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Phenomenological Constitutive Equations for Numerical Simulations of SMA's Structures. Effects of Thermomechanical Couplings

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Abstract : Tension-compression tests at different room temperatures and at different strain rates have been performed on Shape Memory Alloys (CuZnAl, NiTi) using a thermomechanical device. The experiments underline the main role of the temperature variations induced by the deformation process on the stress-strain curves. These variations are essentially due to the latent heat of phase change and the analysis of the associated energy balances shows that the intrinsic dissipated energy remains very small compared to deformation work or latent heat of phase change. On the basis of these results, a behavioral model is proposed that assumes an intrinsic dissipation identically equal to zero and that considers anisothermal deformation processes. This model, written under the formalism of Generalized Standard Materials takes into account the thermoelastic couplings and considers two self-accommodating martensite variants. It is implemented in a finite element code realized to predict the effects of thermomechanical couplings. An implicit integration scheme is used to derive at each step in time the fields stress, strain, temperature, and volume proportions of phases. At each step and due to the thermomechanical coupling, we have to solve non-symmetric linear systems. Numerical simulations are shown first to verify the coherence with the experimental results obtained under uniaxial loading, and secondly to underline the practical interest of such an approach to design SMA's structures.

1. INTRODUCTION

Tension-compression tests at different room temperatures and at different strain rates have been performed on Shape Memory Alloys like CuZnAl and NiTi. These experiments, carried out with a thermomechanical device, underline the main role of the temperature variations induced by the deformation process. These variations are essentially due to the latent heat of phase change. The detailed analysis of the associated energy balances shows that the intrinsic dissipated energy remains very small compared to deformation work or latent heat of phase change. On the basis of these results, a behavioral model is proposed that assumes an intrinsic dissipation identically equal to zero and that considers anisothermal deformation processes. This model, written under the formalism of Generalized Standard Materials takes into account the thermoelastic couplings and considers two self-accommodating martensite variants. It is implemented in a finite element code realized to predict the effects of thermomechanical couplings [1]. An implicit integration scheme is used to derive at each step in time the fields stress, strain, temperature, and volume proportions of phases. Numerical simulations are shown first to verify the coherence with the experimental results obtained under uniaxial loading, and secondly to underline the practical interest of such an approach to design SMA's structures.

2. THERMODYNAMICAL FRAMEWORK AND EXPERIMENTAL RESULTS

2.1. Thermodynamical framework - Energy balance

To characterize the thermodynamical state of the considered system, the following variables are chosen : T absolute temperature (we will also use the temperature variation $\theta = T - T_0$, with T_0 the equilibrium absolute temperature), ϵ strain tensor (small perturbation hypothesis), x_1 and x_2 volume proportions of martensite variants, linked to the phase change strain tensors β^1 and β^2 . (The portion of strain due to the phase change is : $\epsilon^{pc} = x_1 \beta^1 + x_2 \beta^2$).

• Without any heat volume exchange with the outside, the first two principles of thermodynamics can be written as : [2] :

$$\rho \dot{U} = \sigma : \dot{\epsilon} - \text{div } q \quad (1) \quad \text{and} \quad \rho T \dot{s} = D_1 - \text{div } q \quad (2)$$

U stands for the total energy of the system,

σ is the stress tensor, q the heat influx vector through the outer surface,

s the specific entropy, ρ the volume mass, D_1 la dissipation intrinsic.

• For a test realizing a thermodynamical cycle (strain, stress and temperature go back to their initial values), the integration along the cycle C of equation (1) gives :

$$\int_C \sigma : \dot{\epsilon} \, d\tau = \int_C \text{div } q \, d\tau = A_h \quad (3)$$

noting U is a state function. A_h stands for the hysteresis area in a (σ, ϵ) diagram.

