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# Machine Learning-Assisted Microscopic Public Transportation Simulation: Two Coupling Strategies

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## Abstract

Evaluating the performance of public transportation, such as bus lines for example, is a major issue for **Public Transportation** operators. To be able to integrate specific and local behaviors, microscopic line simulations, modelling each buses on a daily basis, provide actual added value in terms of precision and quality. Carrying out more realistic and accurate simulations requires the use of appropriate parameters. To achieve this, machine learning models trained on **real-world** data can be used to feed and parameterize simulation models. To address this scientific question, it is necessary to determine how to **efficiently integrate** machine learning and simulation models. This study aims to couple machine learning and microscopic simulation models using **various** strategies, evaluate their accuracy and performance and discuss the advantages and drawbacks of each. A case study involving three bus lines was conducted, with results validated against real-world data, showing a good fit for both online and offline strategies. With the best simulation time, good accuracy and adequate travel times and bus punctuality, **an offline strategy** seems to stand out from other coupling strategies.

**Keywords:** Machine learning, Microscopic simulation, ML-assisted simulation, Travel time variability, Bus travel time, Bus punctuality, Bus line simulation

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## 1. Introduction

Rapid progress in urbanization has modernized the lives of many people, but also brought major problems and challenges, such as energy consumption, pollution and traffic congestion [1; 2]. **To reduce traffic congestion**, and therefore its negative impacts, cities around the world are trying to shift personal traffic to **Public Transportation (PT)** [3; 4; 5], also called public transport, **public transit or mass transit**. It is defined as passenger transportation service, provided by public or private agencies, available to the general public.

In PT, reliability is considered **as one of the most critical features** for evaluating Quality of Service (QoS) from the perspective of passengers and operators. Reliability refers to the certainty that passengers have about the level of service they will experience while travelling [6]. Maintaining reliable service is important for both transit passengers and transit operators [7]. Travel time, waiting time, transfer time and comfort level experienced during the transit trips **are also some of the most important attributes of reliability** [8], **while punctuality and regularity are among the most important measures for evaluating public transport operations**. **Punctuality** is a feature consisting of a predefined vehicle arriving, departing or passing at a predefined point at a predefined time [9].

**In practice**, performance indicators are often estimated purely statistically by practitioners over several months or years of data. This method provides a relatively consistent picture of the past behaviour of bus lines with low modelling effort and computational cost, but does not allow these indicators to be evaluated in different "what if?" scenarios (e.g. roadworks, new traffic priorities, etc.). **To face these challenges**, bus operators need efficient microscopic bus

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lines simulation models to evaluate the performance indicators of current lines and forecast indicators on potential developments of these lines.

Machine learning (ML), a branch of Artificial Intelligence (AI), involves using algorithms to enable systems to learn from data and make predictions or decisions, emulating aspects of human learning. ML and simulation have an area of intersection, namely machine learning-assisted simulation, describing the integration of ML into simulation [10]. Performing ML and simulation in the same framework aims at improving the quality of simulation results to some extent. However, incorporating ML techniques into the simulation model tends to make the overall framework more complex and very time-consuming.

In this paper, to couple ML models trained on actual bus data with a microscopic transit simulation model, we propose two strategies: an online strategy with more precise but time-consuming ML models, and an offline strategy that is less time-consuming but with approximated ML results. The accuracy and performance of the resulting coupled models will be evaluated using a case study based on real-world data provided by an operator. This evaluation will include an analysis of travel time day-to-day and period-to-period variability and punctuality performance indicators. In addition, a discussion on the advantages and limitations of each coupling strategy will be conducted.

The remainder of this article is structured as follows: section 2 reviews related literature, including travel time variability and prediction, traffic simulation models, as well as the coupling of ML with simulation models. Section 3 provides an overview of the proposed framework for coupling ML and microscopic simulation framework, describes and illustrates the two suggested coupling strategies in detail. A case study scenario will be described in section 4. In section 5, the simulation results will be analyzed and validated based on a set of performance indicators. A discussion of the analyses will be presented in section 6 and some concluding remarks in section 7.

## 2. Literature Review

### 2.1. Travel Time Variability and Prediction using Machine Learning

Travel time variability (TTV), also known as travel time uncertainty, is the key indicator for measuring the performance of the transport system, and can be divided into three distinct components: day-to-day variability, variability over the course of a day and vehicle-to-vehicle variability [11]. Research emphasizes day-to-day variability, which describes the degree of variation in travel time for a trip taking the same route over a specific period [12]. TTV importance can be seen from the standpoint of operators and passengers. From the operators' point of view, high TTV leads to poor performance of the transport system. This could therefore lead to a loss of passengers and thus revenue for transport operators. From a passengers' perspective, travelers expect that the transport system travel time should not exceed the average or scheduled time by more than an acceptable amount. [13].

Probabilistic distributions are capable of describing the nature and the pattern of TTV. Understanding travel time distributions and their components is a prerequisite for reliability analysis. Appropriate choice of travel time distribution is an essential element for efficient microscopic simulations of transportation and transit systems, as well as for predicting travel time and modeling discrete choices in route selections [14]. Various studies have made considerable effort to fit travel times using different types of distributions, such as normal [15], lognormal [16; 17; 18; 19; 20], gamma [21; 22], Weibull [23], Burr [24; 25], Generalized extreme value (GEV) distribution [26], Gaussian Mixture Model [27]. Such modelling aimed to find the best statistical distribution to describe and explain the shape and the pattern of TTV, because a distribution fitted to travel time values could illustrate a more comprehensive nature of the TTV [13].

Estimated Time of Arrival (ETA), also known as expected time of arrival, is the time at which a transportation system is expected to arrive at its destination. A number of works have been devoted to predicting ETA [28; 29; 30; 31; 32; 33; 34; 35; 36]. Moreover, ML techniques have been widely reported for travel time prediction, due to their ability to solve complex problems and extract patterns. A number of ML approaches have been widely implemented to predict the estimated bus arrival time [37; 38; 39; 40; 41; 42; 43; 44] and bus travel time [45; 46; 47; 48; 49; 50; 51; 52].

### 2.2. Traffic Simulation Models

Traffic simulation can be defined as the mathematical model of transportation systems, implemented through the application of dedicated computer software. They can be divided according to the level of details provided into microscopic and macroscopic traffic simulation models. Microscopic traffic simulator focuses on the movement of

66 each individual entity in the system. They provide a detailed picture of each individual vehicle including: location,  
67 time and speed [53]. These models are very effective in assessing heavily congested conditions. However, they  
68 are time-consuming, costly, and can be difficult to calibrate. Macroscopic traffic simulators rely on deterministic  
69 relationships between traffic flow, speed and density. They are originally developed to model traffic within specific  
70 transportation sub-networks, such as freeways and rural highways [54].

71 Over the past decades, a number of traffic simulation frameworks have been developed, among which:

- 72 • *TRANSIMS* developed at Los Alamos National Laboratory (USA) is an integrated set of tools for performing the  
73 analysis of a regional transportation system based on a cellular automata microscopic simulation model [55];
- 74 • MIT (Massachusetts Institute of Technology) developed *MITSIMLab*, an open-source microscopic traffic sim-  
75 ulator that evaluates the impacts of alternative traffic management systems, public transport operations and  
76 various strategies at the operational level [56];
- 77 • *MATSim* (Multi-Agent Transport Simulation) developed by ETH Zurich, is a major open-source framework,  
78 used to implement large-scale agent-based transport simulations, it is highly modular, allowing a very high  
79 level of customization [57];
- 80 • *SUMO* (Simulation of Urban MObility) was developed at the German Aerospace Centre. It is a microscopic  
81 multi-modal traffic simulator capable of simulating different types of traffic data, in which vehicles, public  
82 transport and persons are modeled explicitly [53];
- 83 • *Starling*, an agent-based simulation software, proposed by Leblond et al.[58], was developed as a generic frame-  
84 work to deal with spatial issues of territories. The simulation framework is designed to evaluate a specific  
85 mobility service.

### 86 2.3. Machine Learning and Simulation Models

87 The fields of ML and simulation have an intersecting area, which can be divided into three subfields: 1) Simulation-  
88 assisted machine learning describes the integration of simulation into ML; 2) Machine-learning assisted simulation  
89 describes the integration of ML into simulation; and 3) A hybrid combination describes a combination of ML and  
90 simulation with a strong mutual interaction [10].

91 In recent years, several works have opted for simulation-assisted machine learning, including an approach using  
92 unsupervised ML algorithms to automatically detect repetitive patterns in a program's execution, to reduce costly  
93 simulation time without significant loss in accuracy [59]. Shafizadeh et al.[60] coupled ML techniques including  
94 SVM, ANNs, tree-based models and statistical models with cellular automata to simulate urban growth in the city  
95 of Tehran. Elbattah et al.[61] proposed a framework incorporating simulation modeling along with ML to design  
96 pathways and assess the return on investment of implementation. Chabanet et al.[62] combined a computationally  
97 expensive simulator with a KNN classifier, which is less computationally costly to use online but whose predictions  
98 are only approximations of the simulator.

99 On the other hand, ML assisted simulations have been performed in a number of studies, including a proposed  
100 simulation framework to explore the effectiveness of different ML approaches in streamflow simulation for four rivers  
101 in the United States [63]. Yan et al.[64] proposed a method for coupling neural networks and numerical models to  
102 simulate and identify high-risk areas for urban flooding, as well as to predict water accumulation depths. The outputs  
103 of the simulation models are used to feed the neural network. Shahhosseini et al.[65] proposed an approach to couple  
104 a simulation model with ML techniques, incorporating simulation results into the ML models to enhance corn yield  
105 predictions in the US Corn Belt. Abdelaty et al.[66] used the simulated energy consumption scenarios to develop four  
106 different data-driven modelling techniques.

107 In the field of transportation, many studies have used simulation data and results to build ML models. Al Mamlook  
108 et al.[67] evaluated and compared different ML approaches to predict road accidents, based on driving simulation data.  
109 In another work, Sroczynski et al.[68] used the simulation results to develop and test ML models for traffic prediction.  
110 ML has also been implemented to assist traffic simulation models, among which can be cited Jiang et al.[69], that used  
111 unsupervised ML techniques for parameter calibration of a traffic simulation model. Ratrouf et al.[70] proposed a ML  
112 model-based calibration methodology for the PARAMICS model. Jang et al.[71] proposed a method for integrating

113 deep reinforcement learning into traffic simulation modeling. Daguno et al.[72] presented a method for calibrating  
 114 microsimulation models using artificial neural networks.

115 The use of frameworks combining ML models and public transportation simulators is still relatively underutilized.  
 116 Othman et al.[73] proposed a framework integrating neural network models into a public transport simulation model  
 117 to improve real-time supply based on multiple demand scenarios. First, a Multi-Layer Perceptron combined with a  
 118 Linear Regression model, trained on traffic data and weather information, was employed to predict congestion type,  
 119 duration, and associated travel delays. These predictions are then input into a simulator to model various scenarios,  
 120 with the goal of optimizing a scheduling plan in the most cost-effective manner possible.

#### 121 2.4. ML-Simulation Coupling

122 A framework for coupling ML and simulation model will mainly include four layers: a data layer, a ML layer, a  
 123 simulation layer and an evaluation layer. The coupling scheme depends on the nature of the coupling. In simulation-  
 124 assisted ML approaches: input data will be used to prepare datasets to train ML models, the generated ML models will  
 125 be used during the simulation, the results of which will be evaluated using key performance metrics. In ML-assisted  
 126 simulation approaches, the process begins by setting up and running the simulation scenario. The results from this  
 127 simulation are then used to create datasets for training ML models. These models are subsequently evaluated using  
 128 appropriate performance metrics. An overview of the ML coupling scheme is shown in Figure 1.

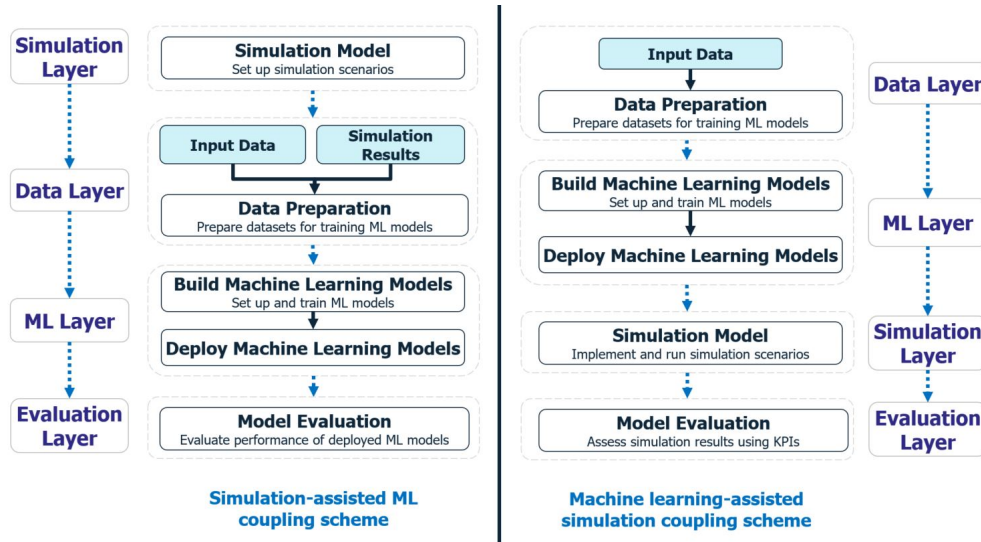


Figure 1: ML-Simulation coupling scheme

129 In the field of transportation, there might be a research gap related to the lack of methodology to couple ML and  
 130 microscopic models for public transport simulation. Although there is limited existing works on the topic, the cou-  
 131 pling process itself, including the exchange between ML and simulation layers, is briefly outlined in most studies. To  
 132 address this research gap, this work contributes to the literature by proposing and comparing two strategies for cou-  
 133 pling ML with a public transport simulation model. We refer by *online* the coupling strategy in which the ML models  
 134 will provide PT simulation model with bus travel times, the two *exchanging* directly via a request-response process.  
 135 On the other hand, we refer by *offline* the coupling strategy in which the simulation model will not directly exchange  
 136 with the ML models, but will only have access to the resulting outputs of ML models. In other microscopic traffic  
 137 simulation works, online/offline strategies refer to online/offline learning, while in this study we refer to online/offline  
 138 coupling. In other words, whether a ML is accessible (online) or not (offline). In offline coupling, the results of ML are  
 139 integrated (loaded) as input into the simulation model. It is also interesting to evaluate the accuracy and performance  
 140 of the simulation model and to understand to what extent each of the coupling strategies can be applied. An overview  
 141 of a proposed framework for coupling ML and public transport simulation model is given in Figure 2.

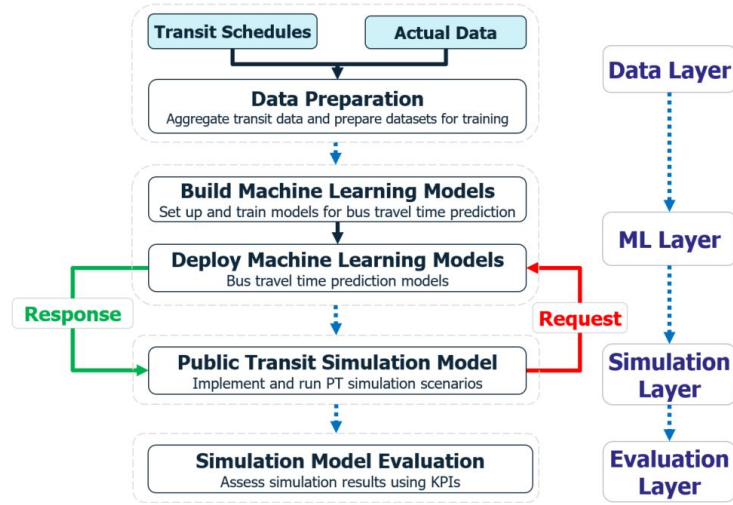


Figure 2: An overview of a framework for coupling ML and public transport simulation models. It consists of four layers: **Data layer**, in which transit schedules and actual data are used to generate aggregated datasets. **ML layer**, in which datasets will be first prepared, a ML model will be set up, then trained for bus travel time prediction, and finally deployed. **Simulation layer**, in which a simulation scenario is implemented and then simulated, in which travel times are estimated by ML models following a request-response process. **Evaluation layer**, in which the simulation will be evaluated using a set of KPIs

Reference	Simulation-Assisted ML	ML-Assisted Simulation	Transportation	Public Transport	Travel Time Prediction	Travel Time Variability	Description
Abdelaty et al.[66]	x						ML prediction models for battery-electric bus energy consumption in transit
Al Mamlook et al.[67]	x		x				ML to predict the freeway traffic accidents-based driving simulation
Chabanet et al.[62]	x	x					Coupling digital simulation and ML metamodel
Daguano et al.[72]		x	x				Automatic calibration of microscopic traffic simulation models using ANNs
Elbattah et al.[61]		x					Designing care pathways using simulation modeling and ML
Hamerly et al.[59]	x						Using ML to guide architecture simulation
Jang et al.[71]		x	x				Agent-based simulation modeling with Deep RL for smart traffic signal control
Jiang et al.[69]		x	x				Parameters calibration of traffic simulation model based on data mining
Othman et al.[73]		x	x	x	x		ML aided simulation of public transport utilization
Ratrou et al.[70]		x	x				Calibration of PARAMICS model: Application of AI-based approach
Shafizadeh et al.[60]		x					Coupling ML, tree-based and statistical models with CA to simulate urban growth
Shahhosseini et al.[65]	x						Coupling ML and crop modeling improves crop yield prediction in the US Corn Belt
Sroczynski et al.[68]	x		x				Road traffic prediction: by ML equally effectively as by complex microscopic model
Tongal et al.[63]		x					Simulation & forecasting of streamflows: ML coupled with base flow separation
Yan et al.[64]	x						A prediction model of urban flood inundation: coupling ML and numerical simulation
Proposed work		x	x	x	x	x	ML-assisted microscopic PT simulation: two coupling strategies

Table 1: Comparative table of related works

142 In Table 1, We compare our proposed work with existing studies based on the following aspects: whether the  
143 framework is simulation-assisted ML or ML-assisted simulation, whether the focus is on transportation and public  
144 transport, and whether the work addresses TTV and prediction.



