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# Control of skyrmions in confined devices for multistate memory application

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**Abstract** – The dynamics and stability of magnetic skyrmions within a nano-track with multiple confinements are investigated. The motion of a single skyrmion under a polarized electric current is studied. By adjusting the current magnitude and pulse width, the study reveals the possibility of pinning the skyrmion in each confinement. The depinning of the skyrmion from the top confinement requires two pulses with adjustable time delay while a single pulse is enough to depin it for the case of bottom confinement. The study is extended to two skyrmions and it is found that once a skyrmion is pinned in one confinement, the second one stabilizes in the nearest available empty state. The results show that a multistate device could be obtained with the existence of only one skyrmion per state. This scheme offers an accurate way of controlling the resistance of the devices and thus could be used for multistate memory devices.

## 1. Introduction

A skyrmion is a magnetic quasiparticle with a swirling spin pattern that is topologically nontrivial. It is a two-dimensional object with a topology that can be described as a localized, smooth, and non-singular spin configuration. Since the first experimental observations of skyrmions in crystals [1,2] and thin ferromagnetic layers at room temperature [3,4], intensive studies have been focused on understanding their behavior. The nanoscale size and stability of these quasi-particle magnetic structures make them attractive for their implementation in different applications such as memory [5–8], logic [9] and neuromorphic computing [10–15]. Recently, it has been demonstrated that skyrmions can be created, displaced and annihilated by applying a magnetic field [16,17], spin transfer torque (STT) [18–21], spin-orbit torque [22], ultrafast heating pulses [23,24] or plasmonic resonance [25]. It is worth noting that skyrmions can be displaced with current density with values that could be better than  $10^{11}$  A/m<sup>2</sup> [26] which is much lower than what is required for moving a magnetic domain wall case [27–29]. It has been reported that controlling the materials' intrinsic properties provides an easy way to tune the skyrmions' size and their velocity [30–33], which are among the key characteristics of a functional device; i.e. small size leads to higher memory capacity while high velocity reflects the speed of writing the data. Although the motion of skyrmions within nano-tracks has been widely investigated, their accurate positioning remains a challenge and has not been deeply investigated. In our previous work, we showed that creating stepped confinement could help pin and stabilize a skyrmion [33]. In this paper, we demonstrate the possibility of controlling the position of skyrmions in a multi-stepped nanowire. The study reveals that in the proposed design only a single skyrmion could be stabilized in each confinement. This is mainly due to the optimized confinement dimension. The flow of more than a skyrmion could be properly controlled along the nanowire. The effect of the repulsive force from the edge and the force between the skyrmions play a major role in the observed behavior.

## 2. Theoretical method

The theoretical model of multistate device generation is performed by micromagnetic simulation using Mumax3 software [34] which is based on solving the modified

Landau–Lifshitz–Gilbert (LLG) equation. For the case of current flowing in the plane of the film (CIP), the LLG equation can be written as

$$\frac{d\mathbf{m}^\rho}{dt} = -\gamma \mathbf{m}^\rho \times \mathbf{H}_e^\rho + \alpha \left( \mathbf{m}^\rho \times \frac{d\mathbf{m}^\rho}{dt} \right) + \Gamma_{\text{SST}}^\rho \quad (1)$$

The first and the second term on the right side of (1) are the precession and damping terms, respectively. The effective magnetic field  $\mathbf{H}_e^\rho$  is expressed as:

$$\mathbf{H}_e^\rho = \frac{2A_e}{\mu_o M_s} \nabla^2 \mathbf{m}^\rho + \frac{2K_u}{\mu_o M_s} m_z \hat{z} + \mathbf{H}_D^\rho + \mathbf{H}_{\text{DMI}}^\rho \quad (2)$$

