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Magnetic tracking for catheterization procedure, using giant-magneto-resistance and space-varying magnetic field free point

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ABSTRACT

X-ray fluoroscopic imaging is the standard method for obtaining catheter position and monitoring the patient's vascular network during catheterization procedures. However, this method exposes both patients and doctors to ionizing radiation. To address this issue, we propose an alternative method for tracking the catheter inside the human body by integrating a magnetic sensor at the catheter tip and generating a known magnetic field (MF) around the operative zone. The catheter's position can then be determined by measuring this MF.

Due to the mandatory small size of the catheter, we utilized giant-magneto-resistance (GMR) sensors for this tracking system. GMR sensors require only two wires for connection, have a wide bandwidth that allows flexibility in selecting the working frequency and can detect low-intensity MFs down to the nano Tesla range.

Our method is based on the time detection of a moving null MF, known as the Field-Free Point (FFP) for MF generation. This approach requires only a single sensor smaller than $300 \mu\text{m}^2$, making it suitable for any catheter. We constructed an experimental setup to demonstrate the feasibility of this method in one dimension and obtained promising performance results.

KEYWORDS

Magnetic tracking, catheter position assessment, micrometric magnetic sensor.

HIGHLIGHTS

- A method based on magnetic particle imaging is adapted to track a catheter
- Small sized giant magnetoresistors are integrated into a catheter
- An experimental setup is built to show the tracking feasibility in 1D

I - INTRODUCTION

Catheterization is a minimally invasive surgery used for various diagnostic and therapeutic purposes [1]. These procedures typically involve a small incision (1 to 3 mm, according to [2]), do not always require general anesthesia, and can be fast to perform, among other advantages [3]. With the help of a contrast agent opaque to X-rays, doctors can get a 2D image showing the catheter inside the patient's blood vessel. For example, it can detect potential aneurysms and assess the patient's vascular network condition. Medical professionals treat aneurysms through different procedures, including coiling or stent placement [4], all carried out through an inserted catheter.

Although catheterization has seen extensive development, there remains room for improvement [5]. Despite careful dosage and protective equipment, X-rays still raise safety concerns due to ionizing radiation exposure for both patients and medical staff, particularly

87 during long procedures. Additionally, practitioners must rely on a 2D image showing a projection
88 of the 3D arteria, which can impede navigation [5, 6]. In clinical use, the position of the catheter
89 must be known with good precision and in real-time [7]. Hence, time and spatial resolutions are
90 critical specifications of catheter tracking systems [8]. X-ray fluoroscopy performs significantly
91 well with a spatial precision below 1 mm and an image at around 24 Hz sampling frequency,
92 creating real-time visualization. X-ray imaging is a mature technology, and its characteristics will
93 be challenging to overcome. Nonetheless, they give a baseline for comparison.

94
95 However, X-ray fluoroscopy is not without its limitations, including the associated radiation risks
96 and the need for injection of contrast agents, which are not suitable for all patients, especially
97 those with kidney deficiencies. The magnetic tracking (M-tracking) system developed in this
98 study does not directly compete with X-rays but could be a contributing imaging method to
99 improve overall vascular treatment. In this regard, besides a lesser spatial or temporal resolution,
100 the M-tracking shows many other advantages. One key advantage is that M-tracking eliminates
101 ionizing radiation, reducing potential risks, particularly in procedures requiring prolonged
102 exposure. For example, it could reduce the dose of contrast agents for kidney-deficient patients
103 [9]. Moreover, M-tracking's ability to operate without continuous X-ray use can offer added
104 safety, potentially decreasing cumulative radiation exposure for both patients and clinicians.
105 From a long-term perspective, the M-tracking could be a first step toward a non-radiative imaging
106 method. However, obtaining an image of the vascular network and overlaying the catheter's
107 position will be necessary, which may be challenging, particularly due to breathing movements.

108
109 Regarding the Magnetic Field (MF) generation and waveform, there are different approaches to
110 obtaining a position from a magnetic measurement. A known method is to find the position of
111 the sensor by optimizing the unknown position and orientation in the three directions of space,
112 denoted $(x, y, z, \alpha, \beta, \gamma)$, so the measured field matches the calculation for those positions.
113 Examples of such system can be found in [10] or [11] and usually requires 3 orthogonal sensors.
114 The MF encodes the volume with a nearly bijective relationship between positions and MF
115 measurements. Our system is different; it was inspired by the magnetic particle imaging (MPI)
116 setup described in [12]. If the Magnetic Field (MF) can be zero at a unique position called Field
117 Free Point (FFP) at a given time, and if this FFP can move throughout the whole volume, then
118 knowing when the sensor measures the FFP would indicate its position. Therefore, a time-varying
119 MF with an FFP covering the entire volume must be built to make such tracking possible. This
120 work's novelty relies on the single magnetic sensor and the tracking routine. Indeed, to our
121 knowledge, only few magnetic tracking uses a GMR sensor such in [13], even though the
122 possibility has been mentioned [14]. Most of other application use coils or commercially available
123 Hall-effect sensor [15]. GMR sensors are highly sensitive and can detect low-intensity MFs,
124 including static fields, over a wide frequency range. Their small size (tens of micrometers)
125 facilitates miniaturization, even for the most minor catheters with diameters as small as 300 μm .

126
127 Using MF with a sensor inside a catheter requires a small and precise sensor. GMR sensors are
128 well-suited for this purpose, being extremely compact and capable of detecting low-intensity
129 fields. Their wide bandwidth allows for adaptation to the clinical environment, particularly in
130 noisy settings such as clinical rooms. This paper demonstrates that in a 1D configuration, the GMR

131 and the innovative tracking algorithm are useful for determining the sensor's location. The
 132 achieved time and spatial resolutions provide a baseline for future improvements and the
 133 transition to 2D and 3D configurations.

134

135 **II – GIANT MAGNETO-RESISTANCE SENSOR**

136

137 GMRs are composed of multiple thin layers, including two ferromagnetic films separated by a
 138 non-magnetic metallic spacer, with a total active thickness typically less than 30 nm. These layers
 139 are deposited on a silicon substrate (around 300 μm thick), which can be thinned down if
 140 necessary [16, 17]. Table 1 shows the detailed composition of a typical GMR sensor and the
 141 thickness of each layer.

142

143 **Table. 1** – GMR typical layers' composition and thickness in nm [13].

144

Layer composition	Ta	NiFe	CoFe	Cu	CoFe	Ru	CoFe	IrMn	Ru	Ta
Layer thickness (nm)	3	5	2.1	2.3	2.1	0.85	2	6	0.4	5

145

146 GMRs have a wide frequency range and can even operate under static MF. They can detect low-
 147 intensity fields in the nano Tesla range [18]. These characteristics make them suitable candidates
 148 for our applications. The first ferromagnetic layer, known as the reference (or fixed) layer, acts as
 149 a permanent magnet. The second ferromagnetic layer, called the free (or unfixed) layer, is
 150 magnetically soft and changes its magnetization in response to external magnetic fields. These
 151 changes lead to fluctuations in overall resistance due to the spin-dependent charge transport
 152 phenomenon [19].

