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# **Empirical Orthogonal Functions for ecology**

- 2 Baptiste Alglave<sup>1,2</sup>, Benjamin Dufée<sup>1,3</sup>, Said Obakrim<sup>4</sup>, and James T. Thorson<sup>5</sup>
- 3 **Abstract:** Spatio-temporal data are ubiquitous in ecology. As the volume of ecological data increases,
- 4 they encompass long time periods on large spatial domains, frequently involving multiple species and
- 5 variables. Developing methods to summarize these data while providing ecological interpretability is
- 6 crucial for maximizing the insights they offer.
- 7 Empirical Orthogonal Functions (EOFs) are a well-documented and widely used method for reducing
- 8 the dimensionality of spatio-temporal data. First, introduced in the 1950s, EOFs essentially involve
- 9 performing Principal Component Analysis on spatio-temporal data. Subsequently, a substantial body
- 10 of literature has developed around EOFs, primarily in the fields of meteorology and climate studies.
- 11 While a substantial body of research has applied EOFs in meteorology and climate science, their use
- 12 in ecology is relatively new and remains overlooked, despite their huge potential.
- 13 In this paper, we aim at presenting the basics of EOFs and introduce new related methods that address
- 14 specific ecological questions. To illustrate their potential, we use two different datasets: (1) satellite
- 15 data for the Normalized Difference Vegetation Index (NDVI) over France, and (2) spatio-temporal
- 16 predictions from an integrated species distribution model that maps several fish species in the Bay of
- 17 Biscay.
- 18 Since EOFs do not incorporate ecological constraints, their results may not always be directly
- 19 interpretable from an ecological perspective. In this paper, we develop a method that incorporates a
- 20 temporal ecological variable into EOFs to improve their interpretability. Using satellite NDVI data,
- 21 we demonstrate how EOFs results can be informed by including a steady seasonal variable, which
- 22 helps to better represent a North-South gradient across France.
- 23 Finally, EOFs can be a valuable tool for investigating community and ecosystem spatio-temporal
- 24 dynamics, though this implies to move to a multivariate framework. We illustrate several ways to
- 25 leverage EOFs for multivariate analysis and highlight shared spatial and temporal patterns among

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- 26 several spatio-temporal variables. Using multispecies fish data from the Bay of Biscay, we identify
- 27 both common temporal trends and shared spatial patterns in reproduction timing and locations. A set
- 28 of reproducible codes are provided in the manuscript to assist ecologists interested in applying these
- 29 techniques in practice.
- 30 Keywords: spatio-temporal data, dimension reduction, satellite data, NDVI, species distribution
- model, multivariate analysis, canonical correlation analysis.

#### 32 1 Introduction

- 33 Spatial and temporal data are ubiquitous in ecological research, providing insights across
- 34 various scales. Survey data, analyzed through multivariate integrated modeling, help
- 35 understanding species distribution, ecosystem states and community dynamics (Isaac et al.,
- 36 2020; Zipkin et al., 2021). Citizen science initiatives yield extensive opportunistic datasets
- 37 over long periods, facilitating studies on phenomena such as bird migration (Martin et al.,
- 38 2020; Sullivan et al., 2014). GPS data allows to track animal movements at high resolution
- 39 (Nathan et al., 2022). Remote sensing offers high-resolution information for monitoring
- 40 land use, habitat suitability, and the impacts of climate change in near real-time (Poggi et al.,
- 41 2021; Garrigues, Allard, and Baret, 2008). Together, these diverse spatio-temporal data
- 42 sources are crucial for unraveling spatial ecological processes, their temporal trends, and
- 43 the interactions affecting ecological processes across various scales.
- 44 Typically, integrated species distribution models (SDM) allow to infer the spatio-temporal
- 45 distribution of species from distinct data sources and provide the common information
- shared between all these data (Isaac et al., 2020; Seaton, Jarvis, and Henrys, 2024). As
- 47 a consequence of the massive amount of data that are gathered to feed the model, the
- 48 spatio-temporal predictions can result in long time series of spatial maps (Alglave, Olmos,

- 49 et al., 2024). These still need to be analysed and processed to study the ecological processes
- 50 structuring these outcomes.
- 51 Given the extensive spatial and temporal coverage of these data, dimension reduction (or
- 52 ordination) methods become critical for synthesizing the information embedded within these
- 53 spatio-temporal data. Empirical Orthogonal Functions (EOFs) represent the keystone method
- 54 for performing dimension reduction on spatio-temporal data. They were first introduced
- 55 by Lorenz (1956), Obukhov (1947), and Fukuoka (1951) and they could be basically
- 56 summarized as a Principal Component Analysis (PCA) performed on spatio-temporal data
- 57 where individuals are locations and variables are time steps. Since their first formulation,
- 58 EOFs methods have entailed a rich literature, particularly in meteorology and climate
- 59 applications (Hannachi, Jolliffe, and Stephenson, 2007).
- 60 Recently, these methods have expanded to ecology. First applications have remained close
- 61 to their original use by analysing the output of climatic or physical models. For instance,
- 62 Gedalof, Peterson, and Mantua (2005) explored the relationship between climatic variables
- 63 and wildland fire data, while other studies analyzed oceanographic and soil variables to
- 64 understand ecosystem dynamics, marine-terrestrial synchrony, and water conservation
- 65 for ecological management (Schrum, John, and Alekseeva, 2006; Iida and Saitoh, 2007;

Di Lorenzo et al., 2008; Woillez et al., 2010; Le Mezo et al., 2016; Berkelhammer, 2019;

67 Wu et al., 2023).

66

- 68 Researchers have also applied EOFs to species' spatio-temporal distributions (with a specific
- 69 emphasis on fish and marine ecosystems), linking them to climate variables, particularly in
- 70 studies of sardines and anchovies in the California Current system (Norton and Mason, 2005)
- 71 or in the Bay of Biscay (Petitgas, Masse, et al., 2006; Petitgas, 2008; Petitgas, Doray, et al.,
- 72 2014). Some research used MFA (a derived method of PCA) to explore the spatial structure
- 73 of the ecosystem based on multi-trophic observations (Woillez et al., 2010; Petitgas, Huret,

- 74 et al., 2018; Grandremy et al., 2023). Additionally, Van Audenhaege et al. (2022) examined
- 75 vent mussel habitats based on imagery data, highlighting small-scale variability influenced
- 76 by tidal cycles and temperature anomalies.
- 77 These methods gained wider recognition through the development of the Vector-
- 78 Autoregressive Spatio-temporal (VAST) package (Thorson, 2019; Thorson, Anderson,
- 79 et al., 2024). VAST implements a joint hierarchical model with an underlying EOFs struc-
- 80 ture. It allows (1) to integrate spatio-temporal data from several ecological variables and
- 81 species, (2) provide a low rank representation of the ecosystem variability and (3) predict the
- 82 effect of climate change on the ecosystems (Thorson, Ciannelli, and Litzow, 2020; Thorson,
- 83 Cheng, et al., 2020; Thorson, Arimitsu, et al., 2021).
- 84 At this stage, despite their huge potential these methods remain underused in ecology and
- 85 mostly unknown in terrestrial ecology. This may be due to their perceived complexity and
- 86 the lack of clear examples showing how they can be applied to address ecological questions.
- 87 In this paper, we provide a comprehensive introduction to the basics of EOFs and how to
- 88 fairly interpret them. Additionally, to further demonstrate the potential of EOFs for ecology,
- 89 we introduce two related methods that extend EOFs: (1) a method that informs EOFs with
- 90 an ancillary ecological variable, and (2) a method that generalizes EOFs to the multivariate
- 91 case, enabling EOFs analyses on spcies communities or entire ecosystems.
- 92 EOFs do not incorporate any ecological constraints, and their results may not always have a
- 93 direct ecological interpretation due to standard PCA constraints (i.e. orthogonality). Using
- 94 canonical correlation analysis (CCA), we impose an ecological constraint on EOFs to
- 95 improve their ecological interpretability. Additionally, EOFs have proven to be valuable
- 96 tools for community modeling and for ecosystem dynamics analysis (Petitgas, Huret, et al.,
- 97 2018; Thorson, Arimitsu, et al., 2021). Here, we introduce two approaches to perform

multivariate EOFs, corresponding to two types of data representation: a temporally synthetic 99 representation and a spatially synthetic representation. These approaches illustrate the 100 flexibility of the EOFs method for multivariate modeling. While providing different insights 101 into community dynamics, they allow to identify the shared spatial and temporal patterns as 102 well as the distinct habitats or seasons among the species (or ecological variables) included 103 in the analysis. 104 To illustrate these methods, we apply them to two real ecological case studies. First, we use 105 a terrestrial ecology example based on monthly Normalized Difference Vegetation Index (NDVI) satellite data (MODIS) from 2000 to 2023 (MODIS, 2021). This case study aims at 106 demonstrating the potential of EOFs for terrestrial systems. Second, we use spatio-temporal 107 predictions from an Integrated Spatio-Temporal Species Distribution Model (IST-SDM) 108 109 (Alglave, Vermard, et al., 2023). EOFs can be a valuable tool to analyse results of an 110 integrated model, providing a synthetic representation of the information gathered from 111 all the datasets. We analyze several demersal species in the Bay of Biscay between 2008 112 and 2018 at a monthly time step, inferred jointly from scientific survey data and catch declaration data here common sole (Solea solea, Linnaeus, 1758), squid (Loligo vulgaris, 113 Lamarck, 1798), and whiting (Merlangius merlangus, Linnaeus, 1758). 114 115 In the following sections, we first summarize the basics of EOFs, introducing (1) the main mathematical concepts underlying EOFs and (2) how results should be interpreted (Section 116 2). We then present the dataset used to illustrate these methods (Section 3) and apply 117 118 EOFs methodology on both case studies (Section 4). Next, we introduce a method derived from CCA to inform EOFs with ancillary ecological temporal variables (Section 5), and 119 finally, we demonstrate the flexibility of EOFs for modeling multiple species and performing 120 121 community analysis (Section 6). Both real case studies are used throughout the manuscript

- 122 to illustrate the methods. Additionally, code sets are provided to guide practitioners in
- performing the analysis in the simplest way possible.

#### 124 2 Basics of EOFs

- 125 EOFs were initially introduced by Fukuoka (1951), Obukhov (1947), and Lorenz (1956) for
- 126 the analysis and prediction of weather. The method involves extracting the main spatial and
- 127 temporal patterns that (1) capture the most variance and (2) are orthogonal to each other. In
- 128 the upcoming subsections, we introduce the notations and outline the principal properties
- of EOFs through both theoretical explanations and practical applications.

