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Modeling impairment of ionic regulation with extended Adaptive
 Exponential integrate-and-fire models
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11

Abstract

To model the dynamics of neuron membrane excitability many models can be considered, from the 12 most biophysically detailed to the highest level of phenomenological description. Recent works at the 13 single neuron level have shown the importance of taking into account the evolution of slow variables such as ionic concentration. A reduction of such a model to models of the integrate-and-fire family is interesting 15 to then go to large network models. In this paper, we introduce a way to consider the impairment of 16 ionic regulation by adding a third, slow, variable to the adaptive Exponential integrate-and-fire model 17 (AdEx). We then implement and simulate a network including this model. We find that this network was 18 able to generate normal and epileptic discharges. This model should be useful for the design of network 19 simulations of normal and pathological states. 20

21 **1** Introduction

In the study of seizure dynamics at the single neuron level, experiments have shown the importance of ionic regulation. Indeed, elevation of external ionic potassium concentration leads to seizure-like behaviors of the cells. Biophysical models have shown underlying mechanisms responsible for such activities [Depannemaecker et al., 2022b, Bazhenov et al., 2004].

Detailed biophysical network models have been developed to study seizure mechanisms [Rodrigues et al., 26 2015, Tejada et al., 2014, Santhakumar et al., 2005]. However, these models are complex with many parameters 27 and variables, making their dynamics difficult to analyze. While seizures are typically seen as network events, similar dynamics can also be observed at the single-cell level in biophysical models [Bikson et al., 2003, Bragin 29 et al., 1997, Chizhov et al., 2018, Cressman et al., 2009]. Phenomenological models, characterized by their 30 minimal number of parameters and variables, enable comprehensive dynamical analyses and replicate many 31 of the activities observed in experimental settings [Jirsa et al., 2014]. Some works integrate both approaches 32 by reducing a detailed biophysical model to a lower-dimensional form, preserving the benefits of a generic 33 model [Depannemaecker et al., 2022b].

³⁵ However, these models are based on the Hodgkin-Huxley formalism [Hodgkin and Huxley, 1952], where ³⁶ the action potential occurs thanks to the nonlinear dynamics of the gating variables. The stiffness of these ³⁷ gating variables requires to use of very small time steps in order to simulate them accurately. This limits the ³⁸ use of such models as building blocks of large networks for long simulations. To address this issue we propose ³⁹ to reduce some aspects of the dynamics captured by the biophysical detailed model by using a formalism ⁴⁰ based on an integrate-and-fire type model. The adaptive exponential integrate-and-fire (AdEx) [Brette and ⁴¹ Gerstner, 2005, Naud et al., 2008] model extends the classical integrate-and-fire (IF) model by incorporating

two additional mechanisms: spike threshold adaptation through an exponential term and adaptation with 42 an additional variable. In the AdEx model, the exponential term captures the subthreshold behavior of the 43 neuron's membrane potential. Specifically, the exponential term reflects the voltage-dependent conductance 44 of the neuron's membrane, which is a function of the difference between the neuron's membrane potential and 45 its threshold potential. The adaptation mechanism is modeled by an additional current term that reflects the neuron's ability to adjust its firing threshold in response to the recent history of input. Specifically, 47 this current term represents the activation of voltage-dependent potassium channels that contribute to the 48 membrane's afterhyperpolarization following a spike. The strength and time course of the adaptation current 49 can be adjusted by the model's parameters in order to reproduce a variety of observed neuronal responses. 50 This adaptation variable enters as a current in the membrane voltage equation, which can create unrealistic 51 values of individual membrane potential [Górski et al., 2021], but may not affect qualitatively the global 52 dynamics at network levels [Depannemaecker et al., 2022a]. We thus introduce a third variable, which 53 accounts for the effect of ionic impairment by modulating parameters that are conceptually associated with, 54 or may be affected by ionic changes (e.g. reversal potential, spiking threshold).

Such a model can then become the basis to build large networks [Depannemaecker et al., 2022a], and hence study not only seizure propagation but also the emergence of such pathological patterns at the network level. The article is organized as follows. In Section 2, we present both the single-neuron and the network model that we are going to analyze. Then, in Section 3, we show a correspondence with another model based on the Hodgkin-Huxley formalism and study different possible network configurations leading to the emergence of different patterns associated with epilepsy. We show how the severity of the local impairment or the size of the cell population concerned, leads to different patterns and propagation profiles. Finally, in Section 4, we summarise our findings and propose a few perspectives for future work.

