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*DFT2FEFFIT***: a density functional theory-based structural toolkit to analyze EXAFS spectra**

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This article presents a Python-based program, *DFT2FEFFIT*, to regress theoretical extended X-ray absorption fine structure (EXAFS) spectra calculated from density functional theory (DFT) structure models against experimental EXAFS spectra. To showcase its application, Ce-doped fluorapatite $[Ca₁₀ (PO_4)_6F_2$] is revisited as a representative of a material difficult to analyze by conventional multi-shell least-squares fitting of EXAFS spectra. The software is open source and publicly available.

1. Introduction

Extended X-ray absorption fine structure (EXAFS) spectroscopy is an established method for characterization of the local structure of liquids, glasses and crystalline materials (Chantler *et al.*, 2020). The chemical nature, number and distance of atoms located in successive spherical shells around the X-ray photoabsorber are obtained by fitting the experimental EXAFS signal to the theoretical $\chi(k)$ function (Stern *et al.*, 1975; Rehr & Albers, 2000; Rehr *et al.*, 2020):

$$
\chi(k) = S_0^2 \sum_{i}^{\text{shells}} \frac{N_i}{kR_i^2} f_i \exp(-2R_i/\lambda_i) \exp(-2\sigma_i^2 k^2)
$$

 \times sin(2kR_i + ϕ _i), (1)

where *k* is the photoelectron wavenumber, $k = \sqrt{\frac{2m_e \Delta E_0}{\hbar^2}}$ $(m_e$ is the mass of the electron?), ΔE_0 is the shift in the Fermi level between experiment and theory, S_0^2 is a scale factor taking into account amplitude damping due to multielectron effects, the sum is over shells of atoms of a particular type *i* and similar distance from the photoabsorber, N_i is the coordination number, R_i is the interatomic distance, f_i is the photoelectron backscattered amplitude, λ_i is the mean free path of the photoelectron, σ_i^2 is the mean-square radial displacement of atoms in the *i*th shell (Debye–Waller term) and Φ_i is the phase shift of the electronic wave. Although equation (1), strictly speaking, applies only to single scattering paths from neighboring shells of atoms, Rehr & Albers (1990) showed that this formula can be generalized to represent the contribution from *N* equivalent multiple scattering contributions of path length 2*R*.

Characterizing the local structure requires solving the inverse problem of finding a plausible structure model that corresponds to the measured EXAFS signal (Timoshenko *et al.*, 2019; Terry *et al.*, 2021). As powerful a structural method as EXAFS is, the analysis of chemically complex and structurally defective materials is challenging (Boyanov *et al.*, 1996).

Because the information content of quality EXAFS data is typically bandwidth-limited to about $k_{\text{max}} \simeq 14 \text{ Å}^{-1}$, two overlapping subshells separated by less than \sim 0.10–0.15 Å are unresolved in multi-elemental materials. Furthermore, EXAFS fails to distinguish neighboring atoms of similar scattering power and phase shifts ($\Delta Z <$ ~10). Yet another difficulty arises when the interatomic distances in an atomic shell are unequal. In equation (1), the radial distribution function (RDF) of the atoms in shell *i* is assumed to be Gaussian,

$$
G_i(R) = \frac{N_i}{\sigma \sqrt{2\pi}} \exp\left[-\frac{(R - R_i)^2}{2\sigma_i^2}\right].
$$
 (2)

Poorly crystalline and compositionally heterogeneous materials frequently have more complicated analytical atomic distributions than Gaussian. An asymmetric distribution of distances results in an apparent loss of coordination and usually reinforces correlations between the N and σ parameters in the fit (Marcus *et al.*, 1986; Crozier, 1997). Still, the asymmetric shape of the distribution may be obtained by a cumulant EXAFS analysis of the disordered shell, but this model-independent method is limited to small degrees of disorder when the cumulant series rapidly converges within the EXAFS *k* range (Dalba & Fornasini, 1997).

A prototypical case of a material difficult to analyze by EXAFS is fluorapatite $[Ca_{10}(PO4)_6F_2$, FAp]. Its structure comprises two Ca sites, a larger nine-coordinated Ca1 site forming with the phosphate groups the walls of a honeycomb framework, and a smaller seven-coordinated Ca2 site along the sub-nanometre-sized tunnels containing the column F site (Hughes *et al.*, 1989) (Fig. 1). The coordination of Ca1 is really $6+3$ rather than 9, and that of Ca2 is $6+1$, and the six Ca1 $-$ O and six Ca2—(O,F) distances are unequal, which is a source of uncertainty in the determination of the site occupancy of a substituent (Fig. 2). The situation is not improved beyond the first coordination shell, because the Ca—O, Ca—P and Ca—Ca distances are widely distributed and partly overlap.

