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Vesicular Neurotransmitters Exocytosis Monitored by Amperometry: Theoretical Quantitative Links Between Experimental Current Spikes Shapes and Intravesicular Structures.

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Abstract:

Single cell amperometry has proven to be a powerful and well-established method for characterizing single vesicular exocytotic events elicited at the level of excitable cells under various experimental conditions. Nevertheless, most of the reported characteristics are descriptive, being mostly concerned with the morphological characteristics of the recorded current spikes (maximum current intensities, released charge, rise and fall times, etc.) which are certainly important but do not provide sufficient kinetic information on exocytotic mechanisms due to lack of quantitative models. Here, continuing our previous efforts to provide rigorous models

rationalizing the kinetic structures of frequently encountered spike types (spikes with unique exponential decay tails and kiss-and-run events), we describe a new theoretical approach enabling a quantitative kinetic modeling of all types of exocytotic events giving rise to current spikes exhibiting exponential decay tails. This model follows directly from the fact that the condensation of long intravesicular polyelectrolytic strands by high concentrations of monocationic neurotransmitter molecules leads to a matrix structure involving two compartments in constant kinetic exchanges during release. This kinetic model has been validated theoretically (direct and inverse problems) and its experimental interest established by the analysis of the amperometric spikes relative to chromaffin and PC12 cells previously published by some of us.

Keywords: vesicular exocytosis, single cell amperometry, spikes with one or two-exponential decay tails, theoretical modeling, intravesicular matrix condensation structure.

Introduction

Neurons and secretory cells release molecular messengers including neurotransmitters stored inside intracellular vesicles through exocytosis. In these processes, a local fusion of the vesicle and cellular membranes occurs, creating a nanoscale fusion pore through which the vesicle content can be gradually released extracellularly (Fig. 1a) and detected by its oxidation at the tip of a carbon ultramicroelectrode in contact with the membrane of target neurons or neuroendocrine cells.¹⁻³ These highly regulated activated processes depend significantly on cell types and/or their environment as well as the frequency and amplitude of activation pulses of adequate elicitors (e.g. Ca^{2+} , Ba^{2+} , K^+ , etc.). This allows recording of long-lasting amperometric traces consisting of large

series of brief transient current spikes featuring sequential release events from individual vesicles.⁴ These informative traces encompass three major categories of current spikes which can be described based on their general shapes and whose relative proportions depend on the nature and conditions of the eliciting procedure as well as on the type of cell investigated. The most common category (>50–80%) contains well-defined current spikes involving a rapid increase in current intensity, primarily due to the opening of fusion pore, followed by a much longer monotonic decrease in current, termed hereafter the spike tail, leading to a gradual decrease while the current return to the baseline. A second category displays groups of accidental superposition of a few independent spikes from the first category when the local delay time between spikes is less than the average duration of their tails. The relative proportion of these overlapping signals can be significantly reduced by adequate modulation of the eliciting conditions. The peaks of this second category do not require specific theoretical analyzes since they can be easily modeled by statistical superpositions of peaks belonging to the first category. The third category, primarily observed for neurons probed under synapse-like conditions, represents complex events which could be precisely rationalized and quantitatively described as the result of flickering opening/closing sequences of fusion pores.^{5,6}

Based on this categorization, it follows that most spikes containing kinetic information of interest for revealing general mechanistic features of exocytotic vesicular release control belong to the first category. This justifies the considerable efforts made to extract such fundamental biological information through physicochemical modeling and precise analyzes of this type of spikes.^{7–11} However, due to the absence so far of any rigorously established model and theory, these theoretical analyzes have necessarily been limited to spikes in the first category that exhibit a single exponential decay tail. But this omits spikes of the first category that exhibit two exponential tails

although they generally represent a large proportion of events from this category and may even characterize most of them (see below for PC12 cells^{12,13}). Such a particular shape has been qualitatively interpreted considering that it comes directly from non-isotropic intravesicular granular matrix structures (also known in the literature as “dense core” and “halo”^{14,15}) that are expected to result from the imperfect condensation of the polyelectrolyte chromogranin by monocationic molecules.^{12,13,16,17} Indeed, as will be established therein, such granular structure implies the existence of complex kinetic exchange between differently condensed intravesicular domains while extracellular release of neurotransmitter proceeds.

Hereafter, we wish to establish theoretically and validate this new kinetic model based on the analyses of experimental spikes with two-exponential tails. A first scope is to rationalize theoretically the origin of these spikes as indicated above. A second objective is to develop a quantitative computational procedure based on this model to ensure precise extractions of structural, biophysical and kinetic information on intravesicular organization as well as on the size of fusion pores and their opening kinetics.

Results and Discussion

Our main objective below is to describe and validate an original physicomathematical model aimed at accounting for the existence of the two types of current spikes of the first and most common class displayed in the amperometric traces recorded with carbon fiber microelectrodes from single neuroendocrine cells (see, e.g., Fig. 1b) in order to extract structural and kinetic features sustaining neurotransmitters (NT) release mechanism (Fig. 1a). The innovative contributions of the following report rest therefore essentially on theoretical and numerical bases. However, in order to validate this new model and document the efficiency of the resulting original extraction procedure, we will

