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Adrien J Mourey, Alexandre Carrara, Thomas Shea, Fidel Costa Rodriguez, Marc-Antoine Longpré. The influence of olivine settling on the formation of basaltic cumulates revealed by micro-tomography and numerical simulations. Journal of Volcanology and Geothermal Research, 2024, 449, pp.108051. 10.1016/j.jvolgeores.2024.108051. hal-04772798

HAL Id: hal-04772798 https://hal.science/hal-04772798v1

Submitted on 8 Nov 2024

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2	tomography and numerical simulations				
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16	Abstract				
17	The speed at which crystals settle in magmatic reservoirs affects the solidification rate of magmas and				
18	their differentiation. Despite extensive prior work on the subject, most of our quantitative				
19	understanding of the process is still restricted to treating crystals as spherical particles and does not				
20	address the geometric complexities of natural crystals. Here, we use three-dimensional (3D) X-ray				
21	microcomputed tomography (X-µCT) observations on olivine crystals from Kīlauea Volcano (Hawaiʻi)				
22	to document their highly intricate and variable geometries, and the textural growth relationships				
23	between the olivine crystals and their inclusions (melt, spinel, and fluid/vapor bubbles). Olivine crystals				
24	generally have clustered polyhedral or skeletal shapes, which reflect variable magmatic conditions (or				
25	growth rates) during their formation. The cumulative presence of spinel, melt, fluid, and vapor				
26	inclusions affects the density of the host crystals by up to 6% relative, and thus plays a limited role on				
27	modifying crystal settling rate. In contrast, the overall crystal shape plays a major role. We performed				
28	numerical simulations employing a finite element method to investigate the effect of crystal				
29	morphology on settling rate and the evolution of the particle volume fraction in a magmatic convective				
30	layer. We show that for all olivine geometries investigated, the settling velocity is highest when the				

31 long axis of the crystal is aligned with the flow direction of the melt. Increasing the aspect ratio of the 32 olivine tends to decrease its settling velocity and results in an increase in the influence of its 33 orientation on the terminal velocity (U_T) . Extrapolation of the simulation results to variable particle 34 volume fractions (ϕ = 0-0.5) indicates high crystal settling rates (U_T = ~9.7 x 10⁻⁶ – 1.4 x 10⁻⁵ m/s) that 35 are used to estimate the timescales for the formation of olivine cumulates in natural melt-dominated 36 basaltic systems. The formation of olivine cumulates is therefore rapid, potentially leading to the 37 accumulation of a crystal layer at the bottom, where the frictional contacts between the crystals exert a 38 rheological lock-up acting against further convection. Crystal accumulation in the locked layer 39 (parametrized with the solid/liquid volume ratio in the reservoir) is a function of the reservoir size and 40 crystal fraction, and takes a few years in small reservoirs (less than 1 km thick) and a few decades in 41 larger reservoirs (several kms thick). We propose a calibration of olivine suspension timescales for 42 mafic magma reservoirs (based on the knowledge of the particle volume fraction, reservoir height, and 43 olivine morphology). This calibration is used to estimate the rate of cumulate build-up, and can help 44 interpret crystal size distributions in the framework of crystal suspension times. 45 46 **Keywords** 47 Olivine; crystal settling; crystal morphology; X-ray microcomputed tomography; numerical simulations 48 49 Highlights 50 Solidification of a basaltic reservoir strongly depends on the settling rate of olivine ٠ 51 • Olivine terminal velocity is highest when the crystal long axis is aligned with the melt flow. 52 Inclusions in olivine play a limited role on modifying crystal settling rate. ٠

• Crystal accumulation in mafic systems takes a few years to a few decades.

54

55 1. Introduction

56 Crystal settling has been considered a ubiquitous process in magma reservoirs for a long time (Murata

and Richter, 1966). Crystal settling is thought to control the mode of solidification of magmas on Earth

58 (Martin and Nokes, 1988; Koyaguchi et al., 1990; Pankhurst et al., 2018a) and in planetary magma

59 oceans (Elkins-Tanton, 2012). Quantifying the rate at which magma reservoirs solidify is essential for

60 the understanding of their chemical differentiation through time. Differentiation of a cooling magma is a

61 mediated process by crystal nucleation and growth or dissolution, settling and reentrainment (by 62 magma replenishment or assimilation). Crystal growth rates in basaltic magmas are relatively well 63 quantified (e.g., Jambon et al., 1992; Arzilli et al., 2015; Mourey and Shea, 2019) and the 64 reentrainment of negatively buoyant particles (entrainment of grains in convective layers) has been addressed experimentally (Solomatov et al., 1993a; Lavorel and Le Bars, 2009) and theoretically 65 66 (Solomatov and Stevenson, 1993b). In most cases, the accumulation of crystal layers at the bottom of 67 mafic reservoirs involves growth or reprecipitation of olivine crystals while in suspension in the melt, 68 followed by mechanical settling, compaction through pressure, dissolution at grain contacts, and 69 expulsion of the interstitial melt (e.g., Schmidt et al., 2012; Holness et al., 2017). Experimental studies 70 have previously reproduced textures of olivine-rich layers (Schmidt et al., 2012), but the influence of 71 crystal shape on settling remains poorly quantified.

72

73 The shape of natural olivine crystals is highly variable (e.g., equant, elongated, tabular, skeletal, 74 hopper, dendrite) and is related to undercooling, cooling rate and the melt composition (e.g., 75 Donaldson, 1976; Faure et al., 2003; Mourey and Shea, 2019). The well-faceted, polyhedral, tabular 76 and hopper morphologies have been associated with relatively low undercooling ($-\Delta T < 25^{\circ}$ C; Faure et 77 al., 2003; Mourey and Shea 2019, where $-\Delta T$ is the temperature difference between the olivine 78 liquidus and a temperature of interest below the liquidus), whereas skeletal and dendritic crystals are 79 formed at moderate to high undercooling ($-\Delta T > 25^{\circ}C$; Faure et al., 2003; Mourey and Shea 2019). 80 Polyhedral crystals were initially assumed to crystallize at near-equilibrium conditions (Pearce, 1984) 81 and in a concentric "tree-ring" fashion (e.g., Clark et al., 1986). However, morphological remains of an 82 early rapid growth (e.g., stepped hopper cavities) are commonly observed in polyhedral olivine 83 phenocrysts (e.g., Welsch et al., 2013), challenging the assumption of near-equilibrium, low 84 undercooling conditions. Instead, polyhedral olivine phenocrysts are considered to have an initial rapid 85 growth history, forming a skeletal olivine framework that is progressively infilled as undercooling and 86 growth rates decrease (e.g., Welsch et al., 2013; Mourey and Shea, 2019; Wallace et al., 2021). 87

88 Olivine is the most abundant mineral in Hawaiian eruptions, and the only mineral (along with Cr-spinel) 89 within active summit reservoirs (e.g. Thornber et al., 2015). Moreover, both olivine and spinel are the

90 first minerals to crystallize in basaltic melts with >7 wt.% MgO (Roeder et al., 2001). Unsurprisingly,

91 spinel inclusions are common in olivine crystals.

92 In this study, we demonstrate how modern X-ray microcomputed tomography (X-µCT) scans of olivine 93 crystals can provide a wealth of new information on the three-dimensional (3D) distribution of melt 94 inclusions, vapor bubbles, and spinels, in addition to the true 3D shape of crystals. The complexities of 95 the inclusions network trapped in the crystals can help document crystal growth histories and thermal 96 (undercooling) conditions.

97 We collected high-resolution X- μ CT scans of three populations of olivine crystals from the 1820 98 Golden Pumice eruption (unit K1 from the Keanakāko'i Tephra) at Kīlauea Volcano (Hawai'i). We 99 document the internal complexities (melt inclusion, vapor bubble and spinel fractions) of well-faceted 100 polyhedral crystals and more skeletal crystals, and interpret those complexities in terms of crystal 101 growth conditions. Using numerical simulations, we test how different olivine morphologies affect 102 settling velocities, with implications for the timescales of olivine-rich mush and dunite cumulate 103 formation. We quantify how the volume fraction of inclusions impacts a crystal's density and terminal 104 velocity. To investigate the influence of crystal morphology on settling, realistic crystal morphologies 105 identified with X-µCT scans are used to define initial crystal meshes with equal volumes and mass. 106 The meshes are then integrated into numerical simulations of melt flow around the crystal employing 107 the finite element method. The simulations explore the influence of the orientation of olivine crystals 108 with the flow direction of the melt and the influence of their shape on the settling velocities. These 109 velocities are then used to estimate settling timescales as a function of the crystal fraction and the 110 reservoir size. Those timescales bring important new constraints on the rates at which cumulates and 111 mush piles may form in mafic reservoirs, and can help petrologists better interpret crystal population 112 characteristics (e.g. size distributions) in the light of suspension and accumulation rates.

113

114 2. Methods

115 2.1. Sample description

We used a sample from the Unit K1 (formerly Golden Pumice) eruption that occurred around 1820
C.E. during the explosive Keanakāko'i Tephra eruptive period at Kīlauea (Fig.1; Swanson et al., 2012).
The eruption consisted in high lava fountains that produced fall deposits comprising chiefly rapidly
cooled golden pumice with sparse lithic materials. The sample is glassy with 6.8 – 9.1 wt.% MgO in

120 the glass (Lynn et al., 2017) and contains different olivine populations (Fo₈₀₋₈₉ (Fo = Mg/[Mg+Fe] in

121 mol.%; Lynn et al. 2017; Mourey et al., 2022). No other phenocryst phases were found.

