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Graph-Level Heterogeneous Information Network Embeddings for Cardholder Transaction Analysis

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Abstract

Graph-related applications, including classification, regression, and clustering, 11 have seen significant advancements with the development of graph neural net-12 works (GNNs). However, a gap remains in effectively using these models for 13 heterogeneous graphs, as current methods primarily focus on homogeneous 14 graphs, often overlooking potentially valuable semantic information. To address 15 this issue, our work introduces a novel approach, G-HIN2VEC (Graph-Level 16 Heterogeneous Information Network to Vector), specifically designed to generate 17 heterogeneous graph representations. This method uniquely leverages a single 18 graph to learn its own embeddings without relying on a graph dataset, by shar-19 ing model parameters across the dataset. Inspired by recent developments in 20 unsupervised learning in natural language processing, G-HIN2VEC employs a 21 negative sampling technique to learn graph-level embedding matrices from a 22 variety of metapaths. This approach has been applied to real-world credit card 23 data, facilitating the analysis of cardholder transactions through three down-24 stream applications—graph-level regression and classification tasks, including age 25 and income prediction, and gender classification. G-HIN2VEC outperforms tra-26 ditional methods, demonstrating improvements in gender classification accuracy 27 by 2. 45% and income prediction R-squared (R2) by 7. 19%. Furthermore, for age 28 prediction, we achieved an increase of 6. 55% in the mean absolute error (MAE) 29 compared to DiffPool, a strong baseline. 30

Keywords: Unsupervised learning, Learning latent representations, Graph Neural
 Networks, Heterogeneous Information Network , Financial Transaction Analysis

³³ 1 Introduction

Financial institutions manage a variety of transaction types, encompassing a spectrum of financial assets, such as loans, insurance, and investments. In today's increasingly digital era, banks, as ubiquitous entities, offer several financial card products that dominate the retail banking sector. The past decade has seen an impressive increase in cashless payments through plastic and virtual cards, leading to exponential growth in the digital footprint of card transactions ¹.

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Analyzing customer transactions is pivotal for various banking applications, including but not limited to behavior modeling, product recommendation, and advertising strategies [1]. Recent research in financial data analysis [2, 3] suggests the utility of graph data structures to encapsulate the topological information inherent in tabular data, thereby extending and enriching available customer data. Currently, deep learning algorithms have been refined and enhanced, expanding their applicability to a wider range of problems [4–6].

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⁴⁹ Despite the advantages, graph data structures introduce additional complexity, with ⁵⁰ each graph component characterized by unique attributes and local topology. Tasks ⁵¹ such as graph classification, clustering, and regression, which require vectorial repre-⁵² sentations of graphs for the application of machine learning algorithms, become more ⁵³ challenging. Techniques to overcome this challenge include Graph Kernel algorithms ⁵⁴ [7], acting as hand-crafted feature extractors, and embedding algorithms that provide ⁵⁵ dense latent graph encoding [8].

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However, most of these embedding techniques have been designed for homogeneous 57 networks [8], and therefore their application is limited to graphs with a single type 58 of nodes and edges. However, real-world networks often comprise heterogeneous 59 information networks (HINs), where there are different types of interaction between 60 graph components. Graph Neural Networks (GNNs) offer potential solutions for such 61 graphs. GNNs have proven their effectiveness in various graph-related tasks, but they 62 often fail to preserve the network structure fully, especially for HINs [9, 10]. Graph 63 analysis tasks are often confined by the characteristics of the problem at hand and 64 65 the applied embedding techniques [11]. In scenarios involving node-level tasks such as node regression and classification, the embeddings are typically designed to portray 66 low-dimensional representations of nodes. For example, the classification of scientific 67 publications using citation networks exemplifies a node-level task. Conversely, for 68 graph-level tasks, such as graph classification and regression, the embeddings provide 69 a low-dimensional representation of the entire graph. Examples of these tasks include 70 prediction of protein functions using chemical compound graphs and detection of 71 malware based on call graphs [12, 13]. 72

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Recently, random walk-based embedding methods have displayed significant performance improvements in various homogeneous graph (HG) downstream tasks by

¹According to the Federal Prof. of Credit Card Operations of Depository Institutions report, 2020 ref.https://www.federalreserve.gov/publications/files/ccprofit2020.pdf

⁷⁶ preserving the network structure [8]. However, their utility is considerably limited
⁷⁷ when applied to a heterogeneous schema. Concurrently, much of the existing research
⁷⁸ on graph embedding remains heavily focused on learning node representations, leav⁷⁹ ing a gap in the comprehensive understanding and handling of complex heterogeneous
⁸⁰ networks.

In this work, our neural network architecture, called G-HIN2Vec, is specifically 82 designed to embed entire heterogeneous graphs. It relies on joint learning architec-83 tures [14] and random walk-based methods for node embedding. We evaluate the 84 quality of the generated heterogeneous graph embeddings across various downstream 85 tasks using different metrics for credit card transactions. Based on a preliminary lit-86 erature review, we carefully selected our baseline methods. The experimental results 87 show that G-HIN2VEC embeddings outperform the baseline methods HIN2VEC [15] 88 and Metapath2Vec [16]. In particular, G-HIN2VEC exhibits a 2.45% improvement 89 in the precision of the gender classification and a 7.19% increase in the R-squared 90 income prediction (R2) over the strongest baselines, with a loss in the Mean Absolute 91 Error (MAE) in age prediction by 6.55% compared to DiffPool [17]. This shows the 92 effectiveness of our approach in enhancing customer understanding in retail banking. 93 Our contributions are as follows. 94

- We propose an ego-centric graph model for cardholder transactions to build an
 unlabeled heterogeneous graph dataset inspired by egocentric thinking.
- We introduce G-HIN2Vec, a new unsupervised representation learning method
 that employs a double-triplet loss function as task-agnostic approach for entire
 heterogeneous graph representations.
- We experimentally benchmark various GNN models against G-HIN2VEC on real-world credit card datasets for multiple downstream tasks, including graph classification, regression, and clustering tasks.

103 2 Related Work

This section reviews three primary research lines for our work, focusing on hetero geneous information networks, graph-level embedding, and financial card transaction
 data analysis.

• Heterogeneous Information Network (HIN) Embedding: Heterogeneous Information Network Embedding has emerged as a significant area of research, primarily due to its ability to effectively represent complex real-world data. These networks encompass interactions among various types of objects, offering a more detailed representation of real-world scenarios.

Recent algorithms in HIN embedding primarily focus on node or edge-level embedding, as evidenced in studies by [15, 16, 18], This focus, however, introduces constraints when addressing graph-level downstream tasks. In a recent comprehensive review [19], 13 HIN embedding methods were benchmarked on four distinct datasets designed for node- and edge-level tasks. These studies have consistently demonstrated that the effectiveness of an HIN embedding algorithm depends on

the specific requirements of the downstream task, underlying the graph schema, and other experimental variables, as highlighted in [9, 10]. A critical limitation in the field is the lack of a unified framework for HIN embeddings, as pointed out by [8]. This absence has been identified as a significant barrier, particularly when addressing graph-level downstream tasks.