Furthermore, using the chosen set of variables (T, ϵ, x_v) and the classical two definitions of C_α (specific heat capacity) and of ψ ($\psi = U - Ts$), Helmholtz free energy) :

$$C_\alpha = T \frac{\partial s}{\partial T} \quad \text{et} \quad s = - \frac{\partial \psi}{\partial T}$$

we obtain :

$$\dot{s} = C_\alpha \frac{\dot{T}}{T} + \frac{\partial s}{\partial \epsilon} : \dot{\epsilon} + \frac{\partial s}{\partial x} \dot{x} \quad (4), \quad \rho T \dot{s} = \rho C_\alpha \dot{T} + \rho T \frac{\partial s}{\partial \epsilon} : \dot{\epsilon} + \rho T \frac{\partial s}{\partial x} \dot{x} \quad (4')$$

(4) and (4') integrated along the cycle C lead to :

$$\int_C \rho T \dot{s} \, d\tau = \int_C \rho \theta \frac{\partial s}{\partial \epsilon} : \dot{\epsilon} \, d\tau + \int_C \rho \theta \frac{\partial s}{\partial x} \dot{x} \, d\tau$$

When integrating (2) along the same cycle C , (3) we get :

$$A_h = \int_C D_1 \, d\tau + \int_C \rho \theta \frac{\partial^2 \psi}{\partial T \partial \epsilon} : \dot{\epsilon} \, d\tau + \int_C \rho \theta \frac{\partial^2 \psi}{\partial T \partial x} \dot{x} \, d\tau \quad (5)$$

Equation (5) allows to decompose the hysteresis area in a part resulting from the intrinsic dissipation D_1 , a part resulting from the thermoelastic couplings, called isentropic coupling, and a part resulting from phase change effects.

- We find again these different terms in the expression of heat equation, written here assuming a Fourier conduction law ($q = -\lambda \cdot \text{grad}(T)$) where λ is the thermal conduction tensor, assumed to be constant :

$$\rho C_\alpha \dot{\theta} - \lambda \cdot \Delta \theta = D_1 + \rho T \frac{\partial^2 \psi}{\partial T \partial \epsilon} : \dot{\epsilon} + \rho T \frac{\partial^2 \psi}{\partial T \partial x} \dot{x} = w_{ch}' \quad (6)$$

w_{ch}' , right hand side of the equation, is the volume heat source, that can be computed by evaluating the left hand side of (6) thanks to temperature measurements [3].

Connecting (4) and (5), we deduce, for any thermodynamical cycle :

$$A_h = \int_C w_{ch}' d\tau \quad (7)$$

In order to quantify the importance of the dissipation terms and of the thermomechanical coupling terms, one can introduce [4] the coefficient R_T defined by :

$$0 \leq R_T = \frac{A_h}{A_h} \leq 1 \quad \text{with} \quad \overline{A_h} = \int_C |w_{ch}'| d\tau \quad (8)$$

Just remember that intrinsic dissipation is always positive and that coupling terms change sign at every change of loading. Due to this, and for tension-compression loadings, the more the dissipation is preponderant, the closer R_T is to 1. Conversely, the closer R_T is to 0, the more the dissipation can be energetically negligible compared with the heat evolved by thermomechanical couplings.

2.2 Analysis of experimental results [5] and [6]

The related tests have been performed on CuZnAl and NiTi alloys. The experimental device allows uniaxial tension compression loadings at different strain rates and with a controlled room temperature (with an environment chamber). Several loading paths in a stress temperature plane were prescribed, and the amounts of heat involved during the tests were deduced from the temperature measurement made by thermocouples or by infrared thermography. the main results are :

- The analysis of mechanical and thermal measurements points out a transition domain delimited by half lines (fig. 1), pointing to the beginnings and the ends of austenite - martensite transformation. The width of this domain can be characterized by the difference between temperatures A and M, (respectively beginning and end of austenite - martensite transformation under zero stress).
- The experiments realized at different room temperature show (fig. 2) different mechanical responses. Furthermore, the amplitude of temperature variations due to the austenite - martensite transformation is not negligible in comparison with (A-M) (Fig. 3b). These two facts attest the importance of taking into account the temperature in the analysis of shape memory alloys behavior.
- The experiments realizing thermodynamical cycles (zero values of strain and stress at the end of experiment, and same temperature, after a while, than initial reference temperature), have all shown values of ratio R_T (equation 8) less than 0.02, proving the weak value of dissipated energy along a cycle in comparison with the global heat evolved by thermomechanical couplings.

