

Bi-objective Sustainable Crowdshipping with Multi Types of Occasional Drivers

Daniel Sanchez, Audrey Cerqueus, Khakim Habibi, Alexandre Dolgui

To cite this version:

Daniel Sanchez, Audrey Cerqueus, Khakim Habibi, Alexandre Dolgui. Bi-objective Sustainable Crowdshipping with Multi Types of Occasional Drivers. INCOM 2024: 18th IFAC Symposium on Information Control Problems in Manufacturing, Aug 2024, Vienne, Austria. pp.498-503, $10.1016/j.i$ facol.2024.09.261. hal-04782210

HAL Id: hal-04782210 <https://hal.science/hal-04782210v1>

Submitted on 19 Nov 2024

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

[Distributed under a Creative Commons Attribution - NonCommercial - NoDerivatives 4.0](http://creativecommons.org/licenses/by-nc-nd/4.0/) [International License](http://creativecommons.org/licenses/by-nc-nd/4.0/)

Available online at www.sciencedirect.com

IFAC PapersOnLine 58-19 (2024) 498–503 B_0 -objective Sustainable Crowdship Crowdshipping Crowdshipping

Bi-objective Sustainable Crowdshipping Bi-objective Sustainable Crowdshipping Bi-objective Sustainable Crowdshipping Nanchez ∗ Audreich ∗ Audrey ∗ Khakim Habibi ∗∗ Khakim Habibi ∗∗∗ Khakim Habibi ∗∗ Khakim Habibi ∗∗∗ with Multi Types of Occasional Drivers Bi-objective Sustainable Crowdshipping with Multi Types of Occasional Drivers

Daniel Sanchez ∗ Audrey Cerqueus ∗ Khakim Habibi ** Alexandre Dolgui ∗ Alexandre Dolgui ∗ Alexandre Dolgui ∗ Daniel Sanchez ∗ Audrey Cerqueus ∗ Khakim Habibi ∗∗

UMR 6004, Nantes France $(e-mail: \{daniel.sanchez-pineda, \,audrey.cerqueus, \,alexandre.dolgui\}$ e-mail: {daniel.sanchez-pineda, audrey.cerqueus, alexandre.dolgui} $@nmt-atlantique.fr).$
** Rennes School of Business, Rennes, France ∗∗ Rennes School of Business, Rennes, France (e-mail: muhammad.habibi@rennes-sb.com). ∗ IMT Atlantique, Nantes Universit´e, Ecole Centrale, CNRS, LS2N - ∗ IMT Atlantique, Nantes Universit´e, Ecole Centrale, CNRS, LS2N - Alexandre Dolgui ∗ $\frac{1}{\sqrt{2\pi}}$ Rennes School of Business, Rennes, $\frac{1}{\sqrt{2\pi}}$

(e-mail: muhammad.habibidi.habibidi.habibidi.habibidi.habibidi.habibidi.habibidi.habibidi.habibidi.habibidi.h
.

Abstract. The current work presents a deterministic bi-objective sustainable crowdsinpping
problem optimizing both the cost and CO2 emissions, referred to as the Bi-Objective Veproblem optimizing both the cost and CO2 emissions, referred to as the Di-Objective ve-
hicle Routing Problem with Multi types of Occasional Drivers and Time Windows (BO-Increased The William Multiples of Octasional Diversional Time Windows (BO-
VRPMODTW). The goals of this work are to verify the trade-off between transportation cost and environmental emissions generation, considering different types of ODs, and to verify the and environmental emissions generation, considering different types of ODs, and to verify the
impact in different location spreading for customers. Preliminary experimental results show the impact in different location spreading for customers. Preliminary experimental results show the
gain both in terms of cost and CO2 emissions of having ODs of different types. The use of ODs $\frac{1}{2}$ in the non-dominated solutions is also analyzed. (e-mail: muhammad.habibi@rennes-sb.com). Abstract: The current work presents a deterministic bi-objective sustainable crowdshipping gain both in terms of cost and CO2 emissions of having ODs of different types. The use of ODs and environmental emissions generation, considering different types of ODs, and to verify the
impact in different legation conseding for outcomens. Proliminary cynerimental posults chargits and the unit considering the constant α of α or α of α or α of α or α or gain both in terms of cost and CO2 emissions of naving ODs of different types. The use of ODs
in the new deviated relations is also such real hele Kouting Problem with Multi types of Occasional Drivers and Time Windows (BO $v_{\rm KPMOD1}$ w). The goals of this work are to verify the trade-off between transportation cost impact in different location spreading for customers. Preliminary experimental results show the

 α in the non-dominated solutions is also analyzed.
Convright © 2024 The Authors This is an open access article under the CC BY-NC-ND license. Copyright \odot 2024 The Authors. This is an open access article under the CC BY-NC-ND license (https://creativecommons.org/licenses/by-nc-nd/4.0/)

Keywords: Sustainability, Crowdshipping, Multi-objective optimization, Transportation types Keywords: Sustainability, Crowdshipping, Multi-objective optimization, Transportation types Keywords: Sustainability, Crowdshipping, Multi-objective optimization, Transportation types