#### 130 2.1 The raw spatio-temporal field

- 131 We denote a space-time process S such that S(x, t) represents the value of the process S at
- spatial location x and time t. The data under consideration will be a discretized version of
- this underlying process defined on a regular grid, namely a matrix **S** of size  $n \times p$ , where n
- denotes the number of discrete spatial positions, and p denotes the number of time steps,
- with the time stepping denoted by  $(t_1, ..., t_p)$ .

From these data, for a given spatial location x, the temporal average can be calculated as:

$$\bar{\mathbf{s}}^{t}(x) = \frac{1}{p} \sum_{k=1}^{p} S(x, t_k). \tag{1}$$

The time-centered space-time field, also referred to as the anomaly matrix, is then represented by:

$$\mathbf{S}' = \begin{pmatrix} S'(x_1, t_1) & S'(x_1, t_2) & \cdots & S'(x_1, t_p) \\ S'(x_2, t_1) & S'(x_2, t_2) & \cdots & S'(x_2, t_p) \\ \vdots & \vdots & \ddots & \vdots \\ S'(x_n, t_1) & S'(x_n, t_2) & \cdots & S'(x_n, t_p) \end{pmatrix}$$

where

$$S'(x_l, t_k) = S(x_l, t_k) - \bar{\mathbf{s}}^t(x)$$
 for  $l = 1, ..., n, k = 1, ..., p.$  (2)

- 136 Examples of both the raw spatio-temporal data and anomalies are available for satellite
- 137 NDVI data and IST-SDM predictions in Figure 1 and S1. Codes below are provided to
- compute the anomaly matrix (S') from spatio-temporal data contained in a matrix S.

```
# S is the spatio-temporal matrix (n . p)
# 1/ Compute the temporal average map.

Smean <- sweep( S, MARGIN=2, STATS=colMeans(S), FUN="-" )
# 2/ Center the spatio-temporal dataset and
# obtain the anomaly matrix Sprim

Sprim <- S - outer(rep(1, ncol(S), Smean)</pre>
```

#### 40 2.2 EOFs formalism: decomposing the spatio-temporal field

# 141 **2.2.1 The model underlying EOFs**

When dealing with EOFs, we assume that the spatio-temporal field can be decomposed into a (purely) spatial term and a (purely) temporal term. This decomposition can be expressed as:

$$S'(x,t) = \sum_{m=1}^{r} u_m(x) \cdot v_m(t) + \epsilon_m(x,t).$$
 (3)

- 142 Here, r represents the number of dimensions of the EOFs with  $r \leq \min(n, p)$  being the
- 143 rank of the matrix S',  $u_m(x)$  denotes the spatial term of the EOFs for dimension m,  $v_m(t)$
- represents the temporal term of the EOFs for dimension m, and  $\epsilon_m(x,t)$  is an error term. In
- some cases,  $\epsilon_m(x, t)$  may not be explicitly defined in the equation (3), and the r dimensions
- 146 capture all the variability in S'.
- 147 The key aspect of EOFs analysis lies in the constraints imposed on the spatial terms  $u_m(x)$
- or the temporal terms  $v_m(t)$  because they are crucial for the inference and interpretation
- 149 of these indices. The most straightforward and natural constraints involve (1) maximising
- 150 the variance explained by each spatial pattern  $p_m(x)$  which is equivalent to minimizing the
- 151 global error, defined as  $E = \sum_{m} \sum_{x} \sum_{y} \epsilon_{m}(x, t)$ ; (2) setting orthogonal constraints for both
- the spatial and temporal terms.

#### 53 2.2.2 Writing EOFs in matrix form

To obtain the terms  $u_m(x)$  and  $v_m(t)$  of equation (3), it is possible to decompose **S'** through Singular Value Decomposition (SVD), namely:

$$\mathbf{S}' = \mathbf{U}\Lambda\mathbf{V}^T \tag{4}$$

- 154 with **U** a  $n \times r$  matrix and  $\mathbf{V}^T$  a  $r \times p$  matrix,  $r \leq \min(n, p)$  being the rank of the matrix
- 155 S'.  $\Lambda$  is a  $r \times r$  diagonal matrix with non-increasing positive coefficients on the diagonal,
- denoted as  $\Lambda = \text{Diag}(\lambda_1, ..., \lambda_r)$  with  $\lambda_1 \ge \lambda_2 \ge ... \ge \lambda_r > 0$ . This is essentially the same
- 157 computation that is performed when conducting PCA on any type of multivariate data.
- Here, the columns of  $\mathbf{U} = (\mathbf{u}_1, ..., \mathbf{u}_r)$  are referred to as the Empirical Orthogonal Function
- 159 (EOF) maps of the anomaly matrix S'. In PCA terms, they are often called factors; in the
- 160 following, they will be referred to as spatial factors.
- 161 The columns of  $V = (v_1, \dots, v_r)$  are often referred to as loading factors in PCA terms.
- Here, they will be called either loadings or temporal loadings of the anomaly matrix S'.
- 163 These columns contain the terms  $v_m(t)$  from Equation (3).

As stated previously, the spatial factors are constructed to be spatially orthogonal, and the loading factors are also temporally orthogonal, meaning that:

$$\langle \mathbf{u}_i; \mathbf{u}_j \rangle_{\mathbb{R}^n} = 0 \quad i \neq j$$

$$\langle \mathbf{v}_i; \mathbf{v}_j \rangle_{\mathbb{R}^p} = 0 \quad i \neq j$$
(5)

where  $\langle \cdot, \cdot \rangle$  denotes the euclidean scalar product.

Finally,  $\Lambda$  contains the singular values of S' along the diagonal. It represents the amount of

variance captured by each dimension of the EOFs also called the inertia in standard PCA. If we note  $I_m$  the variance (or inertia) related to dimension m, we obtain:

$$I_m = \lambda_m^2$$

- 165 The matrix decomposition of equation (4) coincides with equation (3) provided the spatial
- 166 factors  $\mathbf{u}_m$  are normalized by the singular values. Below are the codes to perform SVD in R
- and the corresponding R objects related to the EOFs equations.

```
Perform SVD on the anomaly matrix

E <- svd(Sprim)

SpFactors <- E$u # spatial factors, dimension (n . p)

TempLoadings <- E$v # temporal loadings, dimension (p . p)

SgValues <- E$d # singular values, vector of dimension (p)
```

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169

analysis (*e.g.*, k-means, Hierarchical Clustering on Principal Components - HCPC) to group individuals into homogeneous clusters. A similar approach can be applied to EOFs to either group locations with similar temporal trends or time steps with similar spatial patterns

Finally, note that in standard multivariate statistics, PCA is often combined with clustering

173 (Lindegren et al., 2022; Alglave, Olmos, et al., 2024). This will be discussed later, as it

174 can be particularly useful for identifying functional habitats from species spatio-temporal

175 distributions (Alglave, Olmos, et al., 2024).

#### 6 2.2.3 Interpretation of EOFs

177 The construction of EOFs discussed in the previous subsection implies that the first EOFs 178 map is the spatial pattern  $\mathbf{u}_1$  that captures the most variance in S'. The second EOFs,  $\mathbf{u}_2$ , 179 captures the next most variance while being orthogonal to  $\mathbf{u}_1$ . 180 The loading factors contained in  $\mathbf{v}_j$ , where  $j \in 1, \dots, r$ , are temporal indices. Each is associated with a corresponding spatial factor  $\mathbf{u}_i$ . When the loading  $v_i(t)$  is positive,  $\mathbf{S}'$  is 181 distributed according to the spatial factor  $\mathbf{u}_i$ . Conversely, if  $v_i(t)$  is negative,  $\mathbf{S}'$  is distributed 182 according to  $-\mathbf{u}_i$ . It is important to note that the signs of the loading factors and spatial 183 184 factors are arbitrary, meaning that switching the sign of both  $\mathbf{v}_i$  and  $\mathbf{u}_i$  does not change 185 the overall model. This label/sign indeterminacy is common in factor models and should be kept in mind when interpreting the results, as the sign of the factors may flip between 186 187 different analyses or software implementations. An important consideration is the number of dimensions retained for interpretation. Several 188 189 rules of thumb can guide this decision. Many are based on the proportion of variance captured by each dimension m of the EOFs denoted  $PV_m = \frac{I_m}{\sum_{k=1}^r I_k}$  and that is often 190 represented through a scree plot. One approach is to keep the dimensions that capture 191 the variance of more than what a single variable would capture if all the variables were 192 193 independent. This means retaining dimensions that capture more than 1 out of the number of variables. Another method involves examining the variance graph and selecting dimensions 194 195 up to the point where there is a noticeable drop in variance explained, indicating a significant 196 change in the slope of the scree plot. Finally, one may choose to retain only the dimensions 197 that are interpretable from an ecological point of view. These criteria are not mutually exclusive. For simplicity, in the following text, we represent only the first two dimensions, 198 with additional dimensions being provided in the Supplementary Material. 199

EOFs should be interpreted as statistically significant spatial patterns. However, each 200 201 individual EOFs may not necessarily represent a physically or dynamically relevant spatial 202 pattern (Monahan et al., 2009; Roundy, 2015). For example, a single EOFs dimension may 203 not correspond directly to a specific physical phenomenon; instead, such process might 204 be captured by a linear combination of multiple EOFs. Additionally, there is no constraint 205 separating long-term and short-term signals, so both could be combined within a single dimension. Identifying individual EOFs with underlying processes should be done with 206 great care, always keeping in mind that EOFs capture variance rather than represent an 207 208 ecological process per se. An example of EOFs interpretation in climate science is the North Atlantic Oscillation 209 (NAO) index (Hurrell and Deser, 2010), which is often analyzed through EOFs. The NAO 210 211 is a weather phenomenon in the North Atlantic Ocean characterized by fluctuations in the atmospheric pressure difference at sea level between the Icelandic Low and the Azores High. 212 213 The NAO has been shown to influence ecological dynamics in both marine and terrestrial 214 systems (Ottersen et al., 2001). The first EOFs dimension of the sea-level pressure field over the North Atlantic typically represents the NAO pattern (Figure 8 in Saeed, Kucharski, and 215 Almazroui, 2023). When the loading factor associated with this dimension is positive, it 216 indicates a strong Azores high and a deep Icelandic low, corresponding to the positive phase 217 of the NAO. Conversely, a negative loading factor indicates the negative phase of the NAO, 218 characterized by a deep Azores low and a strong Icelandic high. This EOFs dimension 219 220 captures the primary mode of variability in the North Atlantic sea-level pressure field and is crucial for understanding and predicting regional climate variations. 221

# 222 3 Data and case study for illustration

- 223 In order to illustrate the various methods, we introduce two spatio-temporal datasets to
- 224 serve as a case study: (1) NDVI data from MODIS Vegetation Index Products (satellite data
- 225 on terrestrial ecosystems) and (2) spatio-temporal predictions from a IST-SDM for fishes in
- 226 the Bay of Biscay (IST-SDM on a marine case study).

