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Article

Towards Resonantly Enhanced Acoustic Phonon-Exchange Magnon Interactions at THz Frequencies

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Abstract: Using valid experimental parameters, we quantify the magnitude of resonantly phonon-driven precession of exchange magnons in freestanding ferromagnetic nickel thin films on their thickness L . Analytical solutions of acoustically driven equations for magnon oscillators display a nonmonotonous dependence of the peak magnetization precession on the film thickness. It is explained by different L -dependence of multiple prefactors entering in the expression for the total magnetization dynamics. Depending on the ratio of acoustic and magnetic (Gilbert) damping constants, the magnetization precession is shown to be amplified by a Q -factor of either the phonon or the magnon resonance. The increase in the phonon mode amplitude for thinner membranes is also found to be significant. Focusing on the magnetization dynamics excited by the two first acoustic eigenmodes with $p = 1$ and $p = 2$, we predict the optimum thicknesses of nickel membranes to achieve large amplitude magnetization precession at multi 100 GHz frequencies at reasonably low values of an external magnetic field. By extending the study to the case of Ni-Si bilayers, we show that these resonances are achievable at even higher frequencies, approaching the THz range.

Keywords: magneto-acoustics; magnetization dynamics; ferromagnetic resonance; exchange magnons; acoustic phonons; Landau–Lifshitz–Gilbert equations; ultrafast laser interaction with materials



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1. Introduction

Ultrafast magneto-acoustics investigates peculiarities of ultrafast magnetization dynamics driven by ultrashort, fs-laser-excited acoustic transients [1–5]. In most cases, the physical interpretation of magneto-elastic interactions roots back to numerically solving the Landau–Lifshitz–Gilbert equations for ferromagnetic resonance (FMR) precession driven by time- and space-dependent magneto-elastic fields. This approach is well justified when the characteristic time scales of the magnetization precession are much longer than the duration of the magneto-elastic driving impact. Such simplified approach has been successfully used to describe the phenomenon of ultrafast magnetization switching in magnetostrictive thin films [6] and nanomagnets [7]. However, a closer look at the experimental data for magnetic semiconductors deposited on semi-infinite substrates [8] evidenced some more complicated magnetization dynamics and revealed contributions of the spatially inhomogeneous mod magnetization precession due to perpendicular standing spin wave modes (PSSWs, to be called magnons throughout this paper). The investigated GaMnAs ferromagnetic thin film with a thickness $L = 200$ nm was too thick for individual modes (to be called magnons) to be spectrally resolved. Another complication was that the acoustic excitation in the form of ultrashort acoustic pulses, injected in the GaMnAs layer from a semi-infinite GaAs substrate, was characterized by a continuous acoustic spectrum.

Several steps were undertaken to gain access to and quantify individual phonon–magnon interactions. First, reducing the thickness L of a ferromagnetic layer below a few tens of nanometers allowed the magnon modes to be well separated in frequency

domain [9,10]. Under these conditions, the injection of an ultrashort laser pulse from a semi-infinite substrate results in the excitation of multiple spectrally isolated magnon modes within the continuous frequency spectrum of ultrashort acoustic pulses [11].

Second, Kim and Bigot conceived and conducted an ultrafast optical experiment in a $L = 300$ nm thin freestanding nickel membrane acting as an acoustic cavity [12]. In this experiment, the modes of longitudinal acoustic phonons could be well resolved, each of them interacting with several spectrally overlapping magnon modes. Nevertheless, it was possible to partially discriminate distinct phonon–magnon resonances based on the selection rules for phonon and magnon modes of same/different parity [13].

Third, a recent purely theoretical study by Vernik et al. discussed the details of resonant phonon–magnon interactions for freestanding bi-layer and trilayer structures based on some model parameters for acoustic and magnetic damping.

In the present manuscript, we apply the results of quantitative analysis from Ghita et al. [13] using the extracted frequency-dependent acoustic damping factor $\beta \propto \omega$ and the magnetic Gilbert damping parameter $\alpha = 0.04$ to inspect the dynamics of resonantly enhanced phonon–magnon interactions in the ultrahigh frequency range as a function of nickel thickness L . The purpose of this work is to check the feasibility of experimental observation of this effect in the highest frequencies approaching the THz frequencies, i.e., the range important for studies in fundamental magnetism [10,14–16]. It is important to mention that in the high frequency range, other phenomena due to ultrafast laser demagnetization become apparent, such as, for example, electronic effects [17,18]. In our study, we focus solely on the magneto-acoustic interaction, which we consider to be stronger than other effects in the resonant regime.

2. Theoretical Description of Ultrafast Magneto-Acoustics in Freestanding Magnetostrictive Thin Films

Absorption of an ultrashort acoustic pulse excitation in a freestanding nickel membrane results in a nearly instantaneous (on acoustic time scales) spatially inhomogeneous heating profile, which can be approximated by an exponential function $\Delta T(z) \propto \exp(-z/h)$, see Figure 1a. The characteristic heating depth h typically exceeds the optical penetration depth of laser light due to the diffusion of hot electrons during the picosecond electron–phonon relaxation time [19,20]. Since the electron–phonon relaxation time depends on the excitation conditions [21], the effective heating depth h becomes experiment-specific and is treated as a fitting parameter [13,22]. Throughout this manuscript, we use the value $h = 60$ nm obtained from the comprehensive modeling of recent magneto-acoustic experiments [13].