The terms on the right side of (2) are the exchange field, the crystalline magnetic anisotropy field, the demagnetization field and the Dzyaloshinskii-Moriya interaction (DMI) field, respectively. The last term of Eq. (1) is associated with the STT effect in the case of a current flowing in the plane of the device and can be expressed by Zhang-Li form [35]

$$\Gamma_{\text{SST}}^\rho = -(\mathbf{v}_s \cdot \nabla) \mathbf{m}^\rho + \beta \mathbf{m}^\rho \times (\mathbf{v}_s \cdot \nabla) \mathbf{m}^\rho \quad (3)$$

where  $\mathbf{v}_s$  is the effective spin-current drift velocity and  $\beta$  is the non-adiabatic spin torque parameter. The main objective of this study is to investigate a novel design for controlling the motion of the skyrmion in a memory device. We consider a 2 nm thick nano-track with a length of  $L = 780$  nm and a width of 80 nm. Stepped regions with a size of 30 nm by 75 nm were added and removed from some parts of the track to localize the skyrmion position and to improve the linearity and repeatability of storage devices. The material intrinsic parameters used for this study are saturation magnetization  $M_s = 500$  kA/m, exchange stiffness  $A_e = 15$  pJ/m, Dzyaloshinskii Moriya interaction constant  $D = 3.3$  mJ/m<sup>2</sup>, Gilbert-damping coefficient  $\alpha = 0.1$  and the perpendicular magnetic anisotropy  $K_u = 0.8 \times 10^6$  J/m<sup>3</sup>. The shape anisotropy originated from the dipole-dipole interactions and caused a shift in the constant of uniaxial anisotropy in ultrathin film cases where the non-local effects are negligible [36,37]. The sample is discretized in small cells with the size of  $2 \times 2 \times 2$  nm<sup>3</sup>. The values of  $M_s$ ,  $K_u$ ,  $A_{\text{ex}}$  and  $\alpha$  are characteristics of (Co/Ni),

(Co/Pt) and (Co/Pd) multilayers [37–41]. They can be tuned in a wide range by adjusting the respective thicknesses and the number of repeats. The value of  $D$  in typical asymmetric structures where one Pt or Pd at the interface is substituted by Ir, W, and AlOx for instance [42–44]. The magnetic parameters used in this paper are similar to our previous work [33]. [In the LLG equation, the calculation was carried out at 0 K to isolate and understand the intrinsic dynamics of skyrmions without thermal noise.](#)

Firstly, a Néel-type skyrmion with topological charge  $Q = +1$  is created near the left edge of the nano-track and then an electric current with a spin polarization efficiency  $P = 0.4$  is injected into the nano-track in the CIP geometry to generate a motion of the skyrmion. The non-adiabatic torque coefficient  $\beta$  is fixed to 0.2 and the current flows toward the left so the electron would flow in the opposite direction. The device geometry is shown in Fig. 1(b-i).

### 3. Results and discussions

When the skyrmion is present in a wire it represents bit “1” while its absence at a particular position represents bit “0”. To avoid information loss, the position of the skyrmion has to be fixed at a predefined position and the annihilation has to be avoided; hence in the present work, a constructed wire is used to create pinning regions for the skyrmion to define bit positions. Each region represents one bit, which corresponds to “0” if the region does not contain a skyrmion and “1” if the region contains one skyrmion.

#### 3.1. Dynamics of a Single Skyrmion in Constricted Nanowire

In the first part of this study, the pinning and depinning of the skyrmion from the stepped regions under current pulses to create a multistate memory device is investigated. It can be seen from Fig. 1 that it is possible to achieve 8 states with 7 confined regions using a polarized current by displacing the skyrmion in the confinement regions. The calculations were carried out by creating a skyrmion on the left edge as the initial state and a sequence of current pulses were applied. Both the pulse width and the time delay between the pulses were fixed at 2 ns while the current density was varied. Fig. 1(a) shows the position  $x$  of the skyrmion along the nanowire versus time. In the inset of the graph, the magnitude of the current density and the