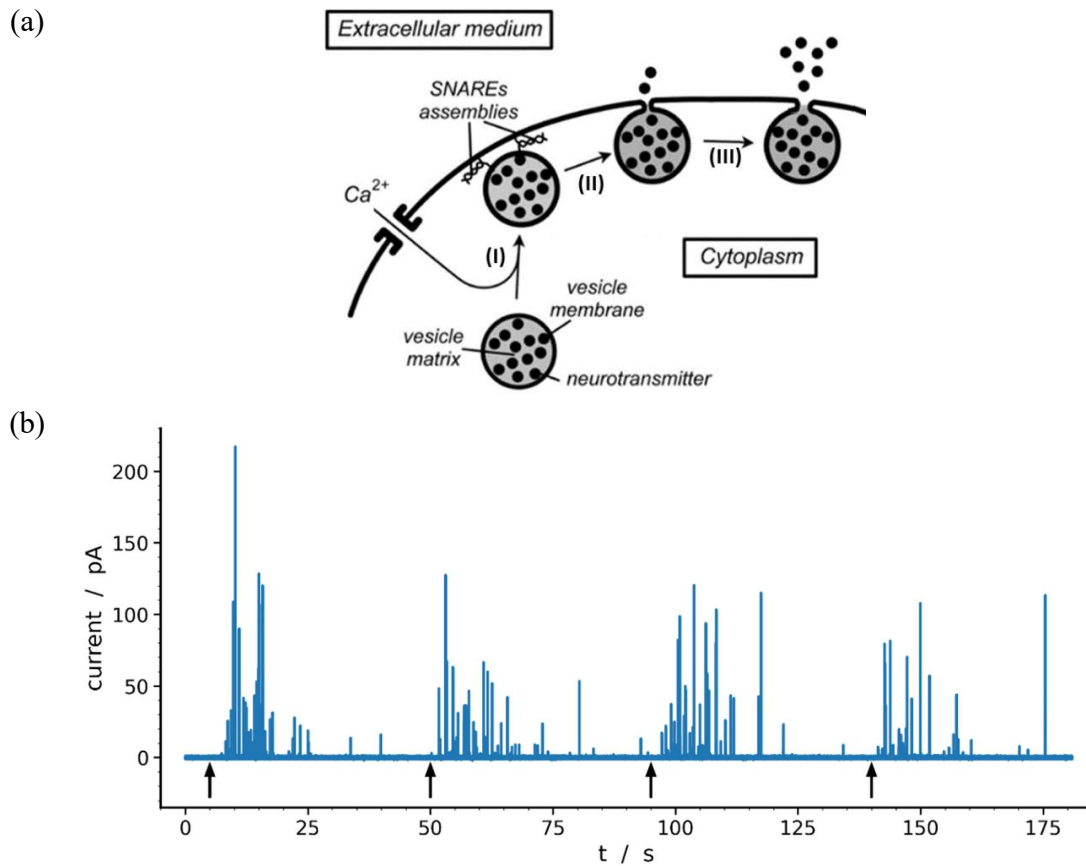


Fig. 1. a) Schematic representation of the main exocytotic release steps¹⁰: (I) Ca²⁺-driven docking of a primed exocytotic vesicle; (II) opening of the fusion pore and beginning of release; (III) final opening of fusion pore and main releasing phase (for simplicity the SNAREs assemblies are only represented at the end of phase I because they play a crucial role in the docking mechanism;^{18,19} for the same reason the membrane cytoskeleton, see Fig.3 in previous work⁹, is not shown). b) Representative amperometric data from a single PC12 cell with highly loaded vesicles¹² recorded in HEPES buffer with 5 μm carbon fiber electrode held at +680 mV vs Ag/AgCl. The 4 distinct groups of spikes seen in the trace were elicited by a series of 5 s duration 105 mM K⁺ puffs (each arrow indicates the beginning of K⁺ pulse for each group). Most of the events displayed in the trace (84%) were analyzable through the model developed here including 97 spikes exhibiting two-exponential tails and 9 single-exponential ones (see Table 1 and Fig 7).

rely mainly on our previously published data relative to chromaffin cells^{1,10} or to PC12 cells containing vesicles with usual²⁰ or high NT loads¹².

Definitions of spikes with single and two exponential decays

Fig. 1b displays a representative amperometric trace recorded from a PC12 cell which contains mostly current spikes of the first category (see Fig. 2). Similar traces are recorded from chromaffin cells and other neuroendocrine cells.²⁰ The fast current rise of spikes of the first category mostly features the fusion pore opening dynamics.³ In contrast, the kinetics of descending branches is mainly controlled by diffusion-limited vesicle emptying, while the fusion pore radius has already reached its maximum value.⁹ It ensues that the existence of two types of spikes within the first category mostly evidences different kinetics of NT diffusional transport within the vesicles during release. These kinetics can be rigorously discriminated by plotting the spikes current in semi-log-scales as evidenced in Fig. 2Ba,b.^{13,21} Note that in order to simplify we use “diffusion” to represent the kinetically equivalent outcome of site-hopping exchange whereby a NT cation shifts from one chromogranin chelating site to an adjacent one. Indeed, as established for the similar situation in polymers,^{10,22–26} at a constant temperature, the corresponding kinetics are identical to those of a straightforward diffusion process.

Let us first briefly recall the basics of the theoretical approach^{9,10,27} that we developed to analyze spikes with single-exponential current decay branches since, as will be made clear later, it is a simplified version of the physicochemical model developed in this work. Note that this previous model was carefully validated experimentally by analyzing several thousands of experimental amperometric spikes recorded from different cells (chromaffin, PC12, neurons, etc.).

First, we assume that the diffusional transport kinetics is essentially limited by the slow NT diffusion within the intravesicular matrix in order to reach the fusion pore and be released out. Indeed, for chromaffin or PC12 cells typical diffusion coefficients of NT inside the vesicle matrix is ca. 10^{-7} cm²/s,²⁸ while it is ca. 10^{-5} cm²/s in the extracellular solution.²⁹ Since the vesicle radius is in the range of 80-300 nm^{1,30} while the electrode – cell gaps are typically 100 – 200 nm,¹ the diffusion times in the gaps (viz., a few μ s) are negligible compared to that in the vesicular matrices (ca. a few tens of ms). Similarly, if the fusion pore connecting vesicle interior and extracellular space has not a flat toroid shape but a cylindrical one we have shown that the diffusion time through the cylindrical tube can be neglected (see section SM1 in Supplementary Material in work¹⁰) unless the pore has length larger than vesicle size which, to the best of our knowledge, was never observed for NT release by cells.

Our former approach¹⁰ relies on Newton and Kelvin views to describe cooling of spherical bodies. This was previously validated for exocytotic vesicular release through accurate 3D numerical simulations for exocytotic vesicles.^{8,9} Interestingly, the approach proposed by Newton and Kelvin permits the use of ordinary differential equations to describe the temporal variations of intravesicular quantities over time periods exceeding a few tenths of the spikes rising times, i.e., as soon as a quasi-steady state diffusion regime prevails inside the whole vesicle.⁸⁻¹⁰ In addition to simplifying the physicomathematical formulations, this considerably reduces the duration of numerical analyzes of amperometric traces containing hundreds of spikes (Fig.1b) to extract kinetic and structural information without any significant loss of precision compared to a 3D approach. Thus, a few seconds only are required per 2-exp spike while the procedure is almost instantaneous for 1-exp ones.