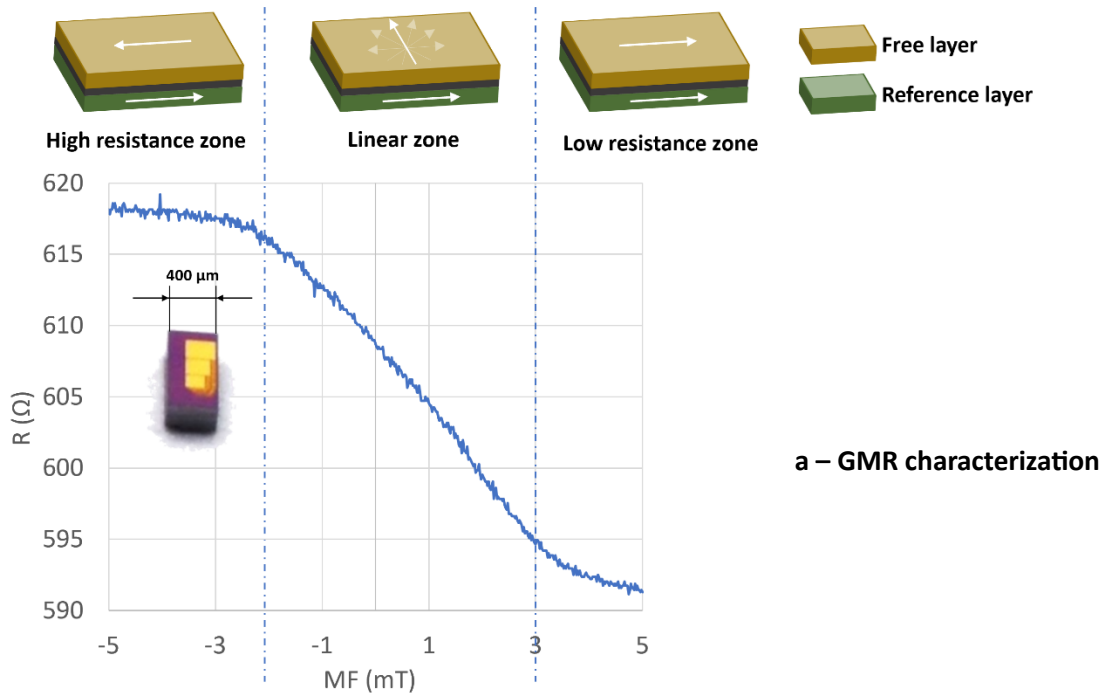
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154 The shape anisotropy of the free layer determines the GMR's linearity. At rest, without an
 155 external field, the angle between the reference and the free layers' orientation is 90°. When a
 156 field is applied in the plane of the stack, the angle can decrease to 0°, reducing the resistance
 157 accordingly. When an opposite field is applied, the angle increases to 180°, and the resistance
 158 increases.

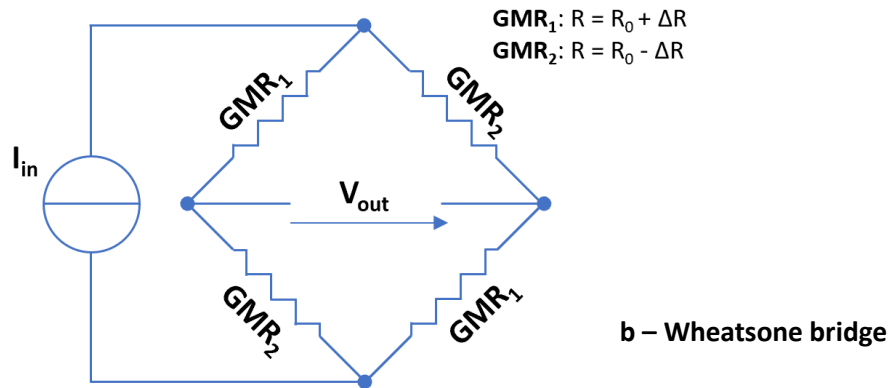
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160 In Fig. 1, we first characterized the GMR used in this study using Helmholtz coils [20, 21]. We
 161 monitored the evolution of the resistance vs. MF ($R(\text{MF})$, Fig. 1a). Then, we implemented it in a
 162 Wheatstone bridge (Fig. 1c). The voltage drop across the bridge for different levels of applied MF
 163 was recorded (Fig. 1b). Where $V_{\text{out}}(\text{MF}) = \Delta R(\text{MF}) \cdot I_{\text{in}}$, ΔR is the GMR resistance variation, and
 164 I_{in} the Wheatstone bridge imposed input current. The Helmholtz coils create a precise and easy-
 165 to-control magnetic field in the volume where the sensor is positioned, allowing us to obtain the
 166 typical response curve. The orientation angle between the reference and the free layers is almost
 167 at its maximum for a field of -2.5 mT and its minimum for 2.5 mT. Between these values, the
 168 change in resistance follows a quasi-linear trend. This field window constitutes the working range
 169 where the GMR behaves as a magnetic sensor. The Wheatstone bridge (Fig. 1c) enhances
 170 sensitivity and accuracy in detecting the small resistance changes of the GMR by suppressing the
 171 resistance offset of each element and some possible thermal drift. The chip in the bottom part of
 172 Fig. 1a includes four integrated Wheatstone bridges. Due to its prominent electrical contacts, it is

