, 2008) proposed to adapt a generic model (a tracking model) to each 3D frame using a set of 83 predefined facial landmarks to control the adaptation based on radial basis functions. The main limitation of this approach is that the 83 landmarks are manually annotated in the first frame of each sequence. Moreover, the adaptation decreases the accuracy of expression recognition when emotions are manifested by subtle changes of the face. A second solution is presented by (Sandbach et al., 2012a, 2011), where the authors used an existing non-rigid registration algorithm (FFD) (Rueckert et al., 1999a) based on B-splines interpolation between a lattice of control points. In this case, dense matching is a preprocessing step used to estimate a motion fields between 3D frames t and t-1. The problem of quantifying subtle deformations along the sequence still remains a challenging task, and the results presented in (Sandbach et al., 2011) are limited to just three facial expressions: happy, angry and surprise. In order to capture and model deformations of the face induced by different facial expressions, we propose to represent the facial surface through a set of parameterized radial curves that originate from the tip of the nose. Approximating the facial surface by an ordered set of radial curves, which locally captures its shape can be seen as a

parameterization of the facial surface. Indeed, similar parameterizations of the face have shown their effectiveness in facial biometrics (Drira et al., 2010a). The mathematical setup for the shape theory offered here comes from Hilbert space analysis (refer to Chapter 2 for DSFs computation).

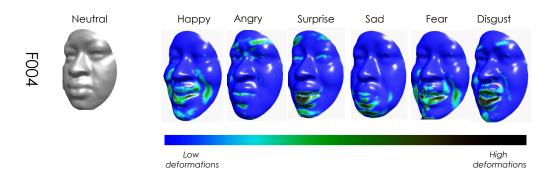


FIGURE 4.8: Optimal deformations (represented by the DFSs) computed between a neural face (on the left) and six apex (maximum expression) frames taken from the BU-4DFE database, each represent one expression from the set (happy, angry, surprise, sad, fear and disgust).

In our experiments, we represent each face with 100 radial curves, and T=50 sampled points on each curve, so that the DSFs between two 3D faces is expressed by a 5000-dimensional feature vector. In Figure 4.8 examples of the deformation fields computed between a neutral face of a given subject and the apex frames of the sequences of the six universal expressions of the same subject are shown. The values of the scalar fields to be applied on the neutral face to convey the six different prototypical expressions are reported using a color scale (blue to black). In particular, colors from green to black represent the highest deformations, whereas the lower values of the dense scalar fields are represented in cyan/blue. As it can be observed, for different expressions, the high deformations are located in different regions of the face. For example, as intuitively expected, the corners of the mouth and the cheeks are mainly deformed for happiness expression, whereas the eyebrows are also strongly deformed for the angry and disgust expressions.

In order to highlight the benefits of the proposed DSFs against other methods for extracting dense deformation features, we selected the Free-Form Deformation approach, which has been originally defined in Rueckert et al. (Rueckert et al., 1999b) for medical images, and later on successfully applied to the problem of 3D dynamic facial expression recognition by (Sandbach et al., 2012a, 2011). In particular, FFD is a method for non-rigid registration based on B-spline interpolation between a lattice of control points. In addition, we also compared our approach with respect to a baseline solution, which uses the point-to-point Euclidean distance between frames of a sequence. Figure 4.9 reports the results for an example case, where a frame of a happy sequence is deformed with respect to the first frame of the sequence. The figure shows quite clearly as the DSFs proposed in this work is capable to capture the face deformations with smooth variations that include, in the example, the mouth, the chin and the cheeks.

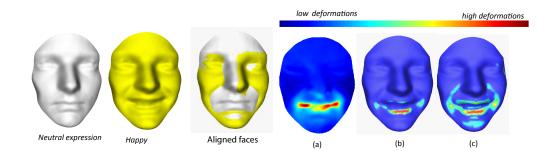


FIGURE 4.9: Capturing the facial deformations between a neutral face and an expressive face trough three methods: (a) the Free Form-based Deformations (FFD); (b) the point-to-point Euclidean distances; and (c) the DSFs deformations.

4.3.3 Expression Recognition using DSFs

Deformations due to facial expressions across 3D video sequences are characterized by subtle variations induced mainly by the motion of facial points. These subtle changes are important to perform effective expression recognition, but they are also difficult to be analyzed due to the face movements. To handle this problem, as described in the previous section, we propose a curve-based parametrization of the face that consists in representing the facial surface by a set of radial curves. According to this representation, the problem of comparing two facial surfaces, a reference facial surface and a target one, is reduced to the computation of the DSFs between them. In order to make possible to enter the expression recognition system at any time and make the recognition process possible from any frame of a given video, we consider subsequences of n frames. Thus, we chose the first n frames as the first subsequence. Then, we chose n-consecutive frames starting index of the sequence every one frame till the end of the sequence. In order to classify the resulting subsequences, we propose two different feature extraction and classification framework based on the DSFs:

- \hookrightarrow Mean Deformation-based features associated to Random Forest classifier. The first frame of the subsequence is considered as a reference frame and the deformation is calculated from each of the remaining frames to the first one using the DSFs. The average deformation of the *n*-1 resulting DSFs represents the feature vector in this classification scheme and is presented, after dimensionality reduction, to multi-class Random Forest classifiers;
- ↔ 3D Motion features combined with HMM classifiers. The deformation between successive frames in a subsequence are calculated using the DSFs and presented to an HMM classifier preceded by LDA-based dimensionality reduction.

In the following, we shall describe the dynamic features derived from the DSFs.

4.3.3.1 Mean Shape Deformation with the Random Forest Classifier

The idea here is to capture a mean deformation of the face in the sliding window on the 3D expression sequence. In order to get this feature, the first frame of each subsequence is considered as the reference one, and the dense deformation is computed from this frame to each of the remaining frames of the subsequence. Let F_{ref} denote the reference frame of a subsequence and F_i the *i*-th successive frame in the subsequence; the successive frame, for example, is denoted by F_1 . The DSFs is calculated between F_{ref} and F_i , for different values of i (i = 1, ..., n - 1), and the mean deformation is then given by:

$$\overline{DSF} = \frac{1}{n-1} \sum_{i=1}^{n-1} DSF(F_{ref}, F_i).$$

$$(4.6)$$

Figure 4.10 illustrates one subsequence for each expression with n = 6 frames. Each expression is illustrated in two rows: The upper row gives the reference frame of the subsequence and the *n*-1 successive frames of the subsequences. Below, the corresponding Dense Scalar Fields computed for each frame are shown. The mean deformation fields is reported on the right of each plot and represents the feature vector for each subsequence. The feature vector for this subsequence is built based on the mean deformation of the *n*-1 calculated deformations. Thus, each subsequence is represented by a feature vector of size equal to the number of points on the face (i.e., the number of points used to sample the radial curves of the face). In order to provide a visual representation of the scalar fields, an automatic labeling scheme is applied: Warm colors (red, yellow) are associated with high $DSF(F_{ref}, F_t)$ values and correspond to facial regions affected by high deformations. Cold colors are associated with regions of the face that remain stable from one frame to another. Thus, this dense deformation fields summarize the temporal changes of the facial surface when a particular facial expression is conveyed.

According to this representation, the deformation of each subsequence is captured by the mean \overline{DSF} defined in Eq. (4.6). The main motivation for using the mean deformation, instead of the maximum deformation for instance, is related to its greater robustness to the noise. In the practice, the mean deformation resulted more resistant to deformations due to, for example, inaccurate nose tip detection or the presence of acquisition noise. In Figure 4.10, for each subsequence, the mean deformation fields illustrate a smoothed pattern better than individual deformation fields in the same subsequence. Since the dimensionality of the feature vector is high, we use LDA-based transformation to map the present feature space to an optimal one that is relatively insensitive to different subjects, while preserving the discriminating expression information. LDA defines the within-class matrix S_w and the between-class matrix S_b . It transforms a *n*-dimensional feature to an optimized *d*-dimensional feature, where d < n. In our experiments, the discriminating classes are the 6 expressions, thus the reduced dimension *d* is 5.

For the classification, we used the multi-class Random Forest algorithm. The algorithm was proposed in (Breiman, 2001) and defined as a meta-learner comprised of many individual trees. It was designed to operate quickly over large datasets and more importantly to be diverse by using random samples to

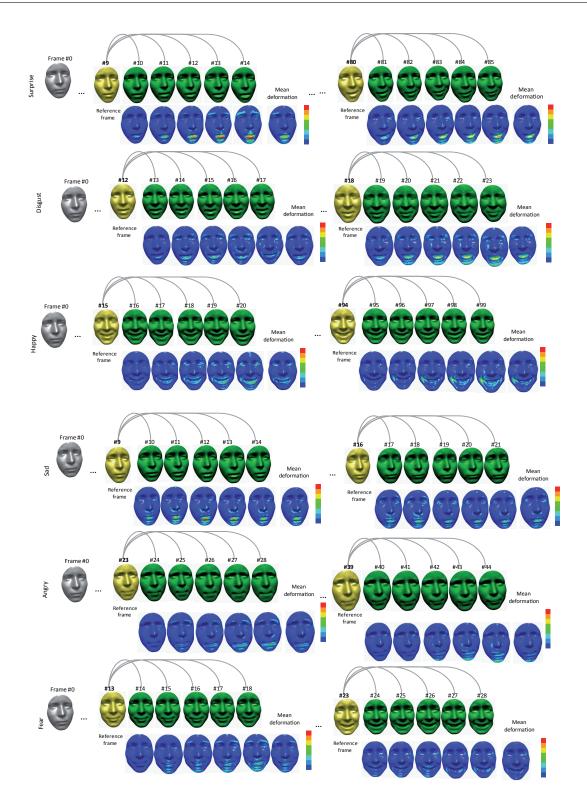


FIGURE 4.10: Computation of dynamic shape deformation on different subsequences taken from the BU-4DFE database. Each expression is illustrated by two rows: the upper one gives the reference frame of the subsequence and the n-1 successive frames. The corresponding deformation fields computed for each frame with respect to the reference one are illustrated in the lower row. The mean deformation fields are given on the right of each lower row.

build each tree in the forest. A tree achieves highly non-linear mappings by splitting the original problem into smaller ones, solvable with simple predictors. Each node in the tree consists of a test, whose result directs a data sample towards the left or the right child. During training, the tests are chosen in order to group the training data in clusters where simple models achieve good predictions. Such models are stored at the leaves, computed from the annotated data, which reached each leaf at train time. Once trained, a Random Forest is capable to classify a new expression from an input feature vector by putting it down each of the trees in the forest. Each tree gives a classification decision by voting for that class. Then, the forest chooses the classification having the most votes (over all the trees in the forest).

4.3.3.2 Motion Extraction with the HMM Classifier

The DSFs, can also be applied for expression recognition according to a different classification scheme. The deformations between successive frames in the subsequence are calculated using the DSFs. In particular, the deformation between two successive 3D frames is obtained by computing the pairwise Dense Scalar Fields $DSF(F_{t-1}, F_t)$ of correspondent radial curves. Based on this measure, we are able to quantify the motion of face points along radial curves and thus capture the changes in facial surface geometry.

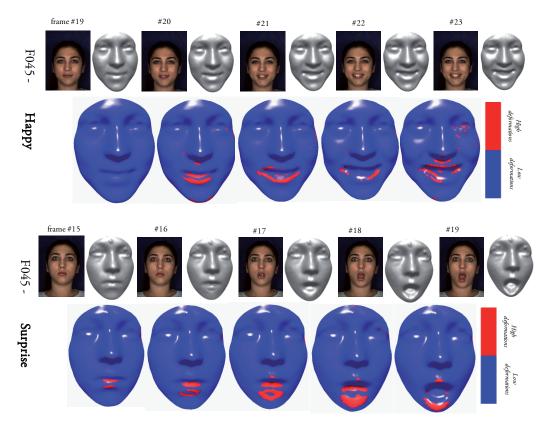


FIGURE 4.11: Examples of DSFs (deformations) between subsequent frames of 3D video sequences: Happy and surprise expressions are shown, respectively, on the left and right.

Figure 4.11 illustrates a direct application of the $DSF(F_{t-1}, F_t)$ and its effectiveness in capturing deformation between one facial surface to another belonging to two consecutive frames in a 3D video sequence. This figure shows two subsequences extracted from videos in the BU-4DFE database (happy and surprise expressions are shown on the left and on the right, respectively). For each sequence, the 2D image and the 3D scans of some frames are shown in the upper row. In the lower row, the deformation scalar fields $DSF(F_{t-1}, F_t)$ computed between consecutive frames (i.e., the current frame and the previous one) in the subsequence is reported. In order to provide a visual representation of the scalar fields, an automatic labeling scheme is applied that includes only two colors: The red color is associated with high $DSF(F_{t-1}, F_t)$ values and corresponds to facial regions affected by high deformations. The blue color is associated with regions that remain more stable from one frame to another. As illustrated in Figure 4.11, for different expressions, different regions are mainly deformed, showing the capability of the deformation fields to capture relevant changes of the face due to the facial expression. In particular, each deformation is expected to identify an expression, for example, as suggested by the intuition, the corners of the mouth and the cheeks are mainly deformed for the happiness expression.

With the proposed approach, the feature extraction process starts by computing for each 3D frame in a given video sequence the Dense Scalar Fields with respect to the previous one. In this way, we obtain as many fields as the number of frames in the sequence (decreased by one), where each field contains as many scalar values as the number of points composing the collection of radial curves representing the facial surface. In practice, the size of $DSF(F_{t-1}, F_t)$ is 1×5000 , considering 5000 points on the face, similarly to the feature vector used in the first scheme of classification (mean deformation-based). Since the dimensionality of the resulting feature vector is high, also in this case we use LDA to project the scalar values to a 5-dimensional feature space, which is sensitive to the deformations induced by different expressions. The 5-dimensional feature vector extracted for the 3D frame at instant t of a sequence is indicated as f^t in the following. Once extracted, the feature vectors are used to train HMMs and to learn deformations due to expressions along a temporal sequence of frames.

In our case, sequences of 3D frames constitute the temporal dynamics to be classified, and each prototypical expression is modeled by an HMM (a total of 6 HMMs λ^{expr} is required, with $expr \in \{an, di, fe, ha, sa, su\}$). Four states per HMM are used to represent the temporal behavior of each expression. This corresponds to the idea that each sequence starts and ends with a neutral expression (state S_1). The frames that belong to the temporal intervals where the face changes from neutral to expressive and back from expressive to neutral are modeled by the *onset* (S_2) and *offset* (S_4) states, respectively. Finally, the frames corresponding to the highest intensity of the expression are captured by the apex state (S_3) . This solution has proved its effectiveness in clustering the expressive states of a sequence also in other works (Sandbach et al., 2012a). Figure 4.12 exemplifies the structure of the HMMs used in our framework.

The training procedure of each HMM is summarized as follows:

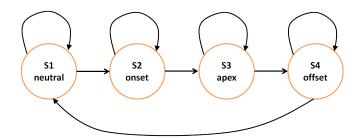


FIGURE 4.12: Structure of the HMMs modeling a 3D facial sequence. The four states model, respectively, the *neutral*, *onset*, *apex* and *offset* frames of the sequence. As shown, from each state it is possible to remain in the state itself or move to the next one (this is known as *Bakis* or left-right HMM).

- \hookrightarrow Feature vectors f^t of the training sequences are first clustered to identify a *codebook* of symbols using the standard LBG algorithm (Linde et al., 1980). This provides the required mapping between multidimensional feature vectors, taking values in a continuous domain, with the alphabet of symbols emitted by the HMM states;
- \hookrightarrow Expression sequences are considered as observation sequences $O = \{O^1, O^2, \dots, O^T\}$, where each observation O^t at time t is given by the feature vector f^t ;
- \hookrightarrow Each HMM λ^{expr} is initialized with random values and the *Baum-Welch* algorithm (Rabiner, 1989) is used to train the model using a set of training sequences. This estimates the model parameters, while maximizing the conditional probability $P(O|\lambda^{expr})$.

Given a 3D sequence to be classified, it is processed, so that each feature vectors f^t corresponds to a *test* observation $O = \{O^1 \equiv f^1, \ldots, O^T \equiv f^T\}$. Then, the test observation O is presented to the six HMMs λ^{expr} that model different expressions, and the *Viterbi* algorithm is used to determine the best path $\bar{Q} = \{\bar{q}^1, \ldots, \bar{q}^T\}$, which corresponds to the state sequence giving a maximum of likelihood to the observation sequence O. The likelihood along the best path, $p^{expr}(O, \bar{Q}|\lambda^{expr}) = \bar{p}^{expr}(O|\lambda^{expr})$ is considered as a good approximation of the true likelihood given by the more expensive forward procedure (Rabiner, 1989), where all the possible paths are considered instead of the best one. Finally, the sequence is classified as belonging to the class corresponding to the HMM whose log-likelihood along the best path is the greatest one.

4.3.4 Experimental Results

The proposed framework for facial expression recognition from dynamic sequences of 3D face scans has been experimented on the BU-4DFE database. Main characteristics of the database and results are reported in the following sections.

BU-4DFE Database: Description and Preprocessing

To investigate the usability and performance of 3D dynamic facial sequences for facial expression recognition, a dynamic 3D facial expression database has been created at *Binghamton University* (Yin et al., 2008). The Dimensional Imaging's 3D dynamic capturing system (Di3D, 2006), has been used to capture a sequence of stereo images and produce the depth map of the face according to a passive stereophotogrammetry approach. The range maps are then combined to produce a temporally varying sequence of high-resolution 3D images with an RMS accuracy of 0.2mm. At the same time, 2D texture videos of the dynamic 3D models are also recorded. Each participant (subject) was requested to perform the six prototypical expressions (i.e., angry, disgust, fear, happiness, sadness, and surprise) separately. Each expression sequence contains neutral expressions in the beginning and the end, so that each expression was performed gradually from neutral appearance, low intensity, high intensity, and back to low intensity and neutral. Each 3D sequence captures one expression at a rate of 25 frames per second and each 3D sequence lasts approximately 4 seconds with about 35,000 vertices per scan (i.e., 3D frame). The database consists of 101 subjects (58 female and 43 male, with an age range of 18-45 years old) including 606 3D model sequences with 6 prototypical expressions and a variety of ethnic/racial ancestries (i.e., 28 Asian, 8 African-American, 3 Hispanic/Latino, and 62 Caucasian). More details on the BU-4DFE can be found in (Yin et al., 2008). An example of a 3D dynamic facial sequence of a subject with "happy" expression is shown in Figure 4.13, where 2D frames (not used in our solution) and 3D frames are reported. From left to right, the frames illustrate the intensity of facial expression passing from *neutral* to *onset*, offset, apex and neutral again.

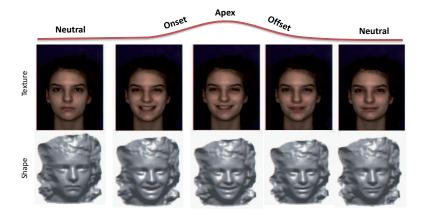


FIGURE 4.13: Examples of 2D and 3D frames extracted from a dynamic 3D video sequence of the BU-4DFE dataset.

It can be observed that the 3D frames present a near-frontal pose with some slight changes occurring mainly in the azimuthal plane. The scans are affected by large outliers, mainly acquired in the hair, neck and shoulders regions (see Figure 4.13). In order to remove these imperfections from each 3D frame the preprocessing pipeline described in Chapter 3 is performed.

Mean deformation-based Expression Classification

Following the experimental protocol proposed in (Sun and Yin, 2008), a large set of subsequences are extracted from the original expression sequences using a sliding window. The subsequences have been defined in (Sun and Yin, 2008) with a length of 6 frames with a sliding step of one frame from one subsequence to the following one. For example, with this approach, a sequence of 100 frames originates a set of $6 \times 95 = 570$ subsequences, each subsequence differing for one frame from the previous one. Each sequence is labelled to be one of the six basic expressions, thus extracted subsequences have the same label. This accounts for the fact that, in general, the subjects can enter the system not necessarily starting with a neutral expression, but with an arbitrary expression. The classification of these short sequences is regarded as an indication of the capability of the expression recognition framework to identify individual expressions. According to this, we first compute for each subsequence the Mean Deformation, which is then presented to multi-class Random Forest, as outlined in Sect. 4.3.3.

Thus, in the following we consider 40 trees and we report detailed results (confusion matrix) with this number of trees in Tab. 4.4. We recall that the rates are obtained by averaging the results of the 10-independent runs (10-fold cross validation). It can be noted that the largest confusions are between the *disgust (Di)* expression and the *angry (An)* and *Fear (Fe)* expressions. Interestingly, these three expressions capture negative emotive states of the subjects, so that similar facial muscles can be activated. The best classified expressions are *happy (Ha)* and *Surprise (Su)* with recognition accuracy of 95.47% and 94.53%, respectively. The standard deviation from the average performance is also reported in the table. The value of this statistical indicator suggests that small variations are observed between different folds.

| % | An | Di | Fe | Ha | Sa | Su | | | | | |
|---------------------------------------|-------|-------|-------|-------|-------|-------|--|--|--|--|--|
| An | 93.11 | 2.42 | 1.71 | 0.46 | 1.61 | 0.66 | | | | | |
| Di | 2.3 | 92.46 | 2.44 | 0.92 | 1.27 | 0.58 | | | | | |
| Fe | 1.89 | 1.75 | 91.24 | 1.5 | 1.76 | 1.83 | | | | | |
| Ha | 0.57 | 0.84 | 1.71 | 95.47 | 0.77 | 0.62 | | | | | |
| Sa | 1.7 | 1.52 | 2.01 | 1.09 | 92.46 | 1.19 | | | | | |
| Su | 0.71 | 0.85 | 1.84 | 0.72 | 1.33 | 94.53 | | | | | |
| Average recognition rate =93.21±0.81% | | | | | | | | | | | |

TABLE 4.4: Confusion matrix for Mean Deformation and Random Forest classifier (for 6-frames window).

I. Effect of the Subsequence Size: We have also conducted additional experiments when varying the temporal size of the sliding window used to define the subsequences. In Figure 4.14, we report results for a window size equal to 2, 5 and 6, and using the whole length of the sequence (on average this is about 100 frames). From the figure, it clearly emerges that the recognition rate of the six expressions increases when increasing the temporal length of the window. This reveals the importance of the temporal dynamics and shows that the spatio-temporal analysis outperforms a spatial analysis of the frames. By considering the

whole sequences for the classification, the result reach 100%. In the work, we decided to report detailed results when considering a window length of 6-frames to allow comparisons with previous studies.

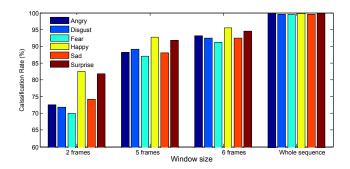


FIGURE 4.14: Effect of the temporal size of the sliding window on the results. The classification rates increase when increasing the length of the temporal window.

II. Effect of the Spatial Resolution of 3D Faces: In the proposed face representation, the DSFs are computed for the points of a set of radial curves originating from the nose tip. Due to this, the density of the scalar fields depend on the number of radial curves and the number of points per curve. So, the resolution used for the number of curves and points per curve can affect the final effectiveness of the representation. To investigated this aspect, we have conducted experiments when varying the spatial resolution of the 3D faces (i.e., the number of radial curves and the number of points per curve). Figure 4.15 expresses quantitatively the relationship between the expression classification accuracy (on the BU-4DFE) and the number of radial curves and the number of points per curve. This can give an indication of the expected decrease in the performance in the case the number of radial curves or points per curve is decreased due to the presence of noise and spikes in the data. From these results, we can also observe that the resolution in terms of number of curves has more importance than the resolution in terms of points per curve.

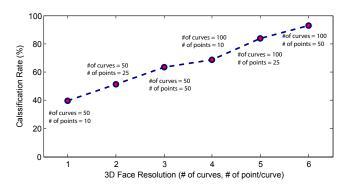


FIGURE 4.15: Effects of varying the 3D face resolution on the classification results.

HMM-based Expression Classification

Following the same setup as in previous section (originally defined in (Sun and Yin, 2008)), for this experiment we trained the HMMs on 6 frames subsequences constructed as discussed above. The 4state structure of the HMMs resulted adequate to model the subsequences. Also in this experiment, we performed 10-folds cross validation on the overall set of subsequences derived from the 60×6 sequences (31970 in total). The achieved results by classifying individual subsequences of the expression sequences (frame-by-frame experiment) are reported in the confusion matrix of Tab. 4.5. Values in the table have been obtained by using features of 6-frames subsequences as input to the 6 HMMs and using the maximum emission probability criterion as decision rule. It is clear that the proposed approach is capable to accurately classify individual frames by analyzing the corresponding subsequence of previous 5 frames. The average recognition rate is equal to 93.83%, slightly higher than the one displayed by Mean Deformation plus Random Forest classification schema (though the standard deviation among different folds shows a greater value in this case). It can also be noted that, compared to the previous classifier, the same tendency of recognition rates is in general achieved. In fact, correct classification of *angry* is high despite the difficulty of this expression analysis. This learning scheme achieved better recognition than the first one for angry (An) expression. Actually, whereas the angry (An) expression is known for its subtle motions, our classifier achieved 93.95% of correct classification, which demonstrates the ability of the proposed DSFs to capture subtle deformations across the 3D sequences. These similar good achievements are mainly the effect of the proposed deformation scalar fields.

| % | An | Di | Fe | Ha | Sa | Su |
|----|---------|---------|---------|--------|--------------|-------|
| An | 93.95 | 1.44 | 1.79 | 0.28 | 2.0 | 0.54 |
| Di | 3.10 | 91.54 | 3.40 | 0.54 | 1.27 | 0.15 |
| Fe | 1.05 | 1.42 | 94.55 | 0.69 | 1.67 | 0.62 |
| Ha | 0.51 | 0.93 | 1.65 | 94.58 | 1.93 | 0.40 |
| Sa | 1.77 | 0.48 | 1.99 | 0.32 | 94.84 | 0.60 |
| Su | 0.57 | 0.38 | 3.25 | 0.38 | 1.85 | 93.57 |
| Av | erage r | ecognit | ion rat | e = 93 | $3.83{\pm}1$ | 1.53% |

TABLE 4.5: Confusion matrix for Motion extraction and HMM classifiers (for 6-frames window).

4.3.5 Discussion and Comparative Evaluation

To the best of our knowledge, the works reporting results on expression recognition from dynamic sequences of 3D scans are those in (Le et al., 2011, Sun et al., 2010a, Sandbach et al., 2012b, fan, 2012), and recently (Reale et al., 2013). These works have been evaluated on the BU-4DFE dataset, but the testing protocols used in the experiments are sometimes different, so that a direct comparison of the results reported in these papers is not immediate. In the following, we discuss these solutions with respect to our proposal, also evidencing the different settings under which the expression recognition results are obtained.

| Authors | Method | Features | Classification | Protocol | T/S-T | RR (%) |
|--------------------------------|-------------------------------|--------------------------------------|------------------------|--|-------|--------------|
| (Sun and Yin, 2008) | MU-3D | 12 Motion Units | HMM | $\begin{array}{cccc} 60 & \mathrm{S}, & 6 & \mathrm{E}, \\ \mathrm{Win}{=}6 \end{array}$ | Т | 70.31, — |
| (Sun and Yin, 2008) | T-HMM | Tracking model | HMM | $\begin{array}{cccc} 60 & \mathrm{S}, & 6 & \mathrm{E}, \\ \mathrm{Win}{=}6 \end{array}$ | Т | 80.04, — |
| (Sun and Yin, 2008) | P2D-HMM | Curvature + Tracking model | T-HMM + S-HMM | $\begin{array}{cccc} 60 & \mathrm{S}, & 6 & \mathrm{E}, \\ \mathrm{Win}{=}6 \end{array}$ | S-T | 82.19, — |
| (Sun and Yin, 2008) | R-2DHMM | Curvature + Tracking model | 2D-HMM | $\begin{array}{cccc} 60 & \mathrm{S}, & 6 & \mathrm{E}, \\ \mathrm{Win}{=}6 \end{array}$ | S-T | 90.44, — |
| (Sandbach et al., 2011) | 3D Motion-based | FFD + Quad-tree | GentleBoost + HMM | —, 3 E, Win=4 | Т | 73.61, 81.93 |
| (Sandbach et al., 2012b) | 3D Motion-based | FFD + Quad-tree | GentleBoost + HMM | —, 6 E, vari- able Win | Т | 64.6, — |
| (Le et al., 2011) | Level curve-based | pair- and segment- wise distances | HMM | 60 S, 3 E, — | S-T | —, 92.22 |
| (Fang et al., 2011, fan, 2012) | AFM Fitting | LBP-TOP | SVM-RBF | 100 S, 6 E, — | Т | —, 74.63 |
| (Fang et al., 2011, fan, 2012) | AFM Fitting | LBP-TOP | SVM-RBF | 100 S, 3 E, — | Т | —, 96.71 |
| (Reale et al., 2013) | Spatio-temporal volume | "Nebula" Feature | SVM-RBF | 100 S, 6 E, Win=15 | S-T | —, 76.10 |
| (Ben Amor et al., 2014a) | Extraction | 3D Motion Extrac- tion | | $\begin{array}{cccc} 60 & \mathrm{S}, & 6 & \mathrm{E}, \\ \mathrm{Win}{=}6 \end{array}$ | Т | 93.83, — |
| (Ben Amor et al., 2014a) | Geometric Mean Deformation | Mean Deformation | LDA-Random For- est | $\begin{array}{cccc} 60 & \mathrm{S}, & 6 & \mathrm{E}, \\ \mathrm{Win}{=}6 & \end{array}$ | Т | 93.21, — |

TABLE 4.6: Comparison of this work to earlier studies. Protocol description: #subjects (S), #expressions (E), Win size (Win). T: temporal only/S-T: spatio-temporal. Accuracy on sliding window/whole sequence (or subsequence).

Table 4.6 summarizes approaches and results reported previously on the BU-4DFE dataset, compared to those obtained in this work. The testing protocols used in the experiments are quite different especially the number of verified expressions, all the six basic expressions in (Fang et al., 2011, Sun et al., 2010a, Sun and Yin, 2008, fan, 2012), and (Reale et al., 2013) whereas (Le et al., 2011, Sandbach et al., 2011) reported primary results on only three expressions. The number of subjects considered is 60, except in (Sandbach et al., 2011) where the number of subjects is not specified. In general, sequences in which the required expressions are acted accurately are selected, whereas in (Fang et al., 2011) and (fan, 2012) 507 sequences out of the 606 total are used for all subjects. In our experiments, we conducted tests by following the same setting proposed by the earliest and more complete evaluation described in (Sun and Yin, 2008). The training and the testing sets were constructed by generating subsequences of 6-frames from all sequences of 60 selected subjects. The process were repeated by shifting the starting index of the sequence every one frame till the end of the sequence. We note that the proposed approaches outperforms state-of-theart solutions following similar experimental settings. The recognition rates reported in (Sun and Yin, (2008) and (Sun et al., 2010a) based on temporal analysis only was 80.04% and spatio-temporal analysis was 90.44%. In both studies subsequences of constant window width including 6-frames (win = 6) is defined for experiments. We emphasize that their approach is not completely automatic requiring 83 manually annotated landmarks on the first frame of the sequence to allow accurate model tracking. The method proposed in (Sandbach et al., 2011) and (Sandbach et al., 2012b) is fully automatic with respect to the processing of facial frames in the temporal sequences, but uses *supervised* learning to annotate individual frames of the sequence in order to train a set of HMMs. Though performed off-line, supervised

learning requires manual annotation and counting on a consistent number of training sequences that can be a time consuming operation. In addition, a drawback of this solution is the computational cost due to Free-Form Deformations based on B-spline interpolation between a lattice of control points for nonrigid registration and motion capturing between frames. Preliminary tests were reported on three expressions: (An), (Ha) and (Su). Authors motivated the choice of the happiness and anger expressions with the fact that they are at either ends of the valence expression spectrum, whereas surprise was also chosen as it is at one extreme of the arousal expression spectrum. However, these experiments were carried out on a subset of subjects accurately selected as acting out the required expression. Verification of the classification system was performed using a 10-fold cross-validation testing. On this subset of expressions and subjects, an average expression recognition rate of 81.93% is reported. In (Sandbach et al., 2012b), the same authors have reported 64.6% classification rate when in their evaluation they consider all the six basic expressions. In (Le et al., 2011) a fully automatic method is also proposed, that uses an *unsupervised* learning solution to train a set of HMMs (i.e., annotation of individual frames is not required in this case). Expression recognition is performed on 60 subjects from the BU-4DFE database for the expressions of happiness, sadness and surprise. The recognition accuracy averaged on 10 rounds of 10-fold cross-validation show an overall value of 92.22%, with the highest performance of 95% obtained for the happiness expression. However, the authors reported recognition results on whole facial sequences, but this hinders the possibility of the methods to adhere to a real-time protocol. In fact, reported recognition results depends on the preprocessing of whole sequences unlike our approach and the one described in (Sun and Yin, 2008), which are able to provide recognition results when processing very few 3D frames. In (Fang et al., 2011) and (fan, 2012), results are presented for expression recognition accuracy on 100 subjects picked out from BU-4DFE database. However, 507 sequences are selected manually according to the following criteria: (1) the 4D sequence should start by neutral expression, and (2) sequences containing corrupted meshes are discarded. In addition, to achieve recognition rate of 75.82%, whole sequences should be analyzed. The authors reported highest recognition rates when only (Ha), (An), and (Su) expressions (96.71%) or (Ha), (Sa) and (Su) (95.75%) are considered. The protocol used in (Reale et al., 2013) is quite different from the others. First, the onset frame for each of the six canonical expressions has been marked manually on each sequence of the BU-4DFE database. Then, a fixed size window of 15 frames starting from the onset frame has been extracted from each expression of 100 subjects. So, although sequences from 100 subjects are used by this approach, it also uses a manual intervention to detect the onset frame and just 15 frames from the onset one are used for the classification (and these typically correspond to the most intense expression, including the apex frames).

According to this comparative analysis, the proposed framework compares favorably with state-of-the-art solutions. It consists of two geometric deformation learning schemes with a common feature extraction module (DSFs). This demonstrates the effectiveness of the novel mathematical representation called Dense Scalar Fields (DSFs), under the two designed schemes.

4.4 Conclusions

In this chapter, our interest was to effectively quantify the facial deformations to perform facial expression classification. Two different methodologies have been presented – (1) a landmark-dependent approach using 3D facial patches extracted around the landmarks and grounding on shape analysis of the patched using iso-level closed curves representation; and (2) a landmark-free approach based on shape analysis of open radial curves. While in the first approach, the use of static 3D data is explored, the geometric deformations from dynamic data is investigated in the second approach. From a methodological point-of-view, (1) proposed such representation using facial patches to cover important Action Units (AU) on the face, then classify the expression according to similar AU movements. Here the correspondence between facial patches is given explicitly by the correspondence between landmarks. In (2) an holistic representation of the face through multiple radial elastic (open) curves handle with the problem of correspondence and allow dense correspondence and tracking across the 3D video. Then two learning schemes of the geometric deformations serve to perform expression recognition.

Chapter 5

Facial Soft-biometrics Estimation

In this Chapter¹, we explore the contribution of the 3D facial geometry to the task of recognizing facial attributes, such as the gender and the age. There is a growing interest to soft biometrics recognition as means of improving automated face recognition since they hold the promise of significantly reducing recognition errors by filtering the number of entries in a database to be searched. For example, if the user can somehow be identified as a middle-aged Asian female, the search can be restricted only to the subjects with this profile enrolled in the database. There are other uses of automatic soft-biometrics estimation ranging from Human-Machine Interaction (HMI) to customize interfaces or services regarding the user's age or gender. It includes also the commercial use when limiting underage alcohol buyer, for instance, and suggest customized advertising. Most of the previous studies investigated the use of color data to make solft-biometrics estimation, only a few work have explored the role of the geometry (or the shape). In this chapter, we demonstrate the richness and the relevance of use 3D shape data to tackle these problems. Using Morphology-inspired descriptions related to the human differences extracted using our Riemannian framework presented in Chapter 2. To our knowledge, we conducted the first study on age estimation (Xia et al., 2014c) and joint soft-biometrics estimation (Xia et al., 2014d)([J3-s]) from 3D faces. Our methodology to quantify the morphological divergences between age-groups or genders is one of the most original points in this work.

5.1 Introduction

Gender, Ethnicity, and Age are natural recognizable attributes in human faces. In their daily life, human beings are performing their estimation naturally and effectively, from the face. In anthropometry studies² (Ziqing et al., 2010), it has also been revealed that significant facial morphology differences

¹The content of this chapter is related to our published conference papers (Xia et al., 2013b) and (Xia et al., 2014c) and submitted journal papers (Xia et al., 2014b)([**J1-s**]) and (Xia et al., 2014d)([**J3-s**]).

²refers to the measurement of the human individual.

exist in different gender, ethnicity and age groups. In sexual dimorphism studies³ (Vicki et al., 1993), researchers have found that male faces usually possess more prominent features than female faces. Male's face usually has a more protuberant nose, eyebrows, more prominent chin and jaws. The forehead is more backward sloping, and the distance between top-lip and nose-base is longer. Research presented in (Ziqing et al., 2010) have also demonstrated that females are smaller in all the concerned anthropometric measurements. When studying the ethnicity differences in face (Farkas LG, 2005), researchers found that compared with the North America Whites, the Asian population usually have broader faces and noses, farther apart eyes, and exhibit the greatest difference in the anatomical orbital regions (around eyes and eyebrows). The clinical study reported in (Alphonse et al., 2013) have revealed that the Caucasians has significantly lower fetal frontomaxillary facial angle (FMFA) measurements than Asians. In (Ziqing et al., 2010), 16 anthropometric measurements have been recognized as significantly different between Asian and Caucasian faces. In face aging studies (Rhodes, 2009, Ramanathan et al., 2009), researchers have concluded that, the craniofacial growth is the main change in baby and adolescent faces, which results in the re-sizing and redistribution of facial features. In this period, the bigger the size of the face, the larger the estimated age. When the craniofacial growth stops at about 18 years old, the face contour and texture changes become the dominant changes. In addition, young adults tend to have a more triangle shaped face with a small amount of wrinkles. In contrast, older adults are usually associated with a U-shaped face with significant wrinkles.

Besides the perception of these soft-biometrics⁴ in the face, gender, ethnicity and age also interact with each other in characterizing the face shape (Ziqing et al., 2010). For example, according to the anthropometric studies above, the shape of the nose is influenced by all the three attributes. Female faces usually look smoother and younger than male faces, and the Asian faces usually look younger than others (Yukio et al., 2003). In (Vignali et al., 2003), the authors have demonstrated both visually and quantitatively that ethnicity and gender are correlated to some extend in 3D face. In (Gao and Ai, 2009), the authors found that the gender classifier trained on a specific ethnicity could not perform better generalization ability on other ethnicity.

5.2 Related Work

From the analysis above, it is clear that the face demonstrates significant cues to recognize gender, ethnicity and age. They are also correlated with each other. In the literature of facial soft-biometrics recognition, abundant works have been proposed for gender classification, ethnicity classification and age estimation, taken separately. These works are done either with features from the 2D face texture (2D texture-based), or features from the 3D face shape (3D shape-based), or features from both of the texture and the shape of face (texture and shape-based). By definition, the face texture represents the reflection

³http://www.virtualffs.co.uk/

 $^{{}^{4}}$ A.K. Jain defined Soft-biometrics as a set of traits providing information about an individual, though these traits are not able to individually authenticate the subject because they lack in distinctiveness and permanence (Jain et al., 2004).

and absorption effects of external illumination caused by the facial skin, while the 3D face shape define the border which distinguishes the face and the environment.

In 2D-based gender classification, (Ylioinas et al., 2011) combine the Contrast Information (strength of patterns) and the Local Binary Patterns (LBP). (Yang et al., 2011) combine Active Appearance Models (AAM) and LBP with sequence selection algorithms. (Shan, 2012) selects discriminating LBP features with Adaboost. (Kumar et al., 2008) use describable visual attributes in face as features. (Wang et al., 2012) enhance the performance of LBP with one of its variants, named Local Circular Patterns (LCP). (Makinen and Raisamo, 2008) compare different gender classification methods, and reveal that the database, normalization, hair, and experimental settings account more for the results, than the classifiers. (Gao and Ai, 2009), learn ethnicity-specific gender classifiers and achieve higher overall classification results on a collection of 2D images. (Giovanna and Jean-Luc, 2012) perform ethnicity-specific gender classification on the 2D FERET and TRECVID datasets. Unexpectedly, they found that the ethnicity information is not helpful in gender classification. Using the 3D shape, (Liu and Palmer, 2003) extract features from the height and orientation differences on symmetrical facial points. (Vignali et al., 2003) use the 3D coordinates of 436 face landmark points as features. (Han et al., 2009) extract geometric features with the volume and area information of faces. In (Hu et al., 2010), the authors divide each face into four regions, and find that the upper part is the most discriminating for gender. Recently, (Toderici et al., 2010) obtain features with the wavelets and the MDS (Multi Dimensional Scaling). In our previous work conducted in (Ballihi et al., 2012c), we propose to select salient geometrical facial features (radial and iso-level facial curves) using adaptive Boosting. The gender classification, is performed by a Nearest Neighbor classifier to Male and Female templates. (Gilani et al., 2013) automatically detect the biologically significant facial landmarks and calculate the Euclidean and geodesic distances between them as facial features. Combining shape and texture (texture and shape-based), (Lu et al., 2006b) fuse the posterior probabilities generated from the range and intensity images using SVM (Support Vector Machine). (Wu et al., 2007) combine shape and texture implicitly with needle maps recovered from intensity images. (Huynh et al., 2012) fuse the Gradient-LBP from range image and the Uniform LBP features from the gray image.