### 145 3. Methodology

146 In this section, the spatial and temporal components of transit bus route, as well as the data used, will be briefly  
147 presented. The proposed approach to couple ML and simulation models, including online and offline strategies, will  
148 then be explicitly detailed and illustrated on a real case application.

#### 149 3.1. Problem Statement

150 A transit bus travels from an origin to a destination, passing through a set of transit stops along the way. Spatial  
151 components can be grouped, according to their type. *Section* refers to the links between consecutive stops. *Segment*  
152 is made up of several consecutive sections. *Route* is formed by the join of all sections from an origin terminal to a  
153 destination terminal [74]. In order to maintain acceptable service reliability, bus operators set up control points along  
154 the bus route. Control points, also called timing points, are particular stops where bus departure times are subject to  
155 regulation or to meet a specific buffer time [8]. Additionally, timing points can be used to divide a transit route into  
156 segments. An illustration of the spatial components of bus routes is given in Figure 3.

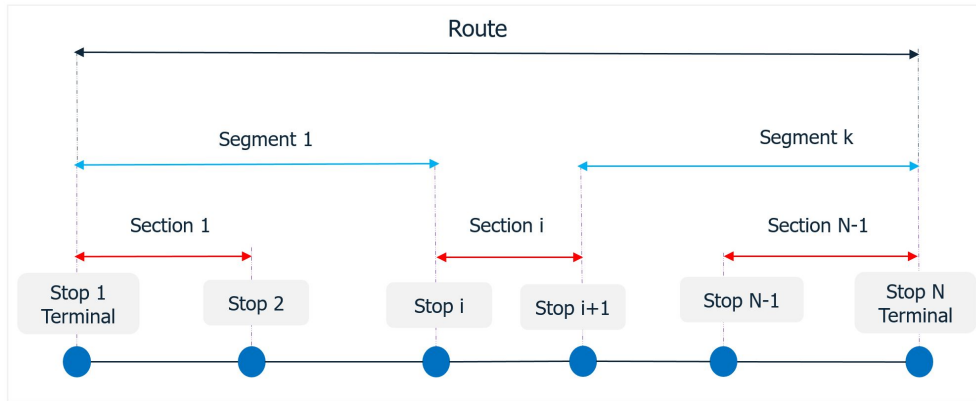


Figure 3: An illustration of the different spatial components of a transit line

157 The temporal components of bus routes can be divided into durations and time points. Travel time, dwell time, and  
158 running time are durations, while arrival time and departure time at bus stops are specific points in time. Travel time  
159 consists of both dwell time and running time. Dwell time refers to the period during which a bus remains stationary  
160 at a scheduled stop, while running time refers to the period during which a bus is in motion between two stops.

161 Depending on the level of detail, operating times can be categorized as follows:

- 162 1. **Section travel time:** This corresponds to the dwell time and running time between successive stops within a  
163 specific section.
- 164 2. **Segment travel time:** This refers to the sum of the travel times for all sections within the segment under  
165 consideration.
- 166 3. **Route travel time:** This refers to the total travel time from the first stop to the last stop.

167 Figure 4 provides an illustration of the temporal components of bus lines at the section level.

168 In this study, the data used consist of: 1) **Transit schedules**, grouped by transit line (e.g., bus line) and formatted  
169 as *GTFS* (General Transit Feed Specification) tables [75]; and 2) **Actual data**, structured similarly to a *GTFS* stop  
170 times table, providing information on transit trips during a specified period of the year, including date, vehicle ID, the  
171 corresponding trip, and actual stop times. The latter are recorded from GPS trackers on transit vehicles at each stop.  
172 Therefore, scheduled and actual stop times can be mapped in the same data structure based on mutual attributes (e.g.,  
173 trip ID and stop ID).

174 Next, the actual observations, which are originally available at the stop level, can be transformed to the section  
175 and segment levels. This transformation aims to mitigate the impacts of imprecise stop times, which are susceptible

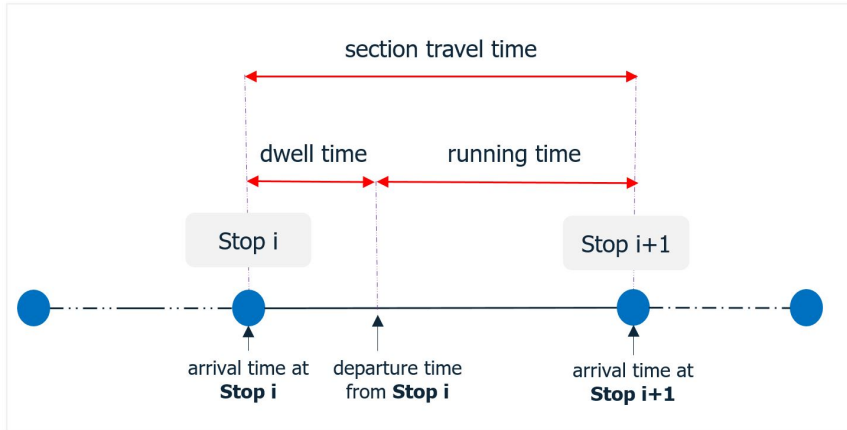


Figure 4: An illustration of the different components of travel time between two transit stops

176 to measurement errors that can adversely affect the quality of ML models. The components of the bus route, as well  
 177 as the stop and travel times of a bus trip, aggregated at the stop, section, and segment levels, are shown in Figure 5.

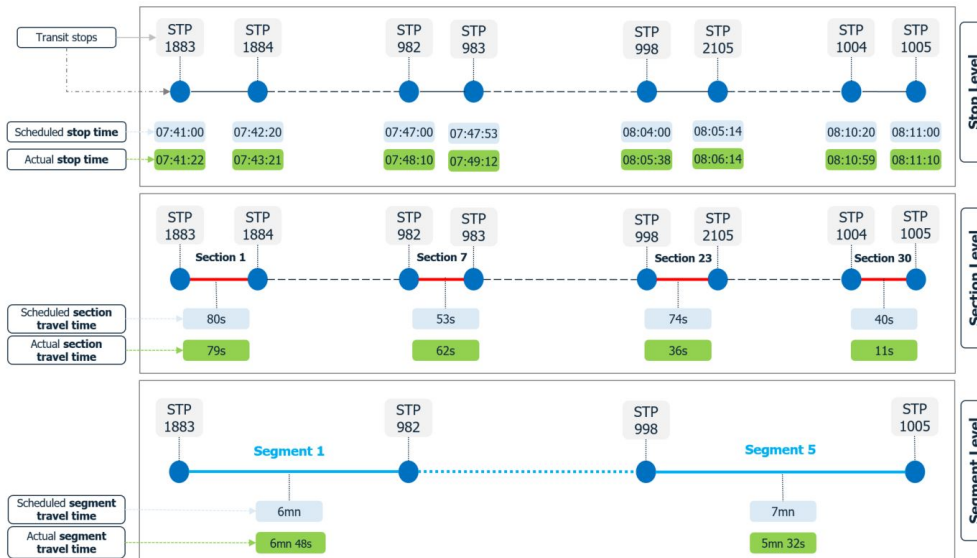


Figure 5: An illustration of the components of a bus route with stop and travel times

### 178 3.2. Coupling ML and Simulation Models

179 Before outlining the proposed approach to couple ML and public transport simulation model within the frame-  
 180 work, an overview of a generic traffic simulation model *Starling* [58] will be given. It combines an agent-based  
 181 framework and a discrete-event approach, it is a microscopic model for mobility simulation. Its aim is to provide  
 182 a basis for the development of computer models for the simulation of specific transportation systems, consisting of  
 183 generic simulation classes that can be extended to match the specifications of the system being simulated.

#### 184 3.2.1. Coupling Approach: Overview

185 The developed coupling approach was designed in order to provide public transport simulation model with more  
 186 realistic travel times, based on historical data via ML models. It consists of three entities: traffic simulation model, the



187 deployed ML models and a ML interface which ensures the exchange between the simulator and the ML models. Ad-  
 188 ditionally, in order to perform transit simulation, scenario data and operator parameters will be added to the simulator  
 189 inputs. An overview of a generic simulation model coupled with deployed ML models is shown in Figure 6.

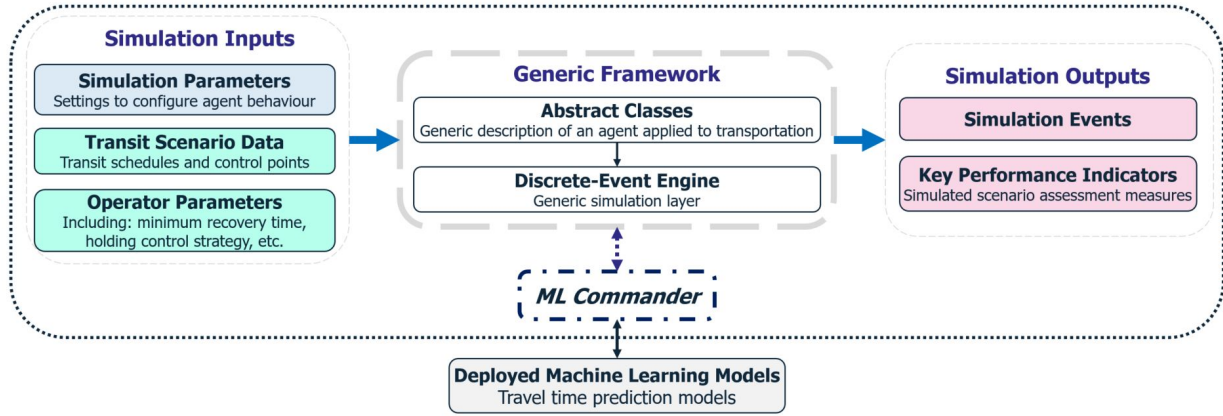


Figure 6: An overview of coupling a generic framework with ML models. It consists of two blocks: the block below groups the ML models deployed for travel times prediction; the block above refers to the simulation framework, its parameters, the scenario data as well as the operator parameters, and in addition to a ML interface (commander) which ensures the exchange between simulator and ML models

190 From a technical point of view, the simulator iterates through the transit trips *one by one*, uses the input control  
 191 points to split the trip route into segments, and applies a specific process to simulate the travel segments. In essence,  
 192 at each control point, the simulated bus requests its next segment travel time by providing the ML interface with the  
 193 route segment and simulation information. The ML commander, on the other hand, selects the most suitable model  
 194 for the requested route segment based on the request information provided. The chosen model will then predict and  
 195 return the travel time of the corresponding segment based on the simulation information. Finally, the ML interface  
 196 will prepare a response and send it back to the simulator. An overview of the coupling process is shown in Figure 7.

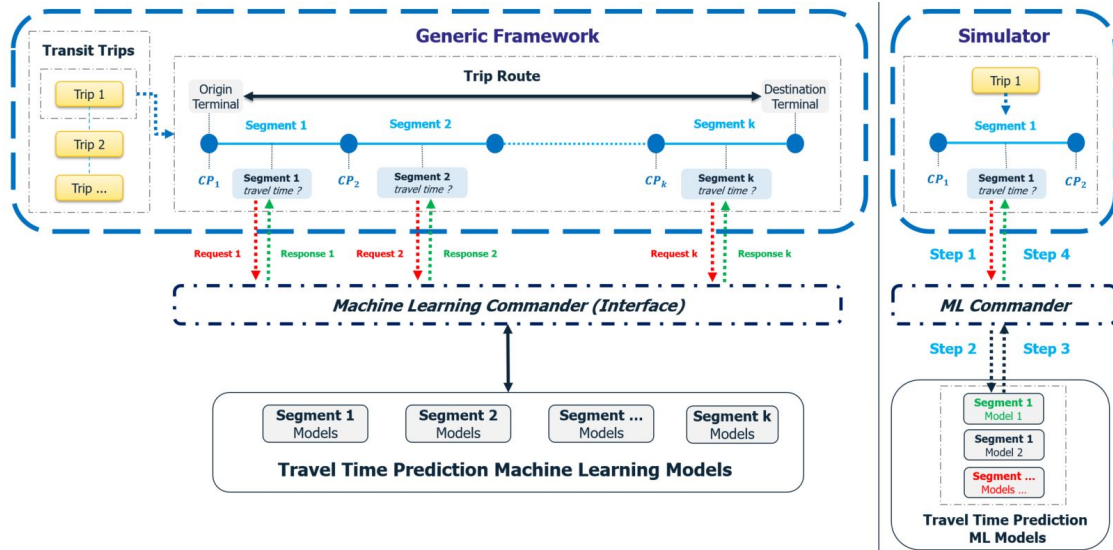


Figure 7: An overview of the proposed coupling process. The simulation model proceeds on trip-by-trip, dividing the trip route into segments according to the defined control points (CPs). At each control point, the travel time of the next segment is estimated through a request-response process. Step1: The simulator requests the segment travel time. Step2: The ML controller selects the appropriate ML model for travel time prediction based on the request information. Step3: The selected model predicts the travel time using the provided information and sends the prediction back to the ML controller. Step4: The ML controller prepares an appropriate response and sends it back to the simulator.

197 3.2.2. Coupling Approach: Online Strategy

198 In this section, the coupling process will be described in more detail. At this stage of the work, a technical  
199 concept that requires further explanation is the simulator request. It consists of three components: 1) Route segment  
200 information, including attributes such as transit line, origin, and destination stops of the route segment, which will be  
201 used to select the corresponding ML models for travel time prediction; 2) Simulation information, including attributes  
202 such as time of day and stop delay, will be mainly used by the selected ML model to predict the travel time of the  
203 corresponding segment; 3) The data type variable refers to the type of response data, which may be a single value,  
204 such as a mean value, or a probabilistic distribution, such as a normal distribution. An example simulator request is  
205 shown in Figure 8.

```
<?xml version="1.0" encoding="UTF-8"?>
<request>
  <route_segment>
    <feature attribute = "transit_line" value = "A" />
    <feature attribute = "from_stop" value = "STP-1883" />
    <feature attribute = "to_stop" value = "STP-982" />
  </route_segment>
  <simulation_info>
    <feature attribute = "time_of_the_day" value = "07:41:50" />
    <feature attribute = "stop_delay" value = "00:00:50" />
  </simulation_info>
  <data_type value = "normal" />
</request>
```

Figure 8: An example of a simulation request, consisting primarily of a route segment and simulation information

206 The coupling process is performed in several steps as follows:

- 207 • The simulator prepares a request and transfers it to the ML interface, including the transit route segment, the  
208 simulation information, and the data type of the predicted values.
- 209 • The ML commander will use the different request information to find the most suitable ML model. This selec-  
210 tion process is carried out in three stages:
  - 211 – In the first stage, the ML interface retrieves the deployed ML models from the model database, which  
212 match the request segment information. For the sake of simplicity, we assume that there is at least one ML  
213 model deployed for each requested route segment.
  - 214 – In the second stage, among the retrieved models, the ML models built with mutual features related to the  
215 simulation information are selected.
  - 216 – In the third stage, the selected deployed models will be compared using evaluation metrics, such as the  
217 coefficient of determination  $R^2$ . The best-fit model will then be chosen by the ML commander to predict  
218 the travel time of the requested segment.
- 219 • Next, the chosen model for the travel time prediction will use the simulation information as the test dataset,  
220 apply the prediction and then return the corresponding travel time parameters to the ML interface.
- 221 • Subsequently, a response will be prepared by the ML commander using the parameters received. Depending on  
222 the type of the request, specific processes will be applied to distinguish two cases: 1) the predicted travel time if  
223 the requested result is a single value; 2) the parameters of the probabilistic distribution, which can be extracted  
224 by fitting the corresponding dataset of the predicted travel time to the requested law.
- 225 • Finally, the prepared response will be sent back to the simulator, including the requested parameters.

226 Figure 9 schematically illustrates the different steps of the coupling process.  
227 In the remainder of the paper, we refer to the ML model as the regression tree model.

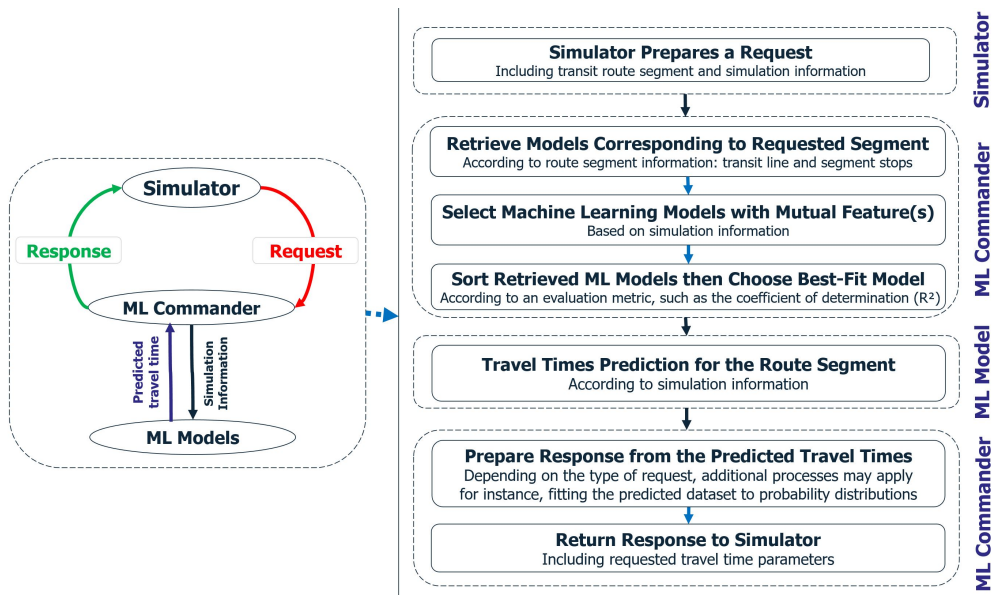


Figure 9: A detailed view of the proposed coupling process. (Left): an illustration of the request-response process, simulator prepares and sends a request to the ML commander, this latter provides the ML models with request simulation information, which will be used to predict the travel time, and this will be returned in response to the simulator afterwards. (Right): coupling process - steps

228 **Travel time prediction by the ML model and response preparation by the ML interface**, the most important steps in  
 229 the coupling process, are presented as follows. First, the simulation information, consisting of a set of feature values,  
 230 will be used to retrieve the appropriate decision rule, and hence the associated travel time. From a technical point  
 231 of view, an ML test dataset will be built by matching the ML model features with the simulation values, and will  
 232 then be used to predict the corresponding decision rule, and therefore the segment travel time. Second, the dataset  
 233 corresponding to the selected decision rule will be retrieved from the original data. As stated above, depending on the  
 234 type of the request, the response may take the form of a single value or a distribution. In the first case, the average  
 235 travel time of the observations will be retained. In the second case, the observations will be fitted with the requested  
 236 probability law, and the latter parameters will be estimated. Finally, the estimated travel time parameters will be  
 237 returned to the simulator. An overview of the coupling process with a focus on travel time prediction and response  
 238 preparation, with the regression tree as the ML model, is shown in Figure 10. In the presented coupling approach, the  
 239 simulator and ML models exchange simultaneously via the ML interface. Therefore, in the remainder of this paper,  
 the proposed approach will be referred to as the *online strategy*.

