

# Vision-based techniques for following paths with mobile robots

Andrea Cherubini

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### DIPARTIMENTO DI INFORMATICA E SISTEMISTICA

Doctoral Thesis in Systems Engineering ING-INF/04 XX Ciclo

# Vision-based techniques for following paths with mobile robots

Andrea Cherubini

Advisor Prof. Giuseppe Oriolo Coordinator Prof. Carlo Bruni

December 2007

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to my family

### Abstract

In this thesis, we focus on the use of robot vision sensors to solve the path following problem, which in recent years, has been a popular target for engaged researchers around the world. Initially, we shall present the working assumptions that we used, along with the relevant kinematic and sensor models of interest, and with the main characteristics of visual servoing. Then, we shall attempt to survey the research carried out in the field of vision-based path following. Following this, we shall present two schemes that we designed for reaching and following paths. These respectively involve nonholonomic robots and legged robots. Both schemes require only some visible path features, along with a coarse camera model, and, under certain conditions, may guarantee convergence even when the initial error is large. The first control scheme is designed to enable nonholonomic mobile robots with a fixed pinhole camera to reach and follow a continuous path on the ground. Two visual servoing controllers (position-based and image-based) have been designed. For both controllers, a Lyapunov-based stability analysis has been carried out. The performance of the two controllers is validated and compared by simulations and experiments on a car-like robot. The second control scheme is more application-oriented than the first and has been used in ASPICE, an assistive robotics project, to enable the autonomous navigation of a legged robot equipped with an actuated pinhole camera. The robot uses a position-based visual servoing controller to follow artificial paths on the ground, and travel to some required destinations. Apart from being a useful testing-ground for this path following scheme, the ASPICE project has also permitted the development of many other aspects in the field of assistive robotics. These shall be outlined at the end of the thesis.

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# Introduction

Mobile land robots require a high degree of autonomy in their operations; a requirement which calls for accurate and efficient position determination and verification in order to guarantee safe navigation in different environments. In many recent works, this has been done by processing information from the robot vision sensors [74]. In this thesis, we shall present the case for utilizing the robot vision sensors for solving the path following (PF) problem, which in recent years, has engaged numerous researchers around the world. In the PF task, the controller must stabilize to zero some *path error function*, indicating the position of the robot with respect to the path [16, 18]. The path to be followed is defined as a continuous curve on the ground. In some works, assumptions on the shape, curvature, and differential properties of the path have been introduced, for focusing on specific applications and control designs.

Much work dealing with the design of visual controllers for the tracking of reference paths has been carried out in the field of autonomous vehicle guidance [4]. In fact, some of the earliest Automated Guided Vehicles (AGVs) were line following mobile robots. They could follow a painted or embedded visual straight line on a floor or ceiling. Later, visual servoing techniques [8] (which were originally developed for manipulator arms with vision sensors mounted at their end-effector [23]) provided excellent results in the field of mobile robot visual navigation. Visual servoing systems are classified in two major categories: *position-based* control and *image-based* control. Position-based visual servoing techniques can be used whenever the visual navigation system relies on the geometry of the environment and on other metrical information. The feedback law is computed by reducing errors in estimated pose space. For instance, in the field of PF, many works address the problem by zeroing the lateral displacement and orientation error of the vehicle at a lookahead distance [49]. Alternative visual navigation systems use no explicit representation of the environment in which navigation takes place. In this case, image-based visual servoing techniques can be used to control the robot: an error signal measured directly in the image is mapped to actuator commands. The image-based approach reduces computational delay, eliminates the necessity for image interpretation, and errors due to camera modeling and calibration [7, 13].

In this thesis, we present two vision-based approaches for path following with mobile robots. The two approaches have respectively been designed and assessed on nonholonomic and on legged robots. In both cases, a pinhole camera is used. However, in the first approach, the camera is fixed, whereas in the second it is actuated. Both approaches require only some visible path features, along with a coarse camera model, and, under certain conditions, guarantee convergence even when the initial error is large.

The first approach is designed to enable nonholonomic mobile robots with a fixed pinhole camera to reach and follow a continuous path on the ground. In this regard, two controllers (position-based and image-based) have been designed. For both controllers, a Lyapunov-based stability analysis is carried out. The performance of the two controllers is validated and compared by simulations and experiments on a car-like robot equipped with a pinhole camera. To our knowledge, this is the first time that an extensive comparison between position-based and image-based visual servoing for nonholonomic mobile robot navigation is carried out.

The second approach is position-based and more application-oriented than the first approach. It has been used in ASPICE, an assistive robotics project, to enable the autonomous navigation of a legged robot in an indoor environment [10]. The robot uses a position-based visual servoing control scheme to follow artificial paths on the ground, and to travel to required targets in the environment. The paths are formed by straight white lines connected by black and white coded square crossings. The approach has been designed in relation to the ASPICE system requirements.

This thesis is organized as follows. In the first chapter we will present the working assumptions that we used for tackling the path following problem. The PF problem is defined, along with the relevant kinematic and sensor models. The main characteristics of visual servoing are also outlined. In the second chapter, we attempt to survey the research carried out in the field of vision-based path following. In Chapter 3, we present two path following (PF) control schemes which enable nonholonomic mobile robots with a fixed pinhole camera to reach and follow a continuous path on the ground. The design,

stability analysis and experimental validation of the two controllers are described. In the fourth chapter, we present the position-based visual path following controller that has been used in the ASPICE project. The image processing aspects and the motion controllers and experimental results of this work, are also presented. The ASPICE project has both provided a useful testbed for this path following scheme and also allowed the development of many other aspects in the field of assistive robotics. These numerous aspects are described in Chapter 5.

# Notations

The following notations will be used throughout this thesis.

$\mathcal{W}$	the robot <i>workspace</i> . It is modeled with the Euclidean space $\mathbb{R}^2$ .
$\mathcal{F}_{\mathcal{W}}$	the world reference frame, with origin W and axes $x', y', z'$ .
$\mathcal{R}$	the <i>robot</i> . It is the compact subset of $\mathcal{W}$ occupied by the robot.
r	the robot reference point. It is the point on the robot, with $\mathcal{F}_{\mathcal{W}}$
	coordinates $[x' y']^T$ , that should track the path.
$\theta$	the robot orientation in $\mathcal{F}_{\mathcal{W}}$ .
$\mathcal{F}_{\mathcal{R}}$	the robot reference frame, with origin $r$ and axes $x, y, z$ .
p	the <i>path</i> . It is represented by a continuous curve in the workspace $\mathcal{W}$ .
n	the number of robot generalized coordinates; in this work, $n = 3$ .
m	the number of control inputs applied to the robot; $m \leq n$ .
q	the robot configuration: $q = [x' y' \theta]^T$ .
u	the <i>control</i> applied to the robot.
d	the path desired reference point. It is the point with $\mathcal{F}_{\mathcal{W}}$ coordinates
	$[x'_d y'_d]^T$ that should be tracked by r.
$\theta_d$	the orientation of the path tangent at $d$ in $\mathcal{F}_{\mathcal{W}}$ .
$c_d$	the path curvature at $d$ .
$q_d$	the robot desired reference configuration: $q_d = [x'_d y'_d \theta_d]^T$ .
$\mathcal{F}_{\mathcal{P}}$	the path reference frame, with origin d and axes $x_d$ , $y_d$ , $z_d$ .
$e_t$	the tangential path error.
$e_n$	the normal path error.
$e_{\theta}$	the orientation path error.
C	the <i>principal projection center</i> of the visual sensor.

$\mathcal{F}_{\mathcal{C}}$	the camera reference frame, with origin C and axes $x_c$ , $y_c$ , $z_c$ .
Ι	the image center, or <i>principal point</i> .
$\mathcal{F}_\mathcal{I}$	the <i>image reference frame</i> , with origin $I$ and axes $X$ and $Y$ .
D	the projection of $d$ on the image plane, with $\mathcal{F}_{\mathcal{I}}$ coordinates $[X Y]^T$ .
P	the projection of the path $p$ on the image plane.
f	the <i>focal length</i> in the perspective camera model.
$(X_I Y_I)$	the <i>principal point error</i> in the perspective camera model.
$(l_X \ l_Y)$	the <i>metric size of the pixel</i> in the perspective camera model.

### Chapter 1

### Working assumptions

The object of this chapter is to present the assumptions used in this thesis. Firstly, we will formally introduce the path following problem for mobile ground robots. Afterwards, the kinematic models of the two classes of robots (i.e., wheeled and legged) that have been used in the experimental part of the thesis are presented. Regarding wheeled robots, the main issues of nonholonomic motion control are discussed, and the two most common models (unicycle and car-like) are outlined. As to legged robots, the gait control algorithm (kinematic parameterized trot) which has been utilized in the thesis is explained in the second section. In the third section, we present the general visual sensor model (the central catadioptric model) which applies to all the systems that will be cited in the survey of Chapter 2, as well as to the systems used in our work. Finally, we recall the main concepts of visual servo control i.e., robot motion control using computer vision data in the servo loop.

#### 1.1 The path following problem

Let us consider a ground mobile robot  $\mathcal{R}$ . We assume that the workspace where the robot moves is planar (i.e,  $\mathcal{W} = \mathbb{R}^2$ ) and we define  $\mathcal{F}_{\mathcal{W}}(W, x', y', z')$  the world frame (shown in Fig. 1.1). The *path* p to be followed is represented by a continuous curve in the workspace  $\mathcal{W}$ . In some cases, a *following direction* can be associated to the path. We assume that the robot has a symmetric plane (the *sagittal* plane) orthogonal to  $\mathcal{W}$ , and is forward oriented. We name r the *robot reference point*, i.e., the point on the robot sagittal plane that should track the path, and  $\mathcal{F}_{\mathcal{R}}(r, x, y, z)$  the robot



Figure 1.1: Path following relevant variables.

frame. The y axis is the intersection line between the sagittal plane and  $\mathcal{W}$ , oriented in the robot forward orientation, and the x axis pertains to  $\mathcal{W}$  and is oriented to the right of the robot. The robot state coordinates (i.e., the robot generalized coordinates) are  $q(\varepsilon) = [x'(\varepsilon) y'(\varepsilon) \theta(\varepsilon)]^T$ , where  $\varepsilon \in \mathbb{R}$  is a parameter with infinite domain,  $[x'(\varepsilon) y'(\varepsilon)]^T$  represent the Cartesian position of r in  $\mathcal{F}_{\mathcal{W}}$ , and  $\theta(\varepsilon) \in [-\pi, +\pi]$  is the orientation of the robot frame y axis with respect to the world frame x' axis (positive counterclockwise). Thus, the dimension of the robot configuration space is n = 3.

Recalling [18], the objective of PF is to drive the error  $e(\varepsilon) = q(\varepsilon) - q_d(\varepsilon) = [e_{x'}(\varepsilon) e_{y'}(\varepsilon) e_{\theta}(\varepsilon)]^T$  to a desired error  $\hat{e}(\varepsilon)$ . Usually,  $\hat{e}(\varepsilon)$  is set to zero. The vector  $q_d(\varepsilon) = [x'_d(\varepsilon) y'_d(\varepsilon) \theta_d(\varepsilon)]^T$  defines a *desired reference configuration*, such that the point  $d(\varepsilon) \in \mathcal{W}$  of coordinates  $[x'_d(\varepsilon) y'_d(\varepsilon)]^T$  belongs to p, and  $\theta_d(\varepsilon)$  is the desired robot orientation. If the tangent of p at  $d(\varepsilon)$  exists, and the path has a following direction (as in Fig. 1.1),  $\theta_d(\varepsilon)$  is the orientation of the tangent in  $\mathcal{F}_{\mathcal{W}}$  considering the direction. Otherwise,  $\theta_d(\varepsilon)$  is defined by the PF specifications. If it exists, the path curvature at d is noted  $c_d$ . If there exist some constraints in the robot model (e.g., nonholonomic constraints), the path must be feasible with respect to such constraints, i.e.  $q_d(\varepsilon)$  must attend to these constraints. Moreover, we note  $u \in \mathbb{R}^m$  the applied control, which usually corresponds to the robot velocities;  $m \leq n$  is the number of control inputs. The reference path cannot contain points where the tracking control

 $u_d \equiv 0.$ 

The PF task is often formalized by projecting the  $\mathcal{F}_{\mathcal{W}}$  errors  $[e_{x'}(\varepsilon) e_{y'}(\varepsilon) e_{\theta}(\varepsilon)]^T$  to the path frame  $\mathcal{F}_{\mathcal{P}}(d, x_d, y_d, z_d)$ , shown in Fig. 3.1(a). Frame  $\mathcal{F}_{\mathcal{P}}$  is linked to the path at d, with  $z_d$  parallel to z,  $y_d$  coincident with the path tangent at d in the following direction, and  $x_d$  completing the right-handed frame. The path error in  $\mathcal{F}_{\mathcal{P}}$  consists of the tangent error  $e_t$  (i.e., the error projection on  $y_d$ ), the normal error  $e_n$  (i.e., the error projection on  $x_d$ ), and the orientation error  $e_{\theta}$ , i.e.:

$$e_{t} = e_{x'} \cos \theta_{d} + e_{y'} \sin \theta_{d}$$

$$e_{n} = e_{x'} \sin \theta_{d} - e_{y'} \cos \theta_{d}$$

$$e_{\theta} = \theta - \theta_{d}$$
(1.1)

With this formalism, the PF task consists of driving error  $[e_t(\varepsilon) \ e_n(\varepsilon) \ e_{\theta}(\varepsilon)]^T$  to a desired error  $[\hat{e}_t \ \hat{e}_n \ \hat{e}_{\theta}]^T$ . In the remainder of the thesis the desired error  $[\hat{e}_t \ \hat{e}_n \ \hat{e}_{\theta}]^T$  is set to  $[0 \ 0 \ 0]^T$ , unless it is otherwise specified.

In opposition to the trajectory tracking problem, where the desired trajectory evolution is determined by a rigid law like  $\varepsilon = \varepsilon(t)$  (i.e., parameter  $\varepsilon$  is associated to the time t), in PF we can choose the relationship that defines the desired reference configuration  $q_d(\varepsilon)$  that the robot should track. We call such relationship path following constraint. The path following constraint eliminates one of the three error coordinates. Details regarding the choice of the projecting function used to define  $q_d(\varepsilon)$  in this work will be given later. In most works, the path following constraint is chosen by defining d as the normal projection of r on p, i.e., by choosing d such that  $e_t = \text{const} = 0$ .

Finally, in PF, the robot should move at all times independently from  $q_d(\varepsilon)$  (clearly, a control law must concurrently ensure convergence to the path). Thus, a motion must be imposed to the robot to guarantee that it moves or progresses. This is the *motion* exigency condition defined in [18].

#### 1.2 Kinematic model and motion control

In this section, we will focus on the kinematic model and motion control of the two classes of robots that have been used in the experimental part of this thesis: wheeled and legged robots.

#### 1.2.1 Wheeled robots

#### Motivations

Wheels are ubiquitous in human designed systems. As might be expected, the vast majority of robots move on wheels. Wheeled mobile robots (WMRs) are increasingly present in industrial and service robotics, particularly when flexible motion capabilities are required on reasonably smooth grounds and surfaces. Several mobility configurations (wheel number, type, location and actuation, single-body or multi-body vehicle structure) can be found in the applications. The most common configurations for single-body robots are differential drive and synchro drive (both kinematically equivalent to a unicycle), tricycle or car-like drive, and omnidirectional steering [53]. Numerous wheeled robots were developed at the NASA Jet Propulsion Laboratory (JPL) [3] in the 1970s, including various rovers for planetary exploration. These developments culminated in the landing of the Sojourner robot on Mars in 2001. Today the most common research robots are wheeled.

Beyond their relevance in applications, the problem of autonomous motion planning and control of WMRs has attracted the interest of researchers in view of its theoretical challenges. In particular, these systems are a typical example of nonholonomic mechanisms due to the perfect rolling constraints on the wheel motion (no longitudinal or lateral slipping).

#### The nonholonomic constraint

The notion of nonholonomy (borrowed from Mechanics) appears in literature on robot motion planning because of the problem of car parking which the pioneering mobile robot navigation systems had not managed to solve [51]. Nonholonomic systems are characterized by constraint equations involving the time derivatives of the system configuration variables. These equations are non integrable; they typically arise when the system has less controls than configuration variables (m < n). For instance, a car-like robot has m = 2 controls (linear and angular velocities) while it moves in a configuration space of dimension n = 3. As a consequence, a path in the configuration space does not necessarily correspond to a feasible path for the system. This explains why the purely geometrical techniques developed in motion planning for holonomic systems do not apply directly to nonholonomic systems. While the constraints due to the obstacles are expressed directly in the manifold of configurations, nonholonomic constraints deal with the tangent space of such manifold. In the presence of a link between the robot parameters and their derivatives, the first question to be addressed is: does such a link reduce the accessible configuration space? This question may be answered by studying the structure of the distribution spanned by the Lie algebra of system controls. Thus, even in the absence of obstacles, planning nonholonomic motions is not an easy task. Today there is no general algorithm which enables one to plan motions for nonholonomic systems, in a way that guarantees that the system reaches exactly a destination. The only existing results are for approximate methods (which guarantee only that the system reaches a neighborhood of the goal) or exact methods for special classes of systems. Fortunately, these classes cover almost all the existing mobile robots.

In the absence of workspace obstacles, the basic motion tasks assigned to a WMR may be reduced to moving between two robot postures and to the following of a given trajectory. From a control viewpoint, the peculiar nature of nonholonomic kinematics makes the second problem easier than the first. Indeed, it is a well known fact that feedback stabilization at a given posture cannot be achieved via smooth time-invariant control [5]. This indicates that the problem is truly nonlinear; linear control is ineffective, even locally, and innovative design techniques are required.

Here, we will briefly outline the theory of Pfaffian nonholonomic systems. Further details can be found in [51] and [53]. Recalling (Sect. 1.1) that q denotes the *n*-vector of robot generalized coordinates, Pfaffian nonholonomic systems are characterized by the presence of n - m non-integrable differential constraints on the generalized velocities of the form:

$$A(q)\dot{q} = 0 \tag{1.2}$$

with A(q) matrix of size  $(n-m) \times n$ . For a WMR, these Pfaffian constraints arise from the rolling without slipping condition for the wheels. All feasible instantaneous motions can then be generated as:

$$\dot{q} = G\left(q\right)u\tag{1.3}$$

for some control input:  $u(t) \in \mathbb{R}^m$ . The columns  $g_i$ , i = 1, ..., m of the  $n \times m$ matrix G(q) are chosen so as to span the null-space of matrix A(q). Different choices are possible for G, according to the physical interpretation that may be given to the



Figure 1.2: Unicycle model relevant variables.

inputs  $u_1, \ldots, u_m$ . Equation 1.3, which is called the (first-order) kinematic model of the system, represents a driftless nonlinear system. We will now present the two kinematic modeling examples most commonly used in robotics: the unicycle model and the car-like model.

#### The unicycle model

A classic locomotion system for a mobile robot is constituted by two parallel driving wheels, the acceleration of each being controlled by an independent motor. The linear accelerations are noted:  $a_r$  and  $a_l$  respectively for the right and left wheel. The stability of the platform is ensured by castors. We assume that the two wheels roll without slipping. The robot reference point r is the midpoint of the two wheels; its coordinates, with respect to  $\mathcal{F}_W$  are denoted by (x', y'). The main direction of the vehicle is the direction  $\theta$  of the driving wheels. This kinematic model is equivalent to that of the unicycle, which corresponds to a single upright wheel rolling on the plane (see Fig. 1.2). With w designating the distance between the driving wheels,  $v_r$  and  $v_l$  the linear velocities respectively of the right and left wheel, the kinematic model is:

$$\begin{bmatrix} \dot{x'} \\ \dot{y'} \\ \dot{\theta} \\ \dot{v_r} \\ \dot{v_l} \end{bmatrix} = \begin{bmatrix} \frac{v_r + v_l}{2} \cos \theta \\ \frac{v_r + v_l}{2} \sin \theta \\ \frac{v_r - v_l}{w} \\ 0 \\ 0 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \\ 0 \end{bmatrix} a_r + \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 1 \end{bmatrix} a_l$$
(1.4)

Clearly,  $a_r$ ,  $a_l$ ,  $v_r$  and  $v_l$  are bounded; these bounds appear at this level as 'obstacles' to avoid in the 5-dimensional manifold. By setting:  $u_1 = \frac{v_r + v_l}{2}$  and  $u_2 = \frac{v_r - v_l}{l}$  (respectively, the linear velocity of the wheel and its angular velocity around the vertical axis), we get the kinematic model, which is expressed as the following 3-dimensional system:

$$\begin{bmatrix} \dot{x'} \\ \dot{y'} \\ \dot{\theta} \end{bmatrix} = g_1(q) u_1 + g_2(q) u_2 = \begin{bmatrix} \cos \theta \\ \sin \theta \\ 0 \end{bmatrix} u_1 + \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} u_2$$
(1.5)

where the generalized coordinates are  $q = [x' y' \theta]^T \in \mathbb{R}^2 \times SO^1$  (n = 3), and  $u_1$  and  $u_2$  are the control inputs (m = 2). The bounds on  $v_l$  and  $v_r$  induce bounds  $u_{1,max}$  and  $u_{2,max}$  on the new controls  $u_1$  and  $u_2$ . System (1.5) is symmetric without drift, and displays a number of structural control properties, most of which actually hold for the general nonholonomic kinematic model (1.3).

The constraint that the wheel cannot slip in the lateral direction is given in the form (1.2) as:

$$A(q)\dot{q} = [\sin\theta - \cos\theta \, 0]\dot{q} = \dot{x'}\sin\theta - \dot{y'}\cos\theta = 0$$

As expected,  $g_1$  and  $g_2$  span the null-space of matrix A(q).

#### The car-like model

From the driver's point of view, a car has two controls: the accelerator and the steering wheel. Let us consider a typical car-like model, where the front wheels can be steered, while the orientation of the rear wheels is fixed. The reference point r with coordinates (x', y') is the midpoint of the rear wheels, and  $\theta$  indicates, as usual, the orientation of the robot sagittal plane with respect to the x' axis. We denote L the distance between rear and front axles, and  $\phi$  the steering angle. A mechanical constraint imposes  $|\phi| \leq \phi_M$ 



Figure 1.3: Car-like model relevant variables.

and, consequently, a minimum turning radius. For simplicity, we assume that the two wheels on each axis (front and rear) collapse into a single wheel located at the midpoint of the axis (*bicycle model*). The generalized coordinates are  $q = [x' y' \theta \phi]^T \in \mathbb{R}^2 \times SO^1 \times [-\phi_M, \phi_M]$  (n = 4). These variables are shown in Fig. 1.3.