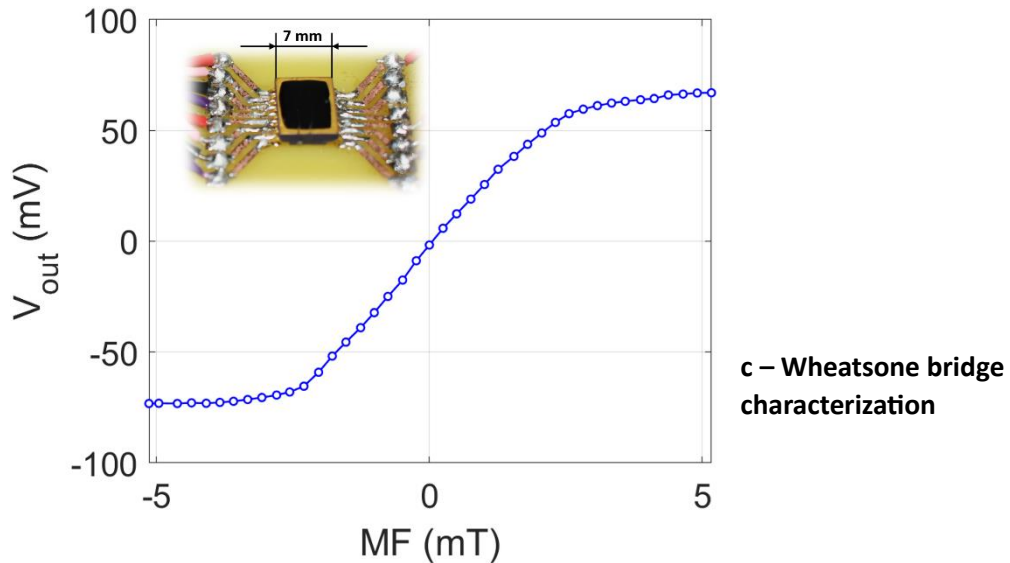
173 easier to manipulate in the laboratory. Since it integrates the same GMR as those implemented
 174 in the catheter, we used it for most of the experimental results reported in this work.
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181
 182 **Fig. 1a** – Resistance of the GMR vs. an external magnetic field. The top sketches show the
 183 corresponding ferromagnetic layers' magnetic orientations. **Fig. 1b** – GMRs plugged in a Wheatstone
 184 bridge configuration. **Fig. 1c** – Output voltage V_{out} along the Wheatstone bridge supplied with a current
 185 source of $I_{in} = 1$ mA for the typical GMR used in this study vs. an in-plane external magnetic field (MF).
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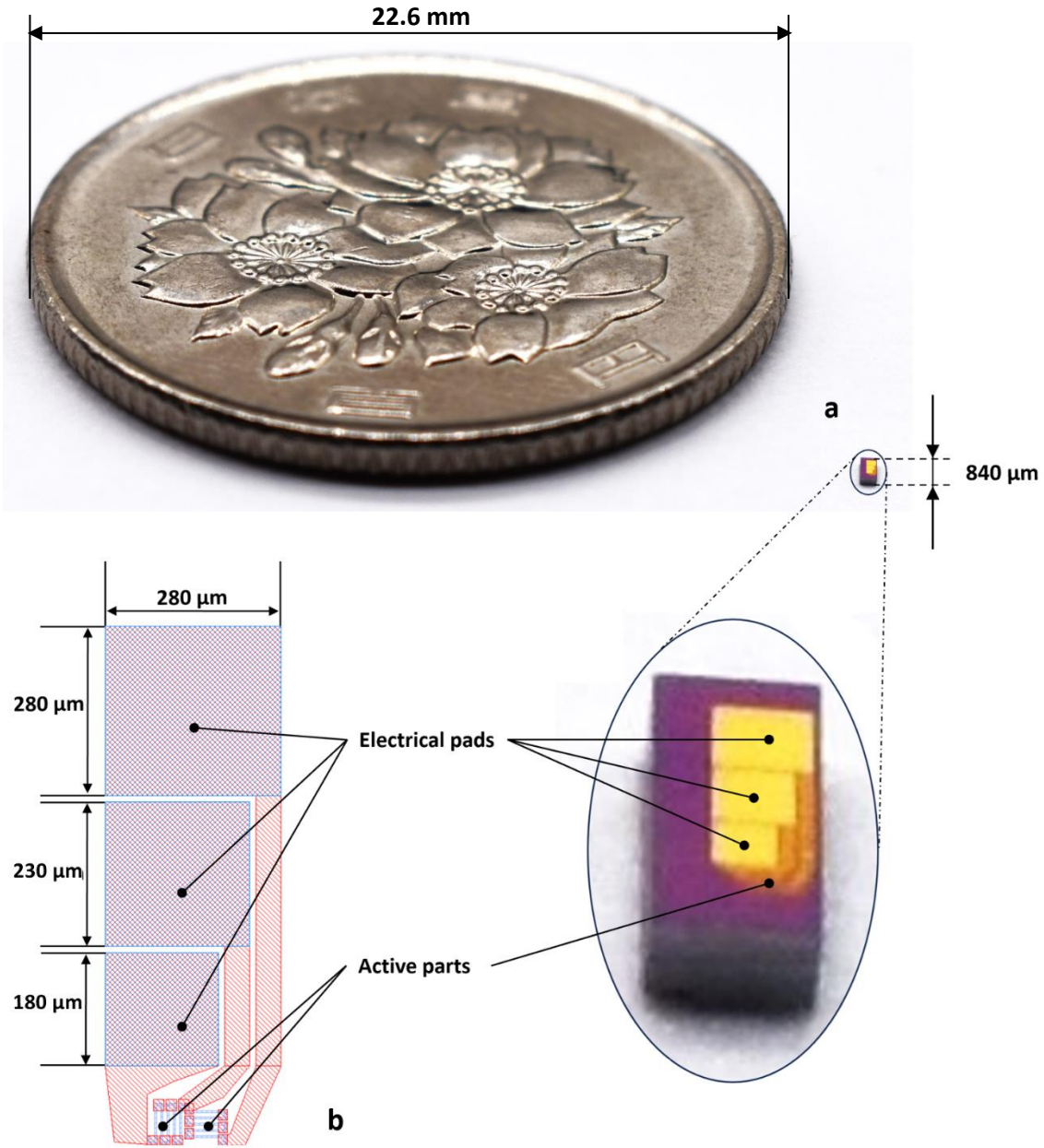
187 GMR sensors offer long-term stability due to their solid-state nature, which eliminates moving
 188 parts and reduces the risk of mechanical failure. Their operation based on spin-dependent
 189 electron transport is highly stable, ensuring consistent performance over time. Furthermore, their
 190 resilience to environmental fluctuations such as temperature changes and electromagnetic
 191 interference adds to their reliability, making them particularly suitable for clinical applications
 192 where precision and durability are essential.

193 When compared to other magnetic sensor technologies, GMR sensors offer a compelling
 194 combination of advantages for catheter tracking. Unlike Hall-effect sensors, which are robust but
 195 lack the sensitivity required to detect weak magnetic fields, GMR sensors can operate in the nano-
 196 Tesla range, making them ideal for precise applications. While anisotropic magnetoresistance
 197 (AMR) sensors offer better sensitivity than Hall sensors, they still fall short of the performance of
 198 GMR in detecting low-intensity magnetic fields. Tunneling magnetoresistance (TMR) sensors,
 199 though comparable in sensitivity to GMR, are more complex and require additional wiring, which
 200 can be cumbersome for catheterization procedures. GMR sensors strike a balance between high
 201 sensitivity, minimal wiring, and low power consumption, making them particularly suited for
 202 space-constrained environments such as medical catheters.

203
 204 **II – INSTRUMENTED CATHETER**
 205

206 The integration of GMR sensors is a significant challenge in this work. The catheters we target
 207 can have an outer diameter as small as 300 μm , as seen in neurovascular applications [22]. Typical
 208 commercially available GMRs are too bulky to be integrated into a catheter. Therefore, additional
 209 GMRs have been designed with integration in mind, making them small enough for catheter
 210 integration. Fig. 2a depicts a photograph of the prepared chips, and Fig. 2b provides a detailed
 211 description and the dimensions.