• The amounts of energy W_{ch} (corresponding to the evolved heat) and W_m (deformation work) are given by :

$$W_{ch} = V_0 \int_{t_{ini}}^t w'_{ch} d\tau \quad \text{and} \quad W_m = V_0 \int_{t_{ini}}^t \sigma : \dot{\epsilon} dt$$

Their evolution during the test (fig. 3a) show the importance of the latent heat associated to phase change in comparison with W_m . The ratio W_{ch} to W_m is about 10 for CuZnAl and 3 for NiTi.

• Finally, calling W_{is} the energy term du to thermomechanical couplings (see equation (5)), we define W_L as the difference between W_{ch} and W_{is} . Then, keeping the hypothesis of a weak dissipation in comparison with the others energetic terms, W_L stands for the amounts of energy associated to phase change. On fig.4 we can see that W_L is proportional to ϵ^{PC} (portion of strain due to phase change). This result has been confirmed for all the thermomechanical loadings used and allows to characterize the relationship between energy used in the phase change and the volume proportion of transformed material.

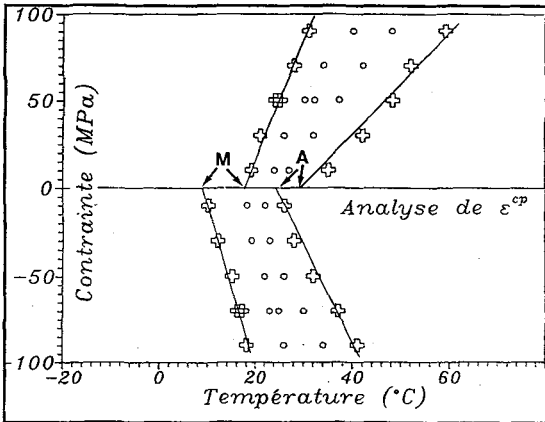


Figure 1 : Transition domains observed for a CuZnAl alloy

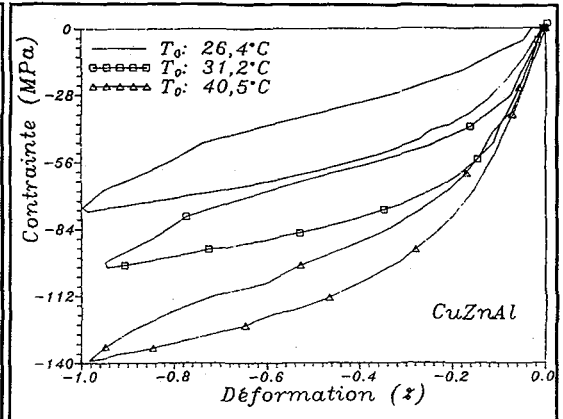


Figure 2 : Stress-strain curves for a compression test, for 3 values of imposed room temperature.

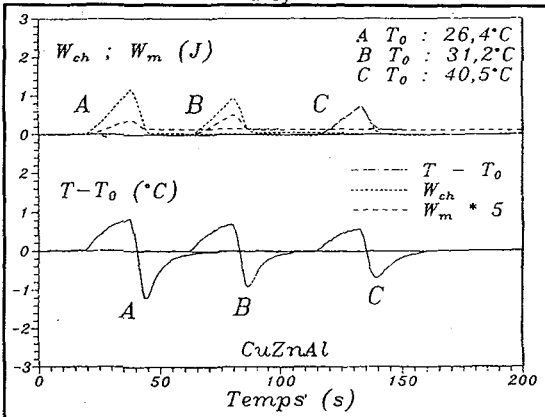


Figure 3 : Evolution during the test of the sample temperature (3a) and of quantities W_{ch} and W_m (3b), for 3 values of imposed room temperature

