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# **DFT2FEFFIT:** a density functional theory-based structural toolkit to analyze EXAFS spectra

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This article presents a Python-based program, DFT2FEFFIT, to regress theoretical extended X-ray absorption fine structure (EXAFS) spectra calculated from density functional theory (DFT) structure models against experimental EXAFS spectra. To showcase its application, Ce-doped fluorapatite [Ca<sub>10</sub>-(PO<sub>4</sub>)<sub>6</sub>F<sub>2</sub>] is revisited as a representative of a material difficult to analyze by conventional multi-shell least-squares fitting of EXAFS spectra. The software is open source and publicly available.

#### 1. Introduction

Extended X-ray absorption fine structure (EXAFS) spectroscopy is an established method for characterization of the local structure of liquids, glasses and crystalline materials (Chantler *et al.*, 2020). The chemical nature, number and distance of atoms located in successive spherical shells around the X-ray photoabsorber are obtained by fitting the experimental EXAFS signal to the theoretical  $\chi(k)$  function (Stern *et al.*, 1975; Rehr & Albers, 2000; Rehr *et al.*, 2020):

$$\chi(k) = S_0^2 \sum_{i}^{\text{shells}} \frac{N_i}{kR_i^2} f_i \exp(-2R_i/\lambda_i) \exp\left(-2\sigma_i^2 k^2\right)$$

 $\times \sin(2kR_i + \phi_i),\tag{1}$ 

where k is the photoelectron wavenumber,  $k = \sqrt{(2m_e\Delta E_0)/\hbar^2}$ ( $m_e$  is the mass of the electron?),  $\Delta E_0$  is the shift in the Fermi level between experiment and theory,  $S_0^2$  is a scale factor taking into account amplitude damping due to multielectron effects, the sum is over shells of atoms of a particular type *i* and similar distance from the photoabsorber,  $N_i$  is the coordination number,  $R_i$  is the interatomic distance,  $f_i$  is the photoelectron backscattered amplitude,  $\lambda_i$  is the mean free path of the photoelectron,  $\sigma_i^2$  is the mean-square radial displacement of atoms in the *i*th shell (Debye–Waller term) and  $\Phi_i$  is the phase shift of the electronic wave. Although equation (1), strictly speaking, applies only to single scattering paths from neighboring shells of atoms, Rehr & Albers (1990) showed that this formula can be generalized to represent the contribution from N equivalent multiple scattering contributions of path length 2R.

Characterizing the local structure requires solving the inverse problem of finding a plausible structure model that corresponds to the measured EXAFS signal (Timoshenko *et al.*, 2019; Terry *et al.*, 2021). As powerful a structural method as EXAFS is, the analysis of chemically complex and structurally defective materials is challenging (Boyanov *et al.*, 1996).



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Because the information content of quality EXAFS data is typically bandwidth-limited to about  $k_{\rm max} \simeq 14 \,\text{\AA}^{-1}$ , two overlapping subshells separated by less than  $\sim 0.10-0.15$  Å are unresolved in multi-elemental materials. Furthermore, EXAFS fails to distinguish neighboring atoms of similar scattering power and phase shifts ( $\Delta Z < \sim 10$ ). Yet another difficulty arises when the interatomic distances in an atomic shell are unequal. In equation (1), the radial distribution function (RDF) of the atoms in shell i is assumed to be Gaussian. 

$$G_i(R) = \frac{N_i}{\sigma\sqrt{2\pi}} \exp\left[-\frac{(R-R_i)^2}{2\sigma_i^2}\right].$$
 (2)

Poorly crystalline and compositionally heterogeneous materials frequently have more complicated analytical atomic distributions than Gaussian. An asymmetric distribution of distances results in an apparent loss of coordination and usually reinforces correlations between the N and  $\sigma$  para-meters in the fit (Marcus et al., 1986; Crozier, 1997). Still, the asymmetric shape of the distribution may be obtained by a cumulant EXAFS analysis of the disordered shell, but this model-independent method is limited to small degrees of disorder when the cumulant series rapidly converges within the EXAFS k range (Dalba & Fornasini, 1997). 