The system is subject to two nonholonomic constraints, one for each wheel:

$$\dot{x}' \sin \theta - \dot{y}' \cos \theta = 0$$
$$\dot{x}'_f \sin (\theta + \phi) - \dot{y}'_f \cos (\theta + \phi) = 0$$

 $(x'_f, y'_f)$  being the position of the front-axle midpoint. By using the rigid-body constraint:

$$x'_f = x' + L\cos\theta$$
$$y'_f = y' + L\sin\theta$$

the second kinematic constraint becomes:

$$\dot{x'}\sin\left(\theta+\phi\right)-\dot{y'}\cos\left(\theta+\phi\right)-\dot{\theta}L\cos\phi=0$$

Hence, the constraint matrix is:

$$A(q) = \begin{bmatrix} \sin \theta & -\cos \theta & 0 & 0\\ \sin (\theta + \phi) & -\cos (\theta + \phi) & -L\cos \phi & 0 \end{bmatrix}$$

and has constant rank 2. Its null-space is two-dimensional, and all the admissible generalized velocities are obtained as:

$$\begin{bmatrix} \dot{x'} \\ \dot{y'} \\ \dot{\theta} \\ \dot{\phi} \end{bmatrix} = \begin{bmatrix} \cos\theta\cos\phi \\ \sin\theta\cos\phi \\ \frac{\sin\phi}{L} \\ 0 \end{bmatrix} u_1 + \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix} u_2$$
(1.6)

Since the front wheel can be steered, we set  $u_2 = \dot{\phi}$ , ( $\dot{\phi}$  is the steering velocity input). The expression of  $u_1$  depends on the location of the driving input. If the car has front-wheel driving, i.e., front wheel velocity as control input  $u_1$ , the control system becomes:

$$\begin{bmatrix} \dot{x'} \\ \dot{y'} \\ \dot{\theta} \\ \dot{\phi} \end{bmatrix} = \begin{bmatrix} \cos\theta\cos\phi \\ \sin\theta\cos\phi \\ \frac{\sin\phi}{L} \\ 0 \end{bmatrix} u_1 + \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix} u_2$$
(1.7)

The control inputs  $u_1$  and  $u_2$  are respectively the front wheel velocity and the steering velocity.

If the car has rear-wheel driving, i.e., rear wheel velocity as control input  $u_1$ , we have:

$$\begin{bmatrix} \dot{x'} \\ \dot{y'} \\ \dot{\theta} \\ \dot{\phi} \end{bmatrix} = \begin{bmatrix} \cos \theta \\ \sin \theta \\ \frac{\tan \phi}{L} \\ 0 \end{bmatrix} u_1 + \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix} u_2$$
(1.8)

The control inputs  $u_1$  and  $u_2$  are respectively the rear wheel velocity and the steering velocity. Note that in (1.8), there is a control singularity at  $\phi = \pm \frac{\pi}{2}$ , where the first vector field blows out. This corresponds to the rear-wheel drive car becoming jammed when the front wheel is normal to the longitudinal axis of the car body. Instead, this singularity does not occur for the front-wheel drive car (1.7), which in the same situation may still pivot about its rear-axle midpoint.

By setting  $u_2 = \frac{u_1 \tan \phi}{L}$  in (1.8), we get a 3-dimensional control system:

$$\begin{bmatrix} \dot{x'} \\ \dot{y'} \\ \dot{\theta} \end{bmatrix} = \begin{bmatrix} \cos \theta \\ \sin \theta \\ 0 \end{bmatrix} u_1 + \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} u_2$$
(1.9)

The control inputs  $u_1$  and  $u_2$  are respectively the rear wheel velocity and the robot angular velocity with respect to r. This representation of the car-like model is consistent with the definitions of Sect. 1.1, since the robot generalized coordinates become:  $q = [x' y' \theta]^T \in \mathbb{R}^2 \times SO^1$  (n = 4). Equation (1.9) can also represent the front-wheel driving by using  $u_1 \cos \phi$  as first control input, and  $\frac{u_1 \sin \phi}{L}$  as second control input. System (1.9) is identical to the unicycle kinematic model (1.5). By construction the values of  $u_1$ and  $u_2$  are bounded. The main difference lies on the admissible control domains, since in (1.9) the constraints on  $u_1$  and  $u_2$  are no longer independent. Moreover, the instantaneous applicable curvature of the car must be smaller than:

$$c_M = \frac{\tan \phi_M}{L} \tag{1.10}$$

In practice, the control inputs in (1.9) must verify:

$$\left. \frac{u_2}{u_1} \right| < c_M \tag{1.11}$$

There is no such bound for the unicycle instantaneous applicable curvature.

#### 1.2.2 Legged robots

#### Motivations

Walking on legs is particularly significant as a mode of locomotion in robotics. Beginning with the automatons built in the nineteenth century, people have been fascinated by legged machines, especially when they display some autonomy. Aside from the sheer thrill of creating robots that actually run, there are two serious reasons for exploring the use of legs for locomotion.

One reason is mobility: there is a need for vehicles that can travel in difficult terrains where wheeled vehicles would not be able to get. Wheels excel on prepared surfaces such as rails and roads, but perform poorly wherever the terrain is soft or uneven. Because of these limitations, only about half of the earth's landmass is accessible to existing wheeled and tracked vehicles, whereas a much greater area can be reached by animals on foot [65]. Legs provide better mobility in rough terrain since they can use isolated footholds that optimize support and traction, whereas a wheel requires a continuous path of support. As a consequence, a legged robot can choose among the best footholds in the reachable terrain; a wheeled vehicle must plunge into the worst terrain. Another advantage of legs is that they provide an active suspension that decouples the body trajectory from the path trajectory. The payload is free to travel smoothly despite pronounced variations in the terrain. A legged system can also step over obstacles. In principle, the performance of legged vehicles can, to a great extent, be independent of the detailed roughness of the ground.

Another reason for exploring legged machines is to gain a better understanding of human and animal locomotion. Despite the skill we apply in using our own legs for locomotion, we are still at a primitive stage in understanding the control principles that underlie walking and running. The concrete theories and algorithms developed to design legged robots can guide biological research by suggesting specific models for experimental testing and verification. This sort of interdisciplinary approach is already becoming popular in other areas where biology and robotics have a common ground, such as vision, speech, and manipulation.

In this work, we shall focus uniquely on robots with  $N_l \ge 4$  legs. In the remainder of this section, we summarize some basic principles of legged locomotion, review some works in the area of legged locomotion, and present the locomotion control algorithm (kinematic parameterized trot) which has been utilized in the thesis.

#### Motion control

From a kinematic viewpoint, legged robots can be considered omnidirectional, i.e., m = 3 control inputs can be independently specified. Usually, these control inputs are the absolute velocities applied in the robot reference point r: forward  $u_1$  in the y axis direction, lateral  $u_2$  in the x axis direction, and angular  $u_3$  around the z axis.

Stable walking requires the generation of systematic periodic sequences of leg movements at various speeds of progression [3]. At slow velocities, stable walking is characterized by static stability: the center of mass of the body remains within the polygon of support formed by the legs in contact with the ground. During motion, the support forces of the legs, momentum and inertial forces are summed to produce dynamic stability. In both humans and animals, each leg alternates between stance (the time its end point is in contact with the ground), and swing (the time it spends in forward motion). To change speed, animals exhibit a variety of gaits. It now appears that the switch from one gait pattern to another occurs, at least in part, by means of mechanisms that attempt to keep the muscular forces and joint loads in the leg within particular limits.

In practice, the major task in enabling a legged robot to walk is foot trajectory generation. This can be based either on the dynamic or on the kinematic model of the robot. A short overview of some approaches used to generate stable legged gaits is presented in the next paragraph. Afterwards, we focus on the approach used in this thesis.

#### Related work

Various approaches for generating stable walking have been explored in literature.

In [61], a graph search method is proposed to generate the gait for a quadruped robot. To determine if a node in the graph is promising or not, each node is endowed with an evaluating function that incorporates the robot configuration, the distance the robot traveled, and the stability margin of a particular configuration. The search method exhibits promising features under adverse terrain conditions. The generated gait is: periodic when the terrain is flat, without obstacles, and free in the presence of obstacles.

Goodwine and Burdick [32] present a general trajectory generation scheme for legged robots. The scheme is based on an extension of a nonlinear trajectory generation algorithm for smooth systems (e.g., wheeled robots) to the legged case, where the relevant mechanics are not smooth. The extension utilizes a stratification model of the legged robot configuration spaces. Experiments indicate that the approach is simple to apply, independently from the number of legs.

Other researchers have successfully applied machine learning techniques for generating stable legged gaits. Krasny and Orin have used an evolutionary algorithm to generate an energy-efficient, natural, and unconstrained gallop for a quadrupedal robot with articulated legs, asymmetric mass distribution, and compliant legs [50]. In [75], a distributed neural architecture for the general control of robots has been applied for walking gait generation on a Sony AIBO robot. Genetic algorithms have been used to An important testbed for developing and improving motion control schemes for legged robots has been the annual RoboCup Four-Legged league<sup>1</sup>. RoboCup is "an attempt to promote AI and robotics research by providing a common task for evaluation of various theories, algorithms, and agent architectures"; the ultimate goal is, "to build a team of robot soccer players, which can beat a human World Cup champion team" [47]. The Robocup Four-Legged League prescribes the use of a standard robot platform: Sony AIBO. No hardware changes are permitted. In particular, since speed is a major key to winning robot soccer games, in the past years, the Robocup Four-Legged League has strongly fostered research in the field of legged motion control.

#### The kinematic parameterized trot walk approach

Here, we will illustrate the walking gait control scheme implemented in this thesis for following paths with a legged robot. The scheme is inspired by the parameterized walk approach developed by Hengst and others [37], which is widely used in the legged robot community. In particular, we will hereby describe the version implemented on Sony AIBO four-legged robots in [24], which inspired our control scheme. The algorithm can be easily extended for gait generation on other platforms, including robots with more than four legs  $(N_l > 4)$ . The approach presented is based on the robot kinematic model, i.e. dynamic effects are not taken into account. This choice is appropriate whenever a complete dynamic model for the robot is unavailable, or whenever the on-board resources are not sufficient for the computation of a dynamic controller (e.g. if the resources are shared with other processes, such as image processing). Since the robot is kinematically omnidirectional on the plane, the robot leg joint angles must be generated in order to let the robot walk with absolute speed applied in r:  $u = [u_1 \ u_2 \ u_3]^T$ . The kinematic parameterized trot walk algorithm consists of two phases. In a first phase, for a given u, the time trajectories of the robot feet in  $\mathcal{F}_{\mathcal{R}}$  are derived. In practice, we shall show that u imposes some constraints on these trajectories, without univocally defining them. In a second phase, the robot leg joint angles enabling each foot to track the time trajectories (derived in the first phase) are derived and used to control the robot motors.

<sup>&</sup>lt;sup>1</sup>www.tzi.de/4legged



Figure 1.4: Foot loci during kinematic parameterized trot walk: the feet are indicated in blue and the loci in red during stance, and in orange during swing.

Consider a robot with  $N_l$  legs noted  $l_1 \dots l_{N,l}$  linked to the robot body. The leg end points (feet) are noted  $f_i$ , with  $i = 1 \dots N_l$ , and shown in blue in Fig. 1.4. A trot gait is used. Each gait step is formed by two phases of the same duration  $\tau$ . During each phase, one half of the legs is in stance on the ground, and the other half is swinging in the air. The legs that were swinging in the previous phase are in stance in the current phase, and viceversa. In practice, during a step, each foot  $f_i$  tracks a 3-D time trajectory in the robot frame  $\mathcal{F}_{\mathcal{R}}$ , named foot locus. Each foot locus has a stance portion (stance locus, red in Fig. 1.4) and a swing portion (swing locus, orange in the figure). A wide set of parameters, noted with vector  $\Upsilon$ , can be tuned independently from u to determine the shape (rectangular in Fig. 1.4) and other characteristics of the foot loci. These parameters allow implementation of completely different walks. Some versions of the kinematic parameterized trot algorithm can interpolate between several provided sets to generate an optimal parameter set  $\Upsilon$  for each u (see [20]). In other versions of the algorithm, since hand tuning the set  $\Upsilon$  is not feasible, machine learning approaches have been used to optimize  $\Upsilon$  for each u (see [68] and [9]). However, there are also some characteristics of the foot loci which are univocally defined by the desired control input u, and the step duration  $\tau$ .

In fact, the absolute robot speed u is generated by the stance legs, which 'push' the robot with respect to the ground. We design as stance loci, straight segments, and fix constant stance feet velocities relative to the robot body, which we note:  $u_{f,i}$  for each foot  $f_i$ . Then, the length and direction of the stance loci can be univocally derived from u and  $\tau$  by applying the rigid body kinematic theory. Firstly, note that every desired motion u results in turning around an Instantaneous Center of Rotation (degenerate for pure translations), noted  $\Omega$  in Fig. 1.4, left. Let us consider the case of pure translations (i.e,  $u_3 \equiv 0$ ):  $u_{f,i}$  for each stance foot must be -u, and the direction of all stance loci must be identical to that of u. On the other hand, for  $u_3 \neq 0$ , the direction of each stance locus is orthogonal to segment  $f_i\Omega$ . Moreover, for  $u_3 \neq 0$ ,  $u_{f,i}$  for each stance foot must be proportional to the length of segment  $f_i\Omega$ , and the application of all stance velocities  $u_{f,i}$  in R must be -u. By imposing these two conditions, all stance foot velocities  $u_{f,i}$  can be calculated. In both cases ( $u_3 \equiv 0$  and  $u_3 \neq 0$ ), since the stance feet velocities are constant, the length of each stance locus is  $|| u_{f,i} || \tau$ .

In summary, during the first phase of the algorithm, the 3-D time trajectories of each foot in the robot frame  $\mathcal{F}_{\mathcal{R}}$  are derived from  $u, \tau$ , and  $\Upsilon$ . Once the desired foot loci are calculated, it is necessary to calculate the required leg joint angles to reach the desired foot position on the locus at each time step. This is done in the second phase of the algorithm. The joint angles necessary to track the desired foot position are calculated by solving the inverse kinematics problem at each time step.

In general, the inverse kinematics problem is a set of non-linear equations, which can only be solved numerically. Instead, we shall show that for the Sony AIBO kinematics, it is possible to derive an analytical closed form solution. Firstly, a solution to the forward kinematics problem is given. This will be used for solving the inverse kinematics problem. The forward kinematics problem consists of calculating the foot position resulting from a given set of joint angles. Consider the fore left leg model<sup>2</sup> shown in Fig. 1.5. With reference to the figure, we define  $\mathcal{F}_{\mathcal{S}}(S, x_s, y_s, z_s)$  the shoulder frame (also shown in Fig. 1.4),  $\delta_u$  and  $\delta_l$  the lengths of the upper and lower limb, and  $\varrho_1$ ,  $\varrho_2$ , and  $\varrho_3$  the joint angles. The target foot position that should be tracked (with  $\mathcal{F}_{\mathcal{S}}$  coordinates  $[x_s, y_s, z_s]^T$ ), is determined by using the following coordinate transformations:

- 1. clockwise rotation about the  $y_s$  axis by joint angle  $\rho_1$
- 2. counterclockwise rotation about the  $x_s$  axis by joint angle  $\rho_2$
- 3. translation along the negative  $z_s$  axis by upper limb length  $\delta_u$

<sup>&</sup>lt;sup>2</sup>Using symmetrical considerations, the following calculations can be extended to all four legs.



Figure 1.5: Fore left leg design: side view (left), and front view (right).

- 4. clockwise rotation about the  $y_s$  axis by joint angle  $\varrho_3$
- 5. translation along the negative  $z_s$  axis by lower limb length  $\delta_l$

In homogeneous coordinates, by using the Denavit and Hartenberg method [35], this transformation can be described as a concatenation of transformation matrices:

$$\begin{bmatrix} x_{s} \\ y_{s} \\ z_{s} \\ 1 \end{bmatrix} = R_{y}(-\varrho_{1})R_{x}(\varrho_{2})T_{-\delta_{u}}R_{y}(-\varrho_{3})T_{-\delta_{l}}\begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix}$$
(1.12)

where  $R_y(\rho_i)$  is the rotation matrix of angle  $\rho_i$  around the  $y_s$  axis, and  $T_{\delta}$  the translation matrix associated to vector  $[0 \ 0 \ \delta]^T$ . The solution of the forward kinematics problem can be derived from (1.12):

$$\begin{cases} x_s = \delta_l \cos \varrho_1 \sin \varrho_3 + \delta_l \sin \varrho_1 \cos \varrho_2 \cos \varrho_3 + \delta_u \sin \varrho_1 \cos \varrho_2 \\ y_s = \delta_u \sin \varrho_2 + \delta_l \sin \varrho_2 \cos \varrho_3 \\ z_s = \delta_l \sin \varrho_1 \sin \varrho_3 - \delta_l \cos \varrho_1 \cos \varrho_2 \cos \varrho_3 - \delta_u \cos \varrho_1 \cos \varrho_2 \end{cases}$$
(1.13)

To solve the inverse kinematics problem, the knee joint angle  $\rho_3$  is initially calculated. Since the knee joint position determines how far the leg is stretched,  $\rho_3$  can be calculated from the distance of the target position  $(x_s, y_s, z_s)$  to the shoulder joint. According to the law of cosine (see Fig. 1.4):

$$|\varrho_3| = \arccos \frac{x_s^2 + y_s^2 + z_s^2 - \delta_u^2 - \delta_l^2}{2\delta_u \delta_l}$$

There exist two solutions, since there are two possible knee positions to reach the target position  $(x_s, y_s, z_s)$ . Here, the positive value of  $\rho_3$  is chosen due to the larger freedom of movement for positive  $\rho_3$ .

Plugging the result for  $\rho_3$  into the forward kinematics solution (1.13) allows determining  $\rho_2$  easily. According to equation (1.13):

$$y_s = \delta_u \sin \varrho_2 + \delta_l \sin \varrho_2 \cos \varrho_3$$

Consequently:

$$\varrho_2 = \arcsin\left(\frac{y_s}{\delta_l \cos \varrho_3 + \delta_u}\right)$$

Since  $|\varrho_2| < 90^\circ$ , the determination of  $\varrho_2$  via arc sine is satisfactory.

Finally the joint angle  $\rho_1$  can be calculated. According to equation (1.13):

$$x_s = \delta_l \cos \varrho_1 \sin \varrho_3 + \delta_l \sin \varrho_1 \cos \varrho_2 \cos \varrho_3 + \delta_u \sin \varrho_1 \cos \varrho_2$$

which can be transformed to:

$$x_s = \delta^* \cos\left(\varrho_1 + \varrho^*\right)$$

with:

$$\varrho^* = \arctan \frac{\delta_l \sin \varrho_3}{-\cos \varrho_2 (\delta_l \cos \varrho_3 + \delta_u)}$$
$$\delta^* = \frac{-\cos \varrho_2 (\delta_l \cos \varrho_3 + \delta_u)}{\sin \varrho^*}$$

Hence:

$$|\varrho_1 + \varrho^*| = \arccos\left(\frac{x_s}{\delta^*}\right)$$

The sign of  $\rho_1 + \rho^*$  can be obtained by checking the  $z_s$  component in (1.13):

 $z_s = \delta_l \left( \sin \varrho_1 \sin \varrho_3 - \cos \varrho_1 \cos \varrho_2 \cos \varrho_3 \right) - \delta_u \cos \varrho_1 \cos \varrho_2 = \delta^* \sin \left( \varrho_1 + \varrho^* \right)$ 

Since  $\delta^* > 0$ ,  $\rho_1 + \rho^*$  has the same sign as  $z_s$ . Hence the last joint value  $\rho_1$  can be computed.

#### 1.3 Central catadioptric vision sensor model

#### 1.3.1 Definitions

Here, we present the fundamental mathematical models of optical cameras and their parameters. Part of this section is taken from [76]. We concentrate on illuminance images, i.e. images measuring the amount of light impinging on a photosensitive device. It is important to stress that any digital image, irrespective of its type, is a 2-D array (matrix) of numbers. Hence, any information contained in the images (e.g. shape, measurements, or object identity) must ultimately be extracted from 2-D numerical arrays, in which it is encoded. A simple look at any ordinary photograph suggests the variety of physical parameters playing a role in image formation. Here is an incomplete list:

- optical parameters of the lens (lens type, focal length, field of view, angular apertures);
- photometric parameters appearing in the model of the light power reaching the sensor after being reflected from the objects in the scene (type, intensity, direction of illumination, reflectance properties of the viewed surfaces);
- geometric parameters determining the image position on which a 3-D point is projected (type of projections, position and orientation of the camera in space, perspective distortions introduced by the imaging process).

The most common vision sensor designs used in robotics are based on the conventional *perspective* camera model, and on the *catadioptric* camera model. The latter is obtained by combining mirrors with a conventional imaging system, in order to increase the field of view of the camera, which is restricted in the perspective model. Originally introduced mainly for monitoring activities, catadioptric visual sensors are now widely used in applications like: surveillance, immersive telepresence, videoconferencing, mosaicing, robotics, and map building [30]. The larger field of view eliminates the need for more cameras or for a mechanically turnable camera.

In literature, several methods have been proposed for increasing the field of view of camera systems. Here, we focus uniquely on *central catadioptric* designs, i.e. designs based on models that utilize a single projection center for world to image mapping.

In central catadioptric vision sensors, all rays joining a world point and its projection in the image plane pass through a single point called *principal projection center*. The conventional perspective camera model, also known as *pinhole camera model* is a typical example of central catadioptric vision sensor, based on the assumption that the mapping of world points into image plane points is linear in homogeneous coordinates. There are central catadioptric systems whose geometry cannot be modeled using the conventional pinhole model. Baker and Nayar in [2] show that all central catadioptric systems with a wide field of view may be built by combining an hyperbolic, elliptical or planar mirror with a perspective camera and a parabolic mirror with an orthographic camera. However, the mapping between world points and points in the image plane is no longer linear. In [30], the unifying model for all central catadioptric imaging systems has been introduced. In this model, which uses a virtual unitary sphere (shown in Fig. 1.6) as a calculus artefact, the conventional perspective camera appears as a particular case. In the remainder of this chapter, this unified central catadioptric model will be utilized to derive the mapping between world points and corresponding image points.

With reference to Fig. 1.6, let us define the reference frames: camera frame  $\mathcal{F}_{\mathcal{C}}(C, x_c, y_c, z_c)$  (*C* is the principal projection center of the central catadioptric system) and image frame  $\mathcal{F}_{\mathcal{I}}(I, X, Y)$ . The world frame  $\mathcal{F}_{\mathcal{W}}(W, x', y', z')$  has been defined in Sect. 1.1. Point coordinates are expressed in meters in  $\mathcal{F}_{\mathcal{W}}$  and  $\mathcal{F}_{\mathcal{C}}$ , and in pixels in  $\mathcal{F}_{\mathcal{I}}$ . The virtual unitary sphere is centered in *C*, and the optical center of the conventional camera (with coordinates  $[0 \ 0 \ -\xi]^T$  in  $\mathcal{F}_{\mathcal{C}}$ ) is denoted *C'*. *I* is the image center, also known as *principal point*.  $I_C$  is the intersection between the  $z_C$  axis and the image plane. Its coordinates in  $\mathcal{F}_{\mathcal{I}}$ ,  $X_I$  and  $Y_I$ , determine the signed offsets in pixels from *I* to the  $z_C$  axis, also known as *principal point error*. The image plane has equation  $z_c = \psi - 2\xi$  in  $\mathcal{F}_C$ . Parameters  $\xi$  and  $\psi$  describe the type of sensor and the shape of the mirror, and are function of mirror shape parameters.

For any world point d (see Fig. 1.6), we want to derive the image coordinates of the corresponding projected point D. The world point is denoted d, because in visual PF it is often chosen coincident with the path desired reference point defined in Sect. 1.1. This relationship can be written:

$$D = {}^{I} T_{C} {}^{C} T_{W} \left[ d^{T} 1 \right]^{T}$$

$$(1.14)$$



Figure 1.6: The unified central catadioptric camera model: virtual unitary sphere, image plane, and other relevant variables.

where the matrices  ${}^{I}T_{C}$  (size 2 × 3) and  ${}^{C}T_{W}$  (size 3 × 4) indicate respectively the transformations: from camera to image, and from world to camera coordinates. Deriving these transformations is equivalent to assuming knowledge of some camera characteristics, known in vision as camera *extrinsic* and *intrinsic* parameters, necessary to derive respectively  ${}^{C}T_{W}$  and  ${}^{I}T_{C}$ . The problem of estimating the value of these parameters is called *camera calibration*.