$_{64}$ 2 Methods

⁶⁵ We present here the single-neuron model. Subsequently, we explain how such a model is used for large ⁶⁶ network simulations.

67 2.1 Single-neuron models

⁶⁸ The model builds on the AdEx [Brette and Gerstner, 2005, Naud et al., 2008], whose equations read:

$$C\frac{dV}{dt} = g_L(E_L - V) + g_L \Delta_T \exp\left(\frac{V - V_T}{\Delta_T}\right) - w + I_s$$

$$\tau_w \frac{dw}{dt} = a(V - E_L) - w$$
 (1)

⁶⁹ together with the following after-spike reset mechanism:

if
$$V \ge V_D$$
 then
$$\begin{cases} V \to V_R \\ w \to w + b \end{cases}$$
 (2)

Based on this formalism, we added a third variable z with a slow timescale (with associated time constant ε) compared to the two other variables V and w. This variable z will phenomenologically aggregate the 71 different impairments that may affect the ionic concentration regulation and thus the excitability of the 72 neuronal membrane. Thus, this variable z modulates parameters (E_L, V_T) , which enter into the other 73 variables' equations. The E_L parameter relates to the hyperpolarizing mechanism while the parameter V_T 74 relates to the opening of sodium channels [Brette and Gerstner, 2005]. Hence, V_T may not be affected in 75 the same way as E_L , and it is thus scaled by parameter β . Furthermore, a counteractive term $-g_p z$ models 76 phenomenologically the effects of the aggregate of biophysical mechanisms that are "working against the 77 impairment" (e.g., the Na/K-pump, co-transporters, exchangers, etc...). Parameter g_p is the global equivalent 78

 $_{79}$ conductance resulting from all these mechanisms. Finally, parameter Z_0 corresponds to the potential to which

 $_{80}$ the system will be attracted (depolarized) due to the pathological impairment. Therefore, the extended AdEx

⁸¹ model that will study takes the form:

$$C\frac{dV}{dt} = g_L((E_L + z) - V) + g_L \Delta_T \exp\left(\frac{V - (V_T - 0.5z)}{\Delta_T}\right) - w - g_p z + I_s$$

$$\tau_w \frac{dw}{dt} = a(V - (E_L + z)) - w$$

$$\frac{dz}{dt} = \varepsilon(Z_0 - V - z)$$
(3)

⁸² with still the after-spike reset mechanism:

if
$$V \ge V_D$$
 then
$$\begin{cases} V \to V_R \\ w \to w + b \end{cases}$$
 (4)

83 2.2 Network model

The network we will be studying is made up of inhibitory fast-spiking cells (FS) and excitatory regular spiking cells (RS). It contains 10,000 cells, 80% of which are excitatory and 20% inhibitory, connected through a random and sparse (Erdős-Rényi type) architecture with a probability of 5%. A conductance-based model of synapses enables connections between cells, it typically takes the form of equation (5) below:

$$I_{syn} = g_E(E_E - V) + g_I(E_I - V),$$
(5)

where $E_E = 0$ mV and $E_I = -80$ mV are the reversal potential of excitatory synapses and of inhibitory synapses, respectively. Parameters g_E and g_I are the excitatory and inhibitory conductances, respectively. They are governed by equation (6), and they are increased by a quantity $Q_E = 1.5$ nS and $Q_I = 5$ nS for each excitatory and inhibitory incoming spike, respectively. The timescale of synaptic conductance is determined by $\tau_{syn} = 5$ ms.

$$\frac{dg_{E/I}}{dt} = -\frac{g_{E/I}}{\tau_{syn}} \tag{6}$$

Parameter	Value	Parameter	Value
C_m	200 pF	g_L	10 nS
E_e	0 mV	a	1 nS
$t_{\text{refractory}}$	5 ms	b	60 pA
E_L	-65 mV	V_T	-55 mV
E_i	-80 mV	I_s	0 pA
V_{reset}	-65 mV	$ au_w$	$0.5 \ \mathrm{s}$
ε	$5 \cdot 10^{-4} \text{ s}^{-1}$	Δ_T	2 ms
Z_0	-40 mV	$ au_{ m syn}$	5 ms
q_p	10 nS	V_D	-40 mV

Table 1: Parameters values used (unless specified otherwise).