122

123 2.2 X-ray micro-tomography

124 In volcanology, X-µCT has been used to measure the 3D shape and distribution of vesicles in volcanic 125 rocks (e.g., Polacci et al., 2006), quantify bubbles nucleation and growth in multiphase systems 126 (Oppenheimer et al., 2021), and characterize the morphology and chemical zoning of olivine crystals 127 (Pankhurst et al., 2014; 2018b; Mourey and Shea, 2019). Traditionally, the interpretation of mineral 128 textures is based on 2D images obtained with optical and electron microscopy. 2D images may lead to 129 inaccurate or erroneous interpretations when addressing the complexities of 3D morphologies (e.g., 130 Mourey and Shea, 2019). The extrapolation to 3D from 2D images can be made by time-consuming 131 and destructive techniques involving serial sectioning and grinding method (e.g., Byron et al., 1995; 132 Daniel and Spear, 1999; Mock and Jerram, 2005). This method however results in low resolution in 133 the direction perpendicular to the observed plane, and most of the material is unfortunately destroyed 134 during polishing. Therefore, only partial records of the complexities of a 3D crystal are observed in 2D 135 sections. Recent advances in X-ray computed microtomography (X-µCT) during the last three 136 decades better allow accessing real 3D information. This technique affords proper interpretation of the 137 spatial relationships between textural and, sometimes, geochemical characteristics. X-µCT is non-138 destructive and high spatial resolutions (sub-micron) can be attained.

139

140 The 1820 C.E. golden pumices were first gently crushed with a mortar and pestle, and a 141 representative variety of olivine morphologies were hand-picked for X-µCT scans. The crystals were 142 coated with glass and, to make crystal faces more apparent, they were immersed in a 1 normal HF 143 solution and cleaned (e.g., Lynn et al., 2017). Crystals were then mounted on carbon tape, carbon 144 coated, and imaged with a JEOL-8500 field emission gun electron microprobe at the University of 145 Hawai'i. A selection of crystals (n=13) were scanned at the X-µCT facility at the University of Austin 146 Texas using an X-ray tube-based scanner (cone-beam geometry, Xradia MicroXCT-400). Each crystal 147 was individually mounted on the rotating sample stage for X-µCT scans. For each tomographic scan, 148 1261 X-ray projections were acquired with a constant angular step over a 360° rotation. The effective 149 pixel size of the images varied between 2.19 and 2.83 µm for a sample-to-detector distance between 8 150 and 54 mm. A maximum beam energy of 70 keV was used for most of the olivine scans but was set at 151 40 or 50keV for some rare crystals showing more beam artifacts (all conditions are reported in 152 supplementary material). 3D reconstructions were done iteratively (e.g., adjustment of beam 153 hardening, filter smooth). The images were imported in the ImageJ software to improve the contrast 154 and brightness. For each scan, a brightness threshold is attributed for each phase (olivine, spinel, melt 155 and vapour) in the Avizo[™] software. Each image is then checked individually for additional 156 segmentation corrections. After segmentation, melt and vapour renderings were smoothed during the 157 surface reconstruction process using the filter packages in Avizo[™] software. Textural measurements 158 (size and volume) of the different phases (olivine, melt inclusions, vapor bubbles, spinels) were done 159 using the Avizo[™] software. The accuracy of the X-µCT technique to retrieve the phase volume (and 160 number) is higher than classical techniques using point counting in transmitted light on 2D 161 petrographic thin sections. For instance, most olivine crystals in a typical thin section are off-center 162 intersected (Shea et al., 2015), and so measurements from thin sections generally underestimate the 163 actual maximum dimensions of the crystals and their numbers.

164

165 2.3. Numerical modeling

Next, we aimed to use morphological constraints gleaned from 3D scans of natural olivine to
investigate the influence of olivine morphology on rates of crystal settling in a basaltic melt. We
simulated the flow of melt around crystals numerically, using morphologies representative of the range
observed in 3D scans.

170 The equation of motion of a crystal suspended in melt (Carrara et al. 2019) may be written as:

171
$$\frac{dv}{dt} = \frac{\Delta\rho}{\rho_c} g - \frac{F_D}{m}$$
(1)

where ρ_c is the density of the crystal, $\Delta \rho$ is the density contrast between the crystal and the surrounding melt ($\Delta \rho = \rho_c - \rho_l$, ρ_l being the density of the melt), **g** is the gravitational acceleration vector, *m* is the mass of the crystal, and the drag force imposed by the melt on the crystal F_D . On the right-hand side of Eq. (1), the first term comprises both the gravitational and Archimedes' forces (reduced weight), while the second term corresponds to the drag force imposed by the melt on the crystal, F_D divided by the crystal mass. The drag force can be further decomposed as the product of that of an isolated crystal and a voidage function (Di Felice, 1994):

179
$$\boldsymbol{F}_{\boldsymbol{D}} = \boldsymbol{F}_{\boldsymbol{D},\boldsymbol{0}} f(\phi)$$
 (2)

180 with $F_{D,0}$ the drag force of an isolated crystal and ϕ the voidage function defined as:

181
$$f(\phi) = (1 - \phi)^{-\beta}$$
 (3)

where ϕ is the solid volume fraction around an isolated crystal, and β is the coefficient of momentum exchange between the crystal and the melt (β increases with crystal size and particle volume fraction; see supplementary material). The coefficient of momentum exchange can be further decomposed as (Di Felice, 1994):

186
$$\beta = 3.7 - 0.65 \exp\left(-\frac{[1.5 - log_{10}(\text{Re})]^2}{2}\right)$$
 (4)

187 which gives the following expression for the drag force:

188
$$F_D = F_{D,0}(1-\phi)^{-\left(3.7-0.65e^{\frac{-(1.5-log_{10}\text{Re})^2}{2}}\right)}$$
 (5)

where *Re* is the particle Reynolds number. β_0 depends on the viscosity and density of the melt, and the shape, size, and orientation of the crystal. The second part of the right-hand side of Eq. (5) is a correction that depends on the solid volume fraction (Di Felice, 1994). The particle Reynolds number (He and Tafti, 2018) is:

193
$$Re = \frac{d_{eq} \| \boldsymbol{v} - \boldsymbol{u} \| \rho_l}{\eta}$$
(6)

where d_{eq} is the diameter of a sphere having the same volume as the crystal, and η is the dynamic viscosity of the melt.

196 For the conditions relevant to crystals settling in melt, *Re* < 0.1, such that Eq. (5) can be simplified as:

197
$$F_D = F_{D,0}(1-\phi)^{-3.7}$$
 (7)

The influence of the shape and orientation of the crystal on $F_{D,0}$ may be isolated from the influence of its size and properties on the liquid phase by expressing it as a function of the drag coefficient, C_D (Zastawny et al. 2012; Sanjeevi et al. 2018):

201
$$\boldsymbol{F}_{\boldsymbol{D},\boldsymbol{0}} = \frac{1}{2} C_D A \rho_l |\boldsymbol{v} - \boldsymbol{u}| (\boldsymbol{v} - \boldsymbol{u})$$
 (8)

with *A* representing the cross-sectional area of the crystal, *u* is the velocity vector of the melt, *v* is the velocity vector of the crystal. The drag force of an isolated crystal for which the cross-sectional area is assumed to be that of an equivalent sphere of diameter d_{eq} such that $A = \frac{\pi}{4} d_{eq}^2$ is defined as:

205
$$\boldsymbol{F}_{\boldsymbol{D},\boldsymbol{0}} = \frac{\pi}{8} C_D \rho_l d_{eq}^2 |\boldsymbol{v} - \boldsymbol{u}| (\boldsymbol{v} - \boldsymbol{u})$$
(9)

206 C_D depends on the density and viscosity of the liquid, the size of the particle, the shape of the particle, 207 and on the relative velocity between the flow and the particle. In the viscous regime, when Re<1 (almost 208 always the case for magmas), C_D is proportional to Re^{-1} (Sanjeevi et al. 2018) and is expressed as:

$$209 \quad C_D = \frac{\xi}{Re} \tag{10}$$

where ξ is a coefficient that depends on the shape and orientation of the particle. When the crystal reaches its terminal settling velocity, U_T, the drag force equals the reduced weight of the particles such as:

213
$$\frac{\Delta\rho}{\rho_c}\boldsymbol{g} = \frac{F_D}{m}$$
(11)

214 Inserting Eqs. 7 & 9 into Eq. (11) gives:

215
$$\frac{\Delta\rho}{\rho_c} \boldsymbol{g} = \frac{\pi C_D \rho_l d_{eq}^{2} (1-\phi)^{-3.7} |\boldsymbol{v}-\boldsymbol{u}| (\boldsymbol{v}-\boldsymbol{u})}{8m}$$
(12)

216 Inserting Eqs. (6 & 10) into Eq. (12):

217
$$\frac{\Delta \rho}{\rho_c} g = \frac{\pi \xi \eta d_{eq} (1-\phi)^{-3.7}}{8m} U_T$$
(13)

218 which gives the following expression for U_T after balancing the forces:

219
$$U_T = \frac{8\Delta\rho gm}{\pi\xi\rho_c\eta d_{eq}(1-\phi)^{-3.7}}$$
 (14)

where *g* is the magnitude of *g*. Increasing the crystal volume fraction decreases the permeability of the suspension and increases the velocity and tortuosity of the flow of liquid in the intergranular spaces, which in turn increases the drag force and decreases the settling velocity (Carrara et al., 2019).

223 To determine the shape and orientation factor, ξ , we conducted numerical simulations of the flow of the 224 melt around the crystal and computed the total force applied by the melt on the surface of the crystal. 225 We simulated the flow of melt around single crystals using the software MIGFLOW (Constant et al., 226 2018), which solves the Navier-Stokes equations for an incompressible liquid employing a finite element 227 method. To generate a tetrahedral mesh around the crystal, we employed the software GMSH 228 (Geuzaine and Remacle, 2009). The computational domain is rectangular with the crystal located at its 229 center (Fig. 2a). The melt is injected at the base of the domain at constant velocity, Uinj, and can flow 230 outside the domain thanks to an outflow at constant pressure located atop. The sides of the domain are 231 free-slip walls and the surface of the crystal is a non-slip wall. Simulations are performed with no gravity 232 so that the force generated by the hydrostatic pressure gradient (i.e., the Archimedes' force) is null and 233 does not influence the estimation of ξ .