#### 1.3.2 Extrinsic parameters

The extrinsic camera parameters are defined as any set of geometric parameters that identify uniquely the transformation  ${}^{C}T_{W}$  between  $\mathcal{F}_{W}$  and  $\mathcal{F}_{C}$ . A typical choice for describing the transformation  ${}^{C}T_{W}$ , is to use:

- a 3-D translation vector T describing the relative positions of the origins of the two reference frames;
- a  $3 \times 3$  orthogonal rotation matrix R that brings the corresponding axes of the

two frames onto each other (N.B: the orthogonality relations reduce the number of degrees of freedom of R to three).

Thus, the relation between the world and camera coordinates (noted  $d_c$ ) of a point d, is:

$$d_c = R(d - T) \tag{1.15}$$

Hence, the  $3 \times 4$  matrix  $^{C}T_{W}$  is:

$$^{C}T_{W} = \begin{bmatrix} R & -RT \end{bmatrix}$$

#### **1.3.3** Intrinsic parameters

The intrinsic parameters are the set of parameters that characterize the optical, geometric and digital characteristics of the viewing camera. They are necessary to link the pixel coordinates of an image point with the corresponding coordinates in the camera reference frame, i.e., to identify the transformation  $^{I}T_{C}$ .

For the conventional perspective camera model, for instance, we need three sets of intrinsic parameters, respectively specifying:

- the perspective projection, for which the only parameter is the focal length f;
- the transformation between  $\mathcal{F}_{\mathcal{C}}$  and  $\mathcal{F}_{\mathcal{I}}$  coordinates, for which the parameters are: the metric size of the pixel  $l_X$  and  $l_Y$  in the axis directions, and the principal point error  $(X_I, Y_I)$ ;
- the geometric distortion induced by the optics; usually, distortion is evident at the periphery of the image (radial distortion<sup>3</sup>), or even elsewhere when using optics with large fields of view; radial distortion is ignored whenever high accuracy is not required in all regions of the image, or when the peripheral pixels can be discarded.

$$X = \tilde{X} \left( 1 + \alpha_1 \tilde{D}^2 + \alpha_2 \tilde{D}^4 \right)$$
$$Y = \tilde{Y} \left( 1 + \alpha_1 \tilde{D}^2 + \alpha_2 \tilde{D}^4 \right)$$

with  $\tilde{X}$  and  $\tilde{Y}$  the coordinates of the distorted points, and  $\tilde{D}^2 = \tilde{X}^2 + \tilde{Y}^2$ . This distortion is a radial displacement of the image points. A simplified model with  $\alpha_2$  set to zero is often still accurate.

 $<sup>^{3}</sup>$ Radial distortions can be modeled rather accurately according to the relations:

Neglecting radial distortion, the relation between the camera and image coordinates of a point d is:

$$\begin{bmatrix} D \ 1 \end{bmatrix}^T = M_{int} \begin{bmatrix} x_c & y_c \\ z_c + \xi \parallel d_c \parallel & z_c + \xi \parallel d_c \parallel & 1 \end{bmatrix}^T$$

The matrix  $M_{int}$  can be written as  $M_{int} = M_c M_m$  where the upper triangular matrix  $M_c$  contains the conventional camera intrinsic parameters, and the diagonal matrix  $M_m$  contains the mirror intrinsic parameters:

$$M_{c} = \begin{bmatrix} \frac{1}{l_{Y}} & 0 & X_{I} \\ 0 & \frac{1}{l_{X}} & Y_{I} \\ 0 & 0 & 1 \end{bmatrix} \qquad \qquad M_{m} = \begin{bmatrix} \psi - \xi & 0 & 0 \\ 0 & \psi - \xi & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

Note that, setting  $\xi = 0$  and  $\psi = f$ , the general projection model becomes the well known perspective projection model. In this case, the 2 × 3 matrix  $^{I}T_{C}$  relating camera and image coordinates becomes:

$${}^{I}T_{C} = \frac{1}{z_{c}} \begin{bmatrix} \frac{f}{l_{X}} & 0 & X_{I} \\ 0 & \frac{f}{l_{Y}} & Y_{I} \end{bmatrix}$$
(1.16)

The relationship:

$$D = {}^{I} T_C d_c \tag{1.17}$$

is nonlinear because of factor  $1/z_c$ , and does not preserve neither distances between points (not even up to a common scaling factor) nor angles between lines. However, it does map lines into lines. A classic approximation that makes this relationship linear is the *weak perspective camera model*. This model requires that the relative distance along the optical axis between any two scene points is much smaller than the average distance  $\bar{z}_c$ , of the points from the viewing camera. In this case, (1.16) can be rewritten by replacing  $z_c$  with  $\bar{z}_c$ . Another simplification, the *normalized perspective camera model*, is obtained by assuming:  $X_I = Y_I = 0$  and  $l_X = l_Y = 1$ .

#### 1.4 Visual servoing

In this Section, which is taken in part from [8], we describe the basic techniques that are by now well established in the field of visual servoing. We first give an overview of the general formulation of the visual servo control problem. We then describe the
two basic visual servo control schemes: image-based and position-based visual servo control. In position-based approaches, visual feedback is computed by reducing errors in estimated pose space. In image-based servoing, control values are computed on the basis of image features directly.

#### 1.4.1 Outline

Visual servo control refers to the use of computer vision data to control the motion of a robot. The vision data may be acquired from a camera that is mounted directly on a robot manipulator or on a mobile robot (in this case, motion of the robot induces camera motion). Otherwise, the camera can be fixed in the workspace (the camera can observe the robot motion from a stationary configuration). Other configurations can also be considered. However, the mathematical development of all these cases is similar, and here we shall specifically focus on the former case (referred to as *eye-in-hand* in the literature), since in this thesis we consider mobile robots with an on-board camera. Visual servo control relies on techniques from image processing, computer vision, and control theory. Since it is not possible to cover all of these in depth, we will focus here primarily on issues related to control, and to those specific geometric aspects of computer vision that are uniquely relevant to the study of visual servo control. For instance, we will not specifically address issues related to feature tracking or three-dimensional pose estimation.

The aim of all vision-based control schemes is to minimize a k-dimensional error e(t), which is typically defined by:

$$e(t) = s(M(t), \mathcal{P}) - s^*$$
 (1.18)

In (1.18), The vector M(t) is a set of image measurements (e.g., the image coordinates of interest points or the image coordinates of the centroid of an object). These image measurements are used to compute a vector of k visual features,  $s(M(t), \mathcal{P})$ , in which  $\mathcal{P}$ is a set of parameters that represent potential additional knowledge about the system (e.g., coarse camera intrinsic parameters or 3-D models of objects). The vector  $s^*$ contains the desired values of the features. Let us consider for simplicity the case of a fixed goal pose and a motionless target, (i.e.,  $s^* = \text{const}$ , and changes in s depend only on camera motion). Moreover, we consider the general case of controlling the motion of a camera with six degrees of freedom: let the spatial velocity of the camera be denoted by  $u_c$ . We consider  $u_c$  as the input to the robot controller. Visual servoing schemes mainly differ in the way that s is designed. Here, we shall consider two very different approaches. First, we describe image-based visual servo control, in which s consists of a set of features that are immediately available in the image data. Then, we describe position-based visual servo control, in which s consists of a set of 3-D parameters, which must be estimated from image measurements. Once s is selected, the design of the control scheme can be quite simple. Perhaps the most straightforward approach is to design a velocity controller. To do this, we require the relationship between the time variation of s and the camera velocity. The relationship between  $\dot{s}$  and  $u_c$  is given by:

$$\dot{s} = L_s u_c \tag{1.19}$$

where the  $k \times 6$  matrix  $L_s$  is named the *interaction matrix* related to s. The term feature Jacobian is also used somewhat interchangeably in the visual servo literature. Using (1.18) and (1.19), we immediately obtain the relationship between the camera velocity and the time variation of the error:

$$\dot{e} = L_s u_c \tag{1.20}$$

If we wish to ensure an exponential decoupled decrease of the error (i.e.,  $\dot{e} = -\lambda e$ ), we obtain using (1.20):

$$u_c = -\lambda L_s^+ e, \tag{1.21}$$

where the  $6 \times k$  matrix  $L_s^+$  is chosen as the Moore-Penrose pseudoinverse of  $L_s$ , that is:  $L_s^+ = (L_s^T L_s)^{-1} L_s^T$  when  $L_s$  is of full rank 6. This choice allows  $\parallel \dot{e} - \lambda L_s L_s^+ e \parallel$  and  $\parallel u_c \parallel$  to be minimal. When k = 6, if det  $L_s \neq 0$ , it is possible to invert  $L_s$ , giving the control  $u_c = -\lambda L_s^{-1} e$ . In real visual servo systems, it is impossible to know perfectly in practice either  $L_s$  or  $L_s^+$ . So an approximation or an estimation of one of these two matrices must be realized. In the sequel, we denote both the pseudoinverse of the approximation of the interaction matrix and the approximation of the pseudoinverse of the interaction matrix by the symbol  $\hat{L}_s^+$ . Using this notation, the control law is in fact:

$$u_c = -\lambda L_s^+ e \tag{1.22}$$

This is the basic design implemented by most visual servo controllers. All that remains is to fill in the details: How should s be chosen? What then is the form of  $L_s$ ? How should we estimate  $L_s^+$ ? What are the performance characteristics of the resulting closed-loop system? These questions are addressed in the remainder of this Section.

#### 1.4.2 Image-based visual servoing

Traditional image-based control schemes use the image-plane coordinates of a set of points (other choices are possible, but we shall not discuss these here) to define the set s. Consider the case of a conventional perspective camera. We assume (recalling the notation from Sect. 1.3) that  $X_I = Y_I = 0$  and  $l_X = l_Y = l$ . Then, for a 3-D point d with image coordinates  $D = [X, Y]^T$ , the interaction matrix  $L_s$  is  $(s \equiv D)$ :

$$L_{s} = \begin{bmatrix} -\frac{f}{z_{c}l} & 0 & \frac{X}{z_{c}} & \frac{lXY}{f} & -\frac{f^{2}+l^{2}X^{2}}{fl} & Y\\ 0 & -\frac{f}{z_{c}l} & \frac{Y}{z_{c}} & \frac{f^{2}+Y^{2}}{fl} & -\frac{lXY}{f} & -X \end{bmatrix}$$
(1.23)

In the matrix  $L_s$ , the value  $z_c$  is the depth of the point d relative to the camera frame  $\mathcal{F}_{\mathcal{C}}$ . Therefore, any control scheme that uses this form of the interaction matrix must estimate or approximate the value of  $z_c$ . Similarly, the camera intrinsic parameters are involved in the computation of  $L_s$ . Thus,  $L_s$  cannot be directly used in (1.21), and an estimation or an approximation  $\hat{L}_s$  must be used. To control the 6 degrees of freedom, at least three points are necessary (i.e., we require  $k \geq 6$ ).

#### 1.4.3 Position-based visual servoing

Position-based control schemes use the pose of the camera with respect to some reference coordinate frame to define s. Computing that pose from a set of measurements in one image necessitates the camera intrinsic and extrinsic parameters to be known. It is then typical to define s in terms of the parameterization used to represent the camera pose. The image measurements M are usually the pixel coordinates of the set of image points (but this is not the only possible choice), and the parameters  $\mathcal{P}$  in the definition of  $s = s(M, \mathcal{P})$  in (1.18) are the camera intrinsic and extrinsic parameters. Many solutions for position-based visual servoing have been proposed in the literature.

# Chapter 2

# **Related work**

This chapter reviews some recent research works in the field of path following. First we shall focus on general works on path following that do not specify the sensor used to detect the path, but assume geometric knowledge of the path characteristics. These works will be referred to as 'sensor-less' approaches, since they focus on the control aspects of PF rather than on the sensor processing required to detect and model the path. In the second section, we shall instead focus on works that use a visual approach to solve path following, and include considerations and practical implementation of the sensing techniques, along with the control aspects. Throughout the chapter, we adopt the notation defined in Chapter 1. Unless otherwise specified, in all works the PF task consists of driving the path error  $e(\varepsilon)$  to  $\hat{e}(\varepsilon) \equiv 0$ .

# 2.1 Sensor-less path following

In [16], Canudas de Wit and others tackle the problem of following a path with a unicycle robot. The path following constraint is chosen by defining d as the normal projection of r on p, i.e., by choosing d such that  $e_t = \text{const} = 0$ . The authors assume that the path curvature is differentiable, and the motion exigency is guaranteed by imposing constant linear velocity:  $u_1 = \text{const} > 0$ . Two alternative controllers on the angular velocity  $u_2$  are designed. The first is a locally stabilizing linear feedback control obtained by tangent linearization of the kinematic model:

$$u_2 = \left(\lambda_1 e_n - \lambda_2 e_\theta + \frac{c_d \cos e_\theta}{1 + c_d e_n}\right) u_1 \tag{2.1}$$

The second controller is nonlinear:

$$u_{2} = \left(\lambda_{1}e_{n}\frac{\sin e_{\theta}}{e_{\theta}} + \frac{c_{d}\cos e_{\theta}}{1 + c_{d}e_{n}}\right)u_{1} - \lambda_{2}\left(u_{1}\right)e_{\theta}$$

$$(2.2)$$

and is used to asymptotically stabilize the system under some conditions on the initial robot configuration. A Lyapunov-based proof is carried out for the second controller. In both controllers,  $\lambda_1$  and  $\lambda_2$  are positive gains. Note that in the nonlinear controller,  $\lambda_2$  is a function of  $u_1$ .

In [15], straight line following with a car-like robot is considered. Although the implementation presented uses an on-board omnidirectional camera, the algorithm relies only on the 3-D features of the line, which can be detected independently from the sensor. For this reason, we consider this controller among the sensor-less path following approaches. The authors use the car-like model (1.9). The path following constraint is  $e_t = \text{const} = 0$ , and the linear velocity  $u_1$  is piecewise constant non-null (hence, the motion exigency is guaranteed). Feedback linearization is used to design a proportional-derivative path following controller on the robot angular velocity with respect to the midpoint of the rear wheels:

$$u_2 = \lambda_1 \frac{e_n}{u_1 \cos e_\theta} - \lambda_2 \tan e_\theta$$

 $\lambda_1$  and  $\lambda_2$  are positive controller gains. Critically damping behavior can be obtained if  $\lambda_2 = 2\sqrt{\lambda_1}$ . Note that this controller presents a singularity for  $e_{\theta} = \pm \frac{\pi}{2}$ .

Frezza and others [29] enable a unicycle robot to follow paths assumed to be representable in  $\mathcal{F}_{\mathcal{R}}$  as: x = x(y,t) (the path changes over time under the action of robot motion). They define moments  $\nu_i$  as a chain of derivatives of the path function, computed in y = 0:  $\nu_i = \frac{\partial^{i-1}x}{\partial^{i-1}y}|_{y=0}$ . The proposed controller should regulate to zero  $\nu_1$ and  $\nu_2$ . Note that this formulation of PF is equivalent to imposing path following constraint:  $e_t = \text{const} = 0$ . Since conventional control via feedback linearization demands exact knowledge of the contour and is not robust to disturbances, they define  $x_b = x_b(y,t)$  as a feasible cubic B-spline instantaneously approximating the path. Under these assumptions, they show that the system can be locally stabilized by controller:

$$u_2 = u_1 \frac{\partial^2 x_b}{\partial^2 y} \left( 0, t \right)$$

For  $u_1$  non-null, the motion exigency is guaranteed.

In [69], a smooth time-varying feedback stabilization method is proposed for a nonholonomic mobile robot with m = 2 control inputs, and  $n \leq 4$  generalized coordinates. The method is based on the chained form model, which is a canonical model for which the nonholonomic motion planning problem can be solved efficiently [58]. The author assumes that the robot kinematic model can be converted into a chained form via input transformation and change of coordinates. An appropriate chained form representation of the model is used:  $[\dot{\chi}_1 \ \dot{\chi}_2 \ \dots \ \dot{\chi}_{n-1} \ \dot{\chi}_n]^T =$  $[u'_1 \ \chi_3 u'_1 \ \dots \ \chi_n u'_1 \ u'_2]^T$ , where  $u'_1$  and  $u'_2$  are the new control inputs. Following a path is equivalent to zeroing  $\Xi = [\chi_2 \ \dots \ \chi_n]^T$ . The author shows that a time-varying control  $u'_2 = u'_2(u'_1, t, \Xi)$  globally asymptotically stabilizes  $\Xi = 0$  for any piecewise-continuous, bounded and strictly positive  $u'_1(t)$ .

# 2.2 Vision-based path following

In [72], Skaff and others study vision-based following of straight lines for a six-legged robot equipped with a fixed conventional perspective camera. The camera leans forward with a constant tilt angle with respect to the ground. The legged robot is modeled as a unicycle. The authors propose two steering policies  $u_2$ , that in the article are called 'position-based controller' and 'field of view respecting controller' in the article. In both controllers, the motion exigency is guaranteed by imposing:  $u_1 = \text{const} > 0$ . In the first case, the path following constraint is  $e_t = \text{const} = 0$ , and the controller is identical to (2.1), in the particular case of straight path ( $c_d \equiv 0$ ):

$$u_2 = \left(\lambda_1 e_n - \lambda_2 e_\theta\right) u_1$$

For the 'field of view respecting controller', the path following constraint is defined in the image. It consists of centering the perspective projection of the line in the image plane. This corresponds to zeroing  $X_{top}$  and  $X_{bot}$ , which are defined (assuming that they always exist) as the abscissas in  $\mathcal{F}_{\mathcal{I}}$  of the intersection points of the image projection of the line with the top and bottom sides of the field of view. Note that if the camera optical axis is in the robot sagittal plane (as it is assumed in the article), this is equivalent to imposing PF constraint  $e_t = \text{const} = 0$ . The states  $[X_{top} X_{bot}]^T$  are mapped to a new state space  $[\varphi_1 \varphi_2]^T$  defined by the projection of the image plane on the ground. In the new state space, a closed loop policy (detailed in the paper):

$$u_2 = u_2\left(\varphi_1, \varphi_2\right)$$

regulates the system to the desired set point. The controller is mapped back to  $[X_{top} X_{bot}]^T$  coordinates, and a Lyapunov-like function is used to prove the asymptotic stability of the system under given conditions on the camera parameters.

More recently, Coulaud and others [14] have proposed a vision-based feedback controller and discussed the existence and stability of an equilibrium trajectory for arbitrary paths. They focus on following paths with a unicycle robot equipped with a fixed conventional perspective camera. The camera leans forward, with a tilt angle of  $45^{\circ}$ . The motion exigency is verified by imposing constant linear velocity  $u_1 = \text{const}$ > 0. Having defined the horizon as the straight line parallel to the wheel axle and at constant distance  $y_h$  ahead of it, and d the intersection point between horizon and path<sup>1</sup>, the proposed controller is:

$$u_2 = \lambda X$$

with  $\lambda$  positive gain and X abscissa in  $\mathcal{F}_{\mathcal{I}}$  of the projection D of d in the image plane. For a circular path, local asymptotic stability of an equilibrium state  $[\theta X]_{eq}^T$ that is function of  $c_d$ ,  $u_1$ , and  $\lambda$  (i.e.,  $[\theta X]_{eq}^T = [\theta (c_d) X (c, u_1, \lambda)]^T$ ) is proved. The authors show that tracking error is bounded for a path with continuously differentiable curvature. Arbitrary paths can be tracked by dynamically adapting  $u_1$ ,  $\lambda$  and  $y_h$ . Design constraints, stability margin and convergence rate are represented in the phase plane  $(\theta, X)$ .

Another interesting work is presented in [54], where vision-based PF for unicycle and car-like robots equipped with a conventional perspective camera is achieved by controlling the curve shape in the image plane. Similarly to [14] and [72], the camera leans forward with non-null tilt angle. The approach is similar to [29]. The authors assume that the curve orthographic projection on the  $z_c = 1$  plane in  $\mathcal{F}_{\mathcal{C}}$  can be represented as:  $x_c = x_c(y_c, t)$  (N.B: time dependance is due to robot motion) and

<sup>&</sup>lt;sup>1</sup>In case of multiple intersection points, D will be the closest to the robot sagittal plane.

define  $\nu_i^c = \frac{\partial^{i-1}x_c}{\partial^{i-1}y_c}$ , with  $i = 1, 2, \ldots$  Then, for linear curvature curves (clothoids), the dynamics of the orthographic projection image curve (i.e.  $\nu_i^c$ ) are proved equivalent to those of the perspective projection image curve. Both can then be expressed as a function of  $\nu_1^c$ ,  $\nu_2^c$  and  $\nu_3^c$  alone. Noting  $[x_c^r y_c^r z_c^r]^T$  the  $\mathcal{F}_{\mathcal{C}}$  coordinates of the contact point between wheel and ground (i.e., the robot reference point r), following the path is equivalent to zeroing  $\nu_1^c|_{y_c=y_c^r}$  and  $\nu_2^c|_{y_c=y_c^r}$ . Again, this is equivalent to imposing PF constraint  $e_t = \text{const} = 0$ . By transforming the system  $[\dot{\nu}_1^c \dot{\nu}_2^c \dot{\nu}_3^c]^T$ in canonical form, "clothoid following" is shown to be globally achievable with piecewise smooth sinusoidal inputs. Such piecewise smooth controllers are given for an arbitrary path, and asymptotic stability of the closed-loop system is proved. In this formulation of PF, the motion exigency specification is not explicitly guaranteed. The practical implementation is rather sophisticated, implying an extended Kalman filter to dynamically estimate the path curve derivatives up to order three.

In [33], Hadj-Abdelkader and others present an image-based visual servoing scheme which enable a mobile robot equipped with a para-catadioptric camera to follow straight lines. The line following control law is designed for generic mobile robots, and is implemented on a unicycle robot in the paper. The PF constraint is  $e_t = \text{const} = 0$ , and the motion exigency is guaranteed by  $u_1 = \text{const} > 0$ . Para-catadioptric cameras are formed by a parabolic mirror combined with an orthographic camera. The central catadioptric model described in Sect. 1.3 can be used for this kind of sensors by appropriately setting  $\xi$  and  $\psi$ . The equation of the conic curve in  $\mathcal{F}_{\mathcal{I}}$ , corresponding to the straight path is derived. Then, a minimal and generic analytical form of the central catadioptric interaction matrix  $L_s$  for the image of 3D straight lines is derived. Finally, the authors rely on a number of experiments to show that the image-based control law (1.22) on the angular velocity enables the unicycle robot to follow the line.

# Chapter 3

# Vision-based path following for a nonholonomic mobile robot with fixed pinhole camera

Applying visual servoing control techniques for navigation with wheeled mobile robots, involves well known control problems related to the nonholonomic constraint. Firstly, the linearization of these systems is uncontrollable, and, secondly, there do not exist smooth state feedback laws for stabilizing these systems to an equilibrium. Notwithstanding, visual servoing techniques have been successfully used to control nonholonomic mobile robots in [36], [56], [77], and more recently in [55]. Here, we present two path following (PF) control schemes (position-based and image based), enabling nonholonomic mobile robots with a fixed pinhole camera to reach and follow a continuous path on the ground by processing a small set of features in the image plane.