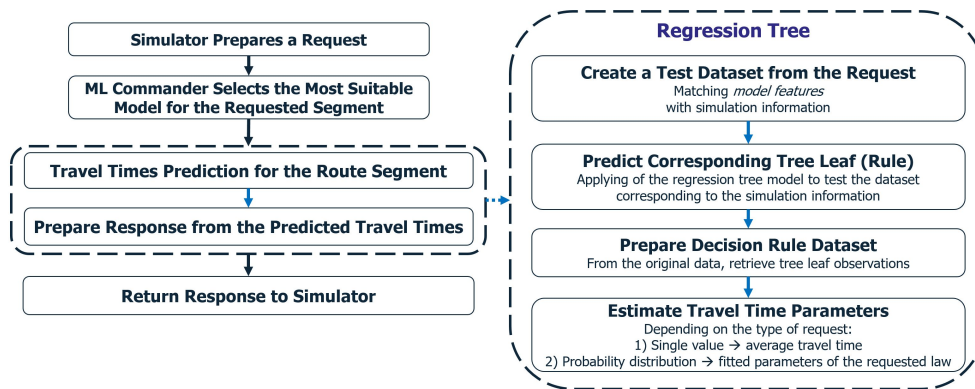


Figure 10: Coupling process - regression tree - the focus is on the stages of predicting travel times and preparing the response

240 3.2.3. Coupling Approach: Offline Strategy

241 Running a simulation scenario with an online strategy may seem time-consuming because, for each simulation  
 242 request, a ML model must be selected and then used to predict the segment travel time. To address the drawbacks of  
 243 the online strategy, an offline coupling strategy is proposed in this section. It aims to run simulation scenarios using  
 244 approximated segment travel times rather than overusing deployed ML models. In the offline coupling approach, a  
 245 pre-simulation is first performed, using ML models to create a table of segment travel times, and then integrating  
 246 the generated table into the framework coupling as part of the ML commander. An overview of the offline coupling  
 247 strategy is presented alongside the online strategy in Figure 11.

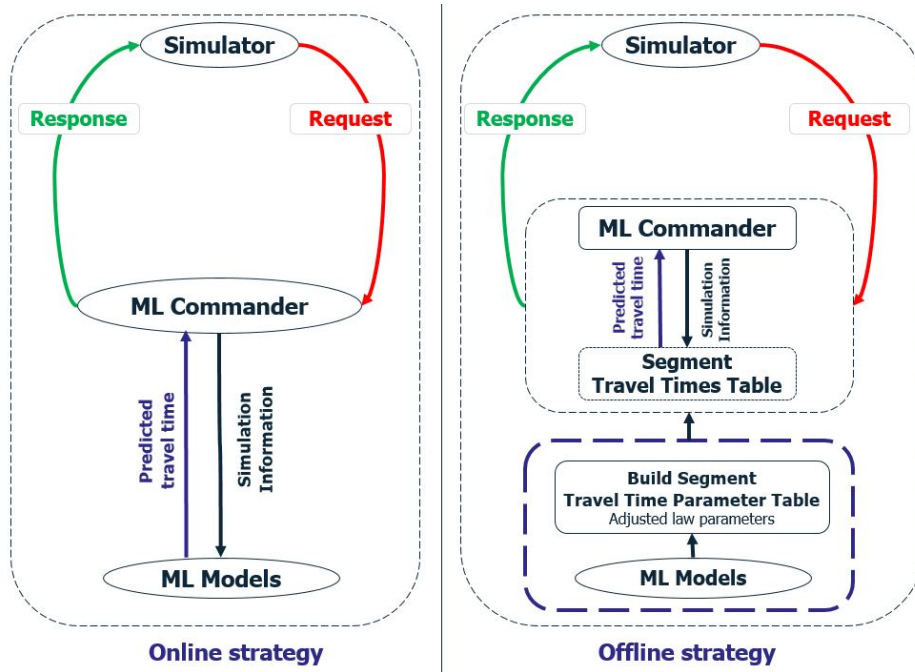


Figure 11: An overview of coupling strategies with emphasis on the request-response process. For the offline strategy, a table with approximate travel time parameters will first be built based on deployed ML models, integrated into the ML interface, and then used to simulate travel times during the request-response process

248 To build the segment travel time parameter table, the following process will be applied. First, based on a set of  
 249 features and an evaluation metric, the best-fit deployed ML model will be retrieved for each route segment. Second, a  
 250 dataset consisting of the actual observations corresponding to each decision rule of the selected model will be prepared.  
 251 Third, the travel time parameters of the decision rules will be estimated. This involves adjusting the corresponding  
 252 observed travel times of each decision rule to the chosen probability law. An overview of generating a table of segment  
 253 travel time parameters based on deployed ML models is depicted in Figure 12.

254 The presented offline strategy travel times table is built according to the set of decision rules (a set of feature  
 255 values). A second alternative for estimating a segment's travel time parameter table can be derived based on static  
 256 time periods (e.g., in 15-minute increments) corresponding to a temporal attribute (e.g., stop time). Therefore, the  
 257 process of generating the segment travel time parameter table for the second variant is given as follows. First of all,  
 258 and similarly to the first offline variant, the ML model best suited to the corresponding segment  $s \in S$  will be selected.  
 259 Next, the selected model rules will be filtered, and only a set of rules  $R$  corresponding to the time period  $t \in T$  will  
 260 be kept. The fitted parameters of the chosen law will then be estimated for each decision rule  $r \in R$ . Next, for each  
 261 selected decision rule  $r \in R$ , a weight value  $w_r$  for period  $t$  will be estimated according to Equation 1. Finally, the law  
 262 parameters per time period  $t \in T$  will be estimated according to Equation 2.

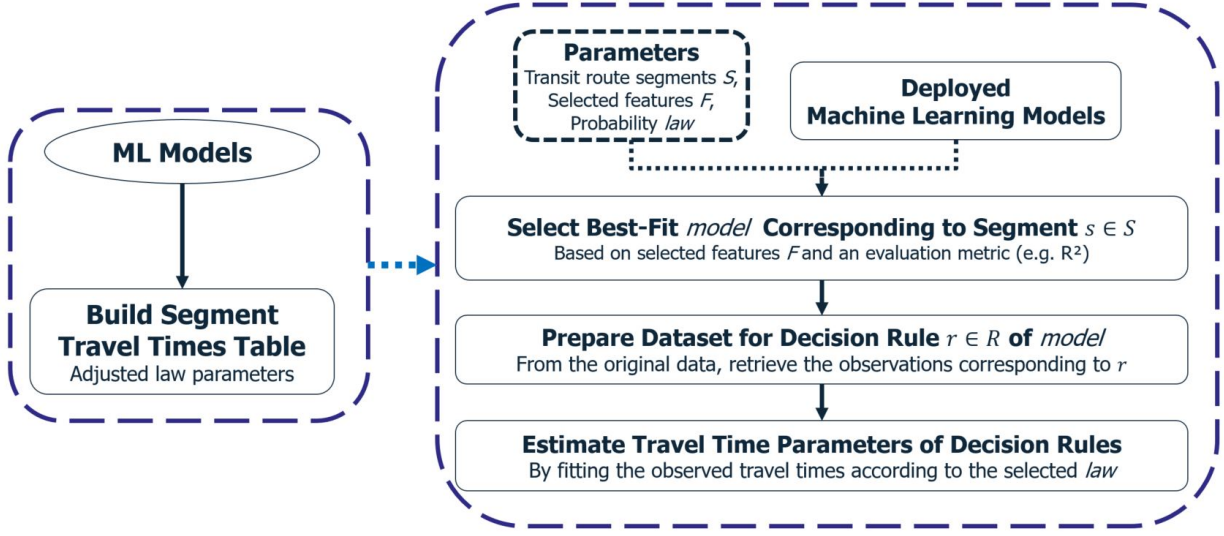


Figure 12: An overview of the building segment travel time parameter table process

$$w_r^t = \frac{|t \cap r_{time\_att}|}{|t|} \quad (1)$$

Where:

- $|t|$ : is the absolute duration of a time period  $t$
- $r_{time\_att}$ : refers to the selected *time attribute* numeric range in which a decision rule  $r$  is satisfied
- $w_r^t$ : is the estimated weight of rule  $r$  for time period  $t$

$$P_i^t = \sum_{r \in R} P_i^r \cdot w_r^t \quad (2)$$

Where:

- $P_i^t$ : refers to the estimated value of the law parameter  $i$  of the time period  $t$
- $P_i^r$ : refers to the estimated value of the law parameter  $i$  of the decision rule  $r$

The normal distribution has been widely used to estimate TTV [15; 14; 76]. An application of Equation 2 according to the normal law is formulated in Equation 3.

$$\begin{aligned} \mu^t &= \sum_{r \in R} \mu^r \cdot w_r^t \\ \sigma^t &= \sum_{r \in R} \sigma^r \cdot w_r^t \end{aligned} \quad (3)$$

Where:

- $\mu$  and  $\sigma$  refer to the mean and standard deviation parameters of the normal distribution, respectively.

An overview of the updated process for estimating travel time parameters with static time periods is presented in Figure 13.



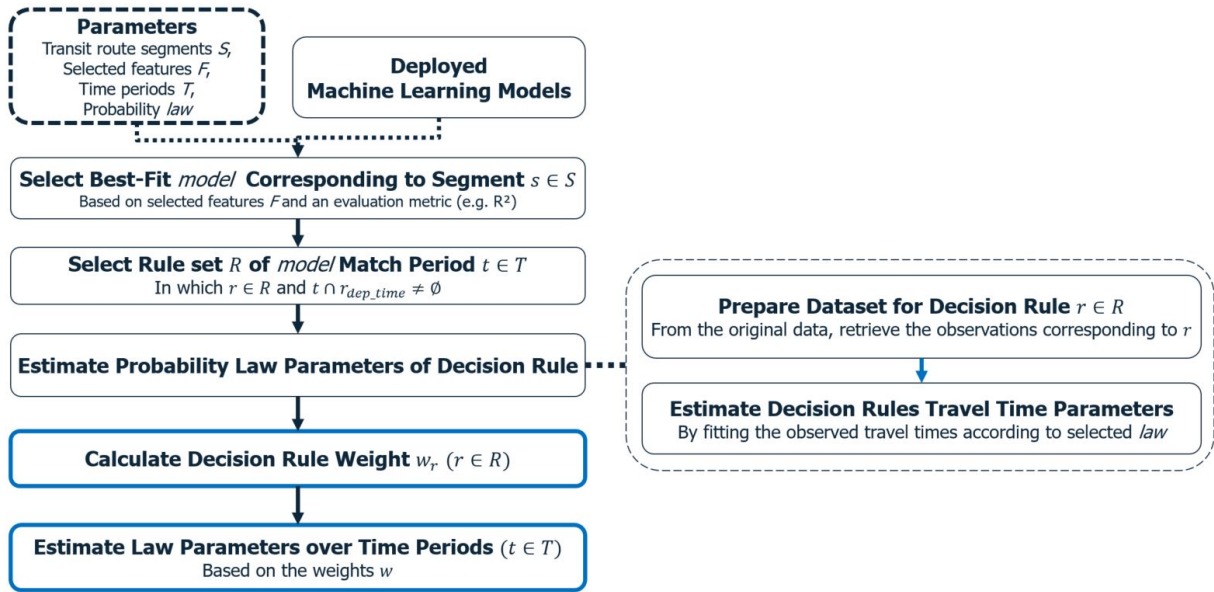


Figure 13: An overview of the process of estimating travel time parameters based on static periods. The process iterates through each of the route segments and time periods, selects the best-fit segment ML model, retrieves and estimates the corresponding decision rules and their travel time parameters, respectively. Finally, the rule weights will be calculated and then used to deduce the corresponding law parameters over static time periods

274 After detailing the process of building the segment travel times table, the next step in the offline strategy is to  
 275 update the request-response process, as follows. First, the simulator prepares its request in the same way as in the  
 276 online strategy. Then, the ML commander uses the simulation information along with the route segment to retrieve the  
 277 corresponding travel time parameters from the created table. Finally, the ML commander prepares its response and  
 278 sends it back to the simulator in the same way as in the online strategy. An overview of the offline request-response  
 279 process is shown in Figure 14.

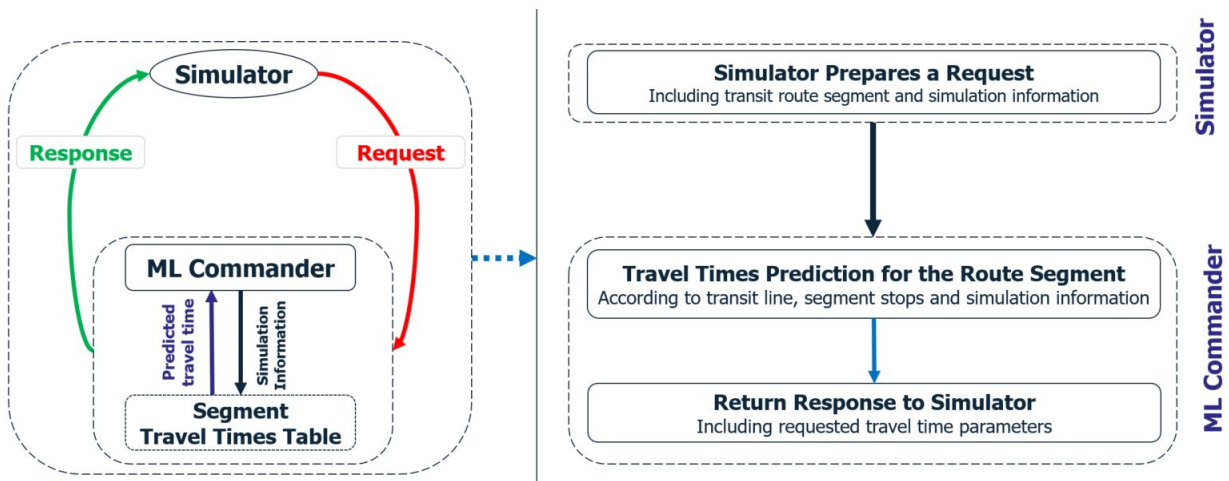


Figure 14: An overview of the request-response for offline coupling strategy. (Left): Overview of the process. (Right): Process steps



280 3.3. Coupling ML-Simulation: Illustrations

281 3.3.1. Online Strategy: Illustration

282 In this section, the application of the described coupling process applied on the first route segment of an any-  
 283 nymous French urban bus line referenced as A, will be detailed in the following. The selected transit route and its bus  
 284 stops are shown in Figure 5. An overview of the coupling framework applied on the chosen route segment is shown  
 285 in Figure 15.

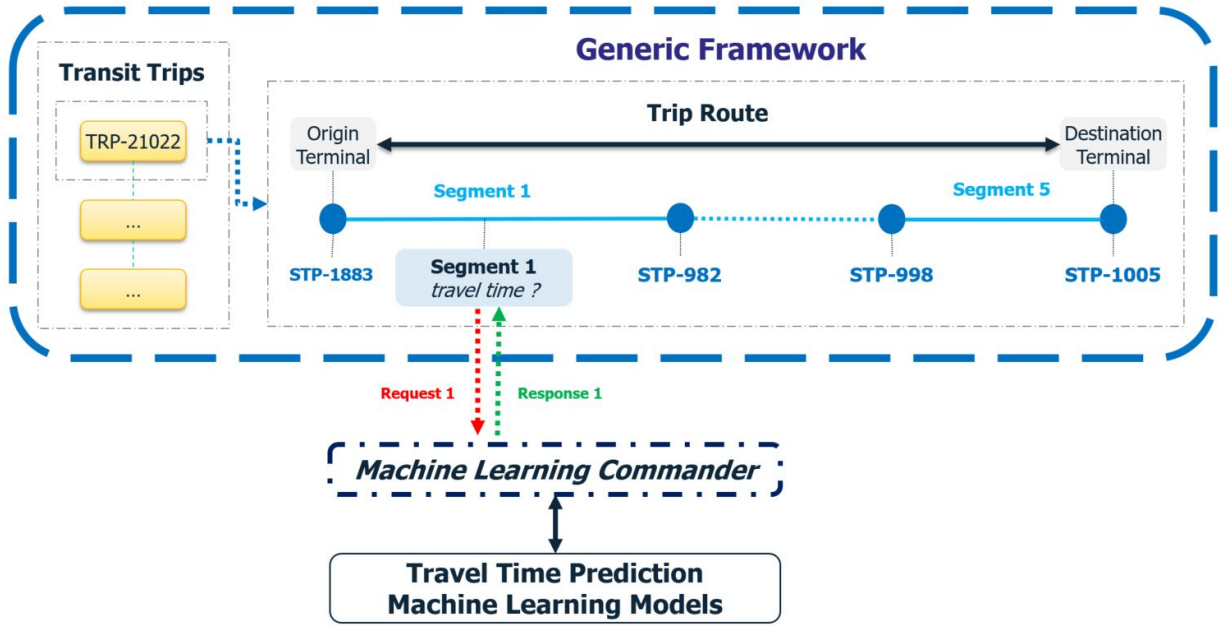


Figure 15: An overview of the coupling framework on a real case application: an anonymous French urban bus line

286 The first step in the coupling process is preparing the request, which includes: the type of the request, route  
 287 segment information, and simulation information, the latter including the stop time of the simulated bus and its delay  
 288 at the stop. An illustration of a simulator request is shown in Figure 8. At this point, it should be noted that the request  
 289 type, which defines the type of the travel time data returned, will be discussed in more detail below.