Compared to gender, ethnicity is less explored in face studies. In 2D texture-based works, the first work was tested on the FERET dataset in (Srinivas et al., 1998), with a hybrid architecture of the Ensemble Radial Basis Function (ERBF) networks and the decision trees. (Srinivas et al., 1998) classify ethnicity with SVM on pixel intensity and Biologically Inspired Model (BIM) features. (Zhiguang and Haizhou, 2007) perform ethnicity classification with LBP features on images of a snapshot dataset and FERET dataset. (Srinivas et al., 1998) classify 2D images into Asian and non-Asian groups with Multi-Scale LDA classifiers. (Giovanna and Jean-Luc, 2012) perform gender-specific ethnicity classification with the 2D FERET and TRECVID datasets. While, again unexpectedly, they found that the gender information is not helpful in ethnicity classification. For the shape-based works, in (Srinivas et al., 1998), the authors perform fuzzy ethnicity recognition of eastern and western groups on 3D FRGC2.0 dataset (Phillips et al., 2005), with the Learned Visual Codebook (LVC) derived from histograms of Gabor features. (Toderici

et al., 2010) extract features using the wavelets and the MDS on the Asian and White subsets of the 3D FRGC2.0 dataset. The only texture and shape-based work is presented in (Lu et al., 2006b), where the authors used the ensemble of 2D and 3D scans from the UND and MSU datasets, considering Asian and non-Asian groups.

In age estimation literature, all existing approaches are 2D-based. As pointed in (Rhodes, 2009, Ramanathan et al., 2009), the mathematical cardioid strain model was first proposed for modeling face aging in young ages. After this, face-appearance-based approaches and intrinsic/extrinsic-factor-aided approaches make the two main branches of research in automatic age estimation. Considering that different people have similar aging patterns in face, researchers have employed the Active Appearance Model (AAM) (Lanitis et al., 2004, 2002, Wu et al., 2012), the manifold embedding parameters (Wu et al., 2012, Guo et al., 2008a,b, Li et al., 2012), and the bio-inspired Features (BIF) (Guodong et al., 2009) for revealing the public-level aging patterns. Beyond this, based on the observation that similar faces tend to age similarly, (Lanitis et al., 2004, 2002) first cluster face images into groups according to their inner similarity, and then perform age estimation within each group. These works confirm that the group-level aging patterns exist and are useful in age estimation. Considering that different people aged differently, (Xin et al., 2007, 2006) proposed the Aging-Pattern-Subspace (AGES) constructed from a temporal sequence of individual images, to study the individual-level aging patterns. Moreover, considering different face components age differently, (Jinli et al., 2010) studies the component-level aging patterns with a hierarchical And-Or Graph, and found that the forehead and eye regions are the most informative. The intrinsic/extrinsic-factor-aided approaches study age estimation together with face appearance and the intrinsic factors (permanent factors like gene, gender, ethnicity, identity, etc.), and the extrinsic factors (temporary factors like lifestyle, health, sociality, expression, pose, illumination, etc.). Thinking that faces age differently in different age range, age-specific approaches are adopted by (Lanitis et al., 2004, Guo et al., 2008a,b), where age estimation is obtained by using a global age estimator first, then adjusting the estimated age by a local estimator that operates within a specific age range. Considering that different gender age differently, (Ramanathan et al., 2009, Guo et al., 2008b, Lakshmiprabha et al., 2011, Kazuya et al., 2010) estimate age on male and female groups separately. (Lanitis et al., 2002) encodes the individual lifestyle information in age estimation and demonstrate its importance in determining the most appropriate aging function of the individual. (Kazuya et al., 2010) gives weights to different lighting conditions for illumination-robust age estimation. (Li et al., 2012) gives consideration of the feature redundancy and uses feature selection to enhance age estimation. All of the previous work considering the intrinsic/extrinsic factors have gained better age estimation performance in comparison of using face appearance only.

From the analysis above, we notice that most of the work in literature deals with gender, ethnicity and age recognition separately. The correlations among these soft-biometrics have attracted little consideration. Only few works perform ethnicity-specific gender classification (Gao and Ai, 2009, Giovanna and Jean-Luc, 2012), gender-specific ethnicity classification (Giovanna and Jean-Luc, 2012), and gender-specific age estimation (Xia et al., 2014c, Ramanathan et al., 2009, Guo et al., 2008b, Lakshmiprabha et al., 2011,

Kazuya et al., 2010). To the best of our knowledge, the age-specific gender or ethnicity recognition, and ethnicity-specific age estimation has never been addressed in the literature. Also, no consensus has been achieved regarding the correlation between gender and ethnicity. The experimental results in (Giovanna and Jean-Luc, 2012) show gender and ethnicity are not helpful in each others' recognition tasks. While, the experimental results of (Gao and Ai, 2009) demonstrate that ethnicity-specific gender classifiers achieve higher overall performances. Since both of these works are 2D texture image based, we think that, in addition to their sensitivity to illumination and pose changes, the face images incorporate distorted shape information. Thus, in this work, we propose to explore the use of the 3D shape of the face to better study these attributes as well as their correlation. In (Yuxiao et al., 2010), the authors have demonstrated that, with the 3D scans, human observers perform better on both gender recognition and ethnicity recognition tasks than with 2D face images. In biological studies (Harold et al., 1995), researchers also found that, when considering gender and ethnicity recognition tasks, the usage of 2D face images is limited to full-face view, while the 3D scans are proved to be adaptable to angled views (non-frontal poses). The proposed study gives a thorough study of the correlations among the three attributes. In particular, we are going to study the following questions :(1) Can 3D face shape reveal your gender, ethnicity and age? (2) Can the gender, ethnicity and age information be useful in each others recognition task? (3) How much they are correlated in the facial shape? and (4) Are their correlations useful in real-world like applications?

5.3 Methodology and Contributions

To address the over-mentioned questions, two consecutive steps are designed in our approach: the feature extraction step and the classification/regression step. Within the first step, we first pre-process the 3D scans to limit the facial region, and then extract four types of features from the 3D shape of the face. These four descriptions reflect different perspectives of face perception. Withing the classification/regression step, we feed the features to Random Forest for Gender or Ethnicity classification, and Age estimation. To enhance the performance, we have also introduced two additional steps in our approach, the *Feature Selection* and the *Fusion*. The feature selection method is used for highlighting the salient subset of features which contains the information of gender, ethnicity and age. The Fusion method merges all the information from the four types of features to account for the different perspectives. The main contributions of this work could be summarized as follows:

↔ We propose four different and complementary facial descriptions based on shape analysis of facial radial curves (Chapter 2), with which we demonstrate that the 3D shape of the face can reveal our gender, ethnicity and age. Extensive evaluations on the challenging FRGC2.0 dataset (Phillips et al., 2005) demonstrate the effectiveness of the proposed facial attributes recognition approach and its robustness to facial expressions.

- ↔ We demonstrate that gender, ethnicity and age are correlated in the 3D face, and the correlations are helpful in each others' estimation. Our conclusion is significantly different with (Giovanna and Jean-Luc, 2012), which claims that gender and ethnicity are not helpful for each other's recognition. We also discover that the correlation between ethnicity and age is the strongest among the correlations.
- \hookrightarrow We demonstrate that the correlation of these soft-biometrics can be useful in real-world applications.
- ↔ This is the first work in the literature which gives a thorough study of the correlations among Gender, Ethnicity and Age with 3D faces. It is also the first work which studies 3D face based age estimation (Xia et al., 2014a).

In the following, we will describe our Morphology-inspired descriptions extracted based on our Riemannian approach for 3D face analysis.

5.4 Geometrical Features Extraction

In this section, we describe four different morphological descriptions extracted from the 3D shape of the face. These descriptions are densely extracted using shape analysis of 3D radial curves of the face. Based on this representation, earlier studies on 3D face recognition (Drira et al., 2013b) and 4D expression recognition (Ben Amor et al., 2014b) have been successfully conducted. Again, we demonstrate here how this representation is convenient to quantify the morphological divergences of gender, ethnicity and age groups.

5.4.1 Features Computation

In this section, different facial morphology descriptions will be presented. Each of them reflects face morphological properties based on the 3D face geometry. Through the facial representation using multiple curves, one can define an efficient way to deform one shape into another (using geodesics) and effectively quantify their divergence using the Dense Scalar Fields, introduced in Chapter 2. A possible interpretation of the DSFs is the local deformations needed to go from one shape to another through a dense and accurate correspondence between the shapes. We have demonstrated in Chapter 4 a first use of the DSFs to capture geometric deformation across sequences of 3D faces. In this chapter, the use of DSFs is different as it will be used to derive four morphological descriptions from static 3D faces, as described in the following:

 \hookrightarrow The 3D-Symmetry description (3D-sym.) shown in Figure 5.2 (a) 3D-sym. captures densely the deformation between bilateral symmetrical curves (β_{α}^{S} and $\beta_{2\pi-\alpha}^{S}$). This description allows to study the relationship between the bilateral symmetry and the 3D facial attributes, Age, Gender

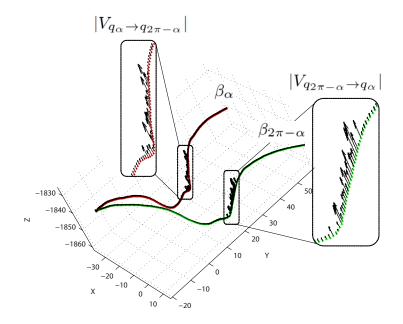


FIGURE 5.1: 3D-Symmetry description from pairwise radial curves. Illustration of the obtained direction needed to deform β_{α} to fit $\beta_{2\pi-\alpha}$ ($|V_{q_{\alpha} \to q_{2\pi-\alpha}}|$) and inversely ($|V_{q_{2\pi-\alpha} \to q_{\alpha}}|$). q_{α} and $q_{2\pi-\alpha}$ denote SRVF of bilateral symmetrical curves β_{α} and $\beta_{2\pi-\alpha}$, respectively extracted from an arbitrary face.

and Ethnicity. In Figure 5.1, we illustrate the DSFs computation between arbitrary symmetric curves on the face. Its is clear from this figure that although the geodesics lengths connecting q_{α} and $q_{2\pi-\alpha}$ and inversely, are same, the DSFs vectors $|V_{q_{\alpha}\to q_{2\pi-\alpha}}|$ and $|V_{q_{2\pi-\alpha}\to q_{\alpha}}|$ are different $(|V_{q_{\alpha}\to q_{2\pi-\alpha}}| \neq |V_{q_{2\pi-\alpha}\to q_{\alpha}}|)$, in general.

- \hookrightarrow The 3D-Averageness description (3D-avg.) shown in Figure 5.2 (b) compute DSFs between pairwise curves with the same angle index α , β_{α}^{S} and β_{α}^{T} extracted from the face and a template face, respectively. The template T (presented in 5.2(b)) is defined as the middle point of geodesic path from a representative male face to a representative female face. The 3D-Averageness description is a way to explore the idea that different population groups deviate differently from a given mean facial shape. Faces of different morphology could show different deformations to reach the template face.
- \hookrightarrow The 3D-Spatial description (3D-spat.) shown in Figure 5.2 (c) captures the deformation of a curve β_{α} to the middle-up curve β_{0} , emanating from the nose tip and goes over the nose and the forehead in *S*. As β_{0} is the most rigid curve in the face, the 3D-Spatial description captures the smooth intrinsic deformation from the most rigid part of the face.
- \hookrightarrow The 3D-Gradient description (3D-grad.) shown in Figure 5.2 (d) captures the differences between pairwise neighboring curves (β_{α}^{S} and $\beta_{\alpha+\Delta\alpha}^{S}$). It captures the local deformations on the face. This description is useful to detect wrinkles on the face , for example, by performing a kind of "derivation" across the indexed curves.

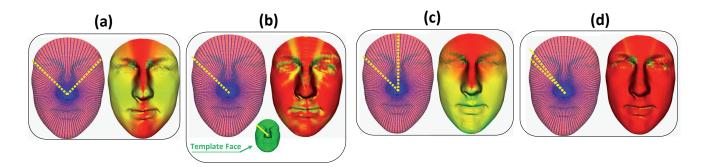


FIGURE 5.2: Illustrations of different features on 3D shape of the face S. (a) 3D-Symmetry Description: shape differences from each radial curve β_{α}^{S} to its symmetrical curve $\beta_{2\pi-\alpha}^{S}$; (b) 3D-Averageness Description: shape differences from radial curve β_{α}^{S} in a preprocessed face to radial curve β_{α}^{T} in face template (with same angle index α); (c) 3D-Spatial Description: shape differences from radial curve β_{α}^{S} to the middle-up radial curve β_{0}^{S} in the forehead; (d) 3D-Gradient Description: shape differences from radial curve β_{α}^{S} to its neighbor curve $\beta_{\alpha+\Delta\alpha}^{S}$

In each panel of Figure 5.2, the left part illustrates the extracted radial curves and the curve comparison strategy, the right part shows the corresponding features as color-map on the face. On each point of the face, the warmer the color, the lower the deformation magnitude and the higher the description magnitude. For example, the most symmetrical part of the face is located around the symmetrical plane (red colors), further away the symmetry plane, increasing asymmetry is observable on the face (colder colors). It can be seen, from panel (a) in Figure 5.2 that the local asymmetry emerges around the eyes, mouth, nose, chin, etc. Panel (b) shows clearly that faces shapes differences reside on these features (yellow-green colors). The rest of the facial region shows similarities across the faces (warmer colors). In panel (c), a smooth changing map shows the shape deviation from the upper profile. In panel (d), the gradient highlights local changes (details) around the facial features (yellow-green colors).

5.4.2 Relationship with Facial Morphology

Our goal in this section is to show the relationship between the computed features and the face morphology differences across age, ethnicity and gender groups. First, the **3D-sym.** descriptor densely characterizes the bilateral asymmetry of the face. Also, this description can be employed to distinguish younger and older people, as the latter generally have less symmetric faces. The **3D-sym.** description offers an effective way to study the effect of facial bilateral symmetry on the studied attributes. Second, the morphological differences between shapes can be densely captured using the **3D-avg.** descriptor. This description is very important to distinguish Male and Female faces, as stated in many previous studies (Ziqing et al., 2010, Vicki et al., 1993). In general, Male face has a more protuberant nose, eyebrows, more prominent chin and jaws. The forehead is more backward sloping, and the distance between top-lip and nose-base is longer. It has been shown that differences are observable between Asian and non-Asian faces (Farkas LG, 2005). The Asian population usually has broader faces and noses, farther apart eyes, and exhibit the greatest difference in the anatomical orbital regions (around the eye and eyebrow). It

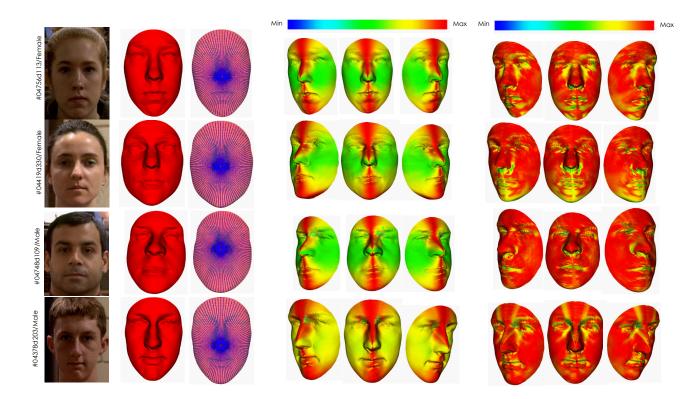


FIGURE 5.3: Examples of bilateral symmetry DSFs and averageness DSFs computed on two female faces (top rows) and two male faces (bottom row). The color, the 3D shape and the representation using radial curves are shown. Notice that in the color bars Max (warmer colors) mean maximum symmetry or averagness. Inversely, the Min in color bars reflect maximum asymmetry or distinctiveness (colder colors).

is also well known that the craniofacial growth is an important change in the baby and adolescent face, which results in re-sizing and redistribution of facial features (Rhodes, 2009, Ramanathan et al., 2009). By measuring the deformation from the face to a defined template face, the **3D-avg**. descriptor is able to capture the morphological differences, in term of features sizes, etc. Third, the **3D-grad**. description is useful to capture the smoothness of the human face. It has been demonstrated, in (Yukio et al., 2003) for example, that female faces usually look smoother and younger than male faces, and the Asian faces usually look younger than non-Asian faces. In addition, the **3D-grad**. can be viewed as a gradient operator over the face and can highlight the wrinkles. Finally, the **3D-spat**. descriptor which measures, over the face, the deviation to the most rigid part (the upper profile) and produce a smooth map of those deviations. It reflects global shape changes on the static face. Shown in Figure 5.3 are four examples of the 3D-Sym. and 3D-Avg. descriptions viewed from three different angles for better visibility. When the first two rows illustrate examples of female faces (taken from FRGC2.0 dataset), in the last two rows are given the descriptions for male faces.

The four descriptions allow to capture densely different morphological perspectives from the facial shapes. Accordingly, we seek to know what clues are relevant to each of the studied facial attribute (gender, ethnicity and age)? In Figure 5.4, we show the magnitude of the correlation between the facial features

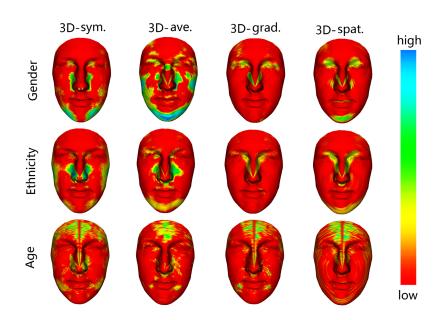


FIGURE 5.4: Correlation between facial features and facial attributes on each point of the face. 3D-sym.
: Symmetry — 3D-ave. : Averageness — 3D-grad. : Gradient — 3D-spat. : Spatial.

and the facial attributes as color-map on each point of the face. The correlations are calculated with the 466 earliest scans of FRGC2.0 dataset. Formally, for all the 466 scans, the *i*th feature of a face description makes one dimensional vector $D_i = (d_i^1, d_i^2, \ldots, d_i^{466})$, where d_i^m denotes the *i*th feature of the m^{th} face. Then for a given facial attribute, the labels for 466 scans make a vector $L_a = (L_1, L_2, \ldots, L_{466})$, where L_m denotes the attribute label of the m^{th} face. Then, the correlation between the *i*th feature of the description and the studied attribute is given by the *Pearson Correlation Coefficient* between D_i and L_a . This coefficient is defined as the covariance of the two variables divided by the product of their standard deviations. Formally, for two variables X and Y, the *Pearson correlation coefficient* $p_{X,Y}$ is defined as $p_{X,Y} = cov(X, Y)/(\sigma_X \sigma_Y)$, where *cov* denotes the covariance, σ denotes the standard deviation. The absolute value of *Pearson Correlation Coefficient* ranges from 0 to 1. The higher the value, the higher the linear correlation between the two variables. In our case, the higher the correlation between a facial attribute. Each column of Figure 5.4 shows the correlation between a face description and a facial attribute, each row shows the correlation between each face description and a facial attribute. The higher the correlation between a face description and each facial point.

According to these results, we can confirm three things. First, the green and blue colors in the figure show that the face features are considerably correlated with the facial attributes. With this, we confirm that the 3D face shape is informative for Gender, Ethnicity and Age. Secondly, we confirm that the four descriptions in our approach give different and complementary perspectives for perception of Gender, Ethnicity an Age. For gender, the *3D-sym.* description 'sees' the inner eye corners, the conjecture area of

the nose and the cheeks, and the chin-side regions. The 3D-avg. description 'looks' at the eyebrows, the eyes, the nose, the lips, and gives big attention to the cheek-sides and the chin. The 3D-grad. description emphasizes the eyes and the dorsal nasals of the nose, while the 3D-spat. description also considers the chin and the sides of the nostrils. For Ethnicity, the 3D-sym. description 'sees' the nose regions and the cheeks. The 3D-ave. description 'looks' at the conjecture area of the nose and the cheek-sides, and the chin region. The 3D-grad. description emphasizes the inner eye-corners and the dorsal nasals of the nose, while the 3D-spat. description also emphasizes the chin and the area around the nostrils. For Age, the 3D-sym. description 'sees' the whole forhead, the nose, the outer eye corners, and the the regions besides the mouth corners. The 3D-ave. description mainly 'looks' at the center part of the forehead, the inner eye corners, and the nose surrounding regions. The 3D-grad. description emphasizes the center part of the forehead, the eye corners, the nose bridge, and the mouth corners, while the 3D-spat. description emphasizes the center part of the forehead, the eye corners, and the nose bridge. Thus, according to these observations, the four descriptions 'see' different and complimentary clues of Gender, Ethnicity and Age in the face. Thirdly, it confirms the relevance of the facial geometry to the Gender, Ethnicity and Age. For Gender, the eyes, nose, cheek-sides, lips and the chin are particularly informative. In somehow, it matches with the previous findings in sexual dimorphism (Vicki et al., 1993), which claim that males have protuberant nose, eyebrows, chin and jaws than females, and the distance between top-lip and nose-base is longer. For Ethnicity, the eyes, nose, cheek-sides and chin are more informative. This echoes the findings in (Farkas LG, 2005, 17) which stated that the non-Asians have broader faces and noses, farther apart eyes, and lower fetal front-maxillary facial angle (FMFA) measurements than Asians. For both Gender and Ethnicity, the forehead gives little information. While for Age, the forehead, together with the nose, the eye corners and the mouth corners, show the strongest hints. It naturally goes with the knowledge that wrinkles usually are developed on the forehead, around the eyes, the nose and the mouth regions.

5.5 Facial Soft-biometrics Recognition

In this section, we present the remaining steps in our facial attributes recognition method. First, we perform the correlation-based Feature Selection on our descriptions. Then, we feed these selected features to Random Forest for attribute recognition. We note that these two steps are common and useful steps in many recognition tasks and contributions in these fields are out of the scope of this work.

5.5.1 Correlation-based Feature Selection

Feature subset selection is the process of identifying and removing as much irrelevant and redundant information as possible (Hall, 1999). There are mainly two types of feature selection methods, *the filter* methods which use heuristics based on general characteristics of the data to evaluate the merit of feature subsets, and *the wrapper* methods which use an induction algorithm along with a statistical re-sampling

technique such as cross-validation to estimate the final accuracy of feature subsets (Kohavi, 1995). We choose a filter method for feature selection, named the Correlation-based-Feature-Selection (CFS) (Hall, 1999), because the filters operate independently of learning algorithm and are generally much faster than wrappers. The chosen CFS filter comprises of two parts, a feature correlation measure using the Pearson's correlation coefficient, and a Best-First heuristic search algorithm which moves through the search space by greedy hill-climbing augmented with a backtracking facility. In practice, we perform feature selection for all the three facial attributes, the gender (labeled as male and female), the ethnicity (labeled as Asian and non-Asian) and the age (labeled in two groups, more than 25 and less than 26). After Feature selection, we retain a subset of 10 to 20% of the original features, for each description. Thus, the feature selection procedure significantly reduces the size of the original features.

5.5.2 Random Forest Classification/Regression

Random Forest is an ensemble learning method that grows many decision trees $t \in \{t_1, \ldots, t_T\}$ considering an attribute (Breiman, 2001). To estimate the attribute from a new instance represented as a feature vector, each tree gives a decision result and the forest does the overall estimation. In growing of each tree, two types of randomness are introduced. First, to make the training set, a number of Ninstances are sampled randomly with replacement from the original data. Then at each node of the tree, a constant number of m (m << M) variables are randomly selected, and the best split on these mvariables is used to split the node. The process goes on until the resulted subsets of the node are totally purified in the label. The performance of the forest depends on the correlation between any two trees, and the strength of each individual tree. The forest error rate increases when the correlation decreases, or the strength increases. Reducing m reduces both the correlation and the strength. Increasing it increases both. Thus, an optimal m is needed for the trade-off between the correlation and the strength. In Random Forest, the optimal value of m is found by using the oob-error rate (out-of-bag-error rate). For making the overall decision, in classification work, the forest predicts the attribute with majority voting. The classification mode of Random Forest is designed for instances with discrete class labels, such as the Gender and Ethnicity labels. While in regression tasks, it takes the average of predictions. The regression mode of Random Forest is designed for instances with continuous class labels, such as the Age labels. Thus, in our work, we use Random Forest in classification mode for Gender and Ethnicity recognition, and in regression mode for Age estimation.

5.6 Experiments

Our experiments are carried out on the Face Recognition Grand Challenge 2.0 dataset (Phillips et al., 2005). The dataset contains 4007 3D near-frontal face scans of 466 participants, where 203 are female and 263 are male, 102 are Asian and 354 are non-Asian. Their age ranges from 18 to 70, with 107 subjects

under 26 years old and 359 subjects above 25. With the FRGC2.0, two types of experiments are carried out:

- \hookrightarrow Expression-Dependent Experiment uses the 466 earliest scans from FRGC2.0 for training and testing. The majority of the scans in this subset are neutral. This data subset leads to a possible study of the facial attribute recognition when imposing a neutral expression.
- \hookrightarrow Expression-Independent Experiment involves the whole 4007 scans of FRGC2.0 (where more than 40% of the scans are expressive). This makes possible to test the robustness of the approach against facial expression variations.

We use the *Leave-One-Person-Out (LOPO)* cross-validation approach in all our experiments, where each time the scans of one subject are used for testing, and the scans of the rest subjects are used for training. Each subject is tested equally only once and the experiments are conducted in a subject-independent fashion. Thus, there are altogether 466 folds in the cross-validation. There are two major reasons for choosing this experimental setting, the first is its similarity to real-world applications, and the second is it allows training with a maximum number of scans. To establish a comparative study with the previous studies, we will report also the results using person-independent 10-fold cross-validation.

Gender Classification Experiments

Gender classification is to automatically label a query, a 3D face scan in our case, into Male and Female. In the experiments, we first perform LOPO gender classification with Random Forest on the original extracted features. Then, we perform correlation-based feature selection on the original features and carry out the experiments with the selected features. After that, we perform the experiments in consideration of ethnicity and age in the *Ethnicity-specific* and *Age-specific* settings, respectively. For *Ethnicity-specific*, we separate the 466 subjects into Asian group (112 subjects) and non-Asian group (354 subjects) first, and then perform the LOPO experiments on these subsets, separately. For *Age-specific*, we separate the 466 subjects into an older group (\geq 26 years, 107 subjects) and younger group (\leq 25 years, 359 subjects) first, and then perform LOPO experiments on the younger and older groups, separately. We have also done the experiments considering both ethnicity and age. In the *Eth.& Age-specific* setting, we perform experiments within the scans of the same ethnicity and age groups, described above.

The Gender classification accuracy are shown as bar-plots in Figure 5.5. The y-axis shows the classification rate following the LOPO settings. The x-axis shows the different experiments. The left panel corresponds to the Expression-Dependent experiments, the right one shows the results when tolerate facial expression variations (Expression-Independent experiments). With the 466 scans in the Expression-Dependent experiments, the original features achieve > 85% gender classification rate for each description. With the feature selection step, the results are improved by 2 - 5%. Now, when considering the ethnicity

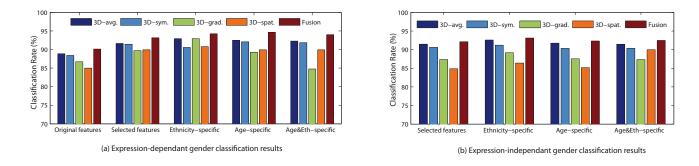


FIGURE 5.5: Gender classification results under Expression-dependent and Expression-Independent settings. Features, 3D-avg.: Averageness — 3D-sym.: Bilateral Symmetry — 3D-grad.: Gradient — 3Dspat.: Spatial — Fusion: their fusion by concatenation. Features processing, Original features: No feature selection applied — Selected features: Correlation-based features selection applied before classification. Settings, Ethnicity-specific: Selected features within each ethnicity group — Age-specific: Selected features within each age group — Age&Eth-specific: Selected features within the same ethnicity and age group.

information in the *Ethnicity-specific* classification setting, the results are improved, in general. These results indicate that Asian and non-Asian show different gender patterns. When considering the age information in the Age-specific protocol, a more significant improvement is shown. This result shows that people of different age have different gender related patterns. In other worlds, human beings' gender patterns correlate to their age. When considering both *Ethnicity-specific* and *Age-specific*, termed Age&Eth-specific, the accuracy is generally higher than the Feature Selection and quite comparable to *Ethnicity-specific* and *Age-specific*. With these results, we also find that the fusion of the features always outperforms the descriptions taken individually. The highest gender classification rates, 94.64%and 94.21%, are achieved by the Fusion under the Age-specific and Ethnicity-specific settings, respectively. These findings are furthermore confirmed in the Expression-Independent settings. As shown on the right panel of Figure 5.5, for each description, the gender classification performance is always higher when considering Ethnicity and Age information. The fusion of these features always outperforms each individual description, and achieves an 93.13% accuracy in the *Ethnicity-specific* setting. These results show also that the expression variations affect slightly the performances. Among the four descriptions, generally, the 3D-avg. descriptor, which captures the shape difference to a given template face, achieves the highest performance. This confirms the studies on sexual dimorphism (Vicki et al., 1993) which claim that Male and Female faces present different morphological features, in their facial shapes. Also, the 3D-sym. descriptor, gives a confirmation on asymmetry differences related to the gender groups (Liu and Palmer, 2003). In addition to these confirmations, this experiment shows the relationship between the gender patterns to two influencing factors, the age and the ethnicity.

Ethnicity Classification Experiments

Ethnicity classification consists on automatically label a query instance into corresponding ethnicity class (Asian or non-Asian groups in the present study). Similarly to the experiments conducted in section 5.6 for Gender classification, an LOPO experiment is conducted using the original features, then the selected features and a study on *Gender-specific* and *Age-specific* are conducted under the following Expression-Dependent and Expression-Independent settings.

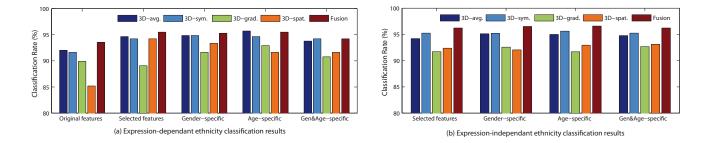


FIGURE 5.6: Ethnicity classification results under Expression-dependent and Expression-Independent settings. Features, 3D-avg.: Averageness — 3D-sym.: Bilateral Symmetry — 3D-grad.: Gradient — 3D-spat.: Spatial — Fusion: their fusion by concatenation. Features processing, Original features: No feature selection applied — Selected features: Correlation-based features selection applied before classification. Settings, Gender-specific: Selected features within each gender group — Age-specific: Selected features within the same gender and age group.

The ethnicity classification results are shown in Figure 5.6. As shown in the left panel, under the Expression-Dependent settings, the results from the original features are always higher than 85%. The feature selection process improves the results with 2% - 7% compared to the previous results. It shows the capability of the feature selection method in ethnicity classification, as outlined in gender classification. Under the *Gender-specific* and *Age-specific* settings, the results are slightly higher than the previous result. This shows that the Male and the Female have different ethnicity related patterns. In addition, it indicates that people of different age have different ethnicity related patterns. Here, the highest ethnicity classification rates of 95.71% and 95.49% are achieved by the 3D-avg. description and the fusion, respectively. Again, like in gender classification, the fusion of these features always outperforms the individual description. These results are confirmed in the right panel of Figure 5.6 with a higher accuracy of 96.6%. This demonstrates the robustness of the proposed approach against the facial expressions in ethnicity classification. Roughly speaking, according to the results presented above, Ethnicity (Asian and non-Asian) classification is influenced by gender and age factors. Here also, the 3D-avg. description achieves higher accuracy, compared to the remaining descriptions. It confirms the findings of previous studies (Farkas LG, 2005) (Alphonse et al., 2013) that a significant morphological differences exist between Asian and non-Asian faces. In addition, according to the results in Figure 5.6, the bilateral asymmetry (3D-sym.) can play an important role in Ethnicity classification.

Age Estimation Experiments

Given a query, estimating its Age consists of automatic label with an estimated age or an age group/range. In the following, we use Random Forest in regression mode to estimate the exact age of a query instance. Again, The LOPO experimental protocol is used for training and testing. Similarly to the previous experiments for Gender and Ethnicity classifications, here again, we compare the results achieved with the original features, results from the selected features and results reported under *Gender-specific* and Ethnicity-specific settings. In feature selection, we use a different age group partition here than in Agespecific experiments. The 466 subjects are divided into two age groups, one ≥ 23 years with 162 subjects, and another group < 22 years with 304 subjects. This partition can better balance the number of scans in the two groups. It also goes with the idea that the craniofacial growth stops at the age of about 20, and faces convey different aging morphology before and after this age. For *Gender-specific* setting, the 466 subjects are separated into Male (263 subjects) and Female groups (203 subjects) first, and then we experiment on each group separately. For *Ethnicity-specific* setting, we separate the 466 scans into Asian group (112 subjects) and Non-Asian group (354 subjects) first, and then do experiments on them separately. The age estimation accuracy is typically measured by the mean absolute error (MAE) and the cumulative score (CS). The MAE is defined as the average of the absolute errors between the estimated age and the ground truth age, while the CS criteria, proposed firstly by (Xin et al., 2007) in age estimation, shows the percentage of cases among the test set where the absolute age estimation error is less than a threshold. In this work, the experimental results are shown as MAEs in Figure 5.7.

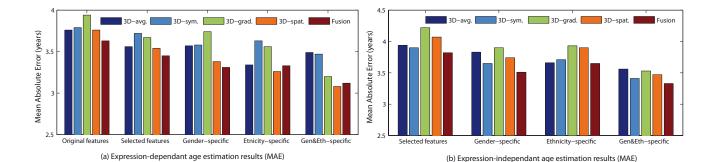


FIGURE 5.7: Age estimation accuracy under Expression-dependent and Expression-independent settings.
Features, 3D-avg.: Averageness — 3D-sym.: Bilateral Symmetry — 3D-grad.: Gradient — 3D-spat.: Spatial — Fusion: their fusion by concatenation. Features processing, Original features: No feature selection applied — Selected features: Correlation-based features selection applied before classification. Settings, Gender-specific: Selected features within each gender group — Ethnicity-specific: Selected features within each gender group — Ethnicity group.

Under the Expression-Dependent settings, the MEAs for all the descriptions are always < 4 years. After feature selection, the errors decrease which confirms again the usage of feature selection in our approach. Again, the errors decreases when testing under the *Ethnicity-specific* and the *Gender-specific* protocols. It means that **different ethnicity have different aging patterns**, and also, **Male and Female** people has different aging patterns. The overall effect of gender and ethnicity information in age estimation is evaluated in the *Gen.&Eth.-specific* setting. The MAEs are even lower than the ones under the *Ethnicity-specific* and *Gender-specific* settings. It demonstrates that the combination of gender and ethnicity information gives the strongest improvement to age estimation performance. The lowest MAEs are achieved in the *Gen.&Eth.-specific* setting, by **3D-spat.** and **Fusion** with 3.08 and 3.12 years, respectively. Under the Expression-Independent experiments, same observations are shown in the right panel of Fig 5.7, where arbitrary expressions could be conveyed by the participants. We notice, despite the facial expression variations, which affect significantly the facial shape, our algorithm still provides high accuracy. The Expression-Independent experiments have also confirmed that the improvement of performance is the most significant when using the gender and ethnicity information together. Also, the *Fusion* of the descriptions always shows better performance compared to separate descriptions. It yields a 3.33 years MAE under the Gen&Eth-specific setting on the whole FRGC2.0 dataset.

| Fusion/Age group | ≤ 20 | (20, 30] | (30, 40] | > 40 | All |
|-------------------------------|-----------|----------|----------|-------|------|
| Expression-dependent | | | | | |
| Original features | 3.93 | 2.29 | 7.03 | 24.45 | 3.63 |
| Selected features | 3.99 | 2.11 | 6.48 | 24.50 | 3.45 |
| Gender-specific | 3.74 | 2.07 | 6.25 | 22.48 | 3.31 |
| Ethnicity-specific | 3.70 | 2.05 | 6.18 | 23.71 | 3.33 |
| Gender and Ethnicity-specific | 3.57 | 1.88 | 6.23 | 21.97 | 3.12 |
| Expression-independent | | | | | |
| Selected features | 3.90 | 2.34 | 6.69 | 23.83 | 3.82 |
| Gender-specific | 3.78 | 2.12 | 6.48 | 21.25 | 3.51 |
| Ethnicity-specific | 3.48 | 2.26 | 6.14 | 23.17 | 3.65 |
| Gender and Ethnicity-specific | 3.44 | 2.04 | 5.98 | 20.26 | 3.33 |
| # of Subjects | 185 | 246 | 20 | 15 | 466 |

| TABLE 5.1: Mean Absolute Errors of the fusion for different age groups under Expression-dependent and |
|---|
| -independent settings. |

To explore in details these results, we show in Table 5.1 the age estimation accuracy in each age group. We find that, no matter in Expression-Dependent or Expression-Independent experiments, the MAEs in this age group are always lower when considering Gender or Ethnicity information, than without such consideration (with the selected features). When considering both Gender and Ethnicity in age estimation, the MAEs in each age group almost reach the lowest (marked in bold). Thus, by giving consideration to Gender and Ethnicity, we have successfully enhanced the age estimation performance for all the age groups. In Table 5.1, we also find that our algorithm performs much better in younger age groups, than in older age groups. Considering the number of training subjects as shown in the last row, it is probably due to the fact that for older age groups, very limited scans are available in the training. To the best of our knowledge, this is the first work which addresses the problem of age estimation from

3D facial shapes. It is also the first work studying the correlations between the three attributes and perform joint estimation, based on three-dimensional data.

Comparison to previous work

As shown in Table 5.2, for gender classification, the works closely related to ours (in term of evaluation settings) are presented in (Toderici et al., 2010), (Ballihi et al., 2012c),(Gilani et al., 2013), and (Wang and Kambhamettu, 2013), which are also tested on the FRGC2.0 dataset. Using all the 4007 scans of FRGC2.0, we achieve 93.11% gender classification rate. Our result is 3% lower than (Gilani et al., 2013) (96.12%). Their approach required accurate landmark detection to compute Surface and Euclidean distances between them, used as features. Our result is comparable to the results reported in (Toderici et al., 2010) (93.5%), and (Wang and Kambhamettu, 2013) (93.7%). For ethnicity classification, the nearest works with ours are presented in (Cheng et al., 2009), and in (Toderici et al., 2010). Using all the 4007 scans of FRGC2.0, we achieve 96.45% ethnicity classification rate. This result is much higher than our previous results reported in (Cheng et al., 2009) (82.38%). Compared to the result reported in (Toderici et al., 2010), our ethnicity classification rate is 2.4% lower. However, their result is based on only the 3676 Asian and White scans of FRGC2.0. In contrast, we work with all the 4007 scans of FRGC2.0, which encounters much more complicated ethnicity challenges.

Further Experiments

The previous experimental section demonstrates that gender, ethnicity and age information are correlated, and their relationship are helpful in each others recognition task. Following this, two questions rise up: (1) To how much extend are they correlated? and (2) How to benefit from their correlations in real-world applications where the ground-truth is unavailable of the other attributes? We address these questions in the following two subsections.

How much are Gender, Ethnicity and Age correlated ? Recall that with feature selection, we have obtained the salient subsets of features for Gender, Ethnicity and Age for each of the four descriptions. Thus, we take these subsets as representations of the Gender, Ethnicity and Age information. With this, we explore two ways to quantify their mutual correlation. The first way is to represent a feature subset as a one-dimensional vector with which the optimal class separation is obtained. Then we measure the correlation directly between such vectors. It will provide a single value for each two attributes, which represents their correlation in the *Decision Level*. To this end, we first apply the Linear Discriminant Analysis (LDA) on each subset. The LDA method is a supervised dimensionality reduction method which projects the data into a subspace where optimal class separation could be obtained. The dimension of the projected subspace equals to the number of classes minus one. In our case, for each of the three attributes, we have always two classes (Male and Female for Gender, Asian and non-Asian for ethnicity, < 23 years and > 22 years for Age). Thus, after LDA projection, for each description, we get one

| | Our work | (Toderici et al., 2010) | (Lu et al., 2006b) | (Cheng et al., 2009) | Author | Ethnicity Classification (Asian | | Our work | (Han et al., 2009) | (Liu and Palmer, 2003) | (Vignali et al., 2003) | (Wu et al., 2007) | (Hu et al., 2010) | (Lu et al., 2006b) | | (Gilani et al., 2013) | | (Xia et al., 2013b) | | (Wang and Kambhamettu, 2013) | (Xia et al., 2013c) | (Toderici et al., 2010) | (Ballihi et al., 2012c) | Method |
|-------------------------|------------------------|-------------------------|------------------------------|-------------------------|-------------|---------------------------------|-------------------------|------------------------|---------------------|--|------------------------|-------------------------------------|--------------------------------------|------------------------------|-------------------------|------------------------|-------------------------|------------------------|-------------------------|------------------------------|-------------------------|-------------------------|-------------------------|-------------|
| 4007 scans o FRGC2.0 | 466 scans o FRGC2.0 | 3676 scans o FRGC2.0 | 1240 scans in UND and MSU | 4007 scans (FRGC2.0 | Dataset | an / non-Asian) | 4007 scans (FRGC2.0 | 466 scans o FRGC2.0 | 61 scans in GavabDB | 111 full 3D scans | 120 3D scans | 260 needle maps o UND | 729 UND scans - 216 private scans | 1240 scans in UND and MSU | 4007 scans o FRGC2.0 | 466 scans o FRGC2.0 | 4007 scans (FRGC2.0 | 466 scans o FRGC2.0 | 4007 scans (FRGC2.0 | 192 scans of HFB | 4007 scans (FRGC2.0 | 4007 scans of FRGC2.0 | 466 scans o FRGC2.0 | Dataset |
| of Yes | of Yes | of Yes | D No | of No | Auto | | of Yes | of Yes | B No | No | No | of No | + Yes | D No | of Yes | of Yes | of Yes | of Yes | of No | No | of No | of Yes | of Yes | Auto |
| s DSF features | s DSF features | s Wavelets | Grid elements | D LVC features | to Features | | s DSF features | s DSF features | Ge | 9 Variance Ratio | 3D coordinates | $PGA \ features$ | s Curvature | Grid elements | s landmark distances | | s DSF features | s DSF features | 3D coordinates | 3 3D coordinates | $DSF+LBP \ features$ | s Wavelets | s Facial curves | to Features |
| Random Forest | Random Forest | Polynomial- SVM | SVM | membership probability | Classifiers | | Random Forest | Random Forest | RBF-SVM | Linear classifier | LDA classifier | Posteriori Probabilities | RBF- SVM | SVM | LDA classifier | LDA classifier | Random Forest | Random Forest | RBF-SVM | RBF- SVM | Random Forest | Polynomial- SVM | Adaboost | Classifiers |
| 10-fold CV | 10-fold CV | 10-fold CV | 10-fold CV | | Setting | | 10-fold CV | 10-fold CV | 5-fold CV | half training / half testing (100 times) | LOPO | 200 training / 60 testing (6 times) | 5-fold CV | 10-fold CV | 10-fold CV | 10-fold CV | 10-fold CV | 10-fold CV | 5-fold CV | 5-fold CV | LOPO | 10-fold CV | 10-fold CV | Setting |
| $96.45\%\pm 0.033$ | $96.78\%\pm 0.023$ | %66 | 886 | 82.38% | Results | | $93.11\% \pm 0.035$ | $95.06\% \pm 0.027$ | 82.56% | 96.22% | 95% | 93.6% | 94.03% | 818 | 96.12% | 97.05% | 88.12% | 90.99% | 93.7% | 94.8% | 93.27% | 93.5% | 86.05% | Results |
| shape | shape | shape | shape + texture | shape | Modality | | shape | ' shape | shape | shape | shape | shape + texture | shape | shape + texture | shape | shape | shape | shape | shape + texture | shape + texture | shape + texture | shape | shape | Modality |

TABLE 5.2: Comparison with previous studies.

dimension vector for each attribute. In Figure 5.8, we show the distribution of the projected LDA features for each attribute in each description, on the 466 earliest scans of FRGC2.0. Each row of the subfigures shows the distributions of projected LDA features for a facial attribute, and each column of subfigures show the distributions in a facial description. In Figure 5.8, clear separation of different classes is shown for all the three attributes in all the descriptions. It confirms that the feature selection method is able to keep the relevant information. And also, the figure shows the LDA projected features are able to characterizing the three attributes.