A prototypical case of a material difficult to analyze by EXAFS is fluorapatite  $[Ca_{10}(PO4)_6F_2, FAp]$ . Its structure comprises two Ca sites, a larger nine-coordinated Ca1 site forming with the phosphate groups the walls of a honeycomb framework, and a smaller seven-coordinated Ca2 site along the sub-nanometre-sized tunnels containing the column F site (Hughes et al., 1989) (Fig. 1). The coordination of Ca1 is really 6+3 rather than 9, and that of Ca2 is 6+1, and the six Ca1-Oand six Ca2-(O,F) distances are unequal, which is a source of uncertainty in the determination of the site occupancy of a substituent (Fig. 2). The situation is not improved beyond the first coordination shell, because the Ca-O, Ca-P and Ca-Ca distances are widely distributed and partly overlap. 

Natural FAp is commonly enriched in trivalent rare earth elements (REE) (Harlov & Rakovan, 2015; Manceau *et al.*,



Figure 1

The structure of FAp projected in the *ab* plane (Hughes *et al.*, 1989; Harlov & Rakovan, 2015). The F atom is located in the middle of the tunnel.

2022). The substitution may occur on the Ca1 or Ca2 site, depending on the ionization energy of the substituent (Manceau et al., 2024). The charge excess resulting from  $REE^{3+}$  for Ca<sup>2+</sup> substitution is generally considered to be balanced by parallel Na<sup>+</sup>  $\leftrightarrow$  Ca<sup>2+</sup> substitution on the Ca1 or Ca2 octahedral site, or Si<sup>4+</sup>  $\leftrightarrow$  P<sup>5+</sup> substitution on the tetra-hedral site (Rønsbo, 1989; Fleet et al., 2000). Furthermore, the charge balance may occur locally, or indifferently at a short- or long-range distance. Other substitutional mechanisms can be envisaged, such as a coupled  $\text{REE}^{3+} + \text{F}^- \leftrightarrow \text{Ca}^{2+}$  substitution with incorporation of an additional F<sup>-</sup> ion in the FAp tunnels, and a coupled  $2REE^{3+} + Vac \rightarrow 3Ca^{2+}$  substitution with creation of a Ca vacancy. Clearly, the conventional multi-shell EXAFS fitting approach has a high risk of failing to find the correct local structure of REE due to the inherent large number of unknowns to fit with multiple optima in parameter space. Not all of the atomic shells can be refined indepen-dently without causing correlations between parameters. Hence, a priori information is required to make educated guesses. Another inherent problem, besides the non-unique-ness of the model parameters resulting from overlapping subshells, is the lack of discrimination between Si and P 



#### Figure 2

Population histograms of (*a*) the Ca1-(O,P,Ca) and (*b*) the Ca2-(O,F,P,Ca) distances in fluorapatite (Hughes *et al.*, 1989). The number of atoms is counted in intervals of 0.05 Å.

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backscatterers, and the low sensitivity of EXAFS spectroscopyto F. Na and vacancies.

An alternative to multi-shell EXAFS fitting is to use the 231 geometric constraints of density functional theory (DFT) 232 models for comparative modeling of the EXAFS spectra 233 (Harris et al., 2006; Cotelesage et al., 2012). The EXAFS signal 234 is a one-dimensional projection in reciprocal space of a 235 spherically averaged three-dimensional structure. Incorpora-236 tion of an impurity in a solid does not modify just its atomic 237 pair distances, but also those of its neighboring atoms and its 238 bond angles. This information is compressed in EXAFS data 239 and not easily and reliably accessible, motivating the use of 240 DFT models as three-dimensional templates of the whole 241 impurity environment. Recently, we followed this approach 242 and showed by calculating the EXAFS spectra of DFT models 243 that Ce<sup>3+</sup> occupies the Ca2 site in FAp with a coupled Si<sup>4+</sup> 244 substituent at a short distance [d(Ce2-Si) = 3.09 Å, Ce2-Si-Si)245 close model], while the coupled  $Na^+ \leftrightarrow Ca^{2+}$  substitution on 246 the Ca1 or Ca2 octahedral site was negated (Manceau et al., 247 2024). 248

