

## Yield surfaces of BCC crystals for slip on the 110 and 112 systems $\$

B. Orlans-Joliet, B. Bacroix, F. Montheillet, J.H. Driver, J.J. Jonas

## ▶ To cite this version:

B. Orlans-Joliet, B. Bacroix, F. Montheillet, J.H. Driver, J.J. Jonas. Yield surfaces of BCC crystals for slip on the 110 and 112 systems. Revue de Physique Appliquée, 1988, 23 (4), pp.707-707. 10.1051/rphysap:01988002304070700 . jpa-00245863

## HAL Id: jpa-00245863 https://hal.science/jpa-00245863v1

Submitted on 4 Feb 2008

**HAL** is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés. YIELD SURFACES OF BCC CRYSTALS FOR SLIP ON THE {110} <111> AND {112} <111> SYSTEMS

X XX X X X X B.ORLANS-JOLIET , B.BACROIX , F.MONTHEILLET , J.H.DRIVER AND J.J.JONAS

- \* Département Matériaux, Ecole Nationale Supérieure des Mines de Saint-Etienne, 158, Cours Fauriel, 42023 SAINT-ETIENNE CEDEX 2, FRANCE.
- Department of Metallurgical Engineering, McGill University, 3450 University Street, MCNTREAL H3A2A7, CANADA.

The development of deformation textures and the plastic anisotropy of textured materials both depend on the plastic properties of the individual grains that make up the aggregate. These properties are essentially described by the shape of the single crystal yield surface (SCYS). The SCYS for fcc crystals which deform by slip on the  $\{111\} < 110 >$  systems is well known [1]; by duality, it is identical to the yield surface of bcc crystals slipping on  $\{110\} < 111 >$ . However, many experimental data [2-4] show that bcc crystals can slip, in the <111 > directions, along planes other than  $\{110\}$ ; the one most commonly observed, excluding  $\{110\}$ , is  $\{112\}$ .

The single crystal yield surfaces for slip in bcc metals on either {112}<111> or mixed slip on {110} <111> & {112}<111> have therefore been derived. In particular, for the general case of mixed slip, the SCYS is described in terms of  $\xi$ , the ratio of the critical resolved shear stresses for slip on the {110}<111> & {112}<111> systems. All the possible types of yield vertices are tabulated and classified into crystallographically non-equivalent groups. It is confirmed that there is a limited range of  $\xi$  for mixed slip:  $\frac{\sqrt{3}}{2} < \xi < \frac{2}{\sqrt{3}}$ 

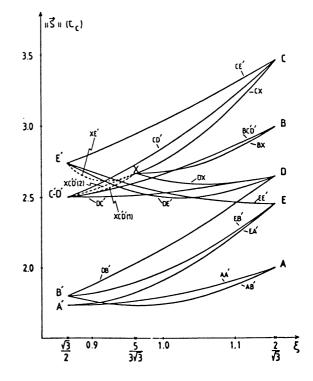
Within this range, there are only 2 different SCYS configurations, depending on whether  $\xi$  is greater or smaller than 5/3/3. Each of these configurations has 15 groups of vertices and 216 stress states (plus their negatives). The two yield surfaces only differ with respect to 3 of the groups of vertices (72 stress states). These latter 72 vertices which activate 3 {110} < 111 > and 2 {112} < 111 > systems when  $\xi > 5/3/3$ , transform into 72 new vertices activating 2 {110} < 111 > and 3 {112} < 111 > systems when  $\xi < 5/3/3$ . Thus when  $\xi$  is changed, for a given configuration, only the position of the vertices are modified and not their types or associated slip systems.

For the 15 basic groups of each of the 2 possible configurations of the mixed SCYS, the dependence of the stress vector moduli on the critical resolved shear stress ratio is presented in Fig.1 for the entire range of existence of the mixed polyhedron. At the upper  $\xi$  limit (2//3), the A,B,C,D,E notation of Kocks et al. [5] for { 110 } <111 > slip is conserved. At the lower limit ( $^{3}$ /2) of  $\xi$ , a similar notation based on A',B',C',D',E' is adopted for { 112 } <111 > slip. The particular point at which the 3 groups of vertices converge ( $\xi = 5/3/3$ ) is denoted X. Intermediate groups of mixed slip vertices are denoted by the letters corresponding to the vertex group at the limiting  $\xi$  values ( $^{3}/2, 5/3/3, 2//3$ ).

The mixed slip stress states activate 5,6,8 slip systems depending on the basic group to which they belong. In the vast majority of cases, only five slip systems are activated so that, by allowing mixed  $\{110\}<112>$  glide, the slip ambiguity problem caracteristic of  $\{110\}<111>$  restricted glide is substantially reduced.

REFERENCES.

- [1] J.F.W. Bishop and R. Hill, Phil. Mag., 42, 414 and 1298 (1951)
- [2] G.I. Taylor and C.F. Elam, Proc. Roy. Soc., 112 A, 337 (1926)
- [3] C.S. Barrett, G. Ansell and R.F. Mehl, Trans. ASM, 25, 702 (1937)
- [4] F.M.A. Carpay, G.Y. Chin, S. Mahajan and
- J.J. Rubin, Acta. Metall., 23, 1473 (1975) [5] U.F. Kocks, G.R. Canova and J.J. Jonas, Acta. Metall., 31, 1243 (1983)



 $\underbrace{Figure 1}_{moduli} \xi \text{ dependence of the yield stress vector}$