212



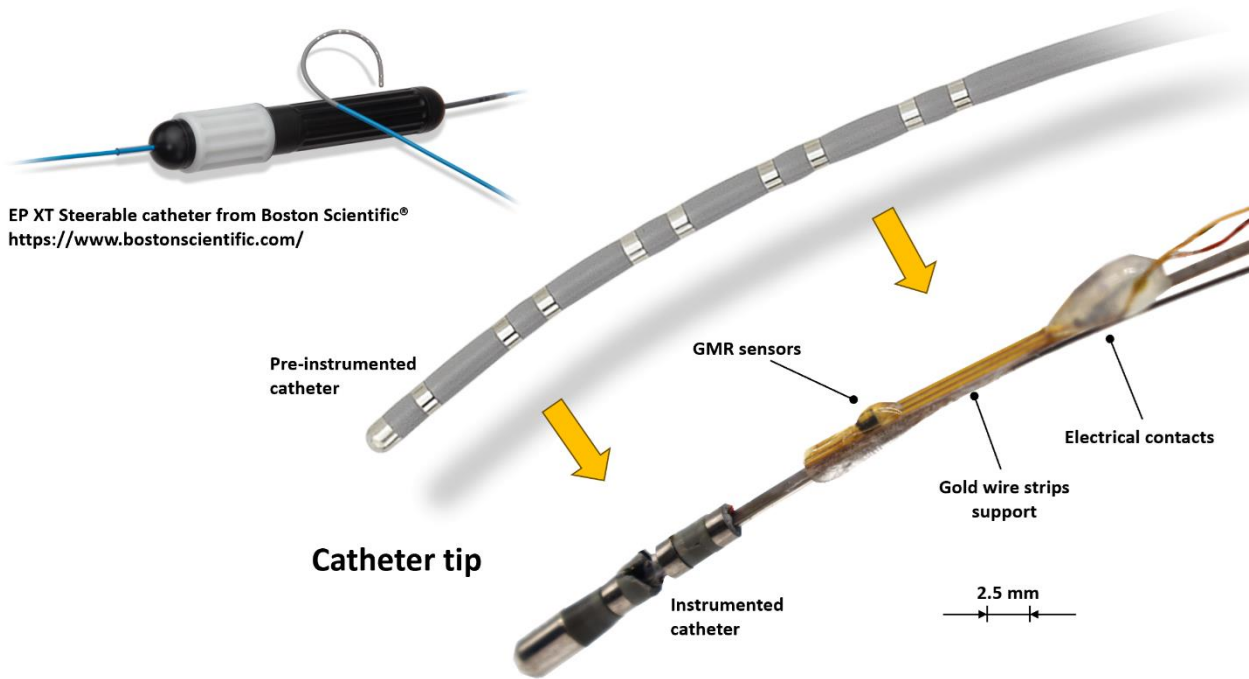
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215 **Fig. 2a** – Picture of the GMR chip. **Fig. 2b** – Description and dimensions of a typical GMR chip
 216 designed for integration on the catheter.
 217

218 Each chip contained two orthogonally arranged GMR sensors, designed to measure magnetic
 219 fields in two directions for potential 2D tracking applications. While this study focused on using a
 220 single sensor for one-dimensional measurements, the same chip can be leveraged in future work
 221 to perform additional 2D tracking tests, demonstrating the versatility of the GMR configuration.
 222 The most prominent parts of the chip are the connection pads, which range from 180 x 180 μm²
 223 to 280 x 280 μm², whereas the active area occupies less than 100 μm² for the two GMRs. The chip
 224 shape and size provide a degree of freedom that can be adjusted when necessary.

225 As a preliminary proof of concept, we mounted a 300 x 700 μm sensor chip onto a catheter with
 226 a 1.5 mm outer diameter. We achieved it by welding the GMR to a flexible gold strip PCB, which
 227 included three gold strips. Each GMR pad was wire-bonded to a gold strip using gold wire. The
 228 catheter's existing wires were soldered on the other end of the gold strips to ensure the electrical
 229 connections. Finally, we covered each part with epoxy for protection. Fig. 3 depicts the resulting
 230 instrumented catheter. Having the sensor at the catheter tip is critical for delivering precise
 231 positional information, still at this study stage and for convenience, we positioned the sensor two
 232 centimeters away from the catheter tip rather than at the tip itself, meaning the measured
 233 position will not correspond exactly to the tip position.
 234



235
 236
 237 **Fig. 3** – Instrumented catheter, including the GMR sensor and the electrical contacts.
 238

239 Our custom-made GMR sensors offer several advantages over commercial alternatives,
 240 particularly in size and performance customization. Their significantly smaller dimensions make
 241 them ideal for integration at the catheter tip. Also, our sensors are specifically tailored for
 242 catheter tracking applications, allowing for the fine-tuning of their magnetic response to match
 243 the experimental conditions.
 244

245 **III – TRACKING POSITION ALGORITHM**
 246

247 Most existing MF-tracking technologies rely on multiple sensors, each sensitive to one spatial
 248 axis. For example, the method described in [10] or [13] combines three sensors. By generating a
 249 known static field and measuring its three spatial components, it is possible to fully determine
 250 the sensors' position (x, y, z) and orientation (α, β, γ) . Most other solutions described in the
 251 scientific literature are based on the same principles but use different sensor technologies (coils

252 in [23, 24]) or methods to generate the Magnetic Field (MF) (eight emitting coils in [25], or a
253 planar field generator in [26]).

254
255 The method proposed here differs in the MF generation and how to determine the sensor and,
256 therefore, catheter position. It could theoretically reduce the number of sensors needed to only
257 one, significantly decreasing the required size and the complexity of the catheter manufacturing.
258 However, it increases the setup complexity. A time-varying MF is created instead of a static MF
259 and is used to compute the sensor's position. This MF is null at a unique point in space called the
260 Field Free Point (FFP). The FFP moves over time inside the working volume. At any given time
261 step, there is a unique FFP. Searching when the GMR sensor detects the FFP allows us to estimate
262 its position accurately.

263
264 This method was inspired by solutions found in the magnetic particle imaging (MPI) framework,
265 where the working volume is swept with an FFP to obtain the local concentration measurements
266 of magnetic nanoparticles [8][27]. The magnetic response from the particles is typically measured
267 via pick-up coils. The FFP method in MPI involves creating a region with no magnetic field,
268 surrounded by areas with high magnetic field gradients. When superparamagnetic nanoparticles
269 are introduced into the body, they align with the magnetic field. By scanning the FFP across the
270 region of interest, MPI detects how the nanoparticles respond to the changing magnetic fields.
271 This data is then processed to reconstruct a detailed image, highlighting the distribution of
272 nanoparticles and providing insights into physiological and pathological conditions [28-30].

273
274 In our study, the GMR sensor replaces the superparamagnetic particles. Moving the FFP inside
275 the operation volume [31] can be done through several methods. The MF induced by a current
276 flowing through a single circular coil, offset from the center by O_z , can be expressed analytically
277 (Eq. 1). In one dimension, considering the field along the rotation axis of the coil, the B_z
278 component is given by:

279
$$B_z = \frac{\mu_0 a^2}{2} \cdot \left[\frac{iN}{(a^2 + (z + O_z)^2)^{3/2}} \right] \quad (1)$$

280 Where i is the current flowing through the coil, N is its number of turns, a its radius, and μ_0 the
281 vacuum permeability. This formula corresponds to a coil with its rotation axis along the z-axis, as
282 illustrated in Fig. 4 below.