Here, we extend our previous approach and present 249 DFT2FEFFIT, a general regression analysis tool that best-fits 250 an EXAFS spectrum using the  $\chi_i$  functions generated by 251 FEFF (Version 8.2; Ankudinov & Rehr, 1997) from a DFT 252 model. Its capabilities are demonstrated with reconstructions 253 of the Ce  $L_3$  edge EXAFS spectrum of the FAp reference 254 from Cerro de Mercado near Durango, Mexico (Manceau et 255 al., 2022). Using DFT2FEFFIT, we show that alternative  $Ce^{3+}$ 256 +  $F^- \leftrightarrow Ca^{2+}$  substitution (Ce2–F model) and  $2Ce^{3+} + Vac \rightarrow$ 257 3Ca<sup>2+</sup> substitution (2Ce2–Vac model) are nonfitting models. 258

#### 2. Software details

## <sup>262</sup> **2.1. Input**

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DFT2FEFFIT is open-source code written in Python. It 264 uses a command-line interface, which is invoked with a Python 265 entry point. The user is then prompted to enter the input 266 filename. The following input data are required: the experi-267 mental  $\chi$  function to fit (line 1), the number of scattering paths 268 (*n*, line 2), the k weighting of  $\chi$  for the fit ( $k^n \chi$ , line 3), the k 269 range of the fit (line 4),  $S_0^2$  (line 5), whether  $\Delta E$  is adjusted 270 (integer 1) or fixed (integer 0) (line 6), the value of  $\Delta E$  if no 271 variation is allowed (integer 0), or its interval of variation 272  $(\Delta E_{\min}, \Delta E_{\max})$  and the step size (line 7), and the list of 273 scattering paths [lines 8 to 8 + (n - 1)]. Each path line is 274 structured as follows: a line number (e.g. path ID); a string 275 (e.g. chemical symbol, SS or MS for single or multiple scat-276 tering path); the path distance, only added for easy reference 277 and not actually part of the fit;  $\chi_i$ ; the format of  $\chi_i$  [FEFF 278 format (chip000*n*) or simply two columns,  $k, \chi_i$ ]; whether  $\sigma_i$  is 279 optimized (1) or not (0); the initial  $\sigma_i$  value;  $\sigma_{i,\min}$ ;  $\sigma_{i,\max}$ ; and 280 the path ID with which the  $\sigma_i$  value is co-varied, -1 if the  $\sigma$ 281 values are not linked. Path lines commented with a hash (#) 282 symbol are ignored. At the end of the refinement, the code 283 provides the optimized values, the experimental and calcu-284 lated k-weighted  $\chi$  functions (ASCII data and plot), the 285

modulus and real part of the Fourier transform (*i.e.* RDF) of  $k^n \chi_{exp}$  and  $k^n \chi_{fit}$  using a Kaiser–Bessel window ( $\beta = 2.5$ ), and the fit residual expressed as the normalized sum of squared differences [NSS =  $\sum (k^n \chi_{exp} - k^n \chi_{calc})^2 / \sum (k^n \chi_{exp})^2$ ].