number of pulses are indicated. The first state was obtained for a pulse with magnitude  $J = 6.0 \times 10^{11} \text{ A/m}^2$  indicated by number 1 in Fig. 1. It can be seen that the skyrmion moves with a constant velocity during the period of 2 ns when the current is applied as indicated by an almost straight line until it reaches a position of about 120 nm then bounces back and stabilizes. This small oscillation of the skyrmion seen before stabilized is due to the repulsive force from the edge. Skyrmion shows noticeable inertia-driven drift after the current pulse is removed rather than stopping immediately. The color scale in Fig. 1(b-i) represents the out-of-plane component  $m_z$  of the magnetization. The displacement of the skyrmion to state 2 (first top confined region) starting from the initial position can be realized by another single pulse with the same duration and  $J = 3.0 \times 10^{11} \text{ A/m}^2$ . The slightly attenuated oscillations after reaching the maximum position indicate that the skyrmion is swirling within the first confinement before stabilizing. [All stated where achieved by starting from a fixed initial point, with state 1 being the initial reference point.](#) Displacing the skyrmion from state 2 to state 3 requires two pulses; the first one to excite the skyrmion while the second one to move it to the third state. Here two pulses with the same magnitude of  $5.5 \times 10^{11} \text{ A/m}^2$  are applied. It is important to mention that the need for two pulses to move the skyrmion from the top confinements is due to the skyrmion Hall effect. It is known that the skyrmion Hall effect which is a deviation of the skyrmion path to the edge represents a challenge for skyrmion-based structures [45–48]. To overcome this issue, an antiferromagnetically coupled structure [49–52] and spin-orbit torque combined with STT [53] have been proposed to reduce skyrmion deviation to the edge effect. The other states could be obtained by altering the amplitude and number of pulses as indicated in Fig. 1(a). Interestingly, to pin the skyrmion in the upper confinement area (states 2, 4, 6 and 8), a single pulse is applied, whereas two pulses are required to move it to the lower confinement area (states 3, 5 and 7). Moreover, the pulse amplitude for the upper confinement was found to be fixed at  $3.0 \times 10^{11} \text{ A/m}^2$  while in the lower confinement, the amplitude changes depending on the history of the skyrmion. From Fig. 1, the oscillation in the  $x$  position with time is observed each time the skyrmion is driven from upper to lower states. In this part of the study, the time delay  $t_d$  between two consecutive pulses was fixed to 2 ns (Fig. 2). This parameter has to be adjusted to avoid the annihilation of the skyrmion as can be seen in Fig. 2(c) for  $t_d = 1$  ns. In contrast, if the two pulses are largely delayed, as shown in Fig. 2(a) for  $t_d = 3$  ns, the

skyrmion will not be displaced to the [next](#) state. As briefly discussed above, the first pulse is for exciting the skyrmion and making it ready for being displaced.

The effect of nanowire geometry on current-induced skyrmion dynamics was investigated. Fig. 2(d) is a plot of the skyrmion trajectory from state 1 to state 2, it is clear that the skyrmion is not moving in a straight line (blue line). The Magnus force acts in the direction normal to the drift velocity of the skyrmion and can therefore cause spiraling trajectories. The dashed lines indicate the border of the magnetic region. The sign of the skyrmion topological charge  $Q$  leads to the opposite direction of the topological Magnus force. It is found that the skyrmion rotation clockwise and counterclockwise depends on the sign of the skyrmion charge [54]. For the case of a Néel-type skyrmion with  $Q = -1$ , the motion is counterclockwise while for  $Q = +1$  the direction of the skyrmion is clockwise. The radius of the path changes depending on the value of the Gilbert damping constant that affects the skyrmion Hall effect and the speed [55]. Here only one pulse is applied to move the skyrmion from state 1 to another stable state at the top confined region. Along its path, it was observed that the skyrmion size can be reduced due to the higher compression of the skyrmion by the barriers. It was observed that the size of the skyrmion was changing and reduced by about 1 nm at position 2 before expanding by about 2 nm when stabilized due to the dipolar repulsive force from the edge. The repulsive force from the edge causes the size of the skyrmion to decrease while passing through the states, if this force is too large in the case of a larger skyrmion or narrower channel for the skyrmion or larger current density, the skyrmion will annihilate. Both the intrinsic parameter and the geometry of the device need to be taken into account while designing the wire, more details can be found in Ref. 33. To move the skyrmion from state 2 to state 3 shown in Fig. 1, two pulses were used. The first one with  $J = 5.5 \times 10^{11}$  A/m<sup>2</sup> and 2 ns pulse width for exciting the skyrmion and the second one with the same  $J$  and pulse width for displacing it to the next state. Fig. 3(a) is a plot of the skyrmion position along the nanowire  $x$ -direction to reach state 1 shown in Fig. 1. When the pulse current with  $J = 6.0 \times 10^{11}$  A/m<sup>2</sup> is applied during the first 2 ns, there is a fast motion of the skyrmion represented by the left edge. For a larger current, the skyrmion can overcome the repulsive force from the first edge and be able to stabilize at the next state. Depending on the current density, the skyrmion can reach any one of the available stepped regions. Fig. 3(b) shows the velocity  $V_x$  of the skyrmion with time. A clear increase of  $V_x$  could be noticed until