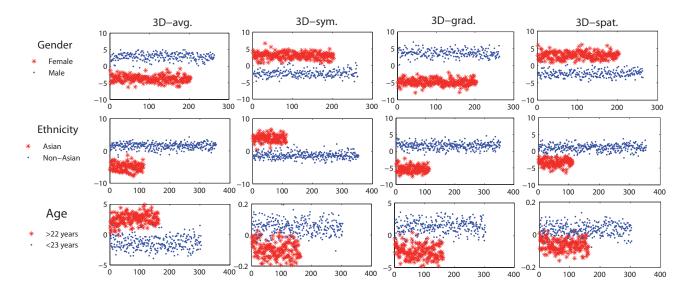
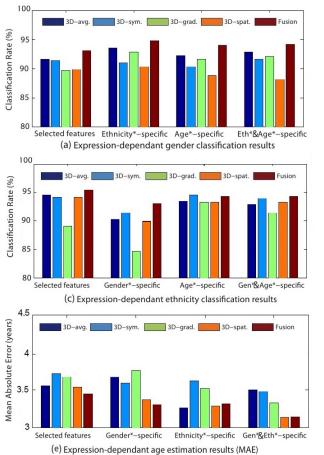


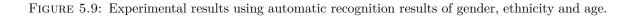
FIGURE 5.8: Distribution of the projected LDA features for gender, ethnicity and age for each face description.

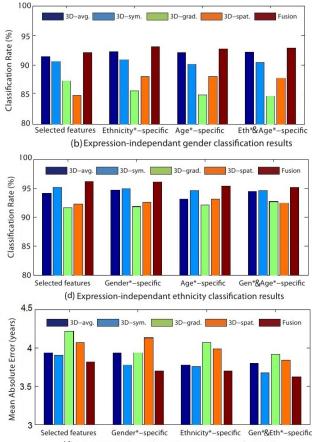
How to benefit from their correlation in real-world applications ?

In realistic applications, we do not have the ground truth of Gender, Ethnicity and Age of the testing instances. While, benefited from the effective recognition performance in the previous section, we can use the recognition results as the gender, ethnicity and age information in the experiments. Thus, instead of using the ground truth, we enroll gender, ethnicity and age information with the predicted gender, ethnicity and age labels given in the previous recognition tasks in the *Feature Selection* setting with the *Fusion* description. The predicted information are termed with * as *Gender**, *Ethnicity** and *Age**. The recognition results are reported in Figure 5.9.

In Figure 5.9 (a) and (b), the gender classification results are presented. In the Expression-dependent experiments, except for the 3D-spat. description, the gender classification results are always higher when considering ethnicity and age information, than without such consideration (in the *Selected features* setting). In the Expression-independent experiments, except for the 3D-grad. description, the gender classification results are always higher when considering ethnicity and age information. With the Fusion description in the *Ethnicity*-specific* setting, we achieve 94.85% Gender classification rate in the







(f) Expression-independant age estimation results (MAE)

Expression-dependent experiments, and 93.08% Gender classification rate in the Expression-independent experiments. The experimental results of ethnicity classification are presented in Figure 5.9 (c) and (d). In both the Expression-dependent and the Expression-independent experiments, the results considering Gender and Age information are comparable or slightly lower, than without such consideration (in the Selected features setting). With the Fusion description, we achieve 94.42% Ethnicity classification rate in the Age^* -specific and the $Gen^* \mathscr{C}Age^*$ -specific settings in the Expression-dependent experiments, and 96.18% Ethnicity classification rate in the *Gen*-specific* settings in the Expression-independent experiments. For Age estimation, the results are shown in Figure 5.9 (e) and (f). Compared to the Feature Selection setting, the MAEs are significantly reduced when considering Gender and Ethnicity information in both the Expression-dependent and the the Expression-independent experiments. With the Fusion description in the $Gen^* \mathscr{C}Eth^*$ -specific setting, we achieve an MAE of 3.13 years in the Expressiondependent experiments, and 3.62 years MAE in the Expression-independent experiments. In summary of these experiments, it is clear that, for Gender and Age recognition, we have obtained higher performance with the automatically recognized information. For Ethnicity recognition, since the training scans are reduced significantly and the classification rate reaches as high as 94.42% (Expression-dependent) and 96.18% (Expression-independent) when considering gender or age information, we still think that using

the automatically recognized information of gender and age is a good strategy in real world application.

5.7 Conclusions

In this chapter, we have presented morphological characteristics that can be extracted using our shape analysis framework of 3D faces. We have explored their relationship with the facial soft-biometrics (gender, ethnicity and age). Again, we have demonstrated the effectiveness of the proposed computational shape analysis framework and its capability to accurately register facial shapes and quantify their divergence. The study presented here provides (1) the first age estimation approach based on the 3D shape of the face⁵; (2) the first joint estimation of the three attributes using four morphological descriptions and their fusion (Xia et al., 2014d) ([J3-s]). We utilize here disjoint ideas from computer vision – Shape Analysis using differential geometry and Machine Learning techniques – and demonstrate the relevance of the proposed approaches in facial attributes estimation.

⁵Our paper (Xia et al., 2014a) won the best paper award in the area of IMAGE AND VIDEO UNDERSTANDING at the International Conference on Computer Vision Theory and Applications, 2014.

Chapter 6

Research Project and Perspectives

Throughout this *habilitation*, we have presented our contributions to the field of 3D shape analysis based on Riemannian methods, with applications to classical problems in pattern recognition. The proposed mathematical representations of 3D shapes which rely on multiple curves are elements of a shape space defined as the invariants under the actions of transformation groups (quotient space). Due to the nonlinearity of the underlying manifolds, tools from differential geometry are used to provide geometric interpretations such as the notion of geodesic (or its length) and its relevance to find the most efficient way to deform one shape into another (or to define the shortest distance between shapes under rigid and non-rigid transformations). The fundamental ingredient of 3D shape analysis is accurate and dense correspondence between shapes before quantifying their difference. The definition of an elastic model allows to achieve jointly accurate registration of 3D shapes and derive an elastic metric which account for bending and stretching of the shapes. In addition, the notion of shooting vector (its norm or its magnitude) along geodesic paths between shapes, captures effectively the deformations between them, through accurate registration. Statistical computation on manifolds, such as the definition of a sample mean of a set of shapes, a sample covariance and explicit statistical models on the tangent space of a sample mean to model the shape class and the variability within the class are suitable for shapes classification and clustering and data completion. Through the multiple experiments conducted on publicly available benchmarks such as FRGC, BU-3DFE, BU-4DFE, Bosphorus, etc., we have demonstrated the interest of the proposed methodology. We have shown also the interest to combine ideas from differential geometry (extraction of Euclidean representations derived from geometric features) with Machine Learning techniques to design efficient classifiers.

However, there are still several question marks and open research avenues from theoretical and practical perspectives. The move to 4D data analyses is still at the beginning, hence, there is an outstanding need to develop processing tools and computational algorithms to process these data and exploit the temporal dimension. From a theoretical point-of-view, the move to analyze dynamic 3D sequences induces fundamental questions such as (1) Which suitable mathematical representation of shapes and

their dynamics (their animations)? (2) How to exploit the dynamics in the analyses? (3) How to compute statistics on shapes (static representations) and animations (dynamic representations)? (4) How to make the representation insensitive to temporal variations? (5) How to design classification and clustering algorithms based on statistical models of representations and their animations? Responses to these questions should bring solutions to make the analyses of shapes and of their motions insensitive (or robust) to,

- → rigid transformations (translation, scaling and rotation) in order to roughly register 3D frames across and between the 3D sequences. Filter out these changes is required for comparing 3D static frames and to define proper distances between frames and sequences;
- \rightarrow non-rigid transformations to finely register 3D frames across the sequences. It is important to propose accurate vertex-level tracking approaches to accurately quantify the motion along the sequences and achieve efficient way to deform one frame into another;
- \hookrightarrow temporal variations caused mainly by the difference in the execution rate and the starting and ending points of the events (activity, emotion, gesture, etc.). Comparing two sequences translates to measure distances between each frame in a **rate-invariant** fashion. The definition of such metric allows accurately comparing, summarizing, and modeling 3D dynamic sequences;
- \hookrightarrow missing and noisy data caused by self-occlusions, pose variations and the 3D (depth) acquisition techniques. Static frame representations should account for this data variability.

It is around these issues that my research project will be organized. Recent advances in 4D facial imaging systems (e.g the Di4D¹ passive stereo photogrammetry technology) allow acquisition of high-resolution (in both spatial and temporal dimensions) facial data. At the same time, the collection of new 4D datasets, such as the Binghamton University 4D Facial Expression databases (Yin et al., 2008) (Zhang et al., 2013), the 4D dataset constructed at University of Central Lancashire (Hi4D-ADSIP) (Matuszewski et al., 2011, 2012), and the dynamic 3D FACS dataset (D3DFACS) for facial expression research (Cosker et al., 2011), open the doors to study the facial deformations and to develop inference strategies for 3D facial shapes and animations. Several applications would benefit from these tools, for example understanding facial expressions, in particular, spontaneous and subtle expressions (called also micro-expressions). Their study requires high-resolution spatio-temporal acquisitions and accurate algorithms to track the facial movements. These tools would also allow to quantify facial distortions from dynamic data, to improve clinical diagnostics and decisions regarding the pathology (or diseases) affecting the face. Following this line, it is required to propose mathematical representations of static shapes and derive special manifolds for 3D frame (static) analysis. Before specify statistical models for full animations, it is necessary to consider some choices for capturing variability in individual shapes. On the underlying representation spaces, one seek to impose dynamical models that capture the variability in shape evolution. The main

¹www.di4d.com

difficulty here is the **temporal variability of the observations**. In fact, the animation data are typically corrupted by variability in execution rates within a class of animation and, thus, causing major problems in the inference process.

From a practical point-of-view, the 3D meshes used in earlier studies, often come from laser-rangefinder scanners or Stereo Photogrammetry cameras of high-resolution which achieve accurate depth measurements. Their use could be a serious limitation in the new research trends called *face analysis in the wild*, as pointed out in recent studies (Wang et al., 2013) (Simonyan et al., 2013) (Sagonas et al., 2013) (Tai, 2014) (Asthana et al., 2014), and in spontaneous facial behavior analysis as pointed out in (Nicolaou et al., 2011)(Bousmalis et al., 2013) and recently in the SFBA² and the FFER³ workshops. With the introduction of a new generation of cost-effective 3D sensors (IR Structured-Light or Time-of-Flight) (Zhang, 2012) capable of dynamic acquisitions, human behavior analysis from dynamic flows under unconstrained conditions is become possible. For instance, the release of Microsoft's Kinect sensors including their Software Development Kit (SDK) have provided a commercially viable approach and hardware platform to capture 3D data in real-time. However, these devices suffer from two major limitations regarding the depth quality that they measure: (1) the low-resolution of depth images due to the large field-of-view of the cameras, and (2) the low-accuracy of depth measurements which results in noisy data. To be able to use these data, one should use appropriate methods and tools to tackle these important issues. Later, we shall introduce our approach to overcome these limitations using subspace methods applied to dynamic flows of 3D data. Our target applications here are face recognition in advertise conditions and analysis of spontaneous emotions from dynamic 3D sequences. Another advantage of using the depth data is its robustness to illumination and pose variations and the ability of the algorithms to track accurately the facial landmarks (eye corners, nose tip, eyebrows, mouth, etc.) as well as the body joints or 3D skeletons (Shotton et al., 2011). The availability of such sparse shape representations (registered landmarks) could be explored as a first level of analyses of human dynamics (including the face movements). At a second level, the **dense shape representations** (sequence of surfaces) would benefit of the results of the previous level, in temporal alignment of sequences for example.

Regarding my experience in the field of face analysis using three-dimensional data and the challenges still open (Phillips et al., 2009), it is natural to continue our investigation using dynamic facial data. Modern face recognition approaches target successful person identification in realistic scenarios, where uncooperative subjects are captured under unconstrained imaging conditions. With the introduction of new 3D sensors capable of dynamic 3D acquisitions, the trend of face analysis from video data is now emerging in 2D as well as in 3D (and sometimes in RGB-D, where RGB refers to the color or 2D and D refers to the depth 3D, respectively). Motivated by these considerations, in this work we propose an effective framework to address face recognition from 3D temporal sequences acquired in adverse conditions, which include internal and external occlusions, pose and expression variations, and talking. Due to the novelty of the proposed scenario, a new database has been collected using a single-view

²http://www.ee.oulu.fi/~gyzhao/ECCV_workshop/

³http://www.vap.aau.dk/ffer14/

structured-light dynamic camera, which allows free movements of the acquired subjects (Figure 6.1), in the field-of-view of the camera. The new database includes several 3D video records (panel A. of Figure 6.1) with freely pose variations, expressions (or talking), external occlusions (glasses, hand, scarf), and full 3D models as shown in panel B. of the same Figure. Despite the over-mentioned limitations regarding the noise and low-resolution data, adding the temporal dimension to 3D acquisitions is motivated by the observation that the face is a deformable 3D surface changing over time, so that using the temporal component can be useful to improve the recognition, especially under adverse acquisition conditions.

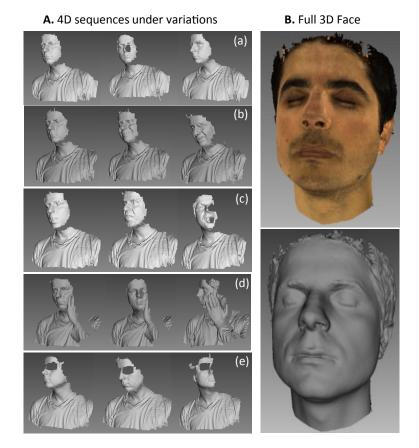


FIGURE 6.1: The new 4D face dataset recently collected for unconstrained 4D face recognition. A.) illusrtaes 3D sequences with expressions.

At least two alternatives could be explored to overcome these limitations and benefit from the available dynamic data: (1) A super-resolution approach which consists on fusing several frames of the 3D video to increase the 3D shape resolution then perform the analysis as proposed recently in (Berretti et al., 2014); or (2) A subspace-based representation (Turaga et al., 2011) which permits to smooth the effect of noisy data, at the same time showing robustness with respect to acquisition variations. In our ongoing research, we adopt and elaborate more on the second solution in the context of two applications: 4D face recognition and analysis of spontaneous emotions from depth-consumer cameras,

 ↔ Unconstrained 4D Face Recognition – As stated earlier, a subspace-based modeling approach is investigated, where the spatio-temporal 3D data is mapped on a finite-dimensional manifold. Each 3D video fragment is considered as an element of a Grassmann manifold (the set of real k-dimensional linear subspaces). This formulation has interesting aspects. First, comparing two subspaces is cheaper than comparing two 3D dynamic fragments; Second, it is more robust to noise and missing data, which are common in realistic scenarios and data from depth sensors. Here, we consider a holistic face descriptor based on shape normals, which do not require any manual/automatic Landmarking step. The facial motion is also modeled and exploited in the recognition process. The 3D temporal sequences are divided into fragments each modeled as a linear subspace in order to embody the shape and the motion of the facial surfaces. In virtue of the Riemannian geometry of the Grassmann manifold, a formulation of the matching between 3D temporal sequences is developed. The underlying representation allows to use differential geometry to develop relevant tools to analyze dynamic 3D data. For example, the use of geodesics to interpolate between subspaces could be an intuitive solution for domain adaptation (Gopalan et al., 2011)(Ni et al., 2013) useful when the test distributions are different from the training distributions. Also, under this representation, it is possible to perform unsupervised clustering over the manifold and compute statistics from populations of dynamic fragments of the same pose, same person, same emotions, same age, or same gender. The shape representation with normals is proposed due to their invariance to location (translation) and resolution (scaling). One important issue to be addressed using this representation is the dense correspondence/tracking of normals across the 3D video, under the variation of expression, pose, missing data, occlusions, etc. Preliminary promising results⁴ were obtained using the proposed framework applied on the new 4D face dataset and on BU-4DFE dataset following the experimental settings of (Sun et al., 2010a).

 \leftrightarrow Analysis of Spontaneous Emotions from Depth-consumer Cameras – Human emotion understanding (Zeng et al., 2009) from facial dynamics (expressions and head movements) and the human body interactions/reactions (Kleinsmith and Bianchi-Berthouze, 2013) is a challenging problem and presents increasing need in many applications. In this research work, we investigate the use of dynamic depth data acquired using cost-effective sensors for emotion analysis. Most of the existing approaches used the facial data to analyze facial expressions and perform classification in discrete space of six universal facial expressions as defined by (Ekman and Friesen, 1978). The datasets used to develop and test these approaches often consider posed (sometimes exaggerated) expressions, i.e the participants are asked to perform one of the six universal expressions. The use of these approaches in real-world applications is difficult, when the user conveys spontaneous emotions involving in general the upper part of the body including his face and hand gestures. We propose to explore the contribution of the upper-body part and its dynamics to perform emotion classification. Again, we adopt the subspace representations of dynamic map-flows to capture the history of the body motions used for emotion (or a group of emotion) detection. Regarding the test datasets, it is very important that psychologists implement the data acquisition settings and perform sequences segmentation. For these reasons, in our ongoing research, we try to use

⁴T. Alashkar, B. Ben Amor, S. Berretti and M. Daoudi, *A Grassmannian Framework for Face Recognition of 3D Dynamic Sequences with Challenging Conditions*, accepted in Sixth Workshop on Non-Rigid Shape Analysis and Deformable Image Alignment (NORDIA), 2014.

Automated analysis of human behavior through visual data has attracted a tremendous interest in the computer vision community. This is due to its huge potential in a wide spectrum of areas, such as human-machine interaction, psychology (Kleinsmith and Bianchi-Berthouze, 2013), surveillance security, health-care and social assistance, and gaming. Beside the verbal communication, the visual data is one of the most important cues in developing systems for understanding human behavior (Mehrabian and Wiener, 1967), ranging from tracking daily activities to classifying emotional states, as well as detecting abnormal and suspicious activities. In this future direction, our goal is to develop computational solutions for human behavior analysis from dynamic depth data. In literature, a vast majority of the features that are extracted to solve this problem often tend to be non-Euclidean manifolds. This means that traditional ideas of comparison and classification need to be generalized to account for the geometry of the manifolds.

 \hookrightarrow Human Motions as Trajectories on Manifolds – Earlier studies in such analyses used videos produced by conventional cameras (Aggarwal and Ryoo, 2011)(Abdelkader et al., 2011)(Chaquet et al., 2013) (Ke et al., 2013) (Veeraraghavan et al., 2009). They analyzed videos in order to exploit visual cues related to the human 'form' (or silhouette) in temporal evolution of images and to capture its dynamics (e.g., using optical flows). However, real-life applications of this approach encounter several difficulties, coming from self-occlusions, pose variations, and the complexity of both imaging environments and activities themselves. Additionally, there are two major challenges which also negatively affect video analysis, (i) the temporal variability caused by differences in execution rates of the motions and periods of them, including arbitrary starting/ending observation times, and (ii) the spatial variability due to interpersonal differences when exhibit similar motion. These were difficult issues when dealing with videos from conventional cameras. The depth maps are independent of human appearance (textures) and provide a more complete human 'form' compared to the silhouette information, explored in the past. They can also help in mitigating the issue of pose variability due to availability of 3D registration methods and the existence of pose-independent features. The relevant question in using depth maps is: How to exploit the depth information in an efficient and robust way? Recently, several approaches have been published in action and activity recognition from depth cameras (Li et al., 2010) (Wang et al., 2013) (Ellis et al., 2013) (Oreifej and Liu, 2013)(Vemulapalli et al., 2014)(Devanne et al., 2014)(Slama et al., 2014). In $[\mathbf{J2}-\mathbf{s}]^6$, we study the problem of classifying actions of human subjects using depth movies generated by the Kinect or other depth sensors. Representing human body as dynamical skeletons, we study the evolution of their (skeletons') shapes as trajectories on Kendall's shape manifold (reviewed in Chapter 2).

⁵L. Ballihi, A. Lablack, B Ben Amor, M. Bilasco, and M. Daoudi, *Positive/Negative Emotion Detection from RGB-D upper Body Images*, accepted for publication in 1st International Workshop on Face and Facial Expression Recognition from Real World Videos (FFER), 2014.

⁶under major revision with IEEE Trans. on Pattern Analysis and Machine Intelligence.

The action data is typically corrupted by large variability in execution rates within and across subjects and, thus, causing major problems in statistical analyses. To address that issue, we adopt a recently-developed framework of (Su et al., 2013) to this problem domain. Here the execution rate changes correspond to re-parameterizations of trajectories, and one uses a parameterizationinvariant metric for aligning, comparing, averaging, and modeling trajectories. The key idea is to use a combination of transported square-root vector fields (T-SRVFs) of trajectories and the standard Euclidean norm. Moreover, we have developed a suite of computational tools for this application domain: smoothing and denoising skeletal trajectories using median filtering, up- and down-sampling actions in time domain, simultaneous temporal-registration of multiple actions, and extracting invertible Euclidean representations of actions. Due to invertibility these Euclidean representations allow both discriminative and generative models for statistical analysis. Action recognition from 3D skeletal data was an excellent application to illustrate our methodology, however, in the future we intend to extend our study to other applications. We will emphasize on facial expression classification from automatic detected 2D and 3D landmarks. The Fig. 2.4, in Chapter 2 provides an example of geodesic path between sets of facial landmarks. We will consider trajectories of shapes to study the facial behavior across time and study the application of our mathematical framework.

↔ Statistical Models for (landmark-based) Shapes and Trajectories – As stated in the previous item, I shall emphasize in my future work on (3D landmark-based) shapes and their motion. The specification of a shape manifold (Kendall's space) and the corresponding metric enables to compare arbitrary trajectories in terms of their shapes, in a rate-invariant way. Additional shape tools, such as the computation of sample mean and sample covariance statistics, and the transfer of deformations using parallel transports becomes straightforward. However, in classification we often need to define statistical models that are tailored to the geometry of that underlying shape space and to specify some probability models for shapes along trajectories. The definition of probability models on shape manifolds and trajectory manifolds will be also explored to perform sequential analysis.

Automated processing and analysis of 3D dynamic data will also open the door to the **large-scale recognition** challenges in which it is important to consider different trade-offs with respect to algorithms efficiency and recognition performance. This topic has received much attention in the computer vision community in the last few years (Taigman et al., 2014), in particular in processing large datasets of images and videos. Hence, there is an outstanding need for developing new computational strategies to adapt the Riemannian methods to fit these requirements. In fact, when the local descriptions provide rich information (high-dimensional features usually represented in Euclidean spaces) and are cheap to compute, the Riemannian methods (involving non-linear spaces) are more costly and provide robustness to several transformations. As presented previously, one possible future direction is to consider two data analysis levels, (1) shape analysis of sparse representations (or landmarks) and (2) shape analysis of dense

representations (or the complete shapes) to tackle the computational cost problem. In human behavior analysis for example, one can exploit the landmark-based representations provided by the depth-consumer cameras such as the skeletal data of the body joints or the 3D Active Shape Model (provided with the Kinect SDK) of the face to derive efficient discriminative and generative models, as a first step. In a second step, the recognition will be restricted to a subset of the large dataset, in which a more complete 3D shape representations are involved.

Applications

In summary, our focus goes to address human (including the face) behavior analysis and recognition in real-world conditions. We explore the use of dynamic depth-flows acquired by cost-effective sensors and high quality 3D sequences of meshes collected using more sophisticated scanners. Despite the temporal dimension, the 3D sequences are independent of human appearance and provide a more complete human 'form' (meshes, depth-maps, landmarks, etc.) compared to the 2D silhouette information, used in the past (Abdelkader et al., 2011). The extracted representations often live on non-Euclidean spaces (Kendall's shape space, shape space of parametrized curves or surfaces, Matrix manifolds, etc.) which required the use of tools from differential geometry to process shapes and their animations. Through the geometric modeling, computing geodesics and interpolate between the shapes is an essential ingredient for comparing, deforming and averaging these elements.

Many applications would be targeted with the developed tools and strategies, in the future. For example, diagnostic, therapy and tracking of diseases like Autism. It is well established nowadays the important role of motion-controlled gaming to improve autistic kid's life by limiting their disables and attract (force) them to communicate with others by sharing space, etc. The above-mentioned ideas could be adapted to track the autism behavior evolution across weeks, months and perhaps years and can provide quantitative statistics, to help doctors and families get clearer picture on the temporal evolution of the children with autism. Other applications exploiting the hand gestures could be also addressed using our recent developments. In fact, new ToF cameras like Softkinetic⁷ cameras (or Creative Senz3D⁸ cameras) and their middle-ware tend to extract and track accurately skeletal data from hands which makes possible the analyses of dynamic shapes as we have proposed in [J2-s]. This open a new avenue to sign language interpretation using the depth data (or the skeletal data) that the cameras provide, for example. We expect that the landmark-based representations automatically estimated and tracked by the depth-cameras will play an important role in shape analysis. In fact, the explicit correspondence between these sparse representations and the dense information (point clouds, meshes, surface patches, etc.) could be exploited to design up-down shape analysis approach linking the shape manifolds of sparse shape representation and the dense shape representations. Finally, our aim is to see our methodologies implemented for those end-users applications!

⁷www.softkinetic.com/

⁸us.creative.com/p/web-cameras/creative-senz3d

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Part III

Selected Publications

scalar fields show a high dimensionality. Linear Discriminant Analysis (LDA) transformation is applied to the deuse feature space. Two methods are then used for classifications: 1) 3.20 r motion extraction with temporal Hidden Markov model (HMM) and 2) mean deformation capturing with random forest. While a dynamic HMM on the features is trained in the first approach, the second one computes mean deformations under a window and applies multiclass random forest. Both of the proposed dynamic HMM on the scale of a study shows the second one of the proposed and applies multiclass random forest. Both of the proposed Manuscript received July 31, 2013; revised February 14, 2014; accepted February 18, 2014. This work was supported by ARR through the 3-D Face Analyzer project under Grann ARR. 10-INTB-030. This paper was recommended by Associate Editor J. Su. B. Ben Annor, H. Drina, and M. Daoudi are with the Institut Miras-Télécom/Télécom Lille, Laboratorie d'Informatique Fondamentale de Lille, Lille LIFL UMR 8022. France (comit: bothbathcheannor/fereteon-Bille fr; hassen.drine@telecom-lille.fr; mohamed.daoudi@telecom-lille.fr). Abstract—In this paper, we present an automatic approach for facial expression recognition from 3-D video sequences. In the proposed solution, the 3-D faces are represented by collections of radial curves and a Riemannian shape analysis is applied A. Srivastava is with the Department of Statistics, Florida State University, Tallahassee, FL 32306 USA (e-mail: asrivastava@fsu.edu). S. Berretti is with the Department of Information Engineering, University of Florence, Florence 50139, Italy (e-mail: stefano.berretti@unifi.it). of verbal and nonverbal messages in communicating feelings paper by Mehrabian and Wiener [1], the relative importance investigated by psychologists, among others. In a seminal (by detecting driver fatigue, for example), and so on. corresponding radial curves of two faces. As the resulting dense to effectively quantify the deformations Markov model (HMM), random forest, Riemannian geometry, directions of the geodesic paths constructed between pairs of expressions in a given subsequence of 3-D frames. This interaction, psychology, computer graphics, transport security applications in several different areas, such as human-machine temporal analysis recognition from 3-D video sequences. results and classification schemes on the scalar fields showed comparable Digital Object Identifier 10.1109/TCYB.2014.2308091 B. Ben Amor and H. Drira contributed equally to this paper. Color versions of one or more of the figures in this paper are available \bigcirc VER THE last few years, automatic recognition of facial expressions emerged on a factor for the second obtained from the dense scalar field, which denotes the shooting The importance of facial expressions was first realized and Index Terms-4-D data, expression recognition, Hidden 4-D Facial Expression Recognition by Learning expressions emerged as a field of active research, with outperformed Mohamed Daoudi, Senior Member, IEEE, and Anuj Srivastava, Senior Member, IEEE Boulbaba Ben Amor, Member, IEEE, Hassen Drira, Stefano Berretti, Member, IEEE, I. INTRODUCTION earlier studies on facial expression Geometric Deformations induced by the facial considerations, there has been a progressive shift evidence that face-to-face communication is governed by the collections of large datasets that include temporal time, advances and the Bosphorus 3-D face database [13]. points as described by a set of action units. vocal, and visual elements, respectively, in communications. 7%-38%-55% rule that balances the relevance of verbal, and attitude is described. In particular, they have provided

facial expressions can be coded through the movement of face consistent across different ethnicity and cultures. The presence in the late 70s. Through his experiments, it is demonstrated knowledge that facial expressions are highly dynamical proframes [4]. This section of paper demonstrates a collective These results, in turn, inspired many researchers to analyze facial expressions in video data, by tracking facial features for scientific analysis. Ekman and Friesen [3] also showed that of these prototypical facial expressions is now widely accepted the neutral one, that are universally recognized and remain anger, disgust, fear, happiness, sadness, and surprise, plus that there is an universal set of facial expressions representing conducted the first systematic studies on facial expressions gestures, postures, facial expressions) also play an important role. Starting from a different point of view, Ekman [2] The nonverbal elements related to the body language (e.g., later papers, it still provides an indication that the words and Despite this rigid quantification has since been refuted in and measuring the amount of facial movements in video tone of the voice form only a part of human communication.

this latter research subject is gaining momentum thanks to the of 3-D scans to lighting conditions and pose variations give can be studied comprehensively by analyzing temporal dy-University 3-D facial expression database (BU-3-DFE) [12] recent availability of public 3-D datasets, like the Binghamton to 3-D in performing facial shape analysis for recognition support to the use of 3-D and 4-D data. Motivated by these as 4-D data). From this perspective, the relative immunity namics of 3-D face scans (3-D plus time is often regarded of facial muscles. In this approach, the facial expressions temporal deformations of 3-D faces, caused by the actions analysis, it is more natural to analyze expressions as spatiothat, rather than being just a static or dynamic 2-D image improve the recognition performance. We further emphasize cesses, and looking at sequences of face instances can help to [5-9], and expression recognition [10], [11]. In particular in 3-D imaging technology have At sequences permitted the same from 2-D

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and challenges in 3-D face recognition and facial expression to a large number of users, thus opening new opportunities that provide fast albeit low-resolution streams of 3-D data such as the consumer 3-D cameras like Kinect or Asus further by the introduction of inexpensive acquisition devices, includes fully coded FACS. This trend has been strengthened (D3DFACS) for facial expression research [17], which also (Hi4D-ADSIP) [15], [16], and the dynamic 3-D FACS dataset the 4-D dataset constructed at University of Central Lancashire University 4-D facial expression database (BU-4DFE) [14], of 3-D scans (i.e., 4-D datasets), such as the Binghamton full expression sequence that is represented as the composition segment. Then, HMMs are used for temporal modeling of the for the onset temporal segment, and the other for the offse

survey on this subject), then we give a general overview of recognition (see the recent paper in [20] for a comprehensive an overview of existing methods for 4-D facial expression solution and to relate it to the state-of-the-art, we provide face deformations with effective classifiers. To motivate our analysis of 3-D faces that combines scalar field modeling of problem of expression recognition from dynamic sequences of 3-D facial scans. We propose a new framework for temporal recognition [18], [19] Motivated by these facts, we focus in this paper on the

our approach.

A. Related Work

approach basically relies on the use of a generic deformable 3-D scans was proposed by Sun et al. [23], [24]. Their of facial expression recognition from dynamic sequences of focussing on facial expression recognition. sequences of 3-D face scans [19], [21], [22], and some papers with just a few papers performing face recognition from In particular, the first approach addressing the problem The use of 4-D data for face analysis is still at the beginning,

not released for public use. 83 manually annotated landmarks of the BU-4DFE that are database. The main limit of this solution resides in the use of features. Exhaustive analysis was performed on the BU-4DFE the spatial and temporal relationships between the extracted a spatial HMM and a temporal HMM were used to model Markov Model (HMM) is used for classification. In particular, Once spatio-temporal features are extracted, a 2-D Hidden information and provides a robust facial surface representation. temporal feature vector that describes both shape and motion depth scan in the sequence can be represented by a spatiotrajectories (vertex flow) of 3-D face scans. As a result, each the 3-D dynamic facial sequences provide a set of motion 3-D face sequence. Correspondences between vertices across applied to adapt the 3-D deformable model to each frame of a In the temporal analysis, a vertex flow tracking technique is in order to extract a spatio-temporal description of the face. 3-D model whose changes are tracked both in space and time sication, and these frames correspond to the most intense published in [31] for spontaneous expressions. database for posing expressions, and on a new database conducted several recognition experiments on the BU-4DFE features, such as curvatures and polar angles. They and just 15 frames from the onset one are used for clas togram is built for different facial regions using geometric the manual intervention is used to detect the onset

The approach proposed by Sandbach *et al.* [25] exploits the dynamics of 3-D facial movements to analyze expresthe training using two classifiers for each expression: motion fields. GentleBoost classifiers are used in order to motion features using a quad-tree decomposition of several sions. This is obtained by first capturing motion between simultaneously select the best features to use and perform frames using free-form deformations (FFD) and extracting one

expression.

However, frame

have

and movement analysis from a volume of 3-D data. Af-ter fitting the volume data to a cubic polynomial, a hisspatio-temporal feature named Nebula for facial expressions landmarks were used in this paper. methodology for facial expression recognition from dynamic sequences of 3-D scans, with an extended analysis and comto the competing solutions. Fang et al. [29] propose a similar used in [25] and [26], showing improved results with respect database for all expressions and for the subsets of expressions along the sequence. Results are provided on the BU-4DFE LBP on three orthogonal planes is used as face descriptor 4-D data registration and dense correspondence between 3-D expression recognition approach with a particular emphasis on training data were not sufficient for learning HMM, the authors used as spatio-temporal features to train HMM, and since the level curves of two 3-D facial shapes. These features are then curves are parameterized using the arclength function. The Le et al. to capture the shape of 3-D facial models. The level expressions are reported. results on the BU-4DFE database using the six universal facial An extension of this paper has been presented in [20], where (i.e., happy, angry, and surprise) of the BU-4DFE database and closing of the sequence again with a neutral expression followed by the activation of the expression, the maximum intensity of the expression, deactivation of the expression offset. These model a sequence with an initial neutral segment of four temporal segments, such as neutral, onset, apex, and spin images and MeshHOG. However, 12 manually annotated ICP and more sophisticated mesh matching algorithms, meshes along the temporal line. The variant of the local binary the corresponding normalized segments, partitioned from these Chamfer distance is applied to measure the distances between Experiments were reported for three prototypical expressions parison of different 4-D registration algorithms, including patterns (LBP) descriptor proposed in [28], which computes happy, sad, and surprise sequences of the BU-4DFE database come the overfitting problem. Results were reported for the proposed to apply the universal background modeling to over-In [26], a level curve based approach is proposed by Recently, Reale et al. [30] have proposed a new 4-D Fang et al. [27] propose a fully automatic 4-D facial , 8

from dynamic sequences are still preliminary, being semiautotions specifically tailored for 4-D facial expression recognition of expressions matic, or are capable of discriminating between only a subse From the discussion above, it becomes clear that the solu

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BEN AMOR et al.: 4-D FACIAL EXPRESSION RECOGNITION

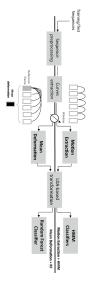


Fig. 1. Overview of the proposed approach. Four main steps are shown: sequence preprocessing and extraction of the radial curves; motion extraction and Mean deformation computation: dimensionality reduction with LDA; HMM and random forest-based classification. Note that both train and test sequences can go through the upper and lower path in the block diagram.

B. Our Method and Contributions

Due to the increasing importance of shape analysis of objects in different applications, including 3-D faces, a variety of mathematical representations and techniques have been suggested, as described above [20], [24], [29]. The difficulty in analyzing shapes of objects comes from the following facts.

- Shape representations, metrics, and models should be invariant to certain transformations that are termed shape preserving. For instance, rigid motions and reparameterizations of facial surfaces do not change their shapes, and any shape analysis of faces should be invariant to these transformations.
- Registration of points across objects is an important ingredient in shape analysis. Specifically, in comparing the shapes of faces, it makes sense that similar biological parts are registered to each other across different faces.

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Furthermore, it is important to use techniques that allow a joint registration and comparisons of surfaces in a comprehensive framework, rather than in two separate steps. These two issues, invariance and registration, are naturally handled using Riemannian methods where one can choose metrics that are invariant to certain transformations and form quotient spaces (termed shape spaces) by forming equivalence classes of objects that have the same shape. The elastic Riemannian metric used in this paper provides a nice physical interpretation of measuring deformations between facial curves using a combination of stretching and bending. These elastic deformations are captured by the dense scalar field (DSF) features used in this paper for classifications. In summary, the main motivation of using a Riemannian approach is to perform registration that matches corresponding anatomical features, and obtain deformation fields that are physically interpretable.

Based on these premises, in this paper we extend the ideas presented in [32] to propose an automatic approach for facial expression recognition that exploits the facial deformations extracted from 3-D facial videos. An overview of the proposed approach is given in Fig. 1. In the preprocessing step, the 3-D mesh in each frame is first aligned to the previous one and then cropped. From the obtained subsequence, the 3-D deformation is captured based on a DSF that represents the 3-D deformation between two frames. Linear Discriminant Analysis (LDA) is used to transform derived feature space to an optimal compact space to betre separate different expressions. Finally, the expression classification is performed

> in the following two ways: (1) Using the HMM models for temporal evolution; and (2) using mean deformation along a window with random forest classifier. Experimental results show that the proposed approaches are capable of improving the state-of-the-art performance on the BU-4DFE database. There are three main contributions in this paper which are as follows.

- Novel DSFs defined on radial curves of 3-D faces using Riemannian analysis in the shape spaces of curves. These scalar fields accurately capture deformations occurring between 3-D faces represented as collections of
- radial curves.

 A new approach for facial expression recognition from
 J dynamic sequences that combines the high descriptiveness of DSFs extracted from successive 3-D scans of a sequence with the discriminant power of LDA features using HMM and multiclass random forest.
- using ruyiv and multiclass railoon lorest. An extensive experimental evaluation that compares the proposed solution with the state of the art methods using a common dataset and testing protocols. The results show that our approach outperforms the published state-

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of-the-art results. The rest of the paper is organized as follows. In Section II, we present a face representation model that captures facial features relevant to categorizing expression variations in 3-D dynamic sequences. In Section III, the dynamic shape deformation analysis using LDA and classification using HMM and multiclass random forest are addressed. The main characteristics of the BU-4DFE and the preprocessing operations performed on the face scans are described in Section IV, with the experimental results and the comparative evaluation performed on the BU-4DFE database reported and discussed in the same Section. Finally, conclusions and future research directions are outlined in Section V.

