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# ISOMERIC STATE AND ROTATIONAL BAND IN ${ }^{158} \mathbf{H o}$ 

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#### Abstract

Résumé. — Le noyau impair-impair ${ }^{158} \mathrm{Ho}$ a été étudié au moyen des réactions ${ }^{159} \mathrm{~Tb}(\alpha, 5 \mathrm{n}){ }^{158} \mathrm{Ho}$ et ${ }^{160} \mathrm{Dy}(\mathrm{p}, 3 \mathrm{n})^{158} \mathrm{Ho}$. Un état isomérique de période $T_{1 / 2}=(29 \pm 3) \mathrm{ns}$ a été mis en évidence. Une bande de rotation a été développée jusqu'au spin $16^{-}$.


> Abstract. - The odd-odd ${ }^{158} \mathrm{Ho}$ nucleus is studied by means of the reactions ${ }^{159} \mathrm{~Tb}(\alpha, 5 \mathrm{n})^{158} \mathrm{Ho}$ and ${ }^{160} \mathrm{Dy}(\mathrm{p}, 3 \mathrm{n})^{158} \mathrm{Ho}$. The life-time of an isomeric state is measured as $T_{1 / 2}=(29 \pm 3) \mathrm{ns}$. A rotational band is developed up to spin $16^{-}$.

1. Introduction. - In the framework of a systematic study of the spectroscopy of neutron-deficient holmium isotopes, the level scheme of the odd-odd nucleus ${ }^{158} \mathrm{Ho}$ has been investigated.
A previous investigation by Stenström and Jung [1] determined the genetic relationships and half-lives of ${ }^{158} \mathrm{Ho}$ isomers. Recently Abdurazakov et al. [2] and Harmatz and Handley [3] have investigated the decay scheme of the nucleus ${ }^{158} \mathrm{Er} \rightarrow{ }^{158} \mathrm{Ho}$. As a result of their investigations the ground state of ${ }^{158} \mathrm{Ho}$ is found to have spin and parity $5^{+}$corresponding to 67 protons and 91 neutrons with a p $7 / 2^{-}[523] \uparrow \mathrm{n} 3 / 2^{-}[521] \uparrow$ configuration. An isomeric state ( $T_{1 / 2}=27 \mathrm{~min}$.) in ${ }^{158} \mathrm{Ho}$ with energy 67.3 keV is known which has been interpreted as having spin and parity $2^{-}$and which corresponds to possible configurations :

$$
\begin{array}{lll}
\text { p } 1 / 2^{+}[411] \downarrow \text { n } 5 / 2^{-}[523] \downarrow & \text { Ref. [2] } \\
\text { p } 7 / 2^{+}[404] \downarrow \text { n } 3 / 2^{-}[521] \uparrow & \text { Ref. [3] } \\
\text { p } 7 / 2^{-}[523] \uparrow \text { n } 3 / 2^{+}[402] \downarrow &
\end{array}
$$

It is the purpose of this letter to discuss the above possibilities and compare them with our data which concern the levels of ${ }^{158}$ Ho studied by in beam spectroscopic methods in the reactions ( $\alpha, \mathrm{xn} \gamma$ ) and ( $\mathrm{p}, \mathrm{xn} \gamma$ ).
2. Experimental procedure and results. - The in beam experiments were carried out at the Grenoble cyclotron. For the ${ }^{159} \mathrm{~Tb}(\alpha, 5 \mathrm{n})$ reaction, a monoisotopic terbium foil target of $5 \mathrm{mg} / \mathrm{cm}^{2}$ was used. The ${ }^{160} \mathrm{Dy}(\mathrm{p}, 3 \mathrm{n})$ reaction was performed with a $5.5 \mathrm{mg} / \mathrm{cm}^{2} 85 \%$ enriched ${ }^{160} \mathrm{Dy}_{2} \mathrm{O}_{3}$ target. The