Spikes with single exponential tails. The instant NT released flux is given by:

$$dq_{out}/dt = -dq_{ves}/dt \quad (1)$$

where $q_{out}(t)$ is a theoretical quantity representing the total NT quantity that has been released by one vesicle at time t in the extracellular space independently of the fact that a large fraction of it has been electrooxidized; $q_{ves}(t)$ is the intravesicular NT quantity at time t . Whenever the diffusion of NTs inside the vesicle to the entrance of the pores is the limiting step, and that NTs are readily oxidized by the electrode one obtains:

$$i(t) = nF dq_{out}/dt = -nF dq_{ves}/dt \quad (2)$$

where n is the number of electrons involved in the oxidation, for example, $n = 2$ for catecholamines,³¹ and q_{ves} time variations are given by:¹⁰

$$dq_{ves}/dt = -k_{\rho}^{diff}(t) \times q_{ves}(t) \quad (3)$$

where $k_{\rho}^{diff}(t)$ is defined as:^{9,10,34}

$$k_{\rho}^{diff}(t) = \left[\frac{D_{ves}}{r_{ves}^2} \times \frac{r_{pore}^{max}}{r_{ves}} \right] \rho(t) = k_{max}^{diff} \frac{r_{pore}(t)}{r_{pore}^{max}} \quad (4)$$

where $\rho(t) = r_{pore}(t)/r_{pore}^{max}$, $r_{pore}(t)$ being the time dependent radius of the fusion pore and r_{pore}^{max} its maximum value and D_{ves} is the apparent NT diffusion coefficient within the intravesicular matrix of radius r_{ves} . Note that $k_{\rho}^{diff}(t)$ and the fusion pore radius, $r_{pore}(t)$, are strictly proportional at any time. Nonetheless, in the following we favor writing kinetic equations involving $k_{\rho}^{diff}(t)$ because it is equivalent to a rate constant.

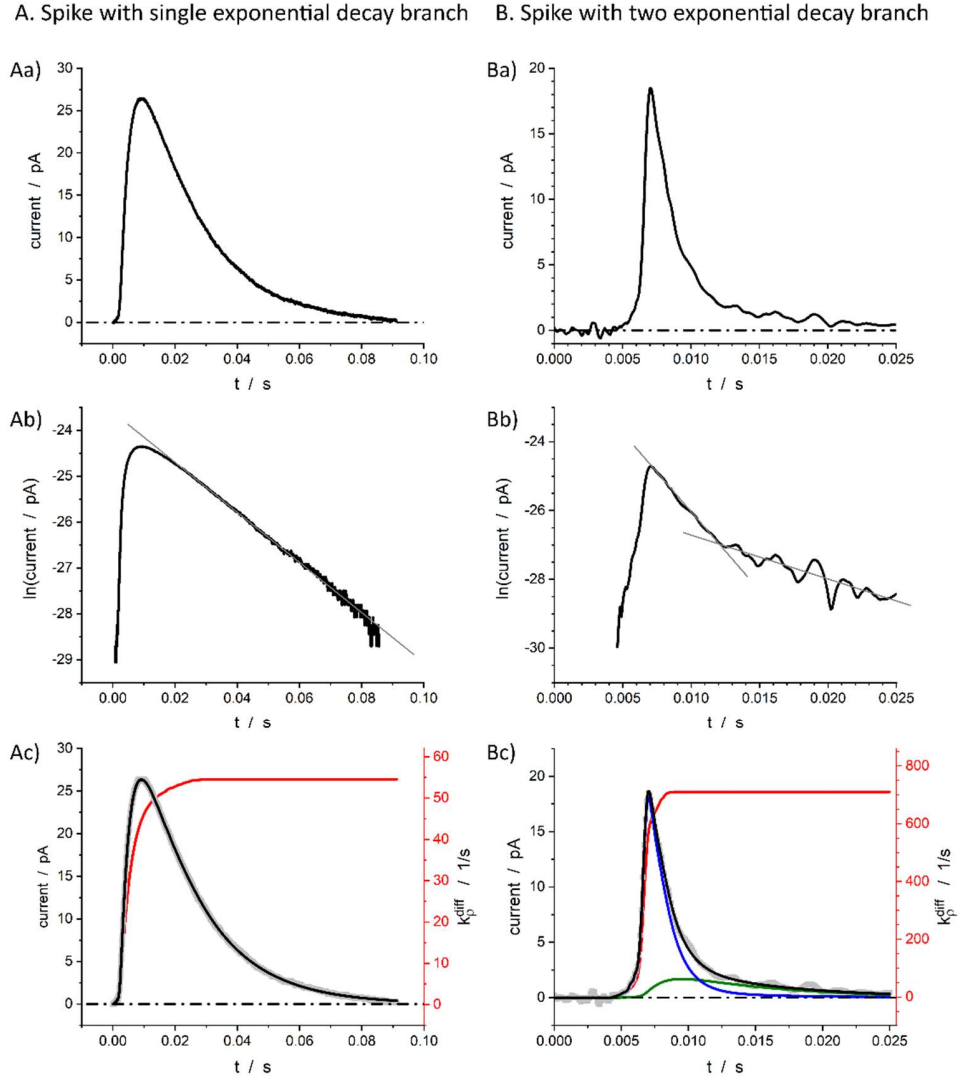


Fig.2. Single (A) and double exponential (B) spikes in linear (a) and semi-log (b) scales; c) shows simulation results of the spike current (black), its components (blue and green in Bc, see below for the meaning) and fusion pore opening dynamics (red, see text for $k_p^{diff}(t)$ definition) with $k_{\rho_{max}}^{diff} = 54.5 \text{ s}^{-1}$ in (Ac) and $k_{\rho_{max}}^{diff} = 710.0 \text{ s}^{-1}$ in (Bc). The grey symbols are the overlaid experimental spikes shown in (a). The spike (A) was obtained from a chromaffin cell, while spike (B) is from a PC12 cell. Assuming $D_{ves}/r_{ves}^2 = 415 \text{ s}^{-1}$,²⁷ $r_{ves} = 156 \text{ nm}$ ³² for chromaffin cells and $D_{ves}/r_{ves}^2 = 5.8 \times 10^3 \text{ s}^{-1}$,³³ $r_{ves} = 95 \text{ nm}$ ³³ for PC12 cells, the maximum pore opening can be evaluated as $r_{pore}^{max} = 20 \text{ nm}$ and $r_{pore}^{max} = 12 \text{ nm}$, respectively.

For the sake of presenting simply our approach, let us first assume that the fusion pore radius reaches its maximal value r_{pore}^{max} , i.e., $\rho = \rho_{max} = 1$, faster than any other time scale of interest, then $k_{\rho}^{diff}(t)$ is a constant noted as k_{max}^{diff} at all relevant times. Under these conditions, one obtains from Eq.(3):

$$i(t) = nF k_{max}^{diff} q_0 \exp(-k_{max}^{diff} t) \quad (5)$$

where q_0 is the total quantity of releasable NT present in the matrix before release starts. q_0 is readily determined by the time integration of the whole spike (see below). Note that Eq.(5) justifies that after fusion pores have reached their maximum values one-exponential decay branches with time constants $\tau_{1exp} = 1/k_{max}^{diff}$ are observed (compare Fig.2Ab).