Once impulsively heated, the film starts vibrating due to the thermal expansion, and the spatio-temporal dynamics of the acoustic strain $\varepsilon_{zz}(z, t)$ can be represented as a superposition of acoustic eigenmodes according to

$$\varepsilon_{zz}(z, t) = \sum_{p=1}^{\infty} \varepsilon_{zz}^{(p)}(z) e^{-\gamma_p t} \cos(\omega_p t + \varphi_p). \quad (1)$$

We assume acoustic eigenmodes to oscillate at frequencies $\omega_p = c_s k_p$ and decay with damping constants γ_p ; φ_p denote their initial phases. In a freestanding film, the acoustic eigenmodes obey the free boundary conditions for the acoustic displacement (corresponding to zero strains at both Ni/air interfaces) resulting in

$$\varepsilon_{zz}^{(p)}(z) = a_p \sin(k_p z), \quad (2)$$

where $k_p = \pi p/L$ is the wavevector of the p th acoustic eigenmode.

According to Ghita et al. [13], in the frequency range of 0–80 GHz, the damping coefficient $\gamma_p = \beta_p \omega_p$ scaled as $\gamma_p = G_{Ni} \omega_p^2$, where $G_{Ni} = 8.57 \times 10^{-14}$ s, is a damping constant characteristic to Ni [13]. As this is in correspondence with a model of damping

due to phonon–phonon scattering processes, we extrapolate this scaling to frequencies up to 0.5 THz, which is the highest frequency of a mode in our study.

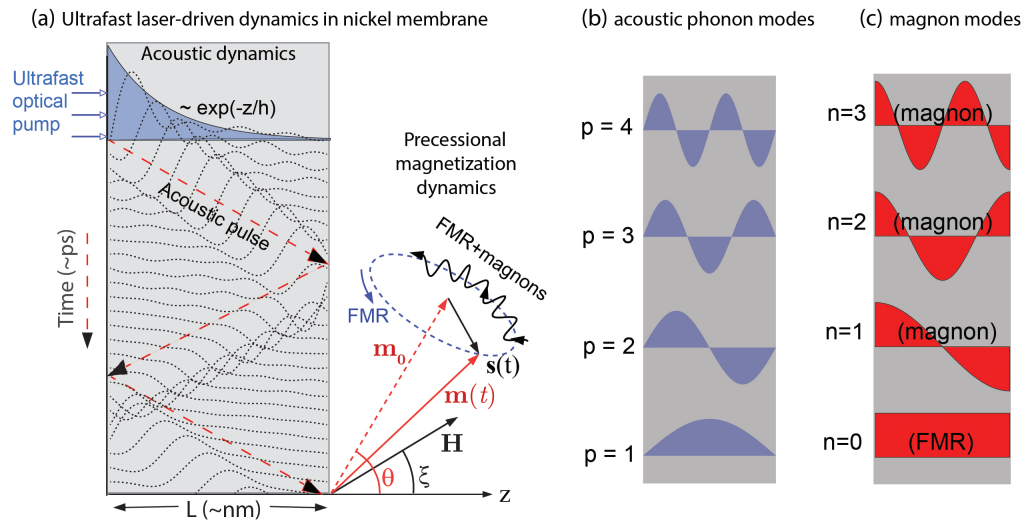


Figure 1. (a) Femtosecond laser excitation of a freestanding nickel membrane generates the thermal strain $\propto \exp -z/h$ launching acoustic pulses and precessional magnetization dynamics. Both dynamics can be decomposed in (b) acoustic phonon modes and (c) magnon modes.

In the same study, it was revealed that assuming an exponential heating profile with penetration depth $h = 60$ nm offers a satisfactory description of the mode amplitudes extracted from the experiment of Kim and Bigot. Assuming that for $z \in [0, L]$, the initial strain in the film is given by $\varepsilon_{zz}(z, 0) = A_0 e^{-z/h}$, the individual mode amplitudes read

$$a_p(L) = \frac{A_0}{L} \int_0^L e^{-z/h} \sin(k_p z) dz = A_0 \frac{\pi p}{(\pi^2 p^2 + (L/h)^2)} \left[1 - (-1)^p e^{-L/h} \right]. \quad (3)$$

In the following, we assume that the amplitude A_0 and the characteristic length scale h of the strain are constant and do not depend on the thickness L of the freestanding thin film. This assumption neglects thin-film effects in light absorption and reflection of heat at the back nickel–air interface. Possible (minor) corrections due to the aforementioned effects do not change the conclusions in this manuscript.

With this in mind, we can examine the dependence of the first three mode amplitudes on the film thickness L . It can be seen that when going down to thinner films, the first acoustic mode becomes over-represented with respect to the higher-order harmonics. As shown in panel (d) of Figure 2, the evolution of the strain amplitude of modes $p = 1$ and $p = 3$ is monotonous with respect to the increase in thickness L . On the contrary, the acoustic mode $p = 2$ displays a maximum at $L = 141$ nm. While these modes start with comparable values around $L = 300$ nm, the first mode experiences a steeper increase than the others as L decreases. Therefore, it is reasonable to assume that at lower film thicknesses, interactions governed by the first acoustic mode will dominate.