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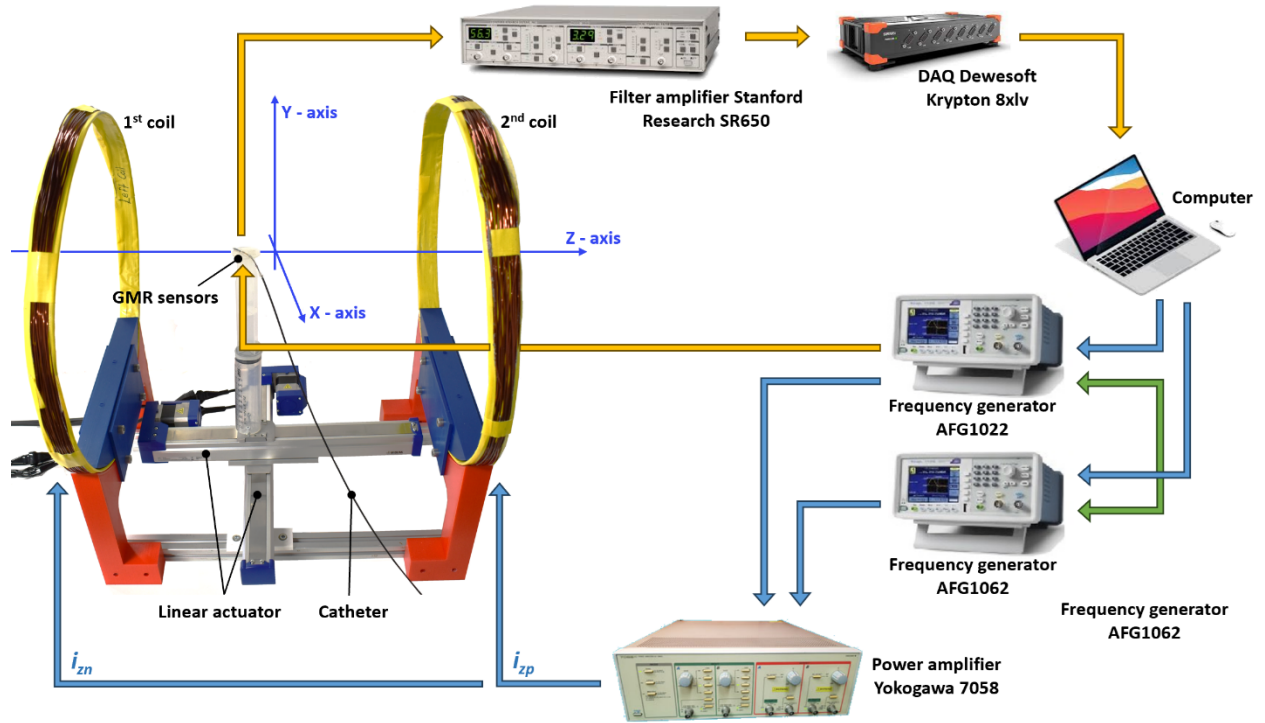


Fig. 4 – Schematic and photo of the 1D experimental setup.

If another similar coil is positioned at the offset $-O_z$ position and two electrical currents, i_{zp} and i_{zn} flow through them, B_z is equal to the addition of the field induced by each coil (Eq. 2):

$$B_z = \frac{\mu_0 a^2}{2} \cdot \left[\frac{i_{zp} N}{(a^2 + (z + O_z)^2)^{3/2}} + \frac{i_{zn} N}{(a^2 + (z - O_z)^2)^{3/2}} \right] \quad (2)$$

Setting the middle of the coils as $z = 0$ induces an opposite spatial offset $\pm O_z$. Eq. 2 depends solely on the electrical currents and the z position, as the radius and the offset distance are known values. When an opposite current is applied to each loop ($i_{zp} = -i_{zn}$), B_z is zero at the position $z = 0$. This FFP is unique on the z -axis and for this combination of currents.

There is a single ratio of currents leading to an FFP for each position. In higher dimensions (2D or 3D), with two coils, more zeros would appear, but only one would remain on the z -axis when B_x and B_y are zero. Fig. 5 shows three profiles. Each current ratio creates a unique FFP at a different position. It is possible to supply both coils with carefully chosen currents varying over time so the FFP moves along the z -axis in the zone separating the excitation coils. Numerous possible current input functions lead to a moving FFP [32]. The differences between them will be in the speed, acceleration, and trajectory of the FFP. These functions will likely impact the system's performance and will be investigated carefully in the following sections of this work.

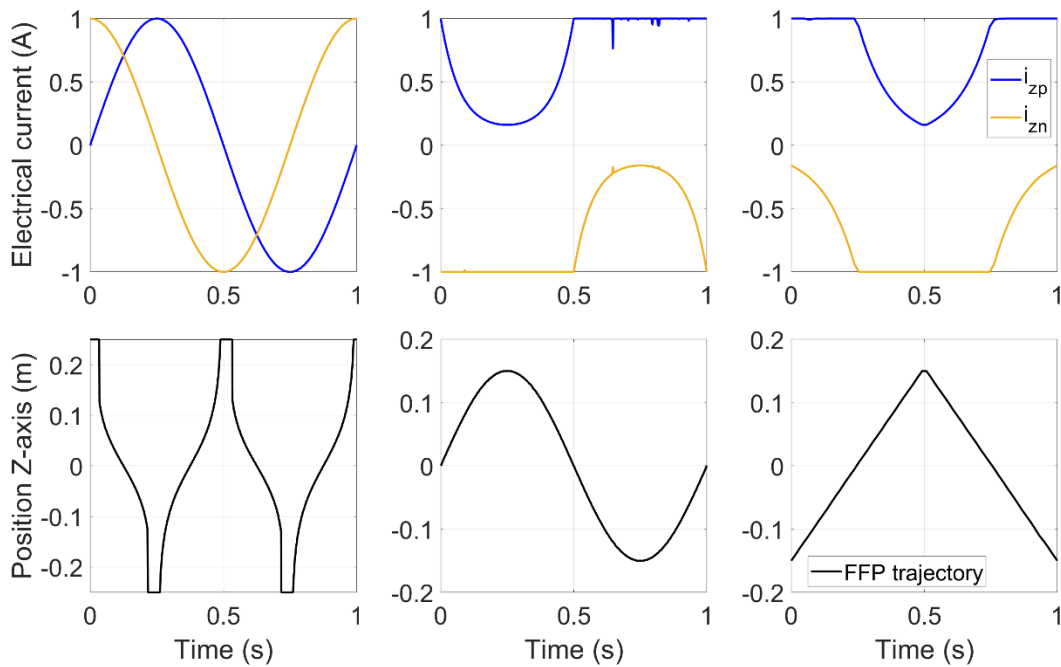


Fig. 5 – Electrical currents i_{zp} and i_{zn} in the excitation coils and their corresponding FFP trajectory below.

When the coils are supplied with specific currents, the GMR sensor detects the FFP at a particular time. This timing depends on the sensor's position. One advantage of this method is that it works with a single sensor. Conversely, because the angles are unknown, measuring a non-zero value would not enable determining the position. Considering a sensor in a random orientation (α, β, γ) , its measured signal depends on the magnetic field vector description (B_x, B_y, B_z) and the angle of the sensor, such as $B_x \sin(\alpha) + B_y \sin(\beta) + B_z \sin(\gamma)$. This expression confirms that it is impossible to determine the component or angle with a single measurement.

Now, if in a unique position, $|B| = \sqrt{B_x^2 + B_y^2 + B_z^2} = 0$, the sensor will measure this null Magnetic Field (MF) independently of its angle. Hence, measuring a zero implies that every component is equal to zero. A zero could still be obtained when the magnetic vector is perfectly orthogonal to the sensor. Still, this situation is unlikely to happen, and using the sensor's previous position can help correct the error.