This chapter is organized as follows. In Sect. 3.1, all the relevant variables utilized in our method are defined. In Sect. 3.2, we propose and illustrate the two controllers. In Sect. 3.3 a Lyapunov-based stability analysis, which takes into account the robot kinematic constraint on maximum curvature, is carried out. The experimental setup and simulated and experimental results are respectively presented in Sect. 3.4, Sect. 3.5 and 3.6. In the conclusion, we summarize the results, and compare the two controllers.



Figure 3.1: Relevant variables utilized in this work. The task for the robot (represented in orange), equipped with a fixed pinhole camera (blue) is to follow the red path, noted p. The figure represents: top view (a,d), image plane (b), and side view (c). The camera field of view and its projection on the ground are represented in cyan. The control inputs are represented in green.

## 3.1 Definitions

In this work, we focus on the path following task for nonholonomic mobile robots equipped with a fixed pinhole camera. All relevant variables (most of which have been defined in Chapter 1) are shown in Fig. 3.1. The camera optical axis has a constant tilt offset  $0 < \rho < \frac{\pi}{2}$  with respect to the y axis and the optical center C is positioned in the robot sagittal plane at  $[x \ y \ z]^T = [0 \ t_y \ t_z]^T$  (see Fig. 3.1(c)). We assume that in  $\mathcal{F}_W$ , the path curve p, can be expressed by a twice differentiable function. A following direction is associated to the path. Point r is chosen as the projection on the ground of the wheels center in the case of a unicycle robot, and of the rear axis center in the case of a car-like robot. We refer to the general nonholonomic model (1.9), which is valid both for unicycle and car-like robots. In (1.9), control input  $u_1$  represents the linear velocity, while control input  $u_2$  represents the angular velocity around the z axis (positive counterclockwise). Recall (see Sect. 1.2.1) that for a car-like robot, the steering angle constraint  $|\phi| \leq \phi_M$  imposes the bound (1.11) on the instantaneous applicable curvature; in the case of a unicycle robot, there is no such bound.

For the nonholonomic model (1.9), the dynamics of the  $\mathcal{F}_{\mathcal{P}}$  path errors  $e_t$ ,  $e_n$  and

 $e_{\theta}$  (see Sect. 1.1) are:

$$\dot{e}_{t} = -u_{d1} - u_{d2} e_{n} + u_{1} \cos e_{\theta}$$
  

$$\dot{e}_{n} = u_{d2} e_{t} - u_{1} \sin e_{\theta}$$
  

$$\dot{e}_{\theta} = u_{2} - u_{d2}$$
  
(3.1)

where  $u_{d1}$  and  $u_{d2}$  are the components of the tracking control  $u_d$ . These must be compliant with the path curvature at d in  $\mathcal{F}_{\mathcal{R}}$ , noted  $c_d^1$ :

$$u_{d2} = c_d \ u_{d1} \tag{3.2}$$

In most works (see Chapter 2), the path following constraint is chosen as  $e_t = \text{const} = 0$ , and the motion exigency as  $u_1 = \text{const} > 0$ . For this formulation of the PF problem, the system becomes:

$$\begin{cases} \dot{e}_n = -u_1 \sin e_\theta \\ \dot{e}_\theta = u_2 - \frac{u_1 c_d \cos e_\theta}{1 + e_n c_d} \end{cases}$$

The path following constraint  $e_t = \text{const} = 0$  does not guarantee that the path is visible. Instead, since in our work the robot camera is the only sensor available, we want to ensure path visibility at all times. Hence, we use a path following constraint that keeps the reference point d in the camera field of view. The path following constraint chosen in this work will be detailed in the next section.

Similarly to [16], [72], and [14], we express the motion exigency as:  $u_1 = \text{const} > 0$ , and we apply a nonlinear feedback on  $u_2$  based on the features of a visible path point. Under the assumption that a portion of the path is always visible, we utilize the features of the *first* (considering the path direction, as defined by  $u_{d1}$ ) visible path point d of coordinates  $[xy0]^T$  in  $\mathcal{F}_{\mathcal{R}}$ , projected to  $D = [XY]^T$  on the image plane (see Fig. 3.1(b)). We note: P the projection of p on the image plane,  $\Gamma$  the oriented tangent of P at D,  $C_D$  the curvature of P at D, and  $\Theta \in [-\pi, \pi]$  the angular offset from  $\Gamma$  to the -Y axis (positive counterclockwise)<sup>2</sup>.



Figure 3.2: Seven possible configurations of P in the image plane. Point D is represented by the red circle.

# 3.2 Control design

In both control schemes that we propose (position-based and image-based), the PF task is defined by path image features. In practice, the PF task is to drive D to the bottom pixel row of the image plane with  $X = \Theta = 0$ , as shown in Fig. 3.2(g). Depending on the position of D in the image plane, the control schemes switch between two primitive controllers: a row controller and a column controller. In both primitive controllers, the task is to drive the path features to a desired configuration, while D is constrained to a line in the image plane: a row of pixels (Y = const) in the first case, and a column of pixels (X = const) in the second case. These conditions determine the path following constraint outlined in Sect. 3.1. The control schemes utilize the two primitive controllers in general initial conditions, based on a switching mechanism. Consider for instance the initial configuration shown in Fig. 3.2(a), with D on the top pixel row of the image plane. Initially, the row controller must be used to drive D to a lateral pixel column of the image plane (e.g., the left column, as in Fig. 3.2(b)). Afterwards, the column controller will be used to drive D along the left pixel column of the image to the bottom left corner (Figures 3.2(c), 3.2(d) and 3.2(e)). Finally, the row controller should be used to drive D along the bottom row of the image plane to the desired configuration (Fig. 3.2(g)).

The task of the position-based path follower is to control the path error in  $\mathcal{F}_{\mathcal{P}}$ , whose dynamics, expressed by replacing (3.2) in (3.1), clearly depend on the curvature  $c_d$ . On the other hand, the task of the image-based path follower is to control the

 $<sup>{}^{1}</sup>c_{d}$  is always defined, since we have assumed that the path curve can be expressed by a twice differentiable function in  $\mathcal{F}_{\mathcal{W}}$ , and this property is preserved in  $\mathcal{F}_{\mathcal{R}}$ .

 $<sup>{}^{2}\</sup>Gamma$  and  $\Theta$  are always defined, since we have assumed that the path curve can be expressed by a twice differentiable function in  $\mathcal{F}_{\mathcal{W}}$  and this property is preserved in  $\mathcal{F}_{\mathcal{I}}$ .

error related to the image features X, Y, and  $\Theta$ , without taking into account the path curvature. Therefore, a major difference between the two proposed controllers is that the position-based controller depends on  $c_d$ , whereas the image-based controller does not. In the remainder of this section, we shall describe how the 3D path features are derived from the corresponding image path features. We shall also illustrate the implementation of the two primitive controllers for both position-based and image-based visual servoing.

#### 3.2.1 Deriving the path 3D features

For the position-based approach, the path 3D features in  $\mathcal{F}_{\mathcal{R}}$  must be derived from the image features by considering a pinhole camera model; radial distortion and principal point error are neglected. Hence, the five camera parameters used for projecting are:

$$\mathcal{P} = \begin{bmatrix} f_X & f_Y & \rho & t_y & t_z \end{bmatrix}^T$$

where the focal lengths in horizontal and vertical pixel size  $f_X$  and  $f_Y$  are the camera intrinsic parameters, and  $\rho$ ,  $t_y$  and  $t_z$  are the extrinsic parameters shown in Fig. 3.1(c).

For simplicity, let us consider a camera model with  $f_X = f_Y = 1$ , known in the literature as normalized perspective camera model. The mapping between the  $\mathcal{F}_{\mathcal{I}}$  and  $\mathcal{F}_{\mathcal{C}}$  coordinates of a ground point gives<sup>3</sup>:

$$x_c = \frac{Xt_z}{\sin\rho + Y\cos\rho} \tag{3.3}$$

$$y_c = \frac{Y t_z}{\sin \rho + Y \cos \rho} \tag{3.4}$$

$$z_c = \frac{t_z}{\sin\rho + Y\cos\rho} \tag{3.5}$$

The robot frame coordinates of the ground point can then be easily derived by using the homogenous transformation from  $\mathcal{F}_{\mathcal{R}}$  to  $\mathcal{F}_{\mathcal{C}}$  (i.e, the camera extrinsic parameters). For the orientation of the tangent at d, we obtain:

$$e_{\theta} = \operatorname{ATAN2}\left(-\sin\Theta\left(\sin\rho + Y\cos\rho\right) - X\cos\Theta\cos\rho, \cos\Theta\right)$$

To derive  $c_d$  (i.e., the path curvature at d in  $\mathcal{F}_{\mathcal{R}}$ ), the image path points are initially projected to  $\mathcal{F}_{\mathcal{R}}$ . Afterwards, the equation of the path osculating circle in d (thus, the value of  $c_d$ ) is derived using least square interpolation.

<sup>&</sup>lt;sup>3</sup>Equations (3.3) - (3.5) do not present singularities, since by construction the image projection of any ground point has  $Y > -\tan \rho$ .

#### 3.2.2 Position-based path follower

#### Row controller

The task of the position-based row controller is to drive  $(x, y, e_{\theta})$  to a desired set point  $(\hat{x}, \hat{y}, \hat{e}_{\theta})$  under constraint  $Y = \text{const} = Y^*$  (i.e., D is constrained to a pixel row in the image plane).

This is equivalent to constraining d to the projection of the pixel row on the ground (see Fig. 3.1(a)), i.e. to the line of equation:

$$y = const = y^*$$

The above equation, which defines the path following constraint, can be rewritten by introducing the position errors in  $\mathcal{F}_{\mathcal{P}}$ :

$$\dot{y} = \frac{d}{dt} \left( e_n \sin e_\theta - e_t \cos e_\theta \right) = 0$$

Using (3.1) simple calculations lead to:

$$u_{d1} = \frac{u_1 + u_2 x}{\cos e_\theta}$$

under the constraint that  $|e_{\theta}| \neq \pm \frac{\pi}{2}$ , which is plausible, assuming that  $\Gamma$  is never parallel to the the X axis of frame  $\mathcal{F}_{\mathcal{I}}^4$ . Replacing  $u_{d1}$  and using (3.1) in:

$$\dot{x} = \frac{d}{dt} \left( -e_n \cos e_\theta - e_t \sin e_\theta \right)$$

gives:

$$\dot{x} = (\tan e_{\theta})u_1 + (y^* + x \tan e_{\theta})u_2$$

Hence, the system state equations are:

$$\begin{bmatrix} \dot{x} \\ \dot{e_{\theta}} \end{bmatrix} = Au_1 + Bu_2 \tag{3.6}$$

where:

$$A = \begin{bmatrix} \tan e_{\theta} \\ -\frac{c_d}{\cos e_{\theta}} \end{bmatrix} \qquad \qquad B = \begin{bmatrix} y^* + x \tan e_{\theta} \\ 1 - \frac{c_d x}{\cos e_{\theta}} \end{bmatrix}$$

<sup>4</sup>This singularity can be avoided by temporarily switching to the position-based column controller.

When  $B \neq 0$  (i.e. r is not at the center of the osculating circle of p at d), the system is controllable and we select as control law:

$$u_2 = -B^+ \left( \left[ \begin{array}{c} \lambda_x e_x \\ \lambda_\theta e_{\hat{\theta}} \end{array} \right] + A u_1 \right)$$
(3.7)

where  $e_x = x - \hat{x}$  and  $e_{\hat{\theta}} = e_{\theta} - \hat{e}_{\theta}$  are the state errors, and  $\lambda_x$ ,  $\lambda_{\theta}$  are given positive gains.

#### Column controller

The task of the position-based column controller is to drive  $(x, y, e_{\theta})$  to a desired set point  $(\hat{x}, \hat{y}, \hat{e}_{\theta})$  under constraint  $X = \text{const} = X^*$  (i.e., D is constrained to a pixel column in the image plane). This is equivalent to constraining d to the projection of the pixel column on the ground (see Fig. 3.1(d)), i.e. to the line of equation:

$$y = y_0 + x \tan \beta$$

where  $y_0$  and  $\beta \in \left]-\frac{\pi}{2}, \frac{\pi}{2}\right]$  (shown in Fig. 3.1(d)) are:

$$\begin{cases} y_0 = t_y - t_z \tan \rho \\ \beta = \operatorname{ATAN} \frac{1}{X \cos \rho} \end{cases}$$

with  $\beta = \frac{\pi}{2}$  at the singularity  $X = 0^5$ .

Let us redefine the system variables in a new frame  $\overline{\mathcal{F}}_{\mathcal{R}}(r, \bar{x}, \bar{y}, \bar{z})$ , obtained by rotating  $\mathcal{F}_{\mathcal{R}}$  by  $\beta$  around z and shown in Fig. 3.1(d).

In this new frame, noting  $\bar{e}_{\theta} = e_{\theta} + \beta$ , we have:

$$\begin{bmatrix} \bar{x} \\ \bar{y} \end{bmatrix} = \begin{bmatrix} -\cos\bar{e}_{\theta} & -\sin\bar{e}_{\theta} \\ \sin\bar{e}_{\theta} & -\cos\bar{e}_{\theta} \end{bmatrix} \begin{bmatrix} e_n \\ e_t \end{bmatrix}$$

The path following constraint becomes:

$$\bar{y} = const = \bar{y}^* \tag{3.8}$$

with  $\bar{y}^* = y_0 \cos \beta$ . Hence, as before, but in  $\bar{\mathcal{F}}_{\mathcal{R}}$ :

$$\dot{\bar{y}} = \frac{d}{dt} \left( e_n \sin \bar{e}_\theta - e_t \cos \bar{e}_\theta \right) = 0$$

<sup>&</sup>lt;sup>5</sup>In that case, the projection of the pixel column on the ground is the line of equation: x = 0.

Using (3.1) simple calculations yield:

$$u_{d1} = \frac{u_1 \cos \beta + u_2 \bar{x}}{\cos \bar{e}_{\theta}}$$

under the constraint that  $|\bar{e}_{\theta}| \neq \pm \frac{\pi}{2}$ , which is plausible, assuming that  $\Gamma$  is never parallel to the Y axis of frame  $\mathcal{F}_{\mathcal{I}}^{6}$ . Replacing  $u_{d1}$  and using (3.1) in:

$$\dot{\bar{x}} = \frac{d}{dt} \left( -e_n \cos \bar{e}_\theta - e_t \sin \bar{e}_\theta \right)$$

gives:

$$\dot{\bar{x}} = (\tan \bar{e}_{\theta} \cos \beta - \sin \beta)u_1 + (\bar{y}^* + \bar{x} \tan \bar{e}_{\theta})u_2$$

Hence, the system state equations are:

$$\begin{bmatrix} \dot{\bar{x}} \\ \dot{\bar{e}}_{\theta} \end{bmatrix} = \bar{A}u_1 + \bar{B}u_2 \tag{3.9}$$

where:

$$\bar{A} = \begin{bmatrix} \tan \bar{e}_{\theta} \cos \beta - \sin \beta \\ -\frac{c_d \cos \beta}{\cos \bar{e}_{\theta}} \end{bmatrix} \qquad \bar{B} = \begin{bmatrix} \bar{y}^* + \bar{x} \tan \bar{e}_{\theta} \\ 1 - \frac{c_d \bar{x}}{\cos \bar{e}_{\theta}} \end{bmatrix}$$

When  $\overline{B} \neq 0$  (i.e. r is not at the center of the osculating circle of p at d), the system is controllable, and we select as control law:

$$u_2 = -\bar{B}^+ \left( \begin{bmatrix} \bar{\lambda}_x \bar{e}_x \\ \bar{\lambda}_\theta \bar{e}_{\hat{\theta}} \end{bmatrix} + \bar{A}u_1 \right)$$
(3.10)

where  $\bar{e}_x = \bar{x} - \hat{x}$  and  $\bar{e}_{\hat{\theta}} = \bar{e}_{\theta} - \hat{e}_{\theta}$  are the state errors, and  $\bar{\lambda}_x$ ,  $\bar{\lambda}_{\theta}$  are given positive gains. Note that in this case, the desired states  $\hat{x}$  and  $\hat{e}_{\theta}$  are expressed in  $\bar{\mathcal{F}}_{\mathcal{R}}$ .

#### 3.2.3 Image-based path follower

Recalling Sect. 1.4, the interaction matrix  $L_s(X, Y, \Theta)$ , relating the path image features with the spatial velocity of the robot camera  $u_c$ , must be derived in order to design the image-based path following controller. In this work:

$$\left[\dot{X}\ \dot{Y}\ \dot{\Theta}\right]^{T} = L_{s}\left(X,Y,\Theta\right)u_{c}$$

<sup>&</sup>lt;sup>6</sup>This singularity can be avoided by temporarily switching to the position-based row controller.

	$-\frac{1}{z_c}$	0	$\frac{X}{z_c}$	XY	$-1 - X^2$	Y
$L_{s}\left( X,Y,\Theta\right) =$	0	$-\frac{1}{z_c}$	$\frac{Y}{z_c}$	$1 + Y^2$	-XY	-X
	$\frac{\cos\rho}{t_z\left(1+\tan^2\Theta\right)}$	0	$\frac{-X \cos \rho + \tan \Theta [\sin \rho + (Y-1) \cos \rho]}{t_z \left(1 + \tan^2 \Theta\right)}$	$-\frac{X{+}(1{-}Y){\tan\Theta}}{1{+}{\tan^2\Theta}}$	$-\frac{\tan\Theta(2X+\tan\Theta)}{1+\tan^2\Theta}$	$-\frac{1}{1+\tan^2\Theta}$ (3.11)

The expression of  $L_s(X, Y, \Theta)$  for the normalized perspective camera model (introduced in Sect. 3.2.1) is shown at the top of this page. In (3.11),  $z_c$  is derived from (3.5). In the following, we shall note  $L_X$ ,  $L_Y$  and  $L_\Theta$  the rows of  $L_s$  (respectively, top to bottom). Note that the singularity at  $\Theta = \pm \frac{\pi}{2}$  does not jeopardize the controller behavior, if, for  $\Theta$  tending to  $\pm \frac{\pi}{2}$ ,  $L_{\Theta}$  is approximated with its limit  $\hat{L}_{\Theta}$ :

$$\hat{L}_{\Theta} = \begin{bmatrix} 0 & 0 & 0 & 0 & -1 & 0 \end{bmatrix}$$

The robot velocity in  $\mathcal{F}_{\mathcal{C}}$  can be expressed in function of u by using the homogenous transformation from  $\mathcal{F}_{\mathcal{R}}$  to  $\mathcal{F}_{\mathcal{C}}$ :

 $u_c = T_R u$ 

with:

$${}^{C}T_{R} = \begin{bmatrix} 0 & -t_{y} \\ -\sin\rho & 0 \\ \cos\rho & 0 \\ 0 & 0 \\ 0 & -\cos\rho \\ 0 & -\sin\rho \end{bmatrix}$$

In the following, we shall note  $T_1$ ,  $T_2$  respectively the first and second columns of  $^{C}T_{R}$ .

Similarly to the position-based path follower, the image-based path follower also utilizes a row a column primitive controllers. However, in this case, the controllers are based on the reference path point image features instead of its 3D features.

#### Row controller

The task of the image-based row controller is to drive  $(X, \Theta)$  to a desired set point  $(\hat{X}, \hat{\Theta})$  under constraint  $Y = \text{const} = Y^*$  (i.e., D is constrained to a pixel row in the

image plane). Since  $\dot{Y} = 0$ , the system state equations are:

$$\begin{bmatrix} \dot{X} \\ \dot{\Theta} \end{bmatrix} = A_c u_1 + B_c u_2 \tag{3.12}$$

where:

$$A_c = \begin{bmatrix} L_X \\ L_\Theta \end{bmatrix} T_1 \qquad B_c = \begin{bmatrix} L_X \\ L_\Theta \end{bmatrix} T_2$$

When  $B_c \neq 0$ , the system is controllable, and we select as control law:

$$u_2 = -B_c^+ \left( \left[ \begin{array}{c} \lambda_X e_X \\ \lambda_\Theta e_\Theta \end{array} \right] + A_c u_1 \right)$$
(3.13)

where  $e_X = X - \hat{X}$  and  $e_{\Theta} = \Theta - \hat{\Theta}$  are the state errors defined in the image plane, and  $\lambda_X$ ,  $\lambda_{\Theta}$  are given positive gains.

#### Column controller

The task of the image-based column controller is to drive  $(Y, \Theta)$  to a desired set point  $(\hat{Y}, \hat{\Theta})$  under constraint  $X = \text{const} = X^*$  (i.e., D is constrained to a pixel column in the image plane). Since  $\dot{X} = 0$ , the system state equations are:

$$\begin{bmatrix} \dot{Y} \\ \dot{\Theta} \end{bmatrix} = \bar{A}_c u_1 + \bar{B}_c u_2 \tag{3.14}$$

where:

$$\bar{A}_c = \begin{bmatrix} L_Y \\ L_\Theta \end{bmatrix} T_1 \qquad \quad \bar{B}_c = \begin{bmatrix} L_Y \\ L_\Theta \end{bmatrix} T_2$$

When  $\bar{B}_c \neq 0$  the system is controllable, and we select as control law:

$$u_2 = -\bar{B}_c^+ \left( \left[ \begin{array}{c} \lambda_Y e_Y \\ \lambda_\Theta e_\Theta \end{array} \right] + \bar{A}_c u_1 \right)$$
(3.15)

where  $e_Y = Y - \hat{Y}$  and  $e_{\Theta} = \Theta - \hat{\Theta}$  are the state errors defined in the image plane, and  $\lambda_Y$ ,  $\lambda_{\Theta}$  are given positive gains.

control scheme	posi	image-based		
primitive controller	row	column	row	column
$\mathcal{X}_1$	x	$\bar{x}$	X	Y
$\mathcal{X}_2$	$e_{ heta}$	$ar{e}_{ heta}$	Θ	Θ
$\mathcal{A}_1$	$\tan e_{\theta}$	$\tan \bar{e}_{\theta} \cos \beta - \sin \beta$	$L_X T_1$	$L_Y T_1$
$\mathcal{A}_2$	$-\frac{c_d}{\cos e_{\theta}}$	$-\frac{c_d\coseta}{\cosar{e}_ heta}$	$L_{\Theta}T_1$	$L_{\Theta}T_1$
$\mathcal{B}_1$	$y^* + x \tan e_{\theta}$	$y^* + \bar{x} \tan \bar{e}_{\theta}$	$L_X T_2$	$L_Y T_2$
$\mathcal{B}_2$	$1 - \frac{c_d x}{\cos e_\theta}$	$1 - \frac{c_d \bar{x}}{\cos \bar{e}_{\theta}}$	$L_{\Theta}T_2$	$L_{\Theta}T_2$
$\mathcal{G}_1$	$\lambda_x$	$ar{\lambda}_x$	$\lambda_X$	$\lambda_Y$
$\mathcal{G}_2$	$\lambda_{ heta}$	$ar{\lambda}_{ heta}$	$\lambda_{\Theta}$	$\lambda_{\Theta}$
$\mathcal{E}_1$	$x - \hat{x}$	$\bar{x} - \hat{\bar{x}}$	$X - \hat{X}$	$Y - \hat{Y}$
$\mathcal{E}_2$	$e_{\theta} - \hat{e}_{\theta}$	$ar{e}_{ heta} - \hat{ar{e}}_{ heta}$	$\Theta - \hat{\Theta}$	$\Theta - \hat{\Theta}$

Table 3.1: Components of:  $\mathcal{X}$ ,  $\mathcal{A}$ ,  $\mathcal{B}$ ,  $\mathcal{G}$ , and  $\mathcal{E}$  for the four controllers

# 3.3 Stability analysis

The stability analysis has been carried out for both control schemes (position-based and image-based) by using a Lyapunov-based approach. Note that the four state equations (3.6), (3.9), (3.12) and (3.14) can be generally written:

$$\dot{\mathcal{X}} = \mathcal{A}u_1 + \mathcal{B}u_2 \tag{3.16}$$

and, similarly, when  $\mathcal{B} \neq 0^7$ , the four control laws (3.7), (3.10), (3.13), and (3.15) can be generally expressed as:

$$u_2 = -\mathcal{B}^+ \left(\mathcal{G}\mathcal{E} + \mathcal{A}u_1\right) \tag{3.17}$$

with  $\mathcal{X} = [\mathcal{X}_1 \ \mathcal{X}_2]^T$ ,  $\mathcal{A} = [\mathcal{A}_1 \ \mathcal{A}_2]^T$ ,  $\mathcal{B} = [\mathcal{B}_1 \ \mathcal{B}_2]^T$ , and  $\mathcal{E} = [\mathcal{E}_1 \ \mathcal{E}_2]^T$  two-dimensional column vectors, and:

$$\mathcal{G} = \left[ \begin{array}{cc} \mathcal{G}_1 & 0 \\ 0 & \mathcal{G}_2 \end{array} \right]$$

The components of  $\mathcal{X}$ ,  $\mathcal{A}$ ,  $\mathcal{B}$ ,  $\mathcal{G}$  and  $\mathcal{E}$  for the four controllers are recalled in Table 3.1. Note that, as mentioned in Sect. 3.2, for the two primitive image-based controllers, as opposed to the position-based controllers, these variables are independent from  $c_d$ .