Natural FAp is commonly enriched in trivalent rare earth elements (REE) (Harlov & Rakovan, 2015; Manceau *et al.*,

Figure 1

The structure of FAp projected in the *ab* plane (Hughes *et al.*, 1989; Harlov & Rakovan, 2015). The F atom is located in the middle of the tunnel.

2022). The substitution may occur on the Ca1 or Ca2 site, depending on the ionization energy of the substituent (Manceau *et al.*, 2024). The charge excess resulting from REE^{3+} for Ca^{2+} substitution is generally considered to be balanced by parallel Na⁺ \leftrightarrow Ca²⁺ substitution on the Ca1 or Ca2 octahedral site, or $Si^{4+} \leftrightarrow P^{5+}$ substitution on the tetrahedral site (Rønsbo, 1989; Fleet *et al.*, 2000). Furthermore, the charge balance may occur locally, or indifferently at a short- or long-range distance. Other substitutional mechanisms can be envisaged, such as a coupled REE³⁺ + F^{$-$} \leftrightarrow Ca²⁺ substitution with incorporation of an additional F^- ion in the FAp tunnels, and a coupled $2REE^{3+} + \text{Vac} \rightarrow 3Ca^{2+}$ substitution with creation of a Ca vacancy. Clearly, the conventional multi-shell EXAFS fitting approach has a high risk of failing to find the correct local structure of REE due to the inherent large number of unknowns to fit with multiple optima in parameter space. Not all of the atomic shells can be refined independently without causing correlations between parameters. Hence, *a priori* information is required to make educated guesses. Another inherent problem, besides the non-uniqueness of the model parameters resulting from overlapping subshells, is the lack of discrimination between Si and P

Figure 2

Population histograms of (*a*) the Ca1—(O,P,Ca) and (*b*) the Ca2—(O,F,P, Ca) distances in fluorapatite (Hughes *et al.*, 1989). The number of atoms is counted in intervals of 0.05 A.

backscatterers, and the low sensitivity of EXAFS spectroscopy to F, Na and vacancies. 229 230

An alternative to multi-shell EXAFS fitting is to use the geometric constraints of density functional theory (DFT) models for comparative modeling of the EXAFS spectra (Harris *et al.*, 2006; Cotelesage *et al.*, 2012). The EXAFS signal is a one-dimensional projection in reciprocal space of a spherically averaged three-dimensional structure. Incorporation of an impurity in a solid does not modify just its atomic pair distances, but also those of its neighboring atoms and its bond angles. This information is compressed in EXAFS data and not easily and reliably accessible, motivating the use of DFT models as three-dimensional templates of the whole impurity environment. Recently, we followed this approach and showed by calculating the EXAFS spectra of DFT models that Ce^{3+} occupies the Ca2 site in FAp with a coupled Si^{4+} substituent at a short distance $\left[d(Ce^2 - Si) = 3.09 \text{ Å}, Ce^2\right]$ -Siclose model], while the coupled $\text{Na}^+ \leftrightarrow \text{Ca}^{2+}$ substitution on the Ca1 or Ca2 octahedral site was negated (Manceau *et al.*, 2024). 231 232 233 234 235 236 237 238 239 240 241 242 243 244 245 246 247 248

Here, we extend our previous approach and present *DFT2FEFFIT*, a general regression analysis tool that best-fits an EXAFS spectrum using the χ_i functions generated by *FEFF* (Version 8.2; Ankudinov & Rehr, 1997) from a DFT model. Its capabilities are demonstrated with reconstructions of the Ce L_3 edge EXAFS spectrum of the FAp reference from Cerro de Mercado near Durango, Mexico (Manceau *et al.*, 2022). Using *DFT2FEFFIT*, we show that alternative Ce^{3+} $+ F^- \leftrightarrow Ca^{2+}$ substitution (Ce2–F model) and 2Ce³⁺ + Vac \rightarrow $3Ca^{2+}$ substitution (2Ce2–Vac model) are nonfitting models. 249 250 251 252 253 254 255 256 257 258