1. INTRODUCTION 1. INTRODUCTION 1. **INTRODUCTION** 1. INTRODUCTION

In the last years, Business-to-Consumer (B2C) E-commerce in the last years, business-to-Consumer (B2C) E-commerce
operations had an exponential increase, representing apoperations had an exponential increase, representing ap-
proximately one-quarter of total global retail sales in 2023. proximately one-quarter or total global retail sales in 2025.
This growth involves an increasing requirement for urban This growth involves an increasing requirement for urban
delivery and last-mile delivery solutions. Last-mile delivery denvery and last-line denvery solutions. Last-line denvery
is renowned as the most complex, expensive, and timeis renowned as the most complex, expensive, and time-
consuming part of delivery logistics. The key challenges consuming part or denvery logistics. The key chanenges
for retailers are guaranteeing faster delivery to meet cusfor retailers are guaranteeing raster derivery to meet cus-
tomers' need while minimizing costs. Therefore, the gencomers need while infinitizing costs. Therefore, the generation of innovative solutions to enhance same-day and eration of innovative solutions to enhance same-day and
last-mile delivery is a priority (Elsokkary et al., 2023). astermile delivery is a priority (Elsokkary et al., 2020). eration of importive solutions to emiance same-uay a is renowned as the most complex, expensive, and timefor retailers are guaranteeing faster delivery to meet cus-
tangers' used relik minimizing saster Thangfore the new eration of innovative solutions to enhance same-day and
hert will delivere is a minimize (Flashborne, the general last-mile delivery is a priority (Elsokkary et al., 2023). operations had an exponential increase, representing approximately one-quarter of total global retail sales in 2023. This growth involves an increasing requirement for urban consuming part of delivery logistics. The key challenges tomers' need while minimizing costs. Therefore, the gen-

One of the innovative solutions considered among on-One or the innovative solutions considered among on-
line retailers is crowdshipping, also referred to as crowdnne retaners is crowdsmpping, also referred to as crowd-
sourced delivery or crowd logistics (Strulak-Wójcikiewicz sourced denvery of crowd logistics (Strutan-Wojchkewicz
and Wagner, 2021). It is a part of a sharing economy trend dent wagner, 2021). It is a part of a sharing coolonity trend ocused on neight transportation, which addresses ulstribution issues by using people who have the willingness to $\frac{1}{2}$ and $\frac{1}{2}$ and $\frac{1}{2}$ and $\frac{1}{2}$ are the winning destinations, execute deliveries on the way to their hormal destinations,
without affecting their habitual route. This use of Occawithout allecting their habitual route. This use of Occa-
sional Drivers - (ODs) aims to exploit underused capacity to cover the businesses' transportation needs (Archetti et al., 2016). to cover the businesses' transportation needs (Archetti et al., 2016). to cover the businesses' transportation needs (Archetti α and β crowdshipping reuses α 1. INTRODUCTION use of sustainable modes that could replace the regular three spin transportation modes based on fossil method transportation and a regeneration and a regeneration and a regeneration and a regeneration of focused on freight transportation, which addresses distribution issues by using people who have the willingness to $\frac{1}{2}$ $\frac{1}{2}$ cover the sourced delivery or crowd logistics (Strulak-Wojcikiewicz and Wagner, 2021). It is a part of a sharing economy trend without affecting their habitual route. This use of Occa-
execute deliveries on the way to the $\frac{1}{2}$ sional Drivers - (ODs) aims to exploit under used capacity to cover the businesses' transportation needs (Archetti line retailers is crowdshipping, also referred to as crowdsourced delivery or crowd-logistics (Strulak-Wojcikiewicz s sional Drivers - (ODs) aims to exploit underused capacity

Because crowdshipping reuses excess capacity of vehicle, it is presented as a sustainable option. However, the indusis presented as a sustainable option. However, the mutus-
trial crowdshipping initiatives have shown that in a largecrial crowdsinpping initiatives have shown that in a large-
scale adoption, it does not necessarily imply sustainability, scale adoption, it does not necessarily imply sustainability,
indeed the compensation schemes defined for the ODs mored the compensation schemes defined for the ODs
can attract more drivers, executing deliveries out of their normal routes, increasing generated emissions and vehicle can attract more drivers, executing deliveries out of their normal routes, increasing generated emissions and vehicle normal routes, increasing generated emissions and vehicle density. It is frequently mentioned that a way to secure density. It is frequently mentioned that a way to seem the sustainable value in crowdshipping is to consider the $\overline{}$ Because crowdshipping reuses excess capacity of vehicle, it
is presented as a sustainable option. However, the indusdensity. It is frequently mentioned that a way to secure density. It is frequently mentioned that a way to secure the sustainable consideration of the consideration of \mathbf{r} mated the compensation schemes defined for the ODS
can attract more drivers, executing deliveries out of their
normal routes, increasing generated emissions and vehicle
density. It is frequently mentioned that a way to sec trial crowdshipping initiatives have shown that in a large- $\frac{1}{100}$ scale adoption, it does not necessarily imply sustainability, indeed the compensation schemes defined for the ODs can attract more drivers, executing deliveries out of their normal routes, increasing generated emissions and vehicle $\overline{\text{use of sustainable modes that could replace}}$ the regular transportation modes based on fossil fuels. However, the transportation mode effectively used has not yet explicitly transportation mode effectively also has not yet explicitly
been defined (de Oliveira Leite Nascimento et al., 2023). been defined (de Oliveira Leite Nascimento et al., 2020). transportation modes based on fossil fuels. However, the
transportation modes based on fossil fuels. However, the been defined (de Oliveira Leite Nascimento et al., 2023). transportation mode effectively used has not yet explicitly been defined (de Oliveira Leite Nascimento et al., 2023).