<sup>&</sup>lt;sup>7</sup>We don't manage singularity  $\mathcal{B} = 0$ , since it is extremely unlikely to occur in practice.

Hence, the following stability analysis is valid for all four controllers. Let us consider the quadratic Lyapunov function candidate:

$$\mathcal{V} = \frac{|\mathcal{E}|^2}{2}$$

Taking the time derivative of this function along a solution of the closed-loop system gives:

$$\dot{\mathcal{V}} = \mathcal{E}^T \dot{\mathcal{X}}$$

Using (3.16) and (3.17) leads to:

$$\dot{\mathcal{V}} = \mathcal{E}^T \left( \mathcal{A} u_1 - \mathcal{B} \mathcal{B}^+ \left( \mathcal{G} \mathcal{E} + \mathcal{A} u_1 \right) \right)$$

If we set  $\mathcal{G}_1 = \mathcal{G}_2 = \mathcal{G}^* > 0$ , since  $u_1 > 0$ ,  $\dot{\mathcal{V}}$  is negative semidefinite if and only if:

$$\frac{\mathcal{E}^{T}\left(\mathcal{A}-\mathcal{B}\mathcal{B}^{+}\mathcal{A}\right)}{\mathcal{E}^{T}\mathcal{B}\mathcal{B}^{+}\mathcal{E}} < \frac{\mathcal{G}^{*}}{u_{1}}$$
(3.18)

To verify the Lyapunov sufficient condition (3.18), the robot kinematic constraint on the maximum applicable curvature  $c_M$  must be analyzed, since it imposes a constraint on the maximum applicable gain  $\mathcal{G}^*$ . In fact, replacing (3.17) in (1.11), gives:

$$-c_M + \mathcal{B}^+ \mathcal{A} < -\frac{\mathcal{G}^*}{u_1} \mathcal{B}^T \mathcal{E} < c_M + \mathcal{B}^+ \mathcal{A}$$

This equation can be used to derive a sufficient condition for (3.18):

$$\left| \frac{\mathcal{E}^T \left( \mathcal{A} - \mathcal{B} \mathcal{B}^+ \mathcal{A} \right)}{\mathcal{E}^T \mathcal{B}} + \mathcal{B}^+ \mathcal{A} \right| < c_M \tag{3.19}$$

In (3.19) we have expressed a sufficient condition for asymptotic stability as a condition on the maximum applicable curvature  $c_M$ , hence on the robot kinematic model. This condition is also determined by the path characteristics, which must be compliant with the robot nonholonomic constraint. Condition (3.19) will be verified numerically, depending on the controller used, on the robot parameters and on the desired states, as will be shown in the next section.

# 3.4 Experimental setup

In the following section, we report the simulated and real experimental results obtained by applying the two proposed PF control schemes. All experiments have been carried out with a CyCab. CyCabs are 4 wheel drive, 4 wheel steered intelligent vehicles designed to carry two passengers. In our CyCab, all computations except the low-level control have been executed on a laptop with a 2 GHz Centrino processor. A 70° field of view, forward looking, B&W Marlin F-131B camera is mounted on the robot. The robot is used in car-like mode (i.e., only the front wheels are used for steering), and the camera is used in auto shutter mode, with image resolution  $320 \times 240$  pixels. The maximum curvature constraint (1.10) must be considered. In particular, for CyCab,  $\phi_M = 0.40$  rad and L = 1.21 m; thus,  $c_M = 0.30$  m<sup>-1</sup>.

The system has been coarsely calibrated, and we obtained:  $f_X = f_Y = 240$  pixels,  $\rho = 0.545$  rad,  $t_y = 550$  mm and  $t_z = 1625$  mm.

The applicable steering angle  $\phi$  used to control CyCab is derived from the angular speed  $u_2$  (calculated using either (3.7), (3.10), (3.13), or (3.15)):

$$\phi = \operatorname{ATAN} \frac{Lu_2}{u_1} \tag{3.20}$$

In all the simulations and experiments, we set  $u_1 = 0.2 \text{ ms}^{-1}$ . Short video clips of the simulations and experiments can be viewed on the web site: http://www.dis.uniroma1.it/~labrob/research/VBPF.html).

## 3.5 Simulations

The possibility of testing the proposed path following scheme in a simulated environment has been crucial from the very early stages of this work. To this end, we have adopted Webots, a mobile robot simulation environment developed by Cyberbotics, which is used by many universities worldwide for modeling and controlling mobile robots. In Webots, a complete mobile robotics setup can be defined, by creating complex environments and equipping robots with sensors and actuators. One can define all physical properties for each object, and the simulated robot can be programmed with the same development environment as the real one. By using Webots, it is possible to debug the algorithms effectively and to test them without endangering the real robot. Besides, the problem of tuning all the gains can be easily solved in the simulation before porting on the CyCab.

In Webots, we have designed a simulated robot with the same kinematic and sensorial characteristics of CyCab. A circular path of radius 12.5 m (i.e.,  $c_d = \text{const}$ 



Figure 3.3: Position-based simulation. The robot positions and corresponding processed images at consecutive time frames are shown during PF.

 $= 0.08 \text{ m}^{-1}$ ) has been drawn in the simulation environment. The two control schemes (position-based and image-based) have been simulated in Webots starting from various initial configurations.

Consider the initial configuration with the path intersecting the right pixel column (see Fig. 3.3, top left). A switching strategy combining the column and row controllers is used. Initially, the column controller (respectively (3.10) for the position-based simulations, and (3.15) for the image-based simulations) is used to drive D along the right pixel column of the image to the bottom right corner. For the position-based controller, we use  $\bar{\lambda}_x = \bar{\lambda}_{\theta} = 7.0$ . For the image-based controller, we use  $\bar{\lambda}_Y = \bar{\lambda}_{\Theta} = 0.5$ . Afterwards, the row controller (respectively (3.7) for the position-based simulations,



Figure 3.4: Evolution of relevant variables during simulated PF with path initially intersecting the right pixel column. Top: applied steering angle  $\phi$  in rad (purple: position-based, green: image-based). Center: state errors  $\mathcal{E}_1$  (red, in m) and  $\mathcal{E}_2$  (blue, in rad) for the position-based column controller (left) and row controller (right). Bottom: state errors  $\mathcal{E}_1^*$  (red, non-dimensional) and  $\mathcal{E}_2$  (blue, in rad) for the image-based column controller (left) and row controller (right).

and (3.13) for the image-based simulations) is used to drive D along the bottom row of the image plane to:  $\hat{X} = \hat{\Theta} = 0$ . An adaptive gain is used. This design choice provides fast convergence for large error values, while avoiding overshoot for small errors. For the position-based simulations, we use:  $\lambda_x = \lambda_\theta = 5 \exp^{-10||\mathcal{E}||} + 5$  with  $||\mathcal{E}|| = \sqrt{e_x^2 + e_\theta^2}$ the error norm. For the image-based simulations, we use:  $\lambda_X = \lambda_\Theta = 3 \exp^{-10||\mathcal{E}||}$ with  $||\mathcal{E}|| = \sqrt{e_X^2 + e_\Theta^2}$  the error norm. With both control schemes, the simulated robot is able to successfully follow the path. For the position-based simulation, the robot positions and processed images at consecutive time frames while Cycab follows the path are shown in Fig. 3.3. The evolution of relevant variables (steering angle and



Figure 3.5: Initial conditions used in the path following experiments. The point D and tangent  $\Gamma$  derived by image processing are indicated respectively by a red circle and a red line.

state errors) for the two control schemes, is plotted in Fig. 3.4. For the image-based controller, instead of state errors  $\mathcal{E}_1 = e_X$  and  $\mathcal{E}_1 = e_Y$ , we have respectively plotted the scaled values  $\mathcal{E}_1^* = \frac{e_X}{2X_M}$  for the row controller, and  $\mathcal{E}_1^* = \frac{e_Y}{2Y_M}$  for the column controller ( $2X_M$  and  $2Y_M$  respectively denote the image width and height). Note that the steering angle  $\phi$ , as well as the state errors  $\mathcal{E}_1^*$  and  $\mathcal{E}_2$ , oscillate more in the image-based simulations, than in the position-based simulations. This occurs because the position-based controller utilizes the path curvature for feedback control, which is not utilized in the image-based scheme: hence, the oscillations in the image-based steering angle are necessary to compensate the state variations introduced by the path curvature. Note that at the end of the first phase (after the column controllers have been applied) the errors on the tangent orientation  $\mathcal{E}_2$  have not reached 0. This is due to the switching condition, which is imposed only by the error on the point position  $\mathcal{E}_1$ . Nevertheless, for both control schemes, when the row controller is applied, the tracking errors converge, and the mean value of the steering angle at steady state is as expected from (3.20): ATAN  $Lc_d = 0.096$  rad.

# 3.6 Experiments

After the Webots simulations, the two control schemes have been tested on the real CyCab in a series of outdoor experiments. The path used in the experiments is composed of two straight lines of length 6 m joined by a 60° arc of circle of radius 10 m (i.e.,  $c_d = \pm 0.1 \text{ m}^{-1}$ , with the sign of  $c_d$  depending on the path direction to be



Figure 3.6: Position-based stability loci of the state variables  $(x, \bar{x} \text{ in m}, e_{\theta}^t, e_{\theta}, \bar{e}_{\theta} \text{ in rad})$  that verify the Lyapunov sufficient asymptotic stability condition (cyan) for  $c_d = 0$  (above) and  $c_d = \pm 0.1 \text{ m}^{-1}$  (below), and for: top row controller (left), right column controller (center), and bottom row controller (right). The desired states are indicated with the blue cross.

followed by the robot). The path features are derived by tracking straight lines and arcs of parabola with the ViSP visual servoing software [21]. The tracker must be initialized by clicking on five path points oriented in the desired path direction.

For each of the two control schemes, experiments with three different initial conditions have been carried out. The three experiments are enumerated below, and the corresponding initial conditions are shown in Fig. 3.5 (left to right).

- 1. Cycab is initially positioned on the path with the correct orientation and small initial error. Hence, D is on the bottom pixel row of the image plane (see Fig. 3.5, left). The row controller is used to drive D to  $\hat{X} = \hat{\Theta} = 0$ .
- 2. CyCab is initially near the path, with D on the right pixel column of the image plane (see Fig. 3.5, center). A switching strategy combining both row and column controllers is used. Initially (phase 2.1), the column controller is used to drive Dalong the right pixel column of the image to the bottom right corner. Afterwards



Figure 3.7: Image-based stability loci of the state variables  $(X, Y \text{ in pixels}, \Theta, \Theta^t \text{ in rad})$  that verify the Lyapunov sufficient asymptotic stability condition (pink) for: top row controller (left), right column controller (center), and bottom row controller (right). The desired states are indicated with the black cross.

(phase 2.2), the row controller is used to drive D along the bottom row of the image plane to  $\hat{X} = \hat{\Theta} = 0$ .

3. CyCab is initially far from the path, with D on the top pixel row of the image plane (see Fig. 3.5, right). Initially (phase 3.1), the row controller is used to drive point D to a lateral pixel column of the image plane. Afterwards (phase 3.2), the column controller is used to drive D along the right pixel column of the image to the bottom right corner. Finally (phase 3.3), the row controller is used to drive D along the bottom row of the image plane to  $\hat{X} = \hat{\Theta} = 0$ .

In order to verify the robustness of the two controllers, the three experiments have been repeated by considering a random calibration error of either +10% or -10% on each of the five camera parameters in  $\mathcal{P}$ .

For the calibrated camera experiments, we have numerically verified the system sufficient asymptotic stability condition (3.19) as the system state variables evolve. The state loci that verify condition (3.19) are represented in Fig. 3.6 for the position-based controllers and in Fig. 3.7 for the image-based controllers. In the position-based case, as mentioned in Sect. 3.3, the system state and the controller depend on the curvature  $c_d$ . In our experimental setup, the value of  $c_d$  can be 0 (for the straight path portions) or  $\pm 0.1 \text{ m}^{-1}$  (for the arc of circle). Hence, in Fig. 3.6, the state loci are represented for  $c_d = 0$  (above) and  $c_d = \pm 0.1 \text{ m}^{-1}$  (below). Besides, in the proposed experiments, three instances of the primitive controllers are used:



Figure 3.8: First position-based experiment: Cycab is initially positioned on the path with small initial error. The robot positions and corresponding processed images at consecutive time frames are shown during PF.

- bottom row controller (throughout the first experiment and during phases 2.2 and 3.3 of the two other experiments),
- right column controller (during phases 2.1 and 3.2),
- top row controller (during phase 3.1).

Hence, in Fig. 3.6 and 3.7, the state loci are represented for each of these three controllers: top row (left in the two figures), right column (center), and bottom row (right).

For the top row controllers, the range of  $\mathcal{X}_2$  (i.e., the range of  $e_{\theta}$  for the



Figure 3.9: Evolution of relevant variables during the first position-based experiment. Top: errors  $\mathcal{E}_1$  in m, and  $\mathcal{E}_2$ , in rad (red and blue: correct camera calibration, pink and cyan: coarse calibration). Bottom:  $c_d$  in m<sup>-1</sup> (purple) and  $\phi$  in rad (green: correct camera calibration, black: coarse calibration).

position-based, and of  $\Theta$  for the image-based cases) is discontinuous:  $]-\pi, -\frac{\pi}{2}[\cup]\frac{\pi}{2}, \pi]$ . Thus, the top row loci are represented by using the orientation of  $y_d$  with respect to -y (noted  $e_{\theta}^t$ ) in the position-based case and the orientation of  $\Gamma$  with respect to Y (noted  $\Theta^t$ ) in the image-based case.

The desired state values are also indicated in the two figures for each controller. Note that in all cases, the desired state values belong to the loci where the asymptotic stability condition is verified. Moreover, the figures show that, for the right column and the bottom row controllers, the loci area is much smaller in the image-based, than in the position-based case. In our opinion, this is due to the fact that the position-based controller takes into account the path curvature  $c_d$ , which is not considered in the image-based case. In Sections 3.6.1 and 3.6.2, the loci of Fig. 3.6 and 3.7 will be used to verify the asymptotic stability condition on the system state during the experiments.

#### 3.6.1 Position-based experiments

In the first position-based experiment (shown in Fig. 3.8), D is on the bottom pixel row of the image plane. The row controller (3.7) is used with  $\mathcal{G}^* = 0.3$ . The evolution



Figure 3.10: Second position-based experiment: D is initially on the right pixel column of the image plane.

of the relevant variables during the experiment is shown in Fig. 3.9. The robot is able to successfully follow the path, and the tracking errors  $e_x$  and  $e_\theta$  (respectively red and blue curves) are low throughout the experiment. At the end of the experiment, both errors are below 0.10. Both errors increase when the robot reaches the discontinuity in the path curvature (frame 335). Correspondingly,  $\phi$  increases in order to compensate for the error and enables CyCab to follow the curve. Using Fig. 3.6, we verify that throughout the experiment, the state variables verify the stability condition.

In the second experiment (shown in Fig. 3.10), CyCab is initially near the path, with D on the right pixel column of the image plane. During phase 2.1, the column controller (3.10) is used, with adaptive gain:  $\mathcal{G}^* = 0.26 \exp^{-15||\mathcal{E}||} + 0.24$ . Then (phase



Figure 3.11: Evolution of relevant variables during the second position-based experiment. Top: errors  $\mathcal{E}_1$  (red, in m) and  $\mathcal{E}_2$  (blue, in rad) with correct camera calibration for phases 2.1 (left) and 2.2 (right). Center: same errors ( $\mathcal{E}_1$  in pink, and  $\mathcal{E}_2$  in cyan) with coarse camera calibration. Bottom:  $c_d$  in m<sup>-1</sup> (purple) and  $\phi$  in rad (green: correct camera calibration, black: coarse calibration).

2.2), the row controller (3.7) is used with:  $\mathcal{G}^* = 0.34 \exp^{-30||\mathcal{E}||} + 0.02$ . The state errors are plotted in the top of Fig. 3.11, for phases 2.1 (left) and 2.2 (right). The path curvature  $c_d$  (purple) and steering angle  $\phi$  (green) are plotted in the bottom graph of Fig. 3.11. The robot is able to successfully follow the path, and the tracking errors converge during both phases. Similarly to the first experiment, while the robot is on the path curve (i.e., from frame 305), the error convergence rate is low. Nevertheless, the steering angle increases to enable the robot to follow the curve and at the end of the experiment both state errors are zeroed. Using Fig. 3.6, we verify that throughout the experiment, the state variables verify the stability condition.

In the third experiment (shown in Fig. 3.12), CyCab is initially far from the path, with D on the top pixel row of the image plane. During phase 3.1, the row controller



Figure 3.12: Third position-based experiment: the initial error is large (D is on the top pixel row of the image plane).

(3.7) is used to drive point D to a lateral pixel column of the image plane. Since initially  $-\frac{\pi}{2} < e_{\theta} < -\pi$ , the controller selects the right side column. We use  $\mathcal{G}^* = 24$ . Afterwards (phase 3.2), the column controller (3.10) is used, with  $\mathcal{G}^* = 0.4$ . Finally (phase 3.3), the row controller (3.7) is used with:  $\mathcal{G}^* = 0.34 \exp^{-30||\mathcal{E}||} + 0.02$ . The state errors are plotted in the top of Fig. 3.13, for phases 3.1 to 3.3 (left to right graphs). The path curvature  $c_d$  (purple) and steering angle  $\phi$  (green) are plotted in the bottom graph of Fig. 3.13. Once again, the robot is able to successfully follow the path and the tracking errors converge. The controller initially saturates the steering angle  $\phi$  to its maximum value  $\phi_M = 0.40$  rad in order to enable the robot to reach the path.



Figure 3.13: Evolution of relevant variables during the third position-based experiment. Top: errors during phases 3.1 to 3.3 (left to right).  $\mathcal{E}_1$  (in m) and  $\mathcal{E}_2$  (rad) are plotted (red and blue: correct camera calibration, pink and cyan: coarse calibration). The iteration steps with state variables not verifying the stability condition are highlighted in yellow. Bottom:  $c_d$  in m<sup>-1</sup> (purple) and  $\phi$  in rad (green: correct camera calibration, black: coarse calibration).

At the end of phase 3.3, both errors are below 0.10. The iteration steps with state variables not meeting the asymptotic stability condition (i.e., values of  $\mathcal{X}$  outside the loci of Fig. 3.6) are highlighted in yellow in Fig. 3.13. The plots show that during most of phase 3.2 and during the beginning of phase 3.3, condition (3.19) is not verified. Nevertheless, the system is able to converge, as outlined above.

The three position-based experiments have been repeated by considering a calibration error on the camera parameters. The evolution of the relevant variables in the coarse calibration experiments is also shown in Fig. 3.9, 3.11, and 3.13 (pink and cyan for the errors, black for  $\phi$ ), for comparison with the calibrated camera experiments. The robot is able to successfully follow the path in all three cases. However, the convergence rate is lower than in the calibrated camera experiments. In particular, in the second experiment, the controller performance is considerably worsened (see Fig. 3.11, center and bottom). Firstly, the column controller convergence is much



Figure 3.14: First image-based experiment: Cycab is initially positioned on the path with small initial error.

smaller than in the calibrated experiment (850 instead of 175 iterations are required for switching from column to row control). Secondly, at the end of phase 2.2,  $e_x$  is higher than in the calibrated experiment (0.35 m instead of 0.05 m). Finally, note that the values of the steering angle oscillate much more than in the calibrated experiment.

#### 3.6.2 Image-based experiments

In the first image-based experiment (shown in Fig. 3.14), D is on the bottom pixel row of the image plane. The row controller (3.13) is used, with:  $\mathcal{G}^* = 0.18 \exp^{-30||\mathcal{E}||} + 0.02$ . The evolution of the relevant variables during the experiment is shown in Fig. 3.15. Instead of  $e_X$ , we have plotted the scaled value  $\mathcal{E}_1^* = \frac{e_X}{2X_M}$ , where  $2X_M$  denotes the



Figure 3.15: Evolution of relevant variables during the first image-based experiment. Top: errors  $\mathcal{E}_1^*$  (non-dimensional), and  $\mathcal{E}_2$  (in rad) are plotted (red and blue: correct camera calibration, pink and cyan: coarse calibration). Bottom:  $c_d$  in m<sup>-1</sup> (purple) and  $\phi$  in rad (green: correct camera calibration, black: coarse calibration).

image width in pixels. The robot is able to successfully follow the path and the tracking errors are low throughout the experiment. At the end of the experiment, both errors are below 0.03. As in the position-based experiment, both errors increase when the robot reaches the discontinuity in the path curvature (frame 335), and correspondingly,  $\phi$  increases in order to compensate for the error. Using Fig. 3.7, we verify that throughout the experiment, the state variables verify the stability condition.