2. Software details

2.1. Input

DFT2FEFFIT is open-source code written in Python. It uses a command-line interface, which is invoked with a Python entry point. The user is then prompted to enter the input filename. The following input data are required: the experimental χ function to fit (line 1), the number of scattering paths (*n*, line 2), the *k* weighting of χ for the fit ($k^n \chi$, line 3), the *k* range of the fit (line 4), S_0^2 (line 5), whether ΔE is adjusted (integer 1) or fixed (integer 0) (line 6), the value of ΔE if no variation is allowed (integer 0), or its interval of variation $(\Delta E_{\text{min}}, \Delta E_{\text{max}})$ and the step size (line 7), and the list of scattering paths [lines 8 to 8 + $(n - 1)$]. Each path line is structured as follows: a line number (*e.g.* path ID); a string (*e.g.* chemical symbol, SS or MS for single or multiple scattering path); the path distance, only added for easy reference and not actually part of the fit; χ_i ; the format of χ_i [*FEFF* format (chip000*n*) or simply two columns, *k*, χ_i]; whether σ_i is optimized (1) or not (0); the initial σ_i value; $\sigma_{i,\text{min}}$; $\sigma_{i,\text{max}}$; and the path ID with which the σ_i value is co-varied, -1 if the σ values are not linked. Path lines commented with a hash (#) symbol are ignored. At the end of the refinement, the code provides the optimized values, the experimental and calculated *k*-weighted χ functions (ASCII data and plot), the 264 265 266 267 268 269 270 271 272 273 274 275 276 277 278 279 280 281 282 283 284 285

modulus and real part of the Fourier transform (*i.e.* RDF) of $k^n \chi_{\text{exp}}$ and $k^n \chi_{\text{fit}}$ using a Kaiser–Bessel window ($\beta = 2.5$), and the fit residual expressed as the normalized sum of squared differences $[NSS = \sum (k^n \chi_{exp} - k^n \chi_{calc})^2 / \sum (k^n \chi_{exp})^2]$.

2.2. Calculation

The software seeks to minimize NSS by optimizing σ_i for each ΔE value. Because χ_{calc} varies nonlinearly with σ_i [equation (1)], the minimization of NSS toward the local minimum is performed iteratively by following the negative of the first derivative of equation (1) with respect to σ_i (gradientdescent method) at each iteration. The scheme is iterated until NSS reaches a plateau (\triangle NSS = 10^{-7}) or for a user-defined fixed number of iterations. Convergence is speeded up by rescaling the input σ_i values to the $[-1, 1]$ range according to $\overline{\sigma} = 2(\sigma_i - \sigma_{\text{mean}})/(\sigma_{\text{max}} - \sigma_{\text{min}})$, with $\sigma_{\text{mean}} = 0.5(\sigma_{\text{max}} - \sigma_{\text{max}})$ σ_{min}). Wolfe's conditions (Wolfe, 1969; Nocedal & Wright, 2006) are used to determine the appropriate step size for each line search of strict descent at a point $m_n = \overline{\sigma}_n$. The update to *m_n* for the next iteration is $m_{n+1} = m_{n+1} + \alpha_n p_n$ [m_{n+1} appears **on both sides of this equation?],** where α_n is the new step size computed from the line search at m_n to satisfy the Wolfe conditions and p_n is the search direction. The input scripts for the DFT models are deposited in the NOMAD repository (Draxl & Scheffler, 2019) at https://dx.doi.org/10.17172/ NOMAD/2024.02.09-1.

The gradient-descent optimization method was preferred over the Levenberg–Marquardt (LM) method for several reasons. The LM method requires an estimation of the Jacobian of the forward problem in order to build the Gauss– Newton Hessian matrix. This step is not needed with the steepest-descent algorithm. The LM method does not include a line search that would ensure proper convergence (Wolfe's conditions), and would therefore need to be coupled with Wolfe's conditions to ensure convergence. Lastly, the LM method requires another tuning parameter for the damping of the diagonal of the Gauss–Newton Hessian matrix.

3. Case study

EXAFS spectroscopy probes the local structure of a given element up to about 6 A . Modeling by DFT the bonding environment of a substituent up to this distance requires optimizing the geometry of rather large clusters comprising more than one hundred atoms. DFT methods exploiting a linear combination of plane waves, as implemented in the *Vienna Ab-initio Simulation Package* (*VASP*), are in this respect more cost effective than methods adopting a linear combination of local atomic orbitals, usually represented as Gaussian-type orbitals, as implemented in *CRYSTAL* (Dovesi *et al.*, 2014). Comparison of the DFT structures obtained with *VASP* and *CRYSTAL14* on Ce–FAp clusters of 336 atoms $(2 \times 2 \times 2$ supercell, radius $\simeq 6$ Å) showed that *CRYSTAL14* did not provide superior models, even with the accurate PBEsol functional (Perdew *et al.*, 2008) and basis sets of triplezeta quality for Ca, P, O and F. Therefore, all optimizations 327 328 329 330 331 332 333 334 335 336 337 338 339 340 341 342

reported in this study were performed with *VASP* to speed up the calculations. Details of the *VASP* parameters and functionals are given in the supporting information.