In this work, we present a bi-objective crowdshipping In this work, we present a bi-objective crowdshipping
problem optimizing both the cost and CO2 emissions, problem optimizing both the cost and CO2 emissions,
referred to as the Bi-Objective Vehicle Routing Problem with Multi types of Occasional Drivers and Time Windows referred to as the Bi-Objective Vehicle Routing Problem referred to as the Bi-Objective Vehicle Routing Problem with Multi types of Occasional Drivers and Time Windows
(BO-VRPMODTW). The goal of this work is to answer
to the following research questions: (1) What is the cost
of reducing emissions in this context? (2) What is the
eco (100 V) and (100 V) . The goal of this work is to answer to the following research questions. (1) What is the cost of reducing emissions in this context? (2) What is the of reducing emissions in this context: (2) What is the economical and environmental gain to consider different economical and environmental gain to consider different
vehicle types for the ODs? (3) How does the geographical spreading of customers and ODs impact the solutions?. spreading of easterners and ODs impact the solutions. referred to as the Bi-Objective Vehicle Routing Problem $(100 - v \text{ft }100)$ to the goal of this work is to allower vehicle types for the ODs! (3) How does the geographical
spreading of sustances and ODs impact the solutions? In this work, we present a bi-objective crowdshipping
problem outlining hath the sectoral $CO2$ musiciment problem optimizing both the cost and CO2 emissions, With Multi types of Occasional Divers and Time Windows
(BO-VRPMODTW). The goal of this work is to answer
to the following research questions: (1) What is the cost
of reducing emissions in this context? (2) What is the
econ spreading of customers and ODs impact the solutions?. $(BU-VRPMUDTW)$. The goal of this work is to answer of reducing emissions in this context? (2) What is the economical and environmental gain to consider different vehicle types for the ODs. (3) How does the geographical

The remainder of this paper is organized as follows: In The remainder of this paper is organized as follows: In The remainder of this paper is organized as follows: In Section 2 a literature review is presented, in Section 3 section 2 a interactive review is presented, in Section 3
the mathematical model is developed, in Section 4 the the mathematical model is developed, in Section 4 the
computational experiment and the results are described, and the conclusions are summarized in Section 5. computational experiment and the results are described, and the conclusions are summarized in Section 5. and the conclusions are summarized in Section 5. The remainder of this paper is organized as follows: In S_{tot} the mathematical model is developed, in Section 4 the computational experiment and the results are described, and the conclusions are summarized in Section \mathfrak{b} . Section 2 a literature review is presented, in Section 3

2. LITERATURE REVIEW 2. LITERATURE REVIEW 2. LITERATURE REVIEW 2. LITERATURE REVIEW

The first crowdshipping model is proposed in (Archetti et al., 2016), referred to as the Vehicle Routing Problem with Occasional Drivers (VRPOD), which is a variant of with Occasional Drivers (VRI OD), which is a variant of the classic capacitated VRP (CVRP), where the company the classic capacitation $V\Lambda F$ ($C\Lambda F$), where the company
considers a set of in-store customers, which are customers considers a set of in-store customers, which are customers
already located in a company store or depot and identified an eady located in a company store or depot and identified
by their expected final destinations, as occasional drivers by their expected final destinations, as occasional directs
able to do a single delivery, in addition to a fleet of able to do a single delivery, in addition to a fleet of capacitated vehicles. The authors aim to minimize the total cost of the regular fleet and the compensation given capacitated vehicles. The authors aim to minimize the total cost of the regular fleet and the compensation given et al., 2016), referred to as the Vehicle Routing Problem
with Occasional Drivers (VDDOD), which is a variant of total cost of the regular fleet and the compensation given The first crowdshipping model is proposed in (Archetti already located in a company store or depot and identified
by their sexested final derivatives, we associated defined by their expected final destinations, as occasional drivers able to do a single delivery, in addition to a fleet of capacitated vehicles. The authors aim to minimize the the classic capacitated VRP (CVRP), where the company considers a set of in-store customers, which are customers able to do a single delivery, in addition to a fleet of

2405-8963 Copyright © 2024 The Authors. This is an open access article under the CC BY-NC-ND license. Peer review under responsibility of International Federation of Automatic Control. 10.1016/j.ifacol.2024.09.261

to the occasional drivers. Their results provide evidence of the use of occasional drivers to reduce total cost.

This problem was extended in (Macrina et al., 2017) with a variant of the VRPOD including Time Windows (VRPODTW). The occasional drivers can make multiple deliveries, according to compensation and a split delivery policy. A variant of the green VRP with crowdshipping and time windows is introduced in (Macrina and Guerriero, 2018). The authors considered a mixed regular fleet composed of conventional combustion engine and electric vehicles, and the possibility to use occasional drivers. The objective was to reduce the cost of regular fleet fuel and energy consumption, and occasional drivers' compensation. Their results exhibit how the use of occasional drivers may complement the electric regular fleet, leading reduced polluting emissions.

This green initiative was extended in (Macrina et al., 2020) where the impact of using ODs on polluting emissions and costs, in a single objective approach for each objective was studied. The results show a sensitive reduction of CO2 emissions when more competitive compensation schemes are used for all ODs. Simoni et al. (2020) developped a simulation based approach to analyze environmental impacts of crowdshipping. It includes delivery routes, traffic and pollution. Their results exhibit the negative environmental impacts of crowdshipping in terms of generated emissions if the right transport mode is not used. Also, the authors point out the additional affectation of occasional drivers' tendency to execute dedicated delivery trips. Pourrahmani and Jaller (2021) reiterate the tendency of ODs to affect their normal routes, increasing vehicle use and generated emissions. They also mention that a way to secure the sustainable value in crowdshipping is to consider the use of sustainable modes that could replace the regular transportation modes based on fossil fuels.