#### 227 3.1 Satellite NDVI data

- 228 For NDVI data, we use the one kilometer monthly product available through MODIS
- 229 (Busetto and Ranghetti, 2016). These are satellite observations data, which provide high-
- 230 resolution information of the Earth's surface. By capturing reflected light in various spectral
- 231 bands, these data allows to compute Normalized Difference Vegetation Index (NDVI),
- 232 a key indicator of vegetation health and density. NDVI values range from -1 to 1, with
- 233 higher values indicating healthier and denser vegetation. This index is particularly useful for
- 234 monitoring changes in vegetation over time, assessing drought conditions, and understanding
- 235 ecosystem dynamics. We filter the data over France and aggregated the data on a grid cell
- with resolution of 10 km (Figure 1). These data range from 2000 to 2023 with a monthly
- 237 time step and consist of 288 maps.
- 238 NDVI spatio-temporal variability is strongly related to temperature and precipitation,
- 239 with significant heterogeneity in these relationships across regions (Piao et al., 2003;
- 240 Vicente-Serrano et al., 2013). Consequently, the seasonal cycle is expected to have a strong
- 241 influence on NDVI through fluctuations in both precipitation and temperature, with possible
- 242 heterogeneity depending on local climatic conditions (Eisfelder et al., 2023). Specifically in
- France, as noted by Eastman et al. (2013), the main pattern should exhibit higher NDVI
- values during spring, summer, and early autumn, corresponding to higher temperatures

- during these periods and increased precipitation in spring and early autumn. In contrast,
- NDVI is expected to be lower in late autumn and winter due to lower temperatures and
- 247 vegetation senescence.

#### 248 3.2 Species distribution model predictions

- 249 For the IST-SDM, we use monthly spatio-temporal predictions for three key species in the
- 250 Bay of Biscay (common sole, Solea solea squids, Loligo vulgaris whiting, Merlangius
- 251 merlangus) spanning a decade from 2008 to 2018 (Figure S1). These predictions were
- 252 derived from a hierarchical model that integrates data from fishers' declarations and scientific
- 253 surveys (Alglave, Rivot, et al., 2022; Alglave, Vermard, et al., 2023). These spatio-temporal
- 254 predictions consist of 132 spatial fields over time.
- 255 When the method is univariate (single species) we only retain sole for the analysis. Sole
- 256 spatio-temporal distribution is strongly structured by reproduction phenology (Arbault,
- 257 Camus, and Bec, 1986; Alglave, Olmos, et al., 2024). Sole migrates offshore during
- 258 reproduction from January to March and then returns to nearshore areas for feeding. It is
- 259 expected that reproduction will be reflected through EOFs. Also, one could constrain EOFs
- 260 with steady seasonality to better emphasize such process.
- 261 In some scenarios, multiple ecological variables must be analyzed together to identify
- 262 shared dynamics. In such cases, EOFs must be tailored to multivariate data to infer the
- 263 common patterns shaping these species (Thorson, Scheuerell, et al., 2015). To illustrate this,
- 264 we consider several species in the Bay of Biscay, including sole, whiting, and squids. These
- 265 species live in relatively coastal areas and share similar ecological niches (Alglave, Vermard,
- et al., 2023). Consequently, they are expected to exhibit shared spatio-temporal patterns,
- 267 such as synchronous reproductive periods from January to March (Moreno et al., 2002;

- 268 Arbault, Camus, and Bec, 1986; Houise, 1993). Our objective is to identify and quantify
- 269 these patterns using multivariate EOFs.
- 270 In the following sections, we illustrate various EOFs and EOF-related methods using these
- 271 case studies.

# 272 4 Applying EOFs to the case studies

- 273 The EOFs method is applied to satellite NDVI data and the IST-SDM dataset (Figure 1, S1).
- 274 Respectively, we see an angle in the graph of variance after the second dimension (NDVI)
- and the fourth dimension (IST-SDM left, Figure 2). Figure 3 illustrates both the spatial
- 276 factors (top) and the temporal loadings (bottom) of the first two dimensions for both case
- 277 studies. The third and fourth dimensions of the IST-SDM case study are presented in Figure
- 278 S2.
- 279 For satellite NDVI data, both the first and second dimensions emphasize seasonality on
- 280 two different phases. The first dimension is related to the winter/summer seasonality with
- 281 a positive peak in June and a progressive decrease until February/March. This signal is
- 282 mainly related to the mountainous and eastern part of France. It is basically the signal that
- 283 represents (1) the decrease of vegetation in winter (especially in mountainous areas) due
- 284 to smaller primary production and snow falls and (2) an increase starting in March when
- 285 temperatures are higher and conditions are favorable for the growth of vegetation.
- 286 By contrast, the second dimension emphasizes another phase in seasonality. Temporal
- 287 loadings are negative from March to June (spring and early summer), which corresponds
- 288 to high NDVI in the western and northern part of France. This can be related to both rain
- and higher temperature conducting to high primary production in this area. From July to

- 290 November, temporal loadings are positive. NDVI is high in mountains (similar to the first
- 291 dimension) and low in the western and northern part of France.
- 292 For the IST-SDM case study, the first dimension highlights strong seasonality. The loadings
- 293 exhibit highly positive values in winter (January to February) and strongly negative values
- 294 during summer (April to August), indicating that soles are concentrated in red/orange areas
- 295 during winter and in blue areas during summer. The second dimension also emphasizes
- 296 some seasonality but primarily depicts a long-term decreasing trend. It suggests that fish
- 297 progressively migrate northward over the period and become more concentrated in Northern
- 298 red areas. Note that dimension 3 also emphasizes seasonal patterns (Figure S2) related to
- 299 reproduction and dimension 4 highlights an important hotspot of sole distribution in the
- 300 south of the Bay of Biscay ( $2^{\circ}W 45.5^{\circ}N$ ).
- 301 EOFs do not disentangle the information between the different dimensions and relevant
- 302 ecological signals are mixed between the several dimensions of the EOFs. For instance, both
- 303 the first and second dimensions for the two case studies capture a similar though different
- 304 seasonal signal (Figure 3). Also, some loadings seem to mix both long term trends and
- 305 seasonnal trends (see the second EOFs dimension of the IST-SDM case study). Finally,
- 306 some spatial areas appear to be shared between both spatial factors (mountain areas in the
- 307 satellite NDVI case study and reproduction areas in the IST-SDM case study).

# 308 5 Informing EOFs with an ancillary temporal variable

- 309 As mentioned in previous sections, EOFs may not effectively disentangle a single process
- 310 in each dimension. There are no constraints on the ecological relevance of the spatial
- 311 factors or temporal loadings, and a single process might be represented across several EOFs
- 312 dimensions. To address this limitation, it is useful to inform the spatio-temporal dimension

- 313 reduction of EOFs with temporal variables that are ecologically meaningfully (also referred
- 314 to as ancillary variables in the following) to inform the spatio-temporal dimension reduction
- 315 of EOFs.
- 316 This section describes the methodology for extracting EOFs patterns that exhibit the
- 317 highest correlation with an ancillary temporal variable. This process involves projecting the
- 318 spatio-temporal data onto the EOFs basis and then performing a CCA between a selected
- 319 set of EOFs loading factors and the ancillary variable. We first review the CCA method,
- 320 demonstrate how to adapt it to our specific context, and finally present an application of this
- 321 technique.

#### 322 5.1 Basics of Canonical correlation analysis

- 323 CCA was first proposed by Hotelling (1992). It is a method used to identify and measure the
- 324 associations among two sets of variables. Consider two space-time processes  $S^{(1)}(x,t)$  and
- 325  $S^{(2)}(x,t)$  at location x and time t. CCA aims at identifying pairs of spatial basis vectors,  $\mathbf{w}_1$
- and  $\mathbf{w}_2$ , for the two processes,  $S^{(1)}$  and  $S^{(2)}$ , that maximize the correlation between their
- 327 projections onto these vectors. Consider the corresponding observed space-time matrices
- 328 denoted  $S^{(1)}$  and  $S^{(2)}$  of size  $n_1 \times p$  and  $n_2 \times p$ , respectively.

The CCA maximizes the following correlation function  $\rho$  between  $\mathbf{y}_1 = \mathbf{S}^{(1)}\mathbf{w}_1$  and  $\mathbf{y}_2 = \mathbf{S}^{(2)}\mathbf{w}_2$ :

$$\rho = \frac{\mathbb{E}(\mathbf{y}_{1}\mathbf{y}_{2})}{\sqrt{\mathbb{E}(\mathbf{y}_{1})\mathbb{E}(\mathbf{y}_{2})}}$$

$$= \frac{\mathbb{E}(\mathbf{w}_{1}^{T}\mathbf{S}^{(2)T}\mathbf{S}^{(2)}\mathbf{w}_{2})}{\sqrt{\mathbb{E}(\mathbf{w}_{1}^{T}\mathbf{S}^{(2)T}\mathbf{S}^{(1)}\mathbf{w}_{1})\mathbb{E}(\mathbf{w}_{2}^{T}\mathbf{S}^{(1)T}\mathbf{S}^{(2)}\mathbf{w}_{2})}}$$

$$= \frac{\mathbf{w}_{1}^{T}\mathbf{C}_{12}\mathbf{w}_{2}}{\sqrt{\mathbf{w}_{1}^{T}\mathbf{C}_{11}\mathbf{w}_{1}\mathbf{w}_{2}^{T}\mathbf{C}_{22}\mathbf{w}_{2}}}$$
(6)

- Here  $\mathbf{y}_1$  and  $\mathbf{y}_2$  are the temporal variables that arise from the linear combination of  $\mathbf{S}^{(1)}\mathbf{w}_1$
- and  $S^{(2)}$  w<sub>2</sub> and which correlation coefficient is to be maximised. Then, the spatial basis
- vectors  $\mathbf{w}_1$  and  $\mathbf{w}_2$  describe which areas contribute to this correlation in the dataset  $\mathbf{S}^{(1)}$  and
- 332  $S^{(2)}$  respectively.