Graph-level Embedding: Despite the abundance of research on node, edge, or 123 subgraph embedding algorithms, studies on entire graph embedding algorithms 124 are relatively sparse [12]. This impacts the downstream graph-related tasks for 125 HIN networks such as graph classification, regression, and clustering. Conversely, 126 HG embeddings have been extensively studied and are well-established in various 127 downstream tasks [20]. Both graph types embedding algorithms seek to preserve 128 topological and semantic similarity across a graph dataset. As discussed in [12] and 129 due to lack of HIN graph-level embedding algorithms, researchers often resort to 130 transforming HINs into HG datasets. This transformation is a proxy approach to 131 leverage existing homogeneous graph embedding algorithms, such as Graph2Vec 132 [20] and Deep Graph Kernels (DGK) [21], for generating graph-level embeddings. 133 While this method has led to improvements in performance, it unfortunately dis-134 cards potentially valuable semantic information. This limitation has pushed research 135 towards developing embedding models tailored for HINs. UGraphEmb [22] addresses 136 the issue as a supervised training model that relies on existing heuristics for graph 137 similarity [23, 24], which is computationally intensive and not scalable. Instead of 138 proxy or supervised approaches, HIN representation can be generated via aggregate 139 functions, such as the average layer, to transform node/edge embeddings into graph 140 embeddings, which often leads to suboptimal results [25]. This is due to the absence 141 of unsupervised HIN graph-level embedding algorithms. 142

Financial Card Transactions: While the field of card transaction research focuses 143 primarily on fraud detection, current graph-based methodologies predominantly uti-144 lize simple graphs [2]. Due to the heterogeneity of the data, this approach does not 145 fully capture the intrinsic complexity of financial networks. This limitation high-146 lights the growing need for HIN-based GNNs for financial transactions. For instance, 147 HINs have been used for the detection of malicious Alipay accounts as a node-level 148 task [13], risky transactions in a B2B network [26], and for bankruptcy prediction in 149 credit risk assessment [27]. However, beyond fraud detection, card transaction data 150 is being increasingly leveraged to gain insights into transaction entities. For exam-151 ple, techniques such as text compression have been used to understand the lifestyles 152 of cardholders [1]. In addition, graph-based approaches have facilitated the analysis 153 of complex relationships between cardholders and merchants as a node-level task [3], 154 and the refinement of marketing strategies as a node-level task [28]. These diverse 155 applications underscore the versatility of HINs in unraveling complex interactions 156 within heterogeneous financial networks, as comprehensively reviewed in [29]. 157

¹⁵⁸ **3** Problem Definition

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Throughout this section, we introduce the notions of HIN and random metapath walks
and discuss the problem addressed in this work. Table 1 shows the mathematical symbols and their definitions used in this article.

Symbol	Definition
G	Dataset of all ego-centric cardholder graphs.
G_k	The k^{th} ego-centric cardholder graph in \mathbb{G} .
$\mathcal{N}_G, \mathcal{R}_G$	Set of nodes and edges in G .
N_G, E_G	Set of node and edge types in G .
τ_N, τ_E	Type mapping functions for nodes and edges.
A_k, D_k, W_k	Adjacency, diagonal, and transition matrices of G_k .
\mathcal{P}, p, π_{mp}	Predefined set of metapaths, a metapath, and its instance.
γ	Teleportation parameter used during random walks.
M	Quantity of negative samples generated during training.
ϕ	Learned graph-level embedding vectors for G.
h	Hidden state representation derived from the model.
α_1, α_2	Margins used in the double-triplet loss function.
θ	Set of all parameters in the G-HIN2VEC model.
W_v, W_e, W_G	weight matrices learned for nodes, edges, and graphs.

 Table 1: Mathematical Symbols and Definitions

162 **Definition 1.** Heterogeneous Information Network, Heterogeneous Information 163 Network, denoted HIN, is defined as a network $G = (\mathcal{N}_G, \mathcal{R}_G, \tau_N, \tau_E, W)$ where G164 is a weighted directed graph, where \mathcal{N}_G and \mathcal{R}_G denote the set of nodes and edges, 165 $W \in \mathbb{R}^{|\mathcal{N}_G|x|\mathcal{N}_G|}$ is the weight matrix, and τ_N and τ_E are type mapping functions for 166 nodes and edges, respectively. In HINs, node types are represented by $\tau_N : \mathcal{N}_G \to \mathcal{N}_G$, 167 where \mathcal{N}_G is a set of node types, and the relations between nodes are indicated by 168 $\tau_E : \mathcal{R}_G \to E_G$, where E_G is a set of edge types.

For HINs, metapaths are used to generate random sequences guided by a predefined
 schema, defined as follows:

Definition 2. Random Metapath Walk. Given the schema of G as defined in Def. 1, a metapath $p \in \mathcal{P}$ is defined as the sequence of triplets (n_i, e_i, n_{i+1}) where $n_i \in N_G$ are the source and target node types, and $e \in E_G$ is the edge type, p is denoted as follows:

$$p: \{ (n_0, e_0, n_1) \to (n_1, e_1, n_2) \dots \to (n_{l-1}, e_{l-1}, n_l) \}$$

$$\tag{1}$$

An instance $\pi_{mp} \sim p(G)$ is a randomized process that begins at $v_i; \tau_N(v_i) = n_i$, and at each iteration moves with respect to a specific sampling strategy Pr(.), to the next v_j . After l iterations, the random metapath walk instance is denoted as the sequence $\pi_{mp} = \{ \langle v_i, e_i, v_{i+1} \rangle \sim Pr(v_i | v_{i-1}; p \in \mathcal{P}) \}_{i=0}^l$ following the naive sampling strategy, defined as a uniform random walk constrained by neighboring node types according to the metapath schema, similar to the approaches in [30, 31]. This ensures that each step of the walk follows the heterogeneous relationships defined by the network schema.

$$Pr(v_i|v_{i-1}; p \in \mathcal{P}) = \begin{cases} \frac{1}{|\mathcal{N}_{n_i}(v_{i-1})|} & e_i \in E \text{ and } \tau_E(e_i) = r_i \\ 0, & otherwise. \end{cases}$$
(2)

where $\mathcal{N}_{n_i}(v)$ denotes the neighbors of v of type n_i , and v_i denotes the node i^{th} in 171 the metapath sequence and $e_i = (v_{i-1}, v_i)$. It is important to mention that n_i and r_i 172 denote the node and relation type of the i^{th} element in the metapath schema in p, 173 respectively. A metapath instance π_{mp} is completed after l iterations, ensuring that 174 the start and end node types match $(\tau_N(n_0) = \tau_N(n_l))$, as required by the schema. 175 This symmetry signifies a structured path through the network, following the sampling 176 strategy of Equation 2. If the path length l allows, the sequence is considered valid 177 and reflects the relationships defined by the metapath p; otherwise, it's discarded as an 178 incomplete. The recursive aspect of the walk, $Pr(v_{l+1}|v_l; p \in \mathcal{P}) = Pr(v_0|v_l; p \in \mathcal{P})$, 179 allows the process to be continuous, maintaining the integrity of the network structure. 180 This methodology is common in HG [30, 31] and adapted for heterogeneous graphs in 181 182 [<mark>16</mark>].

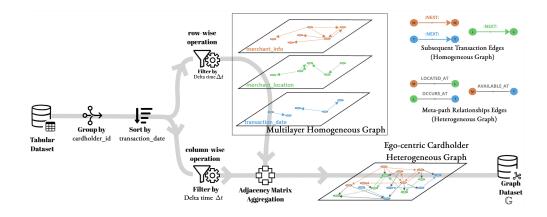


Fig. 1: Illustration of transforming credit card transaction data into an ego-centric cardholder heterogeneous graph dataset, illustrating the process of layering multiple graphs and metapaths to encapsulate the diverse financial interaction patterns within the network.