However, before the fusion pore radius reaches its maximal value one has from Eqs.(2)-(3):

$$i(t) = nF k_{\rho}^{diff}(t) q_{ves}(t) \quad (6)$$

where, owing to the conservation of matter, $q_{ves}(t)$ is given by Eq.(7):

$$q_{ves}(t) = q_0 - \frac{1}{nF} \int_0^t i(\tau) d\tau \quad (7)$$

Additionally, from Eqs.(6) and (7) one obtains the fusion pore time opening function $\rho(t)$:¹⁰

$$\rho(t) = r_{pore}(t)/r_{pore}^{max} = \frac{i(t)}{nF k_{max}^{diff} q_{ves}(t)} \quad (8a)$$

that is:

$$\rho(t) = \frac{i(t)}{nF k_{max}^{diff} \left[q_0 - \frac{1}{nF} \int_0^t i(\tau) d\tau \right]} \quad (8b)$$

so that $k_{\rho}^{diff}(t) = k_{max}^{diff} \rho(t)$ is known at each time. Note that from Eqs.(2) and (3) one has:¹⁰

$$i(t) = nFk_{\rho}^{diff}(t) q_0 \exp\left(-\int_0^t k_{\rho}^{diff}(\tau) d\tau\right) \quad (9)$$

which shows that $i(t)$ and $k_{\rho}^{diff}(t)$ are linked by an integral equation which can be solved in either direction (direct or inverse problem) provided q_0 is known.

Figure 2Ac evidences the high precision of the spike current time-variations predicted by Eq. (9) by comparing them to the experimental recording in Fig. 2Aa (also overlaid onto the theoretical variations in Fig. 2Ac). In Fig. 2Ac is also shown the temporal dynamics of the fusion pore radius under the form of those of $k_{\rho}^{diff}(t)$ which are proportional (Eq.(4)).

Finally, let us recall that q_0 whose value is required to evaluate numerically $\rho(t)$ in Eq. (8) and $i(t)$ in Eq. (9) can be formally obtained by integrating the whole spike current taking into account that oxidation of NTs at the carbon electrode involves $2F/\text{mole}$.³¹ However, it may happen that exponential decaying branches require a large time span to reach a situation where the current becomes sufficiently closely from the zero baseline level for neglecting any error due to the non-integrated part of the tail. In practice, this may happen because the tail current has a too low signal-to-noise value at the very end of the spike, and/or because a following spike current begins before this is achieved. In both cases the experimentally integrated q_0 value would be underestimated. To overcome this problem, the exponential current tail was systematically extrapolated algebraically based on the equation of the linear fit of the spike tail in semi-log plot (see Fig 2Ab) in order to obtain a better estimation of q_0 .¹⁰ So, using Faraday's law, one obtains:

$$nFq_0 = \int_0^{\tilde{t}} i(t)dt + \frac{1}{k_{max}^{diff}} \cdot e^{-k_{max}^{diff} \tilde{t} + b} \quad (10)$$

where $\ln i(t) = (-k_{max}^{diff} t + b)$ is the equation of the linear fit of the exponential segment in semi-log plot and \tilde{t} is the last time point where $i(t)$ was measurable with a correct precision.

Model of individual exocytotic events featuring spikes with two exponential decays branches

The intravesicular matrix consists of strands of negatively charged polypeptides (from the chromogranin family) which are tightly packed through their association with the stored monoamine neurotransmitters cations,³⁵ as well as by calcium ions, ATP, protons, neuropeptides, etc.³⁶ Indeed, the presence inside of exocytotic vesicles of cations and of cationic molecules such as NTs prone to establish a dense network of hydrogen bonds with the charged chromogranin carboxylic groups, allows the whole matrix to condensate. Recent experimental works conducted by the Ewing group based on NanoSIMS investigations have demonstrated that the condensed matrices cannot always be regarded as homogeneous entities.^{15,37–39} In this context, molecular dynamics simulations have shown that truncated granin strands condense inhomogeneously, exhibiting both compacted and lacunar domains,⁴⁰ as we assumed to rationalize some of our former experimental works.^{12,13} In fact, this is in full agreement with condensed matter physics^{16,17} which predicts that the degree of condensation of polyelectrolytes similar to the granins is strongly dependent on the cation charges. Accordingly, a total condensation into a single globular entity is only possible with multivalent cations,^{41,42} and even in this case this often gives rise to splitting of the intravesicular content between a low-condensed domain named “halo” by Ewing and others and highly-condensed one named “dense core” which release their content at different rates.^{7,43,44} Oppositely, monoamine NT are monocations so their electrostatic interaction energies with granins anionic groups are not sufficient to cause such a full condensation, even taking into account the network of hydrogen bonds, due to the large generated negative entropy.^{16,17} Under such conditions the intravesicular matrix is expected to adopt a folded “pearl necklace” structure (Fig.3),^{12,13,17,45} whose “pearls” correspond to well-compacted blobs of chromogranin where the NT cations are

strongly linked to the anionic sites of the polypeptides threaded by less compacted strands in which the NT cations are less associated with the granins backbones. In fact such dual organization has been observed by molecular dynamic investigations.⁴⁰ Note that this obeys a similar physical principle to that involved for the creation of double layers in electrochemistry.

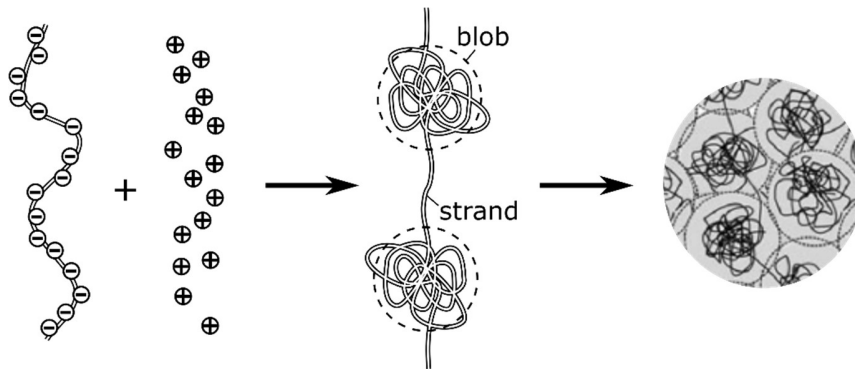


Fig.3. Schematic representation of the intravesicular structure of the secretory vesicle (the terminology “blob” vs. “strand” was introduced by de Gennes).