II. GEOMETRIC FACIAL DEFORMATION

One basic idea to capture facial deformations across 3-D video sequences is to track mesh vertices densely along successive 3-D frames. Since, as the resolution of the meshes varies across 3-D video frames, seatabiling a dense matching on consecutive frames is necessary. For this purpose, som *et al.* [23] proposed to adapt a generic model (a tracking model) to each 3-D frame using a set of 83 predefined facial landmarks to control the adaptation based on

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radial basis functions. A second solution is presented by Sandbach *et al.* [25], [33], where the authors used an existing nornigid registration algorithm (FFD) [34] based on B-splines interpolation between a lattice of control points. In this case, dense matching is a preprocessing step used to estimate a motion vector field between 3-D frames, *t* and *t*-1. The problem of quantifying subtle deformations along the sequence still remains a challenging task, and the results presented till remains a challenging task three facial expressions: happy, angry and surprise.

is the Hilbert space of all square-integrable maps of the type using SRVF representation is that under this representation the elastic metric becomes the standard \mathbb{L}^2 metric and an imated by an indexed collection of radial curves β_{α} , where the space are straight lines. is actually a vector space and geodesics between points in this $q: [0, 1] \rightarrow \mathbb{R}^3$. This space under the natural \mathbb{L}^2 inner product a bijection (up to a translation), and the space of all SRVFs of between their SRVFs. The mapping from a curve β to q is identical reparameterization of curves preserves the \mathbb{L}^2 norm root velocity function (SRVF) [see (1)]. the facial curves using a new function q, called the squareensuing analysis simplifies. As described in [36], we represent metric under which this inequality becomes equality and the problematic. The solution comes from choosing a Riemannian \mathbb{L}^2 norm, the quantity $\|\beta_1 - \beta_2\| \neq \|\beta_1 \circ \gamma - \beta_2 \circ \gamma\|$, which is diffeomorphism from [0, 1] to itself), then under the standard of curves. If γ is a reparameterization function (typically a maps directly is that they change with reparameterizations by these maps. The problem in studying shapes using these $\beta : [0, 1] \rightarrow \mathbb{R}^3$ and our goal is to analyze shapes represented representing facial curves as absolute continuous maps from work is used to study shapes of these curves. We start by by a collection of radial curves and a Riemannian framefrom Hilbert space analysis. A facial surface is represented mathematical setup for the shape theory offered here comes have shown their effectiveness in facial biometrics [35]. The captures its shape can be seen as a parameterization of the facial surface by an ordered set of radial curves that locally that originate from the tip of the nose. Approximating the facial surface through a set of parameterized radial curves duced by different facial expressions, we propose to represent angry, and surprise. in [25] are limited to just three facial expressions: happy facial surface. Indeed, similar parameterizations of the face With the proposed representation, a facial surface is approx-In order to capture and model deformations of the face in-The advantage of the

imated by an indexed collection of radial curves β_{a} , where the index a denotes the angle formed by the curve with respect to a (createring radial curve, in particular, the reference radial curve in (i.e., the curve with a = 0) is chosen as oriented along the vertical axis, while the other radial curves are separated from each other by a fixed angle and are ordered in a clockwise manner. As an example, Fig. 2(a) shows the radial curves we separated for a sample face with happy expression. To extract we the radial curves, the nose this happy expression. To extract we the radial curves, the nose this happy expression is to the each face scan is rotated to the upright position so as to the same index in different face scans (the preprocessing the same the same index in different face scans (the preprocessing the same the same the same the same the same the same the same

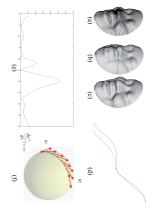


Fig. 2. Figure illustration. (a) Extracted natial curves. (b) and (c) Radial curve on a neutral face and the correspondent curve on the same face with happy expression, respectively. (d) Two radial curves plotted logether. (e) Values of the magnitude of $\frac{1}{2d_1-d_1}(d)$ computed between the curves in (d) are reported for each point & dr the curves. (d) Panallel vector field across the geodesic between q_1 and q_2 in the space of curves C.

(c), two radial curves at $\alpha = 90^{\circ}$ in the neutral and happy scans of the same subject are shown. As emerged Fig. 2(d), facial expressions can induce consistent variations in the shape of corresponding curves. These variations change in strength from expression to expression and for different parts of the face. In order to capture these variations effectively, a DSF is proposed that relies on a Riemannian analysis of facial shapes. Considering a generic radial curve β of the face, it can be parameterized as $\beta: I \rightarrow \mathbb{R}^3$, with I = [0, 1] and mathematically represented through the square-root velocity function (SRVF) [36], [37], denoted by q(t), according to

$$q(t) = \frac{\beta(t)}{\sqrt{\|\hat{\beta}(t)\|}} \quad t \in [0, 1].$$
(1)

This specific representation has the advantage of capturing the shape of the curve and makes the calculus simpler. Let us define the space of the SRVFs as $C = \{q : T \to \mathbb{R}^3, \|q\| = 1\}$ $|I| \subset \mathbb{L}^2(I, \mathbb{R}^3)$, with $\|\cdot\|$ indicating the \mathbb{L}^2 norm. With the \mathbb{L}^2 metric on its tangent space, C becomes a Riemannian manifold. Basically, with this parametrization each radial curve is represented on the manifold C by its SRVF. According to this, given the SRVFs q_1 and q_2 of two radial curves, the shortest path ψ^* on the manifold C between q_1 and q_2 (called *geodesic path*) is a critical point of the following energy function:

$$E(\psi) = \frac{1}{2} \int ||\dot{\psi}(\tau)||^2 d\tau \tag{2}$$

where ψ denotes a path on the manifold C between q_1 and q_2 . r is the parameter for traveling along the path ψ , $\psi \in T_{\psi}(C)$ is the tangent vector field on the curve ψ on C, and ||.|| denotes the \mathbb{L}^2 norm on the tangent space.

Since the elements of C have a unit \mathbb{L}^2 norm, C is a hypersphere in the Hilbert space $\mathbb{L}^2(I, \mathbb{R}^3)$. As a consequence, the geodesic path between any two points $q_1, q_2 \in C$ is simply

as $\frac{d \sqrt{*}}{4}$ of the magnitude computed for each point t of the curves q_0^{1} of radial curves. to capture deformations between two corresponding radial as reported on the x-axis, while the magnitude of the vector is calculated using (5) and the plot of the magnitude of this BEN AMOR et al.: 4-D FACIAL EXPRESSION RECOGNITION and q_{α}^2 ; let T be the number of sampled points per curve, and curves β_{α}^{1} and β_{α}^{2} of two faces approximated by a collection along the geodesic ψ^* the remaining vectors obtained by parallel transport of $\frac{d\Psi}{d\tau}|_{\tau=0}$ geodesic path connecting these two points on the hypersphere Hilbert space through their SRVFs q_1 and q_2 , and shows the field is reported on the y-axis). Finally, Fig. 2(f) illustrates the 50 points are used to sample each of the two radial curves person. The amount of deformation between the two curves two curves lie at the same angle α and belong to the same curves are reported together in Fig. 2(d), where the amount of In Fig. 2(b) and (c), two corresponding radial curves (i.e. tation is its tangent vector field is equal to 0, $\frac{dV^*}{d\tau}$ is parallel along the equation: other words $q_1 = q_2$. In this case, for each τ , $\psi^*(\tau) = q_1 = q_2$ this hypersphere, $\psi^* : [0, 1] \to \mathcal{C}$. This is given by given by the minor arc of the great circle connecting them on we define the function f by $|\Lambda|$ be the number of curves used per face. According to idea to map the two radial curves on the hypersphere C in the vector at each point of the curve is reported in Fig. 2(e) (i.e. deformation between them can be appreciated, although the face of the same person are highlighted, respectively. These radial curves at the same angle α) on a neutral and a happy face with happy expression and all the extracted radial curves loss of information. Accordingly, (4) becomes geodesic ψ^* and one can represent it with $\frac{d\psi^*}{d\tau}|_{\tau=0}$ without any $sin(\theta) = 0$ if the distance between the two curves is zero, in where $\theta = d_{\mathcal{C}}(q_1, q_2) = cos^{-1}(\langle q_1, q_2 \rangle)$. We point out that field whose covariant derivative is zero. According to this The tangent vectors of this geodesic path represent a vector $\frac{nv}{dt}|_{t=0}$ becomes sufficient to represent this vector field with Definition 1: DSF: Let $x_{\alpha}(t) = ||\frac{dy_{\alpha}}{d\tau}|_{\tau=0}(t)||$ be the values Based on the above representation, we define a DSF capable Knowing that on geodesic path, the covariant derivative of The tangent vector field on this geodesic is then written graphical interpretation of this mathematical represen : $[0, 1] \rightarrow T_{\psi}(\mathcal{C})$, and is obtained by the following $\frac{d\psi^*}{d\tau}$ This article has been accepted for inclusion in a future issue of this journal. Content is final as presented, with the exception of pagination $\psi^*(\tau) =$ given in Fig. 2. In Fig. 2(a), we show a sample $\frac{d\tau}{|\tau|} = 0 = \frac{1}{2}$ $d\psi^*$ $f(q_{\alpha}^1, q_{\alpha}^2) = (x_{\alpha}^1, \dots, x_{\alpha}^k, \dots, x_{\alpha}^T)$ - İİ $= \frac{1}{\sin(\theta)} \left(\cos((1-\tau)\theta)q_1 - \cos(\theta\tau)q_2 \right).$ $sin(\theta)$ $-\theta$ $f: \mathcal{C} \times \mathcal{C} \longrightarrow (\mathbb{R}^+)^T$ $\frac{1}{\sin(\theta)} (q_2 - \cos(\theta)q_1) \ (\theta \neq 0).$ $\frac{1}{2}(\sin((1-\tau)\theta)q_1+\sin(\theta\tau)q_2))$ this 3 Æ <u>ل</u> Assuming that $\{\beta_{\alpha}^{l}|\alpha \in \Lambda\}$ and $\{\beta_{\alpha}^{2}|\alpha \in \Lambda\}$ be the collections of radial curves associated with the two faces F^{1} and F^{2} and make an angle α with a reference radial curve on faces F^1 and F^2 , respectively. The initial tangent vector to ψ^* , called also the shooting direction, is computed using (5). Then, we same subject are shown. The values of the scalar field to of the sequences of the six prototypical expressions of the between a neutral face of a given subject and the apex frames curves, and T=50 sampled points on each curve, so that the and F^2 . In practice, we represent each face with 100 radial points of radial curves β_{α}^1 and β_{α}^2 , respectively, of the faces F^1 In this way, the DSF quantifies the local deformation between curve in order to construct the DSFs of the facial surface. consider the magnitude of this vector at each point t of the from the nose tip. Let β_{α}^{1} and β_{α}^{2} denote the radial curves that 3-D faces F^1 and F^2 is to extract the radial curves originating Algorithm 1. The dimension of the DSF vector is $|\Lambda| \times T$. let q_{α}^{\perp} and q_{α}^{\perp} be their SRVFs, the DSF vector is defined by Algorithm 1 Computation of the DSF deformations, whereas the lower values of the dense prototypical expressions are reported using a color scale. In be applied on the neutral face to convey the six different DSFs between two 3-D faces is expressed by a 5000-D vector. particular, colors from green to red represent the $DSF(F^{1}, F^{\perp}) = (f(q_{0}^{1}, q_{0}^{\perp}), \dots, f(q_{\alpha}^{1}, q_{\alpha}^{\perp}), \dots, f(q_{|\Lambda|}^{1}, q_{|\Lambda|}^{\perp})).$ **Dutput:** $DSF(F^1, F^2)$, the DSF between the two faces Input: Facial surfaces F¹ and F²; T, number of sample points In Fig. 3, the examples of the deformation fields computed The steps to compute the proposed DSF are summarized in The first step to capture the deformation between two given on a curve; $\Delta \alpha$, angle between successive radial curves; number of curves per face end procedure procedure COMPUTEDSF(F^1 , F^2 , T, $\Delta \alpha$, $|\Lambda|$) return DSF of $\frac{d\Psi^*}{d\tau}|_{\tau=0}(k)$: compute $DSF(F^1, F^2)$ as the magnitude end while while $n < |\Lambda|$ do $n \uparrow 0$ Eq. (5) as: $f(q_a^1, q_a^2) = (x_a(1), x_a(2), \dots, x_a(T)) \in \mathbb{R}^T_+$ $f(q_a^1, q_a^2) = (x_a(1), x_a(2), \dots, x_a(T)) \in \mathbb{R}^T_+$
$$\begin{split} \theta &= d_C(q_\alpha^1, q_\alpha^2) = cos^{-1}((q_\alpha^1, q_\alpha^2)) \\ \text{compute the deformation vector } \frac{d\Psi_\alpha}{d\tau} (\tau_{\tau=0}^2 \text{ using}) \end{split}$$
for $i \leftarrow 1, 2$ do $\alpha = n \cdot \Delta \alpha$ compute the distance between q_{α}^{\perp} and q_{α}^{\perp} end for $x_{\alpha}(t) = \left|\frac{\theta}{\sin(\theta)} \left(q_{\alpha}^2 - \cos(\theta)q_{\alpha}^1\right)\right|, \ t = 1, \dots, T$ $DSF(F^1, F^2) = (f(q_0^1, q_0^2), \dots, f(q_{|\Lambda|}^1, q_{|\Lambda|}^2))$ compute the SRVF of β_{α}^{i} : extract the curve β'_{0} $q_{\alpha}^{i}(t) \doteq rac{eta_{\alpha}^{i}(t)}{\sqrt{\|\dot{eta}_{\alpha}^{i}(t)\|}} \in \mathcal{C}, \ t = 1, \dots, T$

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Fig. 3. Deformation Scalar Fields computed between a neutral face of a given subject and the apex frames of the sequences of the six prototypical expressions of the same subject. The neutral scan is shown on the left. Corresponding texture images are also illustrated with each DSFs colormap.

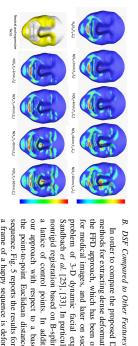


Fig. 4. Effect of the nose tip placement inaccuracy on the shooting directions of the geodesic paths for the DSFs computation). The first row illustrates DSFs when varying the nase tip position along the X-direction. The second row shows DSFs when the variation is performed along the Y-direction.

and

also strongly deformed for the angry and disgust expressions deformed for happiness expression, whereas the eyebrows are expected, the corners of the mouth and the cheeks are mainly in different regions of the face. For example, as intuitively for different expressions, the high deformations are located field are represented in cyan/blue. As it can be observed,

A. Effect of the Nose Tip Localisation Inaccuracy on

consider the effects on the shooting directions of the geodesic on the computation of the proposed DSF. In particular, we possible inaccuracies in the detection of the nose tip can have the DSF Computation In the following, we present a study on the effects that

Y directions and have reported the DSFs computation results (using colormaps on the expressive faces) in Fig. 4. As tolerates errors quite well, up to 4 mm side of the figure illustrates the fact that the DSFs computation to build HMMs or random forest classifiers. However, the left our method is based on learning such geometric deformations impact negatively the performance of the approach. In fact, of the nose tip generates false deformations, which could illustrated in this figure, a large localization error (> 4mm) paths and the radial curves originating from the nose tip. We have changed the nose tip coordinates in the X and

highest scala

> of n frames. Thus, we chose the first n frames as the first system at any time and make the recognition process possible is reduced to the computation of the DSF between them two facial surfaces, a reference facial surface and a target one, a curve-based parametrization of the face that consists in To handle this problem, as described in Section II, we propose from any frame of a given video, we consider subsequences According to this representation, the problem representing the facial surface by a set of radial curves In order to make possible to enter the expression recognition

from the second frame as the second subsequence. subsequence. Then, we chose n-consecutive frames starting cess is repeated by shifting the starting index of the sequence This pro-

are also difficult to be analyzed due to the face movements important to perform effective expression recognition, but they by the motion of facial points. These subtle changes are quences are characterized by subtle variations induced mainly Deformations due to facial expressions across 3-D video se of comparing

III. EXPRESSION RECOGNITION USING DSFS

as the DSF proposed in this paper is capable to capture the face deformations with smooth variations that include the concentrated in the mouth region of the face. variations captured by the other two solutions are much more effects are not limited to the mouth region. Differently, the important to discriminate between different expressions whose first frame of the sequence. The figure shows quite clearly a frame of a happy sequence is deformed with respect to the the point-to-point Euclidean distance between frames our approach with respect to a baseline solution a lattice of control points. In addition, we also compared methods for extracting dense deformation features, we selected mouth, the chin and the cheek, in the example. This result is sequence. Fig. 5 reports the results for an example case, where nonrigid registration based on B-spline interpolation between Sandbach et al. [25], [33]. In particular, FFD is a method for problem of 3-D dynamic facial expression recognition for medical images, and later on successfully applied to the the FFD approach, which has been originally defined in [38] In order to compare the proposed DSF feature against other that uses of a Ŷ

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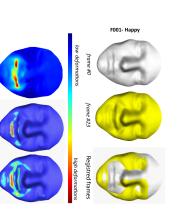


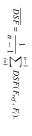
Fig. 5. Comparison of the different features extracted between two frames taken from subject 001 for the happy expression. (a) Free form-based defor-mations (FFD). (b) Point-to-point Euclidean distances (c) DSFs deformations.

the DSF. ent feature extraction and classification framework based on classify the resulting subsequences, we propose two differevery one frame till the end of the sequence. In order to

- 1) Mean Deformation-based Features Associated to Ranfirst one using the DSF. The average deformation of the n-1 resulting DSFs represents the feature vector is calculated from each of the remaining frames to the in this classification scheme and is presented, after is considered as a reference frame and the deformation classifiers dimensionality reduction, to multiclass random forest dom Forest Classifier: The first frame of the subsequence
- 2) 3-D Motion Features Combined With HMM Classifiers: The deformation between successive frames in a subse-quence are calculated using the DSFs and presented to an HMM classifier preceded by LDA-based dimensionality reduction.

A. Mean Shape Deformation with Random Forest Classifier

then given by of a subsequence and F_i the *i*th successive frame in the is computed from this frame to each of the remaining frames of the subsequence. Let F_{ref} denote the reference frame Β subsequence; the successive frame, for example, is denoted by is considered as the reference one, and the dense deformation order to get this feature, the first frame of each subsequence values of i (i = 1, ..., n - 1), and the mean deformation is F_1 . The DSF is calculated between F_{ref} and F_i , for different The idea here is to capture a mean deformation of the face the sliding window on the 3-D expression sequence. In



6

when a particular facial expression is conveyed. cold colors are associated with regions of the face that remain correspond to facial regions affected by high deformations, and yellow) are associated with high $DSF(F_{ref}, F_t)$ values and an automatic labeling scheme is applied; warm colors (red. order to provide a visual representation of the scalar fields, of points used to sample the radial curves of the face). In equal to the number of points on the face (i.e., the number each subsequence is represented by a feature vector of size mean deformation of the n-1 calculated deformations. Thus The mean deformation field is reported on the right of each the corresponding DSFs computed for each frame are shown n = 6 frames. Each expression is illustrated in two rows field summarizes the temporal changes of the facial surface stable from one frame to another. Thus, this dense deformation The feature vector for this subsequence is built based on the plot and represents the feature vector for each subsequence and the n-1 successive frames of the subsequences. Below The upper row gives the reference frame of the subsequence Fig. 6 illustrates one subsequence for each expression with

subsequence is captured by the mean \overline{DSF} defined in (6). According to this representation, the deformation of each

ent subjects, while preserving the discriminating expression information. LDA defines the within-class matrix S_w and thus the reduced dimension d is five. experiments, the discriminating classes are the six expressions, of acquisition noise. In Fig. 6, for each subsequence, deformation resulted more resistant to deformations due to, greater robustness to the noise. In the practice, the mean of the maximum deformation for instance, is related to its an optimized d-dimensional feature, where d < n. In our the between-class matrix S_b . It transforms a *n*-D feature to space to an optimal one that is relatively insensitive to differuse LDA-based transformation to map the present feature Since the dimensionality of the feature vector is high, we than individual deformation fields in the same subsequence. mean deformation field illustrates a smoothed pattern better for example, inaccurate nose tip detection or the presence The main motivation for using the mean deformation, instead the

classify a new expression from an input feature vector by at train time. Once trained, a random forest is capable to of a test, whose result directs a data sample toward the left or computed from the annotated data, which reached each leaf to group the training data in clusters where simple models the right child. During training, the tests are chosen in order solvable with simple predictors. Each node in the tree consists mappings by splitting the original problem into smaller ones to build each tree in the forest. A tree achieves highly nonlinear and more importantly to be diverse by using random samples trees. It was designed to operate quickly over large datasets and defined as a meta-learner comprised of many individual algorithm. The algorithm was proposed by Leo Breiman [39] putting it down each of the trees in the forest. Each tree gives achieve good predictions. Such models are stored at the leaves, a classification decision by voting for that class. Then, the For the classification, we used the multiclass random forest

В

The DSF features described in Section II can 3-D Motion Extraction with HMM Classifier

also

forest chooses the classification having the most votes (over all the trees in the forest).

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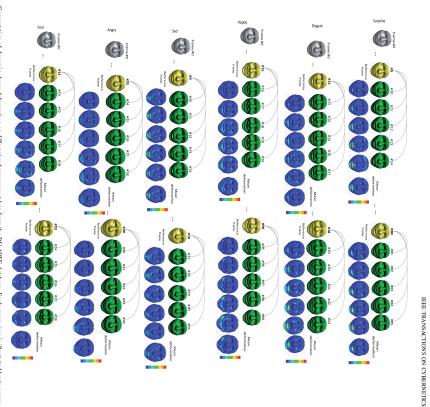


Fig. 6. Computation of dynamic shape deformation on different subsequences taken from the B14-JPE database. Each expression is illustrated by two rows. The upper one gives the reference frame of the subsequence and the r-1 successive frames. The corresponding deformation fields computed for each frame with respect to the reference one are illustrated in the lower row. The mean deformation field is given on the right of each foreign of the sub-with respect to the reference one are illustrated in the lower row. The mean deformation field is given on the right of each foreign of the sub-with respect to the reference one are illustrated in the lower row. The mean deformation field is given on the right of each foreign of the sub-sequence of the reference one are illustrated in the lower row. The mean deformation field is given on the right of each foreign of the sub-sequence of the reference one are illustrated in the lower row. The mean deformation field is given on the right of each foreign of the sub-sequence of the reference one are illustrated in the lower row. The mean deformation field is given on the right of each foreign of the sub-sequence of the reference one are illustrated in the lower row. The mean deformation field is given on the right of each foreign of the sub-sequence of the reference one are illustrated in the lower row. The mean deformation field is given on the right of each foreign of the sub-sequence of the reference one are illustrated in the lower row.

applied for expression recognition according to a different classification scheme. The deformations between successive geometry. dial curves and thus capture the changes in facial surface are able to quantify the motion of face points along raof correspondent radial curves. Based on this measure, we is obtained by computing the pairwise DSF $DSF(F_{t-1}, F_t)$ particular, the deformation between two successive 3-D frames frames in the subsequence are calculated using the DSF. In

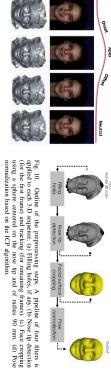
and its effectiveness in capturing deformation between one Fig. 7 illustrates a direct application of the $DSF(F_{t-1}, F_t)$

e corresponds to facial regions affected by high deformations red color is associated with high $DSF(F_{t-1}, F_t)$ values and provide a visual representation of the scalar field, an automatic previous one) in the subsequence is reported. In order to between consecutive frames (i.e., the current frame and the row, the deformation scalar field $DSF(F_{t-1}, F_t)$ computed scans of some frames are shown in the upper row. In the lower respectively). For each sequence, the 2-D image and the 3-D extracted from videos in the BU4DFE database (happy and surprise expressions are shown on the left and on the right, in a 3-D video sequence. This figure shows two subsequences labeling scheme is applied that includes only two colors: The facial surface to another belonging to two consecutive frames

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| BOD- HIND | HICH AND AND AND AND AND AND AND AND AND AND | Texture Textur | Find Hind Hind Hind Hind Hind Hind Hind H |
| Fig. 7. Examples of DSF deformations between subsequent frames of 3-D v left and right. | Examples of DSF deformations between subsequent frames of 3-D video sequences: Happy and surprise expressions are shown, respectively, on the right. | Sape | Fig. 10. Outline of the preprocessing steps. A pipeline of for applied to each 3-D sequence. (a) Filling holes, if any. (b) Nose to (for the first frame) and tracking (for remaining frames). (c) Far using a sphere centered on the lose tip and of radius 90 nm normalization based on the ICB algorithm. |
| The blue color is associated with the regions that remain more stable from one frame to another. As illustrated in Fig. 7, for | | Fig. 9. Examples of 2-D and 3-D frames extracted from a dynamic 3-D video sequence of the BU-4D9FE dataset. | Krotoben = x/8 Krotoben = x/4 Krotoben = 3x/8 Krotetion = |
| different expressions, different regions are manily deformed, different expressions, different regions are manily deformed, showing the capability of the deformation fields to capture relevant changes of the face due to the facial expression. In particular, each deformation is expressed to jubuity an | SI SI SI SI SI SI SI SI SI SI SI SI SI S | A. BU-4DFE Database: Description and Preprocessing To investigate the usability and performance of 3-D dynamic | Before registration |
| particular, cash uccontain to expected to the initiation, the expression, for example, as suggested by the initiation, the corners of the mouth and the cheeks are mainly deformed for the happiness expression. With the proposed approach, the feature extraction process starts by computing for each 3-D frame in a given video | Fig. 8. Structure of the HMMs modeling a 3-D facial sequence. The four states model neutral onset, apex, and offset framess of the sequence. As shown from each state it is possible to remain in the state itself or move to the next one (this is known as Bakis or left-right HMM). | facial sequences for facial expression recognition, a dynamic 3-D facial expression database has been created at Binghannon University [14]. The dimensional imaging's 3-D dynamic capturing system [42], has been used to capture a sequence of stereo images and produce the depth map of the face according | Ater rejutation |
| sequence the DSF with respect to the previous one. In this way, we obtain as many fields as the number of frames in the sequence (decreased by one), where each field contains as many scalar values as the number of points of points of points of the sequence of the sequen | standard LBG algorithm [40]. This provides the required mapping between multidimensional feature vectors, tak- ing values in a continuous domain, with the alphabet of symbols emitted by the HMM states | to a passive stereo-photogrammetry approach. The range maps are then combined to produce a temporally varying sequence of high-resolution 3-D images with an RMS accuracy of 0.2 mm. At the same time, 2-D texture videos of the dynamic 3-D models are also recorded. Each participant (subject) was | Fig. 11. Registration results using the ICP algorithm when rota the z-ratis one of the 3-D perprocessed faces. The first row show rotation applied on the yellow model (before the alignment) and row shows the alignment output (after alignment). |
| practice, the size of $DSF(F_{i-1}, F_i)$ is 1×5000 , considering 5000 points on the face, similarly to the feature vector vector where the feature vector size has a size of the feature vector size has a size has a size of the feature vector size has a siz | 2) Expression sequences are considered as observation sequences $O = \{O^1, O^2, \dots, O^T\}$, where each observation O' at time <i>t</i> is given by the feature vector f' | requested to perform the six prototypical expressions (i.e., angry, disgust, fear, happiness, sudness, and surprise) sepa- rately. Each expression sequence contains neutral expressions | 2) Detect the nose tip on the face scan in the fi of the sequence. The nose tip is detected by i the neak point of the face scan in the denth. |
| Since the dimensionality of the resulting feature vector is high, also in this case we use LDA to project the scalar values to | 3) Each HMM λ^{copr} is initialized with random values and the Baum-Welch algorithm [41] is used to train the | in the beginning and in the end, so that each expression was performed gradually from neutral appearance, low intensity, | The nose tip is then tracked on all the su frames when the search area is limited to a |
| a 5-D teature space, which is sensitive to the deformations induced by different expressions. The 5-D feature vector extracted for the 3-D feature at instant t of a sensence is | model using a set of naming sequences. This estimates the model parameters, while maximizing the conditional mobability $P(O \lambda^{exp})$. | and each 3-D sequence lasts approximately four seconds with | inergnoornood around the nose up detected on frame. 3) Crop the facial area using a sphere centere |
| indicated as f' in the following. Once extracted, the feature vectors are used to train HMMs and to learn deformations due | Given a 3-D sequence to be classified, it is processed as in Section II so that each feature vectors f^{t} corresponds to a | about 35 000 vertices per scan (i.e., 3-D frame). The database consists of 101 subjects (58 female and 43 male, with an | |
| to expressions along a temporal sequence of frames. In our case, sequences of 3-D frames constitute the temporal | test observation $O = \{O^1 \equiv f^1, \dots, O^T \equiv f^T\}$. Then, the test observation O is presented to the six HMMs λ^{expr} that model | age range of 18–45 years old) including 606 3-D model sequences with six prototypical expressions and a variety of | Normalize the pose of a given frame according vious frame using the Iterative Closest Point (IC |
| dynamics to be classified, and each prototypical expression is modeled by an HMM (a total of six HMMs λ^{expr} is required, | different expressions, and the Viterbi algorithm is used to determine the best path $\bar{Q} = \{\bar{q}^1, \dots, \bar{q}^T\}$, which corresponds | ethnic/racial ancestries (i.e., 28 Asian, 8 African-American, 3 Hispanic/Latino, and 62 Caucasian). More details on the | alignment. We point out that our implementa the following parameters to perform the ICP a |
| with $expr \in \{an, di, fe, ha, sa, su\}$). Four states per HMM are used to represent the temporal behavior of each expression. | to the state sequence giving a maximum of likelihood to the observation sequence O. The likelihood along the best | β_{0} -+ λ_{TE} can be round in [1+4]. An example of a -> D dynamic facial sequence of a subject with happy expression is shown in | a) match the nose tips of the faces first; b) n vertices considered to find the optimal tranform |
| This corresponds to the idea that each sequence starts and ends with a neutral expression (state S_1). The frames that belong to | path, $p^{e,p}(O, \mathcal{Q} \lambda^{e,p}) = p^{e,p}(O \lambda^{e,p})$ is considered as a good approximation of the true likelihood given by the more | frames are reported. From left to right, the frames illustrate | effective alignment, this set of parameters all |
| the temporal intervals where the face changes from neutral to expressive and back from expressive to neutral are modeled by | expensive forward procedure [41], where all the possible paths are considered instead of the best one Finally the secuence is | the intensity of facial expression passing from neutral to onset, offset, apex, and neutral again. | an attractive computational cost. |
| the onset (S_2) and offset (S_4) states, respectively. Finally, the frames corresponding to the highest intensity of the expression | classified as belonging to the class corresponding to the HMM whose log-likelihood along the best path is the greatest one. | | and rotate, whereas in our experiments only near-from are considered, as the BU-4DFE database does no |
| are captured by the abox state (53). This solution has proved to effectiveness in clustering the expressive states of a sequence sloo in other ransees [33] Fig. 8 eventifies the structure of | | mainly acquired in the hair, neck, and shoulders regions (Fig. 9). In order to remove these imperfections from each | approach to cope with non-frontal scans, we report i |
| the HMMs used in our framework. The training procedure of each HMM is summarized as | IV. EXPERIMENTAL RESULTS | | some registration results when applying an artificial to one of the 3-D faces to be aligned. It is clear |
| follows. (1) Easture vectors f' of the training sequences are first | from dynamic sequences of 3-D face scans has been experi- mented on the RU-4 DEF database Main characteristics of the | Identify and fill the holes caused, in general, by self- occlusions or onen mouth. The holes are identified by | variations (up to about 30%145°). Instead, the re- method is not able to register a frontal face with |
| clustered to identify a codebook of symbols using the | database and results are reported in the following sections. | locating boundary edges, then triangulating them. | face (right side of the figure). |

dentified them. à

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Pose normalization

L.,

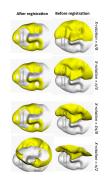


Fig. 11. Registration results using the ICP algorithm when rotating around the *x*-axis one of the 3-D perpresessed faces. The first row shows the initial rotation applied on the yellow model (nefore the alignment) and the second row shows the alignment output (after alignment).

2 Detect the nose tip on the face scan in the first frame of the sequence. The nose tip is detected by analyzing the peak point of the face scan in the depth direction. frames when the search area is limited to a specific neighborhood around the nose tip detected on the first The nose tip is then tracked on all the subsequent

 $\underline{\omega}$ Crop the facial area using a sphere centered on the detected nose tip with a constant radius set to 90 mm based on some observations. frame.

vertices considered to find the optimal tranformation=50; and c) number of iterations=5. In addition to permit effective alignment, this set of parameters allows also Normalize the pose of a given frame according to its prea) match the nose tips of the faces first; b) number of the following parameters to perform the ICP algorithm: alignment. We point out that our implementation uses vious frame using the Iterative Closest Point (ICP)-based

variations (up to about $30^{\circ}/45^{\circ}$). Instead, the registration method is not able to register a frontal face with a profile face (right side of the figure). and rotate, whereas in our experiments only near-frontal faces are considered, as the BU-4DFE database does not contain nonfrontal acquisitions. To account for the capability of our approach to cope with non-frontal scans, we report in Fig. 11 some registration results when applying an artificial rotation to one of the 3-D faces to be aligned. It is clear that the registration method is able to handle with moderate pose In a real-world scenario of use, the head can move freely The performance of random forest classifier varies with the number of trees. Thus, we perform the experiments with B. Mean Deformation-Based Expression Classification BEN AMOR et al.: 4-D FACIAL EXPRESSION RECOGNITION multiclass random forest, as outlined in Section III. Deformation for each subsequence, which is then presented to of the expression recognition framework to identify individual short sequences is regarded as an indication of the capability the system not necessarily starting with a neutral expression, but with an arbitrary expression. The classification of these accounts for the fact that, in general, the subjects can enter sions, thus extracted subsequences have the same label. This following one. For example, with this approach, a sequence of a sliding step of one frame from one subsequence to the have been defined in [23] with a length of six frames with large set of subsequences are extracted from the original exand comparative analysis with respect to the previous papers for the test. In the following, we report experimental evaluation where at each round nine of the ten folds (54 subjects) are used and 10-fold cross validation has been used for training/test domly partitioned into ten sets, each containing six subjects, other papers [23], [26], [27]. The 60 subjects have been ranexperiments according to the evaluation protocol followed in data of 60 subjects have been selected to perform recognition common experimental set up has been used. In particular, the expression, as described in Section III-B. In both the cases, a (deformation) is extracted and then learned for each class of on a dynamic analysis through the 3-D sequences using forest algorithm (Section III-A). The second scheme consists sliding windows that are learned using a multiclass random of the window. This produces dense deformations across Fig. 12. 4-D expression recognition results using a random forest classifier when varying the number of trees. expressions. According to this, we first compute the Mean Each sequence is labelled to be one of the six basic expressubsequence differing for one frame from the previous one 100 frames originates a set of $6 \times 95 = 570$ subsequences, each pression sequences using a sliding window. The subsequences for the training, while the remaining fold (six subjects) is used conventional temporal HMMs-modeling. Here, the 3-D motion DSF computed on each frame with respect to the first frame scheme consists on averaging, within a sliding window, the deformation learning and classification schemes. The computation across the 3-D sequences, Average recognition rate (%) Following the experimental protocol proposed in [23], a In the proposed framework, after preprocessing and DSF This article has been accepted for inclusion in a future issue of this journal. Content is final as presented, with the exception of pagination 10 15 20 25 30 35 Number of trees 40 45 50 we designed two schemes. The first the proposed of the frames. Fig. 13. The clas are observed between different folds. value of this statistical indicator suggests that small variations window 6 Angry Disgust Fear Happy Sad Surprise An Di Fe Ha Sa Su

of 95.47% and 94.53%, respectively. The standard deviation from the average performance is also reported in the table. The are happy (Ha) and surprise (Su) with recognition accuracy facial muscles can be activated. The best classified expressions capture negative emotive states of the subjects, so that similar Fear (Fe) expressions. Interestingly, these three expressions between the disgust (Di) expression and the angry (An) and cross validation). It can be noted that the largest confusions are by averaging the results of the ten independent runs (10-fold number of trees in Table I. We recall that the rates are obtained 40 trees and report detailed results (confusion matrix) with this trees until 40, when the recognition rate reaches 93.21%, and average recognition rate raises with the increasing number of tation is shown in Fig. 12. different numbers of trees and the results of this experimenthen becomes quite stable. Thus, in the following we consider CONFUSION MATRIX FOR MEAN DEFORMATION AND RANDOM FOREST ification rates increase with the increase in the length of the temporal Effect of the temporal size of the sliding window on the results 1.89 1.75 **91.24** 0.57 0.84 1.71 93.11 CLASSIFIER (FOR 6-FRAMES WINDOW) 92.46 2.44 0.85 1.84 0.72 nition rate =93.21±0.81% TABLE I As illustrated in this figure, 95.47 92.46 94.53 0.66 1.83 the

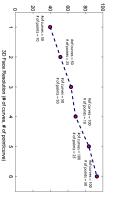
of 6-frames to allow comparisons with previous papers. to report detailed results when considering a window length classification, the result reach 100%. In the paper, we decided the spatio-temporal analysis outperforms a spatial analysis the importance of the temporal dynamics and shows that increase in the temporal length of the window. This reveals the recognition rate of the six expressions increases with the using the whole length of the sequence (on average this is we report results for a window size equal to 2, 5, and 6, and sliding window used to define the subsequences. In Fig. 13, additional experiments when varying the temporal size of the about 100 frames). From the figure, it clearly emerges that Effect of the Subsequence Size: We have also conducted By considering the whole sequences for the

Effect of the Spatial Resolution face representation, the DSF is computed Ŀ, 3-D Faces: for In the for the

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Rate (%)



CONFUSION MATRIX FOR FREE-FORM DEFORMATION (FFD) AND

TABLE II

 1.77
 0.48
 1.99
 0.32
 94.84

 0.57
 0.38
 3.25
 0.38
 1.85

 Average recognition rate
 = 93.83±1.53%

HMM CLASSIFIERS (FOR 6-FRAMES WINDOW)

Di

Ha 1.97

 Sa
 Su

 6.49
 2.86

 4.18
 1.62

 6.31
 2.87

than the resolution in terms of points per curve. resolution in terms of number of curves has more importance in the data. From these results, we can also observe that the per curve is decreased due to the presence of noise and spikes performance in the case the number of radial curves or points This can give an indication of the expected decrease in the expression classification accuracy (on the BU-4DFE) and the number of radial curves and the number of points per curve. Fig. 14 expresses quantitatively the relationship between the number of radial curves and the number of points per curve). when varying the spatial resolution of the 3-D faces (i.e., the To investigate this aspect, we have conducted experiments curve can affect the final effectiveness of the representation So, the resolution used for the number of curves and points per number of radial curves and the number of points per curve Due to this, the density of the scalar field depends on the work can also fit with different deformation fields than the are mainly the effect of the proposed deformation scalar field across the 3-D sequences. These similar good achievements the ability of the proposed DSF to capture subtle deformations achieved 93.95% of correct classification, which demonstrates (An) expression is known for its subtle motions, our classifier

Comparion With the FFD Feature: The proposed frame-

one C. HMM-Based Expression Classification learning scheme achieved better recognition than the first for angry (An) expression. Actually, whereas the The average recognition rate is equal e angry

> Ha Sa Su 1.05 0.51 1.77 0.57 5 1.42 94.55 0.69 1 0.93 1.65 94.58 7 0.48 1.99 0.32 7 0.38 3.25 0.38 1.67 0.62 0.40 93.57

| % An Di Fe Ha Sa Su An 93.95 1.44 1.79 0.28 2.0 0.54 Di 3.10 91.54 3.40 0.54 1.27 0.15 | | - | FOR 6-FRAMES WINDOW | RAMES | WINDO | W) | |
|--|----|-------|---------------------|-------|-------|------|------|
| 93.95 1.44 1.79 0.28 2.0 3.10 91.54 3.40 0.54 1.27 | % | An | Di | Fe | Ha | Sa | Su |
| 3.10 91.54 3.40 0.54 1.27 | An | 93.95 | 1.44 | 1.79 | 0.28 | 2.0 | 0.54 |
| | Di | 3.10 | 91.54 | 3.40 | 0.54 | 1.27 | 0.15 |

| 5 | | |
|---|----------|--|
| MOTION | TA | |
| Dvmn A | TABLE II | |
| | | |
| ļ | | |
| LINANA | | |
| 2 | | |
| THEY FOR MOTION EVERACTION AND UNING CLASSIFIED | | |

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points of a set of radial curves originating from the nose Б

reported in the confusion matrix of Table II. The values in the table have been obtained by using features of six frames defined in [23]), for this experiment we trained the HMMs on six frames subsequences constructed as discussed above. high despite the difficulty of this expression analysis. This value in this case). It can also be noted that, compared to the the standard deviation among different folds shows a greater deformation plus random forest classification schema (though to 93.83%, slightly higher than the one displayed by mean previous five frames. accurately by analyzing the corresponding subsequence of the proposed approach is capable to classify individual frames emission probability criterion as decision rule. It is clear that subsequences as input to the 6 HMMs and using the maximum the expression sequences (frame-by-frame experiment) are achieved results by classifying individual subsequences of derived from the 60×6 sequences (31970 in total). The 10-fold cross validation on the overall set of subsequences the subsequences. Also in this experiment, we performed The 4-state structure of the HMMs resulted adequate to model achieved generally. In fact, correct classification of angry is previous classifier, the same tendency of recognition rates is Following the same setup as in Section IV-B (originally

D. Discussion and Comparative Evaluation (as discussed in Section II). classification accuracy. This can be motivated by the nice that the proposed DSF feature provides a finer discriminative a 5000-D vector to a 5-D subspace). The overall result is reports the confusion matrix obtained by posing FFD in our expression recognition [25] (see also Section II-B). Table III capture the deformation fields on the lattice of points of the proposed DSF. So, considering alternative features to densely invariant properties of the proposed Riemannian framework capability with respect to the FFD, thus resulting in a better points each, and LDA reduction of the deformation field from experiments above (i.e., 100 radial curves, with 50 sampled classification framework, using the same setting as in the registration and has been successfully proved in the context of the FFD [38] feature, which is a standard method for nonrigid DSF feature with different ones. In particular, we considered radial curves of the face can permit a direct comparison of our

results are obtained these solutions with respect to our proposal, also evidencing but the testing protocols used in the experiments are sometimes on expression recognition from dynamic sequences scans are those in [20], [24], [26], [29], and recent the different settings under which the expression recognition in these papers is not immediate. In the following, we discuss different, so that a direct comparison of the results reported These papers have been evaluated on the BU-4DFE dataset To the best of our knowledge, the papers reporting results recently [30] of 3-D

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BEN AMOR et al.: 4-D FACIAL EXPRESSION RECOGNITION