According to our literature exploration, there is scarce development related to multi-objective approaches to crowdshipping extensions of VRPOD or VRPODTW. Also, current mathematical approaches only consider one type of vehicle for ODs and compensation. Studies generally restrict the ODs and over-simplify the CO2 emissions impact on the ODs route. Despite the multiples recommendations on sustainable vehicle use, no decision making tools have been proposed.

3. MATHEMATICAL MODEL

This problem considers ODs that can be located out of the depot, referred to as "out-store" ODs, to complement a regular vehicle delivery fleet. Specifically, the problem generalizes the participation of different numbers of ODs using different types of vehicles (fueled and non-fueled vehicles), for which the origin and destination are known and different. To encourage the use of sustainable transport modes, the compensation policy assigns higher compensation to the non-fueled type. For each type of vehicle, the speed, capacity, emissions factors are different. The time windows are considered for each client and for each OD final destination. The problem is referred to as the Bi-Objective Vehicle Routing Problem with Multi types of Occasional Drivers and Time Windows (BO-VRPMODTW).

3.1 Description

The problem is defined as follows. P is the number of available regular vehicles. T is the set of vehicle types to consider, and K_t is the set of available ODs of type t. Consider a directed graph $G = (N, A)$, with node set $N = C \cup s \cup O_t \cup V_t$, where C is the set of customers, s represents the depot. O_t represents the set of o_{kt} origins for the ODs of type t, and V_t is the set of v_{kt} destinations associated with the ODs of type t. Each node i in $C \cup$ v_{kt} ∪ o_{kt} has a hard time window defined as $[e_i, l_i]$. Each customer $i \in C$ has a demand a_i . Q^R , Q_{kt}^{OD} are the capacity values for regular vehicles and for $\overline{OD} k$ of type t respectively.

 SP^R, SP^{OD} represent average speed for regular vehicles and for ODs of type t respectively. E^R , E_{kt}^{OD} are the CO2/fuel conversion factor (kg CO2/L) considered for the regular vehicles and for the vehicles of the ODs of type t respectively. A represents the set of arcs. Each arc (i, j) in A has cost c_{ij} and distance $dist_{ij}$. The value γ represents the price per liter of fuel for regular vehicles. $c r min^R, c r min^{OD}$ represent the minimum values of fuel or energy consumption per distance unit if the vehicle is empty (L/km), and $crmax^R, crmax^{OD}_t$ are the maximum values of fuel or energy consumption per distance unit for regular vehicles and for ODs of type t respectively (L/km). Let ρ_t the compensation factor for ODs of type t.

Let x_{ij} be a binary variable that represents if a regular vehicle traverses the arc (i, j) , and r_{ij}^{tk} is a binary variable that indicates if the OD k of type t traverses the arc (i, j) . For each node $i \in N$, y_i represents the current load of the regular vehicle right after visiting the customer i and s_i is the arrival time of the regular vehicle to the customer i . Let w_i^{tk} be the current load of OD k of type t after visiting customer and f_i^{tk} indicates the arrival time of OD k of type t. Let tf_{ij}^R be the total fuel consumption if regular vehicle traverses arc (i, j) , related to the current load of the regular vehicle after visiting the customer *i*, and tf_{ij}^{ODtk} be the total fuel consumption if OD k of type t traverses arc (i, j) , related to the current load of the OD k of type t after visiting the customer *i*. Let β_{itk} be a binary parameter equals to 1 if OD k of type t can serve client in node i .

3.2 Formulation

$$
\min \sum_{i \in C \cup s} \sum_{j \in C \cup s} c_{ij} x_{ij} + \gamma \sum_{i \in C \cup s} \sum_{j \in C \cup s} t f_{ij}^R
$$

+
$$
\sum_{i \in C \cup s} \sum_{j \in C \cup s \cup v_{kt}} \sum_{t \in T} \sum_{k \cup K_t} \rho_t dist_{ij} r_{ij}^{tk}
$$

-
$$
\sum_{j \in C} \sum_{t \in T} \sum_{k \cup K_t} \rho_t dist_{o_{kt}v_{kt}} r_{sj}^{tk}
$$

$$
\min \sum_{i \in C \cup s} \sum_{j \in C \cup v_{kt}} \sum_{t \in T} \sum_{k \in K_t} E_t^{D} t f_{ij}^{B}
$$

+
$$
\sum_{i \in C \cup s} \sum_{j \in C s \cup v_{kt}} \sum_{t \in T} \sum_{k \in K_t} E_t^{D} t f_{ij}^{ODtk}
$$

-
$$
\sum_{j \in C} \sum_{t \in T} \sum_{k \in K_t} E_t^{D} c r \min_t^{D} dist_{o_{kt}v_{kt}} r_{sj}^{tk}
$$
(2)

$$
\sum_{j \in C \cup d} x_{ij} - \sum_{j \in C \cup s} x_{ji} = 0 \qquad \forall i \in C \tag{3}
$$

$$
\sum_{j \in C} x_{sj} - \sum_{j \in C} x_{js} = 0 \tag{4}
$$

$$
\sum_{j \in C} x_{sj} \le P \tag{5}
$$

$$
\sum_{j \in C \cup v_{kt}} r_{ij}^{tk} - \sum_{j \in C \cup s} r_{ji}^{tk} = 0 \quad \forall \ i \in C, \ t \in T, \ k \in K_t \tag{6}
$$

$$
\sum_{j \in C \cup v_{kt}} r_{sj}^{tk} - \sum_{j \in C \cup s} r_{j v_{kt}}^{tk} = 0 \qquad \forall \ t \in T, \ k \in K_t \tag{7}
$$