NT diffusion by site-hopping is still feasible in the well-compacted domains, but is considerably slower than in the less compacted areas because any local reorganization of the assembly surrounding each site is more difficult. Nonetheless, molecules initially stored in these highly-compacted compartments may exchange with adjacent vacant sites present in the less compacted ones and be ultimately released through fast site-hopping diffusion up to the entrance of the fusion pore. In first approximation, this release contribution through exchange between the two phases (i.e., from highly- to less-packed domains that are labeled in the following for simplicity as slow and fast compartment, respectively) can be described by the following kinetic scheme (see SI section C for a discussion justifying the consideration of an irreversible transfer):



where, at any given time t , q_s and q_f are the quantities of the total releasable neurotransmitter in the slow and fast compartments, respectively, regardless of the number of domains of each type. \emptyset_f , \emptyset_s represent the quantities of “NT-empty” sites in the fast and slow compartments, correspondingly. Note that here and in the following, “empty” is used for simplicity to name the chromogranin anionic sites where the NT cations have been replaced by other cations, hydrated or not, as required by electroneutrality.³ k_1 is the rate constant characterizing the global displacement of neurotransmitter quantities from slow to fast compartments (see section C in SI); $k_\rho^{diff}(t)$ is the time-dependent global rate constant controlling kinetics of the release, being defined as above for spikes with single exponential decay, i.e., it is proportional to the time dependent fusion pore radius (see Eq.(4)).

At each given time the conservation of the chromogranin anionic sites in each compartment implies that $q_s + \emptyset_s = q_s^0 + \emptyset_s^0$ and $q_f + \emptyset_f = q_f^0 + \emptyset_f^0$ where the quantities before release begins (i.e. $t = 0$) are labeled with the superscript ‘0’. Assuming that at initial times the vesicles are fully loaded, viz., that the quantities of “free” sites \emptyset_f^0 and \emptyset_s^0 are negligible vs q_f^0 and q_s^0 , the terms $(q_s^0 - q_s)$ and $(q_f^0 - q_f)$ represent the amounts of empty sites in each compartment. Taking advantage of our previous works,^{10,13} and following the same lines developed above for the single-exponential case, the release process in Eqs.(11a,b) can be formalized by the following set of non-linear ordinary differential equations:

$$\frac{dq_s}{dt} = -k_1 (q_f^0 - q_f) q_s \quad (12a)$$

$$\frac{dq_f}{dt} = k_1 (q_f^0 - q_f) q_s - k_\rho^{diff}(t) q_f \quad (12b)$$

where, again, k_1 and k_ρ^{diff} apply to the NT releasable quantities present in the slow and fast domains (note that k_1 is formally proportional to the number of slow compartments, see SI section B).

Note that summation of Eqs.(12a) and (12b) shows that the current, $i(t)$, monitored at each instant t due to NT electrooxidation at the electrode surface is equal to $nFk_\rho^{diff}(t)q_f$:

$$\frac{i(t)}{nF} = \frac{dq_{out}}{dt} = -\left(\frac{dq_s}{dt} + \frac{dq_f}{dt}\right) = k_\rho^{diff}(t)q_f \quad (12c)$$

Eqs.(12a-c) are associated to the initial conditions:

$$q_s^{t=0} = q_s^0, \quad q_f^{t=0} = q_f^0, \quad q_{out}^{t=0} = 0 \quad (12d)$$

In addition, owing to the conservation of matter one has also:

$$q_0 = q_s + q_f + q_{out} \quad \text{at any time}$$

$$q_0 = q_s^0 + q_f^0 \quad \text{at } t = 0 \quad (12e)$$

since q_0 is the total (i.e. both fast and slow compartments) releasable NT content before release occurs.

It should be noted that Eqs.(6) and (8a) remain valid for the spikes with two exponential decay provided that $q_{ves}(t)$ is replaced by $q_f(t)$, hence the fusion pore dynamics can be reconstructed exactly as was detailed above for single-exponential spikes as soon as the system (12a)-(12d) is solved.

The system in Eqs.(12a, 12b) obeys two limits depending on the time. At short times, $-\frac{dq_f}{dt} \gg -\frac{dq_s}{dt} \approx 0$ since by definition any release from the slow compartment necessarily lags behind that of the fast compartment. Hence, $q_s \approx q_s^0$ and $dq_s/dt \approx 0$ so that at initial times Eq.(12b) can be approximated by:

$$\frac{dq_{out}}{dt} = -\frac{dq_f}{dt} \approx k_{\rho}^{diff}(t)q_f \quad (13a)$$

Eq.(13a) shows that at initial times, as soon as the fusion pore radius has completed its expansion (viz., $k_{\rho}^{diff}(t) = k_{max}^{diff}$) NT release proceeds through a single exponential decay branch with a time constant $\tau_{1ex} = 1/k_{max}^{diff}$.¹⁰ In other words, up to when the slow compartments start to release significantly, the situation remains essentially identical to the case of single-exponential spikes.

Conversely, when the fast compartment is almost emptied, viz. when $q_f \ll q_f^0$ and $-\frac{dq_s}{dt} \gg -\frac{dq_f}{dt}$, the releasing rate is essentially controlled by the kinetics of transfer of NT molecules from the slow compartments into the fast one in which they can rapidly diffuse to the fusion pore. In other words, NT quantity in the fast compartment is under (quasi-)steady state, so that:

$$q_f \rightarrow \frac{k_1 q_f^0}{k_{\rho}^{diff}(t)} q_s \quad (13b)$$

Substituting Eq.(13b) into (12c) shows that at long times:

$$\frac{dq_{out}}{dt} \approx -\frac{dq_s}{dt} \approx k_1 q_f^0 q_s \quad (13c)$$

This establishes that while time elapses the kinetics of the current decay progressively shifts from a single exponential mode described by Eq.(13a) to another single exponential mode with a time

constant $\tau_{2exp} = 1/(k_1 q_f^0)$ as featured by Eq.(13c). This is in perfect agreement with the experimental observations in Fig. 2B.

To conclude this section, we want to briefly discuss two modeling options that we have not considered above. One of them was proposed by Jackson et al.⁴⁶ and amounts to considering that there exists a single NT isotropic distribution compartment whose release kinetics follows what our model attributes to the second exponential of the decay tails. Under such circumstances, the kinetic regime our model attributes to a two-step kinetic process involving a coupling between (i) the fusion pore opening phase followed by (ii) the first exponential release mode (see below sections I and II of Fig. 4b) would necessarily be replaced by a complex opening of the fusion pore involving a rapid enlargement followed by a slower shrinkage phase before reaching a constant value as obtained by Jackson et al. for vesicular release from chromaffin cells. However, we tend to favor our model firstly because it is perfectly consistent with de Gennes "blob" theory on soft matter, namely the necessary existence of an anisotropy during the condensation of polyelectrolytes by monocations as further elaborated by theoretical physics.^{16,17} Furthermore, the experimental reality of the two-phase structuring of the matrix of catecholamine vesicles cannot be disputed since it has been often observed by TEM imaging (see e.g., the following works^{11,14,47,48}) as well as their granular organization by NanoSIMS.¹⁵ Secondly, because if the mechanism of initial opening of fusion pores seems already understood,⁴⁹ that of a down-regulation of the radius of fusion pores after this phase (for example by synaptophysin-dynamin association⁵⁰) remains still to be clarified.^{49,51}

Finally, if the existence of two main storage compartments were considered in accordance with the theoretical physics of polyelectrolyte condensation, but would be released in parallel, that is to say without any kinetic coupling, such as the observation of two-exponential decay tails may

intuitively suggest, a completely different kinetic result inconsistent with the experimental data would be observed. This solution was therefore not explored in this work.