In the second experiment (shown in Fig. 3.16), CyCab is initially near the path, with D on the right pixel column of the image plane. During phase 2.1, the column controller (3.15) is used, with:  $\mathcal{G}^* = 0.98 \exp^{-3.6||\mathcal{E}||} + 0.05$ . Then (phase 2.2), the row controller (3.13) is used with:  $\mathcal{G}^* = 0.18 \exp^{-30||\mathcal{E}||} + 0.02$  (as in the first experiment). The state errors are plotted in the top of Fig. 3.17, for phases 2.1 (left) and 2.2 (right). Instead of  $e_X$  and  $e_Y$ , we have respectively plotted the scaled values  $\mathcal{E}_1^* = \frac{e_X}{2X_M}$  for phase 2.1, and  $\mathcal{E}_1^* = \frac{e_Y}{2Y_M}$  for phase 2.2 ( $2X_M$  and  $2Y_M$  respectively denote the image width and height). The path curvature  $c_d$  (purple) and steering angle  $\phi$  (green) are plotted in the bottom graph of Fig. 3.17. The robot is able to successfully follow the path, and the tracking errors converge during both phases. At the end of the experiment both state errors are zeroed. Note the completely different initial trend of  $\phi$ , as compared



Figure 3.16: Second image-based experiment: D is initially on the right pixel column of the image plane.

to the position-based experiment (shown in Fig. 3.11, bottom). The iteration steps with state variables not verifying the asymptotic stability condition (i.e., values of  $\mathcal{X}$  outside the loci of Fig. 3.7) are highlighted in yellow in Fig. 3.17. The plots show that, throughout phase 2.1 and during the beginning of phase 2.2, condition (3.19) is not verified. Nevertheless, the system is able to converge.

In the third experiment (shown in Fig. 3.18), CyCab is initially far from the path, with D on the top pixel row of the image plane. The evolution of the relevant variables during the experiment is shown in Fig. 3.19. Once again, in the graphs, the values of  $\mathcal{E}$  have been scaled by the image size. During phase 3.1, the row controller (3.13) is applied, to drive point D to a lateral pixel column of the image plane. Since initially



Figure 3.17: Evolution of relevant variables during the second image-based experiment. Top: errors during phases 2.1 (left) and 2.2 (right).  $\mathcal{E}_1^*$  (non-dimensional) and  $\mathcal{E}_2$  (in rad) are plotted (red and blue: correct camera calibration, pink and cyan: coarse calibration). The iteration steps with state variables not verifying the stability condition are highlighted in yellow. Bottom:  $c_d$  in m<sup>-1</sup> (purple) and  $\phi$  in rad (green: correct camera calibration, black: coarse calibration).

 $-\frac{\pi}{2} < \Theta < -\pi$ , the controller selects the right side column. We use:  $\mathcal{G}^* = 10$ . Afterwards (phase 3.2), the column controller (3.15) is applied, with  $\mathcal{G}^* = 4.0$ . Finally (phase 3.3), the row controller (3.15) is used with:  $\mathcal{G}^* = 0.18 \exp^{-30||\mathcal{E}||} + 0.02$ . The experiment fails during phase 3.3: the error  $e_X$  diverges and the path exits the field of view. Tests with other values of  $\mathcal{G}^*$  are also unsuccessful. The reason is the failure of asymptotic stability condition (3.19) during the experiment. The iteration steps with state variables not verifying (3.19) are highlighted in yellow in Fig. 3.19. The plots show that, during most of phase 3.2 and throughout phase 3.3, the asymptotic stability condition is not verified. Although during phase 3.2 the errors converge in spite of this, during phase 3.3 the experiment fails. As we mentioned throughout this article, a flaw of the image-based control law is that it does not take into account the curvature  $c_d$ . This is particularly relevant in this experiment, and causes, in our opinion, the failure. In fact (see the bottom left snapshot of Fig. 3.18), the robot switches to phase 3.3 with a large error on  $\mathcal{E}_2$ , in a critically curve portion of the path. In contrast with the position-based scheme, in this case, the error dynamics cannot be controlled since the


Figure 3.18: Third image-based experiment: the initial error is large (D is on the top pixel row of the image plane). The experiment fails.

curvature is not used to compute the feedback law. However, the initial state for phase 3.3 (which causes the failure) cannot be changed. In fact, the gains  $\mathcal{G}^*$  during phases 3.1 and 3.2, must be chosen so that the controller saturates the steering angle  $\phi$  to its maximum value  $\phi_M = 0.40$  rad, and thus determine the initial state of phase 3.3.

The two successful image-based experiments (i.e., first and second experiments) have been repeated by considering a calibration error on the camera parameters. The evolution of the relevant variables in the coarse calibration experiments is also shown in Fig. 3.15 and 3.17 (pink and cyan for the errors, black for  $\phi$ ), for comparison with the calibrated camera experiments. The robot is able to successfully follow the path in both cases. The convergence rate is slightly lower than in the



Figure 3.19: Evolution of relevant variables during the third image-based experiment with correct camera calibration. Left to right:  $c_d$  (purple, in m<sup>-1</sup>) with  $\phi$  (green, in rad), and errors  $\mathcal{E}_1^*$  (red, non-dimensional) and  $\mathcal{E}_2$  (blue, in rad) during phases 3.1 to 3.3. The iterations steps with state variables not verifying the stability condition are highlighted in yellow.

calibrated camera experiments. However, in particular for the second experiment, the image-based approach outperforms the position-based approach when the camera is coarsely calibrated.

#### 3.7 Conclusions and future work

In this chapter, we presented two visual servoing control schemes (position-based and image-based) enabling nonholonomic mobile robots with a fixed pinhole camera to follow a continuous path on the ground. The controllers utilize only a small set of path features extracted from the image plane, without using the complete geometric representation of the path. The features are: the position of a path point, and the path tangent orientation at that point. For the position-based controller, the path curvature at that point is also utilized. A major contribution of this work is that both approaches can be used in general initial conditions, thanks to a switching strategy between two primitive controllers. A Lyapunov-based stability analysis has been carried out. The performance of both controllers has been experimentally validated on a car-like robot equipped with a pinhole camera starting from three different initial conditions. The scheme robustness was also verified, by adding camera model errors in all the experiments.

The experiments point out the main characteristics of the two approaches for the specific task of path following. The image-based primitive controllers have smaller

stability zones than the corresponding position-based primitive controllers. As a consequence, one of the three experiments fails when using the image-based approach and succeeds with the position-based approach. On the other hand, for the two other experiments, the image-based approach is more effective (a smoother control input  $\phi$  is needed to achieve the task), and robust to camera calibration errors.

These results confirm the properties of the two control schemes. The image-based controller is less effective when the initial error is large, since it does not rely on the curvature measure, which, acting as a second derivative, fosters the prediction of the error dynamics. On the other hand, by using the path curvature measure, which is typically more biased than path position and path tangent orientation measures, the position-based control law is less smooth and less robust to calibration errors.

## Chapter 4

# Vision-based path following for a legged robot with actuated pinhole camera and its application in the ASPICE project

In this chapter, we present the design and implementation of a vision-based path following scheme which has been integrated in the ASPICE (Assistive System for Patient's Increase of Communication, ambient control and mobility in absence of muscular Effort) project [11].

One central feature of the ASPICE system is the possibility for the user to remotely control the motion of a mobile robot (a Sony AIBO) by means of various input devices, including a Brain-Computer Interface (BCI). While moving, the robot should assist the user by monitoring the environment and by communicating specific requests to the caregiver. Depending on the residual abilities of the user, as well as on the desired task, it is possible to choose between three different navigating modes for controlling the robot motion: *Single step*, *Semi-autonomous* and *Autonomous* navigation modes. In this chapter, we focus on the development of the autonomous navigation mode, which is based on a vision-based path following scheme. The other navigation modes are simply outlined in this chapter for the purpose of comparison with the autonomous mode. They will be described in detail in the Chapter 5, along with other aspects of ASPICE.

The chapter is organized as follows. In Sect. 4.1, the architecture of the ASPICE system is briefly illustrated. In Sect. 4.2, the main features of the AIBO robot are described. Sect. 4.3 presents the primitives developed for the robot PF framework, at perception and motion levels. The robot visual path following scheme that we implemented on the basis of the ASPICE requirements is outlined in Sect. 4.4. The experiments are reported in Sect. 4.5. In the conclusion, we summarize the results.

#### 4.1 The ASPICE project

#### 4.1.1 Overview

The ASPICE project received in 2004 a two-year funding grant from TELETHON, an italian medical research charity foundation. The project involves three partners, including the Clinical Neurophysiopathology Laboratory of the Fondazione Santa Lucia IRCCS and the Robotics Lab of the University of Rome "La Sapienza".

The project is aimed at the development of a technological aid which allows neuromotor-disabled users to improve or recover their mobility and communication within the surrounding environment. The project is particularly addressed towards those patients whose residual muscular strength is low and who is bed-ridden because of practical obstacles or security concerns (see [11] for more details). Hence, the major requirements are: adaptability to different levels of disability, low cost, and robustness to the setting. Depending on the user requirements, the assistive device will be a program running on a common low-power PC, on a palmtop, or on a powerful workstation.

The ASPICE architecture, with input and output devices, is summarized in Fig. 4.1. Some key elements of the system are:

- a variety of input devices for easy access to the Control Unit: these include standard input devices (mouse, joystick, eye tracker, voice recognition) as well as a Brain-Computer Interface;
- the Control Unit, which receives signals from the input devices through a Graphic



Figure 4.1: The ASPICE architecture.

User Interface (GUI) and converts them into commands that drive the output devices (either the domotic appliances or a mobile robot);

- the mobile robot;
- a number of domotic appliances, which must comply with the patient's need for ambient control (e.g., TV, lights, video camera, telephone, personal computer);
- visual feedback (either through the fixed video camera or through the robot vision system) to provide the user with an increased sense of presence in the environment.

The Control Unit contains drivers for all output devices; in some cases, previously existing drivers are utilized, whereas in other cases (e.g., the mobile robot) the driver has been designed "ad hoc" for the specific system. Note that all the signals between the input devices and the Control Unit, and between the latter and the output devices (including visual feedback) are transmitted over a wireless connection. In the remainder of this section, the BCI which is used as input device and the Robot Driver that we implemented are briefly described.

#### 4.1.2 The robot driver

In any assistive robotics project, a major requirement is the user friendliness of the robotic platform. In fact, although in recent years users are becoming, on the average, more acquainted with technology, characteristics such as low cost, safety, and low request for maintenance are still fundamental needs of any biomedical robotic application. Moreover, clinicians have often emphasized the importance of working with a familiar, friendly-looking robot, in order to limit its psychological impact on patients [42]. In our case, these considerations led to the choice of the dog-like robot Sony AIBO ERS-7 (described in Sect. 4.2) for inclusion in the system. Besides, studies using AIBO to improve the quality of life, among elderly, have given good results [44].

AIBO should be driven around the user home with a small set of commands, depending on the residual abilities of the patient. It should also assist the impaired patient in visually monitoring the environment and in communicating with the caregiver. Partial autonomy should be implemented in order to avoid collisions with unexpected obstacles present in the environment. The robot range sensors are used to avoid obstacles, as we shall show in Chapter 5. Another requirement is that AIBO should be able to charge its battery when needed without any user intervention. As already stated, one of the objectives of the ASPICE project is compatibility with a variety of users and their level of disability. In light of this, three navigation modes have been developed: single step, semi-autonomous and autonomous mode. The user is expected to choose single step navigation when he/she wants to retain complete control of the robot motion; e.g., for fine motion in cluttered areas. In semi-autonomous navigation, the user specifies the main direction of motion, leaving to the robot the task of avoiding obstacles. Finally, in the autonomous navigation mode, only a target point in the environment is assigned by the user. The robot then travels to the target; this is useful for quickly reaching some important locations (a window, the front door, the kitchen). This mode of operation is expected to be particularly useful for severely impaired patients who are unable to send frequent commands. To implement the autonomous mode, we have designed a physical roadmap (shown in Fig. 4.2) to reach



Figure 4.2: The roadmap used in autonomous navigation mode. The ID labels of each coded square are indicated. Note that crossings appear larger than they are.

and connect all the relevant destinations in the experimental arena, and utilized a visual path following scheme that will be detailed further in this Chapter.

The roadmap is formed by streets and crossings, made by white adhesive tape, and laid on the ground. The perception primitives that will be described in Sect. 4.3.1 are used to identify the streets (i.e., straight white lines) and crossings (i.e., coded squares) while the motion primitives that will be described in Sect. 4.3.2 are used to drive the robot on the map.

Each navigation mode is associated to a GUI in the ASPICE Control Unit. The three GUIs are shown in Fig. 4.3. By selecting the corresponding button from the single step GUI, the user can control the direction of the step. From the semi-autonomous mode GUI, the user can select one of six directions – the same of the single step mode – or stop the robot. Instead, from the autonomous navigation mode GUI, each button



Figure 4.3: The ASPICE navigation GUIs: single step (above), semi-autonomous (center) and autonomous (below) modes. In each GUI, the home button brings back to the ASPICE main GUI.

that the user can select corresponds to a destination in the user apartment (here, the bedroom, the living room, the bathroom, and the kitchen).

#### 4.2 The robot platform: AIBO

The platform used in this work is a quadruped robot, Sony AIBO ERS-7, pictured in Fig. 4.4. AIBO is a very interesting low-cost robot, widely used for research and entertainment purposes. AIBO has been chosen in ASPICE for its familiar and friendly-looking aspect, since it has been shown that in assistive robotic applications, an important role is played by the robot's design, which should facilitate everyday interaction with the patients [42, 44]. Practical advantages in using legged robots have been outlined in Sect. 1.2.2. The robot is equipped with 20 actuated joints, a CMOS camera, two distance sensors (on the head and on the chest), an accelerometer, a stereo microphone, a MIDI speaker, a set of leds and pression sensors. A wireless LAN card enables remote control and debugging. The actuated joints are: 3 for each leg, 3 for the head (head tilt, head pan, and neck tilt), 2 for the tail, 1 for each ear and 1 for the mouth. AIBO's real-time operating system APERIOS runs a specialized



Figure 4.4: The Sony AIBO ERS-7 used in the ASPICE Project.

layer called OPEN-R, a cross-development environment based on C++. The robot behavior is programmed by loading all executable and configuration files on a memory stick which is read by the on-board processor. In spite of the above features, the AIBO robot presents many limitations, which made its use within the ASPICE project a real challenge. The most severe are the following:

- the closed hardware prevents the addition of sensors and/or actuators;
- since Sony does not release the code of its driver, we had to realize from scratch an *ad hoc* driver for this work;
- the head distance sensor and the CMOS camera move in accordance, making it impossible for the distance sensor to detect obstacles in directions other than the one pointed by the camera: a tradeoff between moving the head for video feedback and moving it for obstacle detection/avoidance had to be reached;
- the chest distance sensor is constrained to the robot body and peculiarly oriented, thus limiting its effective utility;
- vibrational and slipping effects during the quadruped gait cycle make odometric reconstruction very inaccurate in the long run;

• the variable attitude of AIBO during its gait precludes the use of an external sensory system (e.g., based on infrared triangulation with a detector placed on the robot) for solving the localization problem.

#### 4.3 Primitives

In order to utilize AIBO, specific primitives have been developed and integrated in the driver framework. The perception primitives have been designed to identify the visual landmarks on the roadmap, while the motion primitives are used to drive the robot on the map.

The three reference frames which will be used in this work are: the robot frame  $\mathcal{F}_{\mathcal{R}}$  (Fig. 4.7 and 4.6), the image frame  $\mathcal{F}_{\mathcal{I}}$  (Fig. 4.5), and the camera frame  $\mathcal{F}_{\mathcal{C}}$  (Fig. 4.6). For the definition of these frames, refer to Chapter 1. We also note the robot neck tilt, head pan, and head tilt joint angular positions respectively with:  $\varrho_h = [\varrho_{nt} \, \varrho_{hp} \, \varrho_{ht}]^T$ .

#### 4.3.1 Perception primitives

The features that the robot should perceive with the on-board camera are the landmarks that it needs for localization and path planning purposes. The visual landmarks that we use are straight white lines and coded squares placed on the floor. Thus, a *straight white line extractor* and a *coded square extractor* have been developed. Moreover, the visual landmarks should be located in sequential scenes. This task is accomplished by a *visual landmark tracker*.

#### Straight white line extractor

A requirement of the robot driver is straight white line extraction. In order to be independent from color classification, the straight white lines are detected by search on the luminance signal  $\mathcal{I}(X, Y)$ . Thus, line edges are searched at pixels with a strong variation of luminance with respect to that of adjacent pixels. For each pixel located in  $D = [X \ Y]^T$  the gradient of luminance  $\nabla \mathcal{I}(D)$  is computed, using the Roberts



Figure 4.5: Extracting edges (in yellow) for straight white line (left) and coded square (right) detection. The detected coded square center is marked in red and the dot centers are marked in cyan.

operator [66] as in [24]:

$$\mathcal{I}_{xy}(D) = \mathcal{I}(X+1, Y+1) - \mathcal{I}(X, Y)$$
  

$$\mathcal{I}_{-xy}(D) = \mathcal{I}(X+1, Y) - \mathcal{I}(X, Y+1)$$
  

$$|\nabla \mathcal{I}(D)| = \sqrt{\mathcal{I}_{xy}^2(D) + \mathcal{I}_{-xy}^2(D)}$$
  

$$\angle \nabla \mathcal{I}(D) = \operatorname{ATAN2}\left(\mathcal{I}_{xy}(D), \mathcal{I}_{-xy}(D)\right)$$
(4.1)

where  $|\nabla \mathcal{I}(D)|$  is the magnitude and  $\angle \nabla \mathcal{I}(D) \in (-\pi, \pi]$  is the direction of the pixel luminance gradient (with respect to line Y = -X and positive clockwise, see Fig. 4.5. Edges are then detected by applying a threshold test to  $|\nabla \mathcal{I}(D)|$ . We use a threshold  $\mathcal{I}^*$ dependent on the mean value (noted  $\mu_{|\mathcal{I}|}$ ) of  $|\mathcal{I}(D)|$  on the given image:  $\mathcal{I}^* = \mathcal{I}^*(\mu_{|\mathcal{I}|})$ . This adaptive thresholding makes the edge detection algorithm more robust to varying light conditions, as compared to similar works implemented in environments where light conditions had to be controlled. The threshold test may be written:

$$D \in \mathcal{D}_{e} \qquad \text{if } |\mathcal{I}(\mathbf{D})| \ge \mathcal{I}^{*}\left(\mu_{|\mathcal{I}|}\right)$$

$$D \notin \mathcal{D}_{e} \qquad \text{else} \qquad (4.2)$$

where  $\mathcal{D}_e$  is the set of image edge pixels (marked in yellow in Fig. 4.5).

Afterwards, by applying threshold tests to relative distances and to luminance gradient directions of the edge pixels belonging to  $\mathcal{D}_e$ , subsets of line pixels are derived. Indicating with  $N_{SWL}$  the total number of straight white lines extracted on the image, the line pixel subsets are noted:  $\mathcal{D}_{SWL,i}$   $(i = 1 \dots N_{SWL})$ . Each  $\mathcal{D}_{SWL,i}$  defines a line detected on the image frame, must contain at least  $n_{SWL,min}$  pixels. We note  $n_{SWL,i}$  the number of pixels contained in each line pixel subset  $\mathcal{D}_{SWL,i}$   $(n_{SWL,i} \ge n_{SWL,min}$  for each  $i = 1 \dots N_{SWL}$ ).

We tested several other edge detection algorithms (Sobel [67], Susan [73]), but the Roberts operator showed better results, although the aforementioned methods are more efficient for color space based extraction [78]. Besides, due to its low computation time, this line extraction method was preferred to the Hough Transform technique, which we also tested, and which is widely used for line detection in noisy images, with extensions also accounting for line connectivity and thickness, as in [82].

In conclusion, the straight white line extractor algorithm returns the coordinates of the pixels belonging to the  $N_{SWL}$  lines extracted on the image frame (Fig. 4.5):

$$[X_j Y_j]_{SWL,i}^T \in \mathcal{D}_{SWL,i}$$
  

$$j = 1, \dots, n_{SWL,i}$$
  

$$i = 1, \dots, N_{SWL}$$
  
(4.3)

#### Coded square extractor

Along with the straight white lines, we have chosen to use as visual landmarks a set of white coded squares laid on the ground. The identity and orientation of each square is uniquely identified through a dotted black code, similar to the one used in[6]. The choice of binary coding, i.e., black and white, is aimed at using luminance variation instead of color classification, for extracting the square characteristics. We arranged from 1 to 7 black dots on the border of the squares, in order to generate configurations which uniquely define the landmark identity (defined by its label: ID) and orientation. The 15 landmarks that we used can be seen in Fig. 4.2. Note that all the used landmarks are unambiguous with respect to multiple 90° orientation errors. Hence, the landmark identity and orientation can be uniquely identified in spite of the square rotational symmetry.

In practice, edges of squares are searched within the set of edge pixels  $\mathcal{D}_e$  derived as in the straight white line extractor. The robot frame coordinates of all edge pixels are derived from their image frame coordinates, with the projection that will be presented below. Then, the projected edges are compared with a reference square with the same dimensions of the coded square, so that the square perimeter pixels are identified. These define a subset of  $\mathcal{D}_e$  for each square (see Fig. 4.5). Indicating with  $N_{CS}$  the total number of coded squares extracted on the image, the subsets of edge pixels of each square *i* are noted:  $\mathcal{D}_{CS,j}$   $(j = 1 \dots N_{CS})$ . Each  $\mathcal{D}_{CS,j}$  defines a coded square detected on the image frame and must contain at least  $n_{CS,min}$  pixels. Following this, pixels on the segments (scanlines) leading from the center to the perimeter edges are classified by using a binary segmentation which uses the mean value of  $\mathcal{I}$  on the image as threshold. Corke [13] showed how binary segmentation is affected by noise, threshold selection and edge gradient. However, in this application, the choice of binary coding and the use of binary segmentation in only a small image window, and with adaptive thresholding, reduces these problems. Finally, black dots are extracted by associating a sufficient number of near black pixels found on the scanlines.

In conclusion, for each of the  $N_{CS}$  detected coded squares, the coded square extractor returns: the image coordinates of the square center O and of the centers of the  $n_{dots}$  black dots (respectively marked in red, and in cyan in Fig. 4.5):

$$[X_O Y_O]_{CS,j}^T \qquad j = 1, \dots, N_{CS} [X_i Y_i]_{CS,j}^T \qquad i = 1, \dots, n_{dots} \qquad n_{dots} = 1, \dots, 7$$
 (4.4)

#### Visual landmark tracker

The straight white line extractor and coded square extractor only take into account information from the current image. They provide no long-term knowledge. Thus, consistent landmarks must be obtained by comparing the extracted landmarks over consecutive images. This is done by projecting the characteristic points of each extracted visual landmark  $VL = SWL_1, \ldots, SWL_{N_{SWL}}, CS_1, \ldots, CS_{N_{CS}}$  from the image frame  $\mathcal{F}_{\mathcal{I}}$  (coordinates  $[X \ Y]_{VL}^T$ ) to the robot frame  $\mathcal{F}_{\mathcal{R}}$  (coordinates  $[x \ y \ z]_{VL}^T$ ). Such mapping is not one-to-one, and can only determine the projecting ray of the point. However, regarding our application, since all the visual landmarks are on the ground plane, the problem can be solved in closed form.