In order to find the vectors  $\mathbf{w}_1$  and  $\mathbf{w}_2$  that maximize  $\rho$ , we resort to the method of Lagrange multipliers, leading to a generalized eigenvalue problem (Weenink, 2003).

$$\begin{cases} (\mathbf{C}_{11}^{-1}\mathbf{C}_{12}\mathbf{C}_{22}^{-1}\mathbf{C}_{21} - \rho^2)\mathbf{w}_1 = 0\\ (\mathbf{C}_{22}^{-1}\mathbf{C}_{21}\mathbf{C}_{11}^{-1}\mathbf{C}_{12} - \rho^2)\mathbf{w}_2 = 0 \end{cases}$$
(7)

- Here, the eigenvalues  $\rho^2$  represent the squared canonical correlations, and the eigenvectors
- 334  $\mathbf{w}_1$  and  $\mathbf{w}_2$  are the canonical correlation basis vectors.

#### 335 5.2 Coupling CCA with EOFs

- Note that the two datasets  $S^{(1)}$  and  $S^{(2)}$  do not necessarily have the same spatial extent, but
- 337 they must have the same time stepping. Then, to constrain the EOFs with a single ancillary

- 338 variable, it is possible to perform a CCA on the matrix V (Equation 4) composed of the
- temporal loading factors and an ancillary variable that we denote  $An(t), t \in \{1, \dots, p\}$ .
- 340 Usually, we only retain the dimensions of the EOFs that capture the process and leave apart
- the dimension that capture noise (see the rule of thumb in section 2.2.3). In this case,  $\mathbf{w}_1$  are
- 342 coefficients that allow to rotate the temporal loadings as well as the related spatial factors to
- 343 obtain:
- one variable that closely fit the ancillary variable. This is the combination of loadings
- that maximise the correlation with the ancillary variable.
- the related spatial factor (or spatial basis vector) that is a combination of the first
- spatial factors. It will capture as much variance as the first pattern of the EOFs but
- will not be orthogonal to the following EOFs.

#### 349 5.3 Illustration

In this section, we inform EOFs of the NDVI satellite data with an ancillary variable representing seasonality. The ancillary variable chosen here is a steady seasonal signal evidencing seasonality with positive peaks in summer (July) and negative peaks in winter (January - red variable in Figure 4). This variable aims at extracting part of the common seasonal signal shared by the two first dimensions of the EOFs (Figure 3). The seasonal signal is parameterized as:

$$An(t) = A \cdot sin(f \cdot t + D) \tag{8}$$

- 350 To have a ancillary variable that match seasonal cycles (opposite peaks in January and
- July) we set A = 1 (the amplitude of the signal),  $f = 1/12 \times 2\pi$  the frequency of the signal

- 352 components and the delay component D = 1. Note that this procedure is not invariant to a
- change in the phase of the seasonal signal and should be fixed with care.
- 354 We then perform a CCA between the first two loading factors of the EOFs (components of
- 355 the matrix V in Section 2.2) and the seasonal signal. The aim is to identify spatial pattern of
- 356 NDVI related to the cycle of seasons (driven by precipitation and temperature in France).
- 357 The outcomes of this method are presented in Figure 4.

# Perform CCA between EOFs results and a seasonnal time series

```
## Construct the seasonnal variable
p <- ncol(S) # number of time steps</pre>
ts <- seq(1,p,1) # sequence of time steps</pre>
component.strength = 1 # amplitude of the signal
component.freqs = 1/12 # frequency of signal (month^-1)
f.0 = 2 * pi # fundamental frequency (month^-1)
component.delay = 1 # delay of signal components (radians)
# Create the seasonal signal
signal_vec = - component.strength *
    sin(component.freqs * f.0 * ts + component.delay)
## Filter EOFs dimensions and apply CCA
ndim <- 2 # number of dimension to filter in the EOFs
EOFset1 <- E$v[,1:ndim] # filter the loadings</pre>
cca_res = stats::cancor(EOFset1, signal_vec) # perform CCA
## Rotate the temporal loadings and spatial factors
## with CCA results
# Rotate the temporal loadings of the EOFs
ccavar1_t <- (as.matrix(E0Fset1) %*% cca_res$xcoef)[,1]</pre>
# Rotate the spatial factor of the EOFs
ccavar1_x <- as.matrix(E$u[,1:ndim) %*% cca_res$xcoef[,1]</pre>
```

358

359 The loadings obtained from the CCA emphasize a very good fit to the ancillary variable (R2

- = 0.98, Figure 4, top right). By comparison, the first two EOFs loadings have positive, but 360 lower correlation coefficient (R2 = 0.82 and R2 = 0.57). The spatial basis obtained through 361 362 CCA displays a stronger North/South gradient of NDVI compared with the two first EOFs 363 (Figure 3). NDVI are high in orange/red areas during summer (i.e. the center and mountain part of France) which corresponds to high NDVI in mountains and all the southern part and 364 365 eastern part of France. In these areas, either ice melt and temperatures become favorable for vegetation growth (mountains), either temperature are high and rains remain frequent which 366 increases vegetation coverage (eastern and south western part of France). In winter, these 367 368 areas are colder and they can be covered by snow which do not favor vegetation growth.
- 369 In blue areas, NDVI is relatively higher during winter. These areas have a cooler climate
- 370 during winter and strong precipitation which favors vegetation growth.
- 371 A similar analysis is performed on the IST-SDM outputs. It allows to better evidence the
- 372 seasonal cycle of sole reproduction and the offshore-onshore gradients that shapes sole
- 373 migration (Figure S3)

# 374 **6 EOFs for multivariate analysis**

- 375 When studying entire ecosystems or community dynamics, multiple variables need to be
- analyzed jointly using multivariate modeling approaches (Ovaskainen and Abrego, 2020;
- 377 Thorson, Ciannelli, and Litzow, 2020). The EOFs framework is flexible and adapts to the
- 378 multivariate case. It allows to identify the main modes of variability across several variables
- 379 (or ecosystem compartments) and to detect shared temporal trends and related habitats. In
- 380 such cases, the underlying EOFs theory remains unchanged (Section 2); only the matrix to
- 381 be diagonalized S' is modified.

#### 382 6.1 The two approaches for conducting multivariate EOFs

- Let  $v \in \{1, \dots, s\}$  denotes the index representing the number of variables in the analysis,
- and let  $S^{(v)}(x,t)$  denotes the value of the space-time process for location x, time t, and
- variable v. We denote by  $\mathbf{S}'^{(v)}$  the  $n \times p$  matrix of the spatio-temporal variable v.
- 386 Two options are available when conducting multivariate EOFs:
- Construct the matrix by stacking the matrices row-wise. In this case, the matrix is denoted as  $\mathbf{S}'^{(row)}_{multi}$  with dimensions  $(n \cdot s) \times p$ , and it has the following structure:

$$\mathbf{S}_{multi}^{\prime(row)} = \begin{pmatrix} \mathbf{S}^{\prime(1)} \\ \mathbf{S}^{\prime(2)} \\ \vdots \\ \mathbf{S}^{\prime(s)} \end{pmatrix}$$

Alternatively, one can construct the matrix by stacking the matrices column-wise. In this case, the matrix is denoted as  $\mathbf{S}'^{(col)}_{multi}$  with dimensions  $n \times (p \cdot s)$  and is structured as follows:

$$\mathbf{S}_{multi}^{\prime(col)} = \begin{pmatrix} \mathbf{S}^{\prime(1)} & ; & \mathbf{S}^{\prime(2)} & ; & \cdots & ; & \mathbf{S}^{\prime(s)} \end{pmatrix}$$

- 392 Similar to standard EOFs, SVD enables to infer the spatial factors  $\mathbf{u}_i$  and the temporal
- loadings  $\mathbf{v}_i$  (Section 2). However, depending on the data stacking before EOFs, they do not
- 394 have the same dimensions and do not lead to the same interpretation.
- 395 The first case is a temporally synthetic representation of the variability in the multivariate
- 396 data. For each dimension, there is only one single time series of temporal loading and there
- 397 are as many spatial factors as there are variables. The temporal loadings describe how the
- 398 different spatial factors evolve over time. This allows to summarize the temporal variation

- 399 of all the variables in one single temporal variable. A similar approach is adopted in the
- 400 VAST package (Thorson, 2019).
- 401 The second case, is a **spatially synthetic representation** of the variability in the data. For
- 402 each dimension, there is only one spatial factor that summarizes the variability of all the
- 403 variables and as many time series of temporal loadings as there are variables. The loadings
- 404 of the different variables describe how these variables are related to the spatial factor at a
- 405 specific time step.
- 406 Note finally that in some cases, multivariate EOFs can be applied on a single variable with
- 407 some time-lag (Wikle, Zammit-Mangion, and Cressie, 2019). In this case the different
- 408 variables are the lagged version of the spatio-temporal data. This typically allows for a better
- 409 identification of temporal patterns such as periodicity or long-term trends and is referred to
- 410 as lag EOFs in this paper. This approach is often referred to as extended EOFs (Weare and
- 411 Nasstrom, 1982; Wikle, 2002; Dey et al., 2019).