In a thin film of thickness L , the general form of the *spatially inhomogeneous* magnetization precession $\mathbf{m}(z, t) = \mathbf{m}_0 + \mathbf{s}(z, t)$ can be represented as a superposition in magnetic eigenmodes, i.e., PSSWs or exchange magnons superimposed on the FMR precession (see Figure 1a,c):

$$\mathbf{s}(z, t) = \sum_{n=0}^{\infty} \mathbf{s}^{(n)}(t) \cos(k_n z), \quad (4)$$

for $n = 0, 1, 2, \dots$ across the film with quantized wave vectors $k_n = \pi n / L$ and eigenfrequencies

$$\omega_n = \gamma \mu_0 \sqrt{(H \cos \xi - (\tilde{M} - \tilde{D} k_n^2) \cos \theta)^2 + (H \sin \xi + \tilde{D} k_n^2 \sin \theta)(H \sin \xi + (\tilde{M} + \tilde{D} k_n^2) \sin \theta)} \quad (5)$$

where $\tilde{D} = D^*/(\hbar\gamma\mu_0)$ is the exchange stiffness (the numerical value $D^* = 430$ [meV Å²] for Ni taken from ref. [9]), γ stands for the gyromagnetic ratio, μ_0 is vacuum permeability and \hbar is Planck's constant.

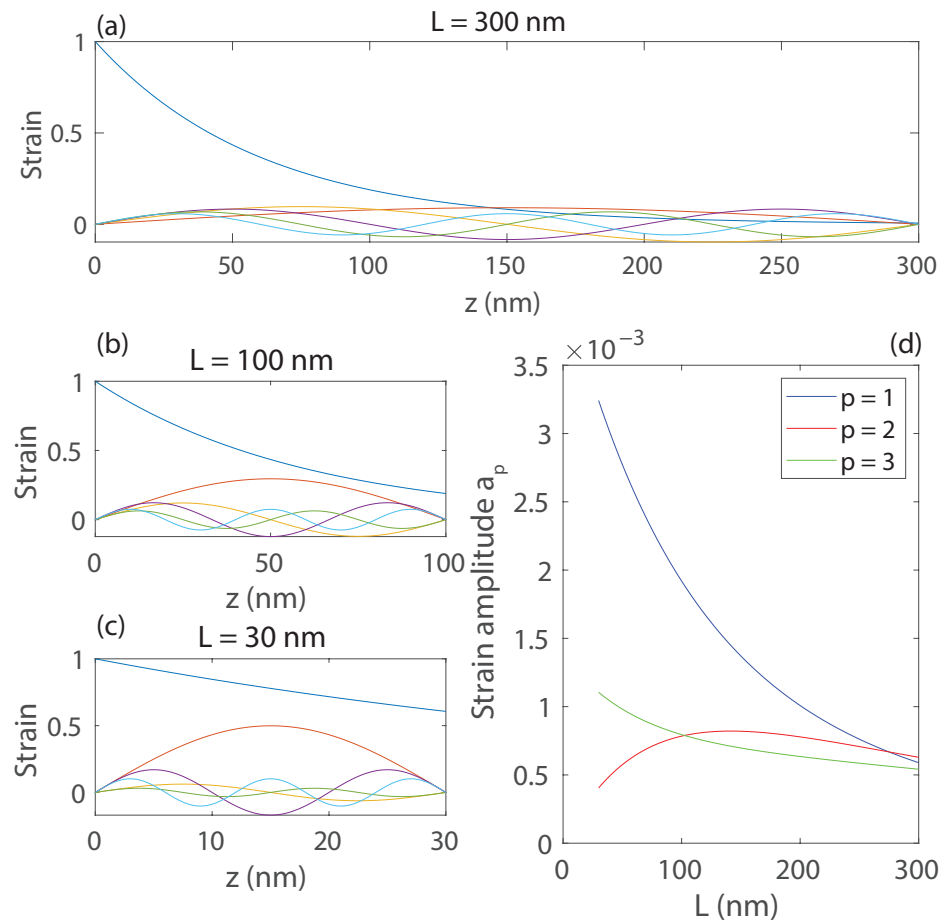


Figure 2. Illustration of the first few acoustic eigenmode profiles (normalized) for (a) $L = 300$ nm, (b) $L = 100$ nm and (c) $L = 30$ nm. In each graph, the blue line indicates the overall strain profile, while the other lines indicate the eigenmode components with their respective amplitudes. (d) Strain amplitudes $a_p(L)$, for the first three modes $p = 1, 2, 3$.

It has been shown recently [11,23] that in the linear approximation, when the acoustic strains are small, the magneto-elastically driven dynamics for each magnon mode satisfy the equation of a damped driven harmonic oscillator,

$$\frac{d^2 s_z^{(n)}}{dt^2} + 2\alpha\omega_n \frac{ds_z^{(n)}}{dt} + \omega_n^2 s_z^{(n)} = f_n(t). \tag{6}$$

The external magneto-elastic driving force,

$$f_n(t) = P_n(\mathbf{H}) \int_0^L \varepsilon_{zz}(z, t) \cos(k_n z) dz, \tag{7}$$

is proportional to the overlap integral between the magnon eigenmode with the acoustic strain pulse $\varepsilon_{zz}(z, t)$. For our experimental geometry, the prefactor,

$$P_n(\mathbf{H}, L) = \frac{\mu_0 \gamma^2 b_1 \sin(2\theta)}{M_0} \left(\tilde{D} k_n^2 \sin \theta + H \sin \xi \right), \tag{8}$$

is proportional to the magnetostriction coefficient b_1 and depends both on the magnitude and orientation of an external magnetic field \mathbf{H} .