A time-dependent FFP position function $FFP(t) = (x, y, z)$ can be defined by describing the position of the FFP over time. The measurement is worth zero when the sensor and the FFP are in the same position, thus giving the sensor position at different instants. The time it takes for the FFP to scan the whole volume gives the rate of position acquisition, hence temporal resolution. The current supplied to the coils and the position function are directly linked. In Fig. 5, three different position functions (bottom row) and their respective current (top row) are shown in a single-dimension configuration. Those functions can be obtained by calculating the MF, B_z and searching the position of the zero for an arbitrary current ratio, as used to compute the sinusoidal

336 current (Left-hand-side plots in Fig. 5). The other way is to arbitrarily decide the position of the
337 zero and optimize the currents via an optimization algorithm using SciPy python module. The
338 second method was used to compute the currents for the sinusoidal (middle plots) and triangular
339 position functions (right-hand-side plots). Because the optimization is not always perfect, some
340 outliers can be seen in Fig. 5 when computing the current for the sinusoidal position function.
341 The current peaks could be removed without changing the FFP trajectory.

342

343 **IV – EXPERIMENTAL RESULTS**

344

345 ***4.1 Experimental setup***

346

347 An experimental setup, schematically described in Fig. 4, was built, including two excitation coils
348 with a radius of 23 cm and 30 turns of 3 mm diameter copper wire. We determined the radius
349 and number of turns based on MF simulations. One significant characteristic of the field under
350 consideration was the field's spatial derivative; a steeper profile results in a more precise zero-
351 crossing. The spatial resolution is directly affected by the sensor's selectivity. With a distance of
352 50 cm between the coils, the generated field should be sufficient to achieve a spatial resolution
353 of 1 mm using our sensor.

354

355 The coils were driven by amplified, modulated sinusoidal currents produced by two separate
356 Tektronix (Beaverton, Oregon, USA) frequency generators, AFG1062 and AFG1022, for the right
357 and left coils, respectively. We achieved the signal synchronization using the synchronization
358 output of the first generator. We accomplished the voltage amplification using a Yokogawa
359 (Tokyo, Japan) 7058 power amplifier set to a gain of 10. The AFG1022 frequency generator also
360 provided the sensor with a 500 Hz sinusoidal signal at 3 V peak-to-peak through its secondary
361 channel.

362

363 The sensing was performed using the GMR sensor described in sections 2 and 3. This sensor
364 was mounted on a Misumi (Tokyo, Japan) RS102 translation stage, allowing movement over a 30
365 cm range along the common axis of the coils, as shown in Fig. 3, ensuring precise positioning. The
366 voltage drop across the GMR sensor was filtered and amplified using a Stanford Research
367 (Sunnyvale, California, USA) SR650 filter. Signal acquisition was carried out with a DEWEsoft
368 (Trbovlje, Slovenia) Krypton 8xLV acquisition system at a sampling frequency of 20 kHz.

369

370 ***4.2 Acquisition***

371

372 We supplied the GMR sensor and the coils with alternating waveforms to enable signal
373 extraction using a digital lock-in amplifier [33]. This method efficiently eliminates unwanted
374 frequency components from the signal and amplifies the relevant ones. The Wheatstone bridge
375 signal contains multiple frequency components, and the objective is to isolate the specific
376 component that carries the desired information. The signal under test is multiplied by both a sine
377 and a cosine wave at the same frequency as the target component. This operation results in two
378 new signals: one with a static component and another at twice the original frequency. By applying
379 a low-pass filter (LPF) to remove the alternating component and retaining only the static

380 component for both signals, it is possible to extract the amplitude of the target component and
 381 determine its phase difference relative to the reference sine and cosine signals. Below is the
 382 mathematical description of the lock-in amplifier process, assuming a pure sinusoidal input signal.
 383 This signal is multiplied by the sine and cosine wave at the same frequency:

$$384 \begin{cases} A_o \sin(2\pi ft + \phi) \cos(2\pi ft) = \frac{A_o}{2} \sin(4\pi ft + \phi) + \frac{A_o}{2} \sin(\phi) \\ A_o \sin(2\pi ft + \phi) \sin(2\pi ft) = \frac{A_o}{2} \cos(4\pi ft + \phi) + \frac{A_o}{2} \cos(\phi) \end{cases} \quad (3)$$

385 With A_o the amplitude of the signal under test, f its frequency, and ϕ its phase. By assuming a
 386 perfect low-pass filter, we reduce the signals to:

$$387 \begin{cases} X = \frac{A_o}{2} \sin(\phi) \\ Y = \frac{A_o}{2} \cos(\phi) \end{cases} \quad (4)$$

388 By using the two above components, we can express the phase and the amplitude:

$$389 \begin{cases} \sqrt{X^2 + Y^2} = \sqrt{\left(\frac{A_o}{2} \sin(\phi)\right)^2 + \left(\frac{A_o}{2} \cos(\phi)\right)^2} = \sqrt{\left(\frac{A_o}{2}\right)^2 (\sin(\phi)^2 + \cos(\phi)^2)} = \sqrt{\left(\frac{A_o}{2}\right)^2} = \frac{A_o}{2} \\ \arctan\left(\frac{X}{Y}\right) = \arctan\left(\frac{\frac{A_o}{2} \sin(\phi)}{\frac{A_o}{2} \cos(\phi)}\right) = \arctan(\tan(\phi)) = \phi \end{cases} \quad (5)$$

390 The GMR sensor response depends upon the supplied voltage and the coils' magnetic field (MF).
 391 The resulting voltage drop across the GMR can theoretically be described as follows:

$$392 V_{out} = \Delta R \cdot I_{in} \quad (6)$$

$$393 V_{out} = \Delta R I_0 \sin(2\pi f_{se} t) \quad (7)$$

$$394 V_{out} = Se \mu_0 H_0 \sin(2\pi f_c t + \phi) I_0 \sin(2\pi f_{se} t) \quad (8)$$

395 Using the product to sum trigonometric identities:

$$396 V_{out} = \frac{Se \mu_0 H_0}{2} \cos(2\pi(f_c - f_{se}) + \phi) - \frac{Se \mu_0 H_0}{2} \cos(2\pi(f_c + f_{se}) + \phi) \quad (9)$$

397 Where f_{se} and f_c are the signal frequency in the sensor and the coils, in this work, we set them
 398 to 500 Hz and 425 Hz, respectively. Se represents the sensor sensitivity, i.e., the variation of the
 399 resistance of the GMR vs. the applied magnetic field. The additive frequency component, $f_{se} + f_c$
 400 = 925 Hz, was extracted with a numerical lock-in amplifier to return the magnetic field amplitude.
 401 Eq. 6 is only valid for a constant field H_0 , corresponding to constant electrical currents in the coils.
 402 However, H_0 must change vs. time for the FFP to move. Therefore, the currents are amplitude-
 403 modulated signals with the envelope frequency chosen to be $f_p = 30mHz$ producing the FFP
 404 movement and the carrier at $f_c = 425Hz$ transmitting the information. Those currents are shown
 405 in Fig. 6a, with the corresponding FFP trajectory induced in Fig. 6b. The sensor was moved from
 406 +/- 15 cm along the z-axis to evaluate the setup performance, with 1 cm step increments and a
 407 total of $q = 31$ points. The sensor remained in the same position for 120 seconds, including 20
 408 seconds of transient regime (stabilization of the lock-in amplifier) and 100 seconds of acquisition.
 409 The final result was the average of the signal over the acquisition period. This approach improves