reaching a maximum value of  $\sim 60$  m/s before a sudden drop indicating a bouncing back of the skyrmion.

### 3.2. Two Skyrmions Dynamics in Constricted Nanowire

In the second part of this study, we considered the case of two skyrmions in a chain, initially located at the left side of the nanowire and the focus was on the possibilities of achieving higher numbers of states. We started with two skyrmions namely  $S_1$  (leading) and  $S_2$  (trailing) and we investigated their motion under a pulsed current similar to a single skyrmion case previously discussed. Initially, skyrmion  $S_1$  is leading  $S_2$  by about 50 nm. Under the same pulse with  $J = 4.0 \times 10^{11}$  A/m<sup>2</sup> and a width of 2 ns, the leading skyrmion  $S_1$  could be displaced to state 2 (top confinement) after overcoming the bottom barrier as shown in Fig. 4 (a). Inside the top confinement and because of the repulsive force as has been discussed in our previous work [33],  $S_2$  undergoes a helical motion and stabilizes outside the confinement. The motion of trailing skyrmion  $S_2$  is quite different. The color code represents the skyrmion radius, which is shrinking when it is closer to the bottom or top edges. The trailing skyrmion  $S_2$  could not reach the top confinement due to the strong interaction with  $S_1$ . It can be seen from Fig. 4(a) that  $S_2$  was back due to the existence of  $S_1$ . The dimension of the confinement and the repulsive interaction skyrmion-skyrmion allows the stability of only one skyrmion per state. Firstly, the size of  $S_1$  is reduced close to the bottom step and when it is closer to  $S_2$  before bouncing back. The snapshots in Figs. 4(b-d) show the positions and size of  $S_1$  and  $S_2$  in three different situation. In Fig. 4(b),  $S_1$  which is very close to the edge of the bottom stepped region, shrinks in size are reported in Fig. 5(b) and indicated by the state A. The radius of  $S_2$  remains unchanged. A second reduction of  $S_1$  radius occurs at state B in Fig. 5(b) corresponding to when it reaches the right edge of the top confinement. This state can also be seen in the snapshot of Fig. 4(c). The third reduction of  $S_1$  happens when it is closer to  $S_2$  corresponding to state C in Fig. 5(b) and snapshot of Fig. 4(d). On the other hand, the size of  $S_2$  is reduced continuously when it is approaching the stepped region until reaches its minimum ( $\sim 20$  nm) when it is also close to  $S_1$  as shown in Fig. 4(a). Fig. 5(a) is a plot of the position of the two skyrmions and the separation between them as a function of time. The positions  $r_1$  and  $r_2$  are taken from the left-bottom edge of the nanowire and the dashed regions in Fig. 5 indicate the



stepped region. The skyrmion-skyrmion repulsive force is maximal when  $S_1$  and  $S_2$  are very close (minimum  $S$ ) which corresponds to a small radius for both skyrmions.

For  $J = 5.0 \times 10^{11}$  A/m<sup>2</sup> of 4 ns duration, it can be seen from Fig. 6(a) that both  $S_1$  and  $S_2$  overcome the first non-magnetic barrier (bottom stepped area) but  $S_1$  could reach the next bottom confinement while  $S_2$  was again bounced back to the top confinement. For  $S_2$ , this is the only nearest available state. By following the path of both skyrmions, one can see from Fig. 6(b) that there is a repulsive force between  $S_1$  and  $S_2$ , which is responsible for the deviation of  $S_2$  from reaching the same state as  $S_1$ . The dashed region in Fig. 6(a) represents the magnetic part of the device. From two interacting skyrmions, it could be seen that under the device geometry, only one skyrmion could be stabilized in each confined region.