We computed the total drag force applied to the crystal by the melt, F_D , by summing the contributions of the liquid force on all the element faces located at the surface of the crystal (Fig. 2b). The integration of the total drag force may be written as (Zastawny et al. 2012):

237
$$\boldsymbol{F}_{\boldsymbol{D}} = \int_{S} (-p\boldsymbol{n}_{\boldsymbol{s}} + \tau) \, dS \tag{15}$$

where *p* is the melt pressure at the surface of the crystal (initially equal to 0), τ is the viscous stress tensor, **n**_s is the outward-pointing normal vector of the surface of the crystal, and *dS* is the incremental area. *p* is positive on the surface facing the flow and is negative on the faces on the other side of the crystal. The viscous stress is calculated as:

242
$$\tau = \eta \frac{\partial u^t}{\partial n_s}$$
 (16)

where u^t is the tangential velocity of the melt to the surface of the crystal, and $\partial u^t / \partial n_s$ is the gradient of the tangential velocity along n_s . The shape and orientation factor of the isolated crystal is then calculated using a combination of Eq. (9) and Eq. (10):

$$246 \quad \xi = \frac{8|F_D|}{\pi \eta d_{eq} U_{inj}} \tag{17}$$

247 Three different characteristic olivine morphologies were tested, with variable aspect ratios along the 248 three crystallographic axes: a- and c-elongated crystals, as well as an equant crystal. The choice of 249 these morphologies is partly based on previous experimental studies and natural olivine crystals 250 (Donaldson, 1976; Welsch et al., 2013; Mourey and Shea, 2019; Gordeychik et al., 2020), including 251 those imaged in this study. All the crystal geometries were generated using MATLAB and have the same 252 volume (\sim 4.19 mm³, which is equivalent to a 1-mm radius sphere). For each crystal morphology, we 253 performed three simulations with one of the crystallographic axes aligned with the flow direction of the 254 melt. For all the simulations and computations of settling velocity, we used the same physical properties 255 for the melt and crystal (see Table 1). The ability of the numerical model to constrain settling velocities 256 was validated by comparing the terminal velocity of a sphere using our numerical model and using the 257 Stokes velocity (relative error of 0.89%; see supplementary material).

258

259 3. Results

260 **3.1. 3D textures of Keanakāko'i Tephra olivine**

261 The Keanakāko'i Tephra (unit K1) contains a large variety of olivine morphologies (Table 2 and Fig.3),

262 which were classified in three morphological populations:

(1) Clustered polyhedral crystals are elongated along the *a*- or *c*-axis (4 clusters analyzed) and have
the largest olivine grains (>2 mm; Fig. 3a). The complex morphology of these crystals is evaluated
using the surface-area to volume (SA:V) ratio, measured by Avizo[™]. Clustered polyhedral crystals
have low SA:V values between 1 mm⁻¹ and 2 mm⁻¹. The clusters analyzed consist in 4 to 7 principal
olivine phenocrysts (>500 µm), with up to 20 additional microphenocrysts- to microlite-sized crystals.
Individual phenocrysts within polyhedral clusters have a more equant shape (relative to the other
crystal morphologies discussed below) and large SA:V ratios (up to 20 mm⁻¹).

271 (2) Clustered skeletal crystals (2 clusters analyzed; Fig. 3b) are elongated along the *a*-axis and 272 connected by melt inclusions that typically track the direction of primary and secondary growth 273 branches (Fig. 3b). These crystals have high SA:V ratios between 7 mm⁻¹ and 14 mm⁻¹. Spinel 274 inclusions are concentrated near the olivine crystal edges. The crystal morphology and the abundance 275 of melt inclusions suggests that clustered skeletal olivine formed at moderate-to-high undercooling 276 conditions (i.e., $-\Delta T = 40-60^{\circ}C$; Mourey and Shea, 2019).

277 (3) Single skeletal crystals (7 crystals analyzed) are generally elongated along the *a*-axis (Fig. 3c).
278 They are characterized by small, elongated melt inclusions (<50 µm) that are fully enclosed and not

connected to vapor bubbles. Larger melt inclusions (up to 400 µm) usually form a tubular melt network
that wraps vapor bubbles from both sides of the olivine crystals and may be open to the olivine surface
(Fig. 3c). Spinel inclusions are only observed near the crystal edges. These crystals have medium

282 SA:V values between 2 mm⁻¹ and 6 mm⁻¹. Similar to the clustered skeletal crystals, single skeletal

283 crystals likely formed at moderate-to-high undercooling conditions (i.e., $-\Delta T = 40-60^{\circ}C$).

284

285 3.1.1. Volume of melt, vapor bubble and spinel inclusions

The volume fraction of melt inclusions (reported in the supplementary material) varies from 3.6 to 22.1 vol.% in the single and clustered skeletal crystals (Fig. 4), but it is much smaller in the polyhedral clusters (between 0.45 and 1.4 vol.%; Fig. 4). Spinel makes up 0.3 - 1.4 vol.% of the total crystal volume. It is mostly located on the edges of skeletal crystals, and in both the cores and rims of polyhedral clusters (Fig. 3a). The volume occupied by vapor bubbles is usually low in polyhedral crystals (0 to 0.15 vol.%), medium in skeletal clusters (1.1 to 1.8 vol.%) and highly variable in single skeletal olivine crystals (0.24 to 4.8 vol.%). The vapor bubbles are generally attached to melt 293 inclusions (but some small bubbles are isolated as fluid inclusions as in k1820-ol8A; see

supplementary material). Spinel, melt and vapor bubble inclusions modify the density of individual

crystals in polyhedral clusters by < 0.5 % (Table 2; see supplementary material for detailed

296 calculations). These inclusions affect the density of skeletal crystals (single or clusters) to a larger

297 extent (up to 6% less dense). In the next sections, we compare the dimensions of the inclusions

298 (spinel, vapor bubble, melt) of the different olivine crystal morphologies.

299

300 **3.1.2. Size distributions of melt, vapor bubble and spinel inclusions**

301 For ease of reporting and discussion, we express the size of individual objects (melt inclusions,

302 spinels, vapor bubbles) as the diameter of a volume-equivalent sphere (d_{eq}).

303 The morphology of olivine-hosted melt inclusions is different in the three olivine types, suggesting 304 variable magmatic conditions (or growth rates) for their formation and/or maturation. The size of melt 305 inclusions (most of which are fully enclosed) in single skeletal olivine is highly heterogeneous (Fig. 5a). 306 The largest melt inclusions in single skeletal olivine vary from $d_{eq} < 5 \ \mu m$ to $d_{eq} = 415 \ \mu m$. As discussed 307 in previous studies (Faure and Schiano, 2005; Mourey and Shea, 2019; Wallace et al., 2021), small 308 melt inclusions may be inherited from larger inclusions that were split during crystal maturation and 309 closing in of the skeletal framework. Melt inclusions in clustered olivine crystals are for the most part 310 highly segregated (and highly oblate), with $d_{eq} < 100 \ \mu m$ (on average, $d_{eq} = 29 \ \mu m$). Melt inclusions in the 311 clustered olivine are equant, slightly larger than those in the skeletal crystals ($d_{eq} < 200 \ \mu m$, $d_{eq} = 46$ 312 µm in average).

313 Vapor bubbles are usually connected to melt inclusions in clustered and single skeletal olivine crystals.

Bubbles in clustered, *c*-elongated crystals are not common. They can be associated with melt

inclusions or isolated as fluid inclusions (Fig. 3). The largest vapor bubbles (on average d_{eq} = 56 µm;

316 maximum $d_{eq} = 275 \,\mu\text{m}$) are observed in single skeletal olivine crystals elongated along the *a*-axis

317 (Fig. 5b). Smaller bubbles are present in clustered skeletal (d_{eq} = 44 µm average size) and c-

318 elongated olivine clusters (d_{eq} = 27 µm average size).

319 Most spinel crystals are completely enclosed within their host olivine, or in some cases, partially

320 exposed at the olivine surface. Their average and maximum sizes vary between the three olivine

321 morphologies (Fig. 5c). In clustered and single skeletal crystals, they are generally smaller (d_{eq} = 9 ± 2

322 μ m and maximum at d_{eq} =40-50 μ m). In the polyhedral clusters dominated by c-elongated olivine

323 crystals, spinel crystals are on average larger (d_{eq} =15 µm) with some well faceted microphenocrysts 324 (up to d_{eq} =170 µm; e.g., k1820-13A or k1820-5B). It is not possible to detect spinels smaller than ~2 325 μ m (voxel resolution) using X- μ CT scans or objects smaller than 8 μ m³. The number density of spinel 326 is low in polyhedral crystal clusters (128 to 2,093 spinels /mm³, or 405 to 3,184 spinels/cluster; Fig. 327 5d), medium-high in skeletal crystal clusters (3,461 and 4,289 spinel /mm³, or 448 to 627 328 spinels/cluster), and highly variable for the single skeletal crystals (1,953 to 17,736 spinel /mm³, or 106 329 to 2,093 spinels/crystal). Spinel size and volume in single and clustered skeletal crystals overlap with 330 those of polyhedral crystal clusters (*c*-elongated, more mature crystals; Mourey and Shea, 2019). The 331 volume of Cr-spinel observed in the olivine is likely related to the kinetics of olivine growth but through 332 the mechanism is not yet understood. Welsch et al. (2013) proposed that Cr enrichments formed 333 around rapidly growing olivine as Cr behaved incompatibly, leading to the crystallization of Cr-spinel 334 that are later progressively buried in the inner part of the olivine crystal during slower growth. 335 However, Cr generally shows partitionless or compatible behavior in the olivine-basalt system 336 (Schreiber 1979; Lang et al. 2022) and therefore cannot easily pile up during rapid growth. It is 337 possible that Cr-spinel simply forms prior to olivine and gets incorporated during rapid or slow growth 338 (e.g., Roeder et al. 2006). The variation in the number density of spinel in the crystal may be related to 339 changed in growth kinetics but further experiments are required to elucidate the exact mechanism 340 through which Cr-spinel is included in olivine, often in high numbers. 341 Overall, the crystals scanned by X-µCT highlight the negligible effect of inclusions (melt/fluid, vapor

bubble, Cr-spinel) on crystal settling (inclusions have little contribution to the particle density). Next, we leverage the morphologies identified in the 3D scans to define initial olivine crystal meshes that are integrated into numerical simulations (see section 2.3.). These simulations explore the influence of crystal shape and its orientation respective to the flow direction of the melt on the settling velocities.