290 Next, the ML commander receives the request from the simulator and processes it in three stages. In the first  
 291 stage, the segment route information from the request will be used to filter the indexed models. Therefore, the models  
 292 corresponding to the transit line A, with STP-1883 as the origin and STP-982 as the destination, will be retrieved.  
 293 These models are presented in Table 2.

key	algorithm	transit line	from stop	to stop	input features	model target	score (R <sup>2</sup> )
68dsfnr6	RT	A	STP-1883	STP-982	stop time	real travel time	36%
frvcc9fb	RT	A	STP-1883	STP-982	stop time	real travel time	35%
...	...	...	...	...	...	...	...
cq5x4ddu	RT	A	STP-1883	STP-982	stop time;stop delay	real travel time	36%
73p81dxi	RT	A	STP-1883	STP-982	stop time;stop delay	real travel time	35%

Table 2: A sample of the indexed models with a focus on the selectable route segment models (in bold)

294 In the second stage, the *time of the day* and *stop delay* attributes will be used to match the suitable ML models.  
 295 Therefore, ML models without mutual attributes will be dismissed. It is worth noting that request attributes with the  
 296 same meaning to model input features will be updated. For instance, *stop time* and *time of the day* are two feature  
 297 attributes with the same meaning. The matched and dismissed models are given in Table 3.

key	algorithm	transit line	from stop	to stop	input features	model target	score (R <sup>2</sup> )
68dsfnr6	RT	A	STP-1883	STP-982	stop time	real travel time	36%
frvcc9fb	RT	A	STP-1883	STP-982	stop time	real travel time	35%
cq5x4ddu	RT	A	STP-1883	STP-982	stop time;stop delay	real travel time	36%
73p81dxl	RT	A	STP-1883	STP-982	stop time;stop delay	real travel time	35%

Table 3: A set of ML models from the indexed database matching the simulator request. (Black): ML models corresponding to simulation attributes. (Red): unselected ML models

298 In the third stage, the selection of the best-fit ML model will be based on evaluation metrics. In this study, the  
 299 coefficient of determination  $R^2$  is used as an evaluation metric and referenced by *score* attribute in the model index  
 300 database. Therefore, the selected ML model for travel time prediction, corresponding to the model with the the highest  
 301 score among the matched models, is given in Table 4.

key	algorithm	transit line	from stop	to stop	input features	model target	score (R <sup>2</sup> )
cq5x4ddu	RT	A	STP-1883	STP-982	stop time;stop delay	real travel time	36%

Table 4: The indexed model chosen for travel time prediction

302 Next, the selected regression tree model will be used to predict the travel time of the illustrated route segment.  
 303 A test dataset is built by matching the simulation information to the model input features, then used to select the  
 304 appropriate decision rule, ending with a tree leaf and hence the predicted travel time class. The test dataset, the  
 305 regression tree used, the rule selected, and its tree leaf are shown in Figure 16.

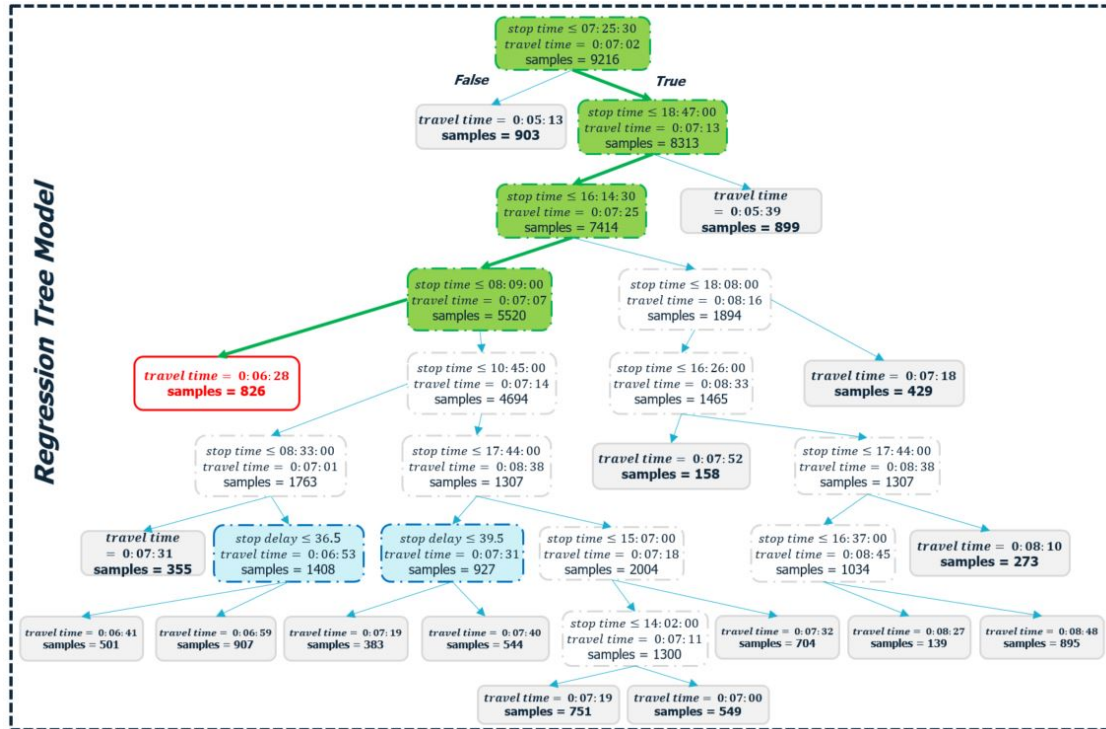


Figure 16: An illustration of applying the chosen regression tree model on the test dataset built on the simulation information. The green nodes constitute the selected path nodes corresponding to the predicted decision rule, the grey nodes are the terminal leaves of the tree, while the red node is the selected tree leaf containing the predicted travel time variable value. On the other hand, white nodes and blue nodes refer to stop time and delay conditions respectively

306 The last step in the coupling process is the preparation of a response from the predicted travel time. In order to  
 307 prepare this last response, the selected decision rule observations will be retrieved from the segment's original dataset.  
 308 Depending on the type of request, two responses are to be considered: 1) Single value request, in which the predicted  
 309 value is the average travel time of the retrieved observations; 2) Probability distribution request, in which the retrieved  
 310 observations are fitted to the requested probability distribution. The parameters of the fitted law will therefore be  
 311 returned. The prepared response, depending on the request type, is shown in Figure 17.

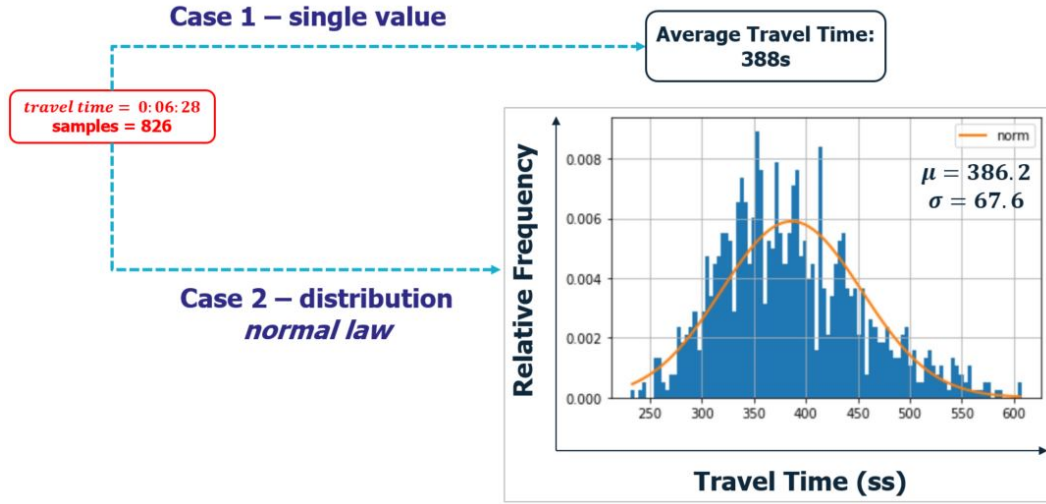


Figure 17: An illustration of the responses prepared based on the type of request. 1) The predicted value is the average travel time of the sample observations. 2) The relative frequency of the retrieved observations is shown, along with the normal law density function requested and its parameters: mean ( $\mu$ ) and standard deviation ( $\sigma$ )

### 3.3.2. Offline Strategy: Illustration

312 After illustrating an application of the request-response process using the online coupling strategy, [this section](#)  
 313 [presents an illustration of the offline strategy](#). It is carried out in two stages: First, the table of segment travel time  
 314 parameters, estimated based on the deployed ML models, will be [provided](#); Second, a detailed illustration of a request-  
 315 response process will be [given](#). The offline strategy will be applied to the same route segment and simulator request  
 316 shown in the previous section.

317 To build the segment travel time parameter table, a number of parameters need to be initialized. As stated above,  
 318 the illustration will take place on the first route segment with *STP-1883* as the origin and *STP-982* as the destination.  
 319 Depending on the offline strategy variant, the following parameters are initialized as follows. For the first variant, the  
 320 attributes *stop time* and *start delay* are considered as selected features; the distribution chosen is the *best-fit*, which  
 321 corresponds to the probability law best suited to the appropriate ML models. For the second variant, the *stop time*  
 322 attribute is considered as the selected feature; the normal distribution is the chosen law, while the time periods are  
 323 increments of 15 minutes. The best-fit deployed models selected to create the segment travel time parameter tables  
 324 are given in Table 5, while the two built segment travel time parameter tables are presented in Table 6 and Table  
 325 7, respectively. More details on the travel time parameter tables, as well as the distribution laws, are presented in  
 326 [Appendix A](#).

key	algorithm	transit line	from stop	to stop	input features	model target	score (R <sup>2</sup> )
cq5x4ddu	RT	A	STP-1883	STP-982	stop time;stop delay	real travel time	36%
68dsfnr6	RT	A	STP-1883	STP-982	stop time	real travel time	36%

Table 5: Selected best-fit deployed ML models from the model database. Depending on the offline strategy variant: for the first variant (in black); for the second variant (in blue).

transit line	segment from stop	segment to stop	feature values	probability law	parameter values
...	...	...	...	...	...
A	STP-1883	STP-982	$07:25:30 \leq \text{stop time} < 08:09:00$	$\chi^2$	loc = 178.97; scale = 11.05; df = 18.83
A	STP-1883	STP-982	$08:09:00 \leq \text{stop time} < 08:33:00$	exponweib	loc = 113.78; scale = 231.19; a = 4.73; c = 1.96
A	STP-1883	STP-982	$08:33:00 \leq \text{stop time} < 10:45:00$ $\wedge \text{stop delay} < 37$	genextreme	loc = 388.95; scale = 70.80; c = 0.18
A	STP-1883	STP-982	$08:33:00 \leq \text{stop time} < 10:45:00$ $\wedge \text{stop delay} \geq 37$	$\chi^2$	loc = 200.05; scale = 11.13; df = 18.26
...	...	...	...	...	...
A	STP-1883	STP-982	$18:47:00 \leq \text{stop time} \leq 23:59:59$	genextreme	loc = 312.36; scale = 65.17; c = 0.16
...	...	...	...	...	...

Table 6: Segment travel time parameter table built for the first offline variant, with *stop time* and *start delay* as selected features and best-fit distribution as the chosen law

transit line	segment from stop	segment to stop	feature values	probability law	parameter values
...	...	...	...	...	...
A	STP-1883	STP-982	$07:30:00 \leq \text{stop time} < 07:45:00$	normal	$\mu = 384; \sigma = 66$
A	STP-1883	STP-982	$08:45:00 \leq \text{stop time} < 08:00:00$	normal	$\mu = 384; \sigma = 66$
A	STP-1883	STP-982	$08:00:00 \leq \text{stop time} < 08:15:00$	normal	$\mu = 404; \sigma = 70$
...	...	...	...	...	...
A	STP-1883	STP-982	$18:45:00 \leq \text{stop time} < 19:00:00$	normal	$\mu = 432; \sigma = 92$
A	STP-1883	STP-982	$19:00:00 \leq \text{stop time} < 19:15:00$	normal	$\mu = 336; \sigma = 70$
A	STP-1883	STP-982	$19:15:00 \leq \text{stop time} \leq 19:30:00$	normal	$\mu = 336; \sigma = 70$
...	...	...	...	...	...

Table 7: Segment travel time parameter table built for the second offline variant, with *stop time* as the selected feature and normal distribution as the chosen law

328 After presenting the two segment travel time parameter tables, an illustration of the application of request-response  
329 process with the offline strategy will be given. An overview of the framework used with offline as a coupling strategy  
330 is shown in Figure 18.

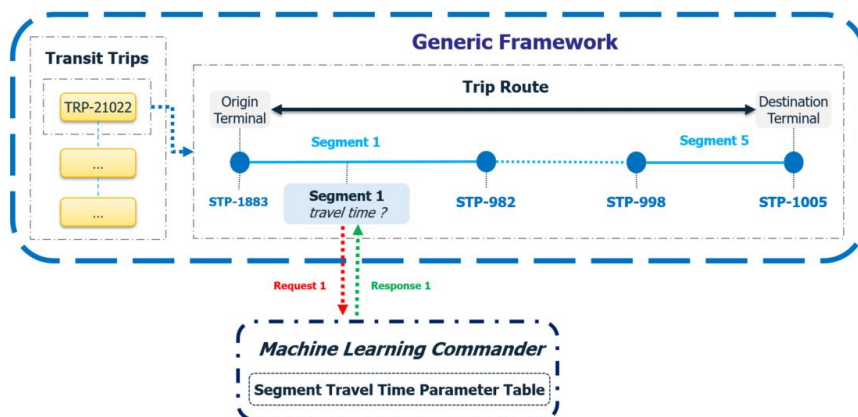


Figure 18: An overview of the framework used with offline as a coupling strategy: a real case of application for an urban bus line

331 Next, the simulation request presented previously (see Figure 15), will be prepared. Furthermore, in offline cou-  
 332 pling, the response is presented in the format of a distribution law with its associated parameters. Therefore, the data  
 333 type will no longer be included in the request. The updated request is shown in Figure 19.

```

  <?xml version="1.0" encoding="UTF-8"?>
  <request>
    <route_segment>
      <feature attribute = "transit_line" value = "A" />
      <feature attribute = "from_stop" value = "STP-1883" />
      <feature attribute = "to_stop" value = "STP-982" />
    </route_segment>
    <simulation_info>
      <feature attribute = "time_of_the_day" value = "07:41:50" />
      <feature attribute = "stop_delay" value = "00:00:50" />
    </simulation_info>
  </request>
  
```

Figure 19: Simulation request updated according to offline strategy

334 Based on the route segment and simulation information, the corresponding decision rule will be selected, by  
 335 matching the request information with the feature values of decision rule. The corresponding decision rules according  
 336 to the offline strategy variant are given in Table 8.

transit line	segment from stop	segment to stop	rule feature values	offline variant	parameter values
A	STP-1883	STP-982	$07:25:30 \leq \text{stop time} < 08:09:00$	first	law = $\chi^2$ ; loc = 178.97; scale = 11.05; df = 18.83
A	STP-1883	STP-982	$07:30:00 \leq \text{stop time} < 07:45:00$	second	law = normal; $\mu = 384$ ; $\sigma = 66$

Table 8: Decision rules selected based on offline variant

337 According to the matched decision rule, a response is prepared by the ML commander, including the corresponding  
 338 law along with its parameters. An illustration of the responses returned by the ML commander to the simulator,  
 339 depending on the offline variant, is shown side by side in Figure 20.

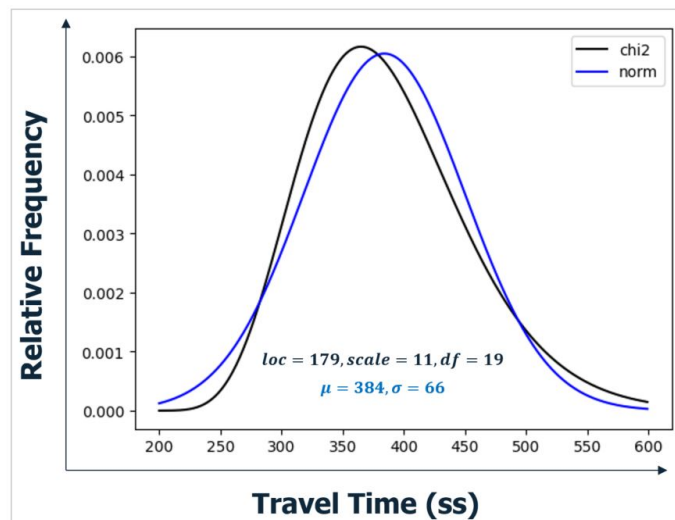


Figure 20: An illustration of the responses returned based on the offline variant, consisting of the selected law density function and its parameters



340 **4. Simulation Scenarios**

341 The simulation scenario was developed for three bus lines referenced respectively as *A*, *B*, and *C*. In this section,  
 342 the chosen bus lines will be **described first**, the timing points will be illustrated, **and** the trained **ML** models as well as  
 343 the simulation model parameters will be **provided**.

344 *4.1. Bus Lines: Description and Timing Points*

345 Line *A* buses run Monday to Saturday from approximately five in the morning **for the first departure** and until  
 346 approximately a quarter past nine in the evening **for the last departure**. On Sundays, the line’s buses run from around  
 347 six in the morning to around a quarter past nine in the evening. Buses on this line serve 33 stops in one direction  
 348 and 34 stops in the other direction, over a distance of approximately nine kilometers and a travel time of thirty-five  
 349 minutes. This bus line is very busy, with **an** average of one bus every ten minutes during peak hours and one bus every  
 350 quarter of an hour during off-peak hours, **resulting in** a total of 179 trips per working day.