#### 412 **6.2 Illustration**

- 413 To illustrate multivariate EOFs analysis, we apply the two alternative approaches to the
- 414 three species in the Bay of Biscay: sole, whiting, and squids. These are coastal species
- 415 (Alglave, Vermard, et al., 2023) with potentially shared spatio-temporal dynamics e.g.
- 416 same reproduction period (Arbault, Camus, and Bec, 1986; Houise, 1993; Moreno et al.,
- 417 2002). From an ecological perspective, a critical issue involves identifying shared spatial or
- temporal dynamics among different species (Thorson, Scheuerell, et al., 2015; Ovaskainen
- and Abrego, 2020; Thorson, Arimitsu, et al., 2021). Additionally, one can seek to identify
- 420 combinations of 'areas x seasons' that can be interpreted as multispecies functional habitats
- 421 (Delage and Le Pape, 2016). To do this, we combine the EOFs (both representations)

- 422 with a clustering analysis (HCPC) to identify clusters of locations and time steps that
- 423 can be interpreted as habitats and seasons from a multispecies perspective. For a detailed
- 424 description of the clustering analysis performed on the EOFs results, see S.1.6 and Alglave,
- 425 Olmos, et al. (2024).
- 426 The temporally synthetic multivariate EOFs (EOFs on  $\mathbf{S}_{multi}^{\prime(row)}$ ) provides seasonal temporal
- 427 loadings that represent the reproduction phenology for all the species (as mentioned in
- 428 Section 3). We select the first two dimensions (Figure 2). For sole, the reproduction areas
- 429 are generally consistent with those identified when conducting univariate EOFs (Figure 5).
- 430 For squids and whitings, reproduction areas are observed along the Landes coast (45°N -
- 431 1.5°W), on the Vendée coast (46.5°N 2°W), and in the north of the Bay of Biscay (47.5°N
- 432 3°W). The clustering confirms these results (Figure S10) with an additional potential
- reproduction area off the continental shelf on the slope (3°W 45°N).
- On the other hand, the spatially synthetic multivariate EOFs (EOFs on  $\mathbf{S}_{multi}^{\prime(col)}$ ) provides one
- 435 single spatial pattern per dimension and as many temporal loadings as variables. An angle
- 436 appears after the fourth dimension (Figure 2). Interestingly, the first spatial factor gathers
- 437 the main reproduction areas for sole and squids that were previously identified (Figure 6
- 438 and S7). Also for all three species a summer area appears on the coast consistently with the
- 439 clustering analysis (Figure S13). The second dimension emphasizes an overall increase in
- 440 the loadings, illustrating a general drift towards the North of the Bay of Biscay and in the
- 441 offshore areas (Figure S8). The loadings are correlated among species, highlighting that
- 442 they share common temporal dynamics relatively to the spatial factors of these dimensions
- 443 (Figure 6). The third dimension is mainly characterized by whiting reproduction areas and
- 444 the fourth dimension by sole reproduction areas (Figure S9).
- 445 Illustration of the lag EOFs is realised on the satellite NDVI data and is presented in S.1.4
- 446 as a complement of the multispecies analysis. Compared with standard EOFs, they allow to

- 447 identify an additional periodic signal with a 6-months phase related to an alternance of high
- 448 growth of vegetation in spring and autumn and lower growth in summer and winter.

#### 449 **7 Discussion**

# 450 Towards a wider use of EOFs in ecology

- 451 EOFs have tremendous potential for ecology. As massive and diverse datasets become
- 452 available through various data sources (such as satellite data, IST-SDM, and biogeochemical
- 453 models), these decomposition methods will play a growing role in (1) reducing data
- 454 dimensionality and (2) extracting ecologically relevant and interpretable information.
- 455 While these methods have been frequently used in marine ecology (Norton and Mason, 2005;
- 456 Petitgas, Doray, et al., 2014; Thorson, Cheng, et al., 2020), they have remained underutilized
- 457 in terrestrial ecology. In this paper, we demonstrate their potential for both terrestrial and
- 458 marine systems. We argue that these methods should be systematically applied whenever
- 459 the time span of the data necessitates post-processing to summarize the information.

#### 460 Accounting for spatio-temporal correlation in EOFs

- 461 One might argue that EOFs do not explicitly account for spatial or temporal correlations
- 462 and then are not per se a spatio-temporal method. It is true that EOFs is basically a PCA
- 463 representation of spatio-temporal data; the spatio-temporal aspects of the method comes
- 464 from the characteristic of the data rather than from the mathematical formulation of the
- 465 method per se.
- 466 In a spatial context, methods have been developed to better handle spatial correlations
- in data and to propose multiscale decompositions of ecological data (Dray et al., 2012;
- 468 P. Legendre and L. Legendre, 2012b). P. Legendre and L. Legendre (2012a) provides an

overview of 'spatial eigenfunction analysis' (e.g., Moran's eigenvector maps, asymmetric 469 470 eigenvector maps, multiscale ordination), which estimate sets of eigenvectors based on 471 spatial configuration matrices. These eigenvectors can be used as predictors in linear models, 472 canonical analysis, or redundancy analysis. They help identify different spatial scales of 473 variation in ecological data and the related spatial patterns. These methods could potentially 474 be extended to spatio-temporal data to identify distinct spatio-temporal scales that structure the ecological processes. 475 More recently, Petitgas, Renard, et al. (2020) and Bez, Renard, and Ahmed-Babou (2023) 476 have proposed a method (Empirical Orthogonal Maps - EOM) based on EOFs that accounts 477 for spatial correlation by rotating the spatial factors to provide spatially decorrelated patterns. 478 EOM provide maps with stronger orthogonality constraints to better separate the information 479 480 carried by different spatial factors. Alternatively, spatial correlations can be represented 481 as spatial latent variables, and EOFs can be applied to those within a hierarchical model 482 (Thorson, 2019). 483 Although these methods are sensitive to the choice of the distance matrix or the spatial lags used in the analysis, they represent promising avenues for enhancing EOFs to explicitly 484

#### 486 Informing EOFs with ancillary variables for a better ecological interpretation

account for spatial and temporal correlation.

485

A significant drawback of EOFs is their limited interpretability regarding the processes underlying the spatio-temporal field particularly in the dimensions up to the second dimension (Mestas-Nuñez, 2000; Monahan et al., 2009). This issue can be attributed to the orthogonal constraints, which do not have per se an ecological meaning. Under Gaussian assumptions, orthogonal constraints allow for the extraction of independent information across different dimensions and facilitate the separation of information along the axes. However, in ecology,

- 493 (1) processes are frequently non-Gaussian and (2) can be highly correlated, non-linear, and
- 494 non-stationary (Ciannelli, Bartolino, and Chan, 2012). Consequently, standard EOFs may
- 495 not always provide the best ecological representation of the data.
- 496 Here drawing on CCA theory (Hotelling, 1992), we propose an approach that enhances the
- 497 interpretability of the spatial factors by informing the EOFs with an ecological ancillary
- 498 temporal variable. A key consideration is the type of ecological ancillary variable that
- 499 can be used to constrain the EOFs. Ideally, any temporal variable with the same temporal
- 500 extent as the spatio-temporal dataset can be used, provided it has ecological relevance to the
- 501 ecological question under study. For example, many studies have explored the relationship
- 502 between EOFs and oceanographic processes, such as the cold pool extent in the Bering
- 503 Sea (Thorson, Ciannelli, and Litzow, 2020; Thorson, Arimitsu, et al., 2021). Constraining
- 504 the EOFs with the cold pool extent would likely improve the interpretability of the spatial
- 505 patterns. In other contexts, ancillary variables could include other oceanographic processes,
- such as upwelling intensity (Sydeman et al., 2014), or any covariates (or sets of covariates)
- 507 that drive the spatio-temporal variability of populations and ecosystems (Petitgas, Doray,
- 508 et al., 2014).

#### 509 EOFs for community and ecosystem analysis

- 510 The use of EOFs for multivariate data has gained significant importance over the past
- 511 decade. Initially, research focused on synthesizing information from temperature-salinity
- 512 diagrams to reduce the complexity of data representation (Fukumori and Wunsch, 1991;
- 513 Sparnocchia, Pinardi, and Demirov, 2003). More recently, EOFs have been applied to study
- 514 ecosystem structure and community dynamics (Woillez et al., 2010; Petitgas, Huret, et al.,
- 515 2018; Grandremy et al., 2023) and to forecast these communities and ecosystems (Thorson,
- 516 Arimitsu, et al., 2021).

Using three coastal fish species in the Bay of Biscay, we demonstrated the ability of EOFs 517 518 to (1) identify shared spatial and temporal patterns among species, (2) evaluate correlations 519 among species, and (3) identify seasons and functional zones common to these species. Two 520 kind of representation are presented in this paper: a spatially synthetic representation and a 521 temporally synthetic presentation. The latter approach aligns with the VAST framework 522 (Thorson, Ciannelli, and Litzow, 2020; Thorson, 2019), while the former is less commonly 523 seen in the literature but remains valuable for identifying shared spatial patterns across multiple variables or species. 524 Developing multivariate EOFs that are both spatially and temporally synthetic is crucial to 525 enhance the interpretability of results. EOFs can be applied to any set of variables (species 526 or ecological variable), potentially encompassing many more than three, to represent several 52.7 528 communities or entire ecosystems. The methodological steps and interpretations presented 529 here would remain applicable. However, as the number of variables increases, either the 530 number of variables contained in the temporal loadings or in the spatial factors increases, 531 leading to results that are difficult to interpret. For example, recent studies by Thorson, Ciannelli, and Litzow (2020) and Thorson, Arimitsu, et al. (2021) proposed multivariate 532 533 EOFs to investigate ecosystem variability by including respectively seven and eighteen variables. In this case, it results in a set of seven and eighteen maps per EOFs dimension 534 and visual inspection does not allow to have a meaningful and synthetic view of the 535 information. New methods based on multidimensional array SVD could be employed to 536 537 develop multivariate spatio-temporal EOFs with more synthetic representations of the temporal and spatial components (Bi et al., 2021). In particular, future research could 538 539 incorporate multiple loadings, representing separate the expansion across spatial, temporal, 540 and multivariate dimensions.