346

347 3.2. Settling velocities

The results of the simulations are reported in terms of the coefficients of momentum exchange and settling velocities (Table 3) in the absence of other crystal (i.e., clusters). Figure 6 displays the evolution of the terminal velocity as a function of the solid volume fraction computed with Eq. (10) for all the orientations we simulated. In the context of a shear flow at low volume fraction, crystals tend to align along the streamlines. At intermediate crystal volume fractions, the contacts between the crystals disturb this alignment and generate bimodal distributions of the shape-preferred direction (Arbaret et al., 2007). The preferential orientation of the crystals along their elongation direction compared to the melt flow minimizes friction with the melt and leads to an increase in the crystal's settling velocity. Overall, increasing the aspect ratio of a crystal tends to exacerbate the influence of its orientation on the settling velocity (Schwindinger and Anderson, 1989).

358 For the two non-equant crystals (elongated parallel to a- and c-axis; Fig. 2), the settling velocity is 359 the highest when the long axis is parallel to the flow of the melt, and the lowest when the short axis is 360 oriented in the flow direction. For the a-elongated crystal, the gap between the two lowest settling 361 velocities (runs A2 and A3 in Fig. 6) is significant because the difference between the lengths of the 362 short and intermediate axes (*b*-axis < *c*-axis) affects the projected areas of the crystal in the direction of 363 the flow. The projected area is largest when the flow is along the *b*-axis (see a-elongated olivine in Fig. 364 2) and the settling velocity at a minimum (Fig. 6). This is illustrated by the larger contribution of the 365 pressure component of the drag force in run A3 (~50% of the total drag force; Table 3) compared to the 366 other simulations. On the contrary, the olivine elongated along the *c*-axis has its short and intermediate 367 axes with similar lengths, such that the projected areas and settling velocities are more similar when the 368 flow is aligned along the a-axis or b-axis (runs B1 and B2). The projected area of the crystal in the 369 direction of the flow is, however, a bit larger when the a-axis is aligned with the flow, as illustrated by the 370 larger contribution of the pressure component to the total drag force in run B1 (Table 3). The effect of 371 the larger projected area on the settling velocity is balanced by the influence of the crystal morphology, 372 which is more protruding along the a-axis than the b-axis (Fig. 2c). This makes the crystal more 373 hydrodynamic along the a-axis than the b-axis, balancing the influence of the projected area and 374 resulting in comparable settling velocities.

For the equant crystal, the difference between the settling velocities is controlled by the morphology of the surface of the crystal. The projected area of the crystal is the largest when the flow is along the *b*-axis, resulting in a lower settling velocity (Fig. 6) and a larger contribution of the pressure component to the total drag force (Table 3). The crystal has almost the same projected area when the flow is aligned along the *a*-axis or *c*-axis. The difference between the two settling velocities in these orientations results from the morphology of the crystal, which is more protruding along the *a*-axis. 381 To summarize, the simulations showed that the settling velocity is highest when the long axis of the 382 crystal is aligned with the flow direction of the melt. Settling velocity decreases with the increasing 383 aspect ratio of the crystal and leads to an increase in the influence of the crystal orientation (with the 384 flow direction) on the terminal velocity. Based on these simulations, we find relatively high crystal 385 settling rates (U_T) of ~9.7 x 10⁻⁶ to 1.4 x 10⁻⁵ m/s (or 3.5 to 5.0 cm/hour) for particle volume fractions 386 (Φ) of 0 to 0.5. The complex olivine geometries decrease by factors of 3 to 5 the settling rates to that 387 of ideal spheres with the same diameter (\hat{U}_{T} ; Fig. 6). Overall, our estimated settling rates are more 388 refined than previous Stockes velocities for Kilauea olivine (6.5×10^{-8} m/s to 4×10^{-5} m/s; 389 Schwindinger 1999). In the following sections, we exploit our new settling rate estimates to constrain 390 the timescales for the formation of olivine cumulates in mafic magma reservoirs. Then, we consider 391 how crystal suspension times in magmatic reservoirs may affect real crystal size distribution (CSD) 392 measured in Kilauea samples.

393

394 4. Discussion

395 4.1. Suspension time of olivine crystals in basaltic melts

396 In this section, we evaluate the timescales over which olivine crystals can stay in suspension in a basaltic 397 melt. We term this timescale the suspension time. We consider olivine crystals with realistic 398 morphologies that undergo vigorous melt convection following an updated version of the model of Martin 399 and Nokes (1988). This model considers a suspension of particles convecting within a viscous liquid of 400 a given volume. A rheologically-locked layer, where the frictional contacts between the crystals oppose 401 motion (Huber et al., 2010) is located at the base of the convecting volume (Fig.7a). Martin & Nokes 402 (1988) model is valid at the base of the fluid where the convective velocity is zero, presumably meaning 403 that that fluid thickness must be rather small. However, their model holds to a very good approximation 404 even when the settling velocity is comparable to the convective velocity over the whole depth of the 405 fluid. Therefore, we consider a convective layer of relatively small thickness (i.e. 200 m; Fig.7a) 406 representative of the inferred size of most of Hawaiian sills (Ryan et al., 1983). The evolution of the 407 number of particles located within the convective volume, N, is calculated using Eq. (6) of Martin and 408 Nokes (1988):

 $409 \quad \frac{dN}{dt} = \frac{-U_T}{h}N \tag{18}$

410 where U_T is the terminal settling velocity, and *h* is the height of the convective layer. Considering all the 411 crystals as having the same volume, the number of particles within the convective layer, V_c , can be 412 expressed as a function of ϕ :

$$413 \quad N = \frac{\phi V}{V_c} \tag{19}$$

where *V* is the total volume of the convective layer (considered constant). Inserting Eq. (19) into Eq.(18) and neglecting the growth or dissolution of crystals (V_c constant) gives:

$$416 \quad \frac{d\phi}{dt} = \frac{-U_T}{h}\phi \qquad (20)$$

417 Inserting Eq. (9) into Eq. (20) gives the following differential equation describing the evolution of ϕ in the 418 convective layer:

419
$$\frac{d\phi}{dt} = \frac{-\Delta\rho gm\phi}{h\rho_c F_{D,0}(1-\phi)^{-3.7}}$$
 (21)

420 To compare our model to that of Martin and Nokes (1988), we consider a convective layer with a 421 height of 200 m with an initial particle volume fraction $\phi_0 = 0.5$. We considered a dilute regime (where 422 particle volume fractions in suspension represent <1 vol.%) and an intermediate regime (with particle 423 volume fractions between 1-50 vol.%) but did not considered concentrated regimes where particle 424 volume fractions is close to the maximum packing and where crystal-crystal interactions become 425 important for the overall effective viscosity, the mobility of magmas and decrease magma convection 426 (Bachmann and Bergantz, 2004; Faroughi and Huber, 2023). The coefficient of momentum exchange 427 and terminal velocity used as input for the models are taken from the result of the 9 numerical simulations (Table 3). Unlike the model of Martin and Nokes (1988), our calculations account for the 428 429 dependence of crystal settling velocity on ϕ . Therefore, the suspension time of crystals in the 430 convective layer is a function of the initial particle volume fraction (ϕ_0 ; Fig. 7). 431 We find that if the settling velocity is constant (with a settling velocity fixed at $\phi = 0$, as predicted by Eq. 432 13), the suspension time tends to be underestimated (predicted by Eq. 20; Fig. 7) and the settling rate 433 of the particles is overestimated in comparison with the Martin and Nokes (1988) model. We neglect 434 the decrease of magma convection caused by the high fraction of particles (ϕ up to 0.5) that can 435 decrease our suspension times and therefore we propose maximum estimates for the suspension 436 times. Moreover, the model does not consider the reentrainment of some crystals near the interface on 437 top of the convective layer after their settling. The volume fraction of particles in suspension ϕ 438 decreases with time for a given reservoir height (Fig. 7). ϕ in the convecting layer reaches less than

439 0.1 after 3 to 4 years for a 200 m magma body. Crystal settling of most of the particles (\$\phi\$ close to 0\$) in
440 a small reservoir (i.e., sill with a height of 200 m) is reached in around 5 years in all the simulations
441 performed.