#### **4. Conclusion**

Towards a multistate spintronics device, a stepped nano-track with bottom and top confinements was proposed. For a common material with perpendicular magnetic anisotropy, the adjustment of current magnitude and its duration enables the displacement of the skyrmion at any position. Furthermore, the study of two skyrmions shows the possibility of moving them accurately with only one skyrmion in each confinement. The dimension of the confinement and the repulsive forces from the edge and from skyrmion-skyrmion are responsible for this finding. Due to the Hall angle, depinning a skyrmion from bottom confinement needs only a single pulse current with an optimal magnitude and duration while two pulses are necessary for depinning from top confinement. If the time delay  $t_d$  between the two pulses is too short, the skyrmion collapses and if  $t_d$  is too large, the skyrmion remains pinned. The dynamic of a large number of skyrmions created at one side shows the possibility of stabilizing/pinning a single skyrmion in each confinement. These results open the way for large-capacity memory devices and neuromorphic computing.

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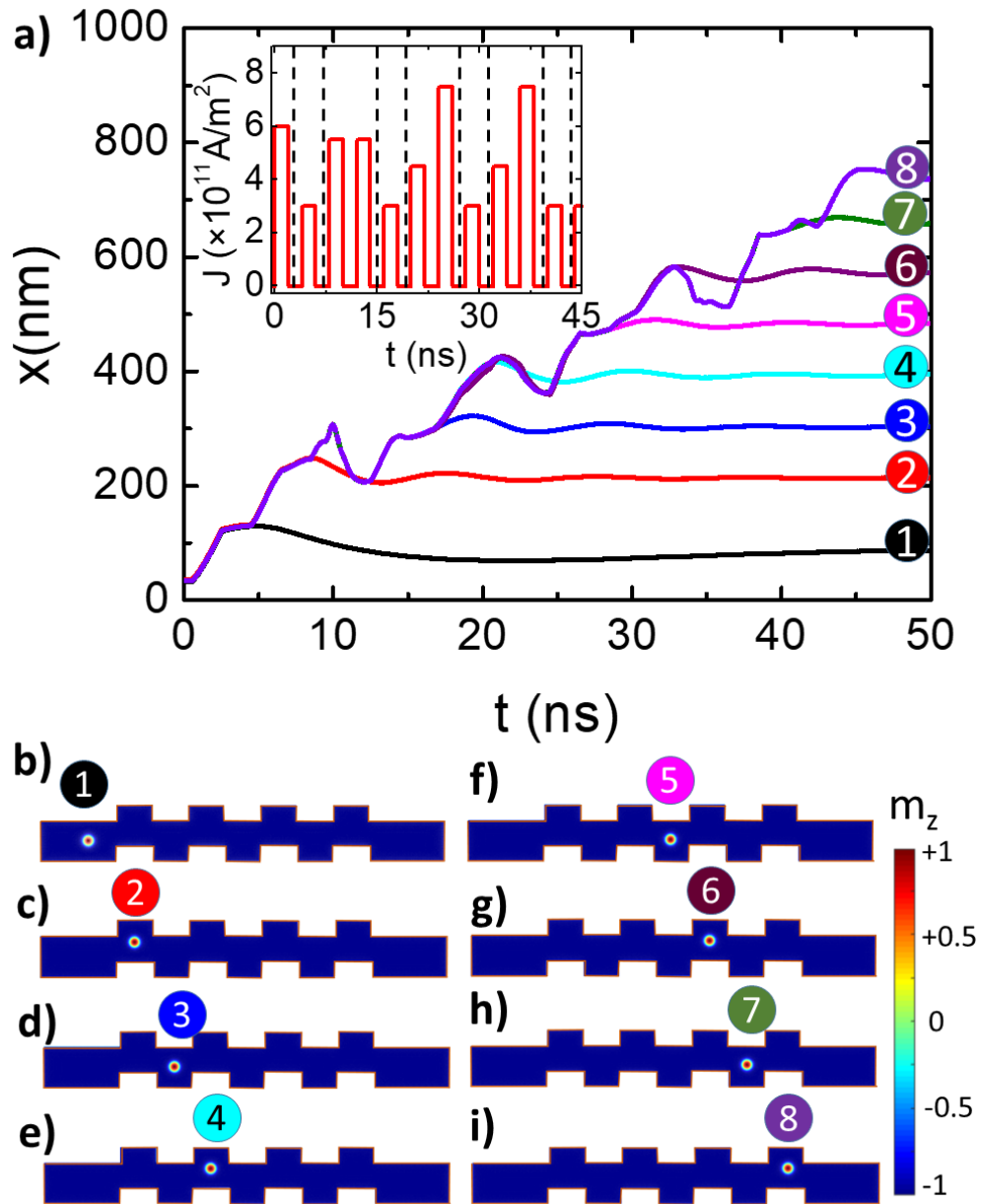