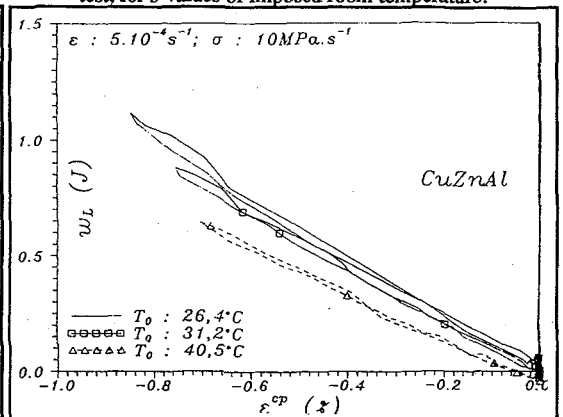


Figure 4 : Relationship between W_L , phase change energy and ϵ^{PC} , portion of strain due to phase change

3. DERIVATION OF THE MODEL - BEHAVIOR LAWS

We suggest a behavioral model for these materials that takes into account of the preceding experimental results, and we choose the thermodynamical framework of Generalized Standard Materials. Classically, Two potentials are introduced, ψ free energy potential, D dissipation potential, as functions of the state variables and their derivatives with respect to time. The state laws and the complementary laws are then deduced from these potentials.

3.1 Free energy potential - State laws

The set of state variables used to describe the behavior is : (ε, T, x_v) .

The considered behavior is a coupled thermoelastic one, taking into account the effects of phase change.

- The free energy ψ is decomposed into ψ_e (corresponding to thermoelastic effects) and ψ_{ch} (corresponding to phase change effects),

$$\rho\psi_e = \frac{1}{2} [a_{ijkl}(\varepsilon_{kl} - \alpha_{kl}\theta - x_v\beta_{kl}^v)(\varepsilon_{ij} - \alpha_{ij}\theta - x_v\beta_{ij}^v) - (C + a_{ijkl}\alpha_{kl}\alpha_{ij})\theta^2] \quad (9-1)$$

(In this expression, suffix v in the product $x\beta$ must be summed over 1 and 2)

$$\rho\psi_{ch} = D[(A-M)(x_1^2 + x_2^2) + (T-A)(x_1 + x_2)] \quad (9-2)$$

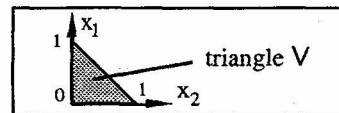
- Finally, as x_1 are x_2 are volume fractions they must stay in the set V defined by :

$$V = \{ (x_1, x_2) \in \mathbb{R}^2 / 0 \leq x_v \leq 1, v = 1, 2 \text{ et } 0 \leq x_1 + x_2 \leq 1 \}$$

V is then a triangle in the plane (x_1, x_2) (see figure below).

To take account of these inequalities, one can introduce, in the expression of free energy, [7] and [8], the indicator function of V , I_V , defined by :

$$I_V(x_1, x_2) = \begin{cases} 0 & \text{if } (x_1, x_2) \in V \\ +\infty & \text{if not} \end{cases} \quad (10)$$



We will finally keep the following expression of ψ :

$$\rho\psi = \rho\psi_e + \rho\psi_{ch} + I_V(x_1, x_2) \quad (11)$$

and consequently we impose an infinite value to ψ when the values of x_1 and x_2 are not physically admissible.

• The derivation of the partial derivatives of ψ with respect to ϵ and to T gives :

$$\rho \frac{\partial \psi}{\partial \epsilon_{ij}} = \sigma_{ij} = a_{ijkl} (\epsilon_{kl} - \alpha_{kl} \theta - x_v \beta_{kl}^v) \quad \text{stress tensor} \quad (12)$$

$$C_\alpha = T \frac{\partial s}{\partial T} = - T \frac{\partial^2 \psi}{\partial T^2} = - T C \quad \text{specific heat capacity} \quad (13)$$

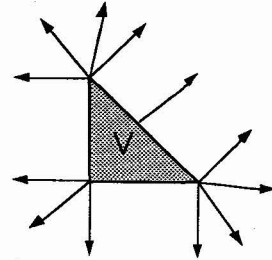
3.2 Dissipation potential - Complementary laws

• In order to translate the experimentally undetected intrinsic dissipation, the mechanical dissipation potential is chosen identically equal to zero. This implicates that the thermodynamical force X^v associated to x_v is identically equal to zero.