$$
\sum_{j \in C} r_{sj}^{tk} - r_{o_{kt}s}^{tk} = 0 \qquad \forall \ t \in T, \ k \in K_t \tag{8}
$$

$$
\sum_{h \in C \cup s} r_{hi}^{tk} \le \beta_{itk} \qquad \forall i \in C, \ t \in T, \ k \in K_t \tag{9}
$$

$$
\sum_{j \in C} r_{sj}^{tk} \le 1 \qquad \forall \ t \in T, \ k \in K_t \ (10)
$$

$$
y_j \le y_i - a_i x_{ij} + Q^R (1 - x_{ij}) \qquad \forall j \in C, \quad (11)
$$

$$
i \in C \cup s
$$

$$
w_{jtk} \le w_{itk} - a_i r_{ij}^{tk} + Q_{kt}^{OD} (1 - r_{ij}^{tk}) \qquad \begin{array}{l} \forall j \in C, \\ i \in C \cup s, \\ t \in T, \\ k \in K_t \end{array} (12)
$$

∀ j ∈ C,

$$
s_j \ge s_i + \frac{dist_{ij}}{SP^R} x_{ij} - M_1(1 - x_{ij}) \qquad \forall i \in C \cup s, \tag{13}
$$

$$
e_i \le s_i \le l_i \qquad \qquad \forall \ i \in C \ (14)
$$

$$
f_{jtk} \ge f_{itk} + \frac{dist_{ij}}{SP_t^{OD}} r_{ij}^{tk} \qquad \forall i \in C \cup s \cup o_{kt},
$$

$$
-M_1(1 - r_{ij}^{tk}) \qquad \qquad t \in T,
$$

$$
+ K_t \qquad \qquad t \in K_t
$$
 (15)

$$
f_{itk} \ge e_{v_{kt}} + \frac{dist_{ij}}{SP_{t}^{OD}} dist_{sj} \qquad \forall i \in C, t \in T, (16)
$$

$$
e_i \le f_{itk} \le l_i \qquad \qquad \forall i \in C \cup s \cup v_{kt} \tag{17}
$$

$$
tf_{ij}^{R} \geq cmin^{R} dist_{ij}
$$

+
$$
cmax^{R} \left(\frac{y_{j}}{Q^{R}}\right) dist_{ij} \qquad \forall i \in C \cup s,
$$

-
$$
-cmin^{R} \left(\frac{y_{j}}{Q^{R}}\right) dist_{ij} \qquad j \in C \cup s
$$

-
$$
-cmax^{R} dist_{ij} (1 - x_{ij})
$$
 (18)

$$
tf_{ij}^{ODtk} \geq c r min_{t}^{OD} dist_{ij}
$$

+
$$
c r max_{t}^{OD} \left(\frac{w_{i}^{tk}}{Q_{kt}}\right) dist_{ij} \qquad \forall i \in C \cup s \cup o_{kt} ,-c r min_{t}^{OD} \left(\frac{w_{i}^{tk}}{Q_{kt}}\right) dist_{ij} \qquad \begin{array}{l} \forall i \in C, \\ \xi \in T, \\ t \in T, \\ k \in K_{t} \end{array} \qquad (19)
$$

-
$$
c r max_{t}^{OD} dist_{ij} (1 - r_{ij}^{tk})
$$

$$
\sum_{j \in C \cup t} x_{ij} + \sum_{k \in K_t} \sum_{t \in T} \sum_{j \in C \cup s} r_{ji}^{tk} = 1 \qquad \forall i \in C \tag{20}
$$

$$
x_{ij} \in \{0, 1\} \qquad \forall (i, j) \in A \tag{21}
$$

$$
r_{ij}^{tk} \in \{0, 1\} \qquad \forall (i, j) \in A, k \in K_t, t \in T \tag{22}
$$

$$
0 \le y_i \le Q^R \qquad \qquad \forall \ i \in C \cup s \ (23)
$$

$$
s_i \ge 0 \qquad \qquad \forall \ i \ \in C \cup s \ (24)
$$

$$
0 \le w_i^{tk} \le Q_{kt}^{OD}
$$

\n
$$
\forall i \in C \cup s \cup v_{kt},
$$

\n
$$
k \in K_t,
$$

\n
$$
t \in T
$$
\n(25)

$$
f_i^{tk} \ge 0
$$
\n
$$
\forall i \in C \cup s \cup v_{kt},
$$
\n
$$
k \in K_t,
$$
\n
$$
t \in T
$$
\n(26)

$$
tf_{ij}^{ODtk} \leq c r max_t^{OD} dist_{ij} r_{ij}^{tk} \qquad \begin{array}{l} \forall i \in C \cup s \cup o_{kt}, \\ j \in C \cup s \cup v_{kt}, \\ t \in T, \ k \in K_t \end{array} (27)
$$

$$
tf_{ij}^{ODtk} \ge 0
$$
\n
$$
\forall i \in C \cup s \cup o_{kt},
$$
\n
$$
j \in C \cup s \cup v_{kt},
$$
\n
$$
t \in T, k \in K_t
$$
\n(28)

$$
tf_{ij}^R \ge 0 \qquad \qquad \forall i \in C \cup s, \quad (29) \qquad \qquad j \in C \cup s
$$

The objective function (1) represents the transportation cost. The terms represent respectively the cost associated with regular vehicles, the total fuel cost associated with regular vehicles, the cost of compensation of the ODs of type t , the cost for the original travel of the ODs of type t . The objective function (2) represents the CO2 emissions. It is composed of the CO2 emissions generated by regular drivers' travel, by ODs, and the one generated in the original travel by ODs.