Problem Analysis and Definition for Cardholder Transactions. Instead of using a tripartite large transaction network to model the problem as a node-level representation [3], we propose to build an ego-centric cardholder graph dataset G to analyze and uncover collective hidden behavior patterns as a graph-level representation problem.

Definition 3. Ego-centric cardholder graph. Given a set of graphs $\mathbb{G} = \{G_i\}_{i=1}^n$, G_k is the k^{th} heterogeneous ego-centric cardholder graph, including merchant names and code categories (MCC), locations, and discretized time units [32], as nodes as nodes $\mathcal{N}_{G_k} \subset \mathcal{N}_G$,

$$\mathcal{N}_G = \bigcup_c^{cols} \mathcal{N}_{G_c} \tag{3}$$

The term 'cols' refers specifically to the attributes following within the transaction data:merchant_info, merchant_location, and transaction_date. A detailed description of these fields is provided in Section 5.1. The cardholder's transaction is the edge $\mathcal{R}_{G_k} = \{(v_i, v_j) \in$ $\mathcal{N}_{G_k} \times \mathcal{N}_{G_k}, w_{i,j}^k \in W_k : (v_i, v_j, w_{i,j}^k)$ and the cardholder's transition matrix $W_k \in [0,1]^{V_k \times V_k}$ is defined from the adjacency matrix G_k denoted A_k , where $[A_k]_{ij}$ represents the total consecutive pairs of transactions within a specific time window Δt , set to 24 hours, if the node types are the same in the cardholder's historical transaction records,,

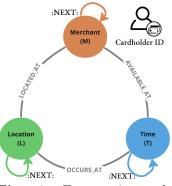


Fig. 2: Ego-centric cardholder heterogeneous graph schema

$$[A_k]_{ij} = \sum_{\substack{\tau_N(v_i) = \tau_N(v_j) \\ \text{row-wise operation}}} [1]_{\Delta t} + \sum_{\substack{\tau_N(v_i) \neq \tau_N(v_j) \\ \text{column-wise operation}}} 1$$
(4)

The transition matrix W_k is refined with a 2-hop step with a column stochastic matrix $W_k = (A_k D_k^{-1})^2$, where D_k is the diagonal matrix with $D_{ij} = \sum_{j=1}^{|\mathcal{N}_{G_k}|} A_{k,(i,j)}$. We amplify the signal in historical data by refining the transition matrix as a weight matrix to enrich the topological and semantic features in G_k . To avoid any confusion, we refer to self-loops in the graph schema as 'next transaction' edges, denoted by :NEXT:, as shown in Figure 2.

¹⁹⁴ **Problem Definition.** After defining the ego-centric cardholder graph dataset \mathbb{G} , we ¹⁹⁵ aim to learn the vector representations $\phi \in \mathbb{R}^{|\mathbb{G}| \times d}$ for every graph $G_i \in \mathbb{G}$, where d¹⁹⁶ is the embedding vector size, d > 0.

Problem 1. (Learn from graph substructures) Given a graph $G_k \in \mathbb{G}$, and a set of metapath instances $\pi_{mp} \sim p$, learn an embedding function $f_G : G_k \to \mathbf{h}_{G_k} \in \mathbb{R}^d$ that preserves the substructure properties of G_k in the latent graph embeddings space ϕ .

Problem 2. (Avoid aggregation functions) The aggregation function operates on graph substructures to represent G_k using average, sum, or max pooling layers; this technique ignores the graph topology. Given a graph $G_k \in \mathbb{G}$, learn ϕ that preserves the proximity between similar graphs in \mathbb{G} and avoid explicit proxy aggregation functions that operate on latent substructure graph embedding.

²⁰⁸ 4 The proposed approach

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Our framework is designed based on an intuitive analogy of graph-level embeddings to define a custom loss function. In this section, we first introduce our motivation and present G-HIN2VEC as an unsupervised learning framework for heterogeneous graphs.

212 4.1 Motivation

The intuition behind our framework is based on a simple analogy with graph kernels for graph-level embeddings. Given two graphs G_i and G_j , for each substructure of an atomic graph a distribution-based measure g is quantified as the similarity between two graphs,

$$D(G_i, G_j) = \sum_{v=1}^{U} g(\mathbf{h}_{i,v}, \mathbf{h}_{j,v})$$
(5)

where $U = \mathcal{N}(G_i) \cap \mathcal{N}(G_j)$ is the set of common substructures in both graphs. In this case nodes where $\mathcal{N}(G_i)$ represent nodes of G_i and $\mathbf{h}_{i,v}$ could indicate the color of the node v in G_i for WL-OA [33], or a random graphlet starting from v for graphlet kernel [23] or a subgraph where the ego node is v for SP-kernel [24], and D is considered as a graph representation kernel. In GNNs, g is applied to atomic graph substructures and D is considered as a graph representation,

$$D(G_i, \emptyset) = \sum_{v=1}^{U} g(\mathbf{h}(i, v), \emptyset) = \sum_{v=1}^{N_{G_i}} w_v \mathbf{h}(i, v)$$
(6)

Here, g could be a static pooling operation such as average operation (where $w_v = \frac{1}{|N_{G_i}|}$) or a learned aggregation layer [17]. Regardless of the local properties encoder function Q could be added and applied to \mathbb{G} to represent G_i by an n-dimensional vector representing the distances from all graphs.

$$Q(G_i) = \bigcup_{G_j}^{\mathbb{G}} \{ D(G_i, G_j) \}$$
(7)

In Equation 5 and 6, g is seen as a distance function that quantifies the dispersion within and between graphs for different local D and global Q representations. Our goal is to learn the graph representation by quantifying this dispersion without the need for explicit aggregation of the graph substructures. Simultaneously, our goal is to avoid using the true distance matrix (Equation 7) for global properties.

4.2 G-HIN2VEC Embedding Learning

The key novelty of G-HIN2VEC is to determine if a metapath instance $\pi_{\rm mp}$ from a given semantic context $p \in \mathcal{P}$ is a subset of the heterogeneous graph G_i , "Does $\pi_{\rm mp} \subseteq G_i$?", thereby learning graph proximity through intra-graph substructures.

Given \mathbb{G} and $p^+ \in \mathcal{P}$, the objective is to maximize the probability,

$$\arg\max_{\theta} \prod_{G_i \in G} \prod_{\pi_{\rm mp} \in p^+(G_i)} Pr(\pi_{{\rm mp}_i}^{(.)}|G_i;\theta)$$
(8)

where $\pi_{\rm mp}^{(.)} = \{\langle v_{i,k}, e_{i,k}, v_{i,k+1} \rangle\}_{k=0}^{l}$ is a sequence of triplets with respect to p^+ , which can be defined as a semantic substructures of G_i , and $Pr(\pi_{\rm mp}^{(.)}|G_i;\theta)$ represents the conditional probability of having $\pi_{\rm mp}^{(.)}$ given G_i .