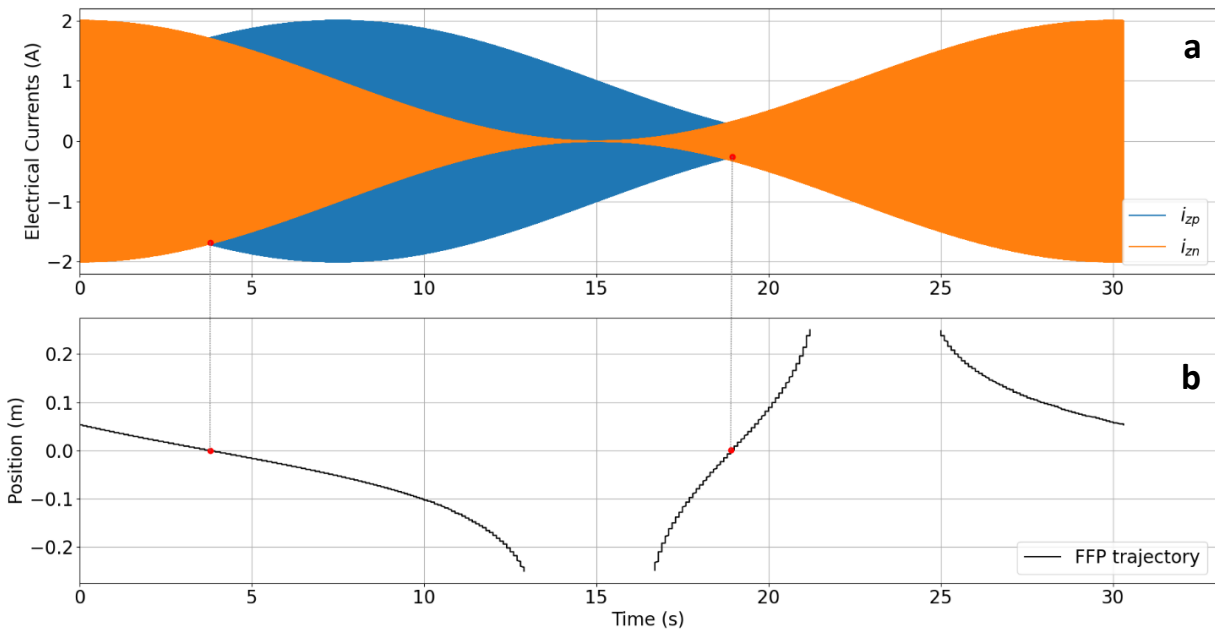
410 the spatial resolution at the cost of the temporal resolution. In this study, to prove the feasibility
411 of the tracking method, we decided to emphasize spatial resolution rather than temporal one.

412
413 Determining the position, even at a low rate, might prove helpful in performing discrete position
414 checks during the procedure. However, measuring a position with too much uncertainty is not
415 practical, regardless of the image refresh rate. During the 100-second acquisition, we measured
416 the position six times to evaluate the variability. Since the sensor remains stationary during this
417 time, the variability should be minimal, and the measured position should align with the actual
418 position.

419 4.3 Results

420
421
422 Fig. 7 shows the first results using the position function displayed in Fig. 6b. The function links
423 the time corresponding to the FFP measurement to a given position. The plotted result
424 corresponds to the average value obtained over the six measurements for each position. The
425 variability (+/- one standard deviation) below 1 mm is too small to be visible in this plot. The
426 orange dotted line is the target. This first result (Fig. 7) leads to an average standard deviation for
427 the complete trajectory (31 positions) of 0.993 mm, reaching a spatial resolution below 1 mm.

428



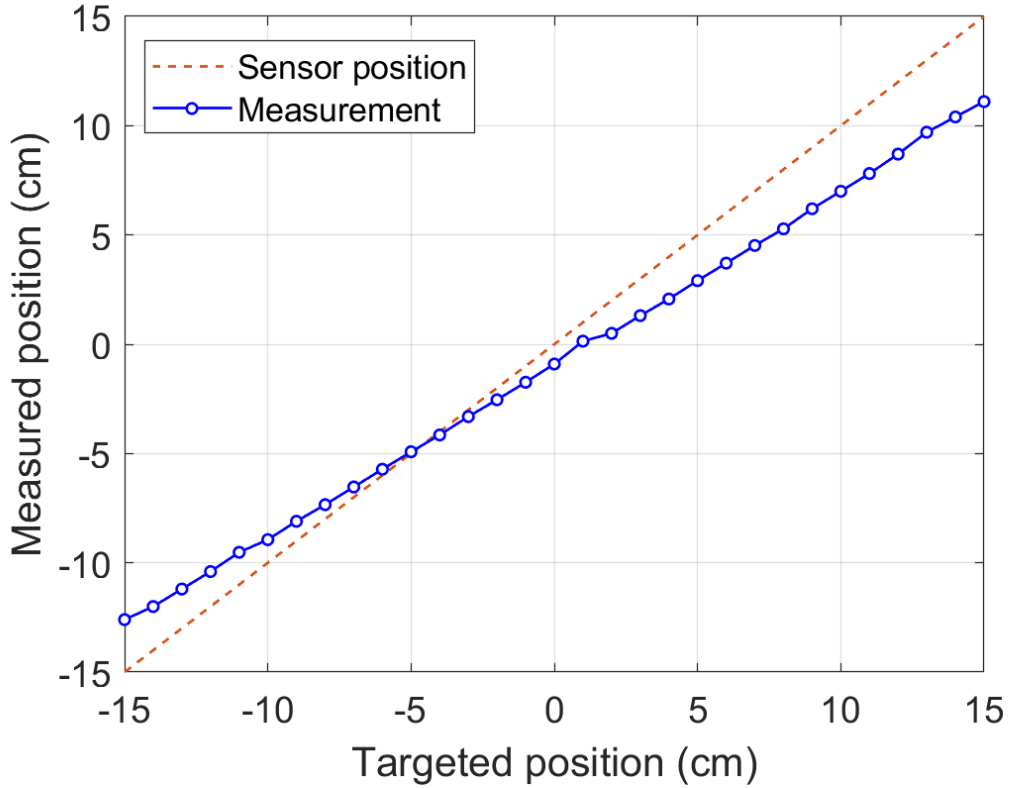
429

430

431 **Fig. 6a** – Electrical current in the excitation coils (i_{zp} , i_{zn}) modulated through a sinusoidal wave.

432 **Fig. 6b** – Corresponding time-dependent positioning function used to return the position. When
433 modulated currents are equals, the FFP is at 0m, middle position of the coils as shown with the
434 dotted line.

435



436
437

Fig. 7 – Comparison between the targeted and experimental positions measured with a lock-in low-pass filter time constant of $\tau = 1\text{ s}$ for a 100 s acquisition time and after a 20 s transient phase.