TABLE IV

COMPARISON OF THIS PAPER TO EARLIER PAPERS. PROTOCOL DESCRIPTION: #SUBJECTS (S), #EXPRESSIONS (E), WIN SIZE (WIN). T: TEMPORAL ONLY/S-T: SPATIO-TEMPORAL. ACCURACY ON SLIDING WINDOW/WHOLE SEQUENCE (OR SUBSEQUENCE)

| Authors | Method | Features | Classification | Protocol | 1/5-1 | 1/S-1 KK (%) |
|------------------------|-----------------------------|----------------------------------|-------------------|----------------------|-------|--------------|
| Sun et al. [23] | MU-3D | 12 Motion Units | HMH | 60 S, 6 E, Win=6 | Т | 70.31, |
| Sun et al. [23] | T-HMM | Tracking model | HMH | 60 S, 6 E, Win=6 | Т | 80.04, |
| Sun et al. [23] | P2D-HMM | Curvature+Tracking model | T-HMM+S-HMM | 60 S, 6 E, Win=6 | S-T | 82.19, |
| Sun et al. [23] | R-2DHMM | Curvature+Tracking model | 2D-HMM | 60 S, 6 E, Win=6 | S-T | 90.44, |
| Sandbach et al. [25] | 3D Motion-based | FFD+Quad-tree | GentleBoost+HMM | —, 3 E, Win=4 | Т | 73.61, 81.93 |
| Sandbach et al. [20] | 3D Motion-based | FFD+Quad-tree | GentleBoost+HMM | -, 6 E, variable Win | T | 64.6, |
| Le et al. [26] | Level curve-based | pair- and segment-wise distances | HMM | 60 S, 3 E, | S-T | -, 92.22 |
| Fang et al. [27], [29] | AFM Fitting | LBP-TOP | SVM-RBF | 100 S, 6 E, | Т | -, 74.63 |
| Fang et al. [27], [29] | AFM Fitting | LBP-TOP | SVM-RBF | 100 S, 3 E, | т | -, 96.7 |
| Reale et al. [30] | Spatio-temporal volume | "Nebula" Feature | SVM-RBF | 100 S, 6 E, Win=15 | S-T | -, 76.10 |
| This work | Geometric Motion Extraction | 3D Motion Extraction | LDA-HMM | 60 S, 6 E, Win=6 | Т | 93.83, |
| This work | Geometric Mean Deformation | Mean Deformation | LDA-Random Forest | 60 S, 6 E, Win=6 | ī | 93.21, |

by shifting the starting index of the sequence every one frame till the end of the sequence. general, sequences in which the required expressions are acted accurately are selected, whereas in [27] and [29] 507 expressions. The number of subjects considered is 60, except in [25] where the number of subjects is not specified. In sequences of 60 selected subjects. The process were repeated constructed by generating subsequences of 6-frames from all described in setting proposed by the earliest and more complete evaluation our experiments, we conducted tests by following the same sequences out of the 606 total are used for all subjects. In all the six basic expressions in [23], [24], [27], [29], and [30] quite different especially the number of verified expressions, whereas [25] this paper. The testing protocols used in the experiments are ously on the BU-4DFE dataset, compared to those obtained in Table IV summarizes approaches and results reported previ-[23]. The training and the testing sets were and [26] reported primary results on only three

of the sequence to allow accurate model tracking. recognition rates reported in [23] and [24] based on temporal analysis only was 80.04% and spatio-temporal analysis was requiring 83 manually annotated landmarks on the first frame We emphasize that their approach is not completely automatic 90.44%. In both papers, subsequences of constant window the-art solutions following similar experimental settings. The width including 6-frames (win = 6) is defined for experiments. We note that the proposed approaches outperforms state-of-

chosen as it is at one extreme of the arousal the valence expression spectrum, whereas surprise was also expressions with the fact that they are at either ends of training sequences that can be a time consuming operation. In Authors motivated reported on and motion capturing between frames. Preliminary tests were between a lattice of control points for nonrigid registration due to free-form deformations based on B-spline interpolation addition, a drawback of this solution is the computational cost manual annotation and counting on a consistent number of Though frames of the sequence in order to train a set of HMMs sequences, but uses supervised learning to annotate individual with respect to the processing of facial frames in the temporal The method proposed in [25] and [20] is fully automatic performed offline, supervised learning requires three expressions: (An), the choice of the happiness (Ha), and (Su). The expression and anger

to the most intense expression, including the apex frames). a subset of subjects accurately selected as acting out cording to the following criteria: 1) the 4-D sequence should tocol. In fact, the reported recognition results depends on the recognition results on whole facial sequences, but this hinders for the happiness expression. However, the authors reported of 92.22% with the highest performance of 95% obtained are used for the classification (and these typically correspond detect the onset frame and just 15 frames from the onset one used by this approach, it also uses a manual intervention to the onset frame has been extracted from each expression of database. has been marked manually on each sequence of the BU-4DFE (95.75%) are considered. rupted meshes are discarded. In addition, to achieve recog-nition rate of 75.82%, whole sequences should be analyzed. start by neutral expression and 2) sequences containing cordatabase. However, 507 sequences are selected manually nition accuracy on 100 subjects picked out from BU-4DFE results when processing very few 3-D frames. one described in [23], which are able to provide recognition preprocessing of whole sequences unlike our approach and the possibility of the methods to adhere to a real-time proten rounds of 10-fold cross-validation show an overall value sadness, and surprise. The recognition accuracy averaged on from the BU-4DFE database for the expressions of happiness. case). Expression recognition is performed on 60 subjects (i.e., annotation of individual frames is not required in this an unsupervised learning solution to train a set of HMMs evaluation by considering all the six basic expressions. have reported recognition rate of 81.93% is reported. Sandbach et al. this subset of expressions and subjects, an average expression was performed using a 10-fold cross-validation testing. required expression. Verification of the classification system 100 subjects. So, although sequences from 100 subjects are First, the onset frame for each of the six canonical expressions (An), and (Su) expressions (96.71%) or (Ha), (Sa) and The authors reported highest recognition rates when only (Ha)The protocol used in [30] is quite different from the others In [27] and [29], results are presented for expression recog-In [26], a fully automatic method is also proposed that uses Then, a fixed size window of 15 frames starting from 64.6% classification rate when 5

l the

work compares favorably with the state-of-the-art solutions According to this comparative analysis, the proposed I frame-

spectrum. However,

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experiments

were

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called DSF, under the two designed schemes. the effectiveness of the novel mathematical representation a common feature extraction module (DSF). This demonstrates consists of two geometric deformation learning schemes with

V. CONCLUSION

containing very different 3-D frames with an average accuracy of 93.83% using HMM-based classifier and 93.21% using to capture subtle deformations in 4-D videos. pability of the proposed geometric shape deformation analysis art settings on the BU-4DFE dataset. This emphasizes the camean deformation-based classifier, following the state-of-theones; it is capable to accurately classify short sequences feature vectors. The proposed approach outperforms previous was applied to decrease the dimensionality of the resulting deformation-based classifier. An LDA-based transformation schema were performed, a HMM-based classifier and a mean tion from successive 3-D frames. Two different classification was applied to quantify dense deformations and extract mocollections of radial curves, a Riemannian shape analysis video sequences. Through a facial shapes representation identity-independent facial expression recognition from 3-D F this paper, we presented an automatic approach for à

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and the low resolution of the acquired scans. Kinect, is a distant goal mainly due the presence of large noise 3-D videos, outputs of the depth-consumer cameras like the analysis (interframe). Second, its adaptation to low resolution paper are, first, its extension to spatio-temporal analysis by introducing a spatial (intraframe) analysis beside the temporal to detect the nose tip. As future perspectives of the presented istic scenarios, more elaborated techniques should be applied contains frontal 3-D faces without occlusion, however, in real-(by glasses, hand, hair, and so on). The BU-4DFE database case of nonfrontal views and/or the presence of occlusions One limitation of the approach is the nose tip detection in

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BEN AMOR et al.: 4-D FACIAL EXPRESSION RECOGNITION

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| Monamed Daoudi, Senior Member, IEEE, and Him Slama | imber, IEEE, and Him Slama | Fig. 1. Different challenges of 3D face recognition: expressions, missing data, and occlusions. | region invoces (Atoms) locarly to influence include lenges of missing data and expression-related deformations. They manually divide the facial area | |
|---|--|--|--|--|
| Abstract-We propose a novel geometric framework for analyzing 3D faces, with the specific goals of comparing, matching, and | 3 D faces, with the specific goals of comparing, matching, and | and mouth. In [25]. Passalis et al. use automatic | into several meaningful components and the regis- | |
| averaging their shapes. Here we represent tacial surfaces by radial curves emanating from the nose tips and use elastic shape analysis of these curves to develop a Riemannian framework for analyzing shapes of full facial surfaces. This representation, al | al curves emanating from the nose tips and use elastic shape | landmarking to estimate the pose and to detect | tration of faces is carried out by separate dense | |
| with the elastic Riemannian metric, seems natural for measuring facial deformations and is robust to challenges such as large facial | acial deformations and is robust to challenges such as large facial | occluded areas. The facial symmetry is used to | alignments to the corresponding ARMs. A strong | |
| expressions (especially those with open mouths), large pose variations, missing parts, and partial occlusions due to glasses, hair, and | ons, missing parts, and partial occlusions due to glasses, hair, and | overcome the challenges of missing data here. | limitation of this approach is the need for manual | |
| so on. This framework is shown to be promising from both-empirical and theoretical-perspectives. In terms of the empirical | ical and theoretical-perspectives. In terms of the empirical | Similar approaches, but using manually annotated | segmentation of a face into parts that can then be | |
| evaluation, our results match or improve upon the state-of-the-art methods on three prominent databases: FHGCv2, GavabDB, and Bosphorus, each posing a different type of challenge. From a theoretical perspective, this framework allows for formal statistical | methods on three prominent databases: FRGCv2, GavabDB, and pretical perspective. this framework allows for formal statistical | models, are presented in [31] and [17]. For example, Lu and Jain [17] use manual landmarks to develop a | analyzed separately. 3. <i>Surface distance-based approaches</i> . There are several | |
| inferences, such as the estimation of missing facial parts using PCA on tangent spaces and computing average shapes. | A on tangent spaces and computing average shapes. | thin-plate-spline-based matching of facial surfaces. | | |
| Index Terms—3D face recognition, shape analysis, biometrics, guality control, data restoration | ality control, data restoration | A strong limitation of these approaches is that the | facial surfaces to define features that are eventually used in recognition. (Some papers call it <i>geodesic</i> | |
| | | extraction of inducial landmarks needed during learning is either manual or semi-automated, except | distance but, to distinguish it from our later use of | |
| | | in [13], where it is fully automated. | geodesics on shape spaces of curves and surfaces, we | |
| | | 2. Local regions/features approaches. Another common | snall call it <i>surface atstance.</i>) These papers assume that surface distances are relatively invariant to | |
| | | framework especially for handling expression varia- | small changes in facial expressions and therefore | |
| JE to the natural, nonintrusive, and high throughput | We note that most recent research on 3D face analysis | | help generate features that are robust to facial | |
| nition has many bonafits when compared to other | inds been directed toward tackning citatiges in ractar | ratios of distances and angles between eight fiducial | expressions. Bronstein et al. [4] provide a limited | |
| etrics. Accordingly, automated face recognition has | spent on handling occlusions and missing parts. Although a | points, followed by an SVM classifier. Similarly, | experimental investation or this invariance by | |
| red growing attention within the computer vision | few approaches and corresponding results dealing with | Gupta et al. [11] use euclidean/geodesic distances | euclidean distances between corresponding points | |
| nunity over the past three decades. Among different | missing parts have been presented, none, to our knowledge, | tion with linear classifiers. As stated earlier, the | on a canonical face surface. To handle the open | |
| indes available for lace inlaging, 3D scatting has a | has been applied systematically to a full real database | problem of automated detection of fiducial points is | region, and then compute the surface distance in the | |
| bles, such as illumination and small pose changes, | containing scale with meaning parts in the paper, we present a comprehensive Riemannian framework for | nontrivial and hinders automation of these methods. | presence of a hole corresponding to the removed | |
| a relatively smaller influence on the observations. | analyzing facial shapes, in the process dealing with large | Gordon [10] argues that curvature descriptors have | art [5]. The assumption of preservation of surface | |
| ever, 3D scans often suffer from the problem of | expressions, occlusions, and missing parts. Additionally, | surface features and are better suited to describing | authors to define distance-based features for facial | |
| ing parts due to sen-occusions of external occusions | we provide some basic tools for statistical shape analysis of | the properties of faces in areas such as the cheeks, | recognition. Samir et al. [28] use the level curves of | |
| tionally, variations in face scans due to changes in | facial surfaces. These tools help us to compute a typical or | forehead, and chin. These descriptors are also | the surface distance function (from the tip of the | |
| expressions can also degrade face recognition | average snape and measure me muacrass variability or shapes, and will even lead to face atlases in the future. | invariant to viewing angles. Li et al. [16] design a feature pooling and ranking scheme to collect | mouth affects the shape of some level curves, this | |
| rmance. To be useful in real-world applications, a | | various types of low-level geometric features, such | method is not able to handle the problem of missing | |
| ace recognition approach should be able to handle | | as curvatures, and rank them according to their | data due to occlusion or pose variations. A similar | |
| challenges, i.e., it should recognize people despite facial expressions occlusions and large nose varia- | The task of recognizing 3D face scans has been approached in | sensitivity to facial expressions. Along similar lines, | polar parameterization of the facial surface is | |
| Some examples of face scans highlighting these | the reader to one of many extensive surveys on the topic, for | wang et al. [52] use a signed snape-dimerence map between two aligned 3D faces as an intermediate | geometric attributes under this parameterization. To | |
| s are illustrated in Fig. 1. | example, see Bowyer et al. [3]. Below we summarize a | representation for shape comparison. McKeon and | deal with the open mouth problem, they modify the | |
| | smaller subset that is more relevant to our paper. | Russ [19] use a region ensemble approach that is | parameterization by disconnecting the top and bottom lips. The main limitation of this approach | |
| Drira, B. Ben Amor, and M. Daoudi are with Laboratoire d'Informatique | 1. Deformable template-based approaches. There have been | | is the need for detecting the lips, as proposed in [5]. | |
| aamentale de Lulie (LIFL), (UMR CNRS 8022), Institut Mines-Telecom/ ECOM Lille 1, Cité Scientifiaue, Rue G. Marconi, BP 20145. | several approaches in recent years that rely on | In [12], Huang et al. use a multiscale local binary | facial etrinos which in turn are used as nodes in a | |
| eneuve d'Ascq 59653, France. É-mail: hassen.drira@telecom-lille1.eu. | deforming facial surfaces into one another, under | pattern for a 3D face jointly with shape index. | graph-based recognition algorithm. | |
| versity, 106D OSB, 600 W College Ave, Tallahassee, FL 32306. | deformations as metrics for face recognition. Among | around automatically detected fiducial points. To | The main limitation of these approaches, apart from the | |
| AR CNRS 8022), University of Lille 1, Télécom Lille 1, Cité | these, the ones using nonlinear deformations facil- | | issues resulting from open mouths, is that they assume that | |
| ntifique, Rue G. Marconi, BP 20145, Villeneuve d'Ascq 59653, France. | itate local stretching, compression, and bending of | encompassing discriminative information, Faltemier | face classes. This is not valid in the case of large | |
| cript received 30 June 2011; revised 7 May 2012; accepted 30 Jan. 2013; | <i>elastic</i> methods. For instance. Kakadiaris et al. [13] | et al. [9] use 38 face regions that densely cover the | expressions. Actually, face expressions result from the | |
| mended for acceptance by K. Siddiqi. | utilize an <i>annotated face model</i> to study geometrical | ICP on each region. A similar idea is proposed in | stretching or the shrinking of underlying muscles and, | |

1 INTRODUCTION

missing parts due to self-occlusions or external occlusions issues are illustrated in Fig. 1. tions. Some examples of face scans highlighting these large facial expressions, occlusions, and large pose variathese challenges, i.e., it should recognize people despite 3D face recognition approach should be able to handle performance. To be useful in real-world applications, a facial expressions can also degrade face recognition Additionally, variations in face scans due to changes in or some imperfections in the scanning technology. However, 3D scans often suffer from the problem of have a relatively smaller influence on the observations. variables, such as illumination and small pose changes, major advantage over 2D color imaging in that nuisance modalities available for face imaging, 3D scanning has a community over the past three decades. Among different received growing attention within the computer vision biometrics. Accordingly, automated face recognition has recognition has many benefits when compared to other UE to the natural, nonintrusive, and high throughput nature of face data acquisition, automatic face missing parts hav few approaches spent on handling expressions while has been direct

utilize an

Digital Object Identifier no. 10.1109/TPAMI.2013.48. 0162-8828/13/\$31.00 © 2013 IEEE Published by the IEEE Computer Society

different anatomical areas such as the nose, eyes,

deformed elastically to fit each face, thus matching variability across faces. The annotated face model is

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- some chos several ap elastic met surfaces to itate local these, the deformatic deforming

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3D Face Recognition under Expressions, Occlusions, and Pose Variations

Hassen Drira, Boulbaba Ben Amor, Member, IEEE, Anuj Srivastava, Senior Member, IEEE, Mohamed Daoudi, Senior Member, IEEE, and Rii

treating the likelihood ratio as a matching score and using the majority voting for face identification. [29] that uses PCA-LDA for feature extraction,

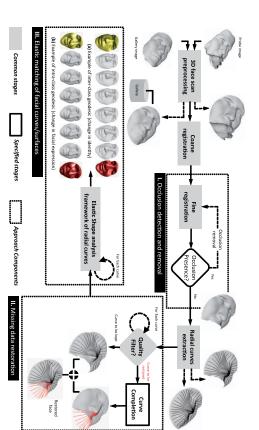
consequently, the facial skin is deformed in a nonisometric manner. In other words, facial surfaces are also stretched or compressed locally, beyond a simple bending of parts.

measure as a similarity measure to match two face images. The authentication score is obtained by combining the SIM values corresponding to the matching of four different face regions: circular and entire face region. In [1], Alyuz et al. use average region models (ARMs) locally to handle the chalelliptical areas around the nose, forehead, and the Queirolo et al. [26] use surface interpenetration DRIRA ET AL.: 3D FACE RECOGNITION UNDER EXPRESSIONS, OCCLUSIONS, AND POSE VARIATIONS

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DRIRA ET AL.: 3D FACE RECOGNITION UNDER EXPRESSIONS, OCCLUSIONS, AND POSE VARIATIONS



Fig. 4. A smile (see middle) changes the shapes of the curves in the lower part of a the face while the act of surprise changes shapes of curves in the upper part of the face (see right).

subset of the Bosphorus dataset that involves occlusions (see the given probes. This approach has been evaluated on a processing is automatic. manual detection of nose coordinates, the remaining Section 4.4). In the last two experiments, except for the the full processing includes Components I+II+III to process missing data restoration (Component II). In these situations,

N RADIAL, ELASTIC CURVES: MOTIVATION

radial facial curves studied using elastic shape analysis. An important contribution of this paper is its novel use of

2.1 Motivation for Radial Curves

example, during a smile, the top half of the face is relatively curves [27], [28]. curves for 3D face recognition was mostly based on level shapes and that is why their role becomes important. The appropriately, curves have the potential to capture regional person is surprised the effect is often the opposite. If chosen unchanged while the lip area changes a lot, and when a affect different regions of a facial surface differently. For and efficient [30], [33]. The changes in facial expressions shapes and the resulting algorithms are very sophisticated has been significant progress in the analysis of curves curves and not other kinds of facial features? Recently, there tip of the nose for representing facial shapes? First, why Why should one use the radial curves emanating from the limitation that each curve goes through different facial separate interclass variability from the intraclass variability field. Ideally, one would like curves that maximally level curves of a function or as the streamlines of a gradient Curves on a surface can, in general, be defined either as the Which facial curves are suitable for recognizing people? important reason for their selection. The next question is: locality of shapes represented by facial curves is an Actually, the previous work on shape analysis of facial regions and that makes it difficult to isolate local variability level curves (of the surface distance function) has (typically due to expression changes). The past usage of the the

4

have tremendous potential. This is because: In contrast, the radial curves with the nose tip as origin

:-The nose is in many ways the focal point of a face. It is example, those used by sketch artists (cheek conrelatively easy and efficient to detect the nose tip tours, forehead profiles, eye boundaries, etc.). automatically extract other types of curves, for automated fashion. It is much more difficult to curves, with the nose tip as the center, in a completely (compared to other facial parts) and to extract radial

> (D) Radiai Bunnan (c) +ac

Fig. 5. An example of matching radial curves extracted from two faces beionging to the same person: a curve with an open mouth (on the left) and a curve with a closed mouth (on the right). One needs a combination of stretching and shrinking to match similar points (upper lips, lower lips, etc.).

- i) Different radial curves pass through different reface, while for the right face the main differences lie relative to the left face, lies in the lower part of the face (right). The main difference in the middle face, face (left), a smiling face (middle), and a surprised This is illustrated in Fig. 4, which shows a neutral cheeks can largely be due to changes in expressions while those for curves passing through the lips and can be loosely attributed to the interclass variability shapes of radial curves in the upper half of the face facial expressions. For instance, differences in the gions and, hence, can be associated with different
- at least some part of every radial curve is usually available. It is rare to miss a full radial curve. In In the case of the missing parts and partial occlusion, full geometry and are applicable to a variety Radial curves have a more universal applicability. in the top half. applications, including facial expression recognition. recognition. In contrast, radial curves capture the as efficient for some other tasks, such as face detecting certain expressions, but they have not been some specific tasks, for example, lip contours in The curves used in the past have worked well for g,

ω

exactly) symmetric and, to a limited extent, missing data via reconstruction, as will be described reflection. This issue is important in handling parts of cheeks due to a bad angle for laser occlusion by glasses, the forehead due to hair, later in this paper. the Q,

contrast, it is more common to miss an eye due to

- Natural face deformations are largely (although not we choose a novel geometrical representation radial around the nose. Based on these arguments, are <u>o</u>
- Ś facial surfaces using radial curves that start from the

- nose tip.

2.2 Motivation for Elasticity

across those curves. One would like the correspondence to closed. To compare their shapes, we need to register points open, whereas the expression on the right has the mouth facial expressions. The expression on the left has the mouth points on these radial curves associated with two different call them β_1 and β_2 . Our task is to automatically match Consider the two parameterized curves shown in Fig. . ज़



under large facial expressions. Fig. 2. Significant changes in both euclidean and surface distances

of elastic shape analysis in 3D face recognition. clearly shows that large expressions can cause stretching distance), while in the other two cases they increase. This To demonstrate this assertion, we placed four markers on a face and tracked the changes in the surface and especially for large expressions. This also motivates the use deformation of the shape of the face is not strictly valid, is elastic in nature. Hence, the assumption of an isometric and shrinking of facial surfaces, i.e., the facial deformation euclidean distance and from 115 to 106 mm for the surface case, these distances decrease (from 113 to 103 mm for the surface distances between these points to change. In one the skin surface and thus causing both euclidean and sions leading to a significant shrinking or stretching of under large expressions. Fig. 2 shows some facial expreseuclidean (straight line) distances between the markers

1.2 Overview of Our Approach

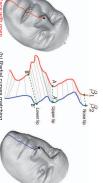
shape analysis. This framework is based on elastically This paper presents a Riemannian framework for 3D facial

as follows: described above. The main contributions of this paper are tip of the nose and it handles several of the problems matching and comparing radial curves emanating from the

- It extracts, analyzes, and compares the shapes of radial curves of facial surfaces.
- It develops an elastic shape analysis of 3D faces by extending the elastic shape analysis of curves [30] to 3D facial surfaces.
- detection and removal step that is based on To handle occlusions, it introduces an occlusion
- tangent spaces of the shape manifold to model the manifolds of curves. Specifically, it uses PCA on To handle the missing data, it introduces a restorarecursive-ICP. tion step that uses statistical estimation on shape

ping), coarse and fine alignment, radial curve extraction, (nose tip localization, filling holes, smoothing, face cropcommon to all situations include 3D scan preprocessing suitable only for specific situations. The basic steps that are application scenarios, there are also some specialized tools laid out in Fig. 3. While some basic steps are common to all quality filtering, and elastic shape analysis of curves The different stages and components of our method are partially observed curves. normal curves and uses that model to complete the

probe images out of nine have large pose variations (see Section 4.3). Some steps are only useful where one anticipates some data occlusion and missing data. These steps include occlusion detection (Component I) and on the GAVAB dataset where, for each subject, four the standard protocol (see Section 4.2). It is also tested basic setup is evaluated on the FRGCv2 dataset following (Component III and quality module in Component II). This



| IEEE TRANSACTIONS ON PATTERN ANALY | EEE TRANSACTIONS ON PATTERN ANALYSIS AND MACHINE INTELLIGENCE, VOL. 35, NO. 9, SEPTEMBER 2013 | DRIRA ET AL .: 3D FACE RECOGNITION UNDER EXPRESSIONS, OCCLUSIONS, AND POSE VARIATIONS | NS, AND POSE VARIATIONS 2275 |
|--|--|---|---|
| | | | similar metric and representation for curves was also developed by Younes et al. [33], but it only applies to planar curves and not to facial curves.) This point is very important as it simplifies the analysis of curves under the elastic metric to the standard functional analysis. Further- more, under the \mathbb{L}^2 -metric, the reparameterization group acts by isometries on the manifold of q functions, which is not the orase for the original curve A for olaborate on the last |
| radial curves: Images in the middle illustrate the the face surface and planes to form two radial not radial curves is illustrated in the rightmost image. The other words, the lips should match the n should match the chin. Clearly, if we th parameterization and match points that distance from the starting point, then the | | Fig. 8. Curve quality filter: examples of detection of broken and short curves (in red) and good curves (in blue). | point, let q be the SRVF of a curve β . Finer, the SRVF of a reparameterized curve $\beta \circ \gamma$ is given by $\sqrt{\gamma}(q \circ \gamma)$. Here γ : $I \to I$ is a reparameterization function and let Γ be the set of all such functions. Now, if q_1 and q_2 are SRVFs of two curves β_1 and β_2 , respectively, then \tilde{r} is a set of two curves β_1 and β_2 , respectively. Then \tilde{r} is asy to show that under the \mathbb{L}^2 norm, $\ g_1 - q_2\ = \ \sqrt{\gamma}(q_1 \circ \gamma) - \sqrt{\gamma}(q_2 \circ \gamma)\ $ in general. This is one more reason why SRVF is a better reasonable for each of an each of a set of the other set. |
| | Fig. 7. Curves extraction on a probe face after its rigid alignment with a gallery face. In (a), the nose region of the probe is missing and filled using linear interpolation. The probe and gallery faces are from the same class for (a) and (b), while they are from different classes for (c). of deformations associated with changes in facial expres- sions and for handling missing data. In our experiments, the probe face is first rigidly aligned to the gallerv face using the ICP algorithm. In this step, it is | In situations involving nonfrontal 3D scans, some curves may be partially hidden due to self-occlusion. The use of these curves in face recognition can severely degrade the recognition performance and therefore they should be identified and discarded. We introduce a quality filter that uses the continuity and the length of a curve to detect such curves. To pass the quality filter, a curve should be one continuous piece and have a certain minimum length, say of | Define the preshape space of such curves: $C = (q: I \rightarrow \mathbb{R}^3 q = 1\} \subset \mathbb{L}^2(I, \mathbb{R}^3)$, where $\ \cdot\ $ implies the \mathbb{L}^2 norm. With the \mathbb{L}^2 metric on its tangent spaces, C becomes a Riemannian manifold. Also, since the elements of C have a unit \mathbb{L}^2 norm, C is a hypersphere in the Hilbert space $\mathbb{L}^2(I, \mathbb{R}^3)$. Furthermore, the geodesic path between any two points $q_1, q_2 \in C$ is given by the great circle, $\psi : [0, 1] \rightarrow C$, where |
| | userul but not critical to accurately find the nose up on the probe face. As long as there is a sufficient number of distinct regions available on the probe face, this alignment can be performed. Next, after the alignment, the radial curves on the probe model are extracted using the plane P_α passing through the nose tip of the <i>gallery</i> model at an angle α with the vertical. This is an important point in that only the | either from missing data or large noise. We show two examples of this idea in Fig. 8, where we display the original scans, the extracted curves, and then the action of the quality filter on these curves. Once the quality filter is applied and the high-quality curves retained, we can perform face recognition procedure using only the remaining curves. That is, the comparison is based only on curves that | $\begin{split} \psi(\tau) &= \frac{1}{\sin(\theta)} (\sin((1-\tau)\theta)q_1 + \sin(\theta\tau)q_2), (1) \\ \text{and the geodesic length is } \theta &= d_c(q_1,q_2) = \cos^{-1}(\langle q_1q_2 \rangle). \\ \text{To study shapes of curves, one should identify all rotations and reparameterizations of a curve as an equivalence class. Define the equivalent class of q as \end{split}$ |
| rization of two curves does not change veen them. This in turn enables us to fix ation of one curve arbitrarily and to he parameterization of the other. This is to a proper distance (geodesic distance) is to raproper distance (geodesic distance) reformation (geodesic) between the shapes ther words, it results in their elastic ase refer to [30] for details. | nose tip of the gallery and a good alignment between the gallery probe is needed to extract good-quality curves. Even if some parts of the probe face are missing, including its nose region, this process can still be performed. To demonstrate this point, we take session ##0405d22, from the FRGCv2 dataset, in which some parts of the nose are missing and are filled using a linear interpolation filter (top row of Fig. 7). The leftmost panel shows the hole- | have passed the quality filter. Let β denotes a facial curve; we define the Boolean function <i>quality</i> : (<i>quality</i> (β) = 1) if β passes the quality filter and (<i>quality</i> (β) = 0) otherwise. Recall that during the preprocessing step, there is a provision for filling holes. Sometimes the missing parts are too large to be faithfully filled using linear interpolation. For this reason, we need the quality filter that will isolate and remove curves associated with those parts. | $\begin{split} & [q] = \operatorname{closure} \{\sqrt{\dot{\gamma}(t)} Oq(\gamma(t)) O \in SO(3), \ \gamma \in \Gamma \}. \\ & \text{Theset of such equivalence classes, denoted by $S = \{ [q] q \in C \}$, is called the slupe space of open curves in \mathbb{R}^3. As described in $\{30\}, S is a metric space with the metric inherited from the larger space C. To obtain geodesics and geodesic distances between elements of S, one needs to solve the optimization problem: $$ $$ $$ $$ $$ $$ $$ $$ $$ $$ $$ $$ $$$ |
| IVES exed collection exed as follows: output of the <i>S</i> is chosen to <i>T</i> rotated to the is obtained by as the none the | filled probe face, the next panel shows the gallery face, the third panel shows its registration with the gallery face and extracted curves on the gallery face. The last panel shows the extracted curves for the probe face. As shown there, the alignment of the gallery face with the probe face is good despite a linear interpolation of the missing points. Then, we use the gallery nose coordinates to extract radial curves on the probe surface. The gallery face in this example belongs | 3 SHAPE ANALYSIS OF FACIAL SURFACES In this section, we will start by summarizing a recent work in elastic shape analysis of curves and extend it to shape analysis of facial surfaces. 3.1 Background on the Shapes of Curves Let B · I → IB³ represent a parameterized curve on the face | $(O^*, \gamma^*) = \underset{(O, \gamma) \in SO(3) \times \Gamma}{\operatorname{argmin}} d_e(q_1, \sqrt{\gamma}O(q_2 \circ \gamma)).$ (2) For a fixed O in $SO(3)$, the optimization over Γ is done using the dynamic programming algorithm while, for a fixed $\gamma \in \Gamma$, the optimization over $SO(3)$ is performed using SVD. By iterating between these two, we can reach a solution for the joint optimization problem. Let |
| | to the same person under the same expression. In the second row, we show an example where the two faces belong to the same person but represent different expressions/poses. Finally, in the lastrow we show a case where the probe and the gallery faces belong to different people. Since the curve extraction on the probe face is based on the gallery nose coordinates, which belong to another person, the curves may be shifted in this nose region. However, this small inaccuracy in curve extraction is actually helpful since it increases the interclass distances and improves the bio- metric performance. | where $I = [0, 1]$. To analyze the shape of β , we shall represent it mathematically using the square-root velocity function (SRVF) [30], denoted by $q(t) = \frac{\dot{\beta}(t)}{\sqrt{\dot{\beta}(t)}}$; $q(t)$ is a special function of β that simplifies computations under the elastic metric. More precisely, as shown in [30], an elastic metric for comparing shapes of curves becomes the simple L ² -metric under the SRVF representation. (A | $q_{\pm}^*(t) = \sqrt{\gamma^*(t)}O^*q_2(\gamma^*(t)))$ be the optimal element of $[q_2]$ associated with the optimal rotation O^* and reparameterization γ^* of the second curve; then the geodesic distance between $[q_1]$ and $[q_2]$ in S is $d_*([q_1], [q_2]) = d_*(q_1, q_2^*)$ and the geodesic is given by (1), with q_2 replaced by q_2^* . 3.2 Shape Metric for Facial Surfaces Now, we extend the framework from radial curves to full facial surfaces. A facial surface <i>S</i> is represented by an |

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S 2 0 °

Fig. 6. Extraction of radi intersection between the curves. The collection of n

be such that geometrix well as possible. In othis force an arc-length para are at the same distant resulting matching with on β_1 will not match the not placed at the same curves, the problem of same as that of optit that we need to funct such that the point $\beta_2(\gamma(t))$, for all *t*. The for an arbitrary β_1 and all such γ_5 is infinite of functions. As described in [30 solving an optimizin gramming algorithm, developed from a Ric termed an *elastic met* same reparameterization the distance between the distance between the distance the parameterization optimization leads to and an optimization leads to comparisons. Please r

2.3 Automated E

preprocessing step. T be the vertical curve i upright position. The slicing the facial surfa as its origin and make the reference curve. T gives the radial curv radial curves from *S* v in a set of curves that shows an example of If needed, we car these radial curves a Each facial surface is of radial curves that Let S be a facial s

represent a surface. strate that the elastic In the later exper

deformation, we compare it qualitatively for faces with score for analyzing faces. In addition to their interpretation distance d_S is computed by the following algorithm. SRVF of the radial curve β_{α}^{i} on the *i*th facial surface. The between two facial surfaces is $d_{\mathcal{S}}: \mathcal{S}^n \times \mathcal{S}^n \to \mathbb{R}_{\geq 0}$, given at the same angle on a gallery face. Thus, the distance at an angle α on a probe face is compared with the curve element of the set S^n . The indexing provides a correspon*n* uniform angles $\mathcal{A} = \{0, \frac{2\pi}{n}, \frac{4\pi}{n}, \dots, 2\pi \frac{(n-1)}{n}\}$. Thus, Fig. 9. Examples of geodesics in the shape space. The top three rows illustrate examples of interclass geodesics and the bottom three rows illustrate intraclass geodesics. 2276 points in between registered points under an ICP registration of the deformation obtained using a linear interpolation illustrated later. To demonstrate the quality of this and measuring the shape covariance of a set of faces, as geodesics can also be used for computing the mean shape as optimal deformations under the chosen metric, the current algorithms that provide some kind of a similarity different expressions and are termed intraclass geodesics illustrate paths between faces of the same person conveying termed interclass geodesics, whereas the remaining rows illustrate paths between faces of different subjects and are between source and target faces. The three top rows Shown in Fig. 9 are examples of some geodesic paths paths between faces when represented as elements of \mathcal{S}^n these full deformations can be shown to be formal geodesic to obtain deformations between full facial surfaces. In fact corresponding curves, we can combine these deformations by $d_S(S^1, S^2) \doteq \frac{1}{n} \sum_{\alpha}$ dence between curves across faces. For example, the curve shape of a facial surface can been represented as indexed collection of radial curves, indexed by These geodesics provide a tangible benefit beyond the Since we have deformations (geodesic paths) between 110 1100 1= 115 10 ALL. Fig. 10. The three rows show, respectively, a 15 110 12 $a_{\alpha \in \mathcal{A}} d_s([q_{\alpha}^1], [q_{\alpha}^2]).$ Here, q_{α}^i denotes the HC? IEEE TRANSACTIONS ON PATTERN ANALYSIS AND MACHINE INTELLIGENCE, VOL. 35, NO. 9, SEPTEMBER 2013 1E 11C HE I Oc the the an <u>ω</u> ω in the mouth area. (bottom row). Algorithm 1. Elastic distance computation ena for $i \leftarrow 1$ to 2 do Output: The distance d_S . Input: Facial surfaces S_1 and S_2 . Compute $d_S = \frac{1}{n} \sum_{\alpha \in \mathcal{A}} d_s(q_{\alpha}^1, q_{\alpha}^{2*})$, where *n* is the number of valid pairs of curves. end for $\alpha \leftarrow 0$ to 2Π do end Extract the curve β_{α}^{i} ; compute de using Eqn. 2

Fig. 10. Examples of geodesics in shape space (top row), preshape space (middle row), and a linearly interpolated path after ICP alignment

in Fig. 10. However, the optimal matching is not established natural opening of the mouth, as illustrated in the top row are well matched across the two surfaces. The upper lips between curves is established and thus anatomical points other words, the optimal matching (reparameterization) the preshape space, and a path using ICP. Algorithm 1 is match the upper lips, for instance, and this helps produce a used to calculate the geodesic path in the shape space. In geodesic path in the shape space, the corresponding path in This results in an unnatural deformation along the geodesic yet when the geodesic is calculated in the preshape space.

if $quality(\beta_{\alpha}^1) = 1$ and $quality(\beta_{\alpha}^2) = 1$ then $d_s([q_\alpha^1], [q_\alpha^2]) = \cos^{-1}(\langle q_\alpha^1, q_\alpha^{2*} \rangle)$ set $q_{\alpha}^{2*}(t) = \sqrt{\dot{\gamma}_{\alpha}^{*}(t)}O_{\alpha}^{*}q_{\alpha}^{2}(\gamma_{\alpha}^{*}(t)))$ re-parameterization alignment O^*_{α} and Compute the optimal rotation and

Computation of the Mean Shape

rithm for computing the Karcher mean is a standard one, function: $\mathcal{V}: S^n \to \operatorname{IR}, \mathcal{V}(S) = \sum_{i=1}^{k} d_S(S^i, S)^2$. The Karcher mean is then defined by $\overline{S} = \arg\min_{S \in S^n} \mathcal{V}(S)$. The algoof facial surfaces $\{S^1, \ldots, S^k\}$ in S^n , we define an objective face of a group of faces. To calculate a Karcher mean define an average face that can serve as a representative example, one can use the notion of Karcher mean [14] to to compute summary statistics of a set of faces. For Riemannian approach over many past papers is its ability As mentioned above, an important advantage of our

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Fig. 11. The Karcher mean of eight faces (left) is shown on the right.

shown in Fig. 11. mean face for eight faces belonging to different people is given facial surfaces $\{S^1, \dots, S^n\}$ that has the smallest total (squared) deformation from all has a nice geometrical interpretation: S is an element of S^n pick any one of those solutions as the mean face. This mean This minimizer may not be unique and, in practice, one can see, for example, [8], and is not repeated here to save space , S^k}. An example of a Karcher

3.4 Completion of Partially Obscured Curves

curves. occluded using information from the visible part and the in the shape space of radial curves to complete the broken the face and points that belong to the occluding object, we occlusion to occur. Once we detect points that belong to strained, there is a high probability for this kind of cooperative situation, where the acquisition is unconocclusions, the majority of radial curves could have hidden occlusions, such as glasses and hair. In the case of external sufficient when parts of a face are missing due to external effective in handling some missing parts, it may not be first remove the occluding object and use a statistical model parts of the occluding object(s) in the scan. In a nonbecause, in addition to the missing parts, we can also have parts that should be predicted before using these curves. removes curves with missing parts. Although this step is Earlier we introduced a filtering step that finds and This problem is more challenging than self-occlusion This replaces the parts of face that have been

earlier, we can compute the sample Karcher mean of their shapes taken from the training faces at that angle. As described curve, and let $q_{\alpha}^1, q_{\alpha}^2, \ldots, q_{\alpha}^k$ be the SRVFs of the curves PCA. Let α denote the angular index of the observed is a nonlinear space, we use the tangent space $T_{\mu}(S)$, coefficients of the observed curve and the coefficients help training shapes. Then, this basis is used to estimate the vector space to form an orthogonal basis representing we use the PCA of the training data in an appropriate complete the observed curve. To keep the model simple, training curves at the same angle that are extracted from (partially observed) curve and 2) several (complete) able for this prediction are as follows: 1) the current predict its completion. The sources of information availsurfaces by curves, is to take a partial facial curve and training data. where μ is the mean of the training shapes, to perform reconstruct the full curve. Since the shape space of curve Sthe curve from the training curves and use that to full faces. The basic idea is to develop a sparse model for The core of this problem, in our representation of facial $\{[q_{\alpha}^{i}] \in S\}$, denoted by μ_{α} . Then, using the

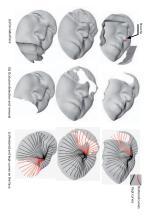


Fig. 12. (a) Faces with external occlusion, (b) faces after the detection and removal of occluding parts, and (c) the estimation of the occluded parts using a statistical model on the shape spaces of curves.