93 **3** Results

Next, we present our findings in two distinct parts. First, we explore the behavior of our single-neuron model (3) in detail. This part will provide insights into how individual neurons function and react under various conditions, with a particular focus on the role of ionic regulation. In the second part, we delve into the dynamics of a large-scale neural network composed of 10,000 individual neurons. This investigation will help us understand how the characteristics of the extended AdEx model (3), discussed in the first part, influence

⁹⁹ the collective behavior and patterns that emerge within the network. This second part gives some insights

¹⁰⁰ into complex pathological phenomena such as seizure propagation.

¹⁰¹ 3.1 Single neuron model

The single-neuron model exhibits different patterns of spontaneous pathological activities upon an increase 102 of the value of Z_0 , consistent with what is observed in biophysical descriptions [Depannemaecker et al., 103 2022b]. However, the integrate-and-fire type model proposed here captures the after-spike repolarization 104 via a reset mechanism. Thus, this after-threshold reset does not allow for the existence of a fixed point 105 for values corresponding to depolarized membrane potential. Therefore, it is impossible to capture events 106 with depolarization blocks. In this model, spontaneous activity appears for values of $Z_0 > 48$ mV, and an 107 increase of frequency is observed at the onset of a sustained tonic spiking pattern. While increasing Z_0 to 108 values higher than 40 mV, the model exhibits a pathological bursting pattern that can be associated with 109 seizures. Finally, for $Z_0 > 20$ mV the model dynamics corresponds to sustained ictal activity associated with 110 status epilepticus and consisting of a constant high-frequency spiking pattern. After intense spiking activity, 111 the current w reaches very high values leading to a strong negative input in the variable V that may take 112 non-realistic values. This problem has been solved previously [Górski et al., 2021]; however, it may not affect 113 the global network dynamics, specifically in the case of seizures as shown in a previous work [Depannemaecker 114 et al., 2022a]. 115



Figure 1: Spontaneous spiking patterns: (a) tonic spiking for $Z_0 = -45$ mV, (b) pathological bursting pattern for $Z_0 = -40$ mV (c) Sustain ictal activity for $Z_0 = -20$ mV. The three simulations start from the same initial conditions, from which the (V, w) subsystem evolves to the specific pattern, driven by the effect of the slow variable z.

In order to understand the different dynamics observed in system (3), we considered z as being the slowest variable, enabling the loss of stability that leads to spiking activity. We then consider z as a parameter which amounts to taking the limit $\varepsilon = 0$ in system (3) and obtaining its so-called *fast subsystem*— and we investigate the bifurcation structure of the resulting 2D system (with reset). The Jacobian matrix (7) of the fast subsystem is given by:

$$\mathbf{J} = \begin{bmatrix} \frac{g_L}{C} \left(-1 + \exp\left(\frac{V - (V_T - 0.5z)}{\Delta_T}\right) \right) & -\frac{1}{C} \\ \frac{a}{\tau_w} & -\frac{1}{\tau_w} \end{bmatrix}$$
(7)

¹²¹ Hence, the trace of \mathbf{J} takes the form:

$$\operatorname{tr}(\mathbf{J}) = \frac{g_L}{C} \left(-1 + \exp\left(\frac{V - (V_T - 0.5z)}{\Delta_T}\right) \right) - \frac{1}{\tau_w}$$
(8)

122 and its determinant reads:

$$\det(\mathbf{J}) = \frac{1}{C\tau_w} \left(-g_L \left(-1 + \exp\left(\frac{V - (V_T - 0.5z)}{\Delta_T}\right) \right) + a \right)$$
(9)

Thus, based on the trace and determinant, we can study the loss of stability in the V - w subsystem considering z as a parameter. In the figure 2 (a), we show the evolution of the two fixed points of the subsystem V-w (similar to the classical AdEx [Naud et al., 2008,Brette and Gerstner, 2005]). With the evolution



