

Coupling Variational Data Assimilation and Operator Learning For Effective State Estimation on Complex Systems

Stiven Briand God Massala, Ludovic Chamoin, Massimo Pica Ciamarra

▶ To cite this version:

Stiven Briand God Massala, Ludovic Chamoin, Massimo Pica Ciamarra. Coupling Variational Data Assimilation and Operator Learning For Effective State Estimation on Complex Systems. 16th World Congress on Computational Mechanics and 4th Pan American Congress on Computational Mechanics, International Association for Computational Mechanics (IACM); The Canadian Association for Computational Science and Engineering (CACSE), Jul 2024, Vancouver (BC), Canada. hal-04753140

HAL Id: hal-04753140 https://hal.science/hal-04753140v1

Submitted on 29 Oct 2024

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés. Advances in neural operators for scientific modeling July 21-26, 2024, Vancouver Convention Centre, Vancouver, British Columbia, Canada

COUPLING VARIATIONAL DATA ASSIMILATION AND OPERATOR LEARNING FOR EFFECTIVE STATE ESTIMATION ON COMPLEX SYSTEMS

Stiven Briand God Massala Moussounda^{*1}, Ludovic Chamoin² and Massimo Pica Ciamarra³

¹ENS Paris-Saclay, NTU Singapore, CNRS, LMPS Paris-Saclay
²ENS Paris-Saclay, Institut Universitaire de France
³NTU Singapore, Consiglio Nazionale delle Ricerce CNR-SPIN

ABSTRACT

We introduce a hybrid twin approach to solve physical systems modeled by parametrized Partial Differential Equations (PDE). Our approach, combines the variational data assimilation (PBDW) [1] with operator learning(Deeponets)[2] to reconstruct the state of an imperfect physical system given many observations. The PBDW method is a non-intrusive, reduced basis, in-situ data assimilation framework, that estimates the solution of a biased model given many observations. This method provide a state estimate framework for parameterized model that estimate both the anticipated and the non anticipated physics while ensuring orthogonality between both parts. The anticipated physics is approximated by a background space constructed with reduced basis while the non-anticipated physics is infered by a Deeponets. The hybrid twin was performed using two approaches to ensure orthogonality. A first approach with a weak constrain, that regularizes the loss function of the neural operator with the dot product between the un-anticipated physics and the background space, in this case the trunk net learn from the whole space but the constrain is only garanteed in the training stage. And a second approach with strong constrain where the trunk is replaced by a set of basis function, each orthogonal to the background space by construction, that garantee orthogonaly in both the training and inference stage of the un-anticipated physics. The hybrid twin was applied on a 2D Helmoltz equation on a homogeneous and bounded domain with a biased source, to showcase its potential for solving complex physical systems.

 [1] Maday, Y., Patera, A. T., Penn, J. D. and Yano, M. A parameterized-background data-weak approach to variational data assimilation : formulation, analysis, and application to acoustics International Journal for Numerical Methods in Engineering 2015

[2] DeepONet: Learning nonlinear operators for identifying differential equations based on the universal approximation theorem of operators