To learn a graph representation $\phi \in \mathbb{R}^{|\mathbb{G}| \times d}$, we made a simple extension to the heterogeneous skip-gram model presented in [16], to incorporate the metapath schema to learn from graph substructure by maximizing logarithmic probability,

$$\arg\max_{\theta_1,\theta_2} \sum_{G_i \in G} \sum_{\pi_{\rm mp} \in p^+(G_i)} \sum_{t=1}^l \log(\Pr(\pi_{\rm mp}^{(t+)}|G_i;\theta_1) \Pr(\pi_{\rm mp}^{(\neq t+)}|G_i;\theta_2))$$
(9)

Here, it is assumed that the positive metapath context instance $\pi_{mp}^{(\neq t+)} = \{ \langle v_{i,k}, e_{i,k}, v_{i,k+1} \rangle \}_{k=0,k\neq t}^{l}$ and the target instance $\pi_{mp}^{(t+)} = \{ \langle v_{i,t}, e_{i,t}, v_{i,t+1} \rangle \}$ are independent for a given G_i , where $\pi_{mp}^{(t+)}$ represents the t^{th} triplet in the metapath sequence and $\pi_{mp}^{(\neq t+)}$ represents the entire sequence excluding the t^{th} triplet.

In general, a heterogeneous graph requires more than one metapath to capture rich semantics; for this, G-HIN2VEC expands Equation 9 to cover the entire set of predefined metapaths \mathcal{P} ,

$$\arg\max_{\theta_1,\theta_2} \sum_{G_i \in \mathbb{G}} \sum_{p^+ \in \mathcal{P}} \sum_{\pi_{\rm mp} \in p^+(G_i)} \sum_{t=1}^l log Pr(\pi_{\rm mp}^{(t+)}|G_i;\theta_1) + log Pr(\pi_{\rm mp}^{(\neq t+)}|G_i;\theta_2)$$
(10)

where $Pr(\pi_{mp}^{(.)}|G_i)$ is defined as

$$\frac{exp(\mathbf{h}_{\pi_{\mathrm{mp}}^{(.)}}^{+} \cdot \mathbf{h}_{G_{i}})}{\sum_{G_{j} \in \mathbb{G}} \sum_{\pi_{\mathrm{mp}_{j}} \in p^{+}(G_{i})} exp(\mathbf{h}_{\pi_{\mathrm{mp}_{j}}^{(.)}}^{+} \cdot \mathbf{h}_{G_{j}})}$$
(11)

In order to train our G-HIN2VEC model more efficiently and avoid the exhaustive computation of considering every substructure within the entire graph dataset for each metapath in \mathcal{P} and target element in $\pi_{mp}^{(.)}$, we adopt a negative sampling technique. Specifically, instead of using negative samples from different graphs in the dataset, we generate negative samples directly within the graph of interest using Algorithm 1. This allows us to create more contextually relevant and computationally efficient negative instances. For every positive instance, we generate 5 negative instances, setting the M negative sample instances to 5 for each positive instance, thus maintaining a 1:5 ratio. This ratio is a tunable hyperparameter, and while our current infrastructure supports a 1:5 ratio, this can be adjusted according to the scale and capacity of the training setup. The sampling distribution for each metapath in \mathcal{P} is carefully specified, drawing inspiration from [14]. In the same direction, Equation 10 can be expressed as

a distance-based objective function following Equation 5 and 6 to customize the loss function introduced in [15][20]. Therefore, we have the following objective:

$$\mathscr{L} = \sum_{\substack{\pi_{\rm mp}^+ \sim p^+(G_i) \\ \pi_{\rm mp}^- \sim p^-(G_i) \\ (p^+, p^-) \sim \mathcal{P} \\ p^+ \neq p^-}} \underbrace{\left[g_{nn} (\mathbf{h}_{\pi_{\rm mp}^{t+}}^+, \mathbf{h}_{G_i}^+)^2 - g_{nn} (\mathbf{h}_{\pi_{\rm mp}^{t-}}^-, \mathbf{h}_{G_i}^-)^2 + \alpha_1 \right]_+}_{\substack{N^{ode} \\ Triplet} : \text{ Triplet node loss}} + \underbrace{\left[f_{nn} (\mathbf{h}_{\pi_{\rm mp}^{\pm t+}}^+, \mathbf{h}_{G_i}^+)^2 - f_{nn} (\mathbf{h}_{\pi_{\rm mp}^{\pm t-}}^-, \mathbf{h}_{G_i}^-)^2 + \alpha_2 \right]_+}_{Graph}_{Triplet} : \text{ Triplet graph loss}}$$
(12)

where $[\cdot]_{+} = max(\cdot, 0)$, and $p^{-} \sim_{unif.} \mathcal{P}$ is the negative metapath and π_{mp}^{-} is the negative metapath instance defined as a random sequence of triplets with respect to p^{-} . Note that π_{mp}^{-} does not necessarily exist in \mathbb{G} following Algorithm 1.

Hidden substructure representations are the output of a shared weight network for each triplet element, nodes and edge, $\mathbf{h}_{v_k} = \sigma(W_v \vec{x}_{v_k})$ and $\mathbf{h}_{e_k} = \sigma(W_e \vec{x}_{e_k})$, respectively, with $\vec{x}_v \in \mathbb{R}^{|\mathcal{N}_G|}$ and $\vec{x}_e \in \mathbb{R}^{|E|}$ are the one-hot indicator vectors, and $W_v \in \mathbb{R}^{|\mathcal{N}_G| \times d}$ and $W_r \in \mathbb{R}^{|E| \times d}$ are weight matrices. The same applies for the hidden representation of the graph $\mathbf{h}_{G_i} = \sigma(W_G \vec{x}_{G_i})$, with $\vec{x}_{G_i} \in \mathbb{R}^{\mathbb{G}}$ and $W_G \in \mathbb{R}^{\mathbb{G} \times d}$ are the embedding and weight matrices, $\sigma(\cdot)$ is the sigmoid function. Then a metapathtype-aware concatenation mechanism is used to stabilize the learning process with respect to the heterogeneity of metapaths as a triplet concatenation operation $\mathbf{h}_{\pi_{e_i}^{(\cdot)}} = \text{Concat}(\pi_{\text{mp}}^{(\cdot)})$, defined as

$$\mathbf{h}_{\pi_{\mathrm{mp}}^{(.)}} = W_p(\prod_{k=1}^l (\frac{1-\beta}{2} \mathbf{h}_{v_k}) \odot (\beta \mathbf{h}_{e_k}) \odot (\frac{1-\beta}{2} \mathbf{h}_{v_{k+1}}))$$
(13)

where $\mathbf{h}_{\pi_{\mathrm{mp}}^{(.)}} \in \mathbb{R}^c$ is the hidden representation of $\pi_{\mathrm{mp}}^{(.)}$ and $W_p \in \mathbb{R}^{d \times c}$ is a linear transformation of a nonlinear function to project the hidden representations of the substructure to a specific output dimension, and $\beta \in [0, 1]$ is a signal amplifier for triplet relations, set to 0.4. Same for graph hidden representation where $W_p \mathbf{h}_{G_i} \in \mathbb{R}^c$. Equation 13 is a metapath-aware operation used for similarity measurement, without an activation function.