Figure 2: Bifurcations and trajectories: (a) Poincaré diagram of the fixed point of the V-w subsystem, the evolution of the slow variable z is considered as a parameter, the system loose stability crossing an Andronov-Hopf bifurcation (b) Pathological bursting pattern simulation plotted in the variable spaces, the trajectory does not exist in a single plane, the interaction between the three variables leads to this pattern. (c) Phase-space representation of another bursting pattern Γ (in blue), together with the Nullsurface of v(S^0 , in green, folded along the grey curve F), its intersection with the Nullsurface of w (\mathscr{S}^0 , in black), and the reset plane R. The associated parameter values are: $Z_0 = -51.2$, C = 100, $g_L = 10$, $E_L = -65$, $\alpha = 1$, $\beta = 0.5$, a = 1, b = 0.06, $V_D = -40$, $V_R = -54$, $I_s = 0$, $V_T = -55$, $\Delta_T = 2$, $\tau_W = 200$, $g_p = 1$, and $\varepsilon = 0.001$.

of z, the spiking activity appears through a loss of stability by crossing an Andronov-Hopf bifurcation. The 126 two fixed points then rapidly collapse and disappear, leading to the repeated spiking pattern. In the case of 127 the pathological bursting pattern, the oscillation emerges from the interaction between the three variables 128 V, w, and z (see figure 2 (b)). We thus separate two mechanisms leading to healthy or pathological bursts. 129 Indeed, we should mention that the AdEx model is capable of generating bursting activity, as shown in detail 130 in previous work by Naud et al. [Naud et al., 2008]. The original AdEx model requires an external input to 131 spike (or specific parametrization that would lead to permanent steady-state spiking activity). In the model 132 presented here, the spiking patterns appear through the interaction with the slow variable z. 133

To understand the role of the slow variables we can plot the NullSurface into the phase space, and, project one trajectory of a simulation where the system exhibits bursting activity (see Fig. 2 (c)). We thus visualise the structure enabling the emergence of the bursting pattern.

The loop for bursting emerges with a concomitant effect of w and z, as shown by the trajectory in Fig. 2 137 (c), that exists in a surface in the diagonal on the w-z plan. The loss of stability at the onset of the burst 138 occurs through a saddle-node bifurcation at the folding of the v-null surface $(S^0, \text{ in green in Fig. 2 (c)})$. The 139 offset of the burst occurs through a (nonsmooth) homoclinic bursting, where the reset surface (grey) and the 140 v Nullsurface (green) meet. The intersection of the v- and the w-nullsurfaces forms a curve \mathscr{S}_0 traced on S^0 , 141 which the bursting dynamics would follow if z was the only slow process in the model. However, Fig. 2 (c) 142 shows that the bursting pattern rather follows the surface S^0 and much less the curve \mathscr{S}^0 . This indicates 143 that w should also be considered as a slow process. Further analysis would be required to follow up on such 144 considerations, which are an interesting topic for future work. For more elements about slow-fast bursting 145 dynamics in IF models, we refer the reader to [Desroches et al., 2021, Desroches et al., 2024]. 146

¹⁴⁷ 3.2 Network model

In this section, we detail how the severity of local impairment or the size of the affected cell population 148 influences the emergence of distinctive patterns and propagation profiles in the context of epilepsy. To 149 implement this analysis we performed a large parameter exploration, with a focus on the parameter Z_0 , which 150 determines the level of local impairment, and the parameter N_{SC} which defines the number of impaired cells 151 within the system. The results of the analysis are presented in Fig. 3 I. In panels a) to c) we show the 152 maximum firing rates obtained during an 8-second simulation of the network as a function of Z_0 and N_{SC} . 153 In panels d) to f) we show examples of the different dynamics obtained from the network. We see from this 154 figure that the system's behavior can be generally divided into three regions. In the first region (high Z_0 155 and low N_{SC}) the activity of the system remains in an asynchronous irregular (AI) regime with the impaired 156 cells firing at a higher rate compared to healthy excitatory neurons but remaining within physiologically 157 functional values. In the second region (intermediate values of Z_0 and N_{SC}), the firing rates of impaired cells 158 exhibit already pathological dynamics with an oscillatory activity of large amplitude (up to 150Hz). In this 159 second regime, the activity of the inhibitory cells follows the abnormal activity of the impaired cells, with 160 the emergence of high-amplitude oscillations. This response of the inhibitory cells is enough to prevent the 161 propagation of the pathological activity towards the healthy excitatory cells, which remain within normal 162 values of firing rates with only moderate alteration in their dynamics. Finally, in the third region (low Z_0 and 163 high N_{SC}), the pathological activity also propagates to the healthy excitatory population. For the example 164 shown in panel f) of the figure we see that in the third regime, the entire system exhibits an alternation of 165 periods of normal dynamics and periods of global increases in the firing rates. We notice that the pattern 166 of activity observed in the third regime depends on the specific values of Z_0 and N_{SC} and that the network 167 model exhibits a large repertoire of possible patterns and dynamics. For completeness, we show in Fig. 3 II 168 three different patterns obtained from different combinations of parameters. 169