Validation of the model based on theoretically generated spikes

The above model was developed with the aim of rationalizing the existence in the first category of amperometric spikes with two-exponential tails and to extract the temporal variations of the main parameters, viz., $q_f(t)$, $q_s(t)$, and $k_\rho^{diff}(t)$, which regulate NT release for these events (see SI section A for details of the reconstruction procedure). Note that the model developed above for current spikes with two-exponential decay tails automatically includes the case of spikes exhibiting single-exponential decay branches, i.e., when k_1 or q_s^0 are negligible.¹⁰ The knowledge of q_f^0 and q_s^0 provides important information about the internal grainy structure of each analyzed vesicle while that of $k_\rho^{diff}(t)$ time variations gives a direct access to the fusion pore opening rate as well as to its maximum radius value for each analyzed experimental current spike $i(t)$.

To proceed we wish first to validate the present model by showing that it allows quantitative analyses of two-exponential spikes with a high precision. For this purpose, we relied on the analyses of simulated theoretical spikes $i^{sim}(t)$ corresponding to a series of arbitrarily selected values of k_1 , q_f^0 , q_s^0 and k_{max}^{diff} . To this aim, the time variations of $k_\rho^{diff}(t)$ were assumed to obey the formulation in Eq. (14) with:

$$k_\rho^{diff}(t) = k_{max}^{diff} \frac{(a \cdot t)^m}{1 + (a \cdot t)^m} \quad (14)$$

since some of us previously demonstrated that such adjustable sigmoid functions through variations of parameters a and m fitted extremely well fusion pores opening dynamics extracted

from experimental spikes with single-exponential decay tails.^{9,10,52}

Figure 4a represents a typical amperometric spike, $i(t)$, simulated for the electrooxidative detection of a catecholamine ($n = 2^{31}$) based on the set of Eqs.(12a-12c) for the set of k_1 , q_f^0 , q_s^0 , k_{max}^{diff} , a and m values given in its caption. The corresponding time variations of its two components, viz., $-nF(dq_f/dt)$ and $-nF(dq_s/dt)$ values, are also shown. Figure 4b displays the same data presented in semi-logarithmic plots and illustrates the time ranges (zones II and III) of the two exponential regimes predicted above. Figure 4c presents the time variations of the simulated $q_f(t)$ and $q_s(t)$ values which confirm that the unloading of the well-compacted compartments starts to be visible only when more than 50% of the initial content of the less compacted domain has been released.

Furthermore, for all cases tested as in Fig. 4a-c, the accuracy of the extraction procedure (see details in SI section A) was better than 1% so that the time variations of the extracted time variations of $i(t)$, $q_f(t)$, and $q_s(t)$ were impossible to differentiate graphically from the simulated ones. The only noticed slight discrepancy concerns the long time limit of $k_{\rho}^{diff}(t)$ as evidenced in Fig. 4d, where the k_{max}^{diff} value was ca. 2% smaller than predicted. However, such slight discrepancy in the outcome of the invert problem was expected since in zone III the NT release flux depends essentially on $(k_1 q_f^0)$ because the quantity $q_f(t)$ has almost reached its steady state value predicted by Eq. (13b). Yet, the pore time-opening function, viz., $k_{\rho}^{diff}(t)$, is perfectly reproduced in zone I and in the first part of zone II since in these zones the quantity $q_f(t)$ is still far from its steady state limit.