Using the decomposition of the acoustic strain in its respective eigenmodes, the expression of the magneto-elastic driving force becomes

$$f_n(t) = P_n(\mathbf{H}) \sum_{p=1}^{\infty} I_{np} a_p e^{-\gamma_p t} \cos(\omega_p t + \varphi_p). \tag{9}$$

Here, we introduced the overlap integral [23],

$$I_{np} = \frac{1}{L} \int_0^L \cos(k_n z) \sin(k_p z) dz = \begin{cases} \frac{2p}{\pi(p^2 - n^2)} & \text{for odd } n + p \\ 0 & \text{for even } n + p \end{cases}, \tag{10}$$

between the n th magnetic and p th acoustic eigenmodes.

Therefore, the theoretical modeling in ultrafast magnetoacoustics is reduced to solving Equation (6) driven by a superposition of acoustic eigenmodes. The latter are quantified by amplitudes $a_p(L)$, frequencies $\omega_p(L) = c_s \pi p / L$ and damping constants $\beta_p(L) = G_{Ni} \omega_p(L)$. In order to evaluate the overall efficiency of magneto-elastic interactions, it is sufficient to inspect the analytical solutions for each magnon mode n driven by an individual phonon mode with index p as a function of nickel thickness L . For the purposes of numerical simulations, we use the valid experimental parameters used in [13], namely $\mu_0 M_0 = 0.6$ T, $c_s = 6.04 \times 10^3$ m/s and $G_{Ni} = 8.57 \times 10^{-14}$ s.

We note that the change in thickness of the film leads to a shift of acoustic frequencies with respect to the magnon modes, thus drifting away from the resonant regime. In order to preserve the resonant behavior, one needs to adjust the magnetic field \mathbf{H} . In the following, we preserve the orientation of \mathbf{H} at an angle $\zeta = 45^\circ$ with respect to normal while varying its modulus. Furthermore, we focus in our numerical studies on the interactions of the $p = 1$ and $p = 3$ acoustic modes with the $n = 0$ and $n = 2$ magnon modes, as well as that of the $p = 2$ acoustic mode with the $n = 1$ and $n = 3$ magnon modes.

This resonant tuning of \mathbf{H} to the acoustic frequencies induces a change in the prefactor $P_n(\mathbf{H})$, which in turn changes the driving force amplitude.

In the case of resonant interaction between a phonon and a magnon mode ($\omega_n = \omega_p$), the precession of magnetization in time is given by

$$s_z(t) = \frac{A}{2\omega_p^2(\alpha - \beta_p)} [e^{-\beta_p \omega_p t} - e^{-\alpha \omega_p t}] \sin(\omega_p t + \phi_p). \tag{11}$$

The expression for the maximum amplitude of magnetization precession of the n th magnon mode resonantly driven by the p th acoustic mode reads

$$s_{z,max}^{(np)}(L) = a_p(L) \left[\frac{I_{np} P_n(\mathbf{H}_{np}, L)}{\omega_p(L)^2} \right] A_{max}(\alpha, \beta_p(L)). \tag{12}$$

The damping-dependent factor

$$A_{max}(\alpha, \beta_p) = \frac{1}{2\alpha} \left(\frac{\alpha}{\beta_p} \right)^{-\frac{\beta_p}{\alpha - \beta_p}} \tag{13}$$

can be understood in terms of the quality factors $Q_m = 1/(2\alpha)$ and $Q_p = 1/(2\beta_p)$ for magnon and phonon modes, respectively:

$$A_{max}(\alpha, \beta_p) = Q_m \left(\frac{Q_p}{Q_m} \right)^{\frac{1}{1 - Q_p/Q_m}} \simeq \begin{cases} Q_p & \text{for } Q_m \gg Q_p \\ Q_m & \text{for } Q_m \ll Q_p \end{cases}. \tag{14}$$

Therefore, we conclude that resonant phonon–magnon interactions are enhanced by the smaller Q -factor.

Mathematical derivation of Equations (11)–(13) is provided in Appendix A. The rest of the manuscript is devoted to the numerical analysis for nickel membranes of arbitrary thickness L .

3. Numerical Results for Acoustically Driven Magnetization Dynamics and Their Discussion

In this section, we show the numerical results obtained through the prism of the above-mentioned theoretical treatment. Figure 3 shows the results for driven magnon oscillator equations for the $n = 0, p = 1$ and $n = 1, p = 2$ magnon–phonon pairs, respectively. The expected behavior of the rise and subsequent decay is recovered. We notice that both of the rise and decay time scales are decreasing as the film thickness decreases. Naturally, the frequency of these excitations increases, reaching values of up to 160 GHz.

We can already notice that in case of the $n = 0$ FMR mode driven by the $p = 1$ phonon mode; the maximal magnetization displays the non-monotonous dependence on the film thickness L . Furthermore, the magnetic field needed to achieve this resonance increases with the decreasing thickness. For the considered values of the thickness ($L = 300$ nm, $L = 150$ nm, $L = 75$ nm, $L = 50$ nm and $L = 37.5$ nm), there is no clear conclusion on the dependence of this maximal magnetization in the case of the $n = 1$ magnon mode driven by the $p = 2$ phonon mode. As such, it is interesting to study the dependence of the maximal magnetization achieved, as well as the magnetic field needed for the resonant interaction as a function of film thickness L .