Calling X^v the regular part of X^v that is :

$$X^v = \frac{\partial \psi_e}{\partial x_v} + \frac{\partial \psi_{ch}}{\partial x_v}, \text{ we derive : } X^1 \in \partial_1 I_V(x_1, x_2) \quad \text{et} \quad X^2 \in \partial_2 I_V(x_1, x_2) \quad (14)$$

where $\partial_i I_V(x_1, x_2)$ stands for the components of the sub-differential with respect to x_v of the indicator function I_V . The point is, using these two relations, to write some conditions on the vector $\vec{X}=(X^1, X^2)$ when the vector $\vec{x}=(x_1, x_2)$ describes triangle V . If the point is inside triangle V , then $\vec{X} = \vec{0}$, if \vec{x} is on the boundary of V , then \vec{X} belongs to the normal cone to V .



The advantage of this mathematical formalism consists in his ability to describe correctly the non regular points of domain V (for $\vec{x} = \vec{0}, \vec{x} = (1,0), \vec{x} = (0,1)$). Furthermore, and in light of expressions (9-1), (9-2) and (9-3), equation (14) becomes :

$$\left. \begin{aligned} - \sigma_{ij} : \beta_{ij}^1 + D [2 (A-M) x_1 + (T-A)] \in \partial_1 I_V(x_1, x_2) \\ - \sigma_{ij} : \beta_{ij}^2 + D [2 (A-M) x_2 + (T-A)] \in \partial_2 I_V(x_1, x_2) \end{aligned} \right\} \quad (15)$$

In the following, Z will stand for the quantity $\frac{\sigma_{ij} : \beta_{ij}}{D}$, that qualify the importance of stress level.

• The investigation of the possible situations of \vec{x} in V and the derivation of the corresponding values of \vec{X} allow to define, in a (Z, T) plane, the different transition domains between austenite and the two martensite variants (fig. 5). Concerning temperature higher than A and low values of Z , only austenite is present. For temperature lower than M , there is no more austenite, and if $|Z| < A-M$, Both martensite variants exist. Between M and A , and for $|Z| < A-M$, there is a zone where the three phases are present.

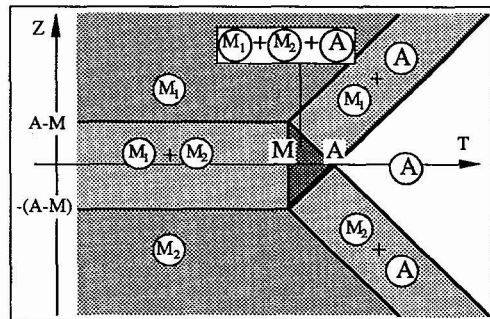


Figure 5 : Transition domains in the (Z, T) plane

3.3 Heat equation

- In order to work under the hypothesis of a dissipation identically equal to zero, the heat equation (6) becomes :

$$\frac{\rho C \alpha}{T_0} \dot{\theta} - \frac{\lambda}{T_0} \Delta \theta = - a \alpha : \dot{\varepsilon} + \frac{\rho L^v}{T_0} \dot{x}_v \quad (16)$$

where $L^v = \frac{T_0}{\rho} (a \alpha : \beta^v + D)$ is the phase change latent heat of the variant v .

3.4 The final behavior laws

In a first step, in order to perform basic numerical simulations of SMA behavior, we made the following assumptions :

- The thermoelastic behavior is supposed to be isotropic. Hence, the material will be describe by its Young's modulus E and its Poisson's ratio ν , and by a thermal dilatation coefficient α .

- The phase change strain tensors β^1 et β^2 are supposed to satisfy :

$$\text{Tr}(\beta^v) = 0 \quad \text{et} \quad \beta_{ij}^1 + \beta_{ij}^2 = 0,$$

in order to translate iso-volumic strain and auto-accommodation properties for the two variants.

Let $\beta = \beta^1 = - \beta^2$.