Constraint (3)-(4) are the flow constraints for regular vehicles. Constraint (5) restricts the number of available regular vehicles. Constraints $(6)-(7)$ are the flow constraints for ODs. Constraint (8) specifies that all ODs making a delivery must go through the depot first. Constraint (9) indicates if OD k of type t can serve client in node i. Constraint (10) limits the number of departures from depot for each ODs of type t.

Constraint (11) represents the total load in the regular vehicles after visiting a customer. Constraint (12) is the total load for ODs of type t after visiting a customer. Constraints (13)-(14) represent the time windows accomplishment for regular vehicles. Constraints (15)-(17) represent the time windows constraints for ODs. Constraint (15) includes the M_1 number, defined as the maximum value between the customers and ODs final destinations time windows latest times l_i . Constraints (18)-(19) represent the total fuel consumption calculation for regular vehicles and ODs respectively. Constraint (20) guarantees that each customer is visited only once, by a regular vehicle or an OD. Constraints (21)-(29) represent decision variable domains.

4. COMPUTATIONAL EXPERIMENT

In this section the computational experiment executed to validate BO-VRPMODTW is presented. The problem was solved on 20 instances and compared with the VRPTW bi-objective results (which can be achieved by modifying the right-hand side of constraints (9) and (10) to 0). The model was implemented and solved using the ϵ -constraint approach minimizing the CO2 emissions and controlling the transportation cost, implemented in Python with Gurobi version 10.0.1, and run in a PC with an Intel 2.30 GHz processor and 32 GB of RAM. The parameters settings for all the experiments are presented in the table 1. The number of vehicles, capacity and speed are based on the structure presented in (Macrina et al., 2017). For the fuel or energy consumption and CO2 conversion factor, the values are based on the ones presented in (Muñoz-Villamizar et al., 2017 and (Ubeda et al., 2014).

Table 1. Experiment parameters

Type	Number		SP^{R}	$crmin^{n}$	$crmax^n$	E^{R}	c_{ij}
		Q_{kt}^{OD}	SP^{OD}	$crmin_{\tau}^{OD}$	$c\nu$	$E_{kt}^{\cal OD}$	ρ_t
Regular drivers	5	200	50	0.254	0.379	2.61	
ODs type 1	5	50	50	0.254	0.285	2.61	1.1
ODs type 2	$\overline{2}$	25	40	0.002	0.004		$1.2\,$

The remainder of this section presents the generation of instances, a comparison for all instances result, and the detailed results for two instances.

4.1 Generation of Instances

The instances used to check the proposed model are based on the Solomon VRPTW instances (see Solomon, 1987). For this case the clustered geographical distribution (C), and random geographical distribution (R) classes of customer locations were selected. A set of 10 clustered small instances and 10 random small instances were created, considering a total of 13 customers. For each instance, the origin and destination for the occasional drivers were generated randomly with a uniform distribution, according to the customers location coordinates. Also, the destinations time windows were randomly generated with a uniform distribution according to customers latest time windows.

4.2 All instances comparison

The summary results for all instances are presented. The comparison for each instance between the BO- VRPMODTW and VRPTW is presented in table 2, considering that the instance names correspond to the original Solomon reference. Specifically, the minimum and maximum cost and CO2 emissions values, number of solutions in the Pareto front (#SP), Pareto front total computational time for both problems, and hypervolume gap are included. For each instance, a normalized hypervolume is computed using as a reference point the maximum values of both objectives, increased by 10%, and the normalized values for cost and CO2 emissions of each solution in the Pareto front. The HV gap is the ratio of the BO-VRPMODTW hypervolume minus the VRPTW hypervolume, to the VRPTW hypervolume. In this case a 0.0% gap means no difference between BO-VRPMODTW and VRPTW fronts, and a higher value of gap implies that VRPTW front is dominated by BO-VRPMODTW front.

Table 2. Instances comparison

	BO-VRPMODTW				VRPTW				
Inst.		Lex optimal			Lex optimal				HV Gap
	Cost	CO ₂	$\#\mathrm{SP}$	Time(s)	Cost	CO ₂	$\#SP$	Time(s)	$(\%)$
	232.96	146.43							
C101	444.92	135.34	10	10.622	232.96	146.43	$\mathbf{1}$	0.062	550
	220.22	138.01							
C102	356.35	127.53	$\overline{4}$	46.330	220.22	138.01	1	2.695	423
	262.05	162.23			262.05	162.23			
C103	400.10	121.30	15	708.122	263.79	162.09	$\overline{2}$	0.677	193
	131.53	89.15			154.17	97.82			
C104	200.95	68.83	11	8386.268	154.72	96.58	3	942.421	750
	160.48	101.93							
C105	340.46	83.34	9	28.636	170.70	104.84	1	0.109	888
	132.89	90.31							
C109	199.78	69.21	$\overline{7}$	1148.846	154.40	96.86	1	7.478	1080
	227.50	140.30							
C201	389.00	126.00	8	52.451	227.50	140.30	$\mathbf{1}$	0.113	657
	219.51	137.23							
C202	258.30	110.38	$\overline{7}$	107.471	219.51	137.23	$\mathbf{1}$	0.265	381
	174.59	105.82							
C204	180.87	97.53	$\overline{4}$	2383.915	182.84	114.29	1	1098.741	8717
	220.09	138.36							
C208	389.58	125.10	10	13773.098	220.09	138.36	$\mathbf{1}$	70.318	425
	369.29	224.36							
R ₁₀₁	465.28	187.79	$\overline{7}$	2.416	417.95	247.52	$\mathbf{1}$	0.055	1381
	398.72	269.76			513.33	305.48			
R102	464.23	179.52	9	138.550	516.02	304.21	$\overline{2}$	0.391	7783
	247.86	153.28			340.46	208.11			
R110	408.97	97.19	19	1310.317	350.44	206.76	$\overline{2}$	13.170	1513
	371.09	233.25			417.47	254.75			
R111	514.70	173.09	14	352.972	420.25	253.78	$\overline{2}$	1.155	758
R112	249.97	152.85							
	378.84	128.89	11	654.509	276.99	173.35	1	265.056	963
	315.69	202.23			437.17	267.25			
R ₂₀₁	431.77	129.15	11	21.728	441.55	263.34	$\overline{2}$	0.152	6508
R ₂₀₂	284.32	173.12	8	75.313	347.18	215.69	$\sqrt{3}$	1.127	4809
	336.80	165.36			353.25	214.20			
R ₂₀₉	312.90	187.95			357.73	225.44			
	400.09	164.85	$\overline{4}$	11.476	364.69	220.32	6	2.385	849
R210	311.66	198.91	$\overline{7}$		347.27	214.23	$\overline{2}$	0.751	1624
	352.76	146.52		52.069	341.50	219.18			
R211	323.15	205.44			323.15	205.44			541
	480.20	158.48	10	368.190			1	11.285	