441

442

The resulting error for this test calculated based on the relative Euclidean distance criteria (RED%) defined in Eq. 10 [34] gave 27.9 %:

443

444

$$\text{RED}(\%) = \frac{100}{q} \cdot \sum_{i=1}^q \frac{\sqrt{(\text{Position}_{\text{exp}i} - \text{Position}_{\text{targ}i})^2}}{\sqrt{(\text{Position}_{\text{targ}i})^2}} \quad (10)$$

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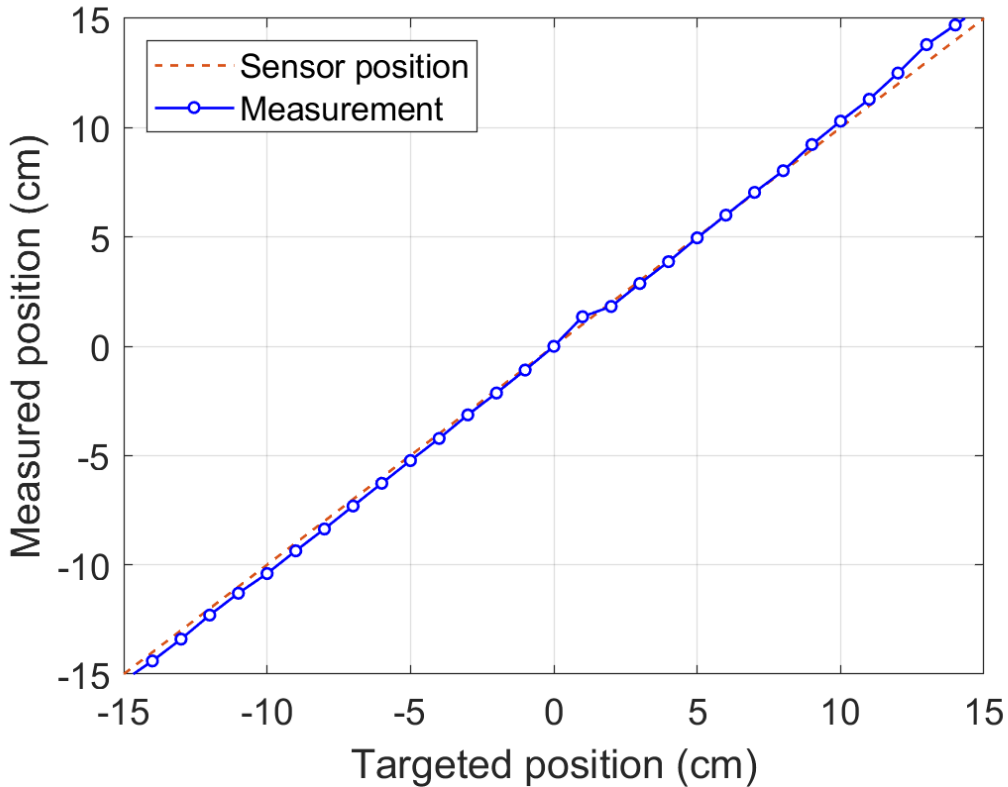
However, we can observe a linear deviation in the experimental results of Fig. 7. This issue might come from an error in the position function (Fig. 6b) after the data acquisition. A minimum RED(%) could have been expected at the zero position with increasing errors on each side since the field derivative should be highest at zero and decrease as one moves towards the coils. This phenomenon, although present, displays an offset to the position of -5 cm. An asymmetry in the currents inside the coils could explain this. Therefore, we applied a linear correction to the function to solve it. As long as the error is consistent, we can use such a correction to achieve better positioning accuracy. The correction was computed by changing the amplitude of the position function and adding a shift as described in Eq. 11:

$$\text{Correction}(\delta) = A\delta + B \quad (11)$$

456 Where δ is the position, A and B are constants set to 1.3 and 0.009, respectively.

457

458 Once the correction was applied, we plotted the newly measured position (see Fig. 8); this new
459 set of experimental results reached a promising average RED(%) of 4.89 %. The correction greatly
460 reduced the error but at a small cost of precision as the average standard deviation increased to
461 1.3 mm.



462

463

464 **Fig. 8** – Comparison between the targeted and experimental positions after correction.

465

466 **V – CONCLUSION**

467

468 In this study, we proposed and verified the feasibility of an innovative method for tracking
469 catheter position using a giant-magneto-resistance (GMR) sensor integrated within the catheter
470 tip. By generating a known magnetic field (MF) and utilizing the time detection of a moving Field-
471 Free Point (FFP), we established a system capable of precise catheter localization without ionizing
472 radiation.

473

474 Our experimental results, limited to a one-dimensional setup, demonstrated promising
475 accuracy and spatial resolution, achieving a standard deviation between 1.3 mm and 0.993 mm
476 with or without post-processing corrections. These performances align with the 1 mm goal for
477 vascular imaging and tracking applications. GMR sensors, known for their high sensitivity and
478 small size, proved advantageous for miniaturization and integration into catheters with
479 diameters as small as 300 μm . We assembled a homemade catheter associated with a GMR

480 sensor, demonstrating the integration possibilities. Further miniaturization is possible, and
481 potential studies will focus on further size reduction.

482

483 Although our method currently focuses on spatial resolution, our findings indicate potential for
484 further refinement and optimization to enhance both spatial and temporal resolution. Future
485 work will aim to transition from 1D to 2D and 3D configurations, explore more complex position
486 functions, and implement error correction mechanisms to improve positioning accuracy. The
487 current method relies on filtration, which limits the acquisition speed but reduces noise, and we
488 will study the balance between speed and noise reduction in higher-dimensional setups.

489

490 We also acknowledge the influence of external magnetic fields, including the Earth's magnetic
491 field, as well as potential interference from the human body. Future experiments will include a
492 calibration stage to correct for the Earth's magnetic field, ensuring accurate tracking. Although
493 the human body generates weak magnetic fields (typically 10–100 pT), we do not anticipate
494 significant interference with the catheter tracking system, given that our setup operates at much
495 higher field strengths (around 1 mT). Should further interference be detected, we will explore
496 the use of magnetic shielding to mitigate external noise.

497

498 Looking forward, we also plan to address the challenge of programming the FFP trajectory and
499 potentially integrating vascular maps into the tracking system. While the current design does not
500 synchronize with predefined vascular networks, future work could explore dynamic FFP control
501 based on patient-specific anatomy, enhancing the precision of catheter navigation. The addition
502 of such vascular mapping would further support real-time decision-making during procedures
503 and provide an essential complement to X-ray fluoroscopy, potentially reducing radiation
504 exposure and improving safety in complex vascular environments.

505

506 Additionally, the incorporation of a feedback mechanism could improve tracking speed and
507 accuracy as we expand into multi-dimensional tracking. Preliminary tests have demonstrated
508 that higher acquisition rates are key to achieving real-time adjustments, and optimizing the FFP
509 trajectory will further enhance the feedback-controlled tracking system. We will continue
510 refining these mechanisms to ensure optimal performance in 2D and 3D tracking scenarios.

511

512 In conclusion, the proposed magnetic tracking system represents a significant step toward
513 safer, more precise catheterization procedures, reducing reliance on ionizing radiation and
514 potentially enhancing the overall effectiveness of vascular treatments. The adaptability and
515 sensitivity of the GMR sensor, combined with the innovative FFP tracking method and future
516 improvements in both feedback mechanisms and vascular mapping, offer a promising avenue for
517 continued research and clinical applications.

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