351 Line *B* operates every day between five in the morning and nine twenty in the evening. **Buses on this line serve**  
 352 32 stops in both directions, covering a distance of approximately nine and a half kilometers and a travel time of just  
 353 over half an hour. In terms of frequency, Line *B* runs on average with one bus every six minutes **during peak hours**  
 354 and twelve minutes **during off-peak hours, resulting in** a total of 208 trips per working day.

355 Line *C* buses operate all week from approximately five in the morning to nine in the evening, serving 6 stops in  
 356 one direction and 5 in the opposite direction. Compared to the previous two lines, bus line *C* is much shorter, **with**  
 357 a distance of around two kilometers and a travel time of seven minutes. This line runs on average with one bus every  
 358 seven minutes **during peak hours** and ten minutes **during off-peak hours, resulting in** a total of 186 trips per day.

<b>route ID</b>	<b>route name</b>	<b>route stops</b>	<b>route distance (kms)</b>	<b>route travel time (minutes)</b>	<b>service frequency on/off peak hours</b>
<i>A<sub>A</sub></i>	<i>A-Aller</i>	33	9.00	37	10/15 minutes
<i>A<sub>R</sub></i>	<i>A-Retour</i>	34	9.39	38	10/14 minutes
<i>B<sub>A</sub></i>	<i>B-Aller</i>	32	9.59	33	6/12 minutes
<i>B<sub>R</sub></i>	<i>B-Retour</i>	32	9.67	31	7/12 minutes
<i>C<sub>A</sub></i>	<i>C-Aller</i>	6	2.19	6	7/10 minutes
<i>C<sub>R</sub></i>	<i>C-Retour</i>	5	1.81	7	7/10 minutes

Table 9: A description of the bus lines studied including: line identifier and name, number of stops per route direction, distance and time travel, in addition to the line’s service frequency during peak and off-peak hours. *A<sub>A</sub>* and *A<sub>R</sub>* respectively designate the route in one direction *Aller*, and the route in the opposite direction *Retour* of line *A*

359 The public transport simulation scenarios will be carried out on working days (Monday to Friday). The operating  
 360 days available for the selected lines covered 86, 274, and 281 days for lines *A*, *B*, and *C*, respectively. A description  
 361 of the bus lines studied is given in Table 9.

362 After selecting the bus lines for the simulation, the next step is to define the control points for each bus route.  
 363 These selected points will be used to divide each bus route into route segments, in order to train and then deploy **ML**  
 364 segment travel time models. **These models** will feed the simulation model with appropriate travel times. The retrieved  
 365 bus timing points, derived route segments, and their scheduled travel times for the selected bus lines are shown in  
 366 Figure 21.

367 *4.2. Machine Learning: Models Trained*

368 In this work, **ML** models are trained and then deployed in order to: 1) directly feed the simulation model with the  
 369 travel times of the route segments in the case of online coupling; 2) build a table of segment travel time parameters in  
 370 the case of offline coupling. This study focuses on accurately estimating travel time variability rather than returning  
 371 a single travel time prediction value. **ML** algorithms such as regression trees, **which divide the original dataset into**  
 372 **samples based on IF-THEN rules**, are suitable for dealing with travel time variability. Thus, **the Regression Tree**  
 373 **algorithm** is chosen as the **ML** algorithm in this study. Next, regression trees are trained with two sets of input  
 374 features: a) with only *stop time*; b) with *stop time* and *stop delay*. The actual travel time attribute is set as the target.



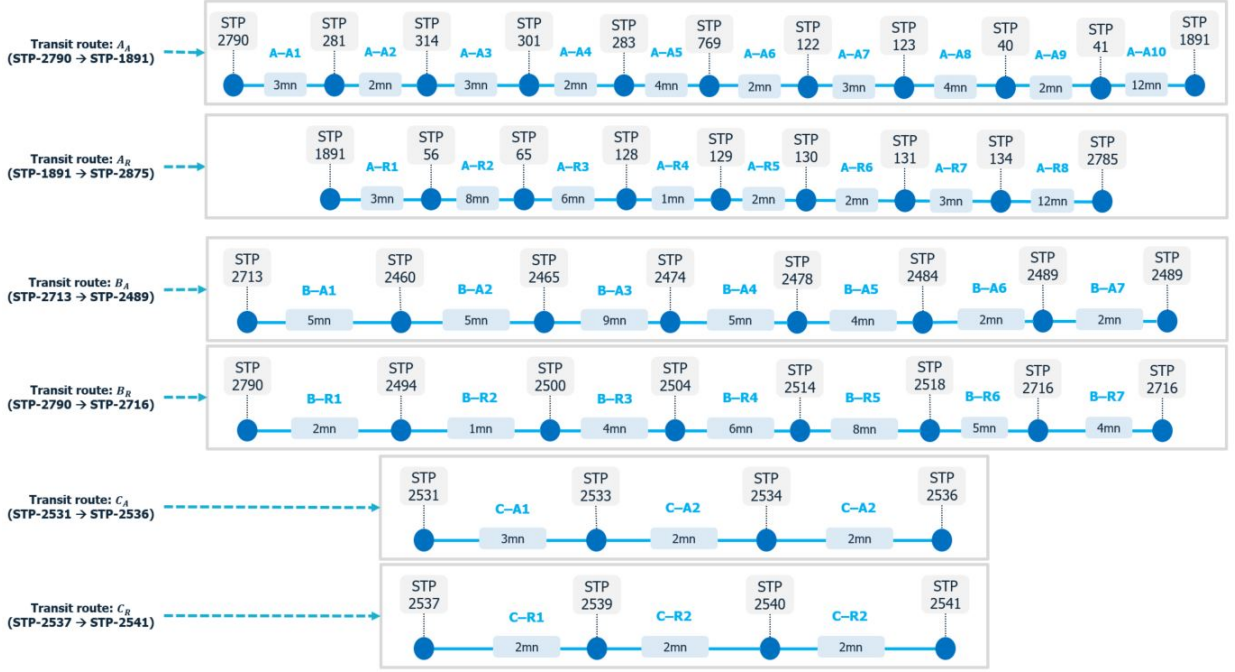


Figure 21: A detailed illustration of the route segments of the three selected bus lines. For bus line A, eleven control points are defined in the *Aller* direction, and nine in the *Retour* direction; there are eight and four timing points per direction for bus lines B and C. The route segment is identified by: its transit line, its route direction (A/R) and its index in the transit route. For instance, B-R2 refers to the *second* segment of the *Retour* route of line B

375 To build the ML model, we opt for k-fold cross-validation (CV), a technique used in ML to evaluate the perfor-  
 376 mance of a model on unseen data. In k-fold CV, the dataset is divided into  $k$  subsets (known as folds). A fold is used  
 377 once in each iteration as testing data, while the remaining folds are used as training data [77]. Thus, the process is  
 378 repetitive until the entire dataset is evaluated. In this study,  $k = 5$  is selected.

379 In terms of parameters, regression trees are built according to the following parameter values: *tree maximum depth*  
 380 varies between five and fourteen levels, while *minimum samples per leaf* takes four values ranging from 25 to 100.  
 381 In total, for each route segment, 80 regression trees are built and deployed. For line A, 800 and 640 models were  
 382 generated respectively, for  $A_A$  and  $A_R$ . For lines B and C, respectively, 560 and 240 models were generated per route  
 383 direction.

### 384 4.3. Simulation Model: Model and Parameters

385 In order to evaluate and validate the quality of the different coupling strategies, a simulation model as well as a  
 386 set of its parameters must be defined. The simulation scenarios will be carried out using an online strategy and three  
 387 offline coupling variants. In the first two offline variants  $S_1$  and  $S_2$ , the segment route travel time parameter table will  
 388 be built based on the *normal* distribution, with a static time period of a quarter of an hour for  $S_1$ . On the other hand,  
 389 the table of parameters of the third variant  $S_{3a}$  will be generated according to the *best-fit* distribution law. We assume  
 390 that  $S_{3a}$  and  $S_{3b}$  are considered equivalent during the simulation runtime because no ML models will be trained during  
 391 the simulation runtime. Thus, the best-fit ML model from which the segment travel times table will be constructed  
 392 will remain the same.  $S_{3a}$  and  $S_{3b}$  will be referred to as  $S_3$  in the remainder of this paper. The different coupling  
 393 variants implemented are given in Table 10.

394 In this study, the simulation scenarios will be performed using a generic framework, briefly described in section  
 395 3.2. A high number of simulation iterations is necessary in order to generate sufficient samples for the evaluation of  
 396 the coupling strategies. The number of runs to be simulated is set for this study to 1000 iterations.

strategy abbreviation	coupling strategy	probability law	time periods
$S_1$	offline	normal	15-minutes
$S_2$	offline	normal	-
$S_{3a}$	offline	best-fit	-
$S_{3b}$	online	best-fit	-

Table 10: Implemented coupling variants for the simulated scenario, including three offline strategy variants ( $S_1$ ,  $S_2$  and  $S_{3a}$ ) and one online strategy ( $S_{3b}$ )

## 5. Experiments and Results

Before presenting the results obtained, the two-step evaluation process undertaken will be briefly detailed. It aims to assess the quality of simulation results obtained from each of the coupling variants using performance indicators. The process is twofold: First, validate ML models for travel time prediction; Second, evaluate the simulated bus on-time performance accuracy of each coupling strategy. From a technical perspective, simulation results will be compared to actual observations, including: 1) segment travel times and 2) bus delays at control points. Furthermore, a computational evaluation of the simulated coupling strategies will take place. Note that the initial dataset was used entirely as a test dataset to validate the simulation performance.

In the first step of the evaluation process, the simulated segment travel times will be compared side-by-side to the actual segment travel times. We denote by  $TT_A^r$  and  $TT_S^r$ , respectively the actual and simulated average travel times of the route segment  $r$ . The two travel times will be compared according to a derived metric  $\Delta_{S,A}^r$ , which refers to the relative difference per route segment  $r$  between  $TT_S$  and  $TT_A$ , formulated in Equation 4. Furthermore, the two-sample Kolmogorov-Smirnov (KS) test [78], a non-parametric method used to assess the similarity between two distributions, will be performed between actual and simulated travel time distributions, in order to evaluate the resulting day-to-day travel time variability. Additionally, TTV over the course of the day will be evaluated.

$$\Delta_{S,A}^r = \frac{TT_S^r}{TT_A^r} - 1 \quad (4)$$

With  $TT_S^r > 0$  and  $TT_A^r > 0$

In the second step of the evaluation process, a quality assessment of simulated bus punctuality, using a punctuality measure (operator service reliability), will be performed. It involves comparing actual and simulated punctuality shares side by side. In this study, the punctuality of the operated and simulated buses will be evaluated based on the departure delay at the bus stop at the timing points of each of the bus lines. A bus can be classified according to its delay at the stop into three categories: a) *ahead*, if the bus is more than one minute ahead of the scheduled time; b) *on-time travel*, if the delay is between not earlier than one minute and not later than five minutes at the timing point; and c) *significant delay*, if the bus is late by more than five minutes [79].

After introducing the bus punctuality measure, the presented on-time performance metric will be applied at control points to the resulting actual and simulated on-time performance shares. Thus, a  $\Delta$  deviation measure defined in Equation 5, aimed at quantifying the part of the sharing poorly located between two sets of shares, will be evaluated.

$$\Delta(S_i, S_j) = \frac{1}{2} \cdot \sum_{c \in C} |S_{i,c} - S_{j,c}| \quad (5)$$

Where:

- $i$  and  $j$  are two datasets
- $C$ : refers to bus punctuality values with  $C = \{ahead, on-time travel, significant delay\}$
- $S_i$ : corresponds to the punctuality shares of the buses from the  $i$  dataset
- $S_{i,c}$ : refers to share of  $c$  in  $S_i$  with  $0 \leq S_{i,c} \leq 1$  and  $\sum_{c \in C} S_{i,c} = 1$
- $\Delta(S_i, S_j)$ : refers to the part of the sharing poorly located between  $S_i$  and  $S_j$  with  $0 \leq \Delta(S_i, S_j) \leq 1$

429 5.1. *ML: Model Validation*

430 5.1.1. *Model Validation: Actual vs Simulated Travel Times*

431 In this section, the first step of the evaluation process will be applied. In order to understand *how well the actual*  
 432 *and simulated travel times based on ML models are fitted*, the simulated travel times resulting from the different  
 433 coupling variants will be compared side by side to the actual travel times. The attributes of the route segments of bus  
 434 line *A*, including its route segment ID, its segment stops, as well as the actual average ( $TT_A$ ) and relative metric values  
 435  $\Delta$ , corresponding to the three simulation scenarios ( $S_1$ ,  $S_2$ , and  $S_3$ ), are given in Table 11.

436 By analyzing the  $\Delta$  values, it can be observed that the simulated travel times provided by the *ML* models match  
 437 the actual travel times well with a very slight deviation. For most route segments of bus line *A*,  $\Delta$  does not exceed 5%,  
 438 with the exception of *A-A2* and *A-R6*. These latter segments are particularly short, at around two minutes of travel  
 439 time. On the other hand, concerning the simulated travel times of  $S_1$ ,  $S_2$ , and  $S_3$ , one can see that the differences are  
 440 negligible.

Segment ID	Segment Stops	$TT_A$	$\Delta_{S_1,A}$	$\Delta_{S_2,A}$	$\Delta_{S_3,A}$
A-A1	STP-2790 → STP-281	222	0%	-1%	-2%
A-A2	STP-28 → STP-314	83	-5%	-5%	-5%
A-A3	STP-314 → STP-301	293	-2%	-2%	-2%
A-A4	STP-301 → STP-283	118	-4%	-3%	-4%
A-A5	STP-283 → STP-769	232	-3%	-3%	-3%
A-A6	STP-769 → STP-122	190	-1%	0%	-1%
A-A7	STP-122 → STP-123	86	-4%	-3%	-4%
A-A8	STP-123 → STP-40	248	0%	0%	0%
A-A9	STP-40 → STP-41	91	-3%	-2%	-3%
A-A10	STP-41 → STP-1891	839	-2%	-2%	-1%
-	-	-	-	-	-
A-R1	STP-1891 → STP-56	272	0%	-2%	-1%
A-R2	STP-56 → STP-65	499	-1%	-1%	-1%
A-R3	STP-65 → STP-128	372	0%	-1%	-1%
A-R4	STP-128 → STP-129	67	-2%	-3%	-2%
A-R5	STP-129 → STP-130	130	-2%	-3%	-2%
A-R6	STP-130 → STP-131	120	-5%	-5%	-5%
A-R7	STP-131 → STP-134	243	-3%	-3%	-2%
A-R8	STP-134 → STP-2785	683	2%	2%	2%

Table 11: Reported average travel times  $TT_A$ ,  $TT_{S_1}$ ,  $TT_{S_2}$  and  $TT_{S_3}$  (in seconds) as well as the related derived relative metric values  $\Delta$ , for each route segment of bus line *A*

441 After analyzing the different travel times of bus line *A*, the next step is to analyze the second bus line *B* and its  
 442 travel times. Regarding the  $\Delta$  values in Table 12, the simulated and actual travel times fit well, with a deviation of no  
 443 more than 3% for most of segments, except for *B-R1*, *B-R5* and *B-R6*. For *B-R1* and *B-R5*,  $\Delta_{S_3}$  is the highest with  
 444 13% and 17% respectively, which is equivalent to a deviation of half a minute and three-quarters of a minute. In total,  
 445 the simulated travel times from three simulation scenarios are almost identical, with the exception of the departure  
 446 and arrival segment as well as *B-R5*.

447 From Table 13, one can see that the route segments of line *C* are relatively shorter than those of the previous two  
 448 bus lines (*A* and *B*). As for  $\Delta$ , the relative differences between route segments are minor, averaging a few seconds  
 449 per route segment. On the other hand, the travel times simulated using  $S_1$  and  $S_2$ , correspond statistically well to the  
 450 actual travel times compared to the simulated travel times of  $S_3$ .

Segment ID	Segment Stops	$TT_A$	$\Delta_{S1,A}$	$\Delta_{S2,A}$	$\Delta_{S3,A}$
B-A1	STP-2713 → STP-2460	288	-2%	-2%	-2%
B-A2	STP-2460 → STP-2465	320	-1%	-1%	-1%
B-A3	STP-2465 → STP-2474	522	-1%	-1%	-1%
B-A4	STP-2474 → STP-2478	411	-2%	-2%	-2%
B-A5	STP-2478 → STP-2484	329	0%	0%	0%
B-A6	STP-2484 → STP-2489	153	3%	3%	3%
-	-	-	-	-	-
B-R1	STP-2490 → STP-2494	219	-7%	-7%	13%
B-R2	STP-2494 → STP-2500	316	-1%	-1%	-1%
B-R3	STP-2500 → STP-2504	357	-3%	-3%	-3%
B-R4	STP-2504 → STP-2514	579	-2%	-2%	-2%
B-R5	STP-2514 → STP-2518	248	0%	0%	17%
B-R6	STP-2518 → STP-2716	320	-6%	-6%	-6%

Table 12: Reported average travel times along with the associated deviation metric values, for each route segment of bus line *B*

Segment ID	Segment Stops	$TT_A$	$\Delta_{S1,A}$	$\Delta_{S2,A}$	$\Delta_{S3,A}$
C-A1	STP-2531 → STP-2533	184	-2%	-2%	-2%
C-A2	STP-2533 → STP-2534	75	0%	0%	5%
C-A3	STP-2534 → STP-2536	76	-2%	-2%	-2%
-	-	-	-	-	-
C-R1	STP-2537 → STP-2539	102	0%	0%	9%
C-R2	STP-2539 → STP-2540	74	-2%	-2%	-2%
C-R3	STP-2540 → STP-2541	65	-5%	-5%	-5%

Table 13: Reported average travel times as well as  $\Delta$  values, for the six segments of the *C* bus line

### 5.1.2. Model Evaluation: Day-to-Day Variability

In order to further analyze the resulting travel times, day-to-day variability will be investigated. Hence, the two-sample Kolmogorov-Smirnov test will be carried out, between on one hand the distribution of actual travel times and on the other hand the distributions of travel times simulated. Cumulative relative frequency distribution curves obtained from the KS test for the three scenarios, over the three lines studied, are given in Figures 22, 23 and 24.

