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# 3D fluid-structure simulation of innovative composites for the design and thermal management of electronic devices

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### 15 Abstract

Thermal management of electronic devices remains a challenging issue, especially the cooling 16 17 of electronic components. Current methods mostly involve noisy, cumbersome and underperforming fans. It has recently been shown that phase change materials (PCMs) can 18 perform better and offer more efficient damping of temperature variations in electronic 19 20 components. Here, we present three novel contributions. First, we consider a triply-periodic minimal surface, called a gyroid, as a porous architectured structure containing the PCM. 21 Such a topology mathematically maximizes the exchange surface between the copper 22 structure and the PCM. Heat transfer and thus the performance of such a composite are 23 therefore optimized. Second, we set up a complete 3D coupled fluid-structure model of the 24 composite. This model simulates the heat transfer (conduction and convection) inside both the 25 PCM and the porous structure, as well as the mechanical stresses induced on the container by 26 thermal expansion of the PCM. The 3D coupled theoretical model is based on open-source 27 software codes, OpenFOAM, CalculiX and preCICE. With this novel model, deformation of 28 the structure and mechanical stresses are now predictable. It is therefore possible to anticipate 29 whether a configuration will be prone to leakage due to mechanical failure. Thermal contact 30 resistance is also computed, giving information on heat transfer quality at the interface 31 between the composite and the electronic component. Third, the application of this model to 32 the innovative composite shows that reducing the initial filling level of PCM is a better 33 solution than strengthening the container to maximize thermal management. 34

Keywords: Electronic component; Gyroid; Phase change materials and conductive matrix
 composite; Fluid-structure interaction; Conjugate heat transfer; CFD

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### 44 List of symbols

- $c_p$  Specific heat at constant pressure  $(J. kg^{-1}. K^{-1})$
- d Structure displacement (m)
- D Thermal diffusivity  $(m^2, s)$
- *E* Young's modulus (*Pa*)
- g Gravitational acceleration  $(m. s^{-2})$
- L Characteristic length (m)
- m Mass (kg)
- p Pressure (Pa)
- $R_{th}$  Thermal resistance  $(K.m^2.W^{-1})$
- s Phase change interface position (m)
- T Temperature (K)
- *u* Velocity  $(m. s^{-1})$
- *V* Volume  $(m^3)$

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### 46 Greek symbols

- $\alpha$  Solid fraction
- $\beta$  Coefficient of thermal expansion ( $K^{-1}$ )
- $\delta$  Peak to valley (*m*)
- $\Delta h_f$  Heat of fusion  $(J. kg^{-1})$
- $\varepsilon$  Temperature range where melting occurs (*K*)
- $\boldsymbol{\varepsilon}$  Infinitesimal strain tensor
- $\zeta$  Square root of the liquid thermal diffusivity over the solid one
- $\eta$  Poisson's ratio
- $\kappa$  Penalization parameter (10<sup>20</sup> kg.m<sup>-3</sup>.s<sup>-1</sup>)
- $\lambda$  Thermal conductivity ( $W.m^{-1}.K^{-1}$ )
- $\mu$  Dynamic viscosity (*Pa.s*)
- $\nu$  Cinematic viscosity  $(m^2. s^{-1})$
- $\xi$  Filling level of PCM
- $\rho$  Density (kg. m<sup>-3</sup>)
- $\sigma$  Stress tensor (Pa)
- au Characteristic time (s)
- $\chi_T$  Adiabatic compressibility ( $Pa^{-1}$ )

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### 48 Subscripts

- 0 Reference configuration
- air Air properties
- conv Convection
- diff Diffusion
- 1 Liquid properties
- m Melting
- s Solid properties

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### 50 Acronyms

CFD Computational Fluid Dynamics

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- CHT Conjugate Heat Transfer
- FSI Fluid-Structure Interaction
- OF OpenFOAM
- PCM Phase Change Material
- 51

### 52 **1. Introduction**

Phase change materials (PCMs) are taking an increasingly prominent place in many fields 53 relating to energy management. With current and future energy issues, applications of these 54 55 materials are emerging or improving. Thermal energy storage is of great interest for renewable energies [1]. Solangi et al. [2] have proposed to use MXene PCMs to store solar 56 57 energy. Palomba et al. [3] assessed the performance of a prototype based on PCMs for renewable energy purposes. More broadly, many studies have been conducted on thermal 58 storage using PCMs over the years [4], [5]. PCMs are also widely used in buildings to 59 improve their insulation [6], [7]. The impact of such materials on electricity consumption has 60 been studied by Qureshi et al. [8], among others. 61

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Thermal management with PCMs is also of great interest in electronics [9], [10], with cooling 63 of electronic components being a key issue in this area. Currently, most of these components 64 are used in combination with fin heat exchangers that dissipate heat by natural or forced 65 convection and radiation. The coolers are mainly composed of noisy moving parts such as 66 fans, which have many disadvantages in terms of performance, ergonomics and safety. Sahoo 67 et al [11] have shown that use of PCMs is particularly suitable for cooling electronic 68 components with intermittent operation. These observations have been confirmed by 69 70 numerous studies that have shown these technologies to be useful [12], [13], [14]. PCMs considerably delay the onset of overheating and limit the energy requirements inherent in 71 moving parts [11], [15], [16]. In this regard, Gharbi et al. [17] compared the thermal 72 73 performances of several PCMs, while a cascade configuration of PCMs to cool devices was 74 studied experimentally and numerically by Huang et al. [18]. The cooling performance of 75 carbon nanotubes associated with paraffin was also investigated experimentally [19]. Ho et al. 76 tried to optimize geometries to improve thermal management [20].

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Most studies in this field are experimental because theoretical predictions are made difficult 78 79 by the complexity of the physical phenomena involved. However, experimentation can become expensive and some configurations may be out of reach. Nowadays, thanks to 80 improved computational performance, Computational Fluid Dynamics (CFD) is increasingly 81 helpful as a complement to experimentation. In particular, simulation can predict the physical 82 behavior of thermal management based on PCMs. Many authors manage heat transfer in 83 PCMs considering only conduction, without convection [21], [22]. Other works take 84 convection into account, which modifies the temperature field and thus thermal performance 85 [23], [24]. These numerical studies were carried out with commercial codes. To reduce the 86 cost of simulations, open-source software should be used. There are a few investigations with 87 free codes such as OpenFOAM [25], since the set of governing equations cannot be solved 88 89 directly but must be implemented personally. 2D numerical simulations of PCMs have been conducted with OpenFOAM [26], [27]. 90

91

Although the technology is promising, containers can suffer from leakage due to the high mechanical stresses induced by thermal expansion [28], [29]. Such issues are not theoretically