# Non-stationary, non-linear EOFs for spatio-temporal analysis under climate change

541

Finally, some important hypotheses underlie EOFs that can be an important drawback 542 in a context of climate change, namely stationarity and linearity (Hannachi, Jolliffe, and 543 Stephenson, 2007). Indeed, the spatial patterns identified through EOFs remain unchanged 544 throughout the period. The spatial EOFs factors may decrease or increase in intensity 545 546 through the linear combination with the temporal loadings, but they will remain the same over the period (Alglave, Olmos, et al., 2024). Consequently, EOFs can not be used to 547 describe propagating patterns such as range expansion or contraction as is common in 548 species redistribution (Cheung et al., 2009; Melles et al., 2011; Scheele et al., 2017). Also, 549 550 as in standard PCA, all non-linear processes will not be detected and captured through EOFs while it is largely recognized that ecosystems are strongly structured by non-linear 551 552 relationships and sometimes switching dynamics (Levin, 1998; Scheffer et al., 2001). More 553 generally speaking, handling non-stationarity in a changing environment is a key challenge 554 for statistical ecology (Litzow et al., 2019; Astigarraga et al., 2020; Bueno de Mesquita 555 et al., 2021). Although some techniques, such as Hilbert complex EOFs or non-linear PCA (Bueso, Piles, and Camps-Valls, 2020; Esquivel and Messina, 2008), allow to handle 556 557 non-linear relationship and to evidence propagating patterns, these have been scarcely used in practice to investigate the effect of climate change on ecosystems. Developing and 558 applying approaches that can handle such non-linearities and non-stationarity is critical in 559 analysing the effect of climate change on ecosystems; it constitues an open research avenue 560 561 for future study of threatened ecosystems in a perspective of conservation and adaptation to climate change (Sala et al., 2000; Parmesan, 2006; Grebmeier et al., 2006). 562

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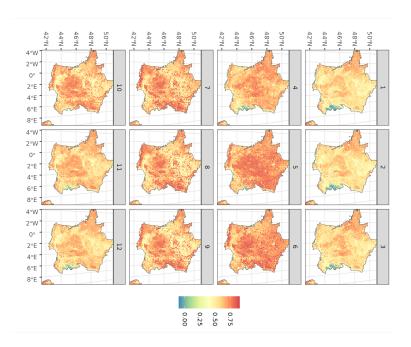
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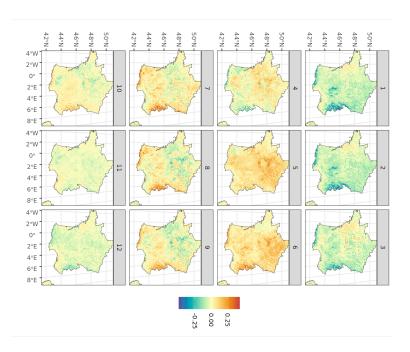


Fig. 1: NDVI data. (left) Monthly spatial data of NDVI S(x,t). (right) Monthly anomalies of the spatial predictions  $S^*(x,t)$ . Each panel corresponds to the average predictions or anomalies for a month over the period 2000 - 2023.

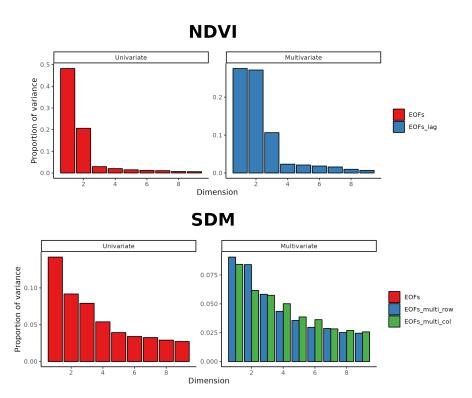


Fig. 2: Proportion of variance explained by each method for each case study. Top: NDVI satellite data, bottom: IST-SDM predictions for sole. (Left) Univariate analysis. (Right) Multivariate analysis. EOFs\_lag is the lagged version of EOFs. EOFs\_multi\_row is the multivariate EOFs conducted on  $\mathbf{S}_{multi}^{(row)}$  (temporally synthetic representation). EOFs\_multi\_col is the multivariate EOFs conducted on  $\mathbf{S}_{multi}^{(col)}$  (spatially synthetic representation).

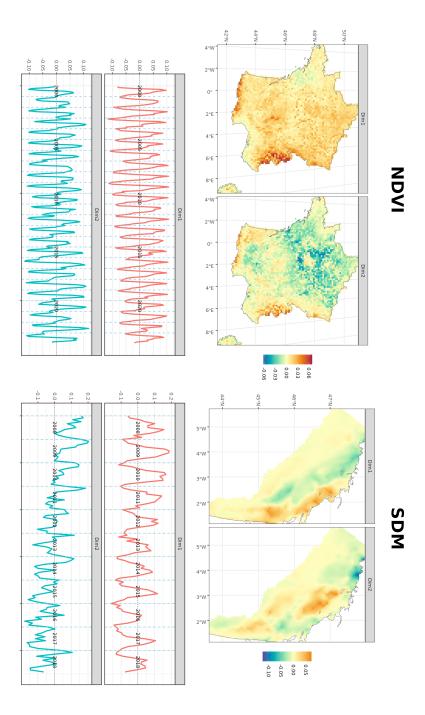


Fig. 3: EOFs results for satellite NDVI data (left) and IST-SDM predictions (right). (Top) Spatial factors for the two first dimensions of the EOFs. (Bottom) Loadings for the two first dimensions of the EOFs. Blue dashed vertical lines correspond to the month of January for each year.

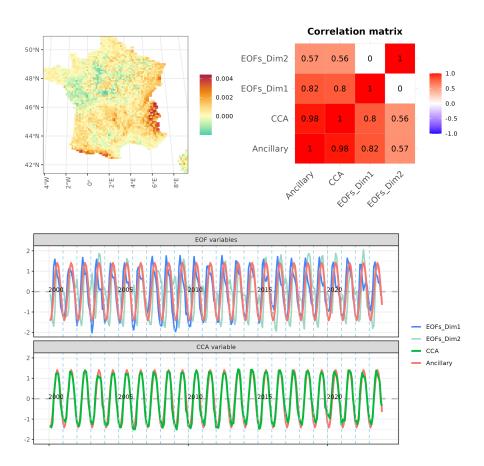


Fig. 4: Satellite NDVI data. Results of the canonical correlation analysis. (Top left) Spatial basis vector that maximize the correlation between the temporal variables  $\mathbf{y}_1$  and  $\mathbf{y}_2$ . (Top right) Correlation matrix between the two first loading factors of the EOFs, the CCA  $\mathbf{y}_1$ , and the ancillary variable. (Bottom) Comparison of the EOFs loadings with the ecological ancillary variable (showing that both variables capture some seasonal pattern), and the CCA variable with the ecological ancillary variable (showing that the CCA now captures seasonality in a single variable). These time series are standardized. Blue dashed vertical lines correspond to the month of January for each year.

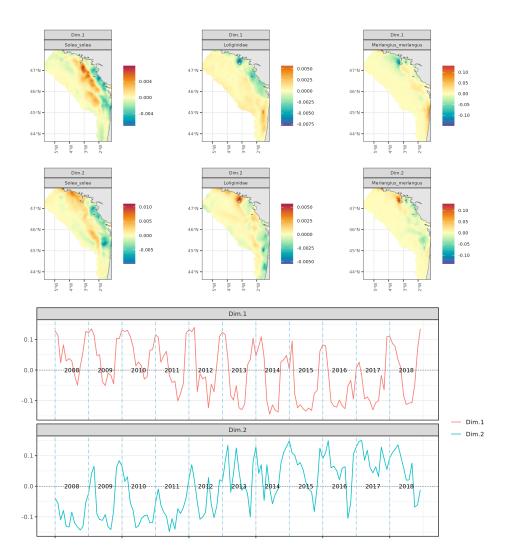


Fig. 5: IST-SDM predictions. Results for the multivariate temporally synthetic EOFs (EOFs on  $\mathbf{S}'^{(row)}_{multi}$ ). (Top) Factor maps for each species and first two dimensions. (Bottom) Loadings for the first two dimensions. For each dimension, loadings represent when the several species of the analysis follow their related spatial distribution. Blue dashed vertical lines correspond to the month of January for each year. The temporal loadings emphasize the seasonality of the reproduction for each three species. Orange areas in both dimensions correspond to the reproduction grounds.

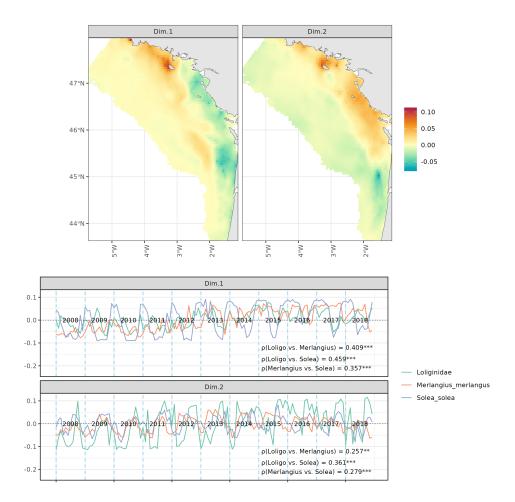


Fig. 6: IST-SDM predictions. Results for multivariate spatially synthetic EOFs (EOFs on  $S_{multi}^{\prime (col)}$ ). (Top) Factor maps for the first two dimensions. (Bottom) Loadings of each species for the first two dimensions. For each dimension, the loadings of the species represent when the several species of the analysis follow the related spatial factor. Blue dashed vertical lines correspond to the month of January for each year. There is a strong offshore-onshore gradient emphasized on both dimensions with coastal areas being summer grounds. All the species emphasize strong correlation relatively to the two first spatial factors.

# 780 S.1 Supplementary material

### 781 S.1.1 IST-SDM spatio-temporal predictions and anomalies

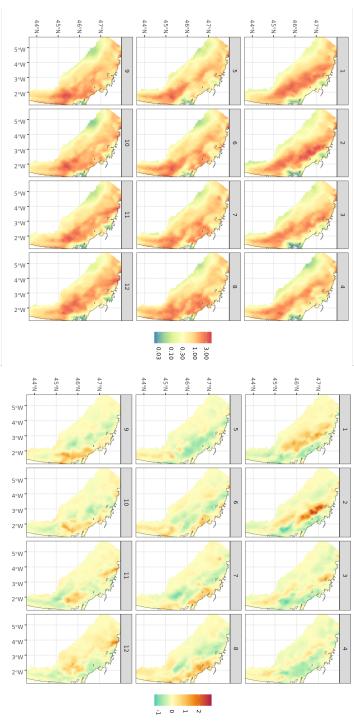


Fig. S1: IST-SDM predictions. (left) Monthly spatial predictions for sole in the log-scale log S(x,t). (right) Monthly anomalies of the spatial predictions  $S^*(x,t)$ . Each panel corresponds to the average anomalies for a month over the period 2008 - 2018.

### 782 S.1.2 Additionnal dimensions for EOFs

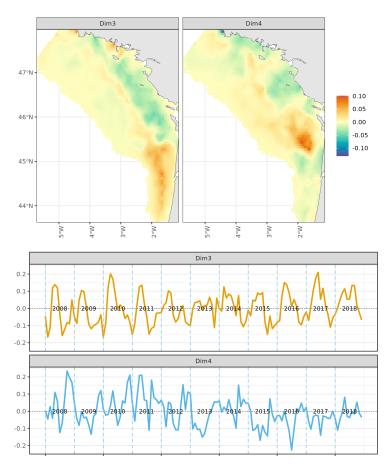


Fig. S2: IST-SDM predictions. (Top) Spatial factors for the dimensions three and four of the EOFs. (Bottom) Loadings for dimensions three and four of the EOFs. Blue dashed vertical lines correspond to the month of January for each year.