Fig. 1. (a) Time dependence of the skyrmion position for different current density values. After each pulse, the time dependence of the position  $x$  is recorded. The following pulse is applied by considering the skyrmion at the initial state. Inset is the current density magnitude versus time. To reach states 3, 5 and 7, two pulses were necessary. The inset is an enlarged  $x$  position of the skyrmion showing that the skyrmion stabilized at the top confined region and swirled in that region before moving to the next bottom confinement. (b)-(i) snapshots of magnetic states as in (a). The length of the wire is  $L = 780$  nm, the width  $w = 80$  nm and the thickness is 2 nm. The color scale shows the out-of-plane component of magnetization.

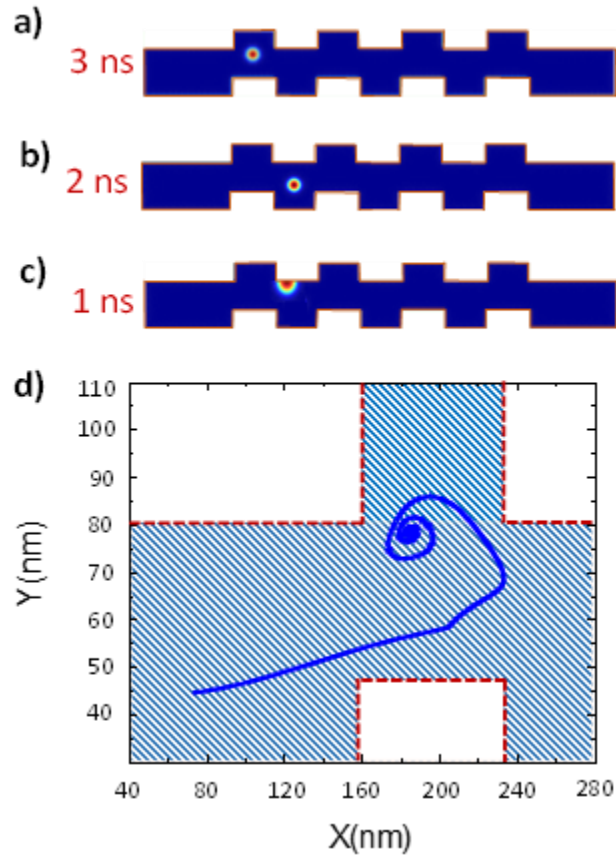


Fig. 2. (a) The skyrmion remains pinned when the time delay is larger than 2.8 ns, (b) the skyrmion moves to the third state when the time delay is between 1 and 2.7 ns and (c) annihilation of the skyrmion when the time delay is less than 1 ns for two fixed pulses of  $5.5 \times 10^{11} \text{ A/m}^2$  and 2 ns duration. (d) The skyrmion trajectory from state 1 to state 2 shows counter-clockwise spiral motion under a pulsed current of  $3.0 \times 10^{11} \text{ A/m}^2$  for 2 ns duration.