94 predictable at present, however, and there are no studies focusing on this limiting problem. To

address it, a fully coupled model should set up between a PCM, which is either solid or liquid,

and solid structures containing the PCM. This model should consider conjugate heat transfers 96 (CHT) and fluid-structure interactions (FSI). There are two ways of solving such a complex 97 problem. First, the monolithic approach [30] considers one set of equations involving every 98 physical phenomenon (fluid and solid). This method is numerically stable but very time-99 consuming, and is therefore very scarcely used by authors. Second, the partitioned approach 100 101 [31] considers several sets of equations, which are solved one at a time, often by different software. This method requires an interface coupling between the codes that are used. For 102 configurations involving a fluid and a solid, there is often one code handling the fluid, a 103 second one managing the solid, and a third one coupling them. Numerical stability issues can 104 occur, but this approach is often preferred in the literature since it is less time-consuming. 105

106

Critical temperatures and power losses depend on the electronic components. Based on the 107 requirements specified for the component, a PCM and a conductive porous matrix must be 108 selected. The investigation of a composite and the modeling of its thermal behavior could 109 make it possible to optimize thermal performance by selecting the porous matrix topology that 110 maximizes heat transfers. The objective of this paper is therefore to propose and model the 111 thermal and mechanical behavior of new composite materials (architectured conductive 112 porous matrix containing phase change materials) that meet precise specifications, such as the 113 highest possible energy density, adapted phase change temperatures, limited volume 114 expansion, properties allowing the intensification of transfers, and the lowest possible thermal 115 resistance between the electronic constituents of the composite materials. Some technical and 116 technological obstacles could be overcome thanks to a better fundamental understanding of 117 the phase transition and transfer phenomena involved in these new heterogeneous materials. 118 Development of innovative solutions for the thermal management of electronic components 119 120 therefore necessarily requires particular attention to the material scale.

121

Here, we present coupled simulations of a PCM inside gyroid structures [32]. Gyroids are 122 triply-periodic minimal surfaces, which maximizes the heat exchange surface between PCMs 123 and the surrounding structure. The simulations were managed by a fully open-source software 124 suite composed of OpenFOAM [25], CalculiX [33] and preCICE [34]. For the first time, 125 coupled fluid-solid simulations of PCMs are performed. 3D conjugate heat transfer is 126 considered first between the solid container and melting PCM. Convection of the liquid PCM 127 is taken into account. Then, 3D fluid-structure simulations of the global system are 128 performed. In particular, the fluid pressure caused by thermal expansion and then the induced 129 stresses in the structure are calculated. This global simulation allows us to predict potential 130 failures and leakage, which is a major step forward. In addition, with the simulated solid 131 deformation, contact thermal resistance can be calculated. This theoretical advance allows the 132 assessment of heat transfer losses due to imperfect contact between PCM systems and 133 electronic components, for instance. While most studies focus on the development of new 134 materials increasing heat transfers and exchanges [35], [36], [37], [38], [39], contact thermal 135 resistance plays a significant role in the thermal management of components and is the first 136 obstacle to be overcome for good thermal management. The fluid-structure coupling will thus 137 allow us to design the porous structure correctly to maintain the same contact between the 138 139 component and the innovative composite throughout the different thermal cycles undergone by the component. The present study therefore challenges the following points: 140

- creating a 3D open-source coupled FSI and CHT modeling of PCMs and porous architectured structures
- computing stresses in porous architectured structures induced by thermal expansion of
   PCMs to settle mechanical failures
- computing structure displacements to assess the contact thermal resistance

- applying the modeling to gyroid structures which mathematically maximize the exchange surface
- 148
- assessing the influence of the initial filling level of PCM and the thickness of the gyroid branches on the structure displacements and mechanical stresses
- 149 150

In the paper, we begin by describing the theoretical modeling of both a PCM and a conductive 151 gyroid solid structure in section 2. The CHT and FSI couplings are described more 152 particularly. The PCM model was implemented in OpenFOAM and must thus be validated. 153 Section 3 focuses on the comparison between our PCM model and the analytical solution of 154 the Stefan problem, as well as experimental data from a specific configuration. Section 4 155 156 presents the numerical configuration of the simulations. In particular, a parameter study is performed on the geometry and filling level of the PCM. Section 5 concerns the results of 157 these simulations. Temperatures, velocities, mechanical stresses and structure displacements 158 159 are studied specifically. The last section discusses the most suitable geometry given the simulated mechanical stresses and displacements. 160

161 162

### 163 **2. Numerical methods**

164 The paper focuses on 3D numerical simulation of the fusion of a Newtonian PCM within a 165 porous architectured structure. First, we present the equations governing the PCM, then those 166 describing the thermo-mechanical behavior of the structure, and finally the interface coupling 167 between both solvers.

168

### 169 **2.1 PCM modeling**

#### 170 *2.1.1 Equations*

After melting, the liquid PCM is Newtonian and the incompressible Navier-Stokes equations (1) thus govern its behavior reliably. The variation in density with temperature is considered by the Boussinesq approximation. The influence of this assumption will be addressed in section 3.2. To avoid any velocity in the remaining solid material, a penalization term is added into the momentum equation. The energy equation is based on the equivalent enthalpy approach, where the melting process is considered through an additional source term.

177

$$\begin{cases} \nabla \cdot \boldsymbol{u} = 0 \\ \frac{\partial \boldsymbol{u}}{\partial t} + \boldsymbol{u} \cdot \nabla \boldsymbol{u} = -\frac{\nabla p}{\rho_0} + (1 - \beta (T - T_0))\boldsymbol{g} + \nu \Delta \boldsymbol{u} - \frac{\kappa \alpha}{\rho_0} \boldsymbol{u} \\ (\rho c_p)_{eq} \left(\frac{\partial T}{\partial t} + \boldsymbol{u} \cdot \nabla T\right) = \nabla \cdot (\lambda_{eq} \nabla T) - \rho_s \Delta h_f \frac{d\alpha}{dt} \end{cases}$$
(1)