- These two assumptions allow to write the latent heat as : $L = \frac{T_0}{\rho} D$
- Consequently, the final behavior laws are :

$$\sigma_{ij} = a_{ijkl} (\varepsilon_{kl} - \alpha_{kl} \theta - (x_1 - x_2) \beta_{kl})$$

$$\frac{\rho C \alpha}{T_0} \dot{\theta} - \frac{\lambda}{T_0} \Delta \theta = - a_{ijkl} \alpha_{kl} : \dot{\varepsilon}_{ij} + \frac{\rho L}{T_0} (\dot{x}_1 + \dot{x}_2)$$

Combined with expressions (15) we can link the stress field, the temperature and the volume proportions of martensite.

4. NUMERICAL SIMULATIONS

4.1 The numerical method

The numerical method relies upon a finite element spatial discretisation (3 nodes triangles with linear interpolation functions). For a two-dimensional solution, each node on the mesh owns three degrees of freedom, two for displacements and one for temperature.

Time discretisation uses an implicit schema allowing, at each step in time, to derive the fields of stress (σ), displacement (u), temperature (θ) and volume proportions (x_v^k) of transformed phase.

The step in time k begins with given fields σ^k , u^k , θ^k et x_v^k . The discretised problem reduces to a linear system solution giving $u^{k'}$ et $\theta^{k'}$, in terms of u^k , θ^k , x_v^k and the loading conditions. We then derive $x_v^{k'}$ as a function of $\theta^{k'}$ and $\sigma^{k'}$, $\sigma^{k'}$ being evaluated from $u^{k'}$, $\theta^{k'}$ et $x_v^{k'}$ and iterate the problem solution and the computation of $x_v^{k'}$ up to the process convergence (convergence is estimated from the successive values of $x_v^{k'}$). At this time, the computed values are σ^{k+1} , u^{k+1} , θ^{k+1} and x_v^{k+1} , and step in time $k+1$ can begin.

Another difficulty to reduce is that the computed system is, at each step in time and at each iterative path, a non symmetric one. This is due to the isentropic coupling term in the heat equation and requires a systematic use of skyline storage.

Finally, the boundary conditions available are imposed displacements and temperature, given effort or heat influx, and also mixed boundary conditions on the surface (like $X_h (T - T_{ext})$ where $T - T_{ext}$ represents the difference between the surface temperature and a prescribed room temperature, and where X_h is an exchange coefficient.)

4.2 The numerical simulations

We simulated the behavior of a shape memory alloy such as CuZnAl with the following set of coefficients.

Young's modulus $E = 8.5 \text{ E}10 \text{ Mpa}$

Poisson's ratio $\nu = 0.3$

Thermal dilatation coefficient $\alpha = 1.7 \text{ E-}05 \text{ }^\circ\text{C}^{-1}$

Thermal Conductivity $\lambda = 120 \text{ W/m}^\circ\text{C}$

Specific heat capacity $C_\alpha = 390 \text{ J/kg}^\circ\text{C}$

Volume mass $\rho = 7900 \text{ kg/m}^3$

Latent heat $L = 7000 \text{ J/kg}$

Phase change strain tensor β : $\beta_{11} = 6 \text{ E-}02$, $\beta_{22} = -6 \text{ E-}02$, $\beta_{33} = 0$, other β_{ij} equal zero.

Reference temperature $T_0 = 20 \text{ }^\circ\text{C}$.

Temperature associated to the beginning and the end of transformation, $M = 5 \text{ }^\circ\text{C}$ et $A = 20 \text{ }^\circ\text{C}$

- The aim of the first numerical tests was to verify the consistency with the experimental experiments. The studied structure (here a sample) is a rectangular piece of 10 cm^2 , the corresponding mesh contains 121 nodes and 200 elements and the prescribed loadings consist in imposed displacements on one side, simulating a tension-compression test along axis 1.

Relating to the test presented below, the imposed displacement (time proportional) allows to reach tension and compression strains up to 2%. The room temperature is kept constant and equals 19°C . Figure 6 shows the executed path in a (Z, θ) plane. The broken lines show a portion of the transition domain defined in figure 5. The first loading path (tension 0-2) is done while the sample has not reached yet a thermal

equilibrium with respect to the room temperature. The portion (0-1) is concerned with low temperature variations (isentropic coupling alone). In (1), we enter martensite variant 1 domain and the latent heat terms induce much more significant temperature variations. In the course of time, a thermal equilibrium is reached around the room temperature (19°C or $\theta = -1^{\circ}\text{C}$), and the following loops (3-4) are stabilized. In (2) the value of x_1 is about 0.33.