The radial distributions of Ce in the Ce2–Si-close, Ce2–F and 2Ce2–Vac models up to $R = 4.3 \text{ Å}$ are shown in Fig. 3, and the Cartesian coordinates of the models are listed in the supporting information. The Ce2–F model essentially differs from the optimal Ce2–Si-close model by (i) an increase in coordination from 6 to 7, and hence an increase in the average Ce2 (O,F) distance from 2.43 \AA to 2.48 \AA due to the incorporation of the interstitial F atom at 2.42 \AA from Ce2, and (ii) the displacement to shorter distance of two Ca atoms $[d(Ce2-Ca) = 3.65-3.75 \text{ Å}]$ and to longer distance of two further Ca atoms $[d(Ce2-Ca) = 4.26 \text{ Å}]$. Regarding the 2Ce2– Vac model, one Ce atom of the paired Ce atoms (Ce2_1) has a similar local structure to Ce in Ce2–Si-close, whereas the other Ce atom (Ce2_2) has a distinctive bonding environment characterized by a split of the first (O,F) shell and longer Ce2—Ca distances.

The best-fit results of the Ce L_3 edge EXAFS spectrum for the Durango FAp with the calculated EXAFS spectra for the three DFT models up to $R = 4.3$ Å, together with the corresponding RDF, are shown in Fig. 4. The data were collected at room temperature on beamline ID24-DCM at the European Synchrotron Radiation Facility (ESRF) in high energy-resolution mode (HERFD-EXAFS) using five analyzer crystals bent to a radius of 0.5 m (Rovezzi *et al.*, 2017; Glatzel *et al.*,

2021). Best-fit calculations were conducted by optimizing initially ΔE and one σ value for all SS paths ($\chi_{NLEG} = 2$ in *FEFF*). Afterwards, individual SS paths were grouped into shells (O1, P1, P2, Ca) and their σ_i values refined. The criterion for retaining a new σ_i was that the fit had to improve by at least 5% and be physically meaningful. A single σ value was applied to all multiple scattering (MS) paths calculated by *FEFF* ($\chi_{NLEG=4}$ - $\chi_{NLEG=2}$). The optimal ΔE value varied marginally (<1 eV) from one fit to another. S_0^2 was fixed to 0.9. Best-fit EXAFS parameters of the three DFT models are reported in the supporting information.

Our results show that coupled $Ce^{3+} + F^- \leftrightarrow Ca^{2+}$ (Ce2–F model) and $2Ce^{3+} + Vac \rightarrow 3Ca^{2+}$ (2Ce2–Vac model) are incompatible models. Adding an F atom or removing a Ca atom near a Ce atom are sources of disorder, which manifests on the calculated RDF by a misfit of the Ce2—(O,F) shell and a loss of amplitude of the Ce2—P and Ce2—Ca peaks. Thus, these results underscore the high sensitivity of *DFT2FEFFIT* for detailed characterization of the local structure of elements in complex environments. EXAFS alone does not allow differentiation between P and Si neighbors, for their scattering powers are similar, nor the detection of a light F atom and a vacancy site. This distinction becomes possible by comparing the theoretical EXAFS spectra derived from DFT structure models with experiment. *DFT2FEFFIT* may, therefore, be considered as a useful tool for the validation of hypothesisdriven structure models based on EXAFS analysis.

Figure 3

Population histograms of the computed Ce2 $-$ (O,F,P,Ca,Ce) distances for (*a*) the Ce2–Si-close model, (*b*) the Ce2–F model and (*c*), (*d*) the two Ce atoms of the 2Ce2–Vac model. Computation details can be found in the supporting information. The number of atoms is counted in intervals of 0.05 Å.

computer programs

Figure 4

Experimental and DFT-derived theoretical Ce L_3 edge EXAFS spectra and radial distribution functions (magnitude and real part of the k^2 -weighted Fourier transform). (*a*), (*b*) Ce2–Si-close model, (*c*), (*d*) Ce2–F model and (*e*), (*f*) 2Ce2–Vac model.

4. Availability of *DFT2FEFFIT*

The Python script of *DFT2FEFFIT* is available in the supporting information and at https://gitlab.esrf.fr/ scientific-software/dft2feffit.

5. Related literature

For further literature related to the supporting information, see Blöchl (1994), Gautier *et al.* (2015), Gonthier *et al.* (2012), Kresse (1995), Kresse & Furthmüller (1996), Kresse & Joubert

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(2011).

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(1999), Perdew *et al.* (1996) and Steinmann & Corminboeuf

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