178

In equations (1),  $\boldsymbol{u}$  is the velocity (m.s<sup>-1</sup>), p is the pressure (Pa), T is the temperature (K),  $T_0$  is 179 a reference temperature (K),  $\rho_0$  is the density at the reference temperature (kg.m<sup>-3</sup>),  $\beta$  is the 180 coefficient of thermal expansion (K<sup>-1</sup>), g is the gravitational acceleration (m.s<sup>-2</sup>), v is the 181 kinematic viscosity (m<sup>2</sup>.s<sup>-1</sup>),  $\alpha$  is the solid fraction,  $\kappa$  is a huge penalization parameter 182  $(10^{20} kg.m^{-3}.s^{-1})$  aiming to avoid velocity in the solid domain,  $\rho$  is the density which 183 depends on temperature (kg.m<sup>-3</sup>),  $c_p$  is the specific heat capacity (J.kg<sup>-1</sup>.K<sup>-1</sup>),  $\lambda$  is the thermal 184 conductivity (W.m<sup>-1</sup>.K<sup>-1</sup>),  $\rho_s$  is the solid density at melting temperature (kg.m<sup>-3</sup>) and  $\Delta h_f$  is 185 the heat of fusion  $(J.kg^{-1})$ . The index *eq* in the energy equation refers to equivalent properties 186 187 giving

$$\left(\rho c_p\right)_{eq} = (1-\alpha)\rho_l c_{p,l} + \alpha \rho_s c_{p,s} \tag{2}$$

$$\lambda_{eq} = (1 - \alpha)\lambda_l + \alpha\lambda_s \tag{3}$$

188 where the l and s indices refer to liquid and solid respectively.

189 Due to the temporal derivative of the solid fraction in the energy equation, a C<sup>1</sup> function is 190 required for  $\alpha$  and must be equal to 0 for temperatures greater than the melting temperature, 191 and equal to 1 for lower temperatures, with as sharp a transition as possible around the 192 melting temperature. Equation (4) presents the chosen function, already used in other models 193 [40], [41]:

194

$$\alpha = \frac{1}{2} \left( \tanh\left(\frac{T_m - T}{\varepsilon}\right) + 1 \right) \tag{4}$$

195

where  $T_m$  is the melting temperature of the solid PCM (K) and  $\varepsilon$  (K) a small parameter controlling the sharpness of the transition. Here we chose  $\varepsilon = 10^{-2}K$ , which is a common choice to avoid numerical issues while maintaining a sharp transition [40], [41]. The derivative of the solid fraction in the energy equation becomes:

200

$$\frac{d\alpha}{dt} = -\frac{1}{2\varepsilon} \left( 1 - \tanh^2 \left( \frac{T_m - T}{\varepsilon} \right) \right) \frac{dT}{dt}$$
(5)

201

To be efficient, the penalization term to avoid velocity inside solid parts must be treated implicitly in the linear resolution, in order to get a huge value on the diagonal of the matrix and thus avoid velocity. The sign of this term also has an impact on numerical stability. In order for the matrix to be strictly diagonally dominant, it is better to add a positive penalization term to the matrix diagonal.

207

Turbulence is not considered in the resolution. The greatest velocities encountered are about 1 cm.s<sup>-1</sup> (section 5) while the structure is also of the order of 1 cm. This leads to a Reynolds number approximately equal to  $Re = \frac{uL}{v} \sim \frac{10^{-2} \times 10^{-2}}{10^{-6}} \sim 100$ , which allows us to assume laminar flows.

- 212
- 213 2.1.2 Numerical schemes

214 The PCM equations are solved with OpenFOAM where they have been implemented. The discretization of the equations is based on the finite volume method. Resolution of the 215 velocity-pressure coupling relies on the classical PISO (Pressure Implicit with Splitting of 216 217 Operator) algorithm. The temporal term is discretized with a blend between the Euler and Crank-Nicolson schemes. In the simulations, the weight associated with the Crank-Nicolson 218 scheme is 0.9, which ensures an almost second-order time discretization with enough 219 numerical diffusion to avoid divergence. The advection term in the momentum equation (1) is 220 discretized with the second-order upwind scheme. In the energy equation, the advection term 221 is discretized with a TVD (Total Variation Diminishing) scheme switching between first 222 (upwind) to second order (centered) depending on the velocity gradient. The central 223 difference discretization is applied to the diffusion term. The mesh discretization and the 224 boundary conditions are discussed in section 4. 225

226

#### 227 2.2 Porous architectured structure modeling

228 The structure is governed by the linear elastic thermo-mechanical equations (6). The first

- equation computes heat conduction while the second describes mechanics.
- 230

$$\begin{cases} \frac{\partial T}{\partial t} = D_s \Delta T \\ \rho_s \frac{\partial^2 d}{\partial t^2} = \nabla \cdot \boldsymbol{\sigma} \end{cases}$$
(6)

 $D_s = \frac{\lambda_s}{\rho_s c_{p,s}}$  is the thermal diffusivity of the solid, which is assumed to remain constant, **d** is 232 the structure displacement and  $\sigma$  is the stress tensor based on Hooke's law and an additional 233 thermal term  $\boldsymbol{\sigma} = \frac{E}{1+\eta} \boldsymbol{\varepsilon} + \frac{E\eta}{(1+\eta)(1-2\eta)} tr(\boldsymbol{\varepsilon}) \boldsymbol{I} - \frac{E\beta}{1-2\eta} (T-T_0) \boldsymbol{I}$ . *E* is Young's modulus of the 234 structure,  $\eta$  is Poisson's ratio,  $\boldsymbol{I}$  is the second rank unity tensor and  $\boldsymbol{\varepsilon} = \frac{1}{2} (\boldsymbol{\nabla}^T \boldsymbol{d} + \boldsymbol{\nabla} \boldsymbol{d}).$ 235 236

These equations were solved with CalculiX, which is based on the finite element method. The 237 temporal terms are discretized with the second-order backward Euler scheme. Section 4 238 presents a mesh convergence on the structure. 239

#### 2.3 Coupling 241

2.3.1 Physical considerations 242

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240

In order to optimize the calculation time, we first conduct a dimensional analysis to predict 244 which phenomena can be neglected in the simulations. Section 4 presents the properties of the 245 materials involved in the simulations in section 5. We use these properties in the following 246 preliminary calculations. The results presented in section 5 show that the velocity is about 1 247 248

presented in section 5 show that the velocity is about 1 cm.s<sup>-1</sup>. The convection time is  $\tau_{conv} = \frac{L}{u} \sim \frac{10^{-2}}{10^{-2}} \sim 1 s$ , the thermal diffusion characteristic time is  $\tau_{diff,s} = \frac{L^2}{D} \sim \frac{10^{-4}}{10^{-4}} \sim 1 s$  in the porous architectured structure and  $\tau_{diff,s} = \frac{L^2 \rho c_p}{\lambda} \sim \frac{10^{-4} \times 10^3 \times 10^3}{10^{-1}} \sim 10^3 s$  in the PCM, and the mechanical characteristic time is  $\tau_{mech} = \frac{L}{\sqrt{\frac{E}{D}}} \sim \frac{10^{-2}}{\sqrt{10^{11} \times 10^{-3}}} \sim 10^{-6} s$ . The deformation velocity of the porous architectured structure is 249