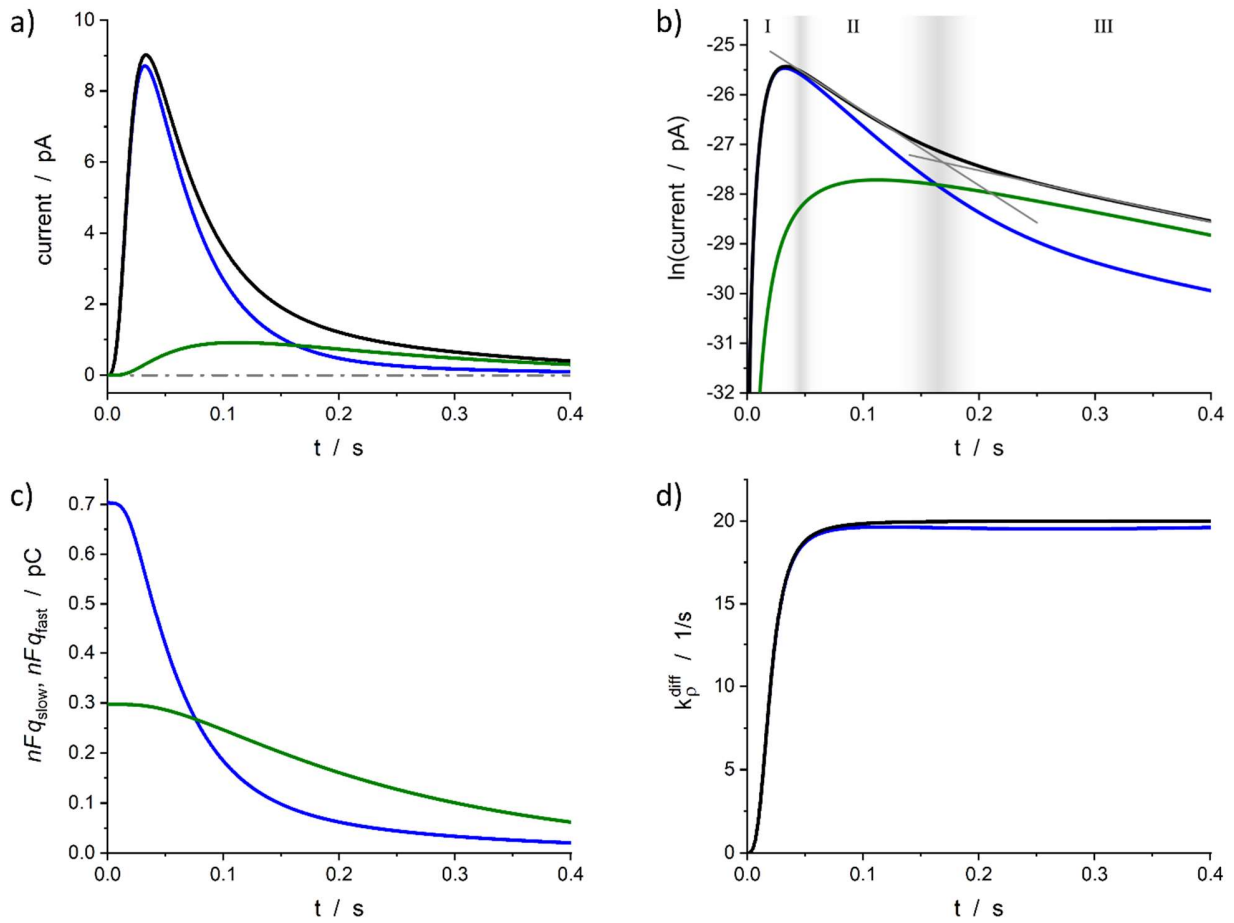


Fig.4. Simulated spike and its reconstructed components in real (a) and semi-log (b) scales. (c)

Changes in the storage of neurotransmitter in fast and slow compartments. (d) Comparison between the imposed function (14) and its reconstruction. Simulation input parameters values (see equations (12a)-(12c)): $a = 50$, $m = 3$, $Q_0 = 2Fq_0 = 1$ pC, $q_f^0/q_0 = 0.7$, $k_1q_f^0 = 5$ s⁻¹, $k_{max}^{diff} = 20$ s⁻¹; reconstructed parameters agreed within 1% except for k_{max}^{diff} value that was obtained with a -2% accuracy. Please refer to the text for a description of zones I-III in (b) and their gray gradient boundaries.

Altogether, these results validate the overall extraction procedure and demonstrate that it can be successfully applied for extracting all the parameters of interest based on the analysis of amperometric spikes with two-exponential tails. Remarkably, the fact that this relies on the solution of set of two coupled differential equations rather than on that of 3D partial derivative systems^{9,52} leads to typical execution times of 3-5 seconds per spike for each reconstruction procedure. This allows a facile and rapid analysis of individual current spikes present in amperometric traces within minutes.

Application to experimental spikes

The above section described the direct theoretical problem and, more interestingly, validated the quality of the procedure allowing the extraction of the important parameters that govern the release events giving rise to amperometric spikes with two-exponential tails. However, the second aspect was validated using simulated spikes which did not present any problem related to the presence of experimental noise although this may affect the accuracy of the reconstruction when analyzing small experimental spikes especially when their peak currents intensities are only a few times larger than the background noise. For this reason, in this section we wish to examine the accuracy of this extraction procedure when applied to real experimental spikes. To this end, we rely below on representative spikes from chromaffin or PC12 cells previously published by some of us.

Fig.5 illustrates reconstructed data for a spike measured from a single chromaffin cell.^{1,10} As can be seen the two current components (Fig.5a,b), time variations of the neurotransmitter quantities in each domain (Fig.5c) and fusion pore dynamics (Fig.5d) can be successfully reconstructed to afford values of the four main parameters: $Q_0 = 4.6$ pC, viz., $q_0 = 24$ amol, $q_f^0/q_0 = 0.71$,

$k_1 q_f^0 = 7.2 \text{ s}^{-1}$, $k_{max}^{diff} = 41 \text{ s}^{-1}$. Importantly, although the current in zone III (as defined in Fig.4b) involves a significant contribution of the background noise (compare Figures 5a and 5b), the accuracy of current measurements in the interzone II/III is sufficient to allow a full extraction of these parameters as well as the time variations of the fusion pore opening function (Fig. 5d).

Based on the value of $D_{ves}/r_{ves}^2 = 415 \text{ s}^{-1}$ determined in our previous works^{10,27} and that published for r_{ves} average value (156 nm)³² the time dependence of the fusion pore radius, $r_{pore}(t)$, was readily deduced from that of $k_{\rho}^{diff}(t)$ using Eq.(4) (see right vertical scale in Fig.5d).

Fig.6 demonstrates the reconstruction quality obtained for a typical experimental spike recorded at a single PC12 cell. Interestingly, although the spike chosen exhibits a pre-spike feature^{21,53} the extraction procedure yields excellent results (see below). The reconstructed parameters were: $Q_0 = 0.15 \text{ pC}$, viz., $q_0 = 0.78 \text{ amol}$, $q_f^0/q_0 = 0.7$, $k_{max}^{diff} = 2.2 \times 10^3 \text{ s}^{-1}$, $k_1 q_f^0 = 4.7 \times 10^2 \text{ s}^{-1}$. These results are in perfect agreement with the known smaller total vesicle content and faster rate constants for PC12 cells vs chromaffin cells.³⁰ It can be pointed out that although the spike current integrates a pre-spike feature (PSF)⁵⁴ in the time range of 0.4 to 1.5 ms, and the noise of the background current has a visible impact on the spike current measurement (see Figs.6a and 6b for $t \geq 4 \text{ ms}$), the reconstruction procedure converges extremely well over the whole current spike duration so $k_{\rho}^{diff}(t)$ and $r_{pore}(t)$ time-dependent values can be extracted including their maxima values (Fig.6d).