[^0]study of excitation functions suggested that alpha and proton particle energies of approximately 63 MeV and 43 MeV respectively were the most favourable for the production of ${ }^{158} \mathrm{Ho}$. Gamma lines belonging to

## Table I

Summary of the experimental results

| $E_{\gamma}$ | $I_{\nu}$ | Assignment |  |
| :---: | :---: | :---: | :---: |
| $67.3 \pm 0.1$ | $95 \pm 8$ | ${ }^{158} \mathrm{Ho}$ | $2^{-} \rightarrow 5^{+}$ |
| $70.9 \pm 0.1$ | $72 \pm 6$ | ${ }^{158} \mathrm{Ho}$ | $6^{-} \rightarrow 5^{-}$ |
| $98.9 \pm 0.1$ | $540 \pm 50$ | ${ }^{158}$ Dy |  |
| $100.6 \pm 0.2$ | $185 \pm 19$ | ${ }^{158} \mathrm{Ho}$ | $7^{-} \rightarrow 6^{-}$ |
| $115.1 \pm 0.2$ | $200 \pm 20$ | ${ }^{158} \mathrm{Ho}$ | $8^{-} \rightarrow 7^{-}$ |
| $156.9 \pm 0.1$ | $1000 \pm 90$ | ${ }^{158 m} \mathrm{Ho}$ | $5^{-} \rightarrow 5^{+}$ |
| $159.3 \pm 0.2$ | $210 \pm 21$ | ${ }^{158} \mathrm{Ho}$ | $9^{-} \rightarrow 8^{-}$ |
| $166.1 \pm 0.1$ | $250 \pm 26$ | $\left\{\begin{array}{l}{ }^{158} \mathrm{Ho} \\ 159 \\ \mathrm{Ho}\end{array}\right.$ | $10^{-} \rightarrow 9^{-}$ |
| $171.5 \pm 0.3$ | w | ${ }^{158} \mathrm{Ho}$ | $7^{-} \rightarrow 5^{-}$ |
| $213.8 \pm 0.2$ | $155 \pm 16$ | $\left\{\begin{array}{l}158 \\ { }^{158} \mathrm{Ho} \\ { }^{18} \mathrm{Dy}\end{array}\right.$ | $11^{-} \rightarrow 10^{-}$ |
| $215.7 \pm 0.2$ | $163 \pm 17$ | ${ }^{158} \mathrm{Ho}$ | $8^{-} \rightarrow 6^{-}$ |
| $218.2 \pm 0.1$ | $1320 \pm 80$ | ${ }^{158}$ Dy |  |
| $221.9 \pm 0.2$ | $89 \pm 12$ | ${ }^{158} \mathrm{Ho}$ | $12^{-} \rightarrow 11^{-}$ |
| $255.9 \pm 0.3$ | $55 \pm 7$ | ${ }^{158} \mathrm{Ho}$ | $13^{-} \rightarrow 12^{-}$ |
| $274.4 \pm 0.3$ | $77 \pm 8$ | ${ }^{158} \mathrm{Ho}$ | $9^{-} \rightarrow 7^{-}$ |
| $277.4 \pm 0.4$ | $35 \pm 12$ | ${ }^{158} \mathrm{Ho}$ | $14^{-} \rightarrow 13^{-}$ |
| $286.4 \pm 0.4$ | $35 \pm 12$ | ${ }^{158} \mathrm{Ho}$ | $15^{-} \rightarrow 14^{-}$ |
| $320.4 \pm 0.1$ | $850 \pm 80$ | ${ }^{158}$ Dy |  |
| $325.4 \pm 0.2$ | $210 \pm 21$ | ${ }^{158} \mathrm{Ho}$ | $10^{-} \rightarrow 8^{-}$ |
| $379.9 \pm 0.2$ | $163 \pm 18$ | ${ }^{158} \mathrm{Ho}$ | $11^{-} \rightarrow 9^{-}$ |
| $425.4 \pm 0.2$ | $50 \pm 5$ | ${ }_{158}^{158} \mathrm{Dy}$ |  |
| $435.8 \pm 0.2$ | $246 \pm 25$ | ${ }^{158} \mathrm{Ho}$ | $12^{-} \rightarrow 10^{-}$ |
| $477.8 \pm 0.2$ | $107 \pm 13$ | ${ }^{158} \mathrm{Ho}$ | $13^{-} \rightarrow 11^{-}$ |
| $533.3 \pm 0.2$ | $155 \pm 16$ | ${ }^{158} \mathrm{Ho}$ | $14^{-} \rightarrow 12^{-}$ |
| $563.8 \pm 0.3$ | $134 \pm 20$ | ${ }^{158} \mathrm{Ho}$ | $15^{-} \rightarrow 13^{-}$ |
| $617.0 \pm 0.3$ | $100 \pm 12$ | ${ }^{158} \mathrm{Ho}$ | $16^{-} \rightarrow 14^{-}$ |