250

251

thus far higher than the other phenomena velocities in the problem. Then, we can consider 252 quasi-static calculations for the mechanical equations. 253

254

Now, let us estimate the impact of mechanical deformations on liquid convection. The 255 calculated liquid pressures in the simulations discussed in section 5 are of the order of 100 Pa. 256 The ratio of the dynamic pressure over the pressure is  $\Pi = \frac{\frac{1}{2}\rho u^2}{n} \sim \frac{10^3 \times 10^{-4}}{10^2} \sim 10^{-3}$ . The 257 pressure variations are thus weakly related with the velocity field, and rather linked with 258 density variations due to the increase in temperature. The simulated structure displacements in 259 section 5 are smaller than  $10^{-4}$  m. This weak value can globally impact neither heat transfer 260 nor convection in the melted PCM. 261

262

Therefore, the impact of solid deformations is negligible on the PCM melting process. The 263 calculations can thus be divided into two simulations and the mechanical and thermal 264 equations can be uncoupled. First, a transient Conjugate Heat Transfer (CHT) simulation is 265 carried out, without solving the mechanical equations. Second, steady Fluid-Structure 266 Interaction (FSI) simulations are performed. 267

- 268
- 269 2.3.2 Conjugate heat transfer coupling

In the CHT coupling, mesh deformation is neglected. This allows us to perform the simulation in an explicit way, whereas considering mesh motion would have required implicit coupling with several sub-iterations. The boundary conditions at the interface for both software codes (OpenFOAM and CalculiX) are based on a Robin-Robin coupling. This means that the temperatures and heat fluxes at the interface are exchanged between the PCM and the structure. Then, a Robin boundary condition is applied to the interface in both codes. This part of the process was handled with preCICE.

277

#### 278 2.3.3 Fluid-structure interaction coupling

The volume of the solid PCM is smaller than that of the liquid PCM after melting. In addition, 279 as temperature increases, the liquid PCM expands. If the container volume is smaller than the 280 liquid volume, then pressure can surge. The paper aims to compute the mechanical impact of 281 the thermal expansion of the PCM on the surrounding porous architectured structure. 282 However, the impact of the expansion of the volume of the liquid on pressure is not calculated 283 in the model described in the prior sections since an incompressible fluid has been considered. 284 285 Density is therefore assumed to be independent of pressure, but does depend on the temperature thanks to the Boussinesq approximation. This assumption is sufficient for the 286 previous CHT simulation, but not for the FSI one. The compressibility of the melted PCM 287 288 must be considered to estimate the pressure variation induced by the fluid thermal expansion. Solving the compressible Navier-Stokes equations requires an equation of state and there is no 289 such a relation in the literature. 290

291

We will thus not be able to compute the liquid pressure during the melting process. However, 292 we are interested in the maximum mechanical stresses in the porous architectured structure. 293 294 This happens at the end of the simulation, when all the PCM has melted and involves the maximum liquid expansion. When the porous architectured structure is only filled with a 295 liquid at a similar temperature thanks to convection, the pressure can be assumed 296 homogeneous. As noticed previously, the pressure gradients induced by the liquid velocity are 297 indeed very weak, and the temperature heterogeneities in the liquid PCM are very low at the 298 end of the melting process. 299

300

The liquid pressure can then be calculated with the following analytical approach. Let us note  $\chi_T = -\frac{1}{v} \frac{\partial V}{\partial p} \Big|_T$  the adiabatic compressibility (*Pa*<sup>-1</sup>). Under the assumption that this property remains constant during compression,

304

$$p - p_0 = \frac{1}{\chi_T} \ln \frac{V_0}{V} \tag{7}$$

305

where  $V_0$  is the volume of the liquid phase under pressure  $p_0$ . With  $p_0 = 0 Pa$ ,  $V_0$  would be the volume of the melted PCM without constraint. We assume that the encapsulating structure is initially partially filled with the PCM at the melting temperature such that  $m = \xi_0 \rho_l(T_m) V_p$ where  $V_p$  is the volume of the encapsulating structure,  $\rho_l(T_m)$  is the liquid PCM density at the melting temperature and  $\xi_0$  is the initial filling level of liquid PCM. Due to thermal expansion, the volume at temperature *T* becomes  $V' = \frac{m}{\rho_l(T)} = \xi_0 \frac{\rho_l(T_m)}{\rho_l(T)} V_p$ . This corresponds to the volume of the melted PCM without compression. So  $V' = V_0$ . The pressure is therefore given by

314

$$p = \frac{1}{\chi_T} \ln \xi \frac{\rho_l(T_m) V_p}{\rho_l(T) V}$$
(8)

The pressure on the structure walls will expand the initial liquid volume, while the stresses induced in the elastic porous architectured structure will tend to avoid such a displacement. To calculate the mechanical balance between pressure and solid stresses, an implicit FSI coupling is necessary.

320

A static simulation based on the temperatures at the final CHT time step is considered. The 321 322 pressure in the liquid is first calculated with equation 8 based on OpenFOAM. The forces undergone by the solid are exchanged and a mechanical computation is performed by 323 CalculiX. Note that the thermal expansion of the solid structure is also considered in the 324 325 simulation. The displacement of the solid PCM structure interface is sent to OpenFOAM, which first deforms the mesh and then computes the new pressure value based on the new 326 liquid volume. The process iterates until convergence. This procedure is summarized in Fig. 327 328 1.

329



Fig. 1. Resolution procedure of the fluid-structure interaction simulation. The interface corresponds to the surface between the PCM and the porous architecture structure. Blue refers
to OpenFOAM, ochre to CalculiX and green to preCICE.

334

The implicit coupling is based on the IQN-ILS method (Quasi-Newton Inverse Least Squares)to accelerate the convergence [42].

- 337
- 338

## **339 3. Validation of the PCM model**

The theoretical model described in section 2.1 was implemented in version 7 of OpenFOAM.
Here, we present two test cases to validate this implementation, both analytically and
experimentally.

343

### 344 **3.1 Stefan problem**

We first compare the model with the analytical solution of the Stefan problem. This consists in a semi-infinite one-dimensional geometry, which is initially considered as solid at temperature  $T_0$ . On the left boundary, a Dirichlet temperature boundary condition  $T_d$  is enforced in order to melt the material. When x tends to infinity, the temperature is supposed to be equal to the initial temperature  $T_0$ . Fig. 2 displays this configuration.



Fig. 2. Stefan problem corresponding to a 1D semi-infinite material initially solid at the temperature  $T_0$ . The left side is then heated, which makes the material melt.