For line *A*, at first glance, negligible differences can be observed between the curves obtained, **except** for segments *A-A8* as well as the two terminal segments *A-A10* and *A-R8*, in which certain differences are observed. Figure 23 shows slight differences overall, **except** for *B-A6* and *B-R1*, *B-R5* for  $S_3$ , in which a more significant difference between the actual and simulated CDF values is observed. From Figure 24, larger differences are observed, for line *C* compared to those for lines *A* and *B*. These differences can be explained by the particularity of line *C*, on which the route segments are significantly short (around 2km) short routes segments and therefore short travel times.

In order to quantify the observed differences between the actual and simulated CFD, Kolmogorov's D statistic (also called the Kolmogorov-Smirnov statistic) - which quantifies the maximum vertical distance between the empirical distribution functions of two samples - will be analyzed for each route segment. The resulting D-statistic values for each route segment of the three lines studied are shown in Figure 25.

For line *A*,  $S_3$  seems to have the lowest D-statistic among the simulated scenarios on average ( $D \approx 0.06$ ). In contrast, no clear trend is observed for  $S_1$  and  $S_2$ , with more similar D-statistic values on average ( $D \approx 0.08$ ). For line *B*, one can observe that  $S_3$  has on average the lowest D-statistic compared to  $S_1$  and  $S_2$ . In contrast and surprisingly,  $S_3$  has the highest D-statistic on the segments *B-R1* and *B-R5* (with  $D \approx 0.19$ ). For line *C*, it can be observed that D-statistic values are relatively higher compared to those of lines *A* and *B*. Overall, the results once again show that  $S_3$  has the lowest D-statistic on average compared to  $S_1$  and  $S_2$ .

Thus, from the results illustrated on the three bus lines studied, the simulated travel times provided by the ML models are statistically similar to the actual travel times. The travel times simulated with  $S_1$  and  $S_2$  coupling strategies

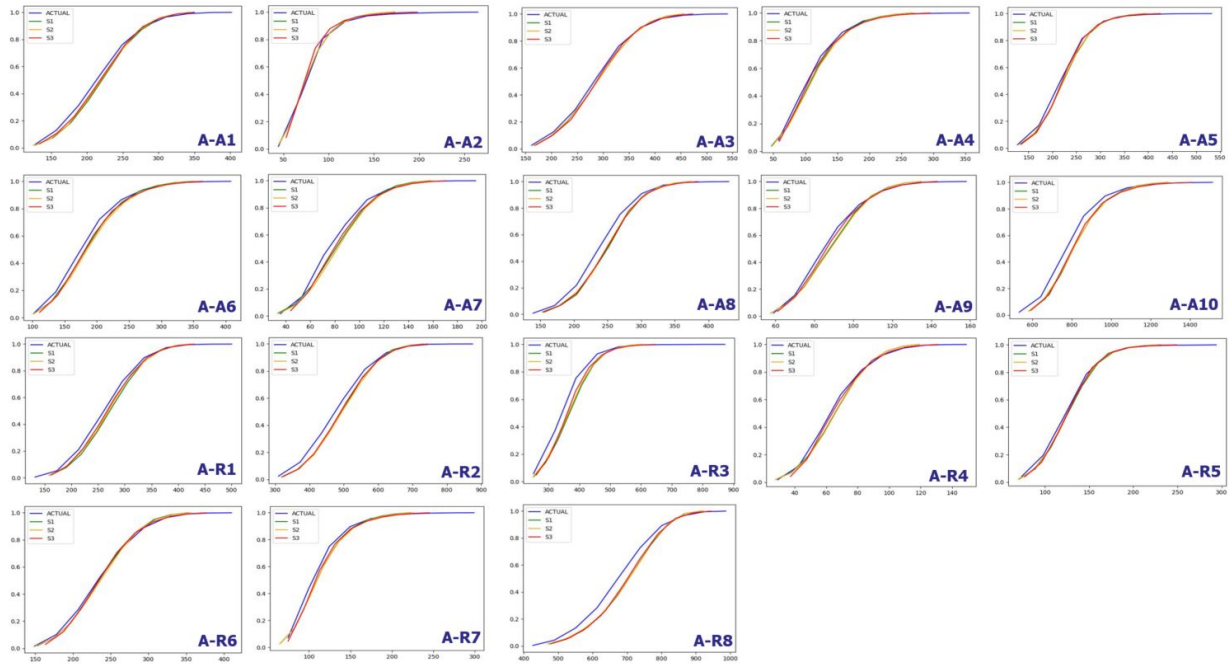


Figure 22: Cumulative relative frequency distribution curves obtained for each route segment of bus line A

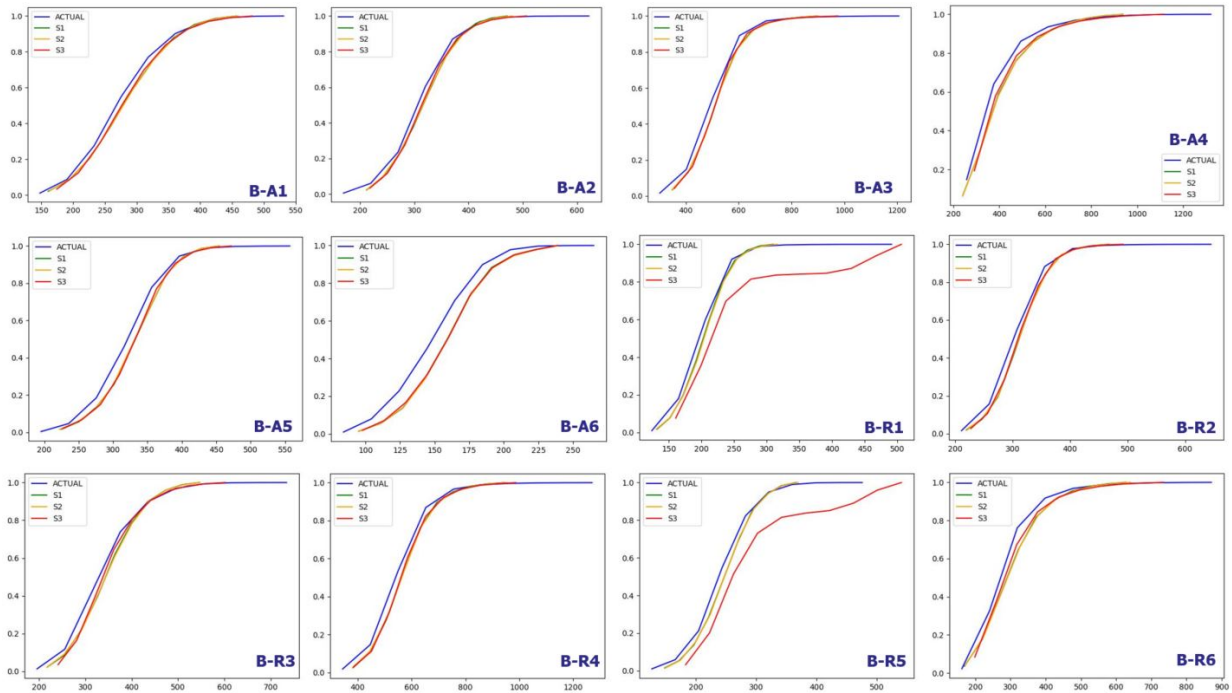


Figure 23: Cumulative relative frequency distribution curves obtained for each route segment of bus line B

475 slightly outperform those generated by  $S_3$ .



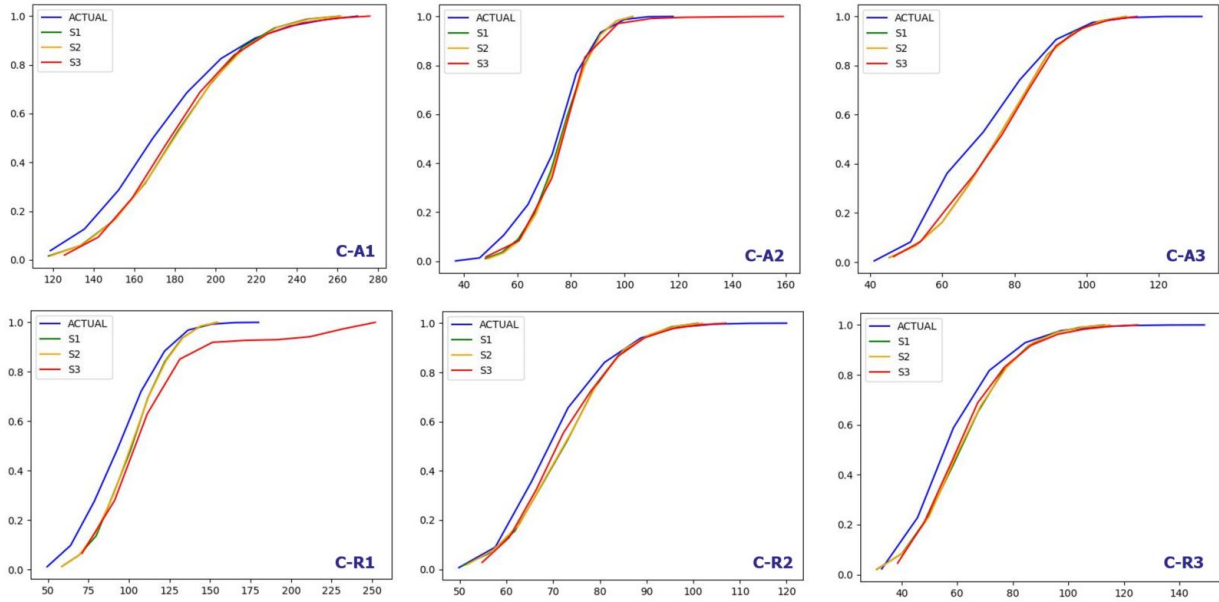


Figure 24: Cumulative relative frequency distribution curves obtained for each route segment of bus line C

### 5.1.3. Model Evaluation: Period-to-Period Variability

After analyzing the day-to-day travel time variability, in this section the focus is on studying the variability of travel times over the course of the day, also known as inter-period or period-to-period variability, which describes the variability between vehicles making similar trips at different times during the same day [74].

From Figure 26, the segments of *A-Aller* route can be grouped into three sets given as follows. The first set consists of segments *A-A1*, *A-A3*, *A-A7*, *A-A8* and *A-A9*, its variation pattern is characterized by two travel time peaks: 1) at noon and 2) at hours during evening rush hour. Furthermore, for most of route segments, a similar trend is observed between actual and simulated travel times. For *A-A1*, the simulation scenarios seem to slightly overestimate the segment travel times. For *A-A3*, a similar tendency is observed during the morning and evening periods, and throughout the day for  $S_3$ , while in contrast,  $S_1$  and  $S_2$  appear to follow a different trend and overestimate the travel times of the segments in the afternoon. For *A-A7*, a few observations need to be pointed out. First, the segment travel times are the shortest among *A-Aller* segments. Second, three travel time peaks are observed (morning, noon and evening). Third, the differences between simulated and actual travel times appear larger compared to other segments. For *A-A8* and *A-A9*, an overestimation of the simulated travel times over most of the day is observed, with the simulated and actual travel times fitting well, during the evening peak hours.

The second set consists of segments *A-A2*, *A-A4*, *A-A5* and *A-A6*, its variation pattern is characterized by a constant increase in the travel times of the segments during the day, from early morning until during evening rush hours. Furthermore, for most route segments, a similar trend is observed between actual and simulated travel times. For *A-A2*, the results show that the simulated travel times are slightly underestimated during evening peak-hours. For *A-A4* and *A-A5*, one can observe a very similar tendency between the actual and simulated travel times. For *A-A6*, one can observe that  $S_1$  and  $S_2$  follow different trends, particularly during the inter-peaks period.

The third set, consisting of segment *A-A10*, is characterized by three travel time peaks, during morning and evening rush hours as well at midday. For *A-A10*, the longest route segment,  $S_3$  on the one hand, seems to follow the same trend as the actual observations (three peaks) with differences that seem to be greater in the morning and evening than at midday.  $S_1$  and  $S_2$ , on the other hand, experience two peaks (morning and evening), with travel times appearing to stabilize during the inter-peak period.

From Figure 27, for *A-Retour*, the segments can be grouped into two sets as follows. The first set consists of *A-Retour* segments (except *A-A5* and *A-A6*), where travel times during the day are characterized by relatively stable values between the morning and evening rush hours.



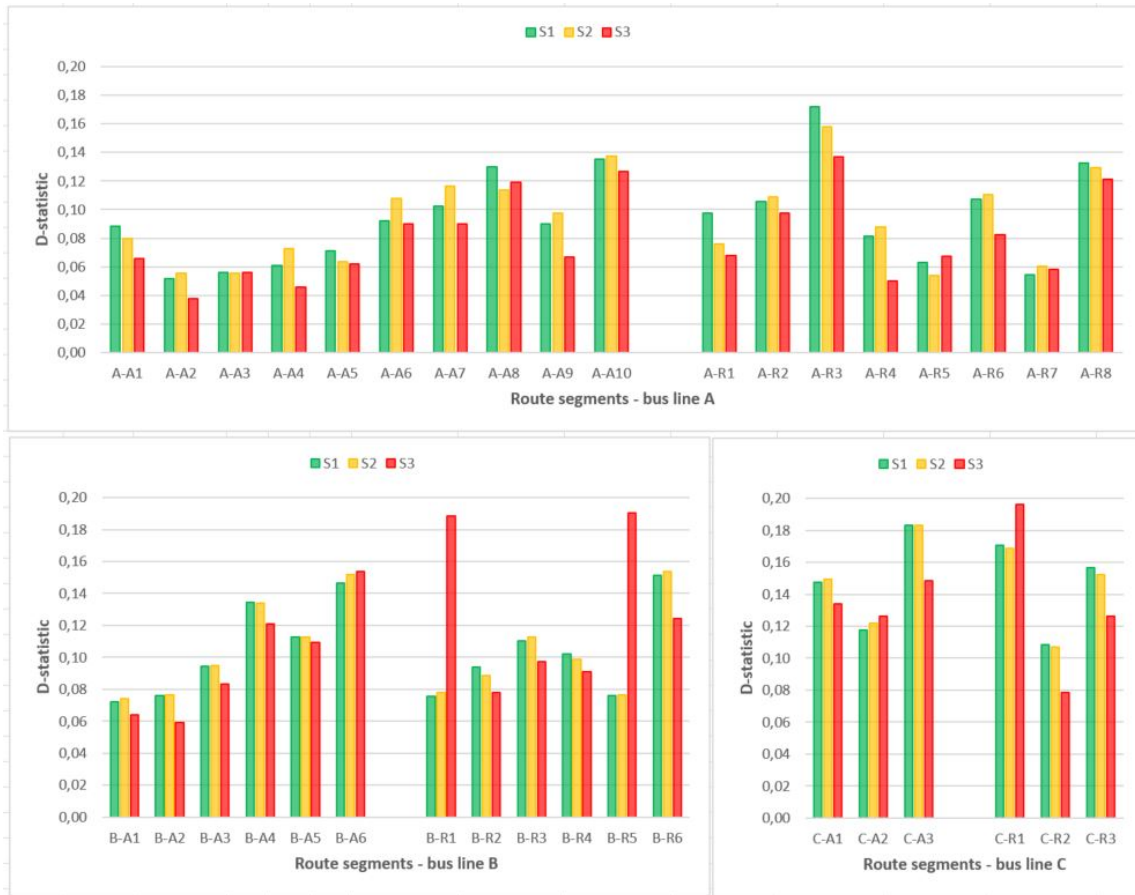


Figure 25: Kolmogorov-Smirnov (KS) test results (D-statistic) for each route segment

505 For *A-R1*, a particular segment with multiple peaks,  $S_3$  on the one hand seems to show similar trends to some  
 506 extent as the actual observations.  $S_1$  and  $S_2$ , however, follow a different trend with two peaks during morning and  
 507 evening rush hours. For *A-R2*, the simulated travel times follow a similar trend to the actual observations, with  $S_3$   
 508 showing a slightly different pattern from  $S_1$  and  $S_2$  in the morning. For *A-R3*, a similar trend is observed with the  
 509 actual observations for  $S_3$  and, to a lesser extent, for  $S_1$  and  $S_2$ . On the other hand, the differences appear most  
 510 significant among the "A-Retour" segments. Similar trends are observed with negligible differences for *A-R4* and  
 511 *A-R7*, while more significant deviations were observed during the morning compared to inter-peak times for *A-R8*.

512 The second set includes *A-R5* and *A-R6*, where a similar trend with a good fit is observed between actual and simu-  
 513 lated travel times. Additionally, travel times observed during evening rush hours were significantly higher compared  
 514 to the rest of the day.

515 From Figure 28, the segments of the *B-Aller* route can be grouped into two sets as follows. The first set consists of  
 516 the first three segments, where the actual travel time variation pattern is characterized by two travel time peaks: 1) at  
 517 midday and 2) during the evening rush hour. The differences between the two peaks are relatively small for segments  
 518 *B-A1* and *B-A2* and larger for segment *B-A3*. Furthermore, a similar trend is observed for the simulated travel times,  
 519 which are slightly longer during most of the day, except during the evening peak hours.

520 The second set, consisting of the last three segments, is characterized by a steady increase in actual travel times  
 521 throughout the day, with significantly high travel times during the evening rush hours, almost twice those observed  
 522 in the morning for *B-A4*. For *B-A4*, *B-A5*, and to a lesser extent *B-A6*, the resulting simulated travel times follow a  
 523 similar pattern to the actual observations with a main peak in the evening, but overestimate travel times throughout  
 524 most of the day.