Figure 4 shows the thickness dependence of the resonant magnetic field (lower panel) and the maximal magnetization (upper panel) for six distinct phonon–magnon resonances. We start our discussion from two phonon–magnon resonances observed in the Kim and Bigot experiment performed for $L = 300$ nm [13]: the $p = 1$ -excited $n = 0$ FMR precession and the $p = 2$ -excited $n = 1$ magnon. In the first case, one can see that for $L = 65$ nm the FMR precession can be amplified by a factor of 10 compared with the Kim and Bigot experiment. Meanwhile, for the driving of the $n = 1$ mode, a peak precession amplitude is achieved for $L = 180$ nm, but the increase in precession with respect to the Kim and Bigot experiment is marginal (only a factor of 1.25).

One can furthermore see that these two *low-order* phonon–magnon resonances are the ones with the largest amplitudes when going towards smaller thicknesses. Furthermore, in terms of the required resonant magnetic fields, for film thicknesses $L > 50$ nm the fields stay in the range below 10 T (and below 5 T for low-order resonances). These experimentally achievable magnetic fields suggest that for this range of thicknesses, a resonant phonon–magnon interaction can be observed and measured. The problem arises when considering the behaviour at very small film thicknesses (or, equivalently, at very high frequencies, exceeding 100 GHz). One notices that the required resonant magnetic fields diverge to unreasonably high values. However, for certain phonon–magnon pairs (evidenced with dotted lines in Figure 4), there is a sharp decrease toward zero of these required magnetic fields. As such, at certain very low thicknesses, one can again find high-frequency phonon–magnon resonances at experimentally reasonable magnetic fields.

We focus our analysis on one of these cases, namely that of a $L = 16$ nm film thickness. Figure 5b shows the magneto-acoustic interaction landscape given by the dependence of the magnitude of the Fourier transform of $s_z(t)$ on the external magnetic field. One notices a rather faint, yet visible trace of resonant behavior at the intersection of the $p = 1$ and $n = 2$ phonon and magnon curves. This resonant enhancement is achieved for the external magnetic field value $H = 0.75$ T at a frequency of approximately 200 GHz. Numerical simulation of magnetization dynamics at this set of experimental parameters indeed shows a behaviour as expected, with the typical rise and decay time being evident in magnetization dynamics. As such, we achieved the main goal of this paper: to demonstrate that previously anticipated higher-order phonon–magnon resonances in hybrid metal–ferromagnet membranes [23] can be indeed achieved using realistic parameters [13] in much simpler structures, i.e., thin nickel membranes.

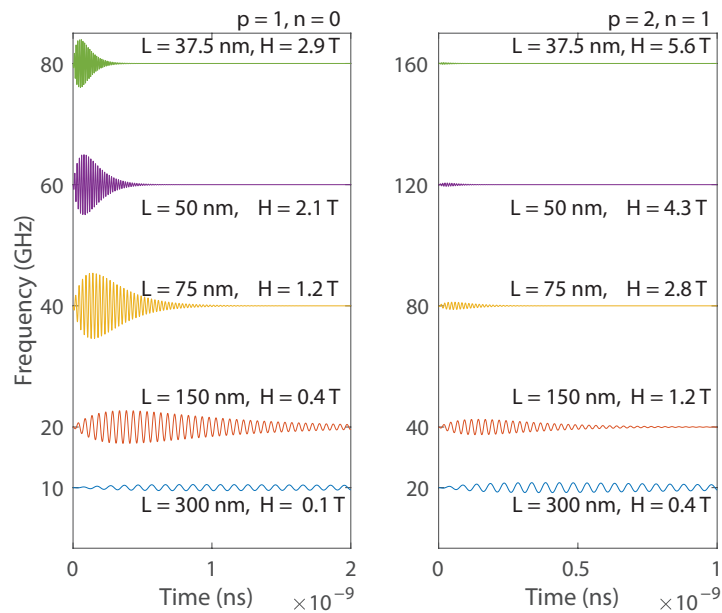


Figure 3. Magneto-acoustic resonances of different acoustic p and magnetic n orders behave differently as the thickness of a freestanding nickel layer decreases. Acoustically driven magnetization precession of $p = 1$ -driven $n = 0$ (FMR) and $p = 2$ -driven $n = 1$ (magnon) precession for different values of film thickness L ($L = 300$ nm, $L = 150$ nm, $L = 75$ nm, $L = 50$ nm and $L = 37.5$ nm). The required magnetic field values are indicated next to each curve.