442 Magma mixing and the addition of gas bubbles in the magma leads to complications for the 443 understanding of crystal settling in natural volcanic systems. In natural magmas, crystals and silicate 444 melt are interacting with exsolved volatiles at shallow depths. Adding a supercritical fluid such as CO₂ 445 bubbles increases the settling rate of crystals (Schwindinger, 1999). Magmas with initially low volatile 446 contents at depths (i.e., 0.3 wt.% CO₂ at >1 kbars for Kīlauea) can exsolve large amounts of volatile at 447 shallower depths (in our previous example, up to 35 vol.% at 50 bars (Holloway, 1977; Flowers, 1979; 448 Silver et al., 1990; Dixon et al., 1995; Anderson, 1995; Schwindinger, 1999). The upward streaming of 449 the gas, associated with an intruding MgO-rich melt, can initiate a lateral segregation of the crystals and 450 enhance the sedimentation rate of the olivine crystals by a factor of 5-10 (Schwindinger, 1999). 451 Therefore, our settling rate estimates should be viewed as minimum values. Considering the likely 452 presence of exsolving volatiles in natural basaltic reservoirs, the suspension time of 1-mm crystals, 453 similar to those modeled in this paper, are on the order of a few years even for large mafic reservoirs 454 (>1 km thick).

455

456 **4.2. Application to mafic systems and the formation of olivine mushy zones**

457 Our crystal settling simulations can be used to constrain the timescales required for the formation of 458 olivine cumulates in basaltic systems. One limitation in our numerical simulations is that we did not 459 consider the lateral motion of crystals expected to occur in natural sills (DiBenedetto et al., 2020). 460 Crystal settling timescales in such sills are assumed to be short, and therefore cumulates can form 461 rapidly in layers where convection is not effective. Notwithstanding, our results have implications for 462 interpreting the formation of mush systems in active magma reservoirs. In mafic systems like Kilauea, 463 the solidification rate of a magma reservoir depends on olivine nucleation, growth and settling rates. 464 Recrystallization can also affect the differentiation of a solidifying reservoir. Settling rates of olivine 465 crystals, and thereby the timescales to form olivine cumulates, can only be constrained with 466 information about their 3D geometry and the respective proportions of each crystal morphology (e.g., 467 same number of crystals elongated along a-, b-, and c-axis). Future work is needed to document the

3D morphology of olivine crystals in exposed olivine cumulates to access information about theirformation.

470 The relatively short suspension times of olivine crystals in a convective layer (a few years depending 471 on the crystal volume fraction and reservoir size) could explain why most Pele's hairs, tears, scoria 472 and tephra collected from lava lakes are typically aphyric (e.g., Thornber et al., 2015). Lava lakes like 473 those at Kīlauea produce occasionally glassy juvenile ejecta falling as Pele's hair and tears, and small 474 clots of spatter on the rim of Halema'uma'u (Wilson et al., 2008), but never sample the large 475 proportions (~14 vol.%; Clague and Denlinger, 1994) of olivine cumulates that are present beneath 476 Kīlauea summit, aerial and submarine Rift Zones (Delaney et al., 1990; Johnson, 1995; Denlinger, 477 1997). One reason may be that olivine settling is fast and efficient, which could be enhanced by 478 exsolved volatiles (Schwindinger 1999). We propose that a rapid increase in the proportion of locked 479 crystals that are not convecting and are not reinjected into the convecting melt is responsible for the 480 formation of olivine aggregates observed in Hawaiian and other basaltic volcanoes. An increase in 481 magma supply rate (as recently observed during the 21st century at Kīlauea, ~0.2 km³/yr; Poland et al., 482 2014) increases the amount of heat provided to the reservoir and in turn the vigor of the convection, 483 and it can trigger the reentrainment of some crystals near the interface between the locked layer and 484 the convective layer. However, Kilauea olivine crystals in the inner part of the locked layer may be well 485 compacted and possibly deformed (Clague and Denlinger, 1994) and therefore not easily unlocked. 486 The preponderance of magma mixing at Kilauea (Lynn et al., 2017; Mourey et al., 2023) also favors 487 undercooling and heating of the existing magma (and its crystal cargo) that counterbalance the 488 solidification of the resident magma.

489

490 Using previous estimates of the vertical extent of olivine cumulate mush piles at Kīlauea (~180-720 m 491 with ~40% porosity; Wieser et al., 2019), the constraints on Kilauea reservoir radius from 492 interferometric synthetic aperture radar (~2-4 km by InSAR; Baker and Amelung, 2012), and for olivine 493 crystals equivalent to a 1 mm-radius sphere (same volume as in our simulations), we can estimate that 494 a locked layer of mush may contain about 2.2 x 10¹⁷ to 3.5 x 10¹⁸ crystals. The convective melt may in 495 turn contain 1.6 x 10¹⁶ to 2.6 x 10¹⁷ crystals, assuming an olivine volume fraction of 0.05 (Thornber et 496 al., 2015). The locked layer (or mush piles) therefore contains ~13times more crystals than the 497 convecting layer. Using our olivine crystal settling rates ($U_T = 7.5 \times 10^{-6}$ to 1.1×10^{-5} m/s at $\phi = 0.05$),

498 we can estimate that 5 vol.% of olivine crystals in the convecting layer can reach the bottom of the 499 180–720 m reservoir in ~6 months to 3 years (ignoring the influence of volatiles and possible lateral 500 segregation). Assuming continuous nucleation of olivine crystals in the magma column, we estimate 501 that olivine mush piles at Kīlauea can be formed in < 5 years. Suspension timescales for olivine 502 crystals are much shorter than crystal storage timescales retrieved from melt inclusion studies (e.g., 503 scavenging of century-old primitive olivine crystals with new olivine cargo during the Maunaulu 1969-504 1974 eruption; Wieser et al., 2019) and a negligeable fraction of the tholeiitic shield stage period at 505 Kīlauea Volcano (starting around 240 ka years ago; Garcia et al., 2017). The low crystal fraction in 506 Kilauea summit lavas (up to 5 vol.%) therefore implies that most of olivine cargo that nucleated at the 507 summit is stored either at the bottom of the summit reservoirs or in the Rift Zones. The poor constraint 508 on the intensity of magma convection at Kīlauea potentially strongly increases our crystal suspension 509 times (longer suspension) in the case of a highly convective magma reservoir. Our model also 510 assumes homogeneous nucleation in the magma column and do not consider any preferential crystal 511 nucleation or the formation of crystal cluster by growth (branching or surface nucleation) or synneusis 512 (reorientation and attachment of the grains to minimize the surface energy) that could also increase 513 our crystal settling estimates (Culha et al., 2020).

514

515 4.3. Application to CSD studies

516 Our olivine settling rates can also be used to evaluate the time frames over which crystal size 517 distributions (CSD) produced by crystal nucleation, growth, and ripening can evolve by gravitational 518 settling in mafic reservoirs. For a fixed reservoir height (h) and terminal velocity (U_T) , the suspension 519 time of olivine crystals is a function of the particle volume fraction ϕ (Fig. 8). For olivine spanning 520 diameters equivalent to phenocryst sizes observed at Kīlauea (250 µm to 8 mm; Vinet and Higgins, 521 2010, 2011; Mourey and Shea, 2019), the suspension times vary from <1 year to a few years for mm-522 sized crystals, up to a few centuries for smaller phenocrysts (250 µm). For instance, the phenocryst 523 fraction (>250 µm) from CSDs extracted from samples of the Maunaulu 1969-1974 eruption (Vinet and 524 Higgins, 2010) correspond to suspension times ranging from ~6 months (for larger phenocrysts) to 525 ~120 years (for crystals close to 250 µm in size). Our calibration could therefore be used to re-interpret 526 CSDs from melt-dominated basaltic systems in terms of crystal suspension times.

528 Conclusion

529 We conducted X-µCT scans of olivine crystals from Kīlauea Volcano to elucidate the complexities of 530 olivine internal textures. The crystal scans reveal complex melt, spinel and vapor bubble shapes, and 531 a large diversity of inclusion volumes. We show that mineral, melt and gas inclusions only modify the 532 density of crystals by up to 6% relative, which has a limited effect on crystal settling rates in 533 comparison with the crystal shape. We thus explore the effect of crystal morphology on settling rate 534 using numerical simulations. We find that the settling velocity is higher when the elongated 535 crystallographic axis is aligned with the flow of the melt. We evaluate the time of the olivine crystals 536 suspended in a reservoir undergoing vigorous convection. Suspension times vary with the initial 537 particle volume fraction, but in general, olivine crystals have short (<5 years) suspension times in a 538 convective layer. The short suspension times may in turn affects the rates of solidification at the base 539 of a basaltic reservoir in synergy with magma cooling and crystallization. We also propose a 540 calibration of olivine suspension times (based on known particle volume fraction, reservoir height, 541 olivine morphology) that can be used to interpret the CSDs in terms of crystal suspension times in a 542 mafic reservoir. Crystal settling is a potentially key melt differentiation mechanism, as has been 543 highlighted at some ocean island volcanoes (e.g., Pankhurst et al., 2018a) but may also be of 544 importance at other melt-dominated mafic volcanoes.

545

546

547 CRediT authorship contribution statement

Adrien J. Mourey: Conceptualization, Data curation, Formal analysis, Investigation, Methodology,
Software, Visualization, Writing – original draft. Alexandre Carrara: Conceptualization, Funding
acquisition, Investigation, Methodology, Software, Visualization, Writing – original draft, Writing –
review & editing. Thomas Shea: Funding acquisition, Investigation, Methodology, Software, Writing –
review & editing. Fidel Costa: Conceptualization, Funding acquisition, Writing – review & editing.
Marc-Antoine Longpré: Conceptualization, Funding acquisition, Writing – review & editing.
Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationshipsthat could have appeared to influence the work reported in this paper.