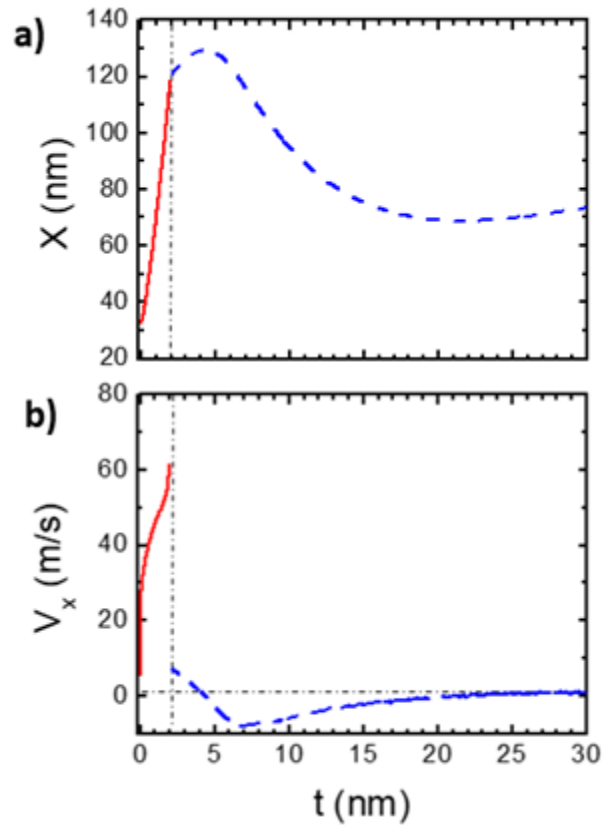


Fig. 3. (a) The  $x$ -position and (b) the velocity of the skyrmion versus time when a current density of  $3.0 \times 10^{11} \text{ A/m}^2$  is applied for 2 ns. The solid and dashed lines are when the current is on and off, respectively.



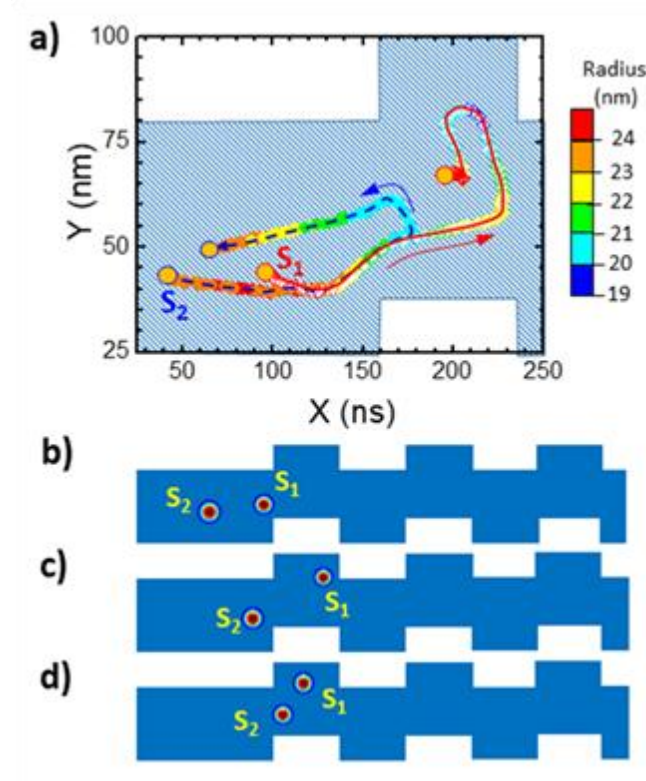


Fig. 4. (a) The Path of skyrmion  $S_1$  (solid line) and skyrmion  $S_2$  (dotted line) under a current density of  $4 \times 10^{11} \text{ A/m}^2$  for 2 ns duration. The code bar represents the radius of  $S_1$  and  $S_2$ . The trailing skyrmion  $S_2$  was bounced back due to the interaction with the leading one  $S_1$ . This later was stabilized near the confined region but not inside because of the net edges repulsive force. (b) to (d) are snapshots of skyrmions  $S_1$  and  $S_2$  within the device at different positions. These images are taken at the three states A, B and C indicated in Fig. 5(b).