#### 2.2. Calculation

The software seeks to minimize NSS by optimizing  $\sigma_i$  for each  $\Delta E$  value. Because  $\chi_{calc}$  varies nonlinearly with  $\sigma_i$ [equation (1)], the minimization of NSS toward the local minimum is performed iteratively by following the negative of the first derivative of equation (1) with respect to  $\sigma_i$  (gradientdescent method) at each iteration. The scheme is iterated until NSS reaches a plateau ( $\Delta NSS = 10^{-7}$ ) or for a user-defined fixed number of iterations. Convergence is speeded up by rescaling the input  $\sigma_i$  values to the [-1, 1] range according to  $\overline{\sigma} = 2(\sigma_i - \sigma_{\text{mean}})/(\sigma_{\text{max}} - \sigma_{\text{min}})$ , with  $\sigma_{\text{mean}} = 0.5(\sigma_{\text{max}} - \sigma_{\text{min}})$  $\sigma_{\min}$ ). Wolfe's conditions (Wolfe, 1969; Nocedal & Wright, 2006) are used to determine the appropriate step size for each line search of strict descent at a point  $m_n = \overline{\sigma}_n$ . The update to  $m_n$  for the next iteration is  $m_{n+1} = m_{n+1} + \alpha_n p_n [m_{n+1} \text{ appears}]$ on both sides of this equation?], where  $\alpha_n$  is the new step size computed from the line search at  $m_n$  to satisfy the Wolfe conditions and  $p_n$  is the search direction. The input scripts for the DFT models are deposited in the NOMAD repository (Draxl & Scheffler, 2019) at https://dx.doi.org/10.17172/ NOMAD/2024.02.09-1.

The gradient-descent optimization method was preferred over the Levenberg–Marquardt (LM) method for several reasons. The LM method requires an estimation of the Jacobian of the forward problem in order to build the Gauss– Newton Hessian matrix. This step is not needed with the steepest-descent algorithm. The LM method does not include a line search that would ensure proper convergence (Wolfe's conditions), and would therefore need to be coupled with Wolfe's conditions to ensure convergence. Lastly, the LM method requires another tuning parameter for the damping of the diagonal of the Gauss–Newton Hessian matrix.

#### 3. Case study

EXAFS spectroscopy probes the local structure of a given 327 element up to about 6 Å. Modeling by DFT the bonding 328 environment of a substituent up to this distance requires 329 optimizing the geometry of rather large clusters comprising 330 more than one hundred atoms. DFT methods exploiting a 331 linear combination of plane waves, as implemented in the 332 Vienna Ab-initio Simulation Package (VASP), are in this 333 respect more cost effective than methods adopting a linear 334 combination of local atomic orbitals, usually represented as 335 Gaussian-type orbitals, as implemented in CRYSTAL (Dovesi 336 et al., 2014). Comparison of the DFT structures obtained with 337 VASP and CRYSTAL14 on Ce-FAp clusters of 336 atoms 338  $(2 \times 2 \times 2$  supercell, radius  $\simeq 6$  Å) showed that CRYSTAL14 339 did not provide superior models, even with the accurate 340 PBEsol functional (Perdew et al., 2008) and basis sets of triple-341 zeta quality for Ca, P, O and F. Therefore, all optimizations 342

reported in this study were performed with VASP to speed up 343 the calculations. Details of the VASP parameters and func-344 tionals are given in the supporting information. 345

The radial distributions of Ce in the Ce2-Si-close, Ce2-F 346 and 2Ce2–Vac models up to R = 4.3 Å are shown in Fig. 3, and 347 the Cartesian coordinates of the models are listed in the 348 supporting information. The Ce2-F model essentially differs 349 from the optimal Ce2-Si-close model by (i) an increase in 350 coordination from 6 to 7, and hence an increase in the average 351 Ce2 (O,F) distance from 2.43 Å to 2.48 Å due to the incor-352 poration of the interstitial F atom at 2.42 Å from Ce2, and (ii) 353 the displacement to shorter distance of two Ca atoms 354 [d(Ce2-Ca) = 3.65-3.75 Å] and to longer distance of two 355 further Ca atoms [d(Ce2-Ca) = 4.26 Å]. Regarding the 2Ce2– 356 Vac model, one Ce atom of the paired Ce atoms (Ce2\_1) has a 357 similar local structure to Ce in Ce2-Si-close, whereas the other 358 Ce atom (Ce2\_2) has a distinctive bonding environment 359 characterized by a split of the first (O,F) shell and longer 360 Ce2-Ca distances. 361