Figure 7 shows the evolution of stress along the loading axis versus the strain in the same direction. Here again, we observe a stabilization of the hysteresis loops from the second loading (2).

These two figures are plotted for a point of the exterior surface of the sample

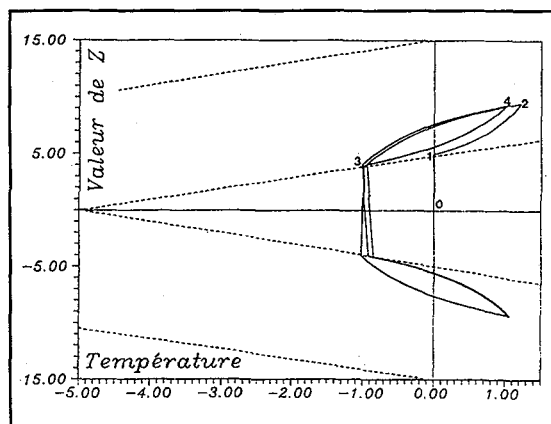


Figure 6 : (Z, θ) curve

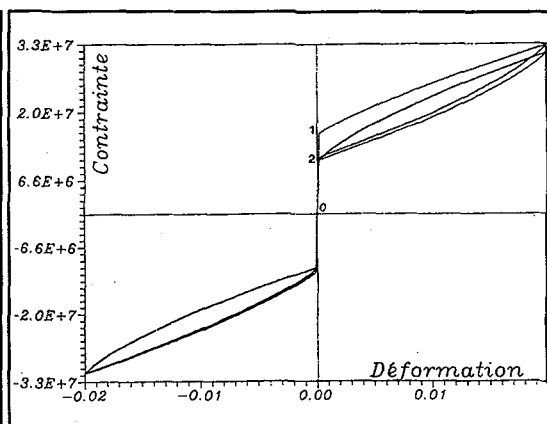


Figure 7 : Stress - strain curve

- It can be of some interest to study the importance of the heterogeneous aspect of the transformation (unavoidable in view of the conditions of heat diffusion). In fact, during these cyclic loadings, the temperature fields can show variations of 3 to 4 degrees between a point in the center of the sample and a point on its boundary. On the other hand, the variations of x_k between the same points are less than 1%. Hence, the transformation can be considered as uniform.

- Others numerical tests were performed in order to describe completely the transition domain of figure 5. (In particular simulations allowing an entire crossing of the transition domain, others for variable room temperature and zero stress and finally simulations with variable stress and given room temperature less than M (autoaccommodation phenomema)).

- Finally, the last tests performed are intended to underline the practical interest of these approaches when designing structures using SMA. (Computation of the efforts in a constrained structure under temperature variations, investigation of the tightening effort in a collar, ...). Giving access to the fields of stress, temperature and volume proportions of transformed phase, the finite element method is found to be totally efficient.

5. CONCLUSIONS

Using a coherent thermodynamical framework, the analysis of experimental results obtained on shape memory alloys allowed us to make some assumptions, especially concerning the anisothermal aspect of the transformation and the weakness of the intrinsic dissipation evolved in comparison with phase change latent heat. These hypothesis are at the source of a behavioral model for these materials that takes into account existing thermomechanical couplings. This model extended with a finite element method, makes it possible to perform numerical simulation of structures or samples made with shape memory alloys. In spite of some simplifications of the behavior (only two martensite variants existing in the model), the obtained results are in good agreement with experimental observations.

Outstanding improvements are related to a much more precise description of the physical aspects of the transformation (increase of the number of potential variants) in order to get a better translation of the material behavior in a structure design. Considering another scale (grains in a polycrystal), an other research line consists in a better characterization of the material behavior especially by taking into account the connections between crystallographic orientations and possible transformation.

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