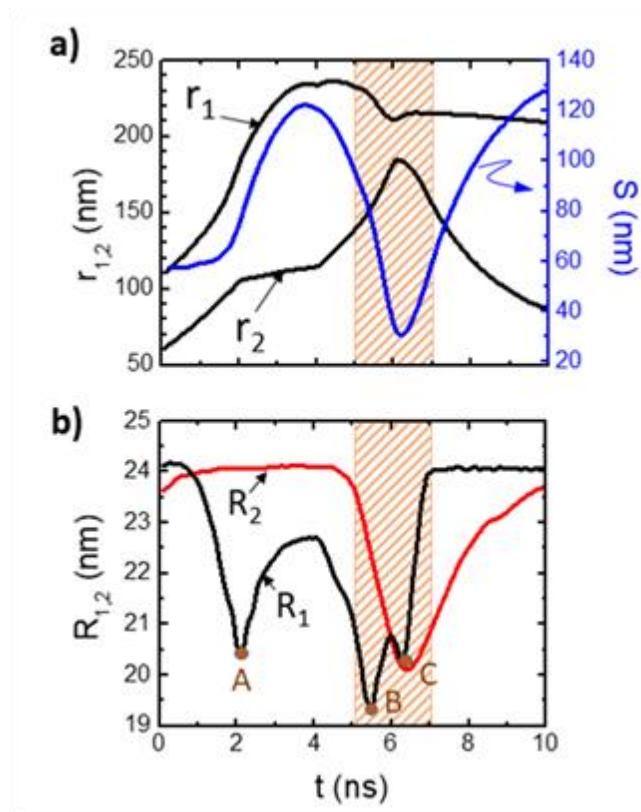


Fig. 5. (a) The time dependence of the positions of  $S_1$  and  $S_2$  and the separation between. (b) The radius of  $S_1$  and  $S_2$  as a function of the time. The dashed regions indicate the stepped region.

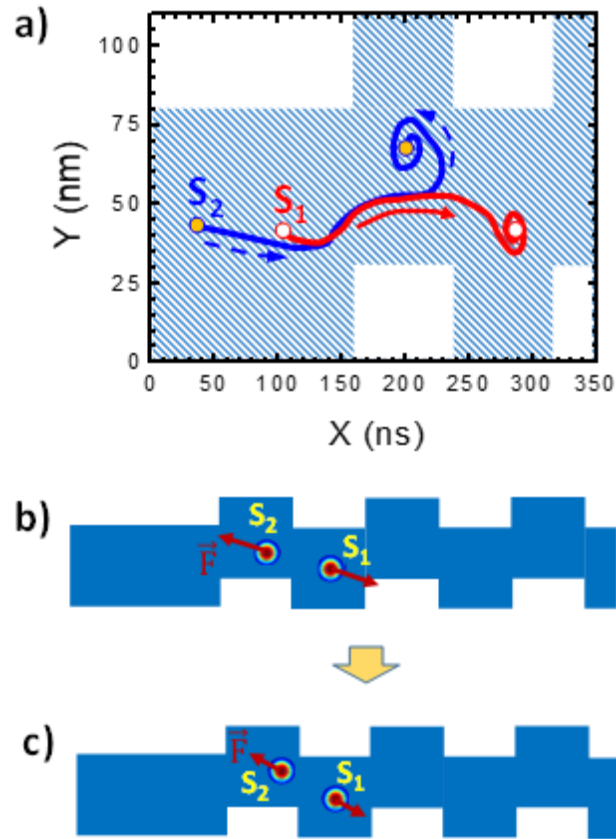


Fig. 6. (a) The Path of skyrmion  $S_1$  (solid line) and skyrmion  $S_2$  (dotted line) under a current density of  $5 \times 10^{11}$  A/m<sup>2</sup> for 4 ns duration. The trailing skyrmion  $S_2$  was bounced back to the top confinement due to the interaction with leading one  $S_1$ . This later was stabilized near the bottom confined region but not inside because of the net edges repulsive force. (b) and (c) are snapshots of skyrmions  $S_1$  and  $S_2$  within the device at different positions. The arrows represent the repulsive forces between  $S_1$  and  $S_2$ .