The phase change interface position s and the temperature field T are known analytically according to the two following relations [43]:

356

$$T(x,t) = \begin{cases} T_d + (T_m - T_d) \frac{\operatorname{erf}\left(\frac{x}{2\sqrt{D_l t}}\right)}{\operatorname{erf}(\psi)} & \text{if } x < s(t) \end{cases}$$
(9)

$$\left(T_0 + (T_m - T_0) \frac{\operatorname{erfc}\left(\frac{x}{2\sqrt{D_s t}}\right)}{\operatorname{erfc}(\psi\zeta)} \text{ otherwise} \right)$$
(10)

$$s(t) = 2\psi\sqrt{D_l t} \tag{11}$$

357 where  $\zeta = \sqrt{D_l/D_s}$  and  $\psi$  is the solution of the transcendental equation

$$\frac{\lambda_s}{\lambda_l}\zeta(T_m - T_0)\frac{e^{-\psi^2\zeta^2}}{\operatorname{erfc}(\psi\zeta)} + (T_m - T_d)\frac{e^{-\psi^2}}{\operatorname{erf}(\psi)} + \psi\Delta h_f\sqrt{\pi}\rho_s\frac{D_l}{\lambda_l} = 0$$
(12)

Let us consider the following properties and parameters of water:  $\rho_l = 1000 \ kg.m^{-3}$ ,  $\rho_s = 920 \ kg.m^{-3}$ ,  $\lambda_l = 0.5 \ W.m^{-1}.K^{-1}$ ,  $\lambda_s = 1.3 \ W.m^{-1}.K^{-1}$ ,  $c_{p,l} = 4.2 \ kJ.kg^{-1}.K^{-1}$ ,  $c_{p,s} = 2 \ kJ.kg^{-1}.K^{-1}$ ,  $\Delta h_f = 333.4 \ kJ.kg^{-1}$ ,  $T_m = 0^\circ C$ ,  $T_0 = -5^\circ C$  and  $T_d = 5^\circ C$ .

Fig. 3.a displays the phase change interface position against time, while Fig. 3.b shows the relative error with the analytical solution. The analytical solution is compared with the results from the corresponding simulation with OpenFOAM. In the figure, dx refers to the spatial step and dt to the temporal step in the simulation. The two most refined simulations lead to similar accurate results.



**Fig. 3.** a) Comparison of the phase change interface position displacement calculated analytically and with three OpenFOAM simulations. b) Relative error of the phase change interface position.

Fig. 4 presents the temperature field one hour after the start of heating. The theoretical interface position is also presented. The OpenFOAM (OF) solution corresponds to the intermediate refinement level in Fig. 3. The simulated temperature is almost equal to the analytical solution, all along the 1D geometry. The energy equation in the set of equations (1) thus gives consistent results.

376





**Fig. 4.** Comparison of the analytical and the simulated temperature field, after one hour.

379

#### 380 **3.2 2D validation with experimental and numerical results**

This section concerns the validation of the model, which can be 3D, based on the 2D numerical results presented in [26], which have been successfully compared with the corresponding experiment carried out by the same authors [44]. The test case consists in melting a PCM within a square which is heated on the left side at 308.15 *K* and maintained at 298.15 *K*, the initial temperature, on the right side. The bottom and top edges are considered to be adiabatic in the simulation discussed in [26], whereas they actually result from conduction in thin plates in the experiment. In our simulation, adiabatic walls are considered. The same PCM properties given in [26] are considered in the present simulation. Note that there is a small opening at the upper left corner in the experimentation to drain the excess amount of fluid resulting from the volume expansion during melting. Fig. 5 compares the phase change interface at different times from our simulation with the simulation and the experimentation achieved by Faden et al. [26] The mesh is composed of 40,000 cells; the same mesh is used in the reference simulation.



394

**Fig. 5.** Phase change interface 1, 2, 3 and 4 hours after the start of heating. The dot points and the crosses stem from [26].

Fig. 6 also displays the velocity field in the physical domain after four hours. The same figure is proposed in [26] and is very similar. It is worth noting that our results are close to the numerical simulation managed by Faden et al. [26], and they are also consistent with the experimental results [26], [44].



402

**Fig. 6.** Velocity magnitude in the geometry four hours after the start of heating. The OF simulation is based on a mesh composed of 40,000 cells. The left side is heated to 10 K warmer than the initial temperature.

406

407 The reference simulation is based on the compressible Navier-Stokes equations, while ours is 408 based on the Boussinesq approximation. The prior results clearly show that the Boussinesq 409 approximation is reliable for this range of temperature variation and is satisfactory in 410 comparison with compressible equations, which are more time-consuming to solve.

411

### 412 **4. Numerical setup**

#### 413 **4.1 Configuration**

The geometry of the encapsulating structure is based on triply-periodic minimal surfaces, which optimize the heat transfer exchange surface [32]. Here, we consider a gyroid surface, given by the implicit equation  $\cos(x)\sin(y) + \cos(y)\sin(z) + \cos(z)\sin(x) = 0.15$ . Giving a thickness to this surface leads to the geometry in Fig. 7. This geometry contains two isolated volumes.





422 box side length.

423 Based on this idea, we propose to build a porous architectured structure containing a volume

like in Fig. 7 enclosed by a cube with the same thickness as the thick faces of the gyroidbranches. This geometry is then filled with PCM. Fig. 8 displays the general geometry that is

investigated in the remaining part of the paper. The side length of the surrounding box is

- 427 equal to 5 cm.
- 428



429

Fig. 8. Geometry investigated in the paper. The blue parts and the surrounding box are solid,while the remaining part is liquid.

The porous architectured structure will be made of copper, while the PCM will be palmitic acid. The melting temperature of palmitic acid is slightly below the usual critical temperature of electronic components. Copper allows a fast thermal conduction process which makes heat transfer efficient. Tab. 1 itemizes the considered properties for both materials. The palmitic acid properties mainly stem from [45], except for thermal conductivities [46]. The gravitational acceleration is assumed to be equal to  $g = 9.81 \text{ m. s}^{-2}$  in the simulations.

438

Properties	Solid palmitic acid	Liquid palmitic acid	Copper
$T_m(K)$	335.35	-	-
$\Delta h_f (kj.kg^{-1})$	211.85	-	-
$\rho (kg.m^{-3})$	989.6	-0.7349(T - 273.15) + 907.54	8950
$c_p (J. g^{-1}. K^{-1})$	Fig. 3 [45]	2.39	380
$\lambda (W.m^{-1}.K^{-1})$	0.22	0.16	401
μ (Pa.s)	-	$4.381 \times 10^{-6} e^{2488.8/T}$	
$\beta(K^{-1})$	-	0.11	$1.7 \times 10^{-6}$
E (GPa)	-	-	130
n	-	-	0.33

Tab. 1. Properties of the materials involved in the simulations. The blank cells are not considered or have no physical meaning.