Figure 3: I- Propagation of pathological activity in a network model. a)-c) Maximum firing rates of the impaired cells (a), inhibitory cells (b), and excitatory cells (c) as a function of Z_0 and N_{SC} (defining the severity of local impairment and number of impaired cells respectively. d)-f) Examples of different neuronal dynamics illustrate the effect of an increasing number of impaired cells N_{SC} leading to qualitative changes in the propagation of the pathological activity. For each case, the corresponding raster plot and average firing rate of each cell population is shown (impaired cells in blue, inhibitory cells in red, and excitatory cells in green). The plots correspond to the parameters $Z_0 = -50mV$ and $N_{SC} = 500, 100,$ and 4000 respectively (the corresponding parameters are indicated with green rectangles in panels a,b,c). II- Examples of different activity patterns for the propagation of pathological activity. The network model exhibits a large repertoire of patterns of activity dependent of specific system parameters. We show in the figure the average dynamics obtained for three different sets of parameters: $Z_0 = -10mV$, $N_{SC} = 4000$ (a); $Z_0 = -10mV$, $N_{SC} = 7500$ (b) and $Z_0 = -40mV$, $N_{SC} = 7500$ (c). The color code is the same as in I.

These network dynamics can be related to experimental observation [Wenzel et al., 2019]. Indeed, the propagation of seizure-like activities from one population of impaired cells to the rest of the network, follows a dynamics which resembles previous experimental observation. In Figure 3 we observe a threshold effect, where the propagation to healthy population is comparable to the phenomenon observable shown in Fig. 6 of the work of Wenzel et al. [Wenzel et al., 2019].

175 4 Discussion

Finally, this article has explored the dynamics of single neurons with an additional variable to account for 176 ionic regulation impairment leading to pathological behavior. Experiments have highlighted the critical role 177 of ionic regulation at the single neuron level, particularly in inducing seizure-like behaviors through elevated 178 external ionic potassium concentrations. Biophysical models, although informative, have their limitations 179 due to the Hodgkin-Huxley formalism, which necessitates small time steps and restricts their applicability in 180 large network simulations [Cressman et al., 2009, Depannemaecker et al., 2022b]. To address this challenge, we 181 have proposed an approach that simplifies certain aspects of the biophysical model using the adaptive expo-182 nential integrate-and-fire (AdEx) formalism, which includes subthreshold behavior modeling and adaptation 183 mechanisms. This approach enables to capture different patterns emerging spontaneously from ionic changes. 184 We show how the model captures these dynamics and their impact on neuronal responses. Furthermore, our 185 exploration extends to the study of network configurations and their associations with epilepsy patterns, 186 demonstrating how local impairment severity and cell population size influence patterns and propagation 187 profiles. 188

¹⁸⁹ If it is a simple model for seizure generation, it has some limitations in terms of dynamical repertoire. In-

deed, a pattern associated with sustained depolarization (depolarization block, or permanent depolarization) can not be captured by this model due to the reset mechanism and thus the impossibility of the existence of a stable fixed point for high values (depolarized) of the membrane potential variable. In case of interest in these specific patterns, other models are more appropriate [Depannemaecker et al., 2023]. Such behaviors appear in mean-field approximation [Bandyopadhyay et al., 2021] of biophysically neuron models [Depannemaecker et al., 2022b].

Our approach proposed here is interesting to model large network dynamics and to capture the overall emergent dynamics. This simple model is thus a good candidate for building a mean-field model [Carlu et al., 2020, Alexandersen et al., 2024, Stenroos et al., 2024] capturing epileptic focus dynamics and which can be integrated into large-scale models of pathological brain states.

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