For all the instances results, the solutions hypervolumes obtained in the proposed model are significantly larger than the ones obtained with the VRPTW. In 5 clustered instances (C101, C102, C201, C202, and C208) and 1 random instance (R211), the original solutions obtained in VRPTW are also efficient for BO-VRPMODTW, concerning the cost. For the other instances, all the original VRPTW solutions are dominated by the BO-VRPMODTW Pareto front. According to this, it can be implied that for a clustered class, there is a relevant participation of a regular fleet in terms of minimizing total cost, considering the ODs compensation. However, from the emissions perspective, the minimum value of CO2 is obtained in the BO-VRPMODTW. For random class, there is a higher participation of ODs of both types in terms of minimizing total cost and emissions.

Fig. 1. Pareto front comparison - Instance C104 - 13 clients

Also, the proposed problem allows to obtain a higher number of possible solutions to generate an expected tradeoff between the cost and emissions minimization including different types of ODs, in contrast to only considering a regular fleet, which for clustered class normally presents only 1 feasible solution, and for random class an average of 2 feasible solutions for both objectives. The difference of computational time between the problems was expected and can be explained considering that the single-objective approach of the BO-VRPMODTW solved in each iteration of the ϵ -constraint is more complex than the VRPTW, thus the solving is more time consumming. Also, since the BO-VRPMODTW is a bi-objective problem, several solutions are sought and the solving time increases with the number of these solutions.

In clustered instances, BO-VRPMODTW solutions include on average 2 regular vehicles, 1 OD of type 1, and 2 ODs of type 2, giving the higher load amount to regular vehicles and ODs of type 2. This allows to confirm how the inclusion of ODs with sustainable vehicle options, even with a higher compensation than ODs with fossil fuel vehicles, could be beneficial to support a regular fleet to attend deliveries in clustered locations. For random instances, the problem solutions normally include an average of 2 regular vehicles, 3 ODs of type 1, and 2 ODs of type 2, giving a similar load amount to regular vehicles, ODs of type 1, and ODs of type 2. For random locations, the results allow to confirm how the inclusion of ODs in general (type 1 or 2), could generate a representative benefit in terms of cost and emissions minimization, not only as a complement, but having a comparable participation to regular drivers.

4.3 Detailed results on two instances

In this part, we focus on one clustered and one random instance, where VRPTW solutions are fully dominated by BO-VRPMODTW solutions. The clustered instance is C104. The Pareto front results comparison between the two approaches is presented in Fig. 1, including the reference point for hypervolume calculation.

For this instance, in the VRPTW approach, a total of 3 feasible solutions are obtained. All the solutions in this approach involve the use of 2 regular drivers. For BO-VRPMODTW, a total of 11 feasible solutions are obtained. On average, the solutions include 1 regular vehicle, 3 ODs of type 1, and 2 ODs of type 2 are used.

Fig. 2. Load carried by type - Instance C104 - 13 clients

Fig. 3. Pareto front comparison - Instance R209 - 13 clients

According to the results it is stated that BO-VRPMODTW outperforms the VRPTW in the bi-objective perspective. ODs activation guarantees a reduction in the total CO2 emissions generated. Also, for this instance, if the goal is minimizing the total cost, the ODs activation allows a reduction in the total value. Fig. 2 presents the percentage of load carried by each type of vehicle, according to the normalized value of cost for each solution in BO-VRPMODTW, to verify the evolution between value 0 (lex optimal cost) to value 1 (lex optimal CO2).

It can be observed that the higher load mobilization for all the solutions corresponds to ODs of type 1 with an average of 52%. Also, it is stated how to generate a reduction of the CO2, the proportion of load assigned to ODs of type 2 evolves from 0% to 15%, with an average of 12%. Finally, for regular vehicles, an average of 36% of the load is carried. This implies that in this case, the most representative type in the bi-objective condition corresponds to ODs with fueled vehicles.

The random instance is R209, for which the Pareto front comparison is presented in Fig. 3. For this instance, from the VRPTW approach, a total of 6 feasible solutions are obtained. This involve the use of 3 regular drivers on average. For BO-VRPMODTW a total of 4 feasible solutions are obtained. On average 2 regular vehicles, 1 ODs of type 1 and 2 ODs of type 2 are used.