In summary, given the projected feature vector for G_i and $\pi_{\rm mp}^{(\cdot)}$ positive and negative contexts, we learn two distinct functions to measure the similarity between the hidden representations of the graph and nodes, $< \mathbf{h}_{\pi_{\rm mp}^{t+}}^{+}, \mathbf{h}_{G_i}^{+}, >$ and $< \mathbf{h}_{\pi_{\rm mp}^{t-}}^{-}, \mathbf{h}_{G_i}^{-}, >$, respectively, with $g_{nn}(\cdot)$, and between the hidden representations of the graph and the metapath instance, $< \mathbf{h}_{\pi_{\rm mp}^{\pm t+}}^{+}, \mathbf{h}_{G_i}^{+}, >$ and $< \mathbf{h}_{\pi_{\rm mp}^{\pm t-}}^{-}, \mathbf{h}_{G_i}^{-}, >$, respectively, with $f_{nn}(\cdot)$. Following [34], both $g_{nn}(\cdot)$ and $f_{nn}(\cdot)$ are fully connected layers with a one-dimensional output, instead of using static functions such as Euclidean distance or cosine similarity.

As $g_{nn}(\cdot)$ and $f_{nn}(\cdot)$ represents a learned metric where the largest the value more the hidden representations are dissimilar, therefore, the dissimilarity and probability defined in Equation 10 must be correlated positively with both functions. Similarly to [34], we define both functions with a softmax activation layer to normalize the output in $[0, 1]^2$ and keep only one dimension as a dissimilarity value formulated as follows:

$$\begin{cases} g_{nn}(\mathbf{h}_{\pi_{\mathrm{mp}}^{(\cdot)}}^{+}, \mathbf{h}_{G_{i}}^{+}) = \operatorname{softmax}(W_{g}^{T} \cdot (\mathbf{h}_{\pi_{\mathrm{mp}}^{(\cdot)}}^{+}, \mathbf{h}_{G_{i}}^{+}) + B_{g})_{0} \\ f_{nn}(\mathbf{h}_{\pi_{\mathrm{mp}}^{(\cdot)}}^{+}, \mathbf{h}_{G_{i}}^{+}) = \operatorname{softmax}(W_{f}^{T} \cdot (\mathbf{h}_{\pi_{\mathrm{mp}}^{(\cdot)}}^{+}, \mathbf{h}_{G_{i}}^{+}) + B_{f})_{0} \end{cases}$$
(14)

where $W_g \in \mathbb{R}^{2c \times 2}$, $W_f \in \mathbb{R}^{2c \times 2}$, $B_g \in \mathbb{R}^{2c \times 1}$, and $B_f \in \mathbb{R}^{2c \times 1}$, are the weight matrices for the learned metric function g_{nn} and f_{nn} and their bias terms, respectively.

	Algorithm 1: MetapathSeqNoising Function.					
	Input : $\pi_{\rm mp}^+, p^-, l, \lambda$					
	Output : π_{mp}^{-} negative metapath instance.					
	$l' = \lceil \lambda l \rceil; //$ Number of noise edges ;					
	$(v_t^-, v_{t+1}^-) \leftarrow \text{Shuffle}(\{v \in V \tau_N(v) \in p^-\}, l');$					
235	$e_t^- \leftarrow \text{Shuffle}(\{e \in E \tau_E(v_t^-, v_{t+1}^-) \in p^-\}, l');$					
	// Noise injection in $\pi_{\rm mp}^+$ as a concatenation process;					
	$l_1 = \left\lceil \frac{l-l'}{2} \right\rceil$ and $l_2 = l - l_1;;$					
	$\pi_{\mathrm{mp}}^{-} \leftarrow \left\{\pi_{i,k}^{+}\right\}_{k=1}^{l_{1}} \oplus \left\{\right\}_{t=1}^{l'} \oplus \left\{\pi_{i,k}^{+}\right\}_{k=l_{2}+1}^{l};$					
	Return : π_{mp}^{-}					

236

In our loss definition in Equation 12, we employ two margin threshold terms, α_1 237 and $\alpha_2 \in [0, 1]$, to modulate the similarity and dissimilarity within and between 238 graph representations. Specifically, α_1 , set to 1, regulates intra-graph similarity, 239 ensuring that positive samples of nodes and substructures within the same graph are 240 embedded closely together in the embedding space. On the other hand, α_2 , set to 241 0.6, governs inter-graph dissimilarity, ensuring that negative samples of nodes and 242 substructures are sufficiently separated in the embedding space. In the unsupervised 243 learning context, where graph labels are unavailable, we refine the weights of G-244 HIN2VEC by minimizing a double-triplet loss function. This process is part of our 245 training data preparation, which aims to generate embeddings for the graph dataset, 246 nodes, and relations. These embeddings are denoted as $\phi \in \mathbb{R}^{|\mathbb{G}| \times d}$ for the graph-level, 247 $X_v \in \mathbb{R}^{|\mathcal{N}_G| \times d}$ for nodes, and $X_r \in \mathbb{R}^{|\mathcal{R}_G| \times d}$ for relations. Our focus in this work is on 248 the representation at the graph-level ϕ . 249

Algorithm 2: G-HIN2VEC training algorithm.

Input : The heterogeneous graph dataset G, metapaths $\mathcal{P} = \{p_1, \dots p_k\}; k > 0,$ global learned weight W_j , batch size Bwalk length l, negative samples M, noise level λ Output : The global weight W_{i+1} matrix. G =Shuffle(\mathbb{G}, B); // Shuffle and Random B samples. for i = 1, ..., B do $p^+ = \text{Shuffle}(p, 1);$ $p^- =$ Shuffle $(\{p \in \mathcal{P} | p \neq p^+\}, M);$ $\pi_{\mathrm{mp}}^+ := \mathrm{MetapathSeq}(G_i, p^+, l);$ for m = 1, ..., M do // M random negative samples, set to 5. $\pi_{\rm mp}^- = {\rm MetapathSeqNoising}(\pi_{\rm mp}^+, p^-, l, \lambda);$ $\mathbf{h}_{G_i} = \sigma(W_G \vec{x}_{G_i});$ for k = 1, ..., l do // For each Triplet in $\pi_{\rm mp}^+$ and $\pi_{\rm mp}^-$; $< v_{i,k}^+, e_{i,k}^+, v_{i,k+1}^+ > \leftarrow \pi_{i,k}^+;$ $< v_{i,k}^{-}, e_{i,k}^{-}, v_{i,k+1}^{-} > \leftarrow \pi_{i,k}^{-};$ // Relation hidden representation transformations; $\mathbf{h}_{e_{i,k}^{+}} = \sigma(W_r \vec{e}_{i,k}^{+});$ $\mathbf{h}_{e_{i,k}}^{i,n} = \sigma(W_r \vec{e_{i,k}});$ // Node hidden representation transformations; $\mathbf{h}_{v_{i,k}}^{+}, \mathbf{h}_{v_{i,k+1}}^{+} = \sigma(W_v \vec{v}_{i,k}^{+}), \sigma(W_v \vec{v}_{i,k+1}^{+});$ $\mathbf{h}_{v_{i,k}}, \mathbf{h}_{v_{i,k+1}} = \sigma(W_v \vec{v}_{i,k}), \sigma(W_v \vec{v}_{i,k+1});$ end t =Shuffle(interval[1, l], 1)// Sample target context ; // Representations alignment and concatenation; $\mathbf{h}_{G_i}^+ = W_{p^+} \mathbf{h}_{G_i}; \quad \mathbf{h}_{G_i}^- = W_{p^-} \mathbf{h}_{G_i};$ $\mathbf{h}_{\pi_{\mathrm{mp}}^{t+}}^{+} = \mathrm{Concat}(\mathbf{h}_{\pi_{\mathrm{mp}}^{t+}}^{-}); \quad \mathbf{h}_{\pi_{\mathrm{mp}}^{t-}}^{-} = \mathrm{Concat}(\mathbf{h}_{\pi_{\mathrm{mp}}^{t-}}^{-});$ $\mathbf{h}^+_{\pi^{\neq t+}_{\mathrm{mp}}} = \mathrm{Concat}(\mathbf{h}_{\pi^{\neq t+}_{\mathrm{mp}}}); \quad \mathbf{h}^-_{\pi^{\neq t-}_{\mathrm{mp}}} = \mathrm{Concat}(\mathbf{h}_{\pi^{\neq t-}_{\mathrm{mp}}});$ // Output layer as learned dissimilarity metric; $d_{node}^+, d_{node}^- = g_{nn} (\mathbf{h}_{\pi_{mn}^{t+}}^+, \mathbf{h}_{G_i}^+)^2, g_{nn} (\mathbf{h}_{\pi_{mn}^{t-}}^-, \mathbf{h}_{G_i}^-)^2;$ $d_{mp}^{+}, d_{mp}^{-} = f_{nn} (\mathbf{h}_{\pi_{mp}^{\pm n+}}^{+}, \mathbf{h}_{G_{i}}^{+})^{2}, f_{nn} (\mathbf{h}_{\pi_{mp}^{\pm n-}}^{-}, \mathbf{h}_{G_{i}}^{-})^{2};$ // Cost function Equation 12; $Cost_i + = [d_{node}^+ - d_{node}^- + \alpha_1]_+ + [d_{mp}^+ - d_{mp}^- + \alpha_2]_+;$ end end $W_{i+1} := \text{miniBatchSGD}(W_i, Cost_i) // \text{Weight updates};$