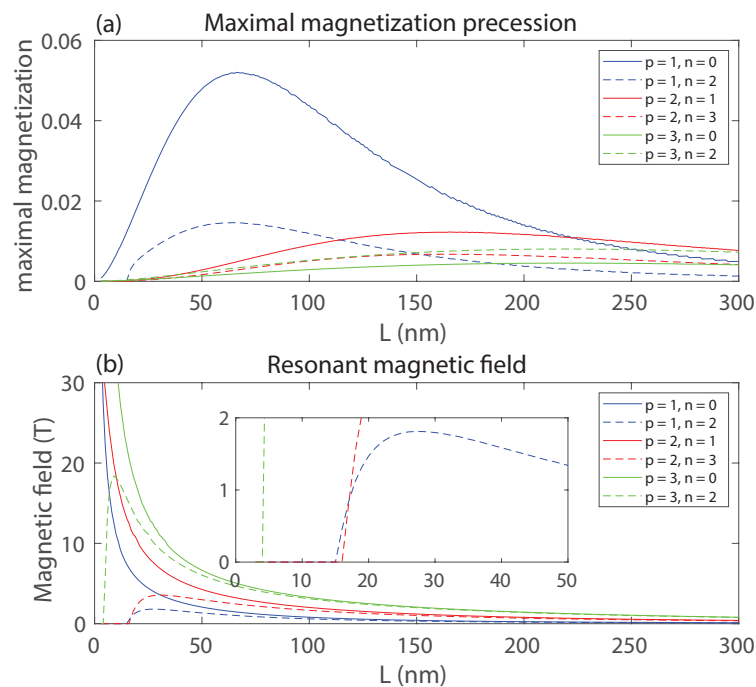


Figure 4. (a) Peak magnetization amplitude dependence on film thickness for different phonon–magnon pairs (p, n). (b) Magnetic field necessary for resonant interaction versus film thickness for different phonon–magnon pairs (p, n). The inset shows the same graph restricted to experimentally feasible magnetic fields in the range of 0 T–2 T and to film thicknesses between 0 and 50 nm. A prominent feature is the sudden fall to zero of the magnetic field necessary to achieve a magnon resonance for film thicknesses of 16 nm ($p = 1, n = 0$ and $p = 2, n = 1$) and 3 nm, respectively ($p = 3, n = 0$).

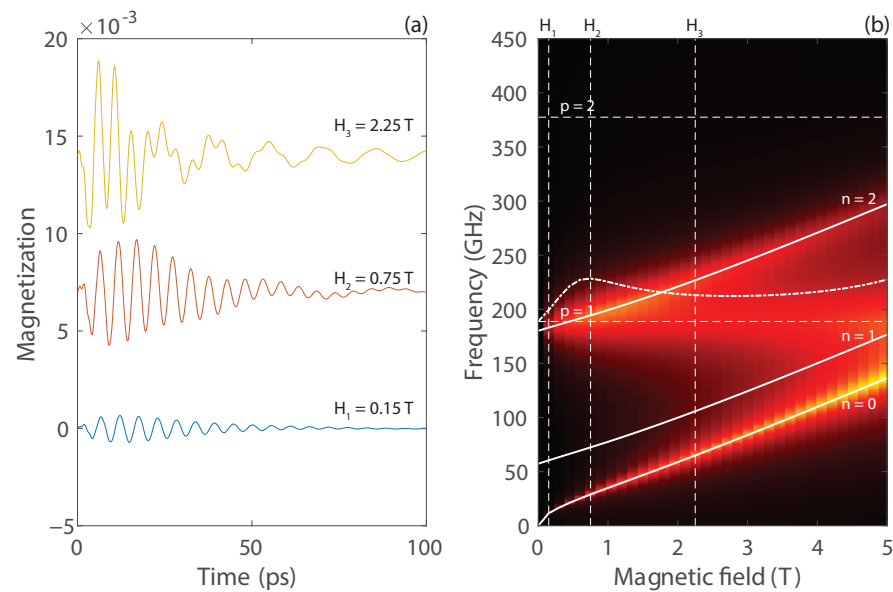


Figure 5. (a) Magnetization dynamics for $L = 16$ nm thick film under magnetic fields $H_1 = 0.15$ T, $H_2 = 0.75$ T and $H_3 = 2.15$ T. The magnetization precession at H_2 presents all the characteristic features of the above-discussed resonant behavior. The precession under the field H_1 is very weak, while the precession at H_3 displays a sharp, strong initial excitation that quickly dies out and decays into an irregular beating pattern. (b) The absolute value of the Fourier transform of $s_z(t)$ displays the magneto-acoustic resonant landscape for $L = 16$ nm. Dashed white lines show acoustic frequencies and solid white lines show magnon dispersion according to Equation (5). The dashed–dotted line displays the cross-section at the $p = 1$ acoustic frequency and is interpreted as the magnetic field dependence of the $n = 2$ resonance driven by the acoustic $p = 1$ mode.

It is worth mentioning that the resonant curve is described by the analytical expression in Equation (12). As such, Equation (12) represents a powerful tool to engineer arbitrary phonon–magnon resonances as a function of magnetic and acoustic material parameters. For example, experiments with magnetic dielectrics BiYIG [15,24–27], characterized by orders-of-magnitude lower values of the Gilbert damping parameter $\alpha \sim 10^{-4}$, may seem better candidates to observe large-amplitude phonon–magnon interactions at first glance. However, in the limit $\alpha \ll \beta_p$, Equation (14) converges towards Q_p indicating the crucial role of the acoustic damping β_p in this case. This rather straightforward example demonstrates that the choice of an optimum combination of membrane’s material and thickness represents a rather nontrivial multiparameter optimization problem.

4. Acoustically Driven Magnetization Dynamics in Freestanding Nickel/Silicon Membranes

Attempts of boosting phonon–magnon interactions at ultrahigh frequencies in freestanding nickel membranes face two serious problems. First, the required ultrathin membranes with 10–20 nm thickness seem to be difficult to fabricate. Second, the substantial acoustic damping in Nickel leads to the reduction in acoustic quality factors, notably in the above 100 GHz frequency range.