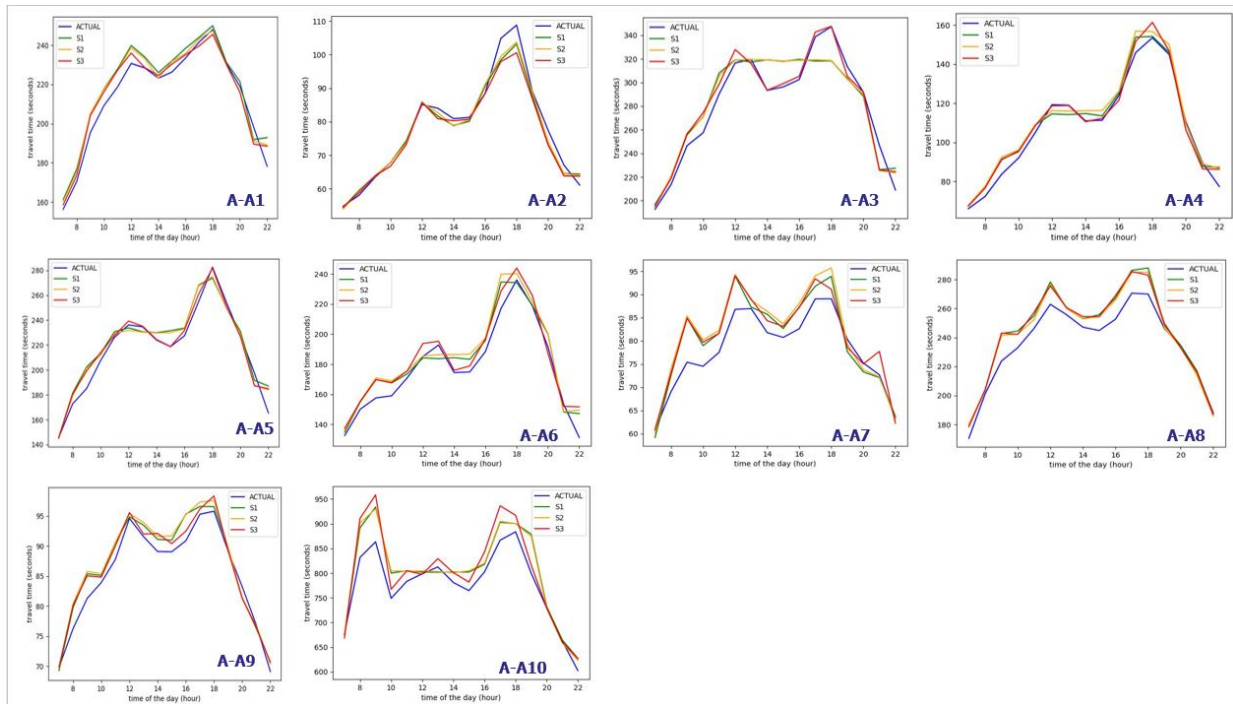


Figure 26: Travel time variability over the course of a day - bus line A - Aller

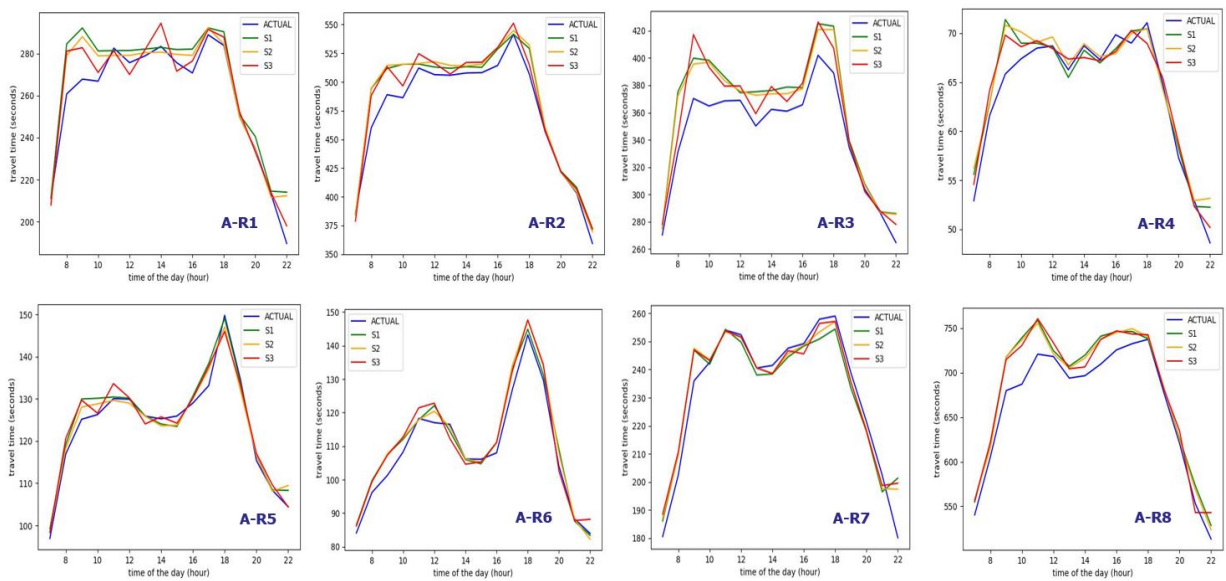


Figure 27: Travel time variability over the course of a day - bus line A - Retour

525 From Figure 29, for *B-Retour*, the segments can be grouped into three sets.

526 The first set, consisting of *B-R1* and *B-R5*, is characterized by a small variation in actual travel times over the course  
 527 of the day. Additionally, the travel times of  $S_1$  and  $S_2$  appear to follow the same pattern as the actual travel times  
 528 with minor deviations. In contrast, the travel times of  $S_3$  seem significantly deviated, with substantial overestimation  
 529 during the evening and afternoon for *B-R1* and early in the morning for *B-R5*.

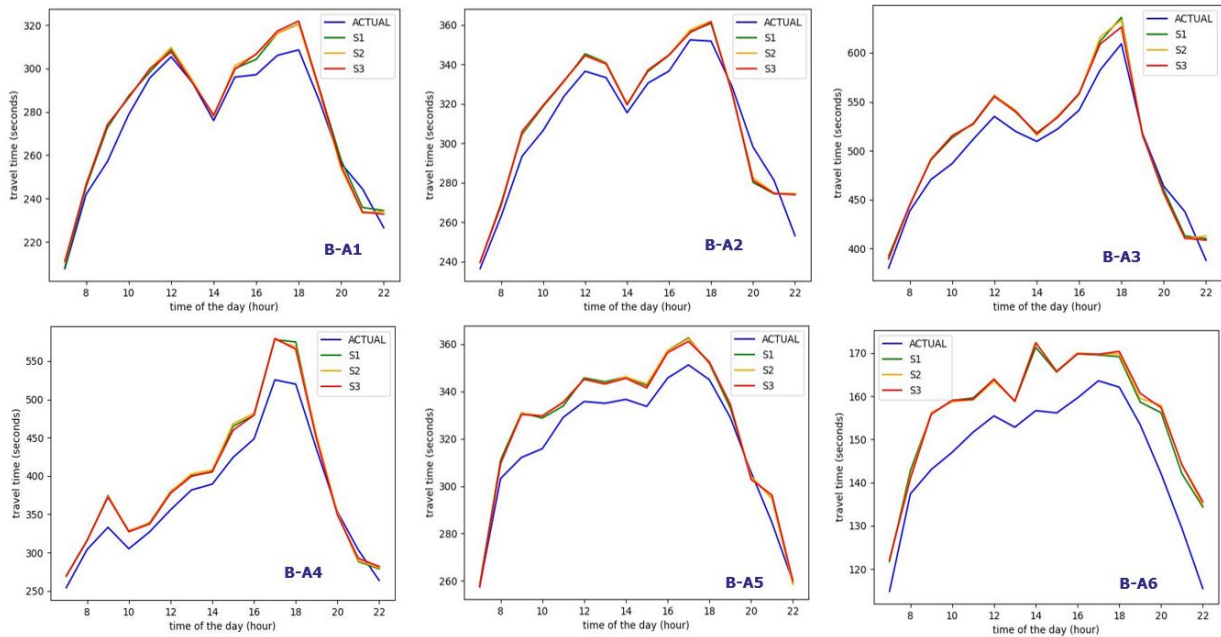


Figure 28: Travel time variability over the course of a day - bus line *B* - Aller

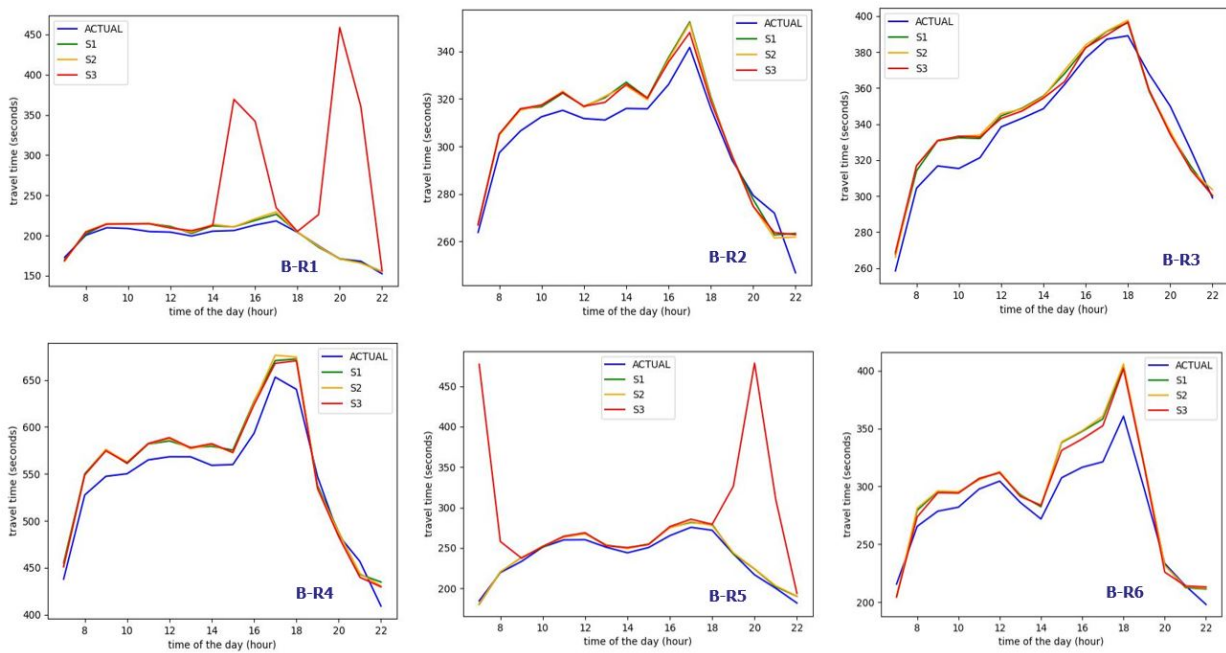


Figure 29: Travel time variability over the course of a day - bus line *B* - Retour

530 The second set includes segments *B-R2*, *B-R3*, and *B-R4*. This set is characterized by a steady increase in travel  
 531 times during the day for *B-R3* and *B-R4* and, to a greater extent for *B-R2*, with a peak in actual travel times during the  
 532 evening rush hours. A similar trend is observed for the simulation scenarios, with travel times overestimated to some  
 533 extent throughout the day, except during the evening.

534 The third set consists of segment  $B-R6$ , where two peaks can be observed at midday and during the evening rush  
 535 hours, with relatively small differences between the two peaks. Additionally, the simulated travel times seem slightly  
 536 overestimated.

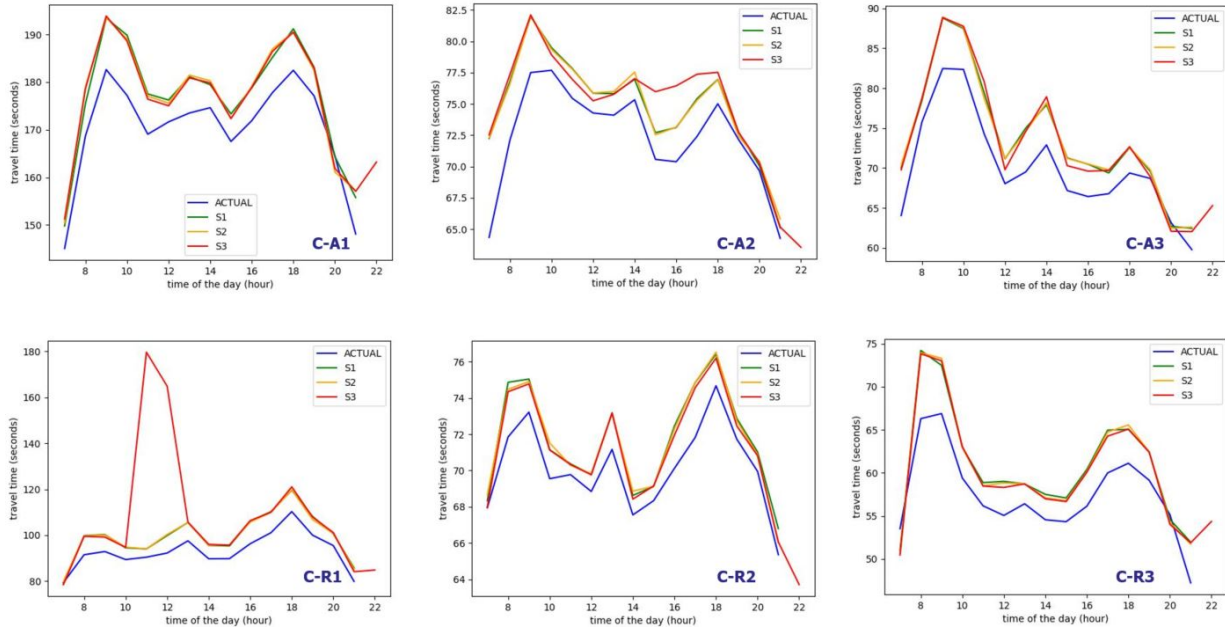


Figure 30: Travel time variability over the course of a day of bus line C

537 After analyzing the period-to-period travel time variability of lines A and B, the next step is to analyze the vari-  
 538 ability of line C, focusing specifically on the departure segments ( $C-A1$  and  $C-R1$ ) with an average travel time of more  
 539 than two minutes.

540 From Figure 30, similar trends between actual and simulated travel times can be observed, including multiple  
 541 peaks (morning, noon, evening). Contrary to the trends observed for lines A and B, travel times during morning rush  
 542 hours are longer than during evening rush hours. Furthermore, the differences appear relatively minor, averaging just  
 543 a few seconds. However, a notable observation is the trend for  $S_3$ , where the simulated travel times are significantly  
 544 overestimated compared to the actual travel times for  $C-A2$  and  $C-R1$ , particularly in the afternoon and around noon.

## 545 5.2. Simulation Model Precision: Actual vs Simulated Bus Punctuality

546 The second step in the evaluation process is to assess simulated bus punctuality. The punctuality measures outlined  
 547 in Section 5 will be estimated based on actual observations and the three simulated scenarios ( $S_1$ ,  $S_2$ , and  $S_3$ ) for each  
 548 of the three bus lines (A, B, and C). The resulting shares, obtained from each dataset, will be statistically analyzed and  
 549 compared side by side.

550 Figure 31 provides initial insights into how bus on-time performance is distributed according to the presented  
 551 metric, applied to all 12 datasets. Further details on the differences between the shares resulting from the simulation  
 552 scenarios and the actual shares are provided in Table 14. At first glance, one can observe some differences in the shares  
 553 between the different bus lines, with A and C appearing to be slightly more punctual than B. Based on ahead shares,  
 554 line C buses are much more ahead compared to lines A and B. Furthermore, line C, with its shortest bus routes, has  
 555 the least number of late buses, where the share of significant delay is negligible, while lines A and B have statistically  
 556 similar ratios for significantly delayed buses.

557 For bus line A, results from actual observations show that approximately two-thirds of buses are on time and  
 558 about one-fifth are early at control points. On the other hand, the shares obtained from the three simulated scenarios  
 559 indicate a very similar trend, with minor differences ( $\pm 2\%$ ) across different delay categories. In total, the simulation  
 560 shares appear to be comparable to the actual shares, with differences ranging from 4% to 5%, resulting from a slight  
 561 underestimation of the share of buses with significant delays.



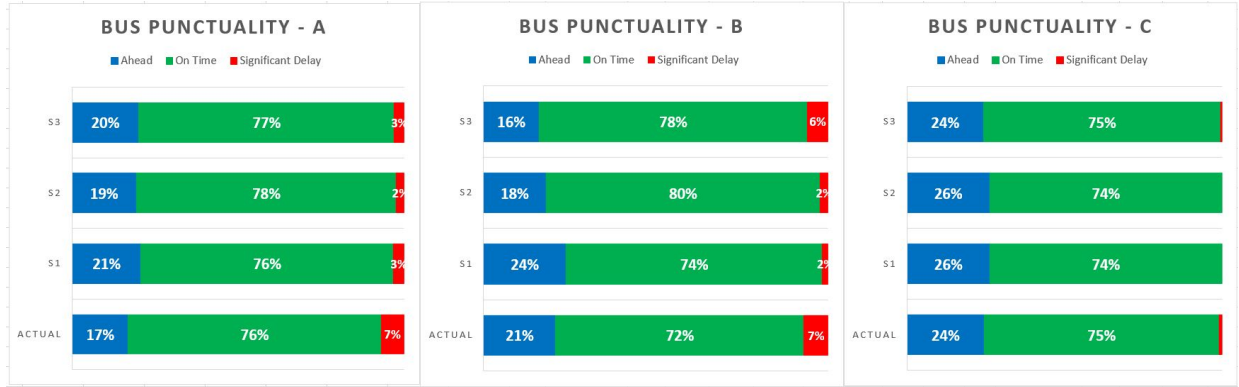


Figure 31: Bus punctuality shares for the bus lines studied, based on the first punctuality measurement. For the three studied lines, a strong similarity shares is observed between  $S_1$ ,  $S_2$  and  $S_3$  compared to actual shares, with  $S_1$  appearing to slightly outperform  $S_2$  and  $S_3$

562 For bus line  $B$ , approximately two-thirds of actual buses are *on-time travel* and one-fifth are *ahead*. Buses with a  
563 significant delay represent less than a tenth of the total buses. Furthermore, the results show that the resulting shares  
564 do not follow exactly the same trend. While  $S_1$  slightly underestimates the share of late buses (-5%),  $S_2$  and  $S_3$  tend  
565 to overestimate the share of *on-time travel* (+8% and +6%, respectively). As with bus line A, the differences between  
566 the actual and simulated shares are moderate, ranging from approximately 5% to 8%.