The best-fit results of the Ce  $L_3$  edge EXAFS spectrum for 362 the Durango FAp with the calculated EXAFS spectra for the 363 three DFT models up to R = 4.3 Å, together with the corre-364 sponding RDF, are shown in Fig. 4. The data were collected at 365 room temperature on beamline ID24-DCM at the European 366 Synchrotron Radiation Facility (ESRF) in high energy-reso-367 lution mode (HERFD-EXAFS) using five analyzer crystals 368 bent to a radius of 0.5 m (Rovezzi et al., 2017; Glatzel et al., 369

2021). Best-fit calculations were conducted by optimizing 400 initially  $\Delta E$  and one  $\sigma$  value for all SS paths ( $\chi_{\text{NLEG}} = 2$  in 401 FEFF). Afterwards, individual SS paths were grouped into 402 shells (O1, P1, P2, Ca) and their  $\sigma_i$  values refined. The 403 criterion for retaining a new  $\sigma_i$  was that the fit had to improve 404 by at least 5% and be physically meaningful. A single  $\sigma$  value 405 was applied to all multiple scattering (MS) paths calculated by 406 *FEFF* ( $\chi_{\text{NLEG}=4} - \chi_{\text{NLEG}=2}$ ). The optimal  $\Delta E$  value varied 407 marginally (<1 eV) from one fit to another.  $S_0^2$  was fixed to 0.9. 408 Best-fit EXAFS parameters of the three DFT models are 409 reported in the supporting information. 410

Our results show that coupled  $Ce^{3+} + F^- \leftrightarrow Ca^{2+}$  (Ce2–F 411 model) and  $2Ce^{3+} + Vac \rightarrow 3Ca^{2+}$  (2Ce2-Vac model) are 412 incompatible models. Adding an F atom or removing a Ca 413 atom near a Ce atom are sources of disorder, which manifests 414 on the calculated RDF by a misfit of the Ce2-(O,F) shell and 415 a loss of amplitude of the Ce2–P and Ce2–Ca peaks. Thus, 416 these results underscore the high sensitivity of DFT2FEFFIT 417 for detailed characterization of the local structure of elements 418 in complex environments. EXAFS alone does not allow 419 differentiation between P and Si neighbors, for their scattering 420 powers are similar, nor the detection of a light F atom and a 421 vacancy site. This distinction becomes possible by comparing 422 the theoretical EXAFS spectra derived from DFT structure 423 models with experiment. DFT2FEFFIT may, therefore, be 424 considered as a useful tool for the validation of hypothesis-425 driven structure models based on EXAFS analysis. 426



397 Figure 3

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398 Population histograms of the computed Ce2-(O.F.P.Ca,Ce) distances for (a) the Ce2-Si-close model, (b) the Ce2-F model and (c), (d) the two Ce atoms of the 2Ce2-Vac model. Computation details can be found in the supporting information. The number of atoms is counted in intervals of 0.05 Å. 399

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### computer programs



#### Figure 4

Experimental and DFT-derived theoretical Ce  $L_3$  edge EXAFS spectra and radial distribution functions (magnitude and real part of the  $k^2$ -weighted Fourier transform). (a), (b) Ce2–Si-close model, (c), (d) Ce2–F model and (e), (f) 2Ce2–Vac model.

#### 4. Availability of DFT2FEFFIT

The Python script of *DFT2FEFFIT* is available in the supporting information and at https://gitlab.esrf.fr/scientific-software/dft2feffit.

#### 5. Related literature

For further literature related to the supporting information, see Blöchl (1994), Gautier *et al.* (2015), Gonthier *et al.* (2012), Kresse (1995), Kresse & Furthmüller (1996), Kresse & Joubert

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(1999), Perdew et al. (1996) and Steinmann & Corminboeuf

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