

A predictability-based characterization of intermittency in turbulence

Ewen Frogé, Carlos Granero-Belinchon, Stéphane G. Roux, Nicolas B.

Garnier, Thierry Chonavel

► To cite this version:

Ewen Frogé, Carlos Granero-Belinchon, Stéphane G. Roux, Nicolas B. Garnier, Thierry Chonavel. A predictability-based characterization of intermittency in turbulence. 1st European Fluid Dynamics Conference (EFDC1), Sep 2024, Aachen, Germany. hal-04694770

HAL Id: hal-04694770 https://hal.science/hal-04694770

Submitted on 11 Sep 2024 $\,$

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

A predictability-based characterization of intermittency in turbulence

E. Frogé*[†], C. Granero-Belinchón*[†], S. G. Roux[‡], N. B. Garnier[‡] and T. Chonavel*

The chaotic nature of the velocity of a turbulent flow, often modeled as a stochastic process, makes the forecast of the future values of velocity from the past ones a complex challenge. Moreover, the intermittency phenomenon implies extreme events at the small scales of the flow velocity, hindering the prediction task. We propose to characterize the predictability of turbulent velocity at time *t* by using the concept of innovation which is defined as the deviation between the actual value of the flow velocity at time *t* and its expected value knowing the precedent ones¹. The estimation of innovation is based on analog forecasting techniques, typically employed in meteorology and dynamical systems ². In this work, we apply analog forecasting methods on a longitudinal turbulent velocity time series from the Modane wind tunnel ³, and propose a characterization of intermittency based on predictability *via* innovation.

The resulting innovation is a non-Gaussian process with heavy-tailed probability density function *i.e.* with extreme events, see figure 1. Despite its white noise structure resulting in a flat second order structure function, higher-order dependencies are significant, as evidenced by the evolution of the flatness. Furthermore, the occurrence of large events in the innovation coincides with the occurrence of large values in the velocity gradient. This highlights the impact of intermittency on the unpredictability of the velocity of a turbulent flow as well as the capacity of innovation to characterize intermittency from a new point of view.



Figure 1: Left) One realization of Modane longitudinal velocity component v(t) (red), its smallest scale increment $\delta_{\tau_s} v(t) = v(t) - v(t - \tau_s)$ (blue) and innovation $\varepsilon(t) = v(t) - \mathbb{E} \{v(t) | v(t - \tau_s), ..., v(t - n\tau_s)\}$ (green). With τ_s being the sampling period of Modane and \mathbb{E} the expected value operator.

Right) Second-order structure function $S_2(\tau) = \mathbb{E}\left\{(Z(t) - Z(t - \tau))^2\right\}$ and flatness $F(\tau) = \frac{1}{3} \frac{\mathbb{E}\left\{(Z(t) - Z(t - \tau))^4\right\}}{S_2(\tau)}$ of *Z*, with *Z* being: the Modane velocity *v* (red) its smallest increment $\delta_{\tau_s} v$ (blue) and innovation ε (green). Lines represent the mean and shadows the standard deviation computed on 10 realizations.

^{*}Department of Mathematical and Electrical Engineering, IMT Atlantique, Lab-STICC, UMR CNRS 6285, 655 Av. du Technopôle, Plouzané, 29280, Bretagne, France

[†]Odyssey, Inria/IMT Atlantique, 263 Av. Général Leclerc, Rennes, 35042, Bretagne, France

[‡]Univ Lyon, ENS de Lyon, CNRS, Laboratoire de Physique, 46, allée d'Italie, Lyon, F-69364, Rhône-Alpes, France

¹Kalman, Journal of Basic Engineering 82 (1960).

²Platzer et al., Journal of the Atmospheric Sciences **78** (2021).

³Kahalerras et al., *Physics of Fluids* **10** (1998).