In fact, recalling Sect. 1.3, the point coordinates in the camera and image frames are related by:

$$D = {}^{I} T_C d_c \tag{4.5}$$

with matrix  ${}^{I}T_{C}$  given by (1.16). This equation can be rewritten:

$$\begin{pmatrix} -\frac{f}{l_X} & 0 & X - X_I \\ 0 & -\frac{f}{l_Y} & Y - Y_I \end{pmatrix} \begin{pmatrix} x_c \\ y_c \\ z_c \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$
(4.6)

with the camera intrinsic parameters f,  $l_X$ ,  $l_Y$ ,  $X_I$  and  $Y_I$  defined in Sect. 1.3. Moreover, given the homogeneous transformation matrix  ${}^{R}T_{C}$  representing the camera frame pose with respect to the robot frame, the coordinates of a point in the two reference frames are related by:

$$\begin{pmatrix} x \\ y \\ z \\ 1 \end{pmatrix} =^{R} T_{C} \begin{pmatrix} x_{c} \\ y_{c} \\ z_{c} \\ 1 \end{pmatrix}$$
(4.7)

We neglect the distance between the robot head tilt and head pan axes, assuming they intersect in a point which stays in a constant position  $\varsigma = [0 y_{\varsigma} z_{\varsigma}]^T$  in the robot frame (see Fig. 4.6). We also assume that during its motion, the robot body maintains constant orientation around the x axis, and null orientation around the two other axes. Under these assumptions,  ${}^{R}T_{C}$  can be easily computed at every frame through the three head joint positions  $\varrho_{h} = [\varrho_{nt} \ \varrho_{hp} \ \varrho_{ht}]^{T}$  and  $\varsigma$ , by using the Denavit and Hartenberg method [35] as in [24]. Since landmarks are on the ground plane (i.e.  $z_{VL} = 0$ ) the third equation from (4.7) can be expanded and used, along with (4.5):

$$\begin{pmatrix} t_{31} & t_{32} & t_{33} \\ -\frac{f}{l_X} & 0 & X_{VL} - X_I \\ 0 & -\frac{f}{l_Y} & Y_{VL} - Y_I \end{pmatrix} \begin{pmatrix} x_c \\ y_c \\ z_c \end{pmatrix}_{VL} = \begin{pmatrix} -t_{34} \\ 0 \\ 0 \end{pmatrix}$$
(4.8)

where  $t_{31} 
dots t_{34}$  indicate the elements of the third row of  ${}^{R}T_{C}$ . Inverting this equation away from singularities, allows for computation of the landmark position  $[x_{c} y_{c} z_{c}]_{VL}^{T}$  in the camera frame, given the landmark position  $[X Y]_{VL}^{T}$  in the image frame returned by the straight white line extractor and coded square extractor. Finally, substituting  $[x_{c} y_{c} z_{c}]_{VL}^{T}$  in (4.7) gives the landmark position  $[x y 0]_{VL}^{T}$  in the robot frame.

The robot frame coordinates of all straight white line points  $[x_j \ y_j \ 0]_{SWL,i}^T$  are then processed with a least square error algorithm in order to identify the path errors



Figure 4.6: The camera frame and head joint positions.

 $[e_n \ e_{\theta}]_{SWL,i}^T$  of each of the  $N_{SWL}$  lines (see Sect. 1.1). In this case, since the path direction is not specified, the path following algorithm chooses the direction with smaller orientation error. Hence, the path errors are defined as shown in Fig. 4.7a. The orientation error  $e_{\theta}$  is always in the interval $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right]$ . The normal path error  $e_n$  is chosen accordingly. A similar approach is used to process all the coded squares characteristic points  $[x_o \ y_o \ 0]_{CS,j}^T$ , and  $[x_i \ y_i \ 0]_{CS,j}^T$ , and obtain the identity  $ID_j = 1...15$  and orientation  $\gamma_j$ , of each of the  $N_{CS}$  coded squares (see Fig. 4.7b). Visual landmarks, extracted and projected at previous frames, are displaced according to the robot measured motion and compared with the current projected landmarks for checking consistency and filtering out false positives. The algorithm returns the characteristics



Figure 4.7: Relevant variables utilized in: (a) straight white line tracking, and (b) coded square tracking.

of the visual landmarks, validated in a sufficient number of consecutive frames:

$$\begin{bmatrix} e_n & e_\theta \end{bmatrix}_{SWL,i}^T & i = 1, \dots, N_{SWL} \\ ID_j & \gamma_j & \begin{bmatrix} x_o & y_o & 0 \end{bmatrix}_{CS,i}^T & j = 1, \dots, N_{CS} \end{bmatrix}$$
(4.9)

#### 4.3.2 Motion primitives

From a kinematic point of view, AIBO can be considered as an omnidirectional robot, i.e., three velocities (forward  $u_1$ , lateral  $u_2$ , and angular  $u_3$  around the robot center, positive for counterclockwise rotation) can be independently specified. In all cases where the robot velocities are specified in  $\mathcal{F}_{\mathcal{R}}$  coordinates as  $V = [V_x V_y]^T$  (e.g., when they are imposed by a user command), they must be mapped to the control input u. To perform this conversion, we have used two strategies. The first (*omnidirectional translational motion*), consists of simply setting:

$$u_1 = V_y \tag{4.10}$$
$$u_2 = V_x$$

with  $u_1$  forward velocity, and  $u_2$  lateral velocity. The robot orientation is not controlled in this first kind of conversion. Instead, the second kind of conversion (nonholonomic-like motion), consists in setting:

$$u_1 = V_y$$

$$u_2 = \operatorname{ATAN2}(V_x, V_y) \tag{4.11}$$

with  $u_1$  and  $u_2$  respectively forward and angular velocity. The advantages of each strategy will be illustrated later.

Basic motion primitives for controlling the robot legs in order to obtain the desired motion u are based on the kinematic parameterized trot walk algorithm described in Sect. 1.2.2. Velocity commands computed by the motion primitives are suitably scaled if any of them exceeds the physical limits of the actuators.

We also developed three primitives: Landmark fixer, Landmark approacher (LA), and Straight line follower, which use visual information returned by the perception primitives to guide the robot. In practice, the robot actuators are driven by a visual servoing scheme. Since the visual landmark tracker returns the position of the visual landmarks relative to the robot, position-based visual servo control turns out to offer a better solution than image-based servoing. The three vision-based motion primitives are explained below.

#### Landmark fixer

Referring to [13], "fixation" is defined as motion aimed at keeping one point in the scene (the "target", noted TG) at the same location in the image plane. In this work, it is of great interest to apply this control technique to a visual landmark, by keeping it centered in the image plane. Advantages include: reducing chances of losing sight of the landmark during motion, reducing motion blur, and reducing the effect of geometric distortion in the lens (since the optical axis will be pointed at the landmark). In many visual servoing works, the knowledge of camera motion during fixation is used to determine the 3D position of the target:  $[x \ y \ z]_{TG}^T$ . Instead, in this application, since the 3D position of the target is returned by the visual landmark tracker algorithm outlined above both for straight white lines and for coded squares, it can be used as is for fixation.

For fixation of a straight white line with parameters  $[e_n e_\theta]^T$ , we choose the 3D position of the target to be the normal projection of the robot center on the line (which is also the point that should be tracked by the robot during PF):  $[x y z]_{TG}^T =$ 

 $[-e_n \cos e_\theta e_n \sin e_\theta 0]^T$ . Instead, for fixation of a coded square with center  $[x_o y_o 0]^T$ , we choose:  $[x y z]_{TG}^T = [x_o y_o 0]^T$ . In both cases, the position  $[x y z]_{TG}^T$  is used for solving the inverse kinematics problem of finding the head joint coordinates for fixation. In practice, given the target coordinates in the robot frame, the fixation task consists in finding the robot head joint positions  $\rho_h = [\rho_{nt} \rho_{hp} \rho_{ht}]^T$  such that the target coordinates in the camera frame are  $[x_c=0 y_c=0 z_c]_{TG}^T$  (corresponding to centering the target in the image plane). This is equivalent to solving equation:

$$\begin{pmatrix} 0\\0\\z_c\\1 \end{pmatrix}_{TG} = {}^{C} T_{R} \begin{pmatrix} x\\y\\z\\1 \end{pmatrix}_{TG}$$
(4.12)

for  $\rho_h$ .  ${}^CT_R$  is the homogeneous transformation matrix representing the robot frame pose with respect to the camera frame coordinates. It is derived by inverting  ${}^RT_C$  away from singularities.

Apart from singular configurations, where no solution can be determined due either to joint limits (e.g. target "behind" the robot head: in this case a different target point must be chosen) or to singularities of  ${}^{R}T_{C}$ , for most configurations the solution of (4.12) is non-unique. In fact, although the head pan joint position  $\rho_{hp}$  can be derived from the first equation in (4.12):

$$\varrho_{hp} = -\text{ATAN2} \left( x_{TG}, y_{TG} - y_{\varsigma} \right) \tag{4.13}$$

replacing it in the two other equations does not guarantee a unique solution for the head tilt and neck tilt joint positions. In our implementation, we choose, whenever possible (i.e. when  $y_{TG}$  is "sufficiently" large) to fix  $\rho_{nt}$  to its lower bound (in order to maximize scene depth  $z_c$ ), and derive  $\rho_{ht}$  from (4.12). If it is not possible to adopt this strategy, due to the  $\rho_{ht}$  joint limits, we fix  $\rho_{ht}$  to its limit and derive  $\rho_{nt}$ .

#### Landmark approacher

When the robot finds a landmark (with the extractors described in Sect. 4.3.1), it should approach it, in order to get a better perception which can be useful for localization purposes. In practice, it is a *posture stabilization* task with reference configuration defined by the absolute position and orientation of the landmark. As we suggested previously, some tasks can be accomplished more effectively if nonholonomic-like motion is enforced. However, no smooth state-feedback control law can solve the non-square posture stabilization problem for a nonholonomic mobile robot [16]. Alternative control approaches (e.g. smooth time-varying [70] and discontinuous feedbacks) have shown limitations such as slow convergence and oscillatory transient. These considerations, along with the requirement of minimizing the path to the target, led us to the choice of omnidirectional motion, instead of nonholonomic motion, in the implementation of the landmark approacher.

The omnidirectional walk that drives the robot to the landmark implements a proportional closed-loop control strategy for reducing the robot's relative distance and orientation with respect to the nearest landmark perceived. In the case of straight white line approaching, this is done by setting robot velocities (respectively: forward, lateral and angular):

$$\begin{cases} u_1 = \lambda_T e_n \sin e_\theta \\ u_2 = -\lambda_T e_n \cos e_\theta \\ u_3 = -\lambda_R e_\theta \end{cases}$$
(4.14)

A similar controller is used for coded square approaching; in this case the robot velocities are set to:

$$\begin{cases}
 u_1 = \lambda_T y_o \\
 u_2 = \lambda_T x_o \\
 u_3 = -\lambda_R \gamma
 \end{cases}$$
(4.15)

In both cases,  $\lambda_T$  and  $\lambda_R$  are positive given gains.

#### Straight line follower

This primitive should solve the path following problem for a straight white line. For this problem, we decided to adopt a nonholonomic model for the robot, in order to obtain more effective obstacle avoidance (as will be shown in Chapter 5), and a more "natural-looking" walk. Moreover, the path following problem differs from the posture stabilization problem in that both linear and non-linear smooth state-feedback control solutions exist for nonholonomic mobile robots [16]. On the other hand, since the task is less stringent than posture stabilization, it can be achieved by using only one control variable. In this work, we utilize only the angular velocity  $u_2$ . The PF constraint, as defined in 1.1, is  $e_t = \text{const} = 0$ , since the robot center must track its normal projection on the line. AIBO is modeled as a unicycle robot, with velocities  $[u_1 u_2]^T$  and it is rather simple to verify that the following kinematic equations hold:

$$\dot{e}_n = -u_1 \sin e_\theta \tag{4.16}$$
$$\dot{e}_\theta = u_2$$

Linear feedback control can be realized by tangent linearization of the two equations above, in the neighborhood of  $(e_n = 0, e_{\theta} = 0)$ . This gives the second order linear system:

$$\dot{e}_n = -u_1 e_\theta \tag{4.17}$$

$$\dot{e}_\theta = u_2$$

which is clearly controllable, and thus asymptotically stabilizable by linear state feedback on  $u_2$ , when  $u_1$  is constant and strictly positive. Thus, the motion exigency (see Sect. 1.1) for this application is:  $u_1 = \text{const} > 0$ . It is rather simple to verify that a stabilizing linear feedback is of the form:

$$u_2 = (\lambda_1 e_n - \lambda_2 e_\theta) u_1 \tag{4.18}$$

with  $\lambda_2 = 2\epsilon\sqrt{\lambda_1}$ . Gain  $\lambda_1 > 0$  must be chosen so as to specify the transient 'rise distance' and  $\epsilon \in (0, 1)$  is the damping coefficient. The validity of this approach at walking and jogging speeds has been proved by similar works (e.g., [72] and [16]), as shown in Chapter 2.

#### 4.4 Visual path following scheme

The visual path following scheme that will be described in this section has been used to control the motion of AIBO in the ASPICE Autonomous navigation mode. With this navigation mode, the ASPICE user selects a target destination on the roadmap (shown in Fig. 4.2), and the robot utilizes the map features in order to reach the destination. The map is formed by streets and crossings, all delineated through white adhesive tape and laid on the ground. The streets are straight segments, which the robot follows using the straight line following primitive. The crossings enable the self-localization of the robot. In order to find the shortest path to the destination, the robot utilizes a Dijkstra-based graph search [19]. Hence, given the initial robot configuration and the desired destination in the workspace, the path to be followed is formed by a continuous,

piecewise differentiable curve (i.e., a series of segments), which is compatible with the definition of path given in Sect. 1.1

The perception primitives described in Sect. 4.3.1 are used to identify the streets (i.e. straight white lines) and crossings (i.e. coded squares) while the motion primitives described in Sect. 4.3.2 are used to drive the robot on the map. When approaching a landmark or following a street, the robot concurrently implements landmark fixing, in order to keep the landmark centered in the image plane. The robot autonomous behavior is represented by a Petri Nets [57] based framework which has been successfully deployed on the AIBO Platform in the Robocup field [83]. The Petri Net Plan formalism allows for high level description of complex action interactions that are necessary in programming a cognitive robot: non-instantaneous actions, sensing and conditional actions, action failures, concurrent actions, interrupts, action synchronization.

The autonomous navigation plan uses the following actions (note that at all times during the actions, the perception primitives are also executed for searching and updating perceived data):

- *Seek streets* The robot seeks streets by exploring the environment, while avoiding collisions. Motion directions are predefined: AIBO alternates forward and rotation steps.
- Approach the nearest street When it perceives some streets with the straight white line extractor, and tracks them with the visual landmark tracker, the robot uses the landmark approacher to walk towards the nearest street.
- *Follow the street* When the robot is sufficiently close to the street, it implements the linear straight line follower for walking on the street, until at least one crossing is detected.
- Plan the path to destination When a crossing is detected with the coded square extractor and is tracked with the visual landmark tracker, the robot will have univocally identified its *ID* and orientation. This information, along with the coded square positions in the robot frame, and with the map, identifies the robot pose (position and orientation). The robot then utilizes a Dijkstra-based graph search [19] to find the shortest path to the destination. Depending on the result of the graph search, the robot will approach and follow another street (repeat



Figure 4.8: The maximum distance at which the robot can detect the roadmap is measured by positioning the robot in various configurations around a straight white line.

the corresponding actions in the plan), or stop if the crossing corresponds to the desired destination.

The autonomous navigation plan repeats the above actions until the destination is reached. Transitions that start or terminate the actions represent events (e.g. *Street seen*, or *Crossing near*) which are triggered by conditions on sensed information (e.g. distance from a line). The plan must also deal with action failures. For instance, whenever the robot loses visual contact with a street it was approaching, the system aborts the current action and moves to the state where the street is not seen, and so on, until the robot reaches the street again.

#### 4.5 Experiments

In this section, we show the results of various experiments that were performed with the visual path following scheme developed for the ASPICE project. Short video clips of the experiments can be viewed on the web site: http://www.dis.uniroma1.it/~labrob/research/ASPICE.html.

In a first experiment, the performance of the straight white line extractor is evaluated by estimating the maximum distance from the roadmap at which the robot is able to detect the straight lines. In our opinion, is also a good metric for evaluating the performance of the ASPICE autonomous navigation mode. In fact, as soon as at least one line is detected, the robot is able to reach the roadmap and find coded squares 'showing' the way to the requested destination. Hence, line detection is the major bottleneck in the visual path following scheme. For the experiment, the robot is placed at a distance of 3 m from a straight white line, in various positions and orientations (some configurations are shown in Fig. 4.8). The distance at which the robot detects the line is measured and averaged along the experiments. After 20 experiments, the average value is 2.14 m, with standard deviation 0.15 m. Clearly, these values are strongly related to the environment light conditions and possible visual occlusions.In the roadmap used for the ASPICE experiments (see Fig. 4.2), the robot is capable of reaching the roadmap from every position in the environment, since the maximum distance between lines is compatible with such results. Moreover, even when the initial position is far from the roadmap, the *seek streets* action (see Sect. 4.4) will lead the robot to a position where it is able to detect at least one line.

In a second series of experiments, the performance of the autonomous navigation mode (and correspondingly, the visual path following scheme) is compared with the other modes developed in ASPICE: single step and semi-autonomous modes. With single step navigation, the user retains complete control of the robot motion: with a fixed step size, the robot can be driven in six possible directions. Before the step, a collision check is executed. Instead, in semi-autonomous navigation, the user specifies the main direction of motion, leaving to the robot the task of avoiding obstacles: the robot walks continuously in a specified direction until in receives a new command and concurrently avoids obstacles that are on the way. Details on the implementation of the ASPICE single step and semi-autonomous modes will be given in Chapter 5. Here, we report the results of the experiment comparing the three navigation modes. The comparison is carried out by driving the robot from a start point to a goal point (noted respectively "S" and "G" in Figures 4.9 and 4.10). The task is repeated 5 times for each of the three navigation modes by using first a mouse (Fig. 4.9), and afterwards a BCI (Fig. 4.10) as input devices. In the BCI experiments, a sequence of icons corresponding to possible ASPICE commands is shown on a screen and aids the user in choosing the command to be sent to the ASPICE Control Unit. The EEG potentials are captured by means of an electrode cap. Details on the BCI will be given



Figure 4.9: Comparison between the three ASPICE navigation modes: with the mouse as input device, the user drives the robot from point S to point G using the single step (above), semi-autonomous (center) and autonomous (below) modes.

in Chapter 5. The comparison between the three modes and between the two input devices is based on execution time and user intervention (i.e. number of times the user had to intervene by updating the commands) averaged over the experiments. As expected, the results (plotted in Fig. 4.11) confirm the qualitative properties expected for each mode. Note that the best choice depends not only on the user preference and ability but also on the specific task (e.g., position of the start and goal points in the environment, presence and position of obstacles). As expected, the user intervention diminishes as the robot autonomy increases (both using BCI and mouse). On the other hand, note that in the specific configuration used in the experiment, the execution



Figure 4.10: BCI-driven single step navigation experiment. A feedback stimulus is provided on the screen. The commands used to drive the robot from point S to point G are displayed on the bottom.

time does not always decrease as autonomy increases. For example, when the robot is mouse-driven, the task is executed in 1:23 minutes using the semi-autonomous mode and in 1:30 using the autonomous mode. The differences may depend, among other factors, on the distances of the start and goal points from the roadmap. The use of the BCI introduces a time delay on each user intervention. This delay is due to the time required for selection of each command. In fact, to reduce the effect of the EEG signal noise, the command selection is validated after the user has 'confirmed' it various times (in our experiment, 6 times). Moreover, BCI control introduces errors during the navigation, due to EEG noise and large user inaccuracy, as compared to mouse



Figure 4.11: Comparison between the 3 navigation modes using 2 input devices: mouse (blue) and BCI (red). Execution time (in minutes): dashed, user intervention (number of commands): solid.

control. Hence, the user intervention is greater with the BCI, since the user must apply extra commands to correct the errors. Consider, for example, the semi-autonomous experiment: with the mouse, four clicks were sufficient, whereas with the BCI, the user had to intervene 11 times. This specific result is related to the characteristics of the semi-autonomous mode, which requires precise timing when switching between walking directions. This requirement is hardly compatible with the BCI. For both the aforementioned reasons (time delay on each command and errors), the total execution time is particularly worsened when a high intervention is required. For instance, in single step mode, the experiment requires 2:22 more with the BCI than with the mouse, whereas in autonomous mode the difference is only 17 seconds. Thus, when using the BCI, the autonomous navigation mode is the most appropriate.

The usefulness of the proposed scheme to increase patient independence in everyday life is shown in an experiment where a domestic task is achieved by taking advantage of the visual path follower. The task is shown in Fig. 4.12: the robot is used to verify whether the bottle of water is on the green table in a domestic environment. The visual feedback from the robot camera supports the user throughout navigation. The robot is initially located far from the roadmap with an obstacle on the way. The user perceives this information via the robot camera, and decides to control AIBO with the semi-autonomous mode to approach the roadmap (Fig. 4.12a). When the user perceives that the robot is sufficiently near the roadmap, the autonomous mode is used to drive the robot to the target nearest to the green table (Fig. 4.12b, c and d). Then, in order to obtain precise motion of the robot camera and check if the bottle is on the table,



Figure 4.12: Executing a domestic task (check if the bottle is on the green table) by taking advantage of all the characteristics of the ASPICE robot driver.

the user controls the robot with the single step mode, and finally displaces the robot camera with the head control menu (Fig. 4.12e). Clearly, the task would have been much harder to achieve in the absence of the path following controller.

Finally, in another experiment, autonomous robot battery charging, is implemented. This behavior is also present in the commercial Sony Driver, but since Sony does not release the code of its driver, we had to realize it *ad hoc* for this project. This experiment not only fulfills an important ASPICE requirement, but also provides an additional testbed for the visual path following scheme. In fact, the AIBO Charging Station is placed near a marked crossing on the roadmap shown in Fig. 4.2, and as soon as the battery level is low, the robot autonomously moves to the station. The experiment is illustrated in Fig. 4.13. The robot position at consecutive time frames is shown while it approaches the roadmap, follows the street up to the battery charger crossing, detects it and makes a turn in order to reach its destination (the charging station) on the basis of the plan.



Figure 4.13: Battery charging experiment.

#### 4.6 Conclusions

In this chapter, we have presented the development, integration, and experimental validation of a vision-based path following scheme for a legged robot with actuated camera, in ASPICE, an assistive robotics project. The path is formed by straight segments connected by coded crossings and enables the robot to reach various desired target-destinations in a domestic environment. The PF scheme has been used in the ASPICE autonomous navigation mode, which enables a user to control the mobile robot with a small set of commands. In particular, the experiments show that severely impaired patients, who are unable to use standard ASPICE input devices and must control the robot with a BCI, would profit greatly from the vision-based path following scheme. In other experiments, the scheme has also been used to enable the robot to autonomously recharge its battery without human intervention, and to execute simple domestic tasks.

## Chapter 5

# Other aspects of the ASPICE project

Although the ASPICE project has provided a useful testbed for the path following scheme which has been described in Chapter 4, it has also permitted the development of many other aspects in the field of assistive robotics. These numerous aspects are described in this chapter.

An important objective in assistive technology is to design versatile systems, which adapt to the user level of disability by offering various human-robot interfaces and various levels of interaction. Semi-autonomous navigation systems for wheelchairs which adapt to the patient autonomy level [27, 46] are an example of this approach. Similarly, in ASPICE, as mentioned in Chapter 4, three navigation modes have been developed. The autonomous navigation mode has been thoroughly described in Chapter 4. In this chapter, we will describe the single step and semi-autonomous navigation modes. Automatic obstacle detection and avoidance is integrated in all navigation modes to guarantee safe, collision-free motion in cluttered environments. This is done by generating an occupancy grid, which will also be described in this chapter, along with the experimental validation of the obstacle avoidance algorithm. Another objective of the ASPICE project is to enable robot control based on signals from different sources, depending on the user residual abilities. In particular, in this chapter, we will describe the Brain-Computer Interface which has been utilized to control AIBO with the user electro-encephalographic brain signals. Other features of the system, such as the video feedback from the robotic platform to the user and the use of AIBO as communication aid, are also briefly described. A third objective of ASPICE is to aid or support a human user in everyday tasks. Hence, the system must be assessed by considering its effects on the quality of the user's life. Human-robot interaction during the ASPICE experimentation has been assessed by patient feedback. The ASPICE clinical assessment on potential users has also been briefly reported at the end of the chapter.