obtain $v_{i,\alpha} = \exp_{\mu_{\alpha}}^{-1}(q_{\alpha}^{i})$, where tangent space using the inverse exponential map. We geometry of S we can map these training shapes in the

$$\exp_{q_1}^{-1}(q_2) = \frac{\theta}{\sin(\theta)} \left(q_2^* - \cos(\theta) q_1 \right), \quad \theta = \cos^{-1} \left(\left\langle q_1 q_2^* \right\rangle \right),$$

significant basis elements. $u_{1,\alpha}, u_{2,\alpha}, \dots, u_{J,\alpha}$, where J represents the number the tangent vectors $\{v_i\}$ leads to the principal basis vectors of q_2 to be aligned with q_1 , as discussed earlier. A PCA of and where q_2^* is the optimal rotation and reparameterization <u>o</u>f

and estimate the SRVF of the full curve according to chosen basis according to $c_{j,\alpha} = \langle q, u_{j,\alpha} \rangle \approx \int_0^\tau \langle q(t), u_{j,\alpha}(t) \rangle dt$ $t > \tau$. Then, we can estimate the coefficients of q under the of this curve q(t) is known for $t \in [0, \tau]$ and unknown for parameter value t in $[0, \tau] \subset [0, 1]$. In other words, the SRVF occluded curve, let us assume that this curve is observed for Now, returning to the problem of completing a partially

$$\hat{q}_{lpha}(t)=\sum_{j=1}^{J}c_{j,lpha}u_{j,lpha}(t)\quad t\in[0,1].$$

passing through the missing parts are restored and shown result of that step is shown in column (b). Finally, the curves is performed as described in the previous section, and the in column (a). The detection and removal of occluded parts with each face corrupted by an external occlusion as shown We present three examples of this procedure in Fig. 12,

of the restoration process. corresponding face in the gallery demonstrate the success signed deviation between the restored face and the Fig. 13. The small values of both absolute deviation and with the complete neutral face of that class, as shown in the restored surface (shown in the top row of Fig. in column (c). To evaluate this reconstruction step, we have compared 12)

recognition method together they facilitate an exhaustive evaluation of a 3D face comprehensive framework for 3D face recognition using a databases have different characteristics and challenges, and variety of well-known and challenging datasets. These In the remainder of this paper, we will apply this

| inside a euclidean sphere of radius 73 mm centered at the nose tip to discard as much hair as possible. The nose tip is automatically detected for scans with occlusions and large pose variation. TAB Comparison of Rank-1 Scores on the FRR Spreaments [29] Wang et al. [31] Berreth et al. [2] O 99% 94.1% 94.1% | <figure><figure><figure><figure><figure><figure><figure></figure></figure></figure></figure></figure></figure></figure> | | |
|---|---|---|--|
| dean sphere of radius 75 mm centered not tested in this dataset. For that end, one would need a protodiscard as much hair as possible. systematic evaluation on a dataset with the missing data is automatically detected for frontal issues, for example, the GavabDB. The best recognition nanually annotated for scans with score on FRGCv2 is reported by Spreeuwers [29], who use an intrinsic coordinate system based on the vertical large pose variation. TABLE 1 TABLE 1 Comparison of Bank-1 Scores on the FRGCv2 Dataset with State-of-the-Art Results Rectal [32] Haar et al. [31] Bernetit et al. [21] Queinolo et al. [26] Faltemer et al. [91] Bernetit et al. [21] 935% 97% | $truys NO MOHNE INTELLIGENCE. VOL. 35, NO. 9, SEPTEMBER 2013 \\ truy ruy \mathsf$ | | |
| TAB TAB Recognition Results Comparison of th Neutral Lee et al. [16] Moreno et al. [22] Ma Expressive 96.67% 97.9% 77.9% Neutral-respressive 94.86% 77.9% 77.9% Rotated looking up - - - Scans from right side - - - Scans from left side - - - | $\label{eq:product} \begin{split} & \ \end{pintument} \\ & \ \end{pintument} \\ & \ \end{pintument} \\ & \ \end{pintument} \\ & \ \end{pintum} | | |
| TABLE 3 TABLE 3 Lee et al. [16] Monor et al. [18] Haar et al. [31] Monsavi et al. [23] current Methods on the GavabDB Lee et al. [16] Monor et al. [18] Haar et al. [31] Monsavi et al. [23] current Methods on the GavabDB 96.07% 90.16% - 100% - 100% - 95.9% - 95.9% - 95.9% - 95.9% - 95.9% - 95.9% - 95.9% - 95.9% - 95.9% - - 95.9% - 95.9% - 95.9% - - - - - - - - - <th col<="" td=""><td>$\label{eq:horizon} \begin{tabular}{ c$</td><td></td></th> | <td>$\label{eq:horizon} \begin{tabular}{ c$</td> <td></td> | $ \label{eq:horizon} \begin{tabular}{ c $ | |

| Fig. 18. Gradual removal of occluding parts in a faces scan strater recursive-CP. Fig. 18. Gradual removal of occluding parts in a face scan strater are occluded in the probe dataset. As far as faces with the neutral expressions are concerned, the recognition accuracy naturally depends on their pose. The performance departs are occluded in those scans. However, for pose variations up to 35 degrees, the performance is still high (100 percent for looking up and 98.36 percent for looking down). Fig. 17 (top row) shows examples of successful matches for up and down looking faces and unsuccessful matches for up and down looking faces and unsuccessful matches for up and down looking faces and unsuccessful matches for up and other approaches in terms of the recognition rate. Note that there is no prior result in the literature on 3D face recognition using sideway-scans from this database. Although our method owrels well on common faces with a range of pose variations within 35 degrees, it can potentially fail when a large part of the nose is missing as it can cause an incorrect alignment between the probe and the gallery. This situation occurs if the face is partially occluded by external objects such as glasses, hair, and so on this section, we will use components I (occlusion the section and removal) and II (missing data restoration in the algorithm. The first problem we encounter in externally occluded faces is the detection of the external object parts. We accompliate this the corresponding scans that are complete, frontal, and have neutral expressions. The basis for such as glassed of the external against and agiven scans is implemented as follows: In each iteration, we match the current face scan with the emplate and a given scans is are incrementally expression of the scan with the emplate scan is ever the external against and against and against and against and against and against and against and against and against and against and against against against against against against against against again | EEE TRANSACTIONS ON PATTERN AMAI |
|---|--|
| Fig. 18 shows an example of this implementation. From left to right, each face shows an increasing alignment of the test face with the englate, with the aligned parts shown in green at the end. In the case of faces with external occlusion, we first resoure them and then apply the recognition procedure. That is, we detect and remove the occuleded part and recover the missing part, resulting in a full face that can be compared with a gallery face using the metric 4.5. The easies the nose tip coordinates are already provided. The Bosphorus database is suitable for this evaluation as it contains scans of 60 men and 45 women, 105 subjects in total, in various poses, expressions, and in the presence of external occlusion (eyeglasses, hand, hain). The majority of the subjects are aged between 25 and 35. The unuber of total face scans is 4,652, at least 54 scans each are available for most of the subjects, while there are only 31 scans each for 34 of them. The interesting part is that for each subject there are four scans with occluded parts. These occlusions refer to I. mouth occlusion by hand, Fig. 19 shows sample images from the Bosphorus 3D dataset illustrating a full scan on the left and the remaining scans with typical occlusions. We pursued the same evaluation protocol used in the presented in Fig. 20 for different approaches disjoint. The rank-1 recognition rate is reported in Fig. 20 for occlusion 2.4. However, if we perform restoration, the recognition rate is improvent when we remove the cocluded parts significantly increases the accuracy of recognition algorithm using the recognition goed by a scans so is stored in Fig. 20 for different approaches disported in Fig. 20 for different significantly increases the accuracy of recognition algorithm using the react is reported in Fig. 20 for different approaches depending upon the type of occlusion 2.4. However, if we perform restoration, the recognition rate is improved to mose it more the are disjoint. The rank-1 recognition r | The terms and the different types of occlusions are lititated. |
| Figure 10 and 10 | DRIPA ET AL: 3D FACE RECOGNITION UNDER EXPRESSIONS, OCCURSIONS, AND POSE VARIATIONS manual data and and and and and and and and and an |
| 5 Discussion <i>et al.</i> 1915 isome at al. 2017 isome at al. 201 | vs, AND POSE VARIATIONS Comparative Stt Recognition Proposed Waysmanne 129 Information 141 Contemporate Information 255 Stationaries et al. 101 Contemporate Cont |

ariations in facial expressions, we have proposed an elastic presentation by using a curve representation of a 3D face nd a quality filter for selecting curves. Second, to handle ollection of curves, and then represent a curve (with atistical shape models. That is, we have constructed a lowen to recover only the missing data on the 3D scan using nape analysis of 3D faces. Finally, in the presence of cognition in noncooperative scenarios. First, to handle ariations of facial expression, pose variations, and occluissing data) as a linear combination of its basis elements. mensional shape subspace for each element of the indexed clusion, we have proposed to remove the occluded parts, ose variation and missing data, we have proposed a local veral properties that make it appropriate for 3D face ons between gallery and probe scans. This method has esented results on 3D face recognition designed to handle atistical shape analysis of facial surfaces. We have also this paper, we have presented a framework for a

CONCLUSION

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DISCUSSION

preprocessing (s)

Comparison time(s)

> 1/11 150 1.27 2.4 Face match-ing (s) 0.65

1/1000 15

18 9.92 TABLE 4 Comparative Study of Time Implementations and Recognition Accuracy on FRGCv2 of the Proposed Approach with State of the Art

ur fully automatic results obtained on the FRGCv2 are near rst column. In the second column, we report the time needed eeded for preprocessing and/or feature extraction in the RGCv2 dataset. For each approach, we report the time e top. Table 4 also reports the computational time of our t for 3D face recognition in the presence of large expresdifferent approaches. Regarding computational efficiency, dumn, we report the accuracy (recognition rate on FRGCv2) evious computation times for each approach. In the last compare two faces. The third column is the sum of the two proach and some state-of-the-nbsp;art methods on the ons, nonfrontal views, and occlusions. As listed in Table 4, we obtained competitive results relative to the state of the ental results using three well-known 3D face databases. We esence of different challenges, we have presented experistudy the performance of the proposed approach in the

ethods for nonfrontal views and for faces that

nanually annotated for nonfrontal and occluded faces. In erformance of our approach since the computation of curve arallel techniques can also be exploited to improve ndergone occlusion. e future, we hope to develop automatic nose tip detection In the case of GavabDB and Bosphorus, the nose tip was stances, preprocessing, and so on, are independent tasks. have

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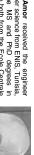
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Abstract—We utilize ideas from two growing but disparate ideas in computer vision—shape analysis using tools from differential geometry and feature selection using machine learning—to select Lahoucine Ballihi, Boulbaba Ben Amor, Mohamed Daoudi, Senior Member, IEEE, Anuj Srivastava, Senior Member, IEEE, and Driss Aboutajdine, Senior Member, IEEE Recognition and Gender Classification and gender classification. Section III overviews the proposed methods. It also presents some progress in 3-D imaging-based an emphasis on facial curve-based and facial feature-based dent of the ethnicity. Specifically, the main contributions of this portant issue in intelligent systems. In this work, we focus on a motivates the use of 3-D shapes for gender classification. recognition. Gender is similar to other soft biometric traits, such esting problem that can be a useful preprocessing step for face state-of-the-art methods have focused on the variability caused summarizes existing approaches on 3-D face recognition with paper include: classifying either facial identity and/or gender, both indepennition grand challenge. Our approach offers the advantage of cial expressions variation, an important focus of the face recogprocess we also develop an effective approach for tackling faeterized curves using tools from differential geometry. In the features is based on latest advances in shape analysis of paramautomatic face recognition and gender classification is an imships both with 2-D information and 3-D shape [1], [2], and it not yet been used extensively for gender classification. Several distinguish their peers. Most existing work on gender classifias skin color, age, eyes colors, and so on, used by humans to At the same time, gender classification is emerging as an interhave proposed methods that are robust to such shape variations by facial deformations, e.g., those due to face expressions, and approach for both the target applications. In Section IV, we faces in an intrinsic fashion, and comparisons of these curve from different types of facial curves extracted from facial surface recognition and gender classification. The features comes automatic and versatile enough for different applications like feature selection technique from machine-learning that is fully works in psychology have shown that gender has close relationhair density and inner morphology of the face, but 3-D shape has cation uses 2-D-images to extract distinctive facial features like The development of a practical, high-performance system for The rest of the paper is organized as follows. Section II suitable for gender discrimination. tion we are interested in finding those facial curves that are most shape represented by collections of curves. In particular, A new gender classification approach using the 3-D face expressions. In particular, we are interested in finding those tics for recognition while handling the challenge of facial A new geometric feature-selection approach for efficient facial curves that are most suitable for 3-D face recogni-3-D face recognition that seeks most relevant characterispression variations components to enhancing the robustness of their system to exerage quantitative weights related to different facial physical which they called multiscale local normal patterns (MS-LNPs) weighted sparse representation of encoded normal information, an expression-robust 3-D face recognition approach by learning of the face in a face recognition system. Li et al. [9] proposed and the eyes are consistently marked as discriminative regions tive information of their vertices. They observed that the nose tices (e.g., image or 3-D meshes) in terms of the discriminaposed a Markov Random Field model for the analysis of latresults on the GAVAB database. In [8] Ocegueda et al. protations to the collected low-level features and achieved good sensitivities to facial expressions. They applied sparse representures, such as curvatures, and ranked them according to their in order to collect various types of low-level geometric feaboth the local similarity and the change characteristics between Gabor, and Local Binary Pattern (LBP) were used to encode tion for the shape comparison. Based on the SSDMs, Haar-like, between two aligned 3-D faces as a intermediate representaet al. [6] computed a signed shape difference map (SSDM) automatically for improving recognition. More recently, Wang temier et al. [5], the nose tip and 28 small regions were selected and the nose. In the 3-D face recognition approach used by Falcomparing the recognition rates, and concluded that the best sesearch over possible combinations of used/unused landmarks, a face is represented as a vector of distances between pairs of recognition. Daniyal et al. [4] proposed an algorithm in which A. Feature Selection-Based 3-D Face Recognition tion and holistic facial curves. previous methods that primarily use local facial feature-selecparison with feature selection techniques, we mainly focus on with a discussion and summary in Section VIII.1 approaches are given in Section VII. We conclude in the paper the feature selection step, for each of the two applications. face using an indexed family of curves which provide an lected optimally by boosting. Using similar features, Li et al. facial shapes. The most discriminative local features were selection corresponded to the landmarks located around the eyes facial landmarks. They selected the landmarks by exhaustive inative power of different facial regions or features for face Experimental evaluations and comparative studies to previous facial surface shape descriptor. They utilized the learned av-[7] proposed to design a feature pooling and ranking scheme The basic idea of these approaches is to represent a sur-Several methods have been proposed to analyze the discrim-As the proposed approach combines curve-based face com-Curve-Based Face Representation II. RELATED WORK C. Gender Classification selection approach for efficient 3-D face recognition. pressions. More recently Ballihi et al. [3] propose a new curve exhibits smooth variations for changes induced by facial exapproximate representation of local morphology of faces that into iso-geodesic stripes and 3DWWs together provided pairs of points of the corresponding stripes. Face partitioning captured mutual relative spatial displacement between all the referred to as 3-D Weighted Walkthroughs (3DWWs), that graph and edges between nodes were labeled with descriptors. width iso-geodesic facial stripes were used as nodes of the distance on the face to extract iso-geodesic facial stripes. Equal reparametrization (or matching) problem that they solve using the dynamic programming algorithm. This approach provided facial surfaces (including opening the mouth) as an optimal time using radial curves. They model elastic deformations of the same authors proposed similar shape analysis approach this performing partial human biometrics. More recently, in [15], In [14], Drira et al. explored the use of shapes of noses for should also be annotated with respect to facial expressions. main limitation of this approach is the need for a large set which sions is obtained by fitting these models to unknown faces. The and facial expression factors. The invariance to facial expres-Then, they construct bilinear models that decouple the identity algorithm that establishes correspondence among a set of faces representation, they proposed an elastically deformable model polar parametrization by disconnecting the lips. Through this the isometry assumption and thus they adapt their geodesic deformation when the mouth is closed. Otherwise, it violates tion, the intrinsics attributes do not change under isometric and the correspondence of curves and points across faces was between these curves. Here also, the matching was not studied metric and a path-straightening method to compute geodesics function that resulted in 3-D curves. They used a nonelastic proposed to compare facial surface by using two metrics: here (that is, the mapping was fixed to be linear). The authors and deform faces; nonlinear matching problem was not studied shape analysis of planar curves, taken from [11], to compare pose is nonfrontal. In [16], Berretti et al. used the geodesic promising results on GAVAB database even where the probe parametrization of the facial surface. With this parametrizasimply linear. In [13], Mpiperis et al. proposed a geodesic polar discussion on how to obtain optimal curves. Later in [12], the Euclidean mean and geometric mean. However, there were no same authors used the level curves of the geodesic distance

forehead and cheeks regions, provides a very compact signature of a 3-D face and a fast classification algorithm for face recogniwith a minimal set of features. This greatly reduced set, consisting of some level curves on the nose and some radial curves in the most in 3-D face recognition and gender classification. First, a large set of geometries curve features are extracted using level sets (cir-cular curves) and streamlines (radial curves) of the Euclidean distion and gender selection. It is also efficient in terms of data storage and transmission costs. Experimental results, carried out using the and derive a composite classifier that achieves high performance known Adaboost algorithm for feature selection from this large set and highlight salient geometrical facial features that contribute a gender classification rate of 86% rate. FRGCv2 dataset, yield a rank-1 face recognition rate of 98% cial surfaces with arbitrarily high accuracy. Then, we use the welltance functions of the facial surface; together they approximate fa-

path, facial curves, machine learning, feature selection. ndex Terms—Face recognition, gender classification, geodesic

I. INTRODUCTION

difficult challenges, such as pose variations, changes in lighting become a major research area in the last few years. Many of the bustness of 3-D observations to lighting conditions and pose conditions, occlusions, and facial expressions. Due to the rothe technology for 2-D image-based face recognition still faces popular modality in the biometrics community. Unfortunately, S INCE facial biometrics is natural, contact free, nonintru-sive, and psychologically supported, it has emerged as a variations, face recognition using shapes of facial surfaces has

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present procedures for extracting facial curves. Section

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¹This work was presented in part in the 4th Eurographics Workshop on 3-D Object Retrieval, 2011 [3].

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and describes the use of the boosting procedure to achieve Section VI, we give formulations to the classification problem recalls the main ideas of the Riemannian geometric shape analysis framework to compare and match facial curves. In define facial curves. Since these curves are planar, they used for instance, used the level curves of the height function approximate representation of the surface. Samir et al. [10]

scanners for capturing three-dimensional (3-D) observations of as illumination and pose. An emerging solution is to use laser are inherently limited by variability in imaging factors such classification is still a distant goal. 2-D Image-based methods makes face gender classification an extremely efficient and has been made, the task of automated, robust face gender fast cognitive process [17]. Although a significant progress The human face presents a clear sexual dimorphism that

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Boosting 3-D-Geometric Features for Efficient Face

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to select the most relevant curves for 3-D face recognition and using adaptive boosting. Thus, we propose to represent a facial shape and we propose to learn the most relevant curves the face, the lower region of the face, the nose and the left eye) the authors assumed that the sex of a face is perhaps its most or femininity of the heads were revealed. In O'Toole et al. [2] cant effects of such manipulations on the apparent masculinity at deciding whether faces are male or female, even when cues in which they tested the human visual system that is accurate gender classification? To address these issues, our strategy in-(ii) How to compare shapes of facial curves?, and (iii) How raises a few issues : (i) How to define curves on facial surfaces? for 3-D face recognition and gender classification. This strategy cial surface by two types of facial curves, radials and levels we consider curves as geometric features that capture local farepresentation/parametrization of facial surfaces. In this paper methods on curve-based 3-D face recognition used a holistic was proposed for fusion of information from four regions (upper region of on SVM, for 3-D frontal neutral expression facial. A method proposed a fusion-based gender classification method, based the registered range and intensity images. Yuan et al. [20] proposed for ethnicity and gender identifications by combining Support Vector Machine (SVM). An integration scheme is also information of human faces for ethnicity identification using a gender classification. Xiaoguang et al. [19] exploited the range leading eigenvectors. They adopted a Bayesian method for normals to increase the gender discriminating power in the ysis (WPGA) method to extract features from facial surface method. They described a weighted principal geodesic analimages using a non-Lambertian Shape-from-shading (SFS) needle-maps) which can be recovered from 2-D intensity classification based on 2.5D facial surface normals (facial representations of the heads. Jing et al. [18] investigated gender across a range of PCA-compressed (dimensionality-reduced) accurate sex classification than the gray level image data showed that the three-dimensional head data supported more level image data from laser-scanned human heads. The results (PCA) separately to the three-dimensional structure and gray salient feature. They applied principal components analysis and chins of the laser-scanned heads were assessed and significhin/jaw. The effects of manipulating the shapes of the noses by having a more protuberant nose/brow and more prominent the average male face differs from the average female face taken with hair concealed and eyes closed. They proved that obtained by laser-scanning, compared photographs that were when asked to judge the sex of 3-D representations of faces authors found that subjects were considerably less accurate from hairstyle, makeup, and facial hair are minimized. The cludes the following steps: human faces, and use this data in performing face gender clas-2) A geometric shape analysis framework based on Rie- A facial surface representation by collection of curves of From the above discussion it is clear that a majority of current of a distance function level sets (circular curves) and streamlines (radial curves) mannian geometry to compare pairwise facial curves; Bruce et al. [1] performed an interesting experiment tions of circular and radial curves. The comparison of pairwise represent resulting facial surfaces by a finite indexed collecmetrical facial features. After preprocessing of 3-D scans, we from machine learning to select and highlight salient 3-D geotools from differential geometry and feature selection derived framework for 3-D face recognition and gender classification. best of our knowledge no previous work has proposed a unique gender classification problem using 3-D face images. To the ditional computational advantage of using a compact signature. highest performance for the face recognition task, with the ad-Furthermore, it is one of the first approaches to address the 4) A through experimental evaluation that compares the pro-3) A boosting method to highlight geometric features ac-In this work, we combine ideas from shape analysis using As

tion. Accordingly, it consists on the following steps: the target applications, face recognition and gender classificasification problem. Fig. 1 overviews the proposed approach with tion for face identification, which is basically a Multiclass clastrapersonal comparisons formulation to achieve feature selec-(Male/Female classes) and we propose to use the inter- and into the target application, the extracted features are trained as rameterized curves using differential geometry tools. According curves, extracted from faces, is based on shape analysis of parecognition, the classification is formulated as a binary problem lected optimally by adaptive boosting. For the case of gender weak classifiers and the most discriminative features are se-Let S be a facial surface denoting the output of a preprocomputed based on selected features which are fused using compared to the gallery faces using only individual scores testing step. this step, we keep the T-earliest selected features for the to each application in a supervised fashion. In face recog-The Offline training step, learns the most salient circular templates are computed, once for all, within the training test face is compared to computed templates of Male and the arithmetic mean. In the gender recognition problem, a face. In the identity recognition problem, a probe face is The **Online test step**, performs classification of a given test final strong classifier, with suitable weights. As a result of these examples, together with labels indicating if they are pairwise curves extracted from facial surfaces. Next, feed nition, for instance, construct feature vectors by comparing and radial curves from the sets of extracted ones, according Female classes using curves selected for that purpose. The learns iteratively the weak classifiers and adding them to a interclass or not. Thus, the adaptive boosting selects and IV. 3-D FACIAL CURVES EXTRACTION

prepares the mesh for curve extraction. We extract radial curves emanating from a reference anchor point (the tip of the nose) cessing step that crops the mesh, fills holes, removes noise, and

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and common experimental settings

demonstrated later, the proposed approach achieves

III. OVERVIEW OF THE PROPOSED APPROACH

posed solution with latest methods on a common data set

cording to the target application

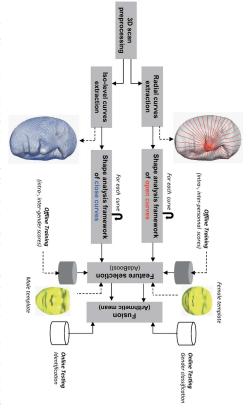


Fig. 1. Overview of the proposed approach, including both stages of training and testing and both target applications: identity recognition and gender classification

simple procedures detailed in the following paragraphs and circular curves having with the same point as the pole, using

A. Radial Curves

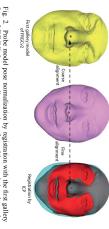
separation. Each curve is indexed by the angle α . extract radial curves from the facial surface at equal angular plane and having as origin the nose tip. We repeat this step to as shown in Fig. 3. That is, a curve β_{α}^{r} is obtained by slicing the makes an angle α with the plane containing the reference curve, surface by a plane P_{α} that has the nose tip as its origin and practice, each radial curve β_{α}^{r} is obtained by slicing the facial curve once the face has been rotated to the upright position. In a radial curve. The reference curve is chosen to be the vertical with a reference radial curve; the superscript r denotes that it is facial surface by P_{α} defined by the angle α with the vertical Let β_{α}^{r} denote the radial curve on S which makes an angle α

extraction then follows. with the first face model (generic model) of FRGCv2 database. the ICP algorithm, as illustrated in Fig. 2. The process of curve lating the probe face to a reference face, using their noses tips. This coarse alignment step is followed by a fine alignment using This step is achieved by performing a coarse alignment by trans-To avoid pose variations problem, all probe faces are aligned

shape of a facial surface and forms the first mathematical reprein Fig. 3. This indexed collection of radial curves captures the dial curves according to $S \approx \cup_{\alpha} \beta_{\alpha}^r = \cup_{\alpha} \{S \cap P_{\alpha}\}$ as illustrated sentation of that surface If needed, we can approximately reconstruct S from these ra-

B. Circular Curves

tance λ from the reference point (nose tip). A similar procedure Let β_{λ}^{c} denote the circular curve on S which makes a dis-



registration is then achieved by the ICP algorithm Fig. 2. Probe model pose normalization by registration with the first gallery face of *FRGCv2*, a coarse alignment is performed by translating the probe face according to the translation vector formed by the tips of the noses. A fine

(100 points per curve here). troduced to achieve the same number of points for all curves between points. However, a curve subsampling procedure is inextraction procedure. We note that any points ordering is needed reference point, in the surface. Fig. 4 illustrates results of such sphere and the facial surface defines equidistant points from the point as center and variable radius λ . The intersection of a given slicing function which is now a sphere M_{λ} having the reference is employed to extract these curves. The only difference is the for both kind of curves since the slicing procedure kept edges

3-D faces. Fig. 5 gives some results of facial curves extraction on several struct S from these circular curves according to $S \approx \bigcup_{\lambda} \beta_{\lambda}^c$ framework which allow matching and comparison of curves $\cup_{\lambda} \{S \cap M_{\lambda}\}\$ as illustrated in Fig. 4, we describe the geometric Similarly to radial curves, we can also approximately recon-П

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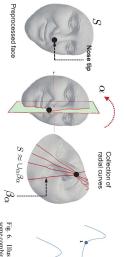


Fig. 3. Procedure for extraction of radial curves, a curve β_{α}^{-} is obtained by slicing the facial surface by P_{α} defined by the angle α with the vertical plane and having as origin the nose tip.

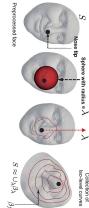


Fig. 4. Procedure for extraction of circular curves, a curve β_{χ}^{z} is obtained by slicing the factal surface by S_{χ} defined by the radius λ and having as center the

nose tip

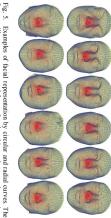


Fig. 5. Examples of facial representation by circular and radial curves. The first row illustrates preprocessed faces of male subjects, the second row gives preprocessed faces of females.

V. GEOMETRIC SHAPE ANALYSIS OF FACIAL CURVES

defined in \mathbb{R}^3 they can use the classic tools for statistical analysis. The recent cent works in this area consider a formal definition of shape on Fourier descriptors, moments or the median axis. More reto analyze shapes of 2-D curves. We can cite approaches based We will adopt this work to our problem since our 3-D curves are generalization of this work to the case of curves defined in \mathbb{R}^n for 2-D curves. Joshi et al. [23], [24] have recently proposed a results of Michor and Mumford [21], Klassen et al. [11], and spaces as a Riemannian manifold of infinite dimension on which Yezzi and Mennucci [22] show the efficiency of this approach We start by considering a curve β in \mathbb{R}^3 . While there are In the last few years, many approaches have been developed

Fig. 6. Illustration of statist metric. In order to compare the two curves in (a), some combination of stretching and bending are needed. The elastic metric mea-sures the amounts of these deformations. The optimal matching between the two curves is illustrated in (b).

shall represent it mathematically using a square-root representa-tion of β as follows; for an interval I = [0, 1], let $\beta : I \longrightarrow \mathbb{R}^3$ a square-root representation under which the elastic metric reduces to the standard L^2 metric and thus simplifies the analysis, of the parametrized curves is particularly appropriate in our function (SRVF), given by: (3) under this metric the Riemannian distance between curves is shapes in presence of elastic deformations, (2) this method uses be a curve and define $q: I \longrightarrow \mathbb{R}^3$ to be its square-root velocity invariant to the reparametrization. To analyze the shape of β , we function representation which allows us to compare local facial application—face analysis under facial expression variations This is because (1) such analysis uses the square-root velocity

$$q(t) \doteq \frac{\dot{\beta}(t)}{\sqrt{|\dot{\beta}(t)|}} \tag{1}$$

of β and is particularly convenient for shape analysis then translation and scaling variability have been removed by we set ||q|| = 1, implying all curves are rescaled to unit length, elastic metric to the well-known calculus of functional a [24]. This point is very important as it simplifies the calc of curves becomes the L2-metric under the SRVF represe describe next. The classical elastic metric for comparing We note that q(t) is a special function that captures the $\|q\|^2 = \int_I \langle q(t), q(t) \rangle dt = \int \|\beta(t)\| dt$, is the length of β . If under the L^2 -metric. Also, the squared L^2 -norm of q, given by Here t is a parameter $\in I$ and $|\cdot|$ is the Euclidean norm

point 2 matches the point 22 on the second curve. An elastic to point 11 on the bottom curve. The part between the point 1 as possible under some geometric criterion. In other words, that points reached at the same time on two curves are as close at what rate we are going to move along the bottom curve so better match that curve with the bottom one, one should know and 2 on the top curve shrinks on the curve 2. Therefore, the illustrates the matching where point 1 on the top curve matches peaks and valleys should be reached at the same time. Fig. 6(b) parametrization of the top curve to be arc-length, i.e., trathis mathematical representation of curves. verse that curve with a constant speed equal to one. In order to Consider the two curves in Fig. 6(a), let us fix the

metric is the measure of that shrinking

several ways to analyze shapes of curves, an elastic analysis

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Fig. 7. (a) Intraclass geodesics between facial surfaces and their associated radial curves. (b) Interclass geodesics between facial surfaces and their associated radial curves.

S. In Fig. 7 we show geodesic paths between radial curves and

A. Radial Open Curves

any two points $q_1, q_2 \in C$ is given by a hypersphere, the formulas for the geodesic and the geodesic of the minor arc connecting the two elements in C. Since C is under the chosen metric. This distance is found to be the length radial curves, we can compute the distance between them in $\ensuremath{\mathcal{C}}$ tangent spaces, C becomes a Riemannian manifold. Since the elements of C have a unit L^2 norm, C is a hypersphere in the The set of all unit-length curves in \mathbb{R}^3 is given by $\mathcal{C} = \{q : I \to \mathbb{R}^3 | \|q\| = 1\} \subset \mathbb{L}^2(I, \mathbb{R}^3)$. With the \mathbb{L}^2 -metric on its length are already well known. The geodesic length between Hilbert space $L^2(I, \mathbb{R}^3)$. In order to compare the shapes of two SRVF representation as earlier, we can define the set of closed curves in \mathbb{R}^3 by $\tilde{\mathcal{C}} = \{q: I \to \mathbb{R}^3 \mid \int_I q(t)|q(t)|dt = 0, \|q\| = 1\} \subset L^2(I, \mathbb{R}^3)\}$. The quantity $\int_I q(t)|q(t)|dt$ is the total dis-B. Circular Closed Curves we show the same for faces belonging to different persons. between two facial surfaces of the same person, while in 7(b) set of points of radial curves. In 7(a) we show a geodesic path the facial surfaces obtained by Delaunay triangulation of the placement in \mathbb{R}^3 while moving from the origin of the curve until We will use β_{λ}^{c} to denote the circular closed curves. Using

$$d_c(q_1, q_2) = cos^{-1}(\langle q_1, q_2 \rangle),$$

and the geodesic path α : $[0,1] \rightarrow C$, is given by

$$\alpha(\tau) = \frac{1}{(\sin((1-\tau)\theta)\alpha_1 + \sin(\theta\tau)\alpha_2)}$$

2

 $\gamma \in \Gamma$, the curve $\beta_{\alpha} \circ \gamma$ is a reparameterization of $\underline{\beta}_{\alpha}$. The corresponding SRVF changes according to $q(t) \mapsto \sqrt{\gamma}(t)q(\gamma(t))$. functions. For example, for a curve $\beta_{\alpha}: I \to \mathbb{R}^3$ and a function itself) and the elements of I' are viewed as reparameterization ents of C can re ing diffeomorphisms of I (to if we rotate a up SO(3) and the Ħ asses in C. Here, Γ to handle this variterization changes la

We define the equivalent class containing q as:

of elastic curves [23]. To obtain geodesics and geodesic dis-The set of such equivalence class is called the shape space S

 $[q] = \{ \sqrt{\dot{\gamma}}(t) Oq(\gamma(t)) | O \in SO(3), \gamma \in \Gamma \},\$

need a Riemannian metric. For this purpose we inherit the standard L²-metric of the large space L²(*I*, R³). For any $u, v \in L^2(I, R^3)$, the standard L² inner-product is given by:

$$\langle \langle u, v \rangle \rangle = \int \langle u(t), v(t) \rangle dt.$$
 (6)

$$\langle \langle u, v \rangle \rangle = \int_{I} \langle u(t), v(t) \rangle dt.$$
 (6)

$$\langle\langle u, v \rangle\rangle = \int_{I} \langle u(t), v(t) \rangle dt.$$
 (6)

$$J_I$$

putation of geodesics and geodesic distances utilize the

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given by:

intrinsic geometries of these spaces. While the detailed description of the geometries of C and S are given in [23], [24], we briefly mention the tangent and normal spaces of C. It can be shown that the set of all functions normal to \hat{C} at a point q are

corresponding equivalence classes $[q_1]$ and $[q_2]$ in shape space

 $T_q(\tilde{\mathcal{C}}) = \left\{ v: I \to \mathbb{R}^3 | v \perp N_q(\tilde{\mathcal{C}}) \right\}$

8

 $S \doteq C/(SO(3) \times \Gamma)$

4

alence classes

tion problem. The resulting shape space is the set of such equiv-

tances between elements of S, one needs to solve the optimiza-

where $\{e^1, e^2, e^3\}$ form an orthonormal basis of \mathbb{R}^3 . Thus, the

 $N_{q}(\tilde{\mathcal{C}}) = \text{span} \left\{ q(t), \frac{q^{i}(t)}{|q(t)|}q(t) + |q(t)|\mathbf{e}^{i}|_{i} = 1, 2, 3 \right\}$

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To defi

represent curves [23], [24], we define the orbits of the rotation group
$$SO(3)$$
 and
there in \mathbb{R}^3 , and the reparameterization group Γ as equivalence classes in \tilde{C} . The
 γ the curves but resulting shape space is:
 $\tilde{c} = \tilde{C} + \tilde{C} + CO(2\pi) + \Gamma \Lambda$

and the reparameterization group Γ from C. As described in

$$\tilde{S} \doteq \tilde{C}/(SO(3) \times \Gamma)$$

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$$\tilde{\mathcal{S}} \doteq \tilde{\mathcal{C}} / (SO(3) imes \Gamma)$$

orientations and reparameterizations can be represented by dif-
ferent elements of
$$C$$
. To define a shape, its representation should

2

the set C represents the set of all closed curves in \mathbb{R}^3 . It is called

the end. If it is zero, the corresponding curve is closed. Thus,

$$g(q_1 + \sin(\theta \tau)q_2)$$
, (3) be independent of its contained and exparameterization. This is obtained mathematically by a removing the rotation group $SO(3)$

$$=\frac{1}{\sin(\theta)}(\sin((1-\tau)\theta)q_1+\sin(\theta\tau)q_2)$$

that its facial curves, we get different SRVFs
their shapes remain unchanged. Another simil
when a curve is reparametrized; a reparamet
the SRVF of curve but not its shape. In order to
ability, we define orbits of the rotation grou
reparameterization group
$$\Gamma$$
 as equivalence cla

The same shape. For example,
this casy to see that several elements
thus its facial curves, we get differ
thus its facial curves, we get differ
thus its facial curves, we get differ
their shapes remain unchanged. An
shapes
the SRVF of curve but not its shape
mation
ability, we define orbits of the roi
unlus of
reparameterization group
$$\Gamma$$
 as equi-
nalysis
is the set of all orientation-preservi-
ven by:

runs into trouble. In fact, their shapes are affected by changes $d(S^1,S^2) = \frac{1}{N_\alpha}\sum_{\alpha=1}^{N_\alpha} d_s \left(\beta_\alpha^{r,1},\beta_\alpha^{r,2}\right) + \frac{1}{N_\lambda}\sum_{\lambda=1}^{n_\lambda} d_{\tilde{s}}\left(\beta_\lambda^{c,1},\beta_\lambda^{c,2}\right)$ $S^2 \ {\rm could} \ {\rm be} \ {\rm defined} \ {\rm by}:$ facial surfaces are compared by comparing their corresponding facial curves. The distance between two facial surfaces S^1 and of the set of circular curves, β_{α}^{r} represents the radial curve and C. Extension to Facial Surfaces Shape Analysis tween circular curves and the facial surfaces obtained by Deand $[q_2]$ an arbitrary path α and then updates this path repeatstraightening method [25] which connects the two points $[q_1]$ S. We use in this context, a numerical method called the pathof a geodesic path between two elements of \tilde{S} , under the Riemannian metric given by (6). Given two curves $\beta_{\lambda_1}^c$ and $\beta_{\lambda_2}^c$, Fig. 8. (a) Intraclass geodesics between facial surfaces and their associated circular curves. (b) Interclass geodesics between facial surfaces and their associated circular curves. 1772 faces. However, their comparison under different expressions N_{α} is the cardinality of the set of radial curves. Two shapes of where β_{λ}^{c} represents the circular curves, N_{λ} is the cardinality surface S by a collection of 3-D circular and radial curves, shapes of facial surfaces. We represent the surface of the facial longing to different persons. the same person, while in 8(b) we show the same for faces be-8(a) we show a geodesic path between two facial surfaces of launay triangulation of the set of points of circular curves. In classes $[q_1]$ and $[q_2]$ in \tilde{S} . In Fig. 8 we show geodesic paths bethe geodesic distance between the corresponding equivalence fined by (9) are geodesic paths in S. We denote by $d_{\bar{s}}(\beta_{\lambda_1}, \beta_{\lambda_2})$ edly in the negative direction of the gradient of energy given by: find a geodesic path between the orbits $[q_1]$ and $[q_2]$ in the space represented by their SRVF respectively q_1 and q_2 , we need to Now, an important tool in our framework is the construction It has been proven in [25] that the critical points of E de-Radial and circular curves capture locally the shape of the In this section we extend our study from shapes of curves to VI. BOOSTING FOR GEOMETRIC FEATURE SELECTION $S \approx \left\{ \bigcup_{\lambda=1}^{N_{\lambda}} \beta_{\lambda}^{c} \right\} \cup \left\{ \bigcup_{\alpha=1}^{N_{\alpha}} \beta_{\alpha}^{r} \right\},$ $E[\alpha] = \frac{1}{2} \int_{s} \langle \dot{\alpha}(s), \dot{\alpha}(s) \rangle ds$ IEEE TRANSACTIONS ON INFORMATION FORENSICS AND SECURITY, VOL. 7, NO. 6, DECEMBER 2012 (II) (10) ૭ being under or over the threshold θ . scores (i) the match scores (intrapersonal comparisons) and (ii) A. Face Recognition rithm 1. {0, 1}. The final strong classifier is defined by a set of a weak classifiers weighted by a set of weights $W = \{w_{t,n}\}_{1 \le n \le N}$. aclass) or negative (interclass), depending on the distance value take a value of distance computed based on a radial or circular of samples are misclassified. Each weak classifier $h_j(x_n^k)$ will threshold classification function such that the minimum number cular or radial curve, the weak classifier determines the optimal non-match score and 1 in the case of match score. For each ciras illustrated in Fig. 9. the remaining Probe versus Probe submatrices, of the size of similarity matrix. We then split the matrices as we keep the and circular curve, we compute the All versus All (4007 \times 4007) use the 3-D face models of FRGCv2 dataset. For each radial facial curves are returned by the algorithm. individual circular curves and radial curves are used as weak and weighted by the quality of its classification. In practice, the samples. At each iteration, the best weak classifier is provided Schapire in [26]. Recall that, boosting is based on iterative seselection step to identify (or localize) the most stable and most in facial expressions. For that purposes, we introduce a feature curve, threshold it, and classify the comparison as positive (intrwith k = r or k = c. y_n can take two values: 0 in the case of ilarity scores between radial or circular curves at the same level. we consider a set of pairs $(x_n^n, y_n)_{1 \le n \le N}$ corresponding to simscores form an input to the boosting algorithm. More formally, the nonmatch scores (interpersonal comparison). Together these cial curves) and these disjoint sets serve as inputs to Adaboost the testing samples (the set of individual distances related to fa- 3541×3541 , for the training. Thus, we separate the training and Gallery versus Probe of size 466×3541 for the testing and uses classifiers. After M iterations, the most relevant T(T < M)lection of weak classifiers by using a distribution of training chine learning algorithm AdaBoost introduced by Freund and discriminative curves. We propose to use the well known ma-The pseudocode of AdaBoost algorithm is summarized in algo-From these areas of the matrices, we extract two kinds of To train and test Adaboost classifier for this application, we where, h_t denotes for the weak hypothesis given by $h_t : \mathcal{X} \rightarrow$ $h_j\left(x_n^k\right) = \begin{cases} 1 & \text{if } x_n^k < \theta \text{ (intra-personal)} \\ 0 & \text{otherwise. (inter-personal)} \end{cases}$ (12) Algorithm 1 AdaBoost Algorithm H(x)Match score
Non-match score Gallery cans (466) is given by: For t = 1, ..., M: $\lambda_0 = N_\lambda + N_c$ Probe (5) ₹ $w_{t,1},\ldots,w_{t,N}$: 1 €; =

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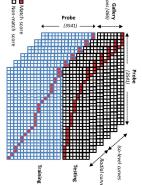


Fig. 9. All versus Probe distance matrices splitting; the Gallery versus Probe distance matrix is kept for testing, as suggested in the FRGC evaluation protocol and the remaining submatrices Probe versus Probe are used for training.

regions.