558	
559	Data availability
560	All data obtained in this study are included in the supplementary data tables.
561	
562	Acknowledgments
563	The authors thank Jessica Maisano at the NSF-supported UTCT facility for assistance with the
564	microtomography scans. A.M. and T.S. received funding from the National Science Foundation (NSF)
565	grant to T.S. (EAR 1725321). A.C. was partly supported by the National Science Foundation grant
566	EAR-1950113, and the Region Auvergne and the European Regional Development Fund (Laboratory
567	of Excellence ClerVolc contribution number XXX). MA.L. was supported through NSF award EAR
568	1650379. The authors thank the editor and the two reviewers (Jérémie Vasseur and Matt Pankhurst)
569	for their detailed evaluation of this manuscript and for the constructive set of comments.
570	References
571	
572	Anderson, A.T., 1995. CO ₂ and the eruptibility of picrite and komatiite. Lithos 34, 19–25.
573	
574	Arbaret, L., Bystricky, M., Champallier, R., 2007. Microstructures and rheology of hydrous synthetic
575	magmatic suspensions deformed in torsion at high pressure. J. Geophys. Res.: Solid Earth, 112(B10).
576	
577	Arzilli, F., Agostini, C., Landi, P., Fortunati, A., Mancini, L., Carroll, M.R., 2015. Plagioclase nucleation
578	and growth kinetics in a hydrous basaltic melt by decompression experiments. Contrib. Mineral. Petrol.
579	170(5-6).
580	
581	Bachmann, O., Bergantz, G. W., 2004. On the origin of crystal-poor rhyolites: extracted from
582	batholithic crystal mushes. J. Petrol. 45(8), 1565-1582.
583	
584	Bachmann, O., Huber, C., 2019. The inner workings of crustal distillation columns; the physical
585	mechanisms and rates controlling phase separation in silicic magma reservoirs. Journal of
586	Petrology, 60(1), 3-18.
587	

- 588 Baker, S., Amelung, F., 2012. Top-down inflation and deflation at the summit of Kilauea Volcano,
- 589 Hawai'i observed with InSAR. J. Geophys. Res. 117, 1–14.
- 590
- 591 Byron, D.N., Atherton, M.P., Hunter, R.H., 1995. The interpretation of granitic textures from serial thin
- 592 sectioning, image analysis and three-dimensional reconstruction. Mineral. Magazine 59, 203–211.
- 593
- 594 Carrara, A., Burgisser, A., & Bergantz, G. W. (2019). Lubrication effects on magmatic mush dynamics.
- 595 Journal of Volcanology and Geothermal Research, 380, 19-30.
- 596
- 597 Clague, D.A., Denlinger, R.P., 1994. Role of olivine cumulates in destabilizing the flanks of Hawaiian
- 598 volcanoes. Bull. Volcanol. 56(6-7), 425–434.
- 599
- 600 Clark, A. H., Pearce, T. H., Roeder, P. L., Wolfson, I., 1986. Oscillatory zoning and other
- 601 microstructures in magmatic olivine and augite: Nomarski interference contrast observations on etched
- 602 polished surface. Am. Mineral. 71, 734–741.
- 603
- 604 Constant, M., Dubois, F., Lambrechts, J., Legat, V., 2018. Implementation of an unresolved stabilised
- 605 FEM–DEM model to solve immersed granular flows. Computational Particle Mechanics.
- 606
- 607 Culha, C., Suckale, J., Keller, T., & Qin, Z., 2020. Crystal fractionation by crystal-driven
- 608 convection. *Geophysical Research Letters*, 47(4), e2019GL086784.
- 609
- 610 Daniel, C.G., Spear, F.S., 1999. The clustered nucleation and growth processes of garnet in regional
- 611 metamorphic rocks from north-west Connecticut, USA. J. Metam. Geol. 17, 503–520.
- 612
- 613 Delaney, P.T., Fiske, R.S., Miklius, A., Okamura, A.T., Sako, M.K., 1990. Deep Magma Body Beneath
- 614 the Summit and Rift Zones of Kilauea Volcano, Hawaii. Science 247(4948), 1311–1316.
- 615
- 616 Denlinger, R.P., 1997. A dynamic balance between magma supply and eruption rate at Kilauea
- 617 volcano, Hawaii. J. Geophys. Res.: Solid Earth 102(B8), 18091–18100.

619	DiBenedetto, M., Qin, Z., Suckale, J., 2020. Crystal aggregates record the pre-eruptive flow field in the
620	volcanic conduit at Kīlauea, Hawaii. Sci. Adv. 6(49), eabd4850.
621	
622	Di Felice, R., 1994. The voidage function for fluid-particle interaction systems. Inter. J. Multiphase
623	Flow 20(1), 153–159.
624	
625	Dixon, J.E., Stolper, E.M., Holloway, J.R., 1995. An experimental study of water and carbon dioxide
626	solubilities in mid-ocean ridge basaltic liquids. Part I: Calibration and solubility models. J. Petrol. 36,
627	1607–1631.
628	
629	Donaldson, C.H., 1976. An experimental investigation of olivine morphology. Contrib. Mineral. Petrol.
630	57, 187–213.
631	
632	Elkins-Tanton, L.T., 2012. Magma Ocean in the inner solar system. Annu. Rev. Earth Planet. Sci. 40,
633	113–139.
634	
635	Faroughi, S. A., Huber, C., 2023. Rheological state variables: A framework for viscosity
636	parametrization in crystal-rich magmas. J. Volc. Geotherm. Res., 440, 107856.
637	
638	Faure, F., Trolliard, G., Nicollet, C., Montel, JM., 2003. A developmental model of olivine morphology
639	as a function of the cooling rate and the degree of undercooling. Contrib.Mineral. Petrol. 145, 251-
640	263.
641	
642	Faure, F., Schiano, P., 2005. Experimental investigation of equilibration conditions during forsterite
643	growth and melt inclusion formation. Earth Planet Sci. Lett. 236, 882-898.
644	
645	Flowers, G.C., 1979. Correction of Holloway's 1977. Adaptation of the modified Redlich-Kwong
646	equation of state for calculation of the fugacities of molecular species in supercritical fluids of geologic
647	interest. Contrib. Mineral. Petrol. 69, 315–318.

- Garcia, M.O., Jicha, B.R., Marske, J.P., Pietruszka, A.J., 2017. How old is Kīlauea Volcano? Insights
 from ⁴⁰Ar/³⁹Ar dating of the 1.7-km-deep SOH-1 core. Geology 45, 79–82.
- 651
- 652 Geuzaine, C., Remacle, J.-F., 2009. Gmsh: A 3-D finite element mesh generator with built-in pre- and 653 post-processing facilities. Inter. J. Num. Meth. Eng. 79(11), 1309–1331.
- 654
- Giordano, D., Russell, J. K., & Dingwell, D. B. (2008). Viscosity of magmatic liquids: a model. *Earth and Planetary Science Letters*, 271(1-4), 123-134.
- 657
- 658 Gordeychik, B., Churikova, T., Shea, T., Kronz, A., Simakin, A., Wörner, G., 2020. Fo and Ni relations
- in olivine differentiate between crystallization and diffusion trends. J. Petrol. 61, egaa083.
- 660
- He, L., Tafti, D. K., & Nagendra, K. (2017). Evaluation of drag correlations using particle resolved
- simulations of spheres and ellipsoids in assembly. *Powder technology*, 313, 332-343
- 663
- Holloway, J.R., 1977. Fugacity and activity of molecular species in supercritial fluids. In: D.G. Fraser,
- Ed., Thermodynamics in Geology. Reidel Publishing, Dordrecht, Holland, 161–181.
- 666
- Holness, M.B., Farr, R., Neufeld, J.A., 2017. Crystal settling and convection in the Shiant Isles Main
 Sill. Contrib. Mineral. Petrol. 172.
- 669
- Huber, C., Bachmann, O., Dufek, J., 2010. The limitations of melting on the reactivation of silicic
- 671 mushes. J. Volcanol. Geotherm. Res. 195(2-4), 97–105.
- 672
- 573 Jambon, A., Lussiez, P., Clocchiatti, R., Weisz, J., Hernandez, J., 1992. Olivine growth rates in a
- tholeiitic basalt; an experimental study of melt inclusions in plagioclase. Chem. Geol. 96, 277–287.
- 675
- Johnson, D.J., 1995. Molten core model for Hawaiian rift zones. J. Volcanol. Geotherm. Res. 66(1-4),
 27–35.

679

680 fluid. Nature 343, 447-450. 681 682 Lang, S., Mollo, S., France, L., Misiti, V., Nazzari, M., 2022. Partitioning of Ti, AI, P, and Cr between 683 olivine and a tholeiitic basaltic melt: Insights on olivine zoning patterns and cation substitution 684 reactions under variable cooling rate conditions. Chemical Geology, 601, 120870. 685 686 Lavorel, G., Le Bars, M., 2009. Sedimentation of particles in a vigorously convecting fluid. Phys. Rev. 687 E 80, 046324. 688 689 Lynn, K.J., Garcia, M.O., Shea, T., Costa, F., Swanson, D.A., 2017. Timescales of mixing and storage 690 for Keanakāko'i tephra magmas (1500–1820 CE), Kīlauea volcano, Hawai'i. Contrib. Mineral. Petrol. 691 172, 76-96. 692 693 Martin, D., Nokes, R., 1988. Crystal settling in a vigorously converting magma chamber. Nature 332, 694 534-536. 695 696 Mock, A., Jerram, D.A., 2005. Crystal size distribution (CSD) in three dimensions: insights from the 3D 697 reconstruction of a highly porphyritic rhyolite. J. Petrol. 46, 1525–1541. 698 699 Mourey, A.J., Shea, T., 2019. Forming olivine phenocrysts in basalt: a 3D characterization of growth 700 rates in laboratory experiments. Front. Earth Sci. 7. 701 702 Mourey, A.J., Shea, T., Lynn, K.J., Lerner, A.H., Lambart, S., Costa, F., Oalmann, J., Lopaka Lee, R., 703 Gansecki, C., 2022. Trace elements in olivine fingerprint the source of 2018 magmas and shed light 704 on explosive-effusive eruption cycles at Kīlauea Volcano. Earth Planet. Sci. Lett. 595, 117769 705 706 Mourey, A.J., Shea, T., Hammer, J.E., 2023. Preservation of magma recharge signatures in Kilauea 707 olivine during protracted storage. J. Geophys. Res.: Solid Earth e2022JB025523. https:// doi. org/ 10.