The chapter is organized as follows. In Sect. 5.1, the occupancy grid generator needed to avoid obstacles during navigation is illustrated. The ASPICE single step and semi-autonomous navigation modes are described respectively in Sect. 5.2 and in Sect. 5.3. In Sect. 5.4, we present the Brain-Computer interface used by severely impaired patients to control AIBO and the other ASPICE appliances. Other aspects of the ASPICE robot driver are described in Sect. 5.5. Simulations and experiments are presented in Sect. 5.6. The ASPICE clinical validation is reported in Sect. 5.7.

#### 5.1 Occupancy grid generator

The main features that the robot should perceive are the obstacles that it should avoid. We chose to use the robot range sensors to detect obstacles. We use a local two-dimensional occupancy grid to represent the detected obstacles, built by the occupancy grid generator.

The robot should be able to recover robust and useful spatial descriptions of its surrounding obstacles, using sensory information. These descriptions should be used for short-term planning in the environment. To do this, we use a tesselated two-dimensional representation of spatial information called the occupancy grid. In the past years, the occupancy grid framework proved to be extremely efficient for performing path planning and obstacle avoidance in unknown and unstructured environments, and researchers have proposed different functions for updating the grid cells (e.g. Fuzzy [60], Bayesian [40], Gaussian [22]). The occupancy grids have also been used for obstacle detection on Sony AIBO. Fasola and others [26] make use of the robot camera to generate a local occupancy grid, used for taking navigation decisions. A similar approach is used in [39], where recent information is integrated along with current information, based on odometric data. However, both works were used in the Robocup



Figure 5.1: Relevant variables utilized in occupancy grid generation.

application, where free space can be easily identified by the green color (the color of the soccer field). Instead, in unknown environments, using visual information for obstacle detection is very challenging. The AIBO range sensors are a better tool, although only two are available. In [41], a scanning motion of the AIBO head distance sensor is used to map the obstacles locally and the position of the barycenter of the sensor readings after every scan is used for robot navigation.

In our approach, the two range finders (head and chest) are used to detect obstacles, although the chest sensor can only detect near obstacles, due to its limited range and particular orientation (see Sect. 4.2), and hence is not used to compute the occupancy grid. Thus, only the head sensor is utilized to build the local occupancy grid by moving the head pan joint along a sinusoidal profile spanning an angular width of 90°. While the origin of the occupancy grid is always on the head pan axis and its longitudinal

extent is limited by the range of the head distance sensor (1 m), its orientation (i.e., the direction of its bisectrix) is the same as the direction of motion introduced in Sect. 4.3.2  $V = [V_x V_y]^T$  (see Fig. 5.1). As is shown in the figure, 30 grid cells are used. The cells are annulus sectors of width 15° and height 0.2 m. Obviously, due to the joint limit, it is impossible to build occupancy grids for backward motions. The grid may be built with the robot when this is in stationary position or in motion. In the second case, the head pan movement is synchronized with the gait cycle and odometric data (reconstructed through the leg joint encoders) are used to build a consistent map: in practice, at every time frame, the previous range readings are displaced on the map according to the robot measured motion. When the pan cycle is complete, a cell in the grid is considered to be occupied if there is a sensor reading indicating an obstacle inside that cell.

#### 5.2 Single step navigation mode

With single step motion, the robot can be driven, with a fixed step size, in any of six directions (forward, backward, lateral left/right, clockwise and counterclockwise rotations). The user selects the desired direction from the corresponding GUI, shown in Fig. 4.3, above. Before performing the motion command, the robot generates the appropriate occupancy grid (oriented along the intention of motion) from its stationary position and verifies whether the step can be performed without colliding with obstacles. The collision is checked by applying a threshold test to the sum of the inverse distances of all the occupied grid cells. We note  $\|\zeta\|$  the distance of the occupied cell center from the robot center. If the collision check is positive:

$$\sum_{\zeta} \frac{1}{\|\zeta\|} > T_{SS}$$

the robot will not step in the desired direction. Otherwise, the step will be performed. Clearly, the contribution of near occupied cells to the above sum is greater than that of far-occupied cells. Note that, since no occupancy grid can be built for backward or rotational motions, the corresponding step commands should be used with care.

#### 5.3 Semi-autonomous navigation mode

With semi-autonomous motion, the user specifies the general directions of motion, which the robot should track as closely as possible. The user selects the desired direction from the corresponding GUI, shown in Fig. 4.3, center. This mode may be useful for "gross" movements, leaving the user the possibility of returning to the single step navigator for finer motion control. In contrast with single step navigation, in the semi-autonomous mode, occupancy grid generation and motion control are executed simultaneously. Instead of executing a single step, the robot walks continuously in the specified direction until it receives a new command (either a new direction or a stop). If the specified direction is forward or lateral<sup>1</sup> (i.e., the user desired direction of motion in the workspace is  $V_{des} = [V_{des,x} \ 0]^T$  or  $V_{des} = [0 \ V_{des,y}]^T$ ), autonomous obstacle avoidance is obtained by the use of potential fields. The algorithm used in this case is explained below.

In fact, the use of potential fields has proved to be a powerful technique for controlling robot motion [45]. Some researchers have used potential fields to address the problem of real time action selection both for navigation and manipulation purposes on the AIBO [43]. Others [64] calculate the potential fields needed for autonomous exploration of an environment, from an occupancy grid. We decided to use the latter approach by generating the occupancy grid as the robot moves and then use it to compute the robot velocities. Our algorithm uses a composition of vortex and repulsive fields to build the velocity field. In particular, for each occupied cell on the occupancy grid, centered at  $\zeta = [x_{\zeta} \ y_{\zeta}]^T$ , with  $x_{\zeta}$  and  $y_{\zeta}$  cell coordinates in the robot frame (see Fig. 5.1), define the repulsive potential as:

$$U_r\left(\left\|\zeta\right\|,\eta\right) = \begin{cases} \lambda_r \left(\frac{1}{\left\|\zeta\right\|} - \frac{1}{\eta}\right)^2 & \text{if } \left\|\zeta\right\| \le \eta \\ 0 & \text{else} \end{cases}$$
(5.1)

where  $\|\zeta\|$  is the distance of the occupied cell from the robot center,  $\eta$  the radius of influence of the potential, and  $\lambda_r$  a given gain. The repulsive field induced by each cell

<sup>&</sup>lt;sup>1</sup>As for the single step mode, no obstacle avoidance can be performed when executing backward or rotational motions.

is simply obtained as the gradient of this potential, i.e.,

$$f_{\zeta}^{r} = \begin{pmatrix} f_{\zeta,x}^{r} \\ f_{\zeta,y}^{r} \end{pmatrix} = \begin{pmatrix} \frac{\partial U_{r}(\|\zeta\|,\eta_{r})}{\partial x_{\zeta}} \\ \frac{\partial U_{r}(\|\zeta\|,\eta_{r})}{\partial y_{\zeta}} \end{pmatrix}$$
(5.2)

while the vortex field [52] is defined as:

$$f_{\zeta}^{v} = \begin{pmatrix} f_{\zeta,x}^{v} \\ f_{\zeta,y}^{v} \end{pmatrix} = \begin{pmatrix} \pm \frac{\partial U_{r}(\|\zeta\|,\eta_{v})}{\partial y_{\zeta}} \\ \pm \frac{\partial U_{r}(\|\zeta\|,\eta_{v})}{\partial x_{\zeta}} \end{pmatrix}$$
(5.3)

Note the different radii of influence  $\eta_r$  and  $\eta_v$  of repulsive and vortex fields, respectively. By choosing  $\eta_v > \eta_r$ , we obtain velocity fields that are essentially vortices at large distances, and become increasingly repulsive at close range. The signs of  $f_{\zeta,x}^v$  and  $f_{\zeta,y}^v$  depend on the position of the occupied cell with respect to the robot sagittal plane: a cell in the right (left) half of the grid will induce a clockwise (counterclockwise) vortex.

The fields generated by all the occupied grid cells are then superimposed with the desired workspace velocity in order to obtain the total velocity field:

$$V = \sum_{\zeta} f_{\zeta}^r + \sum_{\zeta} f_{\zeta}^v + V_{des}$$
(5.4)

This velocity must be mapped to the configuration space velocities either with the omnidirectional translational motion conversion or by enforcing nonholonomic-like motion (4.11). The first is consistent with the objective of maintaining as much as possible the robot orientation specified by the user. Instead, with the second kind of conversion, the orientation of the robot is always tangent to the path; the grid provides more effective collision avoidance since the direction of its angle bisector coincides with the x axis (because the robot lateral velocity is null).

#### 5.4 Brain-Computer Interface

The ASPICE system input devices are customized on the severely motor impaired patients' residual abilities, based on the technologies mentioned in Sect. 4.1.1 (mouse, joystick, eye tracker, voice recognition). Users can utilize the aids they are already familiar with. On the other hand, the variety of input devices provides robustness to the worsening of the patient abilities, which is a typical consequence of degenerative diseases. When the patient is not able to use any of the standard input devices or when a degenerative disease likely implies that in the future he/she will no more be able to use them, a BCI should be utilized to access the Control Unit. The BCI gives the user communication and control channels that do not depend on the brain normal output channels of peripheral nerves and muscles [79]. In other terms, a BCI can detect the activation patterns of the brain, and whenever the user induces a voluntary modification of these patterns, it is able to detect it and to translate it into an action that is associated to the user will. BCI technology has substantially improved in the last decade and it is reasonable to expect that, in the near future, a wider class of users will profit from it. Though the number of completely paralyzed patients is rather small (some one hundred thousand worldwide), BCIs have the relevance that derives from being the 'only' option for such users, who would otherwise be locked in their bodies.

As it emerges from a concise review of related work, real time control tasks based on human electro-encephalography (EEG) have been addressed to simple applications, such as moving a computer cursor on a screen [81], opening a hand orthosis [63] or driving a wheeled robot [17]. Recently, an experimental BCI which was implanted into the brain motor cortex, enabled a tetraplegic to move a computer cursor [38]. However, to our knowledge, the application of non-invasive BCI technology to interaction with a wider set of devices has not been explored yet, and it represents one of the goals of the ASPICE system.

The BCI used in ASPICE can be alternatively based on time domain (i.e., P300 evoked potentials [25]) or on frequency domain features (i.e., sensorimotor rhythms [80]) of the EEG signal. The performance of these two BCI versions varies on an individual basis and the most reliable features are chosen depending on the user predisposition. In both versions, a visual interface (on a screen) aids the user in choosing the command to be sent to the ASPICE Control Unit. The EEG potentials are captured by means of an electrode cap, amplified, digitized and transmitted to a personal computer. Processing is handled by the BCI2000 software package [71]. After a preliminary signal conditioning phase, which includes a linear mixture of channels implementing a high pass spatial filter, the features (either in the time or frequency domain) are extracted and used to identify the user desired command.
When time domain features are employed, a sequence of icons corresponding to possible ASPICE commands is shown on the screen to the user. The icons are highlighted successively one by one (ca. 3 icons are highlighted per second). After each sequence, classification is implemented and the command corresponding to the identified target icon is forwarded to the ASPICE Control Unit. Time domain features are the result of an averaging procedure: the mean of time samples at equal latency from the stimulus (i.e., the icon display) is computed for each channel and for each stimulus. Averaged potentials at specific latencies and channels are fed into a linear classifier. The latency/channel choice and the weights for classification are determined in advance by training the classifier. A threshold is used to assess reliability of the classification. The BCI which has been used in the experiments presented in Sect. 4.5 is based on time domain features.

When frequency domain features are employed, two targets positioned at the top and bottom edge of the screen are shown to the user. Two actions (*scroll* along all possible ASPICE commands and *select* the desired command) are associated with the targets. The subject controls the vertical velocity of a cursor on the visual interface by modulating the amplitude of his EEG sensorimotor rhythms above or below a dynamically adapted threshold value. When the cursor reaches either the top or the bottom target, the corresponding action (scroll or select) is performed in order to choose the command to be forwarded to the ASPICE Control Unit. Frequency domain features are computed using a parametric estimation, which takes into account the latest 300 ms of signal and is updated every 100 ms. The power spectral density values at specific channels and frequency bins (which are identified in advance during the training phase) are linearly combined. The output is detrended using a moving average value, which avoids drift of the control signal if the EEG amplitude is increased or decreased (e.g., due to non-voluntary arousal effects).

### 5.5 Other robot driver features

In this Section, we will describe the implementation of four features of the ASPICE robot driver.

#### 5.5.1 Video feedback

Firstly, a fundamental requirement for effective remote controlled navigation is the feedback of the robot camera to the Control Unit (i.e., to the user). This is not only an essential aid for the user to drive the robot in the environment, but also helpful for exploration and extension of virtual mobility. By driving the robot in a desired spot of the apartment, the disabled person can monitor, with AIBO's on board camera, that area. Thus, an algorithm for feeding back to the ASPICE GUI the image captured by the robot has been developed. Each new image captured by the robot camera is compressed on board using the Independent JPEG Group libraries<sup>2</sup>, before being streamed over a wireless connection to the ASPICE Control Unit. To improve video quality in varying light conditions, the image luminosity is adaptively icremented/reduced before compression, depending on the image average luminosity. This simple approach reduces the variations in the average image luminosity during video stream.

#### 5.5.2 Vocal request interface

Another feature of the system is a GUI for vocal requests that has been included to improve the communication of the patient with the caregiver. This feature covers an important issue in ASPICE, enabling the robot to be socially interactive. Socially interactive robots have been defined by Fong [28] to describe robots whose main task is some form of interaction. Fong categorizes these robots by the aspects of social interaction (speech, gestures, etc.) they use.

When the robot receives a vocal request (e.g., 'I am thirsty') from the control unit, it plays the corresponding prerecorded audio file with its speakers in order to attract the caregiver's attention. The vocal request GUI is shown in Fig. 5.2 (bottom). In the GUI, each button that the user can select corresponds to vocal request (here, 'turn on/off the light', 'Please come', 'I am thirsty' 'Close the window' and 'I am hungry'). Each vocal request is associated to a robot gesture generated by a sequence of fixed joint positions. Joint data containing angles for all joints, as well as timing information that state for how long the values will be sent, is specified in a special description language developed for AIBO and described in [24]. For each vocal request, there is a

<sup>&</sup>lt;sup>2</sup>www.ijg.org



Figure 5.2: The ASPICE GUIs for head control (top), and for vocal requests (bottom).

file in this description language which contains all the joint data.

### 5.5.3 Head control interface

To improve ambient exploration with the camera, a GUI for head control has also been developed. This GUI allows the user to directly move the robot head and point the camera in a desired direction. With this GUI, the user can control the head pan and head tilt angles ( $\rho_{hp}$  and  $\rho_{ht}$ ) with fixed steps, in order to point the camera in a desired direction. The head control GUI is shown in Fig. 5.2 (top).

### 5.5.4 Walking gait

Finally, another issue that deserved attention is AIBO's walking gait, which has been modified on the basis of the ASPICE requirements (e.g., reducing the noise caused by foot contact with the ground). The basic principles of the walking algorithm have been described in Sect. 1.2.2. The goal of the algorithm is to move the robot feet alternatively (in trot style) on rectangular trajectories. The directions and sizes of such rectangles are determined by the motion command u. The joint angles required to drive the feet on the rectangular trajectories are calculated by solving the inverse kinematics problem for each leg. Nevertheless, many walking styles can be implemented, and a set of parameters (e.g., the position of the rectangles with respect to AIBO's body, or their height) defines each possible walking style. Hence, a set of such parameters (noted  $\Upsilon$ in Sect. 1.2.2) was hand tuned and tested to fulfill ASPICE requirements. Clearly, the limitations in the robot hardware forbid usage in environments with steps (e.g. stairs)



Figure 5.3: A simulation result for semi-autonomous navigation.

and steep slopes.

## 5.6 Simulations and experiments

In this section, we show the results of the simulations and experiments that were performed with the robot obstacle avoidance algorithm. Moreover, we discuss the ASPICE clinical validation and its results on the quality of life of potential users. Short video clips of the experiments can be viewed on the web site: http://www.dis.uniroma1.it/~labrob/research/ASPICE.html.

The possibility of testing the robot obstacle avoidance algorithm in a simulated environment without endangering the real robot has been crucial from the very early stages of the ASPICE project. To this end, we have adopted Webots, a mobile robot simulation environment, which has been described in Sect. 3.5. Webots supports a physical model of the robot AIBO ERS7, including cross-compilation of C++ programs based on the OPEN-R Software Development Kit. The simulation environment was built according to the real environment where the ASPICE experiments take place, a small apartment located at Fondazione Santa Lucia in Rome, intended for rehabilitation purposes and the three ASPICE navigation modes have been implemented in Webots.



Figure 5.4: Three experiments showing the performance of semi-autonomous navigation. The user drives the robot using a single command: 'go forward'(top left and bottom) and 'go right' (top right).

A typical simulation of the ASPICE semi-autonomous mode is shown in Fig. 5.3. Here, the user tried to drive AIBO to a given destination in the apartment (indicated by a red arrow in the figure), through a single direction command (forward) along the line joining the initial and final configuration. The obstacle avoidance algorithm was able to successfully accomplish the task in spite of the many obstacles along the way. Here, the nonholonomic conversion entailed by eq. (4.11) was used to map the reference velocities to robot velocities. By using Webots, it was possible to debug the algorithms effectively and to test them without endangering the real robot. It was also possible to progressively develop the obstacle avoidance algorithms (initially based solely on repulsive potential fields) by reducing the local minima cases and developing adaptive vortex fields. Besides, the problem of tuning all the parameters (gains, characteristics of the grid-based map, etc.) could be easily solved in the simulation before porting on the real AIBO.

After the Webots simulations, the obstacle avoidance algorithm has been tested on AIBO in a series of experiments. In the experiments (shown in Fig. 5.4), the performance of the obstacle avoidance algorithms is tested by using the semi-autonomous navigation mode. Omnidirectional translational motion (4.10) is used for mapping desired user velocities to the corresponding control inputs. In the first (top left in the figure) and third (bottom) experiments, a single 'go forward' command is used. The robot is able to successfully avoid the obstacles while maintaining the orientation desired by the user. In the second experiment (top right in the figure), a single 'go right' command is used. Again, the robot avoids the obstacle while maintaining the desired orientation. The robustness of the obstacle avoidance algorithm is evident in the third experiment, where the obstacle scenario is more complex than in the two other experiments. In general, due to the vibrations in the quadruped gait cycle and to the low-quality of AIBO's distance sensors, small and mobile obstacles might not be detected by the robot. However, using the robot camera video feedback presented in Sect. 5.5.1, the user can detect such obstacles and intervene to prevent collisions.

## 5.7 Clinical validation

At this stage of the ASPICE project, the system has been implemented and is available at the Fondazione Santa Lucia in Rome for validation with patients [12]. All domotic appliances used in ASPICE have been installed in the experimental apartment of the Santa Lucia hospital. A portable computer runs the Control Unit program and several input devices are available to cope with as many categories of users as possible. The subjects have been admitted for a neuro-rehabilitation program and the whole procedure underwent the approval of the local ethical committee. The patients have been informed on the device and have given their voluntary informed written consent. Furthermore, they have been interviewed and physically examined by the clinicians, in order to evaluate some variables of interest: the degree of motor impairment and of reliance on the caregivers for everyday activities as assessed by current standardized scale (Barthel Index *BI*), the familiarity with the system input devices, the ability to speak or communicate, and the level of informatics alphabetization measured by the number of hours per week spent in front of a computer. Then, for a period ranging from 3 to 4 weeks, the patient and (when required) her/his caregivers have been practising weekly with the ASPICE system. During the whole period, patients had the assistance of an engineer and a therapist in their interaction with the system. The experiments have been carried out with eight subjects suffering from Spinal Muscular Atrophy type II (SMA II) and six subjects suffering from Duchenne Muscular Dystrophy (DMD). Depending on their level of disability, users controlled AIBO through keyboard, mouse, touchpad, head tracker, microphone or BCI.

According to the score of the BI, all patients were on almost complete dependence of caregivers, especially the six subjects suffering from DMD (BI < 35), who required artificial ventilation, had minimal residual mobility of the upper limbs and very slow speech. Because of the high level of muscular impairment, the DMD patients all had access to the system via joypads. As for the eight SMA II subjects, their level of dependency was slightly lower with respect the DMD patients, but they also required continuous assistance for daily life activity (BI < 50). These patients have accessed the system via joystick, touchpad, keyboard and microphone, since the residual motor abilities were still functionally effective both in terms of muscular strength and range of movements preserved. Four of them interacted with the system via BCI. All of the patients were able to master the system and control AIBO within 5 sessions. Data on user satisfaction, increase of independence, and reduction of caregiver workload, have been collected and structured in questionnaires during the experimentation. For instance, the users were asked to indicate with a number ranging from 0 (not satisfied) to 5 (very satisfied) their degree of acceptance relative to each of the output devices. The average grade given by the patients to their 'personal satisfaction in utilizing the robot' was 3.04 on a 5-point scale. This is a very promising result, considering that the users were originally more accustomed to using and controlling the 'traditional' ASPICE appliances rather than the mobile robot. According to the results of the questionnaire, all patients reported that they were independent in the use of the system at the end of the training and they experienced (as they reported) "the possibility to interact with the environment by myself". From the clinical viewpoint, the robot navigation

system was useful in blending the "desiderata" of the patients (e.g., being in the living room with the relatives, reaching someone far from the patient's location) with their level of disability (which prevented them from acting as first-person in realizing such "desiderata"). For example, patients with a partial preservation of distal arm muscular ability (i.e., most SMA II patients) could have a complete control of the robot via single step navigation. On the other hand, severely impaired patients (i.e. DMD patients), who were unable to send frequent commands, could operate the robot in semi-autonomous and autonomous navigation modes. In summary, the robot driver has been designed in order to be effectively operated by low-speed input devices, such as the ones developed in ASPICE (e.g., the BCI). Hence, in this work we did not attempt to provide a new control interface for robot navigation, but rather focused on the design and implementation of an appropriate robot navigation system, that can be matched to various forms of detection of the user's will. The clinical validation showed feasibility of the proposed approach.

Further studies are necessary to confront a larger population of patients with ASPICE, in order to assess the robot navigation system impact on the quality of life by taking into account a range of outcomes (e.g. mood, motivation, caregiver burden, employability, satisfaction, [48], [1], [59]). However, the results obtained from this pilot study are encouraging for the establishment of a solid link between the field of human machine interaction and neurorehabilitation strategy [34]. The ASPICE system cannot substitute the assistance provided by humans. Nevertheless, it can contribute to relieve the caregiver from the continuous presence in the room of the patient, since the latter can perform some simple activities on his/her own. The perception of the patients is that they no longer have to rely on the caregiver for each and every action. This provides the patient with both a sense of independence, and a sense of privacy. For both reasons, her/his quality of life is sensibly improved.

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