Both problems can be overcome by using hybrid multilayer structures, notably to resolve problems with strong acoustic damping. Similar to previous investigations in magneto-plasmonics, where a combination of lossy ferromagnetic metals (such as Ni, Fe or Co) was partially compensated by low-loss plasmonic materials (i.e., Au, Ag, Cu) [28], here, we propose functionalizing nickel thin films with a layer of low-loss material to decrease the effective damping of acoustic modes in multilayer structures. To be more specific, we consider a bilayer structure consisting of a Ni thin film of thickness L_{Ni} placed on a Si membrane of thickness L_{Si} . The frequency dependence of acoustic damping in Si has

been already extensively studied [29,30]. It can be approximated by the same quadratic dependence of the damping coefficient γ_{Si} on frequency, namely

$$\gamma_{Si} = G_{Si}\omega^2. \quad (15)$$

Here, the value of the damping coefficient $G_{Si} = 1.71 \times 10^{-14}$ s is almost one order of magnitude lower than that of Ni. As such, in a bilayer structure consisting of both Ni and Si, the overall damping still follows a quadratic dependence on frequency, but with an effective damping coefficient given by

$$G = \frac{G_{Ni} \frac{L_{Ni}}{c_{s,Ni}} + G_{Si} \frac{L_{Si}}{c_{s,Si}}}{\frac{L_{Ni}}{c_{s,Ni}} + \frac{L_{Si}}{c_{s,Si}}}. \quad (16)$$

Such an expression, where $c_{s,Ni}$ and $c_{s,Si}$ correspond to the speed of sound in Ni and Si, respectively, can be phenomenologically derived by considering the damping of a back-and-forth propagating acoustic wave over one round trip in the bilayer structure.

We assume that in these structures, the initial strain decays exponentially within the depth $h = 60$ nm from the surface of Ni, and it is equal to zero inside the Si layer which is semi-transparent to the laser beam in the infrared frequency range. In this case, the eigenmode decomposition must be modified to account for the new boundary conditions at the interface between Ni and Si. This procedure has been described in detail by Vernik et al. [23], who studied ultrafast magneto-acoustics in Ni/Au bilayers using order-of-magnitude estimates for the acoustic damping. In this study, we have extended these numerical simulations to account for realistic frequency-dependent damping parameters in Ni and Si.

These simulations for the Ni/Si bilayer structures show that resonant phonon–magnon interactions at even higher frequencies of 0.5 THz are achievable under experimentally feasible conditions. Figure 6 demonstrates that a (5 nm)Ni/(12 nm)Si bilayer membrane should exhibit the magneto-acoustic resonance between the $n = 1$ and $p = 2$ modes at about 0.5 THz under an external field of the order of 1 Tesla.

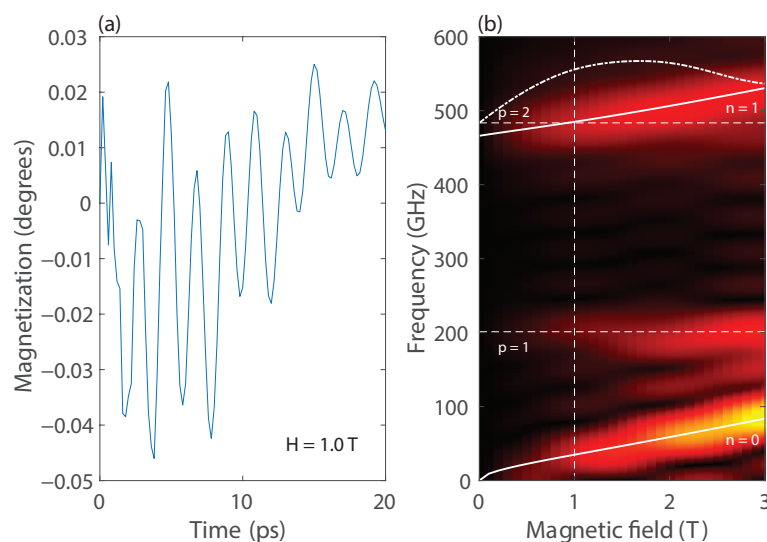


Figure 6. (a) Magnetization dynamics for the $L_{Ni} = 5$ nm, $L_{Si} = 12$ nm bilayer structure under magnetic field $H = 1.0$ T. The frequency of the precession is 0.48 GHz and its amplitude reaches 0.05 degrees. (b) The absolute value of the Fourier transform of $s_z(t)$ displays the magneto-acoustic resonant landscape for such Ni/Si bilayer structure. Dashed white lines show acoustic frequencies and solid white lines show magnon dispersion curves. The dashed–dotted line displays the cross-section at the $p = 2$ acoustic frequency and is interpreted as the magnetic field dependence of the $n = 1$ -magnon resonance driven by the acoustic $p = 2$ mode.