441

In sections 5 & 6, several thicknesses for the gyroid volume will be tested to compare the mechanical stresses. The thicknesses will vary from 2 to 10% of the box side length. The filling level of the structure  $\xi_0$  will also vary between 98.5% and 100%. Below these values, we can check that the thermal expansion of the liquid does not involve compression under 85°C (equation 8), which will not be exceeded in this paper. Higher temperatures damage electronic components, so there is no interest in exceeding this temperature.

In section 5, the bottom face of the box will be heated with a constant power equal to 30 W which is a common power experienced by electronic components. Even if this power involves temperatures greater than 85°C, the simulations will be stopped at this temperature. The other external faces of the box will undergo a convective heat transfer with a coefficient h = $5 W. m^{-2}. K^{-1}$  and an outside temperature of 22°C (which is also the initial temperature). The faces will be free to move.

A few studies focus mainly on the measurement of the adiabatic compressibility of palmitic acid. Due to uncertainties on its value, two FSI simulations will be performed for each configuration. They will rely on  $\chi_T = 4 \times 10^{-10} P a^{-1}$  and  $\chi_T = 10^{-9} P a^{-1}$  [47], [48], [49], [50].

### 458

#### 459 **4.2 Mesh convergence**

#### 460 *4.2.1 Porous architectured structure*

Mesh convergence is achieved on the solid part of the geometry (Fig. 8). Only for mesh 461 convergence, the bottom face is fixed and heated to 90°C. The same boundary conditions as 462 in section 4.1 are considered elsewhere. The properties of the copper are summed up in Tab.1. 463 The static results relying on six meshes are compared in Fig. 9. The meshes consist of 185, 464 465 320 and 580 thousand first or second order elements respectively. The element sizes are respectively equal to 1 mm, 0.8 mm and 0.65 mm. The comparison is made along a 466 curvilinear line in red located in the middle plane in green in Fig. 9.a. The displacement, von 467 Mises stress and temperature along this curve are presented in Fig. 9. There is almost no 468 difference on the displacement (Fig. 9.b). The von Mises stress also varies weakly with the 469 meshes (Fig. 9.c). The greatest deviations appear close to the bottom face, where the stress is 470 471 most significant. The simulated temperatures are grouped according to the number of elements rather than the order of the elements (Fig. 9.d). The order does influence the results 472

473 considerably for the three variables. The number of elements also has a weak impact. Since it
474 does not lead to a prohibitive calculation time, we have chosen the second mesh with 320,000
475 order 1 elements rather than the coarsest one, where there are only 2 tetrahedra in the
476 thickness of the surrounding box, which decreases the stress values close to the bottom face.
477



**Fig. 9.** a) Comparison of the results from six different meshes along the red curve in the green plane. The origin of the curve is on the bottom face (red point). b) Evolution of the structure displacement along the red curve. c) Evolution of the von Mises stress along the red curve. d) Change in the temperature along the red curve (1 k = 1000).

#### 483 *4.2.2 PCM*

478

484 Here, only the volume associated with the PCM is studied. The material properties in the simulations are gathered in Tab. 1. Like in section 4.2.1, the bottom face is heated to 90°C 485 while zero Neumann boundary conditions are imposed on the other faces. The PCM is 486 initially solid at 22°C. The phase change interface position is plotted along the red line in 487 Fig. 10.a. It should be noted that it was not possible to choose a planar curve considering the 488 winding PCM geometry. Three meshes were compared with 40 thousand, 800 thousand and 489 6.8 million cells, corresponding to cell sizes of 1 mm, 0.5 mm and 0.25 mm respectively. 490 There are expected differences in the temperature field during the melting process, 33 minutes 491 after the start of heating (Fig. 10.b). Except at this moment, the gaps remain small. 492 Concerning the change phase interface position, the deviations increase with time (Fig. 10.c). 493 They are linked with the observation of the temperature around the delay on the melting 494 process. Since the computation time of the finest mesh is very long (4 days with 192 495 processors), we consider that the accuracy given by this mesh is not sufficient. In addition, 496 coupled CHT-FSI simulations will be explored, which increases calculation time even more. 497 We thus chose the medium mesh. 498



Fig. 10. a) PCM geometry. The phase change interface position is plotted along the red line
inside the geometry. The origin of the curve is on the bottom face (red point). b) Temperature
according to time at point (0.02, 0.005, 0.02). This point was chosen close to the bottom face,
where the heating process begins early. c) Phase change interface position according to time.

505

### 506 5. Results

#### 507 5.1 Conjugate Heat Transfer simulations

This section focuses on the thermal coupling exclusively, i.e., on the heat transfer and the 508 melting process of the palmitic acid in the porous architectured conductive structure. Five 509 simulations with different gyroid thicknesses (from 2 to 10% of the box side length) are 510 performed. The general behavior of the coupled phenomena is described in specific 511 configurations. Fig. 11 displays the temperature in the middle cross-section of the gyroid box 512 (8% thickness), 17 minutes after the start of heating. The copper temperature, between 76 and 513 78°C, is far greater than that of the PCM. This stems from the thermal conductivity of copper 514 which is 2,000 times higher than for the PCM (Tab. 1). Therefore, even if only the bottom 515 face is heated, the PCM is actually heated mainly by the whole interface with the copper 516 gyroid. Since the PCM melts at 62.2°C, a significant part of the palmitic acid is still solid as it 517 is quite far from edges. 518



Fig. 11. Temperature field both in the PCM and copper, 17 minutes after the start of heating,
in the middle cross-section of the porous architectured structure. The configuration
corresponds to a gyroid thickness of 8%. The white contour corresponds to the limit between
PCM (OpenFOAM) and copper (CalculiX). a) The temperature scale is adapted to the PCM
temperature. b) The temperature scale is adapted to the solid temperature.

The convection process thus begins only from approximately 15 minutes after the start of 526 heating, when the PCM close to the solid interface is melted. Fig. 12 shows local velocity 527 vectors within the liquid PCM at the same time as in Fig. 11. Due to temperature gradients, 528 529 the hot liquid moves upward, following the winding structure geometry. The top part of the PCM therefore melts faster than the bottom, despite the fact it is the bottom face that is 530 heated. This process is also observed in Fig. 11.a, in the top left and right corners of the PCM. 531 The upper parts of these areas melt while the lower parts are still solid. The velocities remain 532 smaller than 4 mm.  $s^{-1}$  at this time but can exceed 1 cm.  $s^{-1}$  during the simulation. 533



Fig. 12. Velocity vectors in a melting area of the PCM, 17 minutes after the start of heatingthe structure composed of an 8% thickness gyroid.