### 783 S.1.3 CCA for the IST-SDM case study

- 784 For IST-SDM predictions, we use the same parameterisation for the ancillary variable
- 785 thought the delay D is fixed to D = 0 so that the peak of the seasonal variable falls in March
- 786 (the peak of the reproduction period). This way we aim at disentangling the seasonnal

- 787 signal related to the alternance of reproduction/feeding that can be found in the four first
- 788 dimensions.
- 789 The top-left panel of Figure S3 shows the resulting spatial basis vector, which reinforces
- 790 the offshore-onshore gradient observed in the EOFs results (Figure 3). The inclusion of
- 791 the ancillary variable enhances the clarity of these spatially distinct positive and negative
- 792 regions within the canonical vector. The first three EOFs show a positive correlation with
- 793 the ancillary variable, with the highest correlation coefficient being observed between CCA
- and the ancillary variable. This indicates that the CCA effectively extracts the temporal
- variation from the first three dimensions, resulting in a new variable that best aligns with
- 796 the ancillary variable.

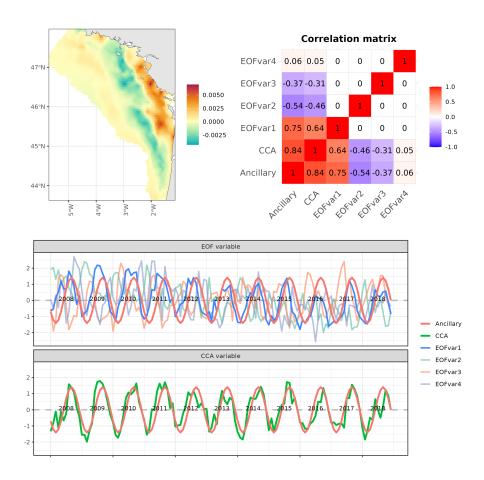


Fig. S3: IST-SDM predictions. Results of the canonical correlation analysis. (Top left) Spatial basis vectors  $\mathbf{w}_1$  that maximize the correlation between the temporal variables  $\mathbf{y}_1$  and  $\mathbf{y}_2$ . (Top right) Correlation matrix between the four first loading factors of the EOFs, the CCA  $\mathbf{y}_1$ , and the ancillary variable. (Bottom) Comparison of the EOFs loadings with the ancillary variable and the CCA variables with the ancillary variable. These time series are standardized. Blue dashed vertical lines correspond to the month of January for each year.

### 797 S.1.4 Lag EOFs on satellite NDVI data

#### 798 S.1.4.1 Data and matrix structure

- 799 In the case of lag EOF, the matrix that is diagonalized contains the spatio-temporal data and
- 800 lagged versions of the data.

Let's denote a vector of lags  $\tau = \{\tau_1, \dots, \tau_j, \dots, \tau_{\mathcal{T}}\}$ . Then, the matrices to bind take the form:

$$\mathbf{S}'^{(\tau_j)} = \begin{pmatrix} S'(x_1, t_1 + \tau_j) & S'(x_1, t_2 + \tau_j) & \cdots & S'(x_1, t_p + \tau_j - \tau_{\mathcal{T}}) \\ S'(x_2, t_1 + \tau_j) & S'(x_2, t_2 + \tau_j) & \cdots & S'(x_2, t_p + \tau_j - \tau_{\mathcal{T}}) \\ \vdots & \vdots & \ddots & \vdots \\ S'(x_n, t_1 + \tau_j) & S'(x_n, t_2 + \tau_j) & \cdots & S'(x_n, t_p + \tau_j - \tau_{\mathcal{T}}) \end{pmatrix}$$

- 801 with  $j \in \{1, 2, \dots, \mathcal{T}\}$
- 802 Then the more usual is to bind the  $\mathcal{T}$  matrices by row (Weare and Nasstrom, 1982).

$$\mathbf{S}'_{lag} = \begin{pmatrix} \mathbf{S}'^{(\tau_1)} \\ \mathbf{S}'^{(\tau_2)} \\ \vdots \\ \mathbf{S}'^{(\tau_T)} \end{pmatrix}$$

- 803 An open question is the choice of the lags. If the data is monthly defined over several years,
- lags  $\tau$  can be months of the year to evidence some sequence of maps that repeat over the
- 805 full time series. For instance,  $\tau = \{0, 3, 6, 9\}$  evidence sequence with quarterly lags over a

- full year.  $\tau = \{0, 1, 2, \dots, 11\}$  would evidence sequence with monthly lags over a full year.
- 807 The matrix  $S'_{lag}$  is then diagonalized like standard EOFs.
- 808 In this case, the spatial factors ( $\mathbf{u}_1$  for instance) are composed of  $\mathcal{T}$  maps and the temporal
- 809 loadings (e.g.  $\mathbf{v}_1$ ) are vectors of length  $p \mathcal{T}$ .

#### 810 S.1.5 Illustration with NDVI data

- 811 We take NDVI satellite data to illustrate lag EOFs. In the example, we consider quarterly
- lags, so  $\tau = \{0, 3, 6, 9\}$ . Based on the scree plot (Figure 2, top right), we select the three
- first dimensions that represents respectively 20%, 20% and 10% of the variance.
- 814 The first and second dimension have an annual period while the third one have a six-month
- 815 period. This last cycle was not evidenced by the standard EOF.
- 816 First and second dimension of the lag EOFs are very similar to the one of the standard EOFs
- with a 3-months offset. They outline the annual variation of NDVI throughout the year with
- 818 high values of NDVI in summer specifically in mountains and low values during winter.
- 819 In the third dimension, loadings are high in February/March as well as August/September
- 820 and low in May/June as well as November/December (Figure S5). The areas that contribute
- 821 most to the sequence of maps are areas in the North of France (Figure S6). This dimension
- 822 highlights that there are peaks of vegetation in spring (April/May) and later in autumn
- 823 (September/October) that can be related to the higher growth of vegetation due most likely
- 824 to rain and moderate temperatures in these areas at this period of the year. By contrast,
- 825 NDVI is low in July and November which are either dry periods for summer or cold period
- which tend to reduce the growth of vegetation.

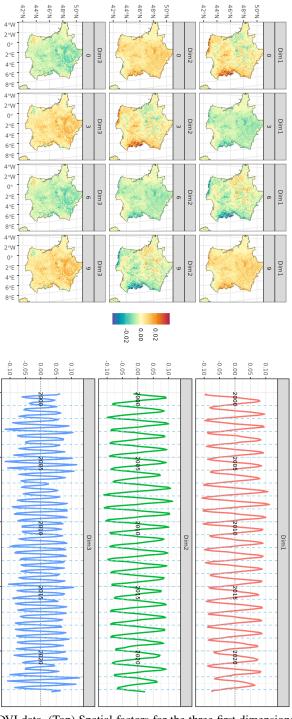


Fig. S4: Satellite NDVI data. (Top) Spatial factors for the three first dimensions of the lag EOFs. (Bottom) Loadings for the three first dimensions of the lag EOFs. Blue dashed vertical lines correspond to the month of January for each year.

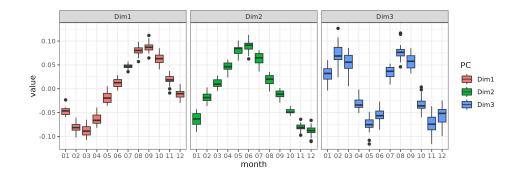


Fig. S5: Satellite NDVI data. Monthly boxplot of the temporal loadings.

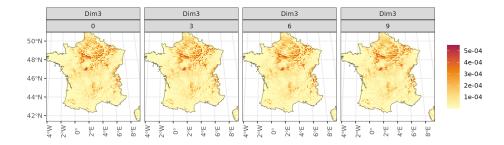


Fig. S6: Satellite NDVI data. Local variance explained by the lag EOFs for the third dimension.

## 827 S.1.6 Multispecies analysis

## 828 S.1.6.1 EOFs raw results

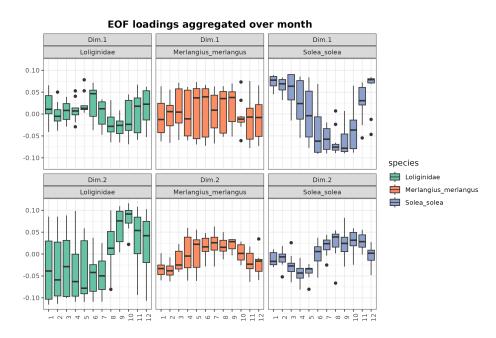


Fig. S7: IST-SDM predictions. Loadings of the multivariate analysis (Figure 6) aggregated over months.

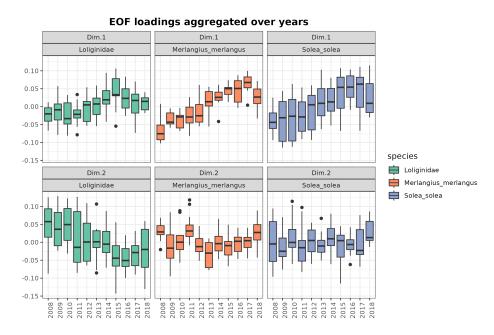


Fig. S8: IST-SDM predictions. Loadings of the multivariate analysis aggregated over years.

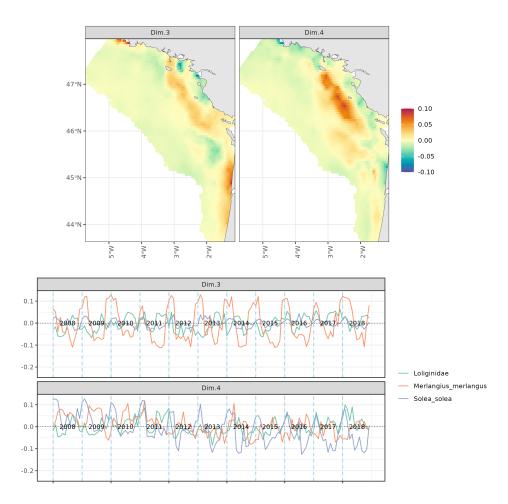


Fig. S9: IST-SDM predictions. Multivariate EOFs on the matrix  $\mathbf{S}'^{(col)}_{multi}$ . (Top) Spatial factors for dimensions three and four. (Bottom) Loadings of each species for dimensions three and four. For each dimension, the loadings of the species represent when the several species of the analysis follow the related spatial factor. Blue dashed vertical lines correspond to the month of January for each year.