For this case, the BO-VRPMODTW also outperforms the VRPTW in the bi-objective perspective, even considering the reduction of the number of available solutions. The ODs activation allows to minimize the total cost and

Fig. 4. Load carried by type - Instance R209 - 13 clients

reduce the total CO2 emissions limits. Fig. 4 presents the percentage of load carried by each type of vehicle for this instance, according to the normalized value of cost for each solution in BO-VRPMODTW. It is observed that for this instance, the higher percentage in load mobilization corresponds to regular driver which on average corresponds to 75%. For ODs, the average for type 1 is 15%, and for type 2 is 10%. In this case, ODs represent a feasible complement for the bi-objective approach, but have as main type the regular fleet.

5. CONCLUSIONS

We proposed a bi-objective crowdshipping problem optimizing both the cost and CO2 emissions, referred to as the Bi-Objective Vehicle Routing Problem with Multi types of Occasional Drivers and Time Windows (BO-VRPMODTW), generalizing the participation of "out store" ODs using fueled and non-fueled vehicles, having a higher the compensation policy for non-fueled type.

For the BO-VRPMODTW, there is good evidence to consider as good the trade-off from a bi-objective perspective, including cost and CO2 emissions, considering the possibility of obtaining a wider range of solutions to increase, decrease, or control both objectives, according to possible business interests. The CO2 emissions reduction reflects positively the use of ODs for deliveries, depending on ODs availability, type, distance to clients, and vehicle capacity.

In random instances, as a deterministic approach, there is a higher use of ODs in both types (fueled and non-fueled) to decrease the assignation of load in Regular vehicles, in terms of reducing CO2 and controlling transportation costs. In clustered instances, there is a higher utilization of regular vehicles, considering the client's grouping, even from a CO2 reduction perspective. However, OD intervention could be considered as a complementary approach, mainly with those who can use a sustainable vehicle. There is initial evidence to consider as good, to include a higher incentive for ODs that use more sustainable modes (nonfueled). In both clustered and random instances, it is stated the use and assignation of ODs with sustainable modes guarantee a decrease in CO2 emissions.

Future works should consider different methods (exact or approximate) to scale up the solution approaches for bigger instances in a bi-objective context. Also, to analyze the inclusion of a third objective, to expand the sustainability

dimensions in the ODs types activation. Other possible approach could be to define multiple availability slots between ODs types, in a deterministic or probabilistic approach, to analyze selection and probability to complement a delivery scheme. Finally, to include an online perspective to the problem.

REFERENCES

- Archetti, C., Savelsbergh, M., and Speranza, M.G. (2016). The Vehicle Routing Problem with Occasional Drivers. European Journal of Operational Research, 254(2), 472– 480. doi:10.1016/j.ejor.2016.03.049.
- de Oliveira Leite Nascimento, C., Gatta, V., and Marcucci, E. (2023). Green Crowdshipping: Critical factors from a business perspective. Research in Transportation Business and Management, 51. doi: 10.1016/j.rtbm.2023.101062.
- Elsokkary, N., Otrok, H., Singh, S., Mizouni, R., Barada, H., and Omar, M. (2023). Crowdsourced last mile delivery: Collaborative workforce assignment. Internet of Things (Netherlands), 22. doi: 10.1016/j.iot.2023.100692.
- Macrina, G., Di Puglia Pugliese, L., and Guerriero, F. (2020). Crowd-shipping: A new efficient and eco-friendly delivery strategy. In Procedia Manufacturing, volume 42, 483–487. Elsevier B.V. doi: 10.1016/j.promfg.2020.02.048.
- Macrina, G., Di Puglia Pugliese, L., Guerriero, F., and Laganà, D. (2017). The Vehicle Routing Problem with Occasional Drivers and Time Windows. In Springer Proceedings in Mathematics and Statistics, volume 217, 577–587. Springer New York LLC. doi:10.1007/978-3- 319-67308-0 58.
- Macrina, G. and Guerriero, F. (2018). The Green Vehicle Routing Problem with Occasional Drivers. In AIRO Springer Series, volume 1, 357–366. Springer Nature. doi:10.1007/978-3-030-00473-6 38.
- Muñoz-Villamizar, A., Montoya-Torres, J.R., and Faulin, J. (2017). Impact of the use of electric vehicles in collaborative urban transport networks: A case study. Transportation Research Part D: Transport and Environment, 50, 40–54. doi:10.1016/j.trd.2016.10.018.
- Pourrahmani, E. and Jaller, M. (2021). Crowdshipping in last mile deliveries: Operational challenges and research opportunities. doi:10.1016/j.seps.2021.101063.
- Simoni, M.D., Marcucci, E., Gatta, V., and Claudel, C.G. (2020). Potential last-mile impacts of crowdshipping services: a simulation-based evaluation. Transportation, 47(4), 1933–1954. doi:10.1007/s11116-019-10028-4.
- Solomon, M.M. (1987). Algorithms for the Vehicle Routing and Scheduling Problems with Time Window Constraints. Operations Research, 35(2), 254–265. doi: 10.1287/opre.35.2.254.
- Strulak-Wójcikiewicz, R. and Wagner, N. (2021). Exploring opportunities of using the sharing economy in sustainable urban freight transport. Sustainable Cities and Society, 68. doi:10.1016/j.scs.2021.102778.
- Ubeda, S., Faulin, J., Serrano, A., and Arcelus, F.J. ´ (2014). Solving the green capacitated vehicle routing problem using a tabu search algorithm. Lecture Notes in Management Science, 6, 141-149. URL www.tadbir.ca.