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4.3 Training Data Preparation

As introduced previously, G-HIN2VEC uses the negative sampling technique to generate training data. Therefore, data preparation is a crucial phase in our approach. As detailed in Algorithm 2 and illustrated in Figure 3, we train our model in minibatches, sampled from \mathbb{G} , and then generate the positive context π_{mp}^+ from G_i with a predefined metapath $p^+ \sim \mathcal{P}$ following our custom sampling strategy.

$$Pr(v^{i}|v^{i-1};p^{+}) = \begin{cases} \beta \frac{1}{|\mathcal{N}_{n_{i}}(v^{i-1})|} & e_{i} \in \mathcal{R}_{G} \text{ and } \tau_{E}(e_{i}) = r_{i} \\ (1-\beta) \frac{1}{|\mathcal{N}_{\neq n_{i}}(v^{i-1})|} & e_{i} \in \mathcal{R}_{G} \text{ and } \tau_{E}(e_{i}) \neq r_{i} \\ 0 & e_{i} \notin \mathcal{R}_{G}; \text{ where } e_{i} = (v^{i}, v^{i-1}) \end{cases}$$
(15)

where β is the teleportation term to escape nodes with high centrality and $\mathcal{N}_{\neq n_i}(v)$ denotes the neighbor v^i of different types of nodes $n_i \in p^+$, denoted by MetapathSeqin Algorithm 1.

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As in Figure 3, our approach intro-256 duces noise to the original positive 257 metapath instances $\pi_{\rm mp}^+$, creating 258 negative contexts π_{mp}^- within the 259 same graph rather than from dif-260 ferent graphs, This is achieved by 261 perturbing π_{mp}^+ with alternative 262 metapaths p^- uniformly sampled 263 from \mathcal{P} . The noise level $\lambda \in [0, 1]$ is 264 set to 0.3; a process we denote as 265 MetapathSeqNoising. After gen-266 erating both positive and negative 267 instances, we apply a series of lin-268 ear transformations to derive the 269 final triplet hidden representations 270 to estimate the dissimilarity metrics. 271

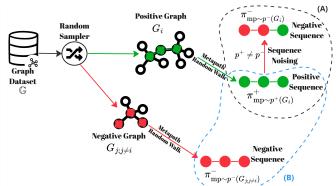


Fig. 3: G-HIN2VEC training data generation process, highlighting the novel approach (A) that deviates from traditional methods (B). It showcases the creation of positive \bullet and negative \bullet samples in an unsupervised learning context.

²⁷³ Depending on the quantified metrics in our unsupervised framework, we optimize the
²⁷⁴ global model weights by minimizing the double-triplet loss via back-propagation and
²⁷⁵ gradient descent to learn meaningful graph-level embeddings for the heterogeneous
²⁷⁶ graph dataset.

277 5 Experiments

In this section, we evaluate the proposed model in a real-world credit card transaction
dataset from a European bank. Our empirical analysis focuses on qualitative and
quantitative analyses. It is important to mention that the dataset used in the current
research work is fully aligned with the General Data Protection Regulation (GDPR)
in the European Union to protect personal data as defined in Article 4.



5.1 Datasets and Tasks 283

We conducted our experiments on a dataset comprising records from 100K card-284 holders and transactions from 2019 to 2021. The dataset's schema includes the 285 transaction table: cardholder_id (as unique INT), merchant_info (as VARCHAR), 286 representing merchant code category and merchant name such as '5661-Shoe Stores' 287 merchant_location (as VARCHAR), detailing the location like 'Paris-France', and 288 transaction_date (as DATE), indicating when the transaction occurred, for instance, 289 '2019-06-21'. This raw data was transformed into an ego-centric cardholder graph 290 dataset, as elaborated in Section 3.3. Furthermore, we used the cardholder table: 291 cardholder_id (as unique INT), Gender (as VARCHAR), Age (as FLOAT) and Income 292 (as FLOAT). All types are according to SQL data types. 293

The cardholder socio-demographic attributes used for supervised machine learning 294 experiments include: 295

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- Gender, $Y_{Gender}^i \in \{0,1\}, \forall i \in \{1,..,n\}$) as a binary attribute indicating the i^{th} cardholder's gender, where 0 represents one gender and 1 represents another.
- Income, Yⁱ_{Income} ∈ [0,1], ∀i ∈ {1,..,n})as a normalized attribute representing the ith cardholder's income.
 Age, Yⁱ_{Age} ∈ [0,1]∀i ∈ {1,..,n} as a normalized attribute repre-
- senting the i^{th} cardholder's age.

For quantitative analysis, we performed a binary classification task on Y_{Gender} and 298 a regression task on Y_{Age} and Y_{Income} to benchmark different hidden representation 299 models on predictive tasks for the ego-centric graph of cardholders. On the other 300 hand, we also performed a qualitative analysis based on cardholder representations 301 as a cluster analysis task to illustrate and interpret hidden communities. 302

5.2 Baselines and Experimental Settings 303

In this section, we outline the baseline methods used for comparison with our G-304 HIN2VEC approach, focusing on homogeneous and heterogeneous graph embeddings, 305 as well as other graph-level representation techniques. These baselines are detailed in 306 Table 2 and grouped into three primary categories. Our G-HIN2VEC method is imple-307 mented using the StellarGraph framework, a Python library for machine learning on 308 graphs. All graph embeddings for the cardholder were learned using G-HIN2VEC and 309 the baseline models. For G-HIN2VEC specifically, the experimental settings include a 310 dropout rate of 0.5, and the use of the SGD optimizer. We adjust the margin thresh-311 olds α_1 and α_2 in our loss function, in Equation 12, to 1 and 0.5, respectively, with 312 a learning rate of 0.005. Additionally, weight decay is accompanied by an L2 penalty 313 set at 0.001 over 50 epochs. 314