Fig. 1. - Example of coincident spectrum (stop by $156.9 \mathrm{keV}-\gamma$ ).


Fig. 2. - Example of coincident spectrum (115.1 keV- $\gamma$ ).
${ }^{157} \mathrm{Ho}$ and ${ }^{159} \mathrm{Ho}$ and their daughter products were observed in the spectrum due to the ( $\alpha, 6 n$ ) and ( $\alpha, 4 n$ ) reactions.

The experimental information consists of $\gamma$-ray spectra (in and out of beam), the life-time of the isomeric state measured using the cyclotron pulses and the prompt and delayed $\gamma-\gamma$ coincidences. The results of our experiments are summarized in table $I$ and in figures $1,2,3$ and 4 . In table I only the energies and the relative $\gamma$-ray intensities for the lines of ${ }^{158} \mathrm{Ho}$ and ${ }^{158} \mathrm{Dy}$ are tabulated. A spectrum obtained using the delayed coincidence method is presented in figure 1. In this figure the $156.9 \mathrm{keV} \gamma$-ray is taken as the gate STOP. Figure 2 gives an example of the prompt coincidences for the $115.1 \mathrm{keV} \gamma$-ray. The decay curve for the 156.9 keV line of ${ }^{158} \mathrm{Ho}$ is shown in figure 3.
3. Data analysis and results. - In the course of measurement of in and out of beam gamma spectra, an intense delayed gamma line at 156.9 keV was found to decay with a half-life of $(29 \pm 3) \mathrm{ns}$. A comparison of this value with those assigned for the isomeric states in odd-odd holmium isotopes is given in the following table.

|  | ${ }^{164} \mathrm{Ho}[4]$ | ${ }^{162} \mathrm{Ho}[5,6]$ | ${ }^{160} \mathrm{Ho}[5]$ | ${ }^{158} \mathrm{Ho}$ |
| :--- | :---: | :---: | :---: | :---: |
|  | - | - | - | - |
| Spin | $6^{-}$ | $6^{-}$ | $\left(5^{-}\right)$ |  |
| $T_{1 / 2}$ | 37.5 min. | 68 min. | 60 ns | 29 ns |
| Energy | 139 keV | 106 keV | 118.1 keV | 156.9 keV |

Thus, while both the ${ }^{162} \mathrm{Ho}$ and ${ }^{164} \mathrm{Ho}$ nuclei seem to have a $6^{-}$isomeric state with the

$$
\text { p } 7 / 2^{-}[523] \uparrow \text { n } 5 / 2^{+}[642] \uparrow
$$



Fig. 3. - The decay of the 156.9 keV peak.