- Input: A set of samples $(x_1^k, y_1), \ldots, (x_N^k, y_N)$ where curves $k \ (1 \le k \le \lambda_0)$ and $y_n = \{0, 1\}$. x_i^{κ} is the score of similarity of the circular or radial
- Let m be the number of nonmatch score and l be the depends on the value of y_n where $n \in 1 \dots N$ Initialization of weights $w_{1,n} = (1)/(2m), (1)/(2l)$ it number of match score.
- 1- Normalize the weights $w_{t,n}$ such that
- $\sum_{n=1}^{\infty} w_{t,n} = 1.$ 2- For each curve β_j (feature), train a weak classifier h_j is determined with the corresponding weight h_j that uses a single curve. The error ϵ_j of classifier

$$=\sum_{n}^{N} w_{t,n} |h_j\left(x_n^j\right) - y_n|$$

- 3- Choose the classifier h_j with the lowest error. 4- Undate the weights $w_{t+1,n} = w_{t,n} \gamma_t^{1-e_n}$, where
- The final hypothesis is a weighted linear combinations correctly classified by h_t and 1 else. $\gamma_t = (\epsilon_t)/(1-\epsilon_t)$ and $e_n = 0$, if the sample x_n is
- proportional to the training errors. The strong classifier of the T hypotheses where the weights are inversely

$$= \begin{cases} 1 & \text{if } \sum_{t=1}^{T} \log \frac{1}{\gamma_t} h_t(x) \ge \frac{1}{2} \sum_{t=1}^{T} \log \left(\frac{1}{\gamma_t}\right);\\ 0 & \text{else.} \end{cases}$$

different subjects. We note that the boosting algorithm selects expressions, whereas, the second row gives curves location on curves on different sessions of the same person with different in Fig. 10. The first row shows the locations of the selected The set of selected curves returned by Adaboost is shown

Fig. 10. The most discriminative radial and circular curves selected by Boosting for face recognition, given on different faces.

the lower part of the face since its shape is affected by exprespressions and radial curves avoiding two parts. The first one is sions. In contrast, the most stable area cover the nasal/forehead passing throw these regions change when conveying expresresponds to the eye/eyebrow regions. Shapes of radial curves sions, particularly when the mouth is open. The second area coriso-curves located on the nasal region, which is stable under ex-

compared to the use of all radial curves or circular curves, recircular curves. We note also that the selection performed on using the training set). As shown in Fig. 11(b), minimum ercurves are produced from the Probe versus Probe matrices (i.e., the rate of False Rejection for different configurations. These ferent graphs in Fig. 11 plot the rate of False Acceptance versus spectively. radial curves only or circular curves only minimizes the errors rors are given by fusing scores of selected radial and selected To demonstrate the usefulness of the curve selection step, dif-

by the fusion of scores related to selected curves as following: The online testing step consists on comparing faces S^1 and S^2

$$d(S^1,S^2) = \frac{1}{N_{\alpha_s}} \sum_{\alpha=1}^{N_{\alpha_s}} d_s \left(\beta_{\alpha}^{r,1},\beta_{\alpha}^{r,2}\right)$$

$$+\frac{1}{N_{\lambda_s}}\sum_{\lambda=1}^{N_{\lambda_s}} d_{\hat{s}} \left(\beta_{\lambda}^{c,1},\beta_{\lambda}^{c,2}\right) \quad (13)$$

and N_{α_s} the cardinality of the set of selected radial curves. where M_{λ_s} is the cardinality of the set of selected circular curves

B. Gender Classification

ship. Different steps are detailed in the following neighbor algorithm denotes the class (Male/Female) member are computed (based only on selected features), and the nearest For the testing step, distances to male and female templates optimally by boosting as done in face recognition application nally, the most discriminative geometric features are selected each curve index) between sample faces and the templates. Figender) and interclass (different gender) pairwise distances (for In fact, this framework allows us to compute intrinsic means metric shape analysis framework for open and closed curves pute Male and Female representative templates using the geo-Then, within the training step, we compute intraclass (same (Karcher mean) of curves that we extend to facial surfaces. For 3-D face-based gender classification task, we first com-



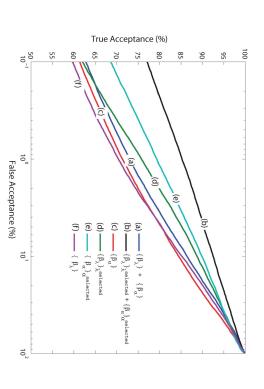


Fig. 11. ROC curves produced from the training set (a) all radial and circular curves, (b) selected radial and selected level curves, (c) all radial curves, (d) selected circular curves, (e) selected radial curves, (a) all circular curves.

tio of facial curves $\{\beta_1^{\alpha}, \ldots, \beta_n^{\alpha}\}$ in C, we define the variance funcdefined as follows: Let $d_{\mathcal{C}}(\beta_i^o,\beta_j^o)$ denotes the length of the geodesic path from curves in \mathcal{C} . To calculate the Karcher mean involves embedding the manifold in a larger vector space, coma nonlinear manifold. The first definition, called extrinsic mean, vantage of the proposed geometrical framework for shape anal-ysis of curves is to calculate some statistics as the "mean" of manifold to define and compute a mean on that manifold. It is mean or the Karcher mean utilizes the intrinsic geometry of the down to the manifold. The other definition, called the intrinsic defining a mean value for a random variable that takes values on manifold enables us to perform such statistical analysis for commean [24]. The Riemannian structure defined on a Riemannian puting the Euclidean mean in that space, and then projecting it puting faces mean and variance. There are at least two ways of facial curves and to extend it to facial surfaces, called Karcher Male/Female Geometric Templates Computation: One ad-

n:
$$\mathcal{V}: \mathcal{C} \to \mathbb{R}, \mathcal{V}(\mu) = \sum_{i=1}^{n} d_{\mathcal{C}} \left(\beta_{i}^{o}, \beta_{j}^{o}\right)^{2}$$
(14)

The K $\overline{\beta^{\alpha}} = \arg\min_{\mu\in\mathcal{C}}\mathcal{V}(\mu)$

$$\nu: \cdots \to n, \nu(\mu) = \sum_{i=1}^{2} uc(v_i:v_j)$$

archer mean is then defined by:

an element of C that can be seen as the smallest geodesic path of points in $\mathcal C$ for which the minimizer of $\mathcal V$ is obtained. $\overline{\beta^{\alpha}}$ is The intrinsic mean may not be unique, i.e., there may be a set

length from all given facial surfaces. We present a commonly

women (ten from each class) from FRGCv1, to calculate

used algorithm for finding Karcher mean for a given set of fa-cial surfaces (by using their curves). This approach, presented atively update the current mean μ . The same pseudo-algorithm in algorithm 2 uses the gradient of \mathcal{V} , in the space $T_{\mu}(\mathcal{C})$, to iterwill be obtained for radial curves defined in the shape space C

Algorithm 2 Karcher Mean Algorithm

Choose a point $\mu_0 \in C$ as an initial guess of the mean. (For Set k = 0. Choose some time increment $\epsilon \leq (1)/(n)$

- example, one could just take $\mu_0 = S_1$.) 1- For each i = 1, ..., n choose the tangent vector
- $f_i \in D$ to S^i . The vector g = $T_{\mu_k}(\mathcal{C})$ which is tangent to the geodesic from μ_k . The vector $g = \sum_{i=1}^{i=n} f_i$ is proportional to the
- gradient at μ_k of the function \mathcal{V} .
- Flow for time ϵ along the geodesic which starts at μ_h

2-

- μ and has velocity vector g. Call the point where you end up μ_{k+1} . Set k = k + 1 and go to step 1.

Geometric Feature Selection: To train and test the boosting algorithm for this application, we use 20 previous 3-D faces of for testing. Firstly, we selected a subset of faces of men and the FRGCv1 dataset for training and 466 subjects of FRGCv2 Female template facial surface is computed by averaging ten females facial surfaces of different person as shown in Fig. 13. Male template facial surface is computed by averaging ten males facial surfaces of different person as shown in Fig. 12.

(15)

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Fig. 12. Different facial surfaces of different male persons taken from FRGCv1 and their Karcher mean. (a) Sample faces (from FRGCv1) used to compute the template face. (b) Female template face (Karcher mean).

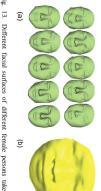


Fig. 13. Different facial surfaces of different female persons taken from FRGCv1 and their Karcher mean. (a) Sample faces (from FRGCv1) used to compute the template face. (b) Female template face (Karcher mean).

TABLE I INPUT FEATURE VECTORS OF BOOSTING ALGORITHM FOR GENDER CLASSIFICATION



parison). the templates for both male and female classes denoted respectively $T^{\rm male}$ and $T^{\rm female}.$ Then, we computed pairwise comparisons) and (ii) the nonmatch scores (intergender comwe extract two kinds of scores (i) the match scores (intragender of templates. Thus, we obtained a matrix containing feature distances (based on curves) between test images and both Ababoost algorithm, as illustrated in Table I. From this matrix, vectors (distance based on curves) which will be used to train

of a geometric feature β_j and a threshold θ , such that: ples are misclassified. A weak classifier $h_j(x_n^k)$ thus consists classification function, such that the minimum number of samcurve β_j , the weak learner determines the optimal threshold same level α, λ and y_n can take two values: 0 in the case of Both score lists represent the input of the boosting algorithm. More formally, we consider a set of pairs $(x_n^{\alpha,\lambda}, y_n)_{1 \le n \le N}$ non-match score and 1 in the case of match score. For each where $x_n^{\alpha,\lambda}$ is a similarity score between two curves at the

$$i(x_n^k) = \begin{cases} 1 & \text{if } x_n^k < \theta \text{ (intra - gender)} \\ 0 & \text{otherwise. (inter - gender)} \end{cases}$$
(16)

 $D(F_k$

•

The final decision $D(F_k)$ for classification is given by:

h

selected curves on different sessions of some female faces. sions of some male faces whereas, Fig. 14 shows the location of Fig. 15 shows the location of selected curves on different ses-

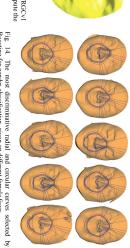


Fig. 14. The most discriminative radial and circular curves selected Boosting for gender classification, given on different female faces.

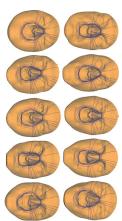


Fig. 15. The most discriminative radial and circular curves selected by Boosting for gender classification, given on different male faces.

sellion regions. for gender classification and radial curves avoiding two parts. on the cheeks region, which is discriminative shape of 3-D face The most stable areas for gender classification cover the cheeks/ We note that the boosting algorithm selects circular curves

tion algorithm is given in algorithm 3. of FRGCv2. The pseudocode of the proposed gender classificaand radial curves between template faces and the 466 test faces calculated different matrices of distances of all selected circular Classification: As described in Table I, this time round, we

Algorithm 3 Gender Classification Algorithm selected circular and Radial curves. For each face request S_k k = 1, ..., 466: curves or radial curves. N^s is the total number of Input: A set of curves c_i where c_i is either circular $\sum_{i=0}^{N^s} d_k \left(T^{\text{male}}, F_k \right) \text{ and } \sum_{i=0}^{N^s} d_k \left(T^{\text{female}}, F_k \right)$ 1- Calculate the geodesic distances:

)
=
$$\begin{cases} 1 & \sum_{i=0}^{N^s} d_k \left(T^{male}, F_k \right) < \sum_{i=0}^{N^s} d_k \left(T^{\text{female}}, F_k \right) \\ 0 & \text{else.} \end{cases}$$

| same sample models same sample models face scans has feature vectors, test face from test face from the pairwing this set ace from selected solutions exist in the larges and the form selected or the 466 sub- | B. Gender Classification B. Gender Classification of 3-D face scans has been experimented using the FRGCv2 database. This was motivated by the fact that this dataset contains the largest number of subjects compared to existing 3-D face datasets as Bosphorus, BU-3DFE, etc. To evaluate the proposed approach, we have considered 466 3-D images related to the 466 sub- jects of FRGCv2 data set. Thus, if several sessions exist in the dataset, we select the earliest (neutral or nonneutral) one for our experiment. We use also few 3-D images taken from FRGCv1 to compute male and female templates, as described in Section VI. The difficulty encountered to compare our approach to related work, is there is no standard protocol to compare gender classification results, unlike FRGC standard protocol for 3-D face recognition. Most of previous approaches [34], [18], [20] reported classification results on a subset taken from FRGCv1 dataset. <i>J) Classification Results</i>: We conducted experiments by first computing Male {T^{remake}} and Female {T^{remake}} using sample 3-D scans taken from FRGCv1. Then, compar- using sample 3-D scans taken from FRGCv1. Then, compare using sample 3-D scans taken from FRGCv1. Then, compare using sample 3-D scans taken from FRGCv1. Then, compare using sample 3-D face reconstruct to build the feature vectors. Finally, two experiments, detailed below, were carried out: Experiment 1. <i>Curve selection-based</i>. To select the most relevant combination of curves using Adaboost algorithm, we first use 10 male 3-D face models and 10 formale models. | and verification verification biometric scenarios supports this data set. Furthermore, we give gender classification performances achieved by our approach, using the same dataset. We note that the subjects in FRGCv2 dataset are 57% male and 43% female. <i>A</i>. 3-D Face Recognition Results <i>I</i>) Identification: For testing on FRGCv2 dataset, only the identification evaluation was carried out. In fact, as mentioned in Section VI since our approach requires a training stage, it was tested on a subset of this dataset following the FRGC evaluation protocol for the identification scenario, as following. We kept, for the test, the <i>Gallery versus Probe</i> (of size 466 × 3541) similarity matrices. The remaining submatrices (i.e., <i>Probe versus Probe</i> similarity scores) were used to train the feature selection as they by boosting algorithm. This means that disjointly similarity vectors are used for the training and the test. Following these settings, our approach achieved 98.02% as rank-1 recognition rate and reached 99% in rank-5 as illustrated in the CMC plot (Cumulative Match Characteristic) given is Fig. 16. We recall that the approach used here is based on both radial and circular facial curves selection. As shown in Table II, the selected curves are located on the nasal region, which means that the masal shape significantly contribute to face recognition. This is due to the fact that its shape is stable to facial expressions. We note also that the use the use of the stable to facial expressions. |
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| | | and verification and verification biometric scenarios supports this data set. Furthermore, we give gender classification performances achieved by our approach, using the same dataset. We note that the subjects in FRGCv2 dataset are 57% male and 43% female. <i>A. 3-D Face Recognition Results</i> <i>I) Identification:</i> For testing on <i>FRGCv2</i> dataset, only the identification evaluation was carried out. In fact, as mentioned in Section VI since our approach requires a training stage, it was tested on a subset of this dataset following the <i>FRGC</i> veraluation protocol for the identification scenario, as following. We kept for the test, the <i>Gallery versus Probe</i> (or size 466 × 3541) similarity matrices. The remaining submatrices (i.e., <i>Probe versus Probe</i> similarity scores) were used to train the feature selection rate and reached 99% in rank-6 as illustrated in the CMC ploi (Cumulative Match Characteristic) given is Fig. 16. We recall the approach used here is based on both radial and circulatification via that the most relevant circular undvidually. We point out that the most relevant circular individually. We point out that the most relevant the approach that the fact that its is due to the fact that its ones) here is and the fact that the approach step is the selection. |
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| | The state-of-the-art except the Work of [6]. | HIGH TO /O OF HIS HIGHER HIS HOLLERN AN A COMMANY |
| ch outperforms | As shown in Table III, the proposed approach outperforms | than 40% of the models are nonneutral. A standard evaluation |
| (*) Results for 10-fc | approach. | dataset contains 4 007 3-D scans of 466 neonle in which more |
| | 98.3% which means that ten more faces are recognized by this | report 5- U face recognition performances on FRUCV2 [27] and |
| 1 | Shape Difference Map between faces, achieved a better result | obtained results with the proposed methods. In particular, we |
| tors (Haar-like, Methods | by Wang et al. [6], based on boosting of descriptors (Haar-like, Color and Local Biner, Bottom (LDD)) commuted on the | In the following, we present conducted experiments and the |
| | state-of-the-art methods. Only the approach proposed recently | VII. EXPERIMENTAL RESULTS |
| the majority of DIFFEREN | is clear that the proposed method outperforms the majority of | IIII Frances marks Decama |
| | neutral scan in the gallery and the remaining as test images. It | |
| | remaining for testing, we note that experiments reported in [28] and [16] follow a modified protocol by keeping the earliest | rig, ro, cumulative materi chalacteristic curve tot selected rautat and rever curves. |
| gallery and the Gender Classificati | the earliest scan of the 466 subjects in the gallery and the | E's 16 Completion Marth Champtoniais areas for selected and it and face |
| | (curve-based, feature selection-based, and others) by keeping | 2 4 6 8 10 12 14 16 18 20 22 24 26 28 30 RANK |
| ous approaches Methods | Table III shows identification results of previous approaches | |
| 1 scenario, the | FRGC standard protocol for the identification scenario, the | 98.2 |
| EXPERIMENTAL (| 2) Comparative Study With State-of-the-Art: Following the | 98.4 - |
| | time-processing of one-to-one face matching | |
| | In addition to performance improvement, the curve selection | scogr |
| * | | nitio |
| 80.0 | | n Rat |
| ++ | 66.51% 1.04 | te (% |
| <u>mk-1 Time(s)</u> Methods 0.4% | Rank-1 1 88.65% | |
| lect | | 994 |
| r Configur ations | RANK-I/COMPUTATION COST (IN SECONDS) FOR DIFFERENT CONFIGURATIONS | 906 |
| | TABLE II | 8,66 |

NG 3-D-GEOMETRIC FEATURES FOR EFFICIENT FACE RECOGNITION

COMPARISON WITH STATE-OF-THE-ART APPROACHES ON FRGCv2 (RANK-1 RECOGNITION RATE) TABLE III

| | % | 98.02% | | | | | Our |
|-------------|-----------------------------------|-----------|-------|--------------|-------------------------------|----------|---------|
| 98.3% 97.2% | 97% | 97.2% | 97.2% | 1 | 94.1% | 97% | Rank-1 |
| [5] | [31] | [4] | [30] | [12] | [15] | [29] | |
| Wang | Ka | Faltemier | Drira | Mpiperis | Berretti(*) | ter Haar | Methods |
| tion-bas | B. Feature selection-basea | B. 1 | on | representati | A. Curve-based representation | A. C | |

N-S" means the earliest neutral scan in the gallery and the remaining as probes.

TABLE IV ARISON OF GENDER CLASSIFICATION METHODS USING

FERENT TYPES OF SELECTED CURVES

| Gender Classification Rate 79.40% 80.69% | | | Methods |
|--|----------------------|-----------------|-------------------------|
| 79.40% | curves | circular | Cur |
| 80.69% | curves | circular Radial | e selectio |
| 84.12% | curves radial curves | circular and | Curve selection-based 3 |

TABLE V

ARISON OF GENDER CLASSIFICATIONS METHODS USING RENT MACHINE LEARNING TECHNIQUES

| - J (7] : C t : D t [| - Montoore | Methode | |
|-----------------------|--|---------------------------|--|
| 0/ 02/1 | AdaBoost ^(*) SVM ^(*) | Classifien | |
| 010100 0100 | SVM ^(*) | Classifier decision-based | |
| 00 0577 | Neural ^(*) Network | based | |

fold cross-validation. ion Kate 86.05% 83.91% 83.05%

dial curves, taken individually. nances compared to selected circular curves r curves and selected radial curves achieved note also that using the combination of selearest neighbor classification. As reported in eature selection step, accumulated distances classification rate. We note that, in this expertting, our approach achieved 84.12% as avsult of the nearest neighbor algorithm. Folvise distances to the templates then make the s, used for the training step. Now, given new models and the templates, in order to build curves only are used and classification is the 466 3-D models of FRGCv2, we com-FRGCv2 subjects are scanned with arbitrary facial expression. guarantee that all subjects will have a neutral expression, some sion of each subject. Note that this ad-hoc division does not and 80 male subjects. However they used more than one ses-[19] a subset of FRGCv1 is used with only 28 female subjects FRGCv1, six female subjects and four male subjects, while in tested on different subsets. In [35] the authors used a subset of gender classification results compared to previous approaches 2) Comparative Study With State-of-the-Art: Table VI shows

st data. Finally, the results from the ten steps ld cross-validation experiment. According to are used for both training and test, and each classifier for the experiment. In this way, all to produce a single estimation of the performes, with each of the 10 subsets used exactly est. Using 10-fold cross validation, training is subjects are split into disjoint subsets for Its. Training and testing steps are carried out ssifier of Adaboost. Table V summarizes the xample, we consider the binary decision of ion step, we consider the final classifier deods, SVM and Neural Network. Instead of me setting, experiments using two machine ing classifier results, we have conducted, fol-Classifier decision-based. In order to evalused for test exactly once. classifications. while the black curves are the common selected curves for both sification, the red curves are selected for 3-D face recognition fication, the blue curves are selected for 3-D face gender clascurves for both applications face recognition and gender classi-Fig. 19 shows some faces with selected iso-level and radial

the classifier decision. complementary (as hair density, etc.) in order to consolidate approach is to introduce the texture information, which contains One solution of this problem and for improving the proposed for a person), to recognize correctly the gender of the person based on the shape information, there is some confusion (even shape of curves. The second reason lies in the fact that only such as some occlusions in relevant regions which affected the misclassification. The first one is the bad quality of 3-D scans, Figs. 17 and 18 shows that there are two major reasons of this The analysis of some misclassified examples given by Fig. 18. Different i row shows 3-D data data . 18. Different female 3-D faces misclassified by our approach. The first shows 3-D data; the second row shows the corresponding texture of 3-D



Fig. 17. Different female 3-D faces misclassified by our approach. The first row gives 3-D data, the second gives the corresponding texture of 3-D data.

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| Image: Provide the second for recognition rate of the proposed approach achieved analysis of the second for recognition rate of the second for the second f | 1778 IEEE TRANSACTIONS ON |
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| 1 To Style of FHE-ART RESULTS 1 Style of FHE-ART RESULTS 2 Style of the style of t | IEEE TRANS ACTIONS ON INFORMATION FORENSICS AND SECURITY, VOL. 7, NO. 6, DECEMBER 2012 |
| [25] E. Klassen and A. Srivastva, "Godelsis between DJ closed carry seine pathetraghtering," in <i>Proc. EECCV Lecture Notes in Computational Learning, Theory, 25(1), Computational Learning, Theory, 25(1), Computational Learning, Theory, 25(1), Computational Learning, Theory, 25(1), Computational Learning, Theory, 25(1), Computational Learning, Theory, 25(1), Computational Learning, Theory, 25(1), Computational Learning, Theory, 25(1), Computational Learning, Theory, 25(1), Computational Learning, Theory, 25(1), Computational Learning, New York, 20(2), pp. 99(2),</i> | BALLIHI et al.: BOOSTING 3-D-GEOMETRIC FEATURES FOR EFFICIENT FACE RECOGNITION |
| Kurat David (M.96-SM/08) reserved the first of detecting degree in computer engineering from the linearity of Linka Li (USLI). France in 2000 rule in a clinic computer Science Dapament for the linearity of Linka Li (USLI). Computer Science Dapament is an international conference and the Bearrah Computer Science Dapament of the mean distribution of the Computer Science Dapament and the hybrid over 100 papes in some of the mean distribution of Mille 1 (USLI). Computer Science Dapament and the Harmon of the mean distribution of Mille 1 (USLI). Computer Science Dapament and the hybrid over 100 papes in some of the mean distribution of Mille 2 partern recognition, mage processing. Compression. Indexing and Ritermarking (Wile), 20(8). He was the bunden access to 2 human object Retrieval (2010) and Multimedia access to 2 human object Retrieval (2010) and Multimedia access to 2 human object Retrieval (2010) and Multimedia access to 2 human object Retrieval (2010) and Multimedia access to 2 human object Retrieval (2010) and Multimedia access to 2 human object Retrieval (2010) and Multimedia access to 2 human object Retrieval (2010) and Multimedia access to 2 human object Retrieval (2010) and Multimedia access to 2 human object Retrieval (2010) and Multimedia access to 2 human object Retrieval (2010) and Multimedia access to 2 human object Retrieval (2010) and Multimedia access to 2 human object Retrieval (2010) and Multimedia access to 2 human object Retrieval (2010) and Multimedia access to 2 human object Retrieval (2010) and Multimedia access to 2 human object Retrieval (2010) and Multimedia access to 2 human object Retrieval (2010) and Multimedia access to 2 human object Retrieval (2010) and Multimedia access to 2 human object Retrieval (2010) and Multimedia access to 2 human object Retrieval (2010) and Multimedia access to 2 human object Retrieval (2010) and Retrieval (2010) and Multimedia access to 2 human object Retrieval (2010) and Sine Copie and the Decretrieval and the Decretrieva of Sine (18 human hum | DOGNITION 1779 |

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| Ahmed Maalej ^{a,b} , Boulbaba | ı Ben Amor ^{a,b,*} , Mohamed Daoudi France | Ahmed Maalej ^{a.b} , Boulbaba Ben Amor ^{a.b.*} , Mohamed Daoudi ^{a.b} , Anuj Srivastava ^c , Stefano Berretti ^d "III (INNC CNES 502) Inhuesty of Ully 1 Forme |
| ⁶ LIP. (UNK CNRS 802.2), University of Lille 1. Fornee ⁶ Institut TELECOM Lille 1. Fornee ⁶ Department of Statistics, Florida State University, USA ⁴ Department of Statistics, Florida State University of Finenze, Italy | France rity, USA sity of Firenze, Italy | |
| ARTICLEINFO | A B S T R A C T | |
| Article history: Received 6 July 2010 | In this paper we address the problem of 3D shape analysis of facial surfaces coupled wi | In this paper we address the problem of 3D facial expression recognition. We propose a local geometric shape analysis of facial surfaces coupled with machine learning techniques for expression classification. |
| 10 February 2011 Accepted 14 February 2011 Available online 19 February 2011 | framework, in a shape space provides a qua are then used as inputs to several classifi | rounputation of the engine of other sectors and the other content of the potential production and a contraminant framework, in a share space provides a quantitative information about their similarities. These measures are then used as inputs to several classification methods. The experimental results demonstrate the |
| Keywords: 3D facial expression classification | errectiveness of the proposed approach. Using we achieved 98.81% and 97.75% recognit prototypical facial expressions on BU-3DFE | enercuveness or me proposed approach. Using multitoosting and support vector matimus (SVV) classifiers, we achieved 98.81% and 97.75% recognition average rates, respectively, for recognition of the six protovorial facial expressions on BU-30FE database. A comparative study using the same experimental |
| SVM | | |
| 1. Introduction | a given 3D namelv Ha | a given 3D model, into one of the six prototypical expressions, namely Happiness Anger Fear. Dispust Sadness and Surprise. It is |
| In recent years, 3D facial expression recognition has received growing attention. It has become an active research topic in | | stated that these expressions are universal among human ethni- city as described in [1,2]. |
| computer vision and pattern recognition community, impacting important applications in fields related to human-machine inter- | Þ. | The remainder of this paper is organized as follows. First, a brief overview of related work is presented in Section 2. In Section |
| action (e.g., interactive computer games) and psychological research. Increasing attention has been given to 3D acquisition systems due to the natural fascination induced by 3D objects | | we describe the BU-3DFE database designed to explore 3D information and improve facial expression recognition. In Section 4. we summarize the shape analysis framework applied earlier |
| visualization and rendering. In addition 3D data have advantages over the 2D data, in that 3D facial data have high resolution and | | for 3D curves matching by Joshi et al. [3], and discuss its use to perform 3D patches analysis. This framework is further |
| convey valuable information that overcomes the problem of pose/ lighting variations and the detail concealment of low resolution acquisition. | | expounded in Section 5, so as to define methods for shapes analysis and matching. In Section 6 a description of the feature vector and used classifiers is given. In Section 7, experiments and |
| In this paper we present a novel approach for 3D identity- independent facial expression recognition based on a local shape analysis. Unlike the identity recognition task that has been the | | results of our approach are reported, and the average recognition rate over 97% is achieved using machine-learning algorithms for the recognition of facial expressions such as multiboosting and |
| subject of many papers, only few works have addressed 3D facial expression recognition. This could be explained through the | | SVM. Finally, discussion and conclusion are given in Section 8. |
| challenge imposed by the demanding security and surveillance requirements. Besides, there has long been a shortage of publicly | ing security and surveillance ig been a shortage of publicly 2. Related work | work |
| available 3D facal expression databases that serve the research- ers exploring 3D information to understand human behaviors and emotions. The main task is to classify the facial expression of | | Facial expression recognition has been extensively studied over the past decades especially in 2D domain (e.g., images and videos) resulting in a valuable enhancement. Existing approaches that address facial expression recognition can be divided into the categories; (1) stufic versus dynamic (2) global versus local: |
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| 0031-3203/S- see front matter © 2011 Elsevi doi:10.1016/j.patcog.2011.02.012 | er Ltd. All rights reserved. | |

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geometric feature based facial expression descriptor, derived from presented a survey where they explored and compared different approaches that were proposed, since the mid 1970s, for facial extraction/detection as a mean to represent and understand facial expressions. Pantic and Rothkrantz [4] and Samal and Jengar [5] issue was presented by Wang et al. [8]. They proposed a novel for 3D facial expression recognition, the first work related to this ment in recognition accuracy compared to the global analysis. As that the local expression analysis showed no consistent improvefacial expressions. They reported, in their study on face images, elementary muscle movements involved in the bio-mechanical of (FACS) manual by Ekman and Friesen [7], and designating the (AUs), defined in the well-known Facial Action Coding System particular, their study is based on the classification of action units versus Global segmentation for facial expression recognition. In sequences. Whitehill and Omlin [6] investigated on the Local expression analysis from either static facial images or image

and test several classifiers. They reported that the highest average recognition rate they obtained was 83%. They evaluated their approach not only on frontal view facial expressions of the BU-3DFE database, but they also tested its robustness to non-frontal views. A second work was reported by Soyel and Demire[19] on the same database. They extracted six characte-istic distances between 11 facial landmarks, using Neural Netthey mentioned that the surprise expression was recognized with facial expressions of disgust and surprise were well identified models to encode both identity and expression. They reported an average recognition rate of 90.5%. They also reported that the achieved was 91.3%. Mpiperis et al. [10] proposed a joint 3D face and facial expression recognition using bilinear model. They fitted work architecture that analysis the calculated distances, they classified the BU-3DFE facial scans into seven facial expressions tures, and they constructed samples that have been used to train an accuracy of 99.2%. rithm, they reported an average recognition rate of 95.1%, and ones. Using regularized multi-class Adaboost classification algodean distances between two picked landmarks from 83 possible with an accuracy of 100%. Tang and Huang [11] proposed an both formulations, using symmetric and asymmetric bilinear including neutral expression. The average recognition rate they an estimation of primitive surface feature distribution. automatic feature selection computed from the normalized Eucli-A labeling scheme was associated with their extracted fea-

> contributions of our approach are the following: (1) We propose a new process for representing and extracting patches on the techniques to perform such classification analysis approach of 3D faces and several machine-learning 3D facial scans. Thus, we combine a local geometric-based shape similarity measure between corresponding patches on different we apply a framework to derive 3D shape analysis to quantify facial surface scan that cover multiple regions of the face and (2) identity-independent facial expression recognition. The main In this paper, we further investigate the problem of 3D

3. Database description

BU-3DFE is one of the very few publicly available databases of annotated 3D facial expressions, collected by Yin et al. [12] at Binghamton University. It was designed for research on 3D

Tappy Angry rear Disgust Sad Surbrise

Fig. 1. Examples of 3D facial expression models (first row 3D shape models, second row 3D textured models) of the BU-3DFE database.

Most of the earlier work in 3D shape analysis use shape descriptors such as curvature, crest lines, shape index (e.g., ridge, saddle, rut, dome, etc.). These descriptors are defined based on the geometric and topological properties of the 3D object, and are used as features to simplify the representation and thus the

the highest intensity level.

4. 3D facial patches-based representation

that undergo specific deformations due to single muscles move-ments when conveying facial expression [7]. In Fig. 1, we illustrate of 83 manually annotated facial landmarks is associated to each Happiness (HA), Anger (AN), Fear (FE), Disgust (DI), Sad (SA) and Surprise (SU). The expressions vary according to four levels of ogy, etc. There are a total of 100 subjects in the database, 56 females and 44 males. A neutral scan was captured for each human face and facial expression and to develop a general understanding of the human behavior. Thus the BU-3DFE dataexamples of the six universal facial expressions 3D models including model. These landmarks are used to define the regions of the face 25 3D facial expression models per subject in the database. A set intensity (low, middle, high and highest or 01–04). Thus, there are subject, then they were asked to perform six expressions namely: human computer interaction, security, communication, psycholbase is beneficial for several fields and applications dealing with

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were able to compare 3D shapes by comparing facial curves facial expressions and rigid motions. Using this approach they being and a point of the extracted curve along the facial surface. This path between a fixed reference point (taken to be the nose tip) (i.e., geodesic distance) defined to be the length of the shortest faces. These curves are level curves of a surface distance function facial surfaces by an indexed collections of 3D closed curves on is needed. In Samir et al. [13] the authors proposed to represent behavior or expression, and a robust facial surface representation the facial surface labeling is a critical step to describe the facial can be sensitive to noisy data. In case of 3D facial range models numerical approximation that involves second derivatives and their rigorous definition, such features are computed based on comparison for 3D shape matching and recognition tasks. Despite motivated by the robustness of the geodesic distance to

of patches extraction.

Each c_{λ}^{j} is a closed curve, consisting of a collection of points situated at an equal distance λ from n. Fig. 2 momentum contents of the set of

 $\|r_l-.\|:c_\lambda^l=\{p\in S|\|r_l-p\|=\lambda\}\subset S,\quad \lambda\in[0,\lambda_0].$

Э

defined the curves as level sets of

use the Euclidean distance function $||r_l - p||$ to characterize the

length between r_l and any point p on S. Using this function we

we choose to consider N reference points (landmarks) $(r_i)_{1 \le i \le N}$ (Fig. 2(a)) and associated sets of level curves $(c_{j}^i)_{1 \le i \le d_0}$ (Fig. 2(b)). These curves are extracted over the patches centered at these points. the facial surface. We are especially interested in capturing mouth corner and the outside eye corner. discarding those marked on the face border. Contrary to the MPEG-4 feature points specification that annotates the cheeks center and based on the facial anatomy structure. Given these points the feature model there are 83 manually picked landmarks, these landmarks are capture differences related to variant expressions. To this end, distance which is sensitive to deformations and thus can better Using a different solution, we compute curves using the Euclidean rather than comparing corresponding shape descriptors by extracting the middle point along the geodesic path between the regions. Thus, we add two extra landmarks at both cheeks, obtained bone, in BU-3DFE there were no landmarks associated with the cheek interested in a subset of 68 landmarks laying within the face area, region on the face can be easily determined and extracted. We were practically similar to the MPEG-4 feature points and are selected stands for the maximum value taken by λ . Accompanying each facial reference point r_l and the point belonging to the curve c'_{λ} , and λ_0 Here λ stands for the value of the distance function between the deformations of local facial regions caused by facial expressions. In our work we intend to further investigate on local shapes of We propose to represent each facial scan by a number of

the facial surface denoted by S. Each patch will be represented by point and P_l a given patch centered on this point and localized on patches centered on the considered points. Let r_l be the reference

an indexed collection of level curves. To extract these curves, we

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Automatically added landmarks Retained landmarks provided by BU-3DFE Discarded landmarks provided by BU-3DFE

> be deformed in a similar way, while those associated with two different expressions will deform differently. The following secby the common belief that people smile, or convey any other and design a similarity measure between corresponding ones on different scans under different expressions. This is motivated Ģ 5.1. 3D curve shape analysis local patches on facial surfaces dynamical deformation process. We expect that certain corretaking part in a specific expression undergo practically the same expression, the same way, or more appropriately certain regions introduced by Joshi et al. [3], and its extension to analyze shape of tions describe the shape analysis of closed curves in \mathbb{R}^3 , initially sponding patches associated with the same given expression will Once the patches are extracted, we aim at studying their shape Framework for 3D shape analysis We start by considering a closed curve β in \mathbb{R}^3 . While there are

using a square-root representation of β as follows; for an interval (2) this method uses a square-root representation under which the elastic metric reduces to the standard \mathbb{L}^2 metric and thus analysis of the parametrized curves is particularly appropriate in 3D curves analysis. This is because (1) such analysis uses a I=[0,1], let $\beta:I\longrightarrow \mathbb{R}^3$ be a curve and define $q:I\longrightarrow \mathbb{R}^3$ to be its To analyze the shape of β , we shall represent it mathematically distance between curves is invariant to the re-parametrization. simplifies the analysis, (3) under this metric the Riemannian compare local facial shapes in presence of elastic deformations, square-root velocity function representation which allows us to several ways to analyze shapes of closed curves, an elastic

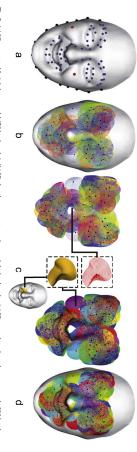


Fig. 2. (a) 3D amotated facial shape model (70 landmarks); (b) 3D closed curves extracted around the landmarks; (c) 3D curve-based patches composed of 20 level curves with a size fixed by a radius /=20 mm; (d) extracted patches on the face.

the orbits q_1 and q_2 , to reduce the notation

denote the length of the geodesic in the shape space S between remainder of the paper, we will use the notation $d_{\mathcal{S}}(\beta_1,\beta_2)$ to

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square-root velocity function (SRVF), given by:

 $q(v) \doteq \sqrt{\|\dot{\beta}(t)\|}$ $\hat{\beta}(t)$

2

5.2.

3D patches shape analysis

the metric: for any $u, v \in T_q(\mathcal{O})$, we define: to a non-linear (closure) constraint on its elements, C is a nonthe set: $C = \{q : \mathbb{S}^1 \longrightarrow \mathbb{R}^3 | \int_{\mathbb{S}^1} q(t) || q(t) || dt = 0\} \subset \mathbb{L}^2(\mathbb{S}^1, \mathbb{R}^3)$. Notice that the elements of C are allowed to have different lengths. Due In order to restrict our shape analysis to closed curves, we define the \mathbb{L}^2 -metric. Also, the squared \mathbb{L}^2 -norm of q, given by: $\|q\|^2 = \int_{\mathbb{S}^1} \langle q(t), q(t) \rangle dt = \int_{\mathbb{S}^1} \|\beta(t)\| dt$, which is the length of β . point is very important as it simplifies the calculus of elastic becomes the L^2 -metric under the SRVF representation [14]. This We note that q(t) is a special function that captures the shape of β and is particularly convenient for shape analysis, as we describe linear manifold. We can make it a Riemannian manifold by using metric to the well-known calculus of functional analysis under next. The classical elastic metric for comparing shapes of curves Here t is a parameter $\in I$ and $\|.\|$ is the Euclidean norm in \mathbb{R}^3

$$\langle u, v \rangle = \int_{-1}^{1} \langle u(t), v(t) \rangle dt.$$

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 $q(\gamma(t))$. We set the elements of the orbit: of β . The corresponding SRVF changes according to $q(t) \mapsto \sqrt{\dot{\gamma}(t)}$ \mathbb{S}^1 (to itself) and the elements of Γ are viewed as re-parameterthis variability, we define orbits of the rotation group SO(3) and see that several elements of C can represent curves with the same shape. For example, if we rotate a curve in \mathbb{R}^3 , we get a different endowed it with a Riemannian structure. Next we consider the issue of representing the *shapes* of these curves. It is easy to function $\gamma : S' \rightarrow S$ ization functions. For example, for a curve $\beta : \mathbb{S}^1 \to \mathbb{R}^3$ and a Here, Γ is the set of all orientation-preserving diffeomorphisms of the re-parameterization group Γ as the equivalence classes in C. changes the SRVF of curve but not its shape. In order to handle arises when a curve is re-parametrized; a re-parameterization SRVF but its shape remains unchanged. Another similar situation So far we have described a set of closed curves and have $\gamma \in \Gamma$, the curve $\beta \circ \gamma$ is a re-parameterization

$[q] = \left\{ \sqrt{\dot{\gamma}(t)} Oq(\gamma(t)) | O \in SO(3), \gamma \in \Gamma \right\},\$

set of such equivalence classes, denoted by $S \equiv C/(SO(3) \times \Gamma)$ is called the *shape space* of closed curves in \mathbb{R}^3 . S inherits a Riemanto be equivalent from the perspective of shape analysis. The

basic idea here is to connect the two points $[q_1]$ and $[q_2]$ by an arbitrary initial path z and to iteratively update this path using the negative gradient of an energy function $E[q_2] \int_{\lambda} dz(s)$, $z(s) \land ds$. The interesting part is that the gradient of *E* has been derived analytically and can be used directly for updating *z*. As in S. Thus, this gradient-based update leads to a critical point of E and q_2 , we want to compute a geodesic path between the orbits $[q_1]$ and $[q_2]$ in the shape space *S*. This task is accomplished using Given any two curves β_1 and β_2 , represented by their SRVFs q_1 curves is the construction of a geodesic between any two elements of S, under the Riemannian metric given in Eq. (3). nian metric from the larger space $\ensuremath{\mathcal{C}}$ due to the quotient structure. which, in turn, is a geodesic path between the given points. In the shown in [15], the critical points of E are actually geodesic paths a path-straightening approach which was introduced in [15]. The The main ingredient in comparing and analysing shapes of

 $\{c_{\lambda}^{2}, \lambda \in [0, \lambda_{0}]\}$ and $\{c_{\lambda}^{2}, \lambda \in [0, \lambda_{0}]\}$, respectively, our idea is to compare the patches curves c_{λ}^{2} and c_{λ}^{2} , and to accumulate these differences over all λ . More formally, we define a distance $d_{S^{(0,b)}}$ given by: curves. Given any two patches P_1 and P_2 , and their level curves two patches are compared by comparing their corresponding level as an element of the set $S^{[0,\lambda_0]}$. In our framework, the shapes of any $||r_l-.|| = \lambda$. Through this relation, each patch has been represented $P_1 \leftrightarrow \{c_2^l, \lambda \in [0, \lambda_0]\}$, where c_2^l is the level set associated with function (Euclidean distance from the reference point r_l). That is, surface S with an indexed collection of the level curves of the $||r_{l}-.|$ analyzing shapes of curves to the shapes of patches. As mentioned earlier, we are going to represent a number of *l* patches of a facial Now, we extend ideas developed in the previous section from

$$d_{an+1}(P_1, P_2) = \int_{-\infty}^{\infty} d_{e}(c_1^1, c_2^2) d\lambda$$

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biometry and other classification experiments, we also have a geodesic path in S^{0,c_0} between the two points represented by P_1 facial expressions. These geodesics are termed inter-class geode mean curvature mapping representations of the patches along the geodesic path from the source to the target. The mean deform in a different way sics. Unlike the intra-class geodesics shown in Fig. 3, these patches contrast, Fig. 4 shows geodesic paths between patches of different the same class of expression, are deformed in a similar way. In of geodesics. This figure shows that certain patches, belonging to areas on the source and target patches and equally spaced steps curvature representation is added to identify concave/convex the geodesic paths. In each row we have both the shape and the models of different subjects. As for the middle column, it shows expressions. The third column represents the targets represents scan models of the same subject, but under different geodesics. In the first column we illustrate the source, which models sharing the same expression, and termed intra-class computed between corresponding patches associated with shape another. Fig. 3 shows some examples of geodesic paths that are tions of facial curves and, thus, facial surfaces from one to and P₂. This geodesic corresponds to the optimal elastic deforma-In addition to the distance $d_{S^{(0,i_0)}}(P_1,P_2)$, which is useful in as scan

6. Feature vector generation for classification

4

one on the reference face scan. All feature vectors computed on the overall dataset will be labeled and used as input data to by BU-3DFED and the two additional cheek points). The ith element of this vector represents the length of the geodesic vector is then formed by the distances computed on all the patches and its dimension is equal to the number of used landpath that separates the relative patch to the corresponding marks N = 70 (i.e., 68 landmarks are used out of the 83 provided curves in the two patches as indicated in Eq. (5). The feature the sum of the distances between all pairs of corresponding candidate scan and the other in the reference scan, is defined as shortest path between two patches at landmark i, one in a for shape analysis of 3D curves (see Sections 5.1 and 5.2). The reference scan is computed using a Riemannian framework between each level curve and its corresponding curve on the landmarks of a reference scans ref. The length of the geodesic path landmark. Similarly, a patch Pref is extracted in correspondence to P_{j}^{i} , a set of level curves $\{c_{\lambda}\}_{j}^{i}$ are extracted centered on the *i*th patches are extracted around facial landmarks. For a facial patch each facial scan. Given a candidate facial scan of a person j, facial In order to classify expressions, we build a feature vector for 1584

1583



| | · | 1 |
|------|-------------|---|
| rate | Recognition | |
| | 98.81% | |
| | 98.76% | |
| | 98.07% | |
| | 97.75% | |

Classifier Multiboost-LDA Multiboost-NB Multiboost-NN SVM-Linear

Table 1 Classification results using local shape analysis and several classifiers.