#### S.1.6.2 Clustering analysis results

- 830 As mentioned in Alglave, Olmos, et al. (2024), to identify distinct essential habitats and
- 831 to relate these to the ecological seasons, two complementary clustering analyses can be
- 832 performed: one on the spatial factors (spatial dimension) and one on the loading factors
- 833 (temporal dimension).

829

- While the clustering in the temporal dimension identifies groups of time steps that have
- 835 similar spatial patterns, the clustering in the spatial dimension identifies locations with
- similar fish density at the same time step. Clusters of locations can be interpreted as distinct
- 837 functional habitats and clusters of time steps can be interpreted as ecological seasons. Both
- 838 can be represented on a single graph and locations can be related to seasons when they are
- in the same direction on the graph (similarly as is done in PCA).
- 840 In a multivariate perspective, depending whether we choose the temporal synthetic repre-
- 841 sentation or the spatially synthetic representation, the information that comes out can be
- 842 different.
- When adopting the temporally synthetic representation (EOFs on  $\mathbf{S}_{multi}^{\prime(row)}$ ), a set of seasons
- 844 (i.e. temporal clusters) is identified for all the species based on the joint temporal loadings.
- 845 By contrast, the spatial clusters are built based on the spatial factors of the different species.
- Thus there is not only one map of spatial cluster, but as many maps of spatial clusters as
- 847 there are species.
- When adopting the spatially synthetic representation (EOFs on  $\mathbf{S}_{multi}^{\prime(col)}$ ), a single map of
- 849 spatial clusters (functional areas) is obtained. By contrast, the temporal clusters are based
- on the loadings of the different species.
- 851 These differences affect the ecological interpretation of the clustering. Developing both

- 852 temporally and spatially synthetic multivariate EOFs method would be relevant to provide a
- 853 tighter representation of the data. We believe this goes beyond the scope of the paper and
- we let this for future research.

855

#### Temporally synthetic representation

- 856 The spatial clusters 3 and 5 are related to seasons B and D which are mainly winter and
- 857 spring months. These are reproduction period for the species under study (Arbault, Camus,
- and Bec, 1986; Houise, 1993; Moreno et al., 2002); the related spatial clusters can be
- 859 interpreted as reproduction areas for these species. This is consistent with the previous
- 860 studies investigating the reproduction areas of these species (Alglave, Vermard, et al.,
- 861 2023). Interestingly, the spatial cluster 5 is only found for whiting and highlights a specific
- 862 reproduction dynamics in the North of the Bay of Biscay during winter (4.5°W 4°N).
- 863 The spatial clusters 1 and 4 are summer grounds. They are related to seasons C and E that
- mainly gather late spring, summer and autumn months. The spatial cluster 1 is mainly related
- 865 to late spring and summer months. The cluster 4 is related to a longer season spanning from
- summer to end autumn just before reproduction happens for sole and whiting.

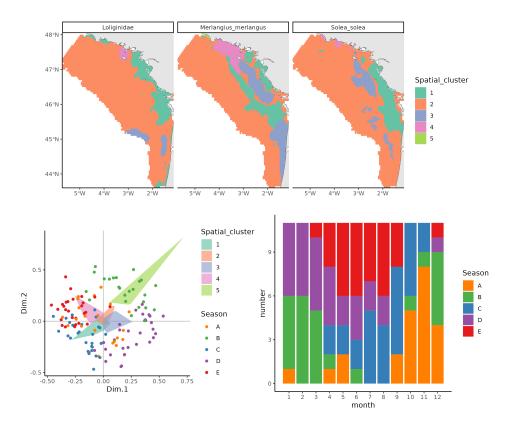


Fig. S10: Clustering analysis for the EOFs outputs of the temporally synthetic representation (EOFs on  $S'^{(row)}_{multi}$ ). (Top row) Spatial clusters representing the functional zones in space for each three species. (Bottom left) Temporal loadings and spatial clusters projected in the two first dimensions of the PCA. (Bottom right) Repartition of the different temporal clusters over the year. Each column sums to eleven *i.e.* the number of year in the analysis. Clustering trees are available below in Figure S11 (locations) and S12 (time steps).

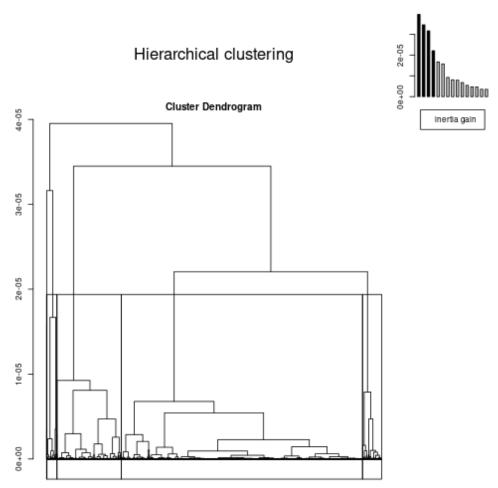


Fig. S11: Clustering tree of the spatial locations for the EOFs outputs of the temporally synthetic representation (EOFs on  $\mathbf{S}_{multi}^{\prime(row)}$ ).

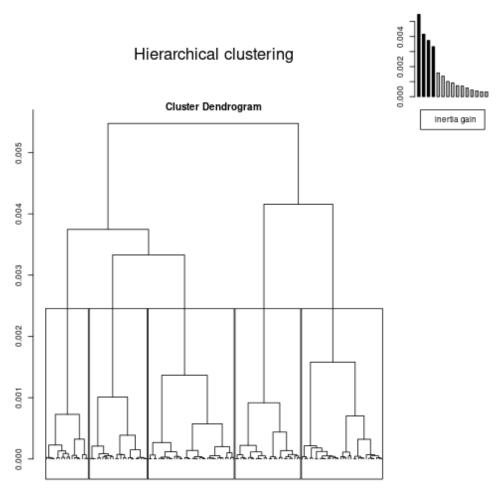


Fig. S12: Clustering tree of the temporal loadings for the EOFs outputs of the temporally synthetic representation (EOFs on  $\mathbf{S}_{multi}^{\prime(row)}$ ).

#### **Spatially synthetic representation**

- 868 Five spatial clusters are identified through the spatially synthetic representation of the EOFs.
- 869 The spatial cluster 1 is related to season B that fall mainly in summer and autumn for each
- 870 three species. The related functional area (spatial cluster 1) can be considered as a summer
- 871 grounds for each three species.

867

- 872 The spatial cluster 4 can be related to the time cluster A that mainly fall in late winter to
- 873 early summer for squids, which includes the period of squids reproduction (January to
- 874 March). For sole it falls in summer during feeding.
- 875 Interestingly, the temporal cluster D falls in winter to spring for each three species (January
- 876 to June depending on the species) and coincides with the reproduction period of the different
- 877 species. For whiting, the cluster E too falls during reproduction. For sole, this coincides
- with the migration off the coast and to the North i.e. off spatial cluster 1 and 4 towards
- spatial clusters 2 and 5.

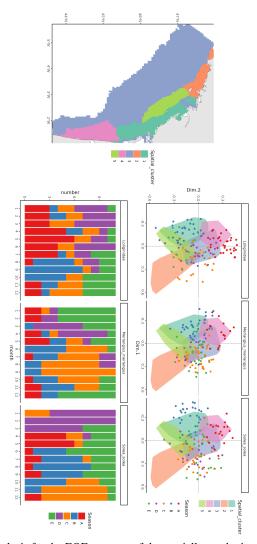


Fig. S13: Clustering analysis for the EOFs outputs of the spatially synthetic representation (EOFs on  $\mathbf{S}_{multi}^{\prime (col)}$ ). (Left) Spatial clusters representing the functional zones in space. (Top row) Projection of the temporal loadings and spatial locations in the two first dimensions of the PCA. The clusters of the locations are the distinct functional zones and the clusters of the temporal loadings can be seen as ecological seasons. (Bottom row) Repartition of the different temporal clusters over the year. Each column sums to eleven *i.e.* the number of year in the analysis. Clustering trees are available below in Figure S14 (locations) and S15 (time steps).

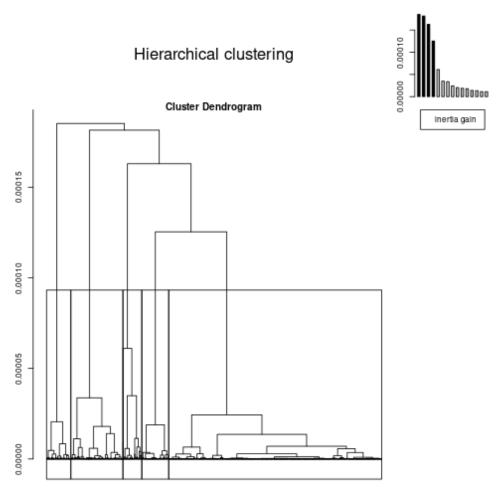


Fig. S14: Clustering tree of the spatial locations for the EOFs outputs of the spatially synthetic representation (EOFs on  $\mathbf{S}'^{(col)}_{multi}$ ).

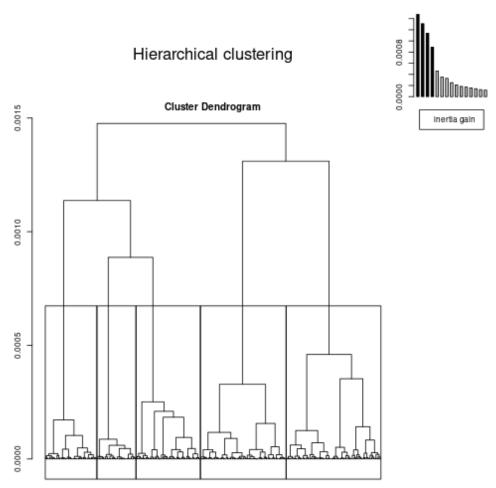


Fig. S15: Clustering tree of the temporal loadings for the EOFs outputs of the spatially synthetic representation (EOFs on  $\mathbf{S}^{\prime(col)}_{multi}$ ).