Fig. 13 shows the change in the solid PCM inside the gyroid structure composed of 6% thick 537 branches. Following the previous results, a melting process starting from the PCM-copper 538 interface towards the center of the PCM is expected. This behavior is observed in Fig. 13. 539 After 10 minutes (Fig. 13.a), only the PCM close to the edges begins to melt, as in Fig. 10. 540 Note that the temperature in the liquid PCM exceeds 65°C. Seven minutes later (Fig. 13.b), 541 the upper part of the PCM is hotter than the lower part, due to convection. The volume of the 542 solid PCM has decreased drastically. Three minutes later (Fig. 13.c), the solid PCM is 543 shrinking sharply, while the temperature varies weakly in comparison with Fig. 13.b. Only the 544 central part of the PCM remains solid after 20 minutes. Finally, after 23 minutes, only a small 545 546 part of the PCM is still in the solid state. The temperature will then increase faster without PCM to melt. A few seconds later, the solid PCM disappears. 547



Fig. 13. OpenFOAM temperature field and solid PCM (in black) in a copper gyroid structure
consisting of 6% thick branches. a) 10 minutes; b) 17 minutes; c) 20 minutes; d) 23 minutes;
after the start of heating.

Fig. 14.a shows the average temperature in the whole PCM according to time, for the five 552 thickness configurations. Before most of the PCM has melted, the lower the thickness, the 553 higher the temperature. During this conduction time, the energy is transferred through the 554 interface. The lower the thicknesses, the greater the exchange interface area. Therefore, there 555 is more conductive heat transfer for copper gyroid structures with thin branches. In addition, 556 for thick gyroid structures, the bounding box is also thicker, so energy coming from the 557 bottom face must diffuse in a thicker copper volume before reaching the PCM. Energy thus 558 559 attains the PCM faster in thin gyroid structures. Very quickly, however, after several hundreds of seconds (Fig. 14.b), the heating rate becomes lower for thin gyroid structures. Since there is 560

more PCM, the melting process plays a more significant role than in thicker configurations. 561 The heating rate thus reduces substantially down to a quasi-constant heating rate of around 562 1°C.min<sup>-1</sup>. This second phase (melting phase) occurs earlier for thin copper gyroid structures 563 since there is more PCM. Due to the quantity, the melting phase is also longer in thin 564 configurations. Fig. 14.a shows greater damping of temperature variation inside thin copper 565 gyroid structures, thanks to the PCM. Finally, a third phase happens, when the PCM is mostly 566 or totally liquid. The heating rate increases again (Fig. 14.b). Since this last phase begins later 567 for the 2% thick gyroid, the temperature is lower than in the other simulations. At the end, the 568 thinner it is, the colder the temperature. 569



570

Fig. 14. a) Average temperature in the PCM according to time for the five thickness cases. b)
Heating rate (time derivative of temperature) in the PCM according to time.

#### 573 **5.2 Fluid-structure interaction simulations**

As described in section 2, we consider a fluid-structure simulation at the end of the melting process of the PCM, when the temperature is almost homogeneous. In the simulation, the final temperature field in the porous architectured structure is considered while the liquid temperature is assumed to be equal to 85°C. The liquid temperature is indirectly involved in equation (8) through the density, and thus has a significant impact on thermal volume expansion. The copper temperature is also involved in the thermal dilatation and generates mechanical stresses in the structure.

The deformation of the porous architectured structure (4% thick), completely filled with PCM ( $\xi_0 = 100\%$ ), is presented in Fig. 15 with a scale factor of 30. Fig. 15.b compares a section before and after deformation. The greatest displacements occur at the box sides due to the pressure gradients. The pressure is indeed significant inside the box while the atmospheric pressure is negligible outside. Instead, the pressure is constrained inside gyroid branches on both sides. Note that the side displacement remains relatively small (240 µm). Displacement (mm) 0 0.05 0.1 0.15 0.24



587

**Fig. 15.** Displacement field of the 4% thick gyroid structure initially fully filled with the PCM  $(\xi_0 = 100\%)$ , from CalculiX. The deformations presented here correspond to the genuine deformation multiplied by 30. a) Displacement of the 3D copper gyroid structure. b) Comparison of the deformed structure with the initial geometry in the central section of the 592 copper gyroid structure.

Fig. 16 displays the von Mises stresses inside the porous architectured structure for the same 593 configuration. The greatest stresses do not occur at the box sides but in the thick branches, 594 especially close to the junctures. These parts undergo compressive forces due to the pressure. 595 The stresses reach as much as 570 MPa at several locations. The value of the compressive 596 yield strength of copper can vary according to the material properties. In the paper, we assume 597 598 that its value is 138 MPa [51]. Based on the von Mises criterion, this configuration thus widely exceeds safe stresses and should lead at least to plastic deformations and perhaps 599 failures. 600



**Fig. 16.** The von Mises stresses from CalculiX in the 4% thick gyroid structure initially fully filled with the melted PCM ( $\xi_0 = 100\%$ ).

604

#### 605 **6. Discussion**

#### 606 6.1 Stresses involved in the encapsulating solid

The model presented allows us to compute the stresses generated by the thermal expansion of 607 the PCM in the encapsulating structure. Based on these results, it is possible to predict 608 whether a configuration is reliable or not from this point of view. In the paper, we focus on 609 the yield stress and not on failure. Since such a product must undergo several cycles, plastic 610 deformation should not occur for safe and efficient use. Like in the prior section, we follow 611 the von Mises criterion. Fig. 17 displays the maximal von Mises stress in copper for each 612 configuration that was tested. We recall that simulations with different filling levels and 613 thicknesses of gyroid branches were carried out. For each configuration, a range is provided 614 for the maximal von Mises stress, corresponding to the FSI simulations with two values of 615 adiabatic compressibility  $\chi_T = 4 \times 10^{-10} P a^{-1}$  and  $\chi_T = 10^{-9} P a^{-1}$  (§4.1). With a branch 616 thickness of only 2% of the box size length, the stresses are very high and exceed the yield 617 stress for every filling level greater than 99%. With less PCM in the host architecture matrix, 618 its volume expansion does not involve sufficient stresses to deform the copper plastically. 619 This is an important issue since this geometry is the hollowest one, so filled with the greatest 620 amount of PCM. With a thickness of 4% to 8%, the stresses decrease, as expected, but to a 621 level which is not sufficient to change the previous conclusions on 2% thick gyroids. Indeed, 622 from a filling level of 99%, a risk of plastic deformation still exists. With a thickness of 10%, 623 the solid structure can undergo high pressures with von Mises stresses remaining smaller than 624 the yield stress. With this thickness, only a completely filled structure could be deformed 625 626 plastically. However, such a geometry contains a smaller amount of PCM than for a gyroid composed of 2% thick branches. Considering the maximum filling level of each geometry 627 without jeopardizing the structure, the 2% thick geometry remains the structure that can be 628 629 filled with the greatest amount of PCM. With a filling level of 98.5%, this geometry can 630 contain  $113 \ cm^3$  of PCM while remaining safe according to the simulations. In comparison, 631 the thicker geometry filled to a level of 99.5% can only contain 82  $\ cm^3$  of PCM. It appears 632 that the filling level is a more interesting parameter since it drastically impacts the stresses 633 involved, while decreasing the quantity of PCM only slightly.