Several facial expression recognition experiments were con-

Discriminant Analysis (LDA), Naive Bayes (NB), and Nearest Neighbor (NN), to the extracted features, and we achieved boost algorithm with three ment for Knowledge Analysis (Weka) [17], we applied the multithe selected references (neutral scan). Using the Waikato Environweak classifiers, namely, Linear

ducted with changing at each time the reference. Fig. 5 illustrates

Fig. 5. Different facial expression average recognition rates obtained using different reference subjects (using multiboost-LDA).

N References

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4

J

σ

50 60 70 8 90

Average Recognition Rate (%)

100 110

99.86

99.58

. ∳8.88

-98.6

98.05

97.91

120

Fig. 4. Examples of inter-class (different expressions) geodesic paths between source and target patches.

7.2. Discussion of the results

machine-learning algorithms such as multiboosting and SVM, where multiboosting is an extension of the successful Adaboost technique for forming decision committees.

Fig. 3. Examples of intra-class (same expression) geodesic paths with shape and mean curvature mapping between corresponding patches.

7. Recognition experiments

To investigate facial expression recognition, we have applied our proposed approach on a dataset that is appropriate for this task. In this section, we describe the experiments, obtained

results and comparisons with related work.

7.1. Experimental setting

For the goal of performing identity-independent facial expression recognition, the experiments were conducted on the BU-3DFE static

dimensions of the captured human faces. Following a similar setup as in [16], we randomly divided the 60 subjects into two sets, the training set containing 54 subjects (648 samples), and the test set them were female and the other half (30) were male, corresponding to the high and highest intensity levels 3D expressive models (03containing six subjects (72 samples) 04). These data are assumed to be scaled to the true physical database. A dataset captured from 60 subjects were used, half (30) of

To drive the classification experiments, we arbitrarily choose a set of six reference subjects with its six basic facial expressions. We the training nor in the testing set. These references, shown in Fig. 5, with their relative expressive scans corresponding to the highest point out that the selected reference scans do not appear neither in

for each of the six classes of expressions. For each reference subject, we derive a facial expression recognition experience. intensity level, are taken to play the role of representative models

the resulting recognition rates in Table 1.





0

Reference



Source

7

Reterence

concave

a.

3

CONV

Query

0

C

1586

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Target

between 83 landmarks, Soyel et al. [9] calculated six distances using a distribution of 11 landmarks, while Wang et al. [8] derived curvature estimation by locally approximating the 3D surface with a smooth polynomial function. In comparison, our approach capture the 3D shape information of local facial patches statistical analysis will generalize to an independent dataset, in [8] a 20-fold cross-validation technique was used, while 6 subject partitions) of the BU-3DFE database. The differences between approaches should be noted: Tang et al. [11] performed Table 2 Average (to derive shape analysis. For assessing how the results of their can see that most relevant patches are localized around the eyebrows and the mouth region. It can be seen that patches patches. Notice that, for example, for the Happy expression the selected patches are localized in the lower part of the face, classification using multiboost-LDA is given in Table 2 reported in [11,9,8], on the same experimental setting (54 versus 7.3. Comparison with related work to this expression. selected for each expression lie on facial muscles that contribute around the mouth and the chin. As for the Surprise expression, we algorithm and the selected patches in each iteration. classifiers. Then, we look at the early iterations of the multiboost expression. In this case, we consider these features as weak tioned above, we apply the multiboost algorithm on feature classes. SU HA E D N automatic feature selection using normalized Euclidean distances vectors built from distances between patches for each class of result in a better linear separation between facial expression features into a more discriminative space and, consequently the capability of the LDA-based classifier to transform the In Table 3 results of our approach are compared against those In order to better understand and explain the results men-Fig. 6 illustrates for each class of expression the most relevant The average confusion matrix relative to the best performing confusion matrix given by multiboost-LDA classifier. Ą 97.92 0.56 0.14 0.56 0.28 0.14 1.11 99.16 0.14 0.14 0.14 0.56 ⊒ 0.14 0.14 **99.72** 0.0 0.0 æ HĂ 0.14 0.0 **98.60** 0.0 SA 0.69 0.14 0.56 **99.30** 1.11

> in [11,9] the authors used 10-fold cross-validation to validate their approach.

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1588

number of instances.

terms of accuracy than the other classifiers. This is mainly due to

7.4. Non-frontal view facial expression recognition

the landmark is visible, but the region nearby is partially occluded, we treat it as a missing data problem for all faces large pose variations. By rotating the 3D shape models in the y-direction, we generate facial scans under six different nonalways available. Thus, non-frontal view facial expression recog-nition is a challenging issue that needs to be treated. We were the geodesic distance between the kth patch belonging to subjects scenario obtained from the training set. Let $d_{ijk} = d_{S^{(0,i_0)}}(P_i^k, P_j^k)$ be values by the means of values already calculated in frontal view imputation technique [18]. In our experiments we employed the entries in the distance matrix are blank and we fill them using an geodesic path between corresponding patches. The corresponding sharing this view. In these cases, we are not able to compute the the given scan. In cases where a landmark is occluded, or where the landmark is visible, but the region nearby is partially perform facial patches extraction around the visible landmarks in occluded facial regions due to the face pose. For each view, we *i* and *j* (*i* \neq *j*). In case of frontal view (*fv*), the set of instances X_i^{fv} mean imputation method, which consists of replacing the missing rotation. We assume that shape information is unavailable for the interested in evaluating our approach on facial scan under frontal views corresponding to 15° , 30° , 45° , 60° , 75° and 90° In real world situations, frontal view facial scans may not be

relative to the subject *i* need to be labeled and is given by:

$$\mathbf{X}_{i}^{\mathbf{V}} = \begin{pmatrix} d_{i11} & \dots & d_{i1k} & \dots & d_{i1k} \\ \vdots & \vdots & \vdots & \vdots \\ d_{ij1} & \dots & d_{ijk} & \dots & d_{ijk} \\ d_{ij1} & \dots & d_{ijk} & \dots & d_{ijk} \end{pmatrix}$$

Χ^{fv} =

where N is the number of attributes. In case of non-frontal view (n/v), if an attribute k stm using, we replace the kth column vector in the distance matrix X₁th by the mean of geodesic distances computed in the frontal view case, with respect to the kth attribute and given by: $m_k^{tp} = \sum_{j=1}^{r} d_{jk}/J$, where J is the total

SU 0.0 0.0 0.14 0.28 **98.19** Table 3 10-fold 20-fold Comparison of this work with respect to previous work [11,9,8]. Cross-validation This work Tang et al. [11] Soyel et al. [9] Wang et al. [8] 98.81% 92.75% 95.1% 91.3%

83.6%



Fig. 6. Selected patches at the early few iterations of multiboost classifier for the six facial expressions (Angry, Disgust, Fear, Happy, Sadness, Surprise) with their associated weights.

Happy

Angry

Fear

Disgust

Sad



As shown in this figure, recognition accuracy remains acceptable, is the best performing methods also in the case of pose variations. from 0° to 90° of rotation are considered), and the multiboost-LDA on the chosen database. From the figure, it can be observed that rates of the four classification methods. The multiboost-LDA only on frontal view facial scans. Fig. 7 shows the average error different testing facial views using the four classifiers trained 3D face by 45° in y-direction even only 50% of data (half face) are available when we rotate the the average error rates increase with the rotation angle (values shows the best performance for facial expression classification recognition. Error recognition rates are evaluated throughout frontal views, we derive a view-independent facial expression To evaluate the robustness of our approach in a context of non-

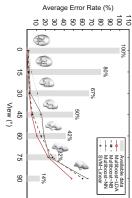


Fig. 7. The average error rates of six expressions with different choices of views corresponding to the best reference and using different classifiers.

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7.5. Sensitivity to landmarks mis-localization

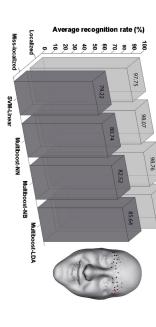
is a challenging problem. The most difficult task remains the localization of points around the eyebrow regions, which appear a region with a radius of 10 mm, as illustrated Fig. 8 by blue circles. Then we performed expression recognition experiments with such noise to the position of the landmarks by moving them randomly in landmarks provided with the BU-3DFED. In particular, we added to detect automatically. In these regions, we added noise to the the points in these regions are expected to be the most difficult specific experiment. We considered the eyebrow regions in that the mis-localization of the landmarks has been addressed in a to play an important role in the expression of emotions. The effect of It is known that the automatic 3D facial feature points detection

BU-3DFE database. We demonstrated the robustness of the proposed method to pose variations. In fact, the obtained recogniscan is missed. tion rate remains acceptable (over 93%) even half of the facial recognition rate for six prototypical facial expressions on the rithm for multi-class classification, we achieved a 98.81% average and test machine-learning algorithms. Using multiboost algoto the six prototypical expressions and used as samples to train geodesic distances between patches were labeled with respect geodesic path were explored to derive shape analysis. The

98.81

8. Conclusions independent facial expression recognition from 3D facial shapes. Our idea was to describe the change in facial expression as a et al [8]. that with the multiboost-LDA algorithm the lower decrease in the recognition rate is observed, and even with a recognition rate equal desic paths) and quantitative (geodesic distances) measures of the between corresponding patches. Qualitative (inter- and intrageonian framework was applied to compute the geodesic path shape descriptors for facial expression representation. A Rieman facial surfaces was proposed. These patches were used as local automatic extraction of local curve-based patches within the 3D deformation in the vicinity of facial patches in 3D shape scan. An to 85.64% the result still outperforms the one reported in Wang noisy landmarks. The results are reported in Fig. 8. It can be noted In this paper we presented a novel approach for identity

Fig. 8. Recognition experiment performed adding noise to the eyebrow landmarks (random displacement). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)



The major limitation of our approach is that the 68 landmarks we used to define the facial partches were manually labeled. For our future work we are interested in detecting and tracking facial feature points, as proposed in [19,20], for automatic 3D facial expression recognition.

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classes. Although several modalities, such as fingerprints FSU, Tallahassee, FL 32306, USA LIFL (UMR USTL/CNRS 8022) Université de Lille 1, France. http://stat.fsu.edu/~anuj/ Departement of Statistics hassen.drira@lifl.fr Anuj Srivastava Hassen drira Abstract http://www.telecom-lillel.eu/people/benamor/ Institut TELECOM ; TELECOM Lille 1, France. http://www.telecom-lille1.eu/people/daoudi/ Institut TELECOM ; TELECOM Lille 1, France. lips, and outside regions. These factors lead to a decrease collected by laser scanners, for studying shapes of peoples' faces and using this data for biometrics. The output from laof this idea. Since 2D (visible light) images of faces are cally gets holes in the scanned data in locations of eyes such surfaces, with the current laser technology. One typi other important challenge relates to data collection and that this variability has become one of the most important change the shapes of facial parts to some extent. We argue metric applications. In fact, changes in facial expressions mating the mood of a person, for example in developing tional state of a person. While they are important in estismile, fear, and anger, etc, are prime indicators of the emochanges in facial expressions. Facial expressions, such as of facial parts. Perhaps the only major remaining variabichers have argued for the need to use 3D face data, typically ments (camera pose, illumination patterns, etc.), the researgreatly susceptible to variations in the imaging environan individual feature/modality in identifying human beings. pristine, continuous facial surfaces, or meshes representing perfections introduced in that process. It is difficult to obtain issue in 3D face recognition as described in [2] and [9]. The intelligent ambient systems, they have a lesser role in biomeasurements of the same person, is the one introduced by lity that is manifested within the same class, i.e. within the mental factors and provide faithful measurements of shapes ser scanners are minimally dependent on external environled to the notion of partial biometrics – the contribution of joint analysis may succeed for large populations. This has feature provides certain a partial information, such that their ferent features (characteristics) and modalities, where each Instead, an emerging consensus to develop a suite of difitself may lead to a generic solution for a large population face images, iris, and gait, have been tried, none of them by LIFL (UMR USTL/CNRS 8022) LIFL (UMR USTL/CNRS 8022) The use of shapes of facial parts is an important example Boulbaba Ben Amor Mohamed Daoudi

> a reasonably large database (involving 2000 scans), (ii) Seevaluate the choice of (shape of) nose as a partial metric on compare surfaces by comparing their corresponding curves [1, 14]. Our goals here are several : (i) Firstly, we want to is Riemannian. That is, we define a differentiable maniin facial expressions make it an important partial biometric choice of feature for biometrics. The shapes of noses seem a facial surface and have compared their contributions. We nasal surfaces distances and Karcher means for clustering and averaging med. Towards this end, we will explore the use of geodesic hierarchical (tree) so that efficient searches can be perforthe database containing noses of a large population into a condly, we want to use Riemannian geometry to organize use a collection of iso-curves to represent a surface and to based on similar ideas followed previously for full faces represent individual noses. Our choice of representation is fold, with a suitable Riemannian metric, whose elements shape analysis, and the invariance of nasal shape to changes The stability of nose data collection, the efficiency of nasal ted using a more elaborate, multi-modal biometric system potheses so that a reduced hypothesis set can be evalua tion, but we argue for its role in shortlisting possible hyficient for identifying human subjects across a vast populaanalysis. We reiterate that this framework may not be sufchoice using real data and automated techniques for shape very similar to a human observer but we will support this analysis of facial parts. are not aware of any past work in an elastic (Riemannian) Faltemier et al. [5] have studied several different regions on shape does not change with facial expressions. Similarly advantage of using the ear, just like the nose [4], is that its have studied the use of human ear for recognition. The main parts for biometrics is not new. For example, [16] and [3] dually, especially for partial biometrics. The use of facial (missing data), we advocate the use of facial parts indivi-Our approach for analyzing shapes of nasal surfaces At the outset, the shape of the nose seems like a bad

> > 2.1. Nasal Curves

Let N be a nasal surface, output of our preprocessing

2 we summarize some past work on comparing shapes of shapes. rather than n, by deriving a hierarchical database of gallery seek to make the database search more efficient, $O(\log(n))$ each query shape to each gallery shape. In the Section 4, we thentification. These experiments are based on comparing distances in two biometric scenarios - identification and aunasal surfaces. In Section 3, we study the use of geodesic classical Karcher mean computation to compute average of idea to analyze shapes of nasal surfaces. Also, we apply the closed curves in \mathbb{R}^3 using an elastic metric, and apply this The rest of this paper is organized as follows. In Section

Ē.

We start by considering a closed curve β in \mathbb{R}^3 . Since

 $c_{\lambda} = \{p \in N | D(p) = GD(r, p) = \lambda\} \subset N$ where r de-

according to $N = \bigcup_{\lambda} c_{\lambda}$ (see figure 1).

on the mesh. We can reconstruct N from these level curves and GD(r, p) is the length of the shortest path from r to p notes the reference point (in our case the tip of the nose) D, also called a **nasal curve**, for the value $\lambda \in D(N)$, i.e nuous geodesic map on N. Let c_{λ} denote the level set of it is a continuous surface. Let $D : N \longrightarrow \mathbb{R}^+$ be a contitriangulated mesh, we start the discussion by assuming that gion) illustrated in Figure 1. Although, in practice, N is a step (removing spikes, filling holes, and cropping nasal re-

it is a closed curve, it is natural to parametrize it using β : $\mathbb{S}^1 \to \mathbb{R}^3$. Note that the parametrization is not assutrizations for improved analysis. To analyze the shape of med to be arc-length; we allow a larger class of parametion

 β , we shall represent it mathematically using a square-root

FIGURE 1. Automatic data preprocessing and nasal curves extrac-

in biometric performance. To handle these issues - shape variability due to facial expressions and presence of holes Our approach is to analyze shapes of nasal surfaces using

A Riemannian Analysis of 3D Nose Shapes For Partial Human Biometrics

lation) of the original surface. At least theoretically, these are invariant to the rigid transformation (rotation and transsic distance function on the surface, their geometries in turn these curves rather than the full continum. nasal curves, have been defined as level curves of an intrinmetries of the associated curves. Since these curves, called and the geometry of a surface is then studied using the geointo an indexed collection of simple, closed curves in \mathbb{R}^3 shapes of iso-curves. In other words, we divide each surface

elastic shape analysis of continuous, closed curves in \mathbb{R}^n we will follow the theory laid out by Joshi et al. [7, 8] for In recent years, there have been several papers for stu-

mainly concerned with curves in \mathbb{R}^2 [11, 12]. In this paper, dying shapes of continuous curves, the earlier papers were information is lost when one works with a finite subset of curves without any ambiguity. In practice, however, some and one can go back-and-forth between the surface and the curves jointly contain all the information about the surface

corresponding curves. We extend past work in Riemannian curves, and to analyze shapes of noses by comparing their low for efficient searches. these ideas in two application contexts : authentication and statistical means, and stochastic clustering. We demonstrate we obtain algorithms for computing geodesics, computing lar Riemannian analysis for nasal surfaces. In particular, analysis of shapes of closed curves in \mathbb{R}^3 to obtain a simirepresent nasal surfaces using indexed collections of isoperforming partial human biometrics. The basic idea is to present a hierarchical organization of nose databases to albase involving 2000 scans from FRGC v2 database, and identification. We evaluate performances on a large data-In this paper we explore the use of shapes of noses for

1. Introduction

cused on body parts and images that try to minimize this and so on. Therefore, the biometrics researchers have focolors, illumination environment, presence of other parts metrics in our increasingly digital society. By human biovariability within class (subjects) and maximize it across have a large variability and are influenced by their shapes human body parts and their appearances, to identify indimetrics we mean the use of physiological characteristics, of safely expect an exponential growth in a general use of bioyears have been motivated by security applications, one can importance and potential. Although its growth in recent The appearances of body parts, especially in imaged data, vidual human beings in the course of their daily activities Human biometrics has become an area of tremendous

2. Riemannian Framework

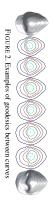
(1) Here $\mathbb{L}^2(\mathbb{S}^1, \mathbb{R}^3)$ denotes the set of all functions from \mathbb{S}^1 to \mathbb{R}^3 that are square integrable. The quantity $\int_{\mathbb{S}^3} q(t) ||q(t)|| dt$ denotes the total displacement in \mathbb{R}^3 as one traverses along the curve from start to end. Setting it accords $\ensuremath{\mathcal{C}}$ due to the quotient structure $\mathcal{C}=\{q:\mathbb{S}^1\to\mathbb{R}^3|\; \int_{\mathbb{T}^1}q(t)\|q(t)\|dt=0\}\;\subset\;\mathbb{L}^2(\mathbb{S}^1,\mathbb{R}^3)$ rence is made clear by the context. curves, we define the set : calculus of elastic metric to the well-known oneunder the sentation [7]. This point is very important as it simplifies $q(t) \doteq \frac{\beta(t)}{\sqrt{\|\dot{\beta}(t)\|}}$. The classical elastic metric for comparing the elements of the set : fold by using the metric : for any $u, v \in T_q(\mathcal{C})$, we define : Due to a non-linear (closure) constraint on its elements, C is that the elements of C are allowed to have different lengths closed valent \mathbb{L}^2 -metric. In order to restrict our shape analysis to closed shapes of curves becomes the $\mathbb{L}^2\text{-metric}$ under this reprea non-linear manifold. We can make it a Riemannian mani- $[q] = \left\{ \sqrt{\dot{\gamma}(t)} Oq(\gamma(t)) | O \in SO(3), \ \gamma \in \Gamma \right\},\$ $\langle u,v\rangle = \int_{\mathbb{S}^1} \left\langle u(t),v(t)\right\rangle dt \; .$

ve from start to end. Setting it equal to zero is equi-
to having a closed curve. Therefore,
$$C$$
 is the set of all
curves in \mathbb{R}^3 , each represented by its SRVF. Notice

on C and the Euclidean metric in \mathbb{R}^3 hoping that the diffe-We have used the same notation for the Riemannian metric

as re-parameterization functions. For example, for a curve $\beta : \mathbb{S}^1 \to \mathbb{R}^3$ and a function $\gamma : \mathbb{S}^1 \to \mathbb{S}^1 \gamma \in \Gamma$, the curve $\beta(\gamma)$ is a re-parameterization of β . The corresponding SRVF changes according to $q(t) \mapsto \sqrt{\gamma(t)}q(\gamma(t))$. We set we define orbits of the rotation group SO(3) and the recurve but not its shape. In order to handle this variability, easy to see that several elements of C can represent curves the issue of representing the shapes of these curves. It is phisms of S^{\perp} (to itself) and the elements of Γ are viewed parameterization group Γ as the equivalence classes in Cparametrized; a re-parameterization changes the SRVF of ged. Another similar situation arises when a curve is re- \mathbb{R}^3 , we get a different SRVF but its shape remains unchanendowed it with a Riemannian structure. Next we consider Here, Γ is the set of all orientation-preserving diffeomorwith the same shape. For example, if we rotate a curve in So far we have described a set of closed curves and have

 $C/(SO(3) \times \Gamma)$ is called the *shape space* of closed curves in \mathbb{R}^3 . *S* inherits a Riemannian metric from the larger space to be equivalent from the perspective of shape analysis. The set of such equivalence classes, denoted by S =



velocity function (SRVF), denoted by q(t), according to

to improve display of geodesics. We will use the notation extracted from the two surfaces, and the intermediate curves dient of an energy function $E[\alpha] = \frac{1}{2} \int_s \langle \dot{\alpha}(s), \dot{\alpha}(s) \rangle ds$. The interesting part is that the gradient of *E* has been deriween the orbits $[q_1]$ and $[q_2]$ in the shape space S. This task β_1 and β_2 . the geodesic in S, between representations of the two curves $d([q_1], [q_2])$ to denote the geodesic distance, or the length of sic α . These curves have been scaled to the same length denote equally-spaced points on the corresponding geodeween level curves. The first and the last curves are the ones different subjects and some examples of geodesic paths betcal point of E which, in turn, is a geodesic path between the shown in [10], the critical points of E are actually geodesic ved analytically and can be used directly for updating α . As and to iteratively update this path using the negative grathe two points $[q_1]$ and $[q_2]$ by an arbitrary initial path α is accomplished using a path straightening approach which SRVFs q_1 and q_2 , we want to compute a geodesic path bet of curves is the construction of a geodesic between any two given points. Figure 2 shows two different surfaces of two paths in S. Thus, this gradient-based update leads to a critiwas introduced in [10]. The basic idea here is to connect 2. Given any two curves β_1 and β_2 , represented by their elements of S, under the Riemannian metric given in Eqn The main ingredient in comparing and analysing shapes

3

2.2. Nasal Surfaces

corresponding nasal curves. Given any two nasal surfaces N^1 and $N^2,$ and their associated curves $\{c^1_{\alpha},\lambda\in[0,\lambda_0]\}$ shapes of any two noses are compared by comparing their gion surface S with an indexed collection of the level curves of the D function. That is, $N \leftrightarrow \{c_{\lambda}, \lambda \in [0, \lambda_0]\}$, where and $\{c_{\lambda}^{2}, \lambda \in [0, \lambda_{0}]\}$, respectively, our idea is to compare the curves c_{λ}^{1} and c_{λ}^{2} , and to accumulate these distances over ted as an element of the set $C^{[0,\lambda_0]}$. In our framework, the c_{λ} is the level set associated with the distance D equal to λ . As mentioned earlier, we are going to represent a nose reall λ . For that, we define two possible metrics : Through this relation, each nasal surface has been represen-- Arithmetic mean : d_a : $\mathcal{C}^{[0,\lambda_0]} \times \mathcal{C}^{[0,\lambda_0]} \rightarrow$ Now we extend the framework from curves to surfaces. $\neq \mathbb{R}_{\geq 0},$

- given by $d_a(N^1, N^2) = \frac{1}{\lambda_0} \sum_{\lambda=1}^{\lambda_0} d(c_{\lambda}^1, c_{\lambda}^2).$

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 $- \text{ Geometric mean}: d_g: \mathcal{C}^{[0,\lambda_0]} \times \mathcal{C}^{[0,\lambda_0]} \to \mathbb{R}_{\geq 0}, \text{ given}$ by $d_g(N^1,N^2) = (\prod_{\lambda=1}^L d(c_\lambda^1,c_\lambda^2))^{(1/\lambda_0)}$

> tic deformations of nasal curves and, thus, nasal surfaces in addition to distances. (Also, the distances have important desics between nose regions that belong to different people subject but different scans, while the other rows show geogeodesic paths - The first row involves nose regions of same from one to other. Shown in Figure 3 are examples of such N^1 and N^2 . This geodesic corresponds to the optimal elaswe have a geodesic path in $C^{[0,\lambda_0]}$ between the two surfaces physical interpretations associated with them.) In particular shapes of surfaces is that one has the actual deformations One advantage of a deformation-based comparisons of

E E C C D E Ø C Ø 0 D 0 0 0 C 0 0 0 C Ò C O Č C õ 0

pressions. Last three rows : inter-class paths. two rows : intra-class paths, source and target with different ex-FIGURE 3. Geodesic paths between source and target noses. First

2.3. Mean Nasal Shape

geometry of the manifold to define and compute a mean on that manifold. It is defined as follows : Let $d_s(N^i, N^J)$ denote the length of the geodesic from N^i to N^j in $C^{[0,\lambda_0]}$. define the variance function : In this particular case d_s came from d_a . To calculate the Karcher mean of nose surfaces $\{N^1, ..., N^n\}$ in $C^{[0, \lambda_0]}$, we mean and variance. The Karcher mean utilizes the intrinsic us to perform such statistical analysis for computing noses ture defined on the manifold of nose surfaces $C^{[0,\lambda_0]}$ enables tictics as the "mean" of surfaces. The Riemannian struc-We can now to use our framework to calculate some sta

$$\mathcal{V}: \mathcal{C}^{[0,\lambda_0]} \to \mathbb{R}, \mathcal{V}(N) = \sum_{i=1}^n d_s(N,N^i)^2 \tag{3}$$

The Karcher mean is then defined by

$$\overline{N} = \arg\min_{N \in \mathcal{L}^{[0,\lambda_0]}} \mathcal{V}(N)$$

4

The intrinsic mean may not be unique, i.e. there may be a set of points in $C^{[0,\lambda_0]}$ for which the minimizer of \mathcal{V} is obtained. To interpret geometrically, \overline{N} is an element of $C^{[0,\lambda_0]}$, surfaces that has the smallest total deformation from all given nose

cher mean for a given set of nose surfaces. This approach vely update the current mean μ . presented in Algorithm 1, uses the gradient of V to iterati-We present a commonly used algorithm for finding Kar-

Algorithm 1 Karcher Mean Algorithm

 $\overline{N}_0 = S1.)$ Set k = 0. Choose some time increment $\epsilon \leq \frac{1}{n}$. Choose a point $\overline{N}_0 \in$ $\mathcal{L}^{[0,\lambda_0]}$ as an initial guess of the mean. (For example, one could just take

1- For each i=1,...,n choose the tangent vector $f_i\in T_{\overline{N}_k}(\mathcal{C}^{[0,\lambda_0]})$

which is tangent to the geodesic from \overline{N}_k to N'. The vector $g = \sum_{k=1}^{n-1} f_k$ is proportional to the gradient at \overline{N}_k of the function \mathcal{V} . $\sum_{k=1}^{n-1} f_k$ is proportional to the gradient at \overline{N}_k of the function \mathcal{V} . Z Flow for time k along the geodesic which starts at \overline{N}_k and has velocitly vector g. Call the point where you and up \overline{N}_{k+1} . **3-**Set k = k + 1 and go to step 1.

using the Karcher mean to compute average faces are shown minimizer of the variance function V. Several examples of Since this is a gradient approach, it only ensures a local

in Figures 4.

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two different biometric scenario. These experiments use a In this section we present some experimental results in

3. Application to Human Biometrics

again and find their representative, and so on. Then, at the next higher level, one can cluster these means placed by their representatives, in this case Karcher means first clustered into small groups and these clusters are re-

nization of a population, where people (or observations) are bilities. For example, one can develop a hierarchical orga-

shapes in a biometric application? There are many possi-

What is the motivation for using statistical means of

FIGURE 4. Examples of shapes and their karcher means

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P.

and d_g in biometric applications FIGURE 5. Verification Rate at FAR=0.1% using (1 to k) curves ł

periment. This hypothesis will be tested and discussed in the following experiments. The results of identification and sing through these cavities could be eliminated from the exquery set is identical to the gallery. The effectiveness of d_a lery contains 2000 sessions for 209 different subjects. The of facial expressions on performance, a distance matrix betauthentication scenarios will be presented separately. which exhibit undesired variability. Therefore, curves pasthe nasal region, there are some areas like nasal cavities choose the curves which can give best results ? Indeed, in the number of curves used. But the question is how to ween a gallery and a query datasets is computed. The galthentication scenarios and to explore effect of the presence In order to produce results for both identification and aularge subset, the first 2000 scans, of FRGC v2 dataset [13] generally increases with

the false accept rates. curve that shows the trade-off between the verification and (FAR) and with a receiver operating characteristic (ROC) the verification rate (VR) for a given false acceptance rate authentication where the performance is measured using Authentication Scenario : The first experiment involves

using a larger number of curves improves the authentication are higher for larger k. For k > 7, this trend is reversed. So that the verification rates using the geometric mean d_g are much better than those using the arithmetic mean d_a . So we rates pass through the nasal cavities. Moreover, we notice best verification rate is obtained using the first seven curves k of curves. For k < 7, the ROC curves using 1 - k curves the ROC curves for experiments involving different number choose this metric for further experiments. Figure 6 shows then it decreases. The curves which decrease the recognition the number of used curves until k = 7 curves are used and As shown in the Figure 5, the verification rate increases with and the geometric mean metric ; it is approximately 65.34%location of these curves on a nose are shown in the left. The puted using both the geometric and arithmetic means. The Figure 5 (right) shows a plot of VR at FAR = 0.1%, com-

> get worse. performance until the seventh curve and , after that, results

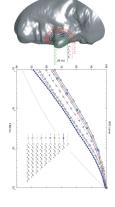


FIGURE 6. ROC curves using 1 to k curves

a rank-one recognition rate. In this experiment the gallery set consists of neutral faces of 209 subjects. Figure 7 shows is for identification for which the performance is quoted as Identification Scenario : The second type of experiment

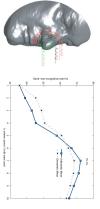


FIGURE 7. Rank one recognition rates using 1 to k curves

are not reliable and can be excluded from the analysis. cavities. Clearly, shapes of this region (made up of cavities) crease the recognition rates are curves 8,9 and 10 and, as we decreasing, for both the metrics. The later curves which dewith the number of curves, reaches a peak and then starts Second, we see that the recognition rate initially increases we obtain 76.1% using this metric using only seven curves. tained when using the arithmetic mean metric d_a . Actually, remarks. First, we notice that the best recognition rate is obthese curves on a nose in the left. We make the following tric and arithmetic mean in the right and the locations of the rank-one recognition rates obtained using both geomesee in the Figure 7 (left), these curves pass through the nasal

rification rates. However, the identification scenario costs a stable curves, we are able to increase identification and veshapes of nose regions. By carefully selecting the set of To summarize, our method allows us to compare the

> minutes. A hierarchical database organization can be per-formed in order to accelerate the identification process. We Tramework study an approach to cluster the gallery dataset using our shape in a dataset of 209 nasal surfaces, we need about 4 lot in terms of time computation. In our case, to retrieve a

4. Hierarchical Gallery Organization

a shape tree we need to be able to cluster similar shapes and that is the problem we study next. parisons are performed only at the nodes. To construct such in form of a hierarchical database, i.e. a tree, where the commade more efficient if we can organize the gallery elements compared to a set of gallery shapes. This comparison can be gion is to conduct biometric searches where query is often One of the main goals for studying shapes of nose re-

4.1. Clustering Algorithm

noted by C_1, C_2, \ldots riance [15]. Let a configuration C consists of clusters debetween its elements : cluster is replaced by a scaled sum of distances (squared) tion, called *pairwise clustering* [6], where the variance of a ted at every iteration. As a solution, one often uses a variacomputationally expensive, especially when they are upda- μ_i s of large shape clusters, and therefore their variances, is riances within clusters. However, the computation of means functions used for clustering, e.g the sum of traces of covain C_i s and n_i s be the sizes of C_i s. There are several cost such a way that they minimize total "within-cluster" vainto k clusters. A general approach is to form clusters in Consider the problem of clustering n noses (in $\mathcal{C}^{[0,\lambda_0]}$ C_k , and let μ_i s be the mean shapes

$$C) = \sum_{i=1}^{k} \frac{2}{n_i} \left(\sum_{N^a \in C_i} \sum_{b < a, N^b \in C_i} d(N^a, N^b)^2 \right).$$
(5)

0

transfer of N_j to cluster C_i is performed with probability : singleton, i.e. not the only element in its cluster, then the cluster C_i keeping all other clusters fixed. If N_j is not a the clustering cost when a shape N_j is re-assigned to the randomly and re-assign it to another cluster. Let $Q_j^{(i)}$ be are following. (1) Move a shape : Here we select a shape value of the resulting configuration. The two types of moves bability proportional to the negative exponential of the Qtwo kinds of moves. These moves are performed with prore-arrangement is performed in a stochastic fashion using reduce Q by re-arranging shapes amongst the clusters. The basic idea is to start with a configuration of k clusters and kov chain search process on the configuration space. The mean d_a . We will minimize the clustering cost using a Marargmin Q(C). Notice that the metric used is the arithmetic We seek configurations that minimize Q, i.e., C^*

> performed with probability : $P_S(T) = \frac{1}{\sum_{i=1}^{2} \exp(-Q^{(i)}/T)}$ fix the number of clusters at k. (2) Swap two shapes : Here $P_M(j, i; T) = \overline{\neg i}$ guration (after swapping), respectively. Then, swapping is original configuration (before swapping) and the new confi and swap them. Let $Q^{(1)}$ and $Q^{(2)}$ be the Q-values of the we select two shapes randomly from two different clusters If N_j is a singleton, then moving it is not allowed in order to plays a role similar to temperature in simulated annealing $\exp(-Q_j^{(i)}/T)$ $\sum_{i=1}^{k} \exp(-Q_j^{(i)}/T)$ $i = 1, 2, \dots, k$. Here T

by Algorithm 2. ficult to establish. The main steps of the algorithm is given local minima, the convergence to a global minimum is dif ling and the random nature of the search help in avoiding simulated annealing approach. Although simulated annea In order to seek global optimization, we have adopted a

Algorithm 2 Stochastic Clustering Algorithm

For n shapes and k clusters, initialize by randomly distributing n shapes among k clusters. Set a high initial temperature T.

1- Compute pairwise geodesic distances between all n shapes. This re-1)/2 geodesic computations.

2- With equal probabilities pick one of the two moves : – Move a shape : Ptck a shape N_j randomly. If it is not a singleton in its cluster, then compute $Q_j^{(i)}$ for all $i=1,2,\ldots,k$. Compute the

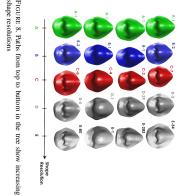
Swap two shapes : Select two clusters randomly, and select a shape probability $P_M(j, i; T)$ for all i = 1, ..., kcluster chosen according to the probability P_M ., k and re-assign N_j to a

from each. Compute the probability $P_S(T)$ and swap the two s according to that probability snape

4- We have used $\beta = 1.0001$. Update the temperature using T = T/β and return to Step 2.

never calculated in this clustering. Secondly, unlike k-mean clustering, the mean shapes are are computed, they are not computed again in the iterations It is important to note that once the pairwise distances

then to individuals as illustrated in Figure 8. ring can be applied repeatedly for organizing a large data-base of human noses into a hierarchy that allows efficient we see the shapes getting more particularized to groups and Figure 8.If we follow a path from top to bottom of the tree whith only one shape. We obtain so the final tree shown in peating this idea a few times, we reach the top of the tree These mean shapes form the level C of the hierarchy. Retogether and a Karcher mean is computed for each cluster obtain shapes at level D. These shapes are further clustered cher mean shapes (representative shapes) for each person to hierarchy, called level E in Figure 8. Then, we compute Kardistinct subjects. These noses form the bottom layer of the this idea, we consider 500 nose scans corresponding to 50 searches during identification process. As an illustration of The algorithms for computing Karcher mean and cluste-



shape resolutions

4.2. Hierarchical Shape Retrieval

red to the shapes of level B. As it is closer to shape B_1 , we example, the query nasal shape (at the top) is first compausing the hirarchical organization of the dataset. For Q1 for on a larger experimental set will be presented in the final is approximately 3-10 times faster than exhaustive comparisame person of the query. Notice that nasal shapes of each tually, the shape D_2 is the mean shape of nasal shapes of the proceed down the corresponding branch. There, the query the query best. Figure 9 illustrates 2 examples of retrieval and proceed down the branch that leads to the closest shape. at the top, compare the query with the shapes at each level dataset. In view of this structure, a natural way is to start of data to conduct biometric search in order to reduce comson as given by table 1 for 11 examples of queries. Results According to our tree, time computation for shape retrieval person at level E are represented by their mean at level D. D. In this case the query is matched to the shape D_2 . Acthe retrieval is given after comparison with shapes at level the closest one in this level to the query. The decision of proceeds down the branch of the shape C_2 as this shape is sible shapes and our goal is to find the shape that matches At any level of the tree, there is a number, say h, of pos needs a comparison of the query shape to the whole gallery putation time, especially in identification scenario, which The last match decides in which cluster the query belongs Once the tree is formed, one can use this representation

5. Conclusions

versions

3D nasal shapes for the use in partial human biometrics. In this paper, we have proposed a geometric analysis of

| incorrect | 16.5 s | 75 s | Q_{10}, Q_{11} |
|------------|---|------------------|-------------------|
| correct | 16.05 s | 75 s | $Q_i, i \in [19]$ |
| Result | Hierarchical | Exhaustive | Query |
| al results | TABLE 1. Average time computation and retrieval results | erage time compu | TABLE 1. Ave |

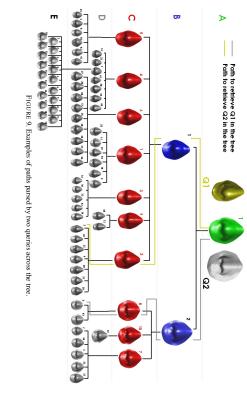
searches. hierarchical organization of noses gallery to allow efficient nasal shapes on a large dataset involving 2000 scans, and thentication and the identifiation biometric scenarios using monstrated these ideas in two application contexts : the auclustering to perform hierarchical clustering. We have deting geodesics, computing statistical means and stochastic curves. In particular, we have presented results for compuputed as the geodesic length between a set of their nasal of geodesic paths between arbitrary two nasal surfaces. The length of a geodesic between any two nasal surfaces is com-The main tool presented in this paper is the construction

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