5. Conclusions

We performed extensive analytical calculations for resonantly enhanced phonon–magnon interactions in freestanding nickel films in fs-laser-excited magnetostrictive membranes of arbitrary thickness L . Solutions of driven harmonic oscillator equations for each magnon modes demonstrate the complex nonlinear dependence on multiple physical parameters highlighting the role of magnetic and acoustic damping factors as well as the heat penetration depth and acoustic mode amplitudes to achieve the maximum peak precession amplitude. The application of this modeling to freestanding ferromagnetic nickel membranes, as well as multilayer structures, suggests that experimental observations of elastically driven multi-100 GHz exchange magnon resonances in ultrathin membranes can be observed at moderate values of the external magnetic field below 1 Tesla. The use of hybrid semiconductor–ferromagnet membranes allows for the substantial reduction in acoustic losses while preserving the magnetic properties of ferromagnetic compounds. Apart from ferromagnetic metals and their hybrids, our analytical results can be adopted to describe ultrafast magneto-acoustics in ferromagnetic semiconductors [1,8] and dielectrics [24,26,27]. The extension of these studies to the THz frequency range are particularly important in view of the inertial effects in magnetization dynamics [14,15,31,32].

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Abbreviations

The following abbreviations are used in this manuscript:

PSSW Perpendicular standing spin waves
FMR ferromagnetic resonance

Appendix A

In this appendix, we present a derivation of Equations (12) and (13), starting from Equations (6)–(10). We consider the resonant interaction regime between any two phonon–magnon modes p and n , i.e., when the driving force frequency ω_p is equal to the magnon frequency ω_n ; thus, we neglect the contribution of any other phonon–magnon pair. In this case, the driving force is simply given by

$$f_n(t) = Ae^{-\beta_p\omega_p t} \cos \omega_p t = \frac{A}{2}e^{(-\beta_p+i)\omega t} + \frac{A}{2}e^{(-\beta_p-i)\omega_p t}, \quad (\text{A1})$$

where the driving force amplitude is $A = P_n(\mathbf{H})I_{np}a_p$. The standard approach is to first find a driven solution of Equation (6), then superpose with an eigensolution of the associated homogeneous equation such that the total solution obeys the initial time conditions $s_z(0) = 0$ and $\frac{ds_z}{dt}(0) = 0$. Let us find the driven solution associated to each term. For the

first term, let us seek a solution of the form $s_{z1} = Be^{(-\beta_p+i)\omega_p t}$. Plugging this back into Equation (6), we find the following condition on B :

$$[2i(\alpha - \beta_p) + \beta_p^2 - 2\alpha\beta_p]\omega_p^2 B = \frac{A}{2}. \tag{A2}$$

Given the typical values of α and β_p , on the order of 10^{-2} , we can distinguish two different regimes. When the difference between α and β_p is large, as is the case for most experimental applications, the terms β_p^2 and $2\alpha\beta_p$ can be neglected. On the other hand, the case where $\alpha \approx \beta_p$ yields qualitatively different behavior. We start with the analysis of the first case. The amplitude of the driven solution s_{z1} is given by

$$B = \frac{A}{4i\omega_p^2(\alpha - \beta_p)}. \tag{A3}$$

By following a similar approach for the second term in the driving force, the total driven solution of Equation (6) can be expressed as

$$s_{z,d} = \frac{A}{2\omega_p^2(\alpha - \beta_p)} e^{-\beta_p\omega_p t} \sin \omega_p t. \tag{A4}$$

Keeping in mind the initial conditions on s_z and its time derivative, we find the following suitable eigensolution of Equation (6):

$$s_{z,e} = -\frac{A}{2\omega_p^2(\alpha - \beta_p)} e^{-\alpha\omega_p t} \sin \omega_p t. \tag{A5}$$

Finally, the solution of the driven magnon oscillator reads

$$s_z = \frac{A}{2\omega_p^2(\alpha - \beta_p)} [e^{-\beta_p\omega_p t} - e^{-\alpha\omega_p t}] \sin \omega_p t. \tag{A6}$$

We note that the above equation contains a sinusoidal oscillation, with an amplitude depending on time as $e^{-\beta_p\omega_p t} - e^{-\alpha\omega_p t}$. Given that the oscillation is usually significantly faster than the time scales of amplitude evolution, we can assume that the maximum of s_z is given by the maximum of the amplitude envelope, whose expression is

$$s_{z,max}^{(np)}(L) = \frac{A}{\omega_p^2} A_{max}(\alpha, \beta_p). \tag{A7}$$

Here, the factor $A_{max}(\alpha, \beta_p)$ captures the maximal value of the envelope given by

$$A_{max}(\alpha, \beta_p) = \frac{1}{2\alpha} \left(\frac{\alpha}{\beta_p} \right)^{-\frac{\beta_p}{\alpha - \beta_p}}, \tag{A8}$$

which finishes our proof.

From an experimental point of view, the value of parameter β_p can be varied by changing the film thickness L given the quadratic dependency of the acoustic damping γ_p on the acoustic frequencies ω_p . Indeed, the frequency of the p acoustic mode scales inversely proportional to the film thickness L according to

$$\omega_p(L) = c_s \frac{\pi p}{L}. \tag{A9}$$

Assuming a quadratic dependence of γ_p on ω_p given by $\gamma_p = G\omega_p^2$, we determine that the damping coefficient β_p corresponding to mode p also scales inversely proportional to the film thickness,

$$\beta_p(L) = G\omega_p(L). \tag{A10}$$

Finally, even though the derivation assumes that there is a large difference between α and β_p , we note that the solution is extendable by continuity around $\alpha = \beta_p$. A numerical study showed that there is no peculiar behavior in this region, such that the solution can still be considered as valid.

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