Koyaguchi, T., Hallworth, M., Huppert, H. et al., 1990. Sedimentation of particles from a convecting

708 1029/ 2022J B0255 23

709

- Murata, K.J., Richter, D.H., 1966. The settling of olivine in Kilauean magma as shown by lavas of the
 1959 eruption. Am. J. Sci. 264(3), 194–203.
- 712
- 713 Oppenheimer, J., Patel, K., Lindoo, A., Hillman, E.M.C., Lev, E., 2021. High-Speed 3D Imaging of
- 714 Multiphase Systems: Applying SCAPE Microscopy to Analog Experiments in Volcanology and Earth
- 715 Sciences. Geochem. Geophys. Geosyst. 22(3).
- 716
- 717 Pankhurst, M.J., Dobson, K.J., Morgan, D.J., Loughlin, S.C., Thordarson, T., Lee, P.D., Courtois, L.,
- 718 2014. Monitoring the magmas fuelling volcanic eruptions in near-real-time using X-ray micro-computed
- 719 tomography. J. Petrol. 55 (3), 671–684.

720

- 721 Pankhurst, M.J., Morgan, D.J., Thordarson, T., Loughlin, S.C., 2018a. Magmatic crystal records in
- time, space, and process, causatively linked with volcanic unrest. Earth Planet. Sci. Lett. 493, 231-
- 723 241.
- 724
- 725 Pankhurst, M.J., Vo, N.T., Butcher, A.R., et al., 2018b. Quantitative measurement of olivine
- composition in three dimensions using helical-scan X-ray micro-tomography. Am. Mineral. 103(11),
- 727 1800–1811.

728

Pearce, T.H., 1984. The analysis of zoning in magmatic crystals with emphasis on olivine. Contrib.

730 Mineral. Petrol. 86, 149–154.

- 731
- 732 Polacci, M., Baker, D.R., Mancini, L., Tromba, G., Zanini, F., 2006. Three-dimensional investigation of
- volcanic textures by X-ray microtomography and implications for conduit processes. Geophys. Res.

734 Lett. 33(13).

- Poland, M.P., Miklius, A., Montgomery-Brown, E.K., 2014. Magma supply, storage, and transport at
- shield-stage Hawaiian volcanoes. USGS Prof. Pap. 1801. pp.179–234.

739	Roeder, P., Gofton, E., Thornber, C., 2006. Cotectic proportions of olivine and spinel in olivine-					
740	tholeiitic basalt and evaluation of pre-eruptive processes. Journal of Petrology, 47(5), 883-900.					
741						
742	Ryan, M.P., Blevins, J.Y.K., Okamura, A.T., Koyanagi, R.Y., 1983. Magma reservoir subsidence					
743	mechanisms: Theoretical summary and application to Kilauea Volcano Hawaii. J. Geophys. Res. 88,					
744	4147–4181.					
745						
746	Sanjeevi, S. K., Kuipers, J. A. M., & Padding, J. T., 2018. Drag, lift and torque correlations for non-					
747	spherical particles from Stokes limit to high Reynolds numbers. International Journal of Multiphase					
748	Flow, 106, 325-337.					
749						
750	Schmidt, M.W., Forien, M., Solferino, G., Bagdassarov, N., 2012. Settling and compaction of olivine in					
751	basaltic magmas: an experimental study on the time scales of cumulate formation. Contrib. Mineral.					
752	Petrol. 164, 959-976.					
753						
754	Schreiber, H. D., 1979. Experimental studies of nickel and chromium partitioning into olivine from					
755	synthetic basaltic melts. In: Lunar and Planetary Science Conference, 10th, Houston, Tex., March 19-					
756	23, 1979, Proceedings. Volume 1.(A80-23557 08-91) New York, Pergamon Press, Inc., 1979, p. 509-					
757	516. Research supported by the Research Corp.; (Vol. 10, pp. 509-516).					
758						
759	Schwindinger, K.R., Anderson, A.T, 1989. Synneusis of Kilauea Iki olivines. Contr. Mineral. And Petrol.					
760	103, 187–198.					
761						
762	Schwindinger, K.R., 1999. Particle dynamics and aggregation of crystals in a magma chamber with					
763	application to Kilauea Iki olivines. J. Volcanol. Geotherm. Res. 88(4), 209–238.					
764						
765	Shea, T., Costa, F., Krimer, D., Hammer, J.E., 2015. Accuracy of timescales retrieved from diffusion					
766	modeling in olivine: a 3D perspective. Am. Mineral. 100, 2026–2042.					
767						

- 768 Silver, L.A., Ihinger, P.D., Stolper, E., 1990. The influence of bulk composition on the speciation of
- 769 water in silicate glasses. Contrib. Mineral. Petrol. 104, 142–162.
- 770
- Solomatov, V., Olson, P., Stevenson, D., 1993a. Entrainment from a bed of particles by thermal
- 772 convection. Earth Planet. Sci. Lett. 120, 387.
- 773
- Solomatov, V., Stevenson, D., 1993b. Suspension in convective layers and style of differentiation of a
 terrestrial magma ocean. J. Geophys. Res. 98, 5375.
- 776
- 577 Swanson, D.A., Rose, T.R., Fiske, R.S., McGeehin, J.P., 2012. Keanakākoʻi Tephra produced by 300
- years of explosive eruptions following collapse of Kīlauea's caldera in about 1500 CE. J. Volcanol.
- 779 Geotherm. Res. 215–216:8–25.
- 780
- 781 Thornber, C.R., Orr, T.R., Heliker, C., Hoblitt, R.P., 2015. Petrologic testament to changes in shallow
- 782 magma storage and transport during 30+ years of recharge and eruption at Kīlauea Volcano, Hawai'i.
- 783 In: Carey, R.J., Cayol, V., Poland, M.P., Weis, D. (Eds.), Hawaiian Volcanoes: From Source to
- 784 Surface. Am. Geophys. Un. Geophys. Mono. 208, 147–188.
- 785
- Vinet, N., Higgins, M. D., 2010. Magma solidification processes beneath Kilauea volcano, Hawaii: A
 guantitative textural and geochemical study of the 1969–1974 Mauna Ulu Lavas. J. Petrol. 51(6),
- 788 1297-1332.
- 789
- Vinet, N., Higgins, M. D., 2011. What can crystal size distributions and olivine compositions tell us
 about magma solidification processes inside Kilauea Iki lava lake, Hawaii?. J. Volcanol. Geotherm.
 Res. 208(3-4), 136-162.
- 793
- Wallace, P.J., Plank, T., Bodnar, R.J., Gaetani, G.A., Shea, T., 2021. Olivine-hosted melt inclusions: a
 microscopic perspective on a complex magmatic world. Ann. Rev. Earth Planet. Sci. 49
- 796

- 797 Welsch, B., Faure, F., Famin, V., Baronnet, A., Bachelery, P., 2013. Dendritic crystallization: a single
- process for all the textures of olivine in basalts? J. Petrol. 54, 539–574.

- 800 Wieser, P.E., Edmonds, M., Maclennan, J. et al., 2019. Crystal scavenging from mush piles recorded
- 801 by melt inclusions. Nat. Commun. 10, 5797.
- 802
- 803 Wilson, D., Elias, T., Orr, T., Patrick, M., Sutton, J., Swanson, D., 2008. Small explosion from new vent
- 804 at Kilauea's summit. Eos Trans. AGU, 89, 203.
- 805
- 806 Zastawny, M., Mallouppas, G., Zhao, F., & Van Wachem, B. (2012). Derivation of drag and lift force
- 807 and torque coefficients for non-spherical particles in flows. International Journal of Multiphase Flow,
- 808 39, 227-239.

809 Fig. 1. Location of Kīlauea Volcano (left panel) and map of Kīlauea's summit (right panel).

- 810 Background digital elevation model from August 2018, with the 2018 collapse area shaded in pink.
- 811 Black cross represents coordinate system at 19.4073° N, 155.2784 ° W. The location of the Golden
- 812 Pumice eruption unit (Unit K1 from the explosive Keanakāko'i Tephra), the source of olivine
- 813 phenocrysts used for this study, is indicated by the red star.

814 Fig. 2. Numerical simulations of olivine settling. (a) Numerical simulation of the flow of melt around 815 an olivine crystal. The black box corresponds to the limit of the computational domain. The two gray 816 surfaces represent the mass inflow and pressure outflow boundary conditions. The crystal is located at 817 the center of the domain. The curves located within the domain are the melt flow streamlines color-818 coded for magnitude of flow velocity. (b) Zoom on the crystal. The red line indicates the edges of the 819 particles. The mesh corresponds to the surface elements on which the force applied by the liquid is 820 computed. (c) Geometry of the olivine crystals we have tested. Crystals used in the numerical 821 simulations are either elongated along the a-axis, elongated along the c-axis or equant. The three 822 crystal morphologies have the same volume ($\sim 4.19 \text{ mm}^3$) equivalent to a 2-mm sphere diameter.

- 824 Fig. 3. Representative secondary electron images (in grey) and 3D renderings of olivine
- 825 crystals from the 1820 Keanakākoʻi (unit K1) eruption. (a) Clustered polyhedral olivine elongated
- 826 along the c-axis; (b) Clustered skeletal olivine elongated along the a-axis; (c) Skeletal olivine
- 827 elongated along the a-axis. Numbers in the pie charts are relative volume % of the different phases in
- 828 the crystal (melt inclusions, Cr-spinel, vapor bubbles) retrieved from the Avizo[™] software. Note that
- 829 only inclusion fractions are represented in the pie charts (not the olivine fraction).