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After the pretraining phase on the graph dataset of cardholders, we benchmarked the 316 performance of the generated embeddings on a set of downstream tasks. Linear and 317 logistic regression were implemented on the graph embedding vector for regression and 318 classification tasks, respectively. The dataset was divided into training, validation, and 319

Category	Category Description	Method	Method Description	
Vectorization-based	Uses node and graph features to represent graphs, focusing on node	N-grams $(N = 1, 2)$	Captures local graph features through individual and pairs of a frequency, emphasizing simpler patterns.	
	frequency, graph statistics, and structural properties such as centrality measures, graph density, and spectral properties.	Bag-of-Features (BoF)	Incorporates comprehensive graph features, including statistics on node degree, clustering coefficients, and triangles and squares sub- graph counts.	
Kernel-based	Employing graph kernels, such as outlined in Equation 5 to map graphs into a vector space. This transformation facilitates the computation of a	Graphlet kernel (GK) [23]	Represents graphs based on the frequency of small subgraphs (graphlets) throughout the graph dataset, ideal for capturing local topology.	
		Shortest path kernel (SPK) [24]	Encodes each graph by the shortest path lengths between nor within the graph dataset, reflecting global connectivity.	
	distance matrix for comparing graphs, as illustrated in Equation 7.	Weisfeiler-Lehman framework (WLG) [33]	Refines graph representation through iterative relabeling based on neighborhood structures to capture structural changes over multiple scales, reflecting both local and global structural differences through- out the graph dataset.	
		Deep GK, Deep SP, Deep WL [21]	Apply deep learning techniques with traditional graph kernels to gen- erate graph-level embeddings. All variants capture different complex structural graph features in the graph dataset.	
GNN-based	Uses deep learning architectures to generate node-level and graph-level embeddings, for node-level architectures an aggregation function is used to produce graph-level embeddings from node-level from node-level and edge-level embeddings, as in Equation 6.	Metapath2vec [16]	Uses guided random walks by metapaths in heterogeneous graphs to generate node embeddings. For graph-level features, the graph node embeddings are then aggregated using mean to produce graph-level embeddings.	
		HIN2VEC [15]	Generate node and relation embeddings in heterogeneous networks by considering multiple types of nodes and relationships. For graph-level features, graph nodes and relationships are aggregated by average to form graph-level embeddings.	
		Graph2Vec [20]	Treat the entire graph as an individual document in a corpus, employ- ing a document embedding approach to learn graph embeddings. This method captures global graph properties and structural features.	
		DiffPool [17]	Implement a differentiable graph pooling module that hierarchically aggregates nodes embeddings into clusters, forming a new, coarser graph at each layer, until final cluster as the graph-level representa- tions.	

Table 2: Detailed overview of graph-based methods categorized by their approach and core features, including graph-level and heterogeneity, with a focus on graph representations.

test sets based on the cardholder ID to ensure that all transactions related to a single cardholder fall into the same group. The split ratio was 2:1:1 for training, validation, and test sets, respectively. The performance results reported on Table 4 are the average of 10-fold cross-validation test sets, with the statistical significance of each metric validated by calculating the p-value. Performance for graph-level representation in the classification task was evaluated using averaged accuracy, AUC, and F1 metrics, and for regression tasks using R-squared (R2) and mean absolute error (MAE) metrics.

327 5.3 Empirical Validation

We performed empirical validation on the graph dataset following the experimental settings described earlier. For non-graph-level representation models such as HIN2Vec, we added a simple averaging layer on top of each node-level representation to generate graph representations. In heterogeneous guided random walk-based GNNs, the definition of the metapath is required.

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For this purpose, experts provided a set of metapaths to answer specific business questions (BQ), as shown in Table 3. Furthermore, metapath-free baselines ignore the predefined metapaths for both node- and graph-level representation methods, ³³⁷ and this will not be considered in both experimental analyses due to the original ³³⁸ implementations.

Category	Method	Gender		Income		Age	
		Acc.	AUC	R2	MAE	R2	MAE
Vectorization based	N-gram (1 & 2-grams)	0.6133	0.601	0.1067	0.1531	0.1045	12.7074
vectorization based	Bag of Features (BoF)	0.7295	0.722	0.1751^{*}	0.1409^{*}	0.2994	10.9955
	Graphlet kernel [23] (GK)	0.5825	0.5647	0.0449	0.1618	0.0846	12.5174
Kernel based	Shortest path kernel [24] (SPK)	0.5477	0.5002	0.0698	0.1597	0.0873	12.9465
	Weisfeiler-Lehman [33] (WL)	0.7001	0.6993	0.2030	0.1410	0.4301	9.8510
	Deep GK	0.5399	0.5185	0.0472	0.1469	0.0842	11.4422
Deep Kernel based [21]	Deep SP	0.5566	0.5137	0.0798	0.1629	0.0922	13.1960
	Deep WL	0.7032^{*}	0.7292^{**}	0.2255	0.1381^{*}	0.4717	9.5978^{**}
	Metapath2vec [‡] [16]	0.6102	0.5586	0.1105**	0.1489	0.1349	12.3272
	$Graph2Vec^{\dagger\$}[20]$	0.7220	0.7331	0.2394^{*}	0.1354	0.5384	9.4021
GNN based	$HIN2VEC^{\parallel}[15]$	0.7809	0.7906	0.2318	0.1399^{*}	0.6385^{*}	6.6019
	DiffPool ^{†§} [17]	0.8047^{*}	0.8194	0.3088**	0.1212**	0.7108*	5.9277
	G-HIN2VEC ^{‡§}	0.8244^{*}	0.8311^{*}	0.3310^{*}	0.1137**	0.6843^{**}	6.3157*

339 5.4 Quantitative Analysis

Table 4: Performance of various graph-based methods in predicting cardholder attributes. Superscripts denote model compatibility: [‡] for heterogeneous graphs, [†] for homogeneous graphs, ^{||} for node-level, and [§] for graph-level downstream tasks. Statistical significance is denoted as: ^{**}p < 0.01, ^{*}p < 0.05.

³⁴⁰ 5.4.1 Regression tasks.

In regression tasks targeting age 341 and income prediction, our evalua-342 tion reveals that vectorization and 343 graph kernel-based methods strug-344 gle to effectively model the complex 345 relationships inherent in heteroge-346 neous graph data, resulting in infe-347 rior performance. In contrast, GNN-348 based models show enhanced out-349 comes due to their advanced archi-350 tectures, which are better suited 351 to capture the complex interactions 352 within these graphs. Notably, our G-353 HIN2VEC model demonstrates sig-354

Table 3: Set of business questions as metapaths by financial experts, where ● Merchant,

 \bigcirc Location, and \bigcirc Time stand for node types.

BQ 1:	What spending habit does the cardholder have?
Metapath 1	M
BQ 2:	Where does the cardholder use the credit card?
Metapath 2	● <u>:Located_in:</u> ● Located_in:
BQ 3:	When does the cardholder use the credit card?
Metapath 3	
BQ 4:	When and where is the credit card used?
Metapath 4	Available_at:

nificant improvements over the strong baseline, DiffPool, with a 7.18% increase in R-squared and a 6.19% decrease in mean absolute error for income prediction, despite its non-Gaussian distribution. For age prediction, which follows a Gaussian distribution, G-HIN2VEC matches the performance of DiffPool. These results affirm the robustness of G-HIN2VEC in generating effective graph-level embeddings for regression tasks, highlighting its potential for broader application in complex graph-based analysis.