Fig. 4. - Plot of effective inverse moments-of-inertia associated with individual cascade transitions for ${ }^{158} \mathrm{Ho}$ and ${ }^{160} \mathrm{Ho}$.
configuration, the isomeric state observed at 118.1 keV in ${ }^{160} \mathrm{Ho}$ apparently has not this configuration as reported by Leigh, Stephens and Diamond [5]. These authors indicated that the $6^{-}$state should also occur in ${ }^{160} \mathrm{Ho}$ and the rotational band observed is probably based on this state with the configuration $6^{-}$, p 7/2- [523] $\uparrow \mathrm{n} 5 / 2^{+}$[642] $\uparrow$. This conclusion was based on the very great similarity between the sequence of $\gamma$-rays transitions in both ${ }^{162} \mathrm{Ho}$ and ${ }^{160} \mathrm{Ho}$. Moreover the oscillations in the energy level spacings for ${ }^{162} \mathrm{Ho}$ and ${ }^{160} \mathrm{Ho}$ obtained by plotting

$$
\left(E_{I}-E_{I-1}\right) / 2 I \text { vs } f(2 I)^{2}
$$

are in phase. The isomeric state could be a $5^{-}$state with the configuration p 7/2- [523] $\uparrow \mathrm{n} 3 / 2^{+}$[402] $\downarrow$.


Fig. 5. - Proposed level scheme of ${ }^{158} \mathrm{Ho}$.
With regard to the nucleus ${ }^{158} \mathrm{Ho}$, it must be noted that the sequence of $\gamma$-transition is different from that in ${ }^{160} \mathrm{Ho}$. This discrepancy may be explained by the presence of the p 7/2- [523] Nilsson level in the
configuration which shows strong perturbation by Coriolis coupling. The increasing perturbation of the p 7/2- [523] band with decreasing mass number is indicated by the variation of the strength of fluctuations in neighbouring ${ }^{157} \mathrm{Ho}$ and ${ }^{159} \mathrm{Ho}$ nuclei [7]. Figure 4 shows this in a plot of $f(2 I)^{2}$ for ${ }^{160} \mathrm{Ho}$ and ${ }^{158} \mathrm{Ho}$. It is clear that the perturbation in the energy level spacing of ${ }^{158} \mathrm{Ho}$ is stronger than that in ${ }^{160} \mathrm{Ho}$. If we suppose that the curves $\left(E_{I}-E_{I-1}\right) / 2 I$ must be in phase in both ${ }^{160} \mathrm{Ho}$ and ${ }^{158} \mathrm{Ho}$, the 156.9 keV state of spin $5^{-}$must be assigned as the isomeric state in the ${ }^{158} \mathrm{Ho}$ nucleus. The spin $I=K=6^{-}$might be attributed to the head of the rotational band.

However, two other assumptions are also possible :

1) The $6^{-}$state could be attributed as the isomeric state and considered as the head of the rotational band.
2) The isomeric state could be assigned as the $5^{-}$ state by supposing a weak transition between the $6^{-}$ and $5^{-}$state. We could not see a gamma line of such low energy with our experimental arrangement; if present, it is undoubtedly highly converted and will be difficult to observe. In this case the $\gamma$-ray
of 72.9 keV could represent the transition between the $7^{-}$and $6^{-}$states.

By choosing the spin and parity of the isomeric state as $5^{-}$, a possible configuration for this state is p $7 / 2^{-}[523] \uparrow \mathrm{n} 3 / 2^{+}$[402] $\downarrow$. According to Galla-gher-Moszkowski's rule, the $2^{-}$state of 67.3 keV in ${ }^{158} \mathrm{Ho}$ is the lower member of the doublet. However, this situation leads to a different interpretation from that given in refs. [2, 3].
4. Conclusion. - a) The level scheme of ${ }^{158} \mathrm{Ho}$ proposed on the basis of our experiments is shown in figure 5.
b) The rotational band observed in ${ }^{158} \mathrm{Ho}$ is highly perturbed by Coriolis coupling. This is due to the fact that the orbits of the proton and neutron states originate from high-j shells of $h_{11 / 2}$ and $i_{13 / 2}$ respectively and to the fact that with decreasing $A$ the perturbation increases rapidly in the neighbouring odd-A nuclei.

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