634

Fig. 17. von Mises stresses for each configuration. The yield stress is displayed in red. The
 error bars are associated with the uncertainties on adiabatic compressibility. They correspond
 to two FSI simulations based on two different values of adiabatic compressibility.

638

#### 639 6.2 Thermal contact resistance

Excessive heat can severely impact electronic devices. The proposed geometry filled with 640 641 PCM is used to reduce the temperature. However, to be efficient, the contact between the innovative composite and devices must be efficient, i.e., the contact surface must be 642 maximized. The deformation of the solid structure decreases the exchange area and leads to a 643 loss in heat transfer (Fig. 18). Thermal contact resistance is defined as the ratio between the 644 peak and valley  $\delta$  (see Fig. 18) and the thermal conductivity of the medium between the 645 innovative composite and the electronic component (often air)  $R_{th} = \frac{\delta}{\lambda_{air}}$ . On the example in 646 Fig. 18,  $\delta \sim 1 \, mm$ , the temperature is approximately 85°C, which yields a thermal 647 conductivity of  $\lambda_{air} \sim 0.03 W. m^{-1}. K^{-1}$ , and  $R_{th} \sim 0.033 K. m^2. W^{-1}$ . The thermal contact 648 resistance is very significant in this configuration which is the worst one tested in the paper 649 and the most adverse case from electronic devices. Fig. 19 displays the displacements 650 according to the gyroid thickness for every filling level. 651



**Fig. 18.** Deformed 2% thick gyroid structure completely filled with PCM (scaled up by a factor of 10). The contact with an electronic component is less efficient due to deformation.  $\delta$ , the so-called peak to valley, is the distance between the component and the structure.

As seen in the previous section, the gyroid with 2% thick branches is the most efficient from 656 the stress point of view. However, with greater displacements, one could expect significant 657 thermal contact resistance. Fig. 19 shows that displacements are indeed far larger in this 658 configuration than with thicker gyroids, except with a filling level of 98.5%. The 659 displacements are of the order of  $10^{-4}$  m, like in every other configuration with thicknesses 660 of 4 to 10%. With such displacements, the thermal contact resistance is approximately  $R_{th} \sim$ 661  $0.0033 K.m^2.W^{-1}$ . Note that this value remains an important issue and must impact the 662 experimental performance. In our model, this feature is not considered and some differences 663 between the theoretical results presented in the paper and experimentation could occur on 664 account of this. Similarly, the contact between the PCM and copper before melting is not 665 taken into account in the model. The heat transfer between every part of the device could 666 therefore be slower than in the simulation, but should modify neither the structure 667 displacement nor the stresses significantly. 668



Fig. 19. Maximal displacement for each configuration. The error bars are associated with the
 uncertainties on adiabatic compressibility. They correspond to two FSI simulations based on
 two different values of adiabatic compressibility.

673

### 674 **7. Conclusion**

Electronic cooling relies on different techniques. Among them, PCMs mitigate temperature 675 increases. This approach is therefore widely used experimentally and is a subject of huge 676 interest in the community. However, the theoretical modeling of the coupled physical 677 phenomena remains a challenge. We have addressed this very complex problem and proposed 678 a complete 3D model involving CHT and FSI simulations, based on 3 open-source software 679 codes: OpenFOAM, CalculiX and preCICE. The PCM model, which has been implemented in 680 OpenFOAM, takes account of phase changes, conduction and convection. This model has 681 been validated on the analytical solution of the Stefan problem and experimental data of a 2D 682 configuration. The CHT simulations relied on the PCM model (OpenFOAM) and the 683 conduction in the solid architectured structure (CalculiX). The interface coupling between the 684 two codes was managed by preCICE. The FSI simulations aimed to compute the structure 685 displacements and induced stresses. Such information is very useful to prevent mechanical 686 failures and improve the efficiency of heat transfer at the interface with electronic 687 components, as deformation of the structure can worsen the contact. 688

This modeling was applied to gyroid structures, triply-periodic minimal surfaces, which are expected to behave efficiently. Such shapes do maximize the exchange surface, thus

intensifying heat transfer during heating and improving thermal damping in electronic 691 components. We have simulated several configurations with different geometry thicknesses 692 and various filling levels of PCM (from 98.5 to 100%). The thicknesses of the gyroid 693 branches ranged from 2% to 10% of the container box side length. Depending on the filling 694 rate, thermal expansion of liquid PCM led to pressure increases inside the 3D architectured 695 porous conductive matrix, and therefore significant mechanical stresses. For the first time, we 696 have shown that the filling ratio has a notable impact on the stresses that are induced. Only 697 1% short of the maximum volume reduces the mechanical stresses and failure risk 698 considerably. Compared to this low value, increasing the thickness of the container cuts a lot 699 more the PCM volume, and thus thermal performance. To optimize thermal management, 700 decreasing the quantity of PCM is thus preferable to strengthening the container geometry, 701 which scales the volume down too much. As the fluid pressure remains low, the solid 702 703 deformation is found to be small even for thin gyroids. The simulated maximal displacement with 2% thick branches is of the same order (0.1 mm), as with consolidated gyroids filled 704 with more PCM. The contact thermal resistance is therefore also of the same order of 705 magnitude. 706

707 With this 3D fluid-structure modeling of the heat and mass transfers in a complex system dedicated to the thermal management of electronic devices, we were able to select the 2% 708 thick gyroid as the most efficient configuration. A future study based on both experimentation 709 and simulation will be carried out with this design of architectured porous structures based on 710 metallic additive manufacturing impregnated with palmitic acid. This innovative composite 711 712 will be characterized to specify the input parameters of the simulations and validate the theoretical results. Following this study, the material will be integrated into a power supply in 713 order to evaluate its performance and its capacity to manage power peaks more effectively. 714

715

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719

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