³⁶² 5.4.2 Classification task.

The gender classification performance of various methods is comprehensively detailed 363 in Table 4. Among the benchmarked methods, vectorization methods are observed to 364 outperform graph kernel-based methods, showcasing their better suitability for clas-365 sification tasks involving categorical data. In contrast, among the baselines, DiffPool 366 stands out as the most effective model. It highlights the benefits of utilizing sophis-367 ticated aggregation techniques rather than averaging at the top of the node-level, 368 thus enhancing the quality of graph-level embeddings. In the specific case of our G-369 HIN2VEC model, significant improvements in gender classification are evident, with 370 increases of 2.44% in accuracy, 1.85% in F1 score, and 1.43% in AUC compared to 371 DiffPool. These statistically significant results demonstrate G-HIN2VEC's superior 372 capability in leveraging complex graph-level embeddings for classification tasks. 373

Additionally, the analysis of the graph 374 structures within our dataset, particu-375 larly their size distribution and nega-376 tive assortativity coefficients as shown 377 in Figure 4, supports these outcomes. 378 This structural characteristic suggests 379 that G-HIN2VEC not only effectively 380 handles disassortative graphs but also 381 benefits from adjustments such as the 382 incorporation of a teleportation term, β , 383 in our sampling strategy (see Equation 384 15), which enhances model robustness 385 and confirms the quantitative findings 386 of improved performance. Furthermore, 387

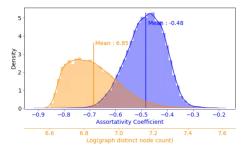


Fig. 4: The probability distribution of (a) the log graph sizes and (b) the assortativity coefficient of graphs in the dataset.

a primary limitation of GNN models, as highlighted in [35], involves their sensitiv ity to assortativity during node-level tasks, which can extend to graph-level tasks,
 potentially impacting performance; our model's design addresses and mitigates this
 limitation effectively.

³⁹² 5.5 Qualitative analysis

In this section, we investigated the cluster assignment of cardholder behavior through the graph-level embeddings. Figure 5 presents a t-SNE visualization of cardholder embeddings, where each color signifies a distinct cluster, corresponding to a unique behavioral pattern in credit card usage. Our assumption is that cardholders who are semantically similar in using credit cards tend to be embedded in close proximity, as shown in [20] and [16] for graph- and node-level representations, respectively.

The clustering of embeddings into 16 distinct groups, as determined by the elbow method using k-means, reveals a granular view of cardholder behaviors, with each cluster capturing a particular lifestyle preference that aligns with previous findings in credit card usage research [1]. In post-clustering analysis, we engaged domain experts to identify cluster identities, extracting and examining metapath instances that were sampled during training. This analysis aimed to quantify the occurrence of directed
sequences within each cluster, thus providing a narrative for the lifestyle categories
annotated in Figure 5. Thus, two cardholders are semantically similar if their credit
card usage behavior is similar with respect to a set of predefined metapaths in Table
3.

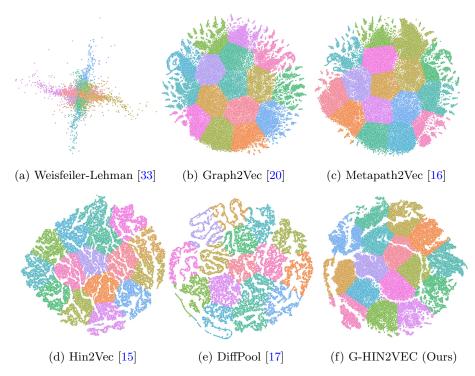


Fig. 5: Cardholder embeddings t-SNE visualization of 16 identified clusters using different embedding algorithms. Each color represents a distinct cluster; ● Grocery Shoppers, ● Commuters ○ Young Workers ● High-Tech ● Elderly ● Restaurant-goers
● Drivers ● Musicophiles ● Bookworm/Bibliophiles ● Business ● FastFood-goers ● Householders ● Cash-Only ● Gamblers ● Peripatetic/Travelers ● Epicureans.

The t-SNE visualizations highlight how well different graph-level embedding meth-410 ods group similar cardholder behaviors. The Weisfeiler-Lehman method results in 411 overlapping clusters, suggesting that it may not be as effective in identifying the finer 412 details of the graph-level features. Graph2Vec and Metapath2Vec improve upon this 413 with more defined clusters, reflecting their stronger ability to map out both the indi-414 vidual elements and graph-level structures. HIN2VEC goes a step further, creating 415 even more distinct clusters that show its capability to capture the variety within 416 the graph dataset, and the DiffPool method stands out with its highly distinct and 417 compact clusters, which means that it is particularly good at understanding complex 418 patterns. Our G-HIN2VEC method generates embeddings that are more distinct than 419

Metapath2Vec but not as tightly clustered as HIN2VEC and DiffPool, suggesting that
it provides a detailed, yet comprehensive overview of cardholder behavior. This aligns
with the solid results we see from our quantitative analysis, where our method shows
a strong ability to accurately group cardholder behaviors.

424 6 Conclusion And Future Work

In this paper, we introduce G-HIN2VEC, a novel approach to generate heteroge-425 neous graph-level embeddings. Our method utilizes a double-triplet loss and an 426 unsupervised learning framework that incorporates negative sampling, eliminating 427 the need for graph-to-graph matching. This allows for more efficient learning without 428 relying on negative samples from the entire graph dataset. We used a real-world 429 financial dataset, modeling it as ego-centric graphs for cardholders to benchmark 430 various graph-level representation models. Our results show competitive performance 431 of G-HIN2VEC with state-of-the-art models, with notable improvements in gender 432 classification accuracy of 2.45% and income prediction R-squared (R2) of 7.19%. 433 Furthermore, for age prediction, we achieved a 6.55% increase in mean absolute error 434 (MAE) compared to the strong baseline, DiffPool. 435

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Looking ahead, we plan to enhance G-HIN2VEC by integrating dynamic metapath 437 selection mechanisms to address node and edge type imbalances in Heterogeneous 438 Information Networks (HINs). We also aim to extend the application of G-HIN2VEC 439 to a wider range of graph-level downstream tasks. Exploring innovative negative 440 sampling techniques, such as sequence noising and nonsampling approaches, will 441 be another focus to further improve graph-level representation learning within an 442 unsupervised framework. A current limitation of our methodology is its reliance on 443 a transductive learning model, which may not perform well with unseen data. To 444 overcome this, our future work will focus on an inductive model that can generalize to 445 new, unseen graph instances, enhancing the applicability and utility of our approach 446 in the field of graph representation learning. 447

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453 Data Availability

⁴⁵⁴ Due to privacy considerations and adherence to the General Data Protection Regula-⁴⁵⁵ tion in the European Union (GDPR) as defined in Article 4, the data supporting this

456 study are not publicly available.

457 Declarations

458 Conflict of Interest

⁴⁵⁹ The authors declare that they have no conflict of interest.

460 Ethical Approval

- ⁴⁶¹ The authors approve that the research presented in this article is conducted following
- the principles of ethical and professional conduct.

463 Consent to Participate

464 Not applicable.

465 Consent for Publication

466 Not applicable.

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