567 According to the results obtained from applying the first metric to the bus line  $C$  datasets, approximately two-  
568 thirds are on time and one-quarter are early. On the other hand, the share of buses with significant delays is very  
569 negligible. Unlike the two previous bus lines (A and B), the resulting shares from the three simulated scenarios show  
570 an identical trend to the actual shares with negligible differences not exceeding 2%.

571 In summary, the analyzed results show significant similarities between the shares of  $S_1$ ,  $S_2$ , and  $S_3$  with minor  
572 differences on bus lines A and C, and to a lesser extent on line B. Compared to actual bus delays, the delay shares  
573 resulting from the  $S_1$  simulation scenario appear to be slightly more accurate than those from  $S_2$  and  $S_3$ , which  
574 slightly overestimate the share of *on-time* buses. In short, the resulting simulation distributions for the three studied  
575 lines are well-fitted to the actual reference distributions according to this metric, demonstrating good accuracy of the  
576 simulation model.

	Line A				Line B				Line C			
	$S_a$	$S_1$	$S_2$	$S_3$	$S_a$	$S_1$	$S_2$	$S_3$	$S_a$	$S_1$	$S_2$	$S_3$
<b>Ahead</b>	17%	21%	19%	20%	21%	24%	18%	16%	24%	26%	26%	24%
<b>On-time travel</b>	76%	76%	78%	77%	72%	74%	80%	78%	75%	74%	74%	75%
<b>Significant delay</b>	7%	3%	2%	3%	7%	2%	2%	6%	1%	0%	0%	1%
$\Delta(S, actual)$	-	4%	5%	5%	-	5%	8%	6%	-	2%	2%	0%

Table 14: Illustration of the differences and gaps between the resulting simulation shares and the actual shares according to the first punctuality metric, for lines A, B and C

### 577 5.3. Coupling Model Performance: Offline vs Online Computation Time

578 After validating the simulated travel times and evaluating the accuracy of the implemented coupling strategies, the  
579 next step is to evaluate the simulation model performance. Figure 32 illustrates the experimental computation times  
580 for building a decision tree for travel time prediction as well as simulation execution time.

581 From Figure 32.(a) and (b), one can observe that the computation time for building one ML model, which includes  
582 dataset preparation and training time, is higher for lines B and C compared to line A. On the other hand, it can be seen  
583 that the total time required to build all segment models is higher for line A than for lines B and C. These trends can be  
584 explained by a larger dataset for bus lines B and C, and a larger number of route segments for line A.

585 From Figure 32.(c) and (d), the simulation time appears to be slightly higher for lines A and B compared to line  
586 C. For the coupling strategies,  $S_1$  is notably the strategy with the lowest simulation time for all three bus lines. On  
587 average,  $S_1$  requires two to three times less computation time compared to  $S_2$  and  $S_{3a}$ , and up to seven times less than  
588  $S_{3b}$ . For  $S_2$  and  $S_{3a}$ , which are based on the *normal* and *best-fit* probability laws, respectively, a similar execution  
589 time can be observed, with  $S_{3a}$  having a relatively higher simulation time than  $S_2$ . As expected, for  $S_{3b}$ , the online  
590 coupling strategy has a high computational time compared to the three offline coupling variants. For the scenarios  
591 conducted, the online strategy simulation is on average twice as slow as its equivalent offline strategy.

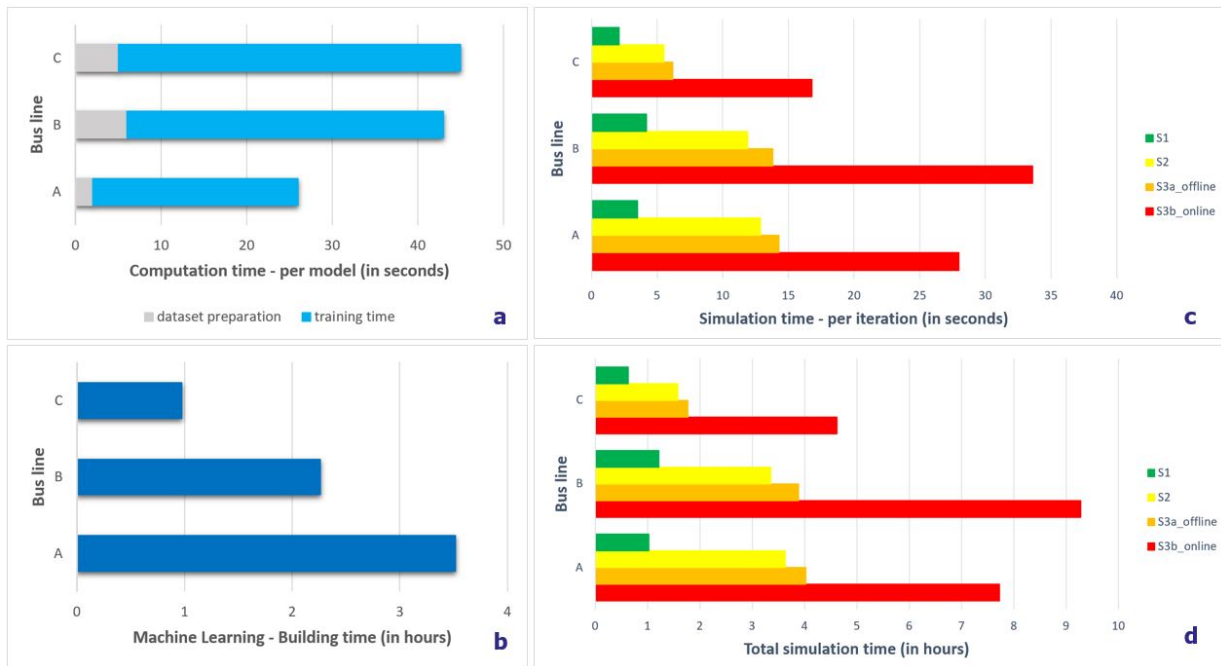


Figure 32: Overview of the different calculation times for each bus line. (a): Average time to prepare the dataset and train tree regression for segment travel time prediction. (b): Total ML model building time per bus line. (c) and (d): Single and total simulation time for each bus line (1000 iterations).  $S_1$  is the strategy with the lowest calculation time, while the online strategy  $S_{3b}$  is the one with the highest computation time

592 The resulting differences in total simulation time between the studied lines can be explained by: 1) the number  
593 of route segments and 2) the number of simulated trips. The advantage of  $S_1$  over other strategies is explained  
594 by the fixed size of the table of segment travel time parameters, built on the basis of a feature (stop time) and a  
595 period static time (15 minutes). Furthermore, the relative difference in calculation time between  $S_2$  and  $S_{3a}$  could be  
596 explained by the fact that the empirical time necessary to generate a valid travel time value with the normal law is, on  
597 average, lower than that of the best-fit law. Additionally, the application of the request-response during the simulation  
598 is time-consuming, particularly using the online coupling strategy, which requires retrieving, for each request, the  
599 corresponding ML model from the indexed ML database. Therefore, excessive access to the index database leads to  
600 a much longer simulation time, as in  $S_{3b}$ . It should be noted that applying an offline strategy requires building a table  
601 of travel time parameters, with the building time being relatively minor compared to the scenario simulation time,  
602 ranging from a few seconds to a few minutes depending on the number of segments and the models built, and to a  
603 lesser extent on the distribution law chosen.



## 604 6. Discussions

605 The simulated travel times provided by the ML models match well with the actual travel times on the three lines  
606 studied, with  $S_1$  and  $S_2$  slightly outperforming  $S_3$ . From Table 12,  $S_3$  appears to significantly overestimate the travel  
607 times of  $B-R1$  and  $B-R5$ , which can be explained by an imprecise trend in period-to-period travel time variability. This  
608 results in a significant deviation in travel times, in the afternoon and evening for  $B-R1$  and during off-peak hours in  
609 the morning and the evening for  $B-R5$ .

610 Concerning day-to-day variability, the differences between the actual and simulated CFD for segments  $A-A10$  and  
611  $A-R8$  (see Figure 22) are the result of a significant overestimation of travel times during morning rush hours and, to a  
612 lesser extent, during evening peak hours, in which travel times are the longest. Similarly for  $B-A6$  (see Figure 23), and  
613 despite a relatively small deviation between the travel times obtained ( $\Delta \approx 3\%$ ), the differences can be explained by a  
614 relative overestimation of the simulated travel times, particularly during off-peak hours in the morning and evening.

615 Concerning period-to-period variability, three trends were observed: 1) A pattern with a peak in the evening,  
616 which can be explained by the impact of the increase in traffic over the course of the day; 2) A pattern with two  
617 peaks at midday and in the evening, which can be explained by a reduction in road congestion in the afternoon; and  
618 3) A pattern with three peaks (morning, noon, and evening), for certain segments of line  $C$ , where the earliest peak  
619 is explained by the presence of traffic lights as well as crossroads near educational facilities such as high schools.  
620 Furthermore, the results showed that travel times during evening rush hours are significantly longer than the rest of  
621 the day, which can be explained by a high level of traffic and congestion.

622 For  $S_1$  and  $S_2$ , a very similar trend was observed, which can be explained by the choice of normal distribution to  
623 fit the observed travel times. The travel times estimated using  $S_1$  and  $S_2$  were more regular during the inter-periods,  
624 which can be explained once again by: 1) the use of normal law and 2) a relatively small variation in the observed  
625 travel times. In contrast, the  $S_3$  trends appear to match those in actual travel times on most route segments. However,  
626 it also fails to accurately estimate travel times, especially during inter-periods, leading to discrepancies, which can be  
627 explained by an unsuitable law for travel time fitting.

628 The delay shares resulting from the simulation generally corresponded well to the actual shares, with a slight  
629 underestimation of the shares of late buses according to the first bus punctuality metric. Furthermore, none of the  
630 applied coupling strategies seem to stand out; the differences appear very limited or even negligible,  $S_1$  and  $S_3$   
631 being slightly more regular and outperforming  $S_2$ . On the other hand, according to the second punctuality metric,  
632 the resulting shares of the simulation lack precision, with significant differences, particularly for buses on time and  
633 slightly late. This could be explained by a late departure of some buses. For instance, if a bus leaves its terminal  
634 relatively late, it may not be able to make up the scheduled stop time and, therefore, be late at control points, resulting  
635 in an increase in the number of delayed buses. To overcome this drawback, integrating actual bus departure delays  
636 into the simulation model will greatly improve the simulation results.

637 From a computational point of view, the bus-line simulation time scales depending on the number of route seg-  
638 ments and trips simulated.  $S_1$  is the strategy with the least simulation time, followed by  $S_2$  and  $S_{3a}$ , while  $S_{3b}$  has  
639 the highest simulation time. The advantage of using an online strategy is retrieving from an updated model database.  
640 Additionally, it provides the ability to use multiple models per route segment. On the other hand, applying an offline  
641 strategy allows the use of a single model per route segment, with the need to rebuild the parameter table each time a  
642 new ML model is built and inserted into the database. The building time of the travel time parameter table increases  
643 slightly each time a new model is indexed but remains much lower than the online simulation time. In summary,  
644 applying an offline coupling strategy requires less simulation time than an online strategy.

645 Overall,  $S_1$  seems to stand out from other coupling strategies with a good trade-off between simulation time and  
646 adequacy to actual observations for both travel time and bus punctuality. In short, the online coupling strategy is more  
647 suitable for real-time applications. On the other hand, offline coupling strategies, with good model accuracy and the  
648 best computation time, are suitable for simulation applications.

649 **7. Conclusions**

650 This paper sheds light on how ML and public transport simulation models can be effectively coupled. In this  
651 paper, we suggested two coupling strategies: 1) online, in which ML models provide PT simulators with travel times,  
652 and 2) offline, in which travel times resulting from ML are integrated as input data into the transit simulation model.  
653 In the proposed framework, various data sources are integrated, ML models are trained and deployed for predicting  
654 bus travel times, and simulation scenarios are implemented and executed. A case study was carried out on three bus  
655 lines in a French city with four scenarios, including three offline coupling variants ( $S_1$ ,  $S_2$ , and  $S_{3a}$ ) and one online  
656 variant ( $S_{3b}$ ) per bus line.

657 A first analysis aimed at validating the simulated travel times was carried out. Furthermore, two analyses were  
658 conducted to further evaluate the variability in travel from day to day and from period to period. The results showed  
659 that  $S_1$  and  $S_2$  followed a very similar trend, while  $S_3$  matched the actual trends but also showed difficulties in ac-  
660 curately predicting travel times in particular situations, leading to some deviations. Overall, the resulting simulated  
661 travel times adequately match actual travel times, with slight differences observed, in which  $S_1$  and  $S_2$  slightly out-  
662 perform  $S_3$ . On the other hand, an evaluation of the accuracy of the model was carried out. Despite the use of more  
663 approximate travel times, the offline strategies show as good a match as the online strategy between the actual and  
664 simulated bus punctuality shares. In terms of performance,  $S_1$  stood out from other coupling strategies with less sim-  
665 ulation time. Overall,  $S_1$  appears to be the best strategy, with good model precision and the best calculation time. We  
666 believe this paper is of particular interest for practitioners in the field, as it provides insights into how to effectively  
667 couple ML and public transport simulation models, as well as the benefits and limitations of each strategy.

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Abbreviation	Description
$\chi^2$	Chi-squared distribution
dweibull	Double Weibull distribution
exponnorm	Exponentially modified Gaussian distribution
exponweib	Exponentiated Weibull distribution
gamma	Gamma distribution
genextreme	Generalized extreme value distribution
log-normal	Log-normal distribution
normal	Normal distribution
rayleigh	Rayleigh distribution

Table A.15: List of probability laws used in this work

feature values	probability law	parameter values						
		loc	scale	a	c	df	K	s
00:00:00 ≤ stop time < 07:25:30	exponnorm	279.04	47.24				0.72	
07:25:30 ≤ stop time < 08:09:00	$\chi^2$	178.97	11.05			18.83		
08:09:00 ≤ stop time < 08:51:00	genextreme	405.45	81.22		0.16			
08:51:00 ≤ stop time < 09:52:30	log-normal	63.20	328.82					0.21
09:52:30 ≤ stop time < 10:45:00	genextreme	397.87	61.38		0.17			
10:45:00 ≤ stop time < 11:05:00	rayleigh	286.08	126.84					
11:05:00 ≤ stop time < 12:32:00	genextreme	420.60	69.58		0.11			
12:32:00 ≤ stop time < 15:02:00	log-normal	-43.50	470.37					0.14
15:02:00 ≤ stop time < 16:09:00	genextreme	416.49	70.86		0.13			
16:09:00 ≤ stop time < 16:26:00	genextreme	432.99	87.79		0.15			
16:26:00 ≤ stop time < 17:32:00	gamma	221.73	57.94	5.32				
17:32:00 ≤ stop time < 17:51:00	gamma	183.22	45.78	7.23				
17:51:00 ≤ stop time < 18:14:00	rayleigh	275.95	165.22					
18:14:00 ≤ stop time < 18:58:30	genextreme	349.26	41.30				1.91	
18:58:30 ≤ stop time ≤ 23:59:59	$\chi^2$	66.03	9.13			29.57		

Table A.16: An illustration of the built travel time parameter table for the route segment, in which *from stop* = STP-1883 and *to stop* = STP-982 of transit line A, with *stop time* as selected feature and best-fit distribution as the chosen law. The meaning of the law parameters can be found in <https://docs.scipy.org/doc/scipy/tutorial/stats/>

feature values	probability law	parameter values						
		loc	scale	a	c	df	K	s
00:00:00 ≤ stop time < 07:25:30	exponnorm	279.04	47.24				0.72	
07:25:30 ≤ stop time < 08:09:00	$\chi^2$	178.97	11.05			18.83		
08:09:00 ≤ stop time < 08:33:00	exponweib	113.78	231.19	4.73	1.96			
08:33:00 ≤ stop time < 10:45:00 ∧ stop delay < 37	genextreme	388.95	70.80		0.18			
08:33:00 ≤ stop time < 10:45:00 ∧ stop delay ≥ 37	$\chi^2$	200.05	11.13			18.26		
10:45:00 ≤ stop time < 12:32:00 ∧ stop delay < 40	genextreme	406.98	64.48		0.06			
10:45:00 ≤ stop time < 12:32:00 ∧ stop delay ≥ 40	gamma	137.61	19.89	16.24				
12:32:00 ≤ stop time < 14:02:00	exponnorm	397.84	53.72				0.78	
14:02:00 ≤ stop time < 15:07:00	exponnorm	372.67	50.53				0.96	
15:07:00 ≤ stop time < 16:14:30	gamma	135.73	19.93	15.81				
16:14:30 ≤ stop time < 16:26:00	dweibull	469.40	85.49		1.34			
16:26:00 ≤ stop time < 16:37:30	dweibull	502.70	100.90		1.33			
16:37:30 ≤ stop time < 17:44:00	exponweib	-403.20	120.65	2346.43	1.03			
17:44:00 ≤ stop time < 18:08:00	$\chi^2$	245.01	28.04			8.80		
17:44:00 ≤ stop time < 18:47:00	exponnorm	357.21	42.61				2.00	
18:47:00 ≤ stop time ≤ 23:59:59	genextreme	312.36	65.17		0.16			

Table A.17: An illustration of the built travel time parameter table for the route segment, in which *from stop* = *STP-1883* and *to stop* = *STP-982* of transit line *A*, with *stop time* and *start delay* as selected features and best-fit distribution as the chosen law. The meaning of the law parameters can be found in <https://docs.scipy.org/doc/scipy/tutorial/stats/>

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