- 831 Fig. 4. Melt inclusion and vapor bubble relative volume % extracted from 3D renderings. Cr-
- 832 spinel in olivine makes up <1.5 volume % in all cases.

- 834 Fig. 5. Size of inclusions in olivine. Distribution (illustrated as violin plots) of equivalent sphere 835 diameters of (a) melt inclusions, (b) vapor bubbles, (c) Cr-spinel crystals and (d) density of Cr-spinel / 836 mm³) in skeletal crystal clusters, polyhedral crystal clusters and single skeletal olivine crystals 837 elongated along the a-axis. Cr-spinels are larger in polyhedral clusters (both the mean and maximum 838 diameter) than in skeletal clusters and skeletal single crystals. Most melt inclusions have an equivalent 839 sphere diameter <100 µm (segmented melt inclusions) but larger melt inclusions (up to 415 µm) are 840 also observed in skeletal olivine crystals elongated along the a-axis. The filled white circles indicate 841 the median value of the distribution, the filled grey areas are the interguartile ranges, and the thin 842 black lines represent the rest of the distribution. 843
- 045

Fig. 6. Variation of the settling velocity (U_T) of olivine crystals with particle volume fraction (ϕ)

846 for different crystal geometries and orientation with respect to the melt flow direction. Inset:

- ratio of olivine settling rates with different geometries to that of ideal spheres with the same diameter
- 848 (\hat{U}_T) as a function of ϕ ($\phi = 0$ for the Stokes' velocity). The highest speeds are those when the
- 849 elongated crystal axis is aligned with the flow. Complex crystal geometries decrease settling rates by
- 850 factors of 3 to 5 compared to spherical shapes.
- 851

Fig. 7. Time evolution of the particle volume fraction (ϕ) in suspension in the convective melt

853 **layer as a function of the crystal morphology.** (a) We consider a convective layer (in blue), in which

convection occurs and with particle volume fraction ϕ =0-0.5, and a locked layer (in red), in which no

855 convection occurs (with ϕ >0.5). The black circles represent the particles. The red arrows indicate the

856 convection. The green dashed line indicates the limit between the convective and locked domain. A

857 relatively small convective layer of 200 m is considered for the calculations since the fluid thickness

858 must be rather small for the Martin & Nokes (1988) model. (b) Suspension times (in years) of olivine

- crystals in the convective layer as a function of the particle volume fraction (ϕ), the crystal morphology
- 860 (see the parameters for the simulations in Tables 1 & 3). The blue, red and black curves correspond

to the numerical solution of Eq. (20) for the different simulations.

863 Fig. 8. Effect of crystal size (d_{eq}) on suspension time and as a function of the particle volume

864 fraction (φ). Only phenocryst sizes between 250 μm and 8 mm (in diameter) are displayed. The size

- 865 of the reservoir (h) is fixed at 200 m for the calculations. The terminal velocity (U_T) is fixed at 1.36 x 10⁻
- 866 ⁵ m/s (olivine elongated along a-axis with the a-axis aligned with the flow, run A1 in Table 3). This
- 867 calibration for the suspension timescales can be adapted for a given magmatic system with a known
- 868 magma reservoir height and olivine morphology.

















Table 1: Physical properties of the crystal and melt. Symbols used are ρ_i (melt density), η (melt viscosity), ρ_c (crystal density), U_{inj} (injection velocity).

Physical properties	Value	Reference
ρ_l	2750 kg m ⁻³	Mourey and Shea (2019)
η	30 Pa s	Giordano et al. (2008)
ρ _c	$3400 \pm 50 \text{ kg m}^{-3}$	Lynn et al. (2017); Mourey et al. (2022)
U _{inj}	10 ⁻³ m s ⁻¹	-

Table 2: Olivine crystal dimensions along a = [100], b = [010], c = [001] axis, equivalent sphere diameter, density of olivine crystal, effect of inclusions (melt, Cr-spinel, vapor bubbles) on crystal density. Details on density calculations are in the supplementary material.

Olivine name	Morphology	[100] length (µm)	[010] length (µm)	[001] length (µm)	Density crystal with inclusions (kg m ⁻³)	Olivine/crystal density difference due to inclusions (%)
k1820_ol1A	Skeletal cluster	2035	159	701	3253- 3340	-3.20 to -2.90
k1820_ol4A	Skeletal cluster	1487	289	849	3212- 3296	-4.45 to -4.11
k1820_ol2B	Skeletal crystal elongated along [100]	1916	353	729	3152- 3239	-6.12 to -5.92
k1820_ol3A	Skeletal crystal elongated along [100]	1735	452	844	3312- 3405	-1.32 to -1.15
k1820_ol14A	Skeletal crystal elongated along [100]	1517	832	330	3155- 3230	-6.38 to -5.83
k1820_ol9A	Skeletal crystal elongated along [100]	872	351	479	3246- 3328	-3.55 to -3.09
k1820_ol15A	Skeletal crystal elongated along [100]	705	297	347	3236- 3326	-3.60 to -3.42
k1820_ol11A	Skeletal crystal elongated along [100]	1040	362	612	3143- 3229	-6.41 to -6.17
k1820_ol10B	Skeletal crystal elongated along [100]	953	304	581	3339- 3434	-0.47 to -0.33
k1820_ol8A_1	Polyhedral crystal elongated along [100]	923	391	600	3381- 3480	+0.87 to +0.94
k1820_ol12A_1	Polyhedral crystal elongated along [100]	1565	580	1207	3381- 3480	+0.11 to +0.16
k1820_ol12A_2	Polyhedral crystal elongated along [100]	1220	556	817	3355- 3454	+0.11 to +0.16
k1820_ol12A_3	Polyhedral crystal elongated along [001]	1030	826	1238	3355- 3454	+0.11 to +0.16
k1820_ol13A_1	Polyhedral crystal elongated along [100]	2311	961	1404	3353- 3453	+0.08 to +0.09
k1820_ol13A_2	Polyhedral crystal elongated along [100]	631	464	619	3353- 3453	+0.08 to +0.09
k1820_ol13A_3	Polyhedral crystal elongated along [100]	927	596	516	3353- 3453	+0.08 to +0.09
k1820_ol13A_4	Polyhedral crystal elongated along [100]	1082	634	650	3353- 3453	+0.08 to +0.09
k1820_ol5B_1	Polyhedral crystal elongated along [001]	1172	813	1261	3358- 3457	+0.20 to +0.25
k1820_ol5B_2	Polyhedral crystal elongated along [100]	971	408	612	3358- 3457	+0.20 to +0.25
k1820_ol5B_3	Polyhedral crystal elongated along [001]	532	350	684	3358- 3457	+0.20 to +0.25
k1820_ol5B_4	Polyhedral crystal elongated along [001]	725	613	1209	3358- 3457	+0.20 to +0.25
k1820_ol5B_5	Polyhedral crystal elongated along [001]	491	467	582	3358- 3457	+0.20 to +0.25
k1820_ol5B_6	Polyhedral crystal elongated along [001]	307	250	371	3358- 3457	+0.20 to +0.25
k1820_ol5B_7	Polyhedral crystal elongated along [001]	87	77	97	3358- 3457	+0.20 to +0.25
k1820_ol5B_8	Polyhedral crystal elongated along [001]	81	233	250	3358- 3457	+0.20 to +0.25

- 1 **Table 3:** List of the simulations and results. ξ is a coefficient that depends on the shape and
- 2 orientation of the particle (see Eq. 17), % press. is the percentage of the contribution of pressure drag
- 3 to the total drag force (\int_{S} -*p* $n_s dS$ in Eq. 15), % frict. is the percentage of the contribution of viscous
- 4 friction to the total drag force ($\int_S \tau \, dS$ in Eq. 15), U_T is the terminal settling velocity, ϕ is the solid volume
- 5 fraction at the location of the
- 6 crystal.
- 7

Run	Crystal	Orientation	Axis lengths a, b, c (µm)	ξ	% press.	% frict.	U_T at $\phi = 0$
							(m s ⁻¹)
A1	Elongated along a-axis	<i>a-axis</i> aligned with the flow	3414; 983; 1648	83.6	21.3	78.7	1.36 × 10 ⁻⁵
A2	Elongated along a-axis	<i>b</i> -axis aligned with the flow	3414; 983; 1648	102.8	31.9	68.1	1.10 × 10 ⁻⁵
A3	Elongated along a-axis	<i>c-axis</i> aligned with the flow	3414; 983; 1648	117.2	50.3	49.7	9.67 × 10 ⁻⁶
B1	Elongated along c-axis	<i>a-axis</i> aligned with the flow	1426; 1742; 3022	100.2	44.3	55.7	1.13 × 10 ⁻⁵
B2	Elongated along c-axis	<i>b</i> -axis aligned with the flow	1426; 1742; 3022	99.7	38.0	62.0	1.14 × 10 ⁻⁵
В3	Elongated along c-axis	<i>c-axis</i> aligned with the flow	1426; 1742; 3022	82.1	22.5	77.5	1.38 × 10 ⁻⁵
C1	Equant	<i>a-axis</i> aligned with the flow	2040; 1942; 1978	88.4	35.6	64.4	1.28 × 10 ⁻⁵
C2	Equant	<i>b-axis</i> aligned with the flow	2040; 1942; 1978	96.4	35.6	64.4	1.18 × 10 ⁻⁵
C3	Equant	<i>c-axis</i> aligned with the flow	2040; 1942; 1978	90.8	38.3	61.7	1.25 × 10 ⁻⁵