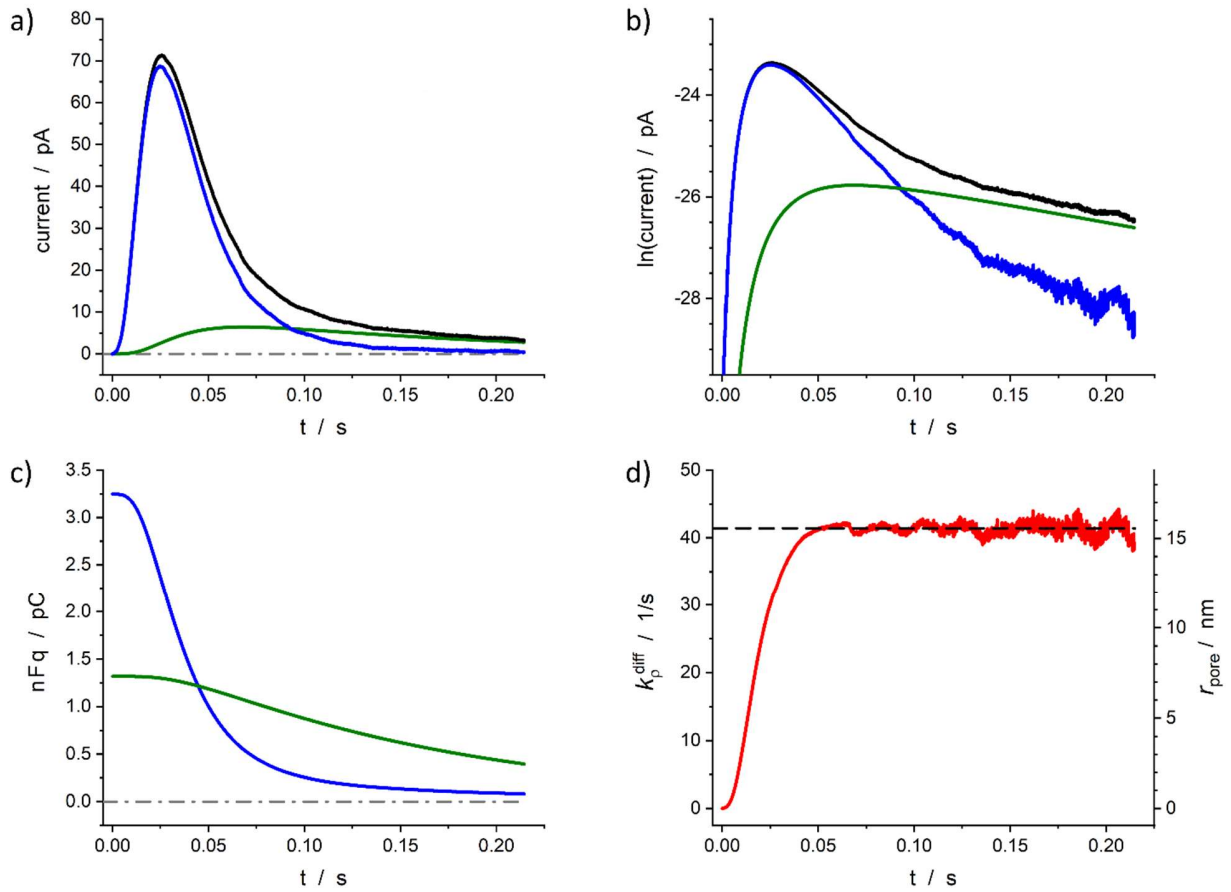


Fig.5. Quantitative analysis of a typical amperometric spike featuring adrenaline release monitored at a chromaffin cell with carbon fiber electrode (CFE). Current spike and its reconstructed compartment-wise components in linear (a) and semi-log (b) scales. Variation of NT content in each domain (c) and reconstructed fusion pore dynamics (d). The dashed line in (d) represents k_{max}^{diff} ; the right vertical axis indicates the corresponding r_{pore} values which were evaluated assuming $D_{ves}/r_{ves}^2 = 415 \text{ s}^{-1}$ ²⁷ and $r_{ves} = 156 \text{ nm}$.³²

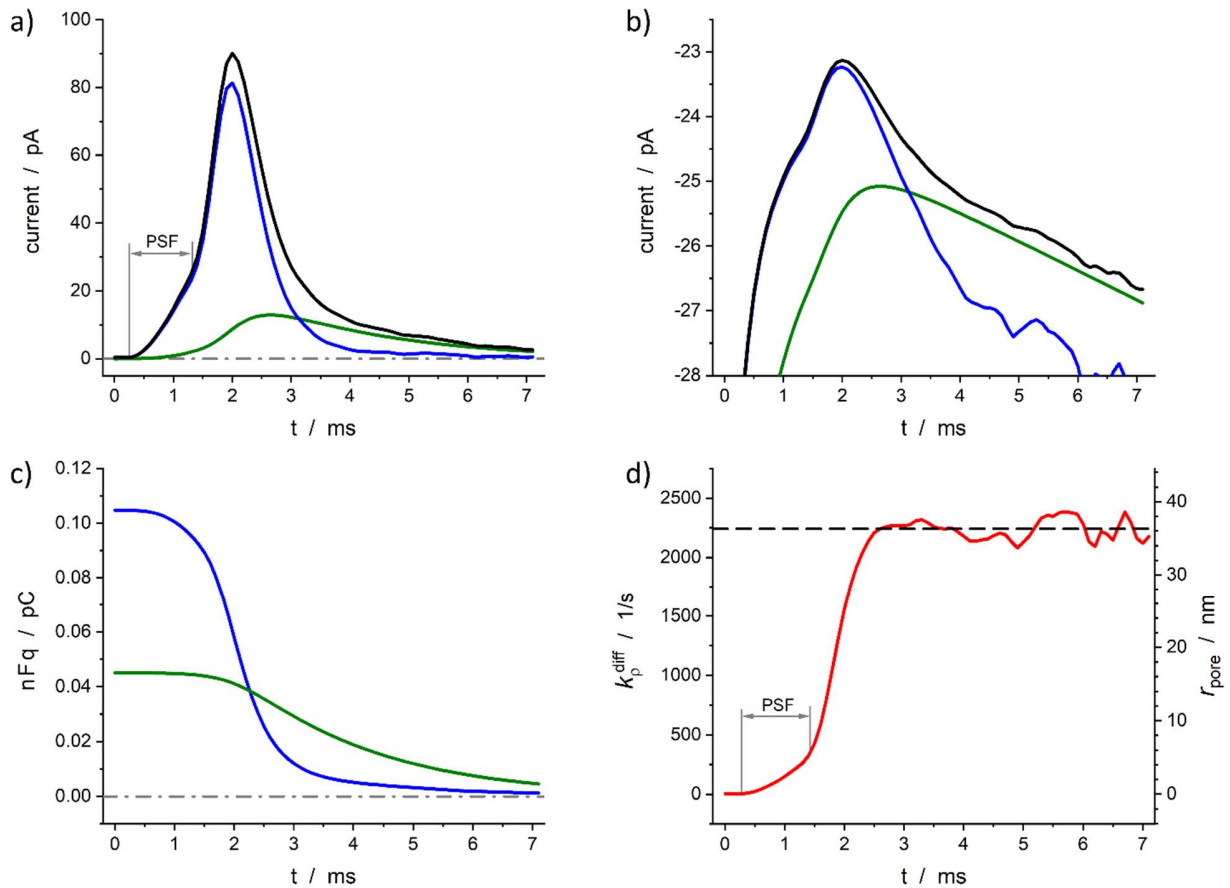


Fig.6. Quantitative analysis of a typical amperometric spike featuring dopamine release monitored at a PC12 cell with CFE. Current spike and its reconstructed compartment-wise components in linear (a) and semi-log (b) scales. Variation of NT content in each domain (c) and reconstructed opening dynamics (d). The dashed line in (d) represents k_{max}^{diff} ; the right vertical axis indicates the corresponding r_{pore} values which were evaluated assuming $D_{ves}/r_{ves}^2 = 5803 \text{ s}^{-1}$ ³³ and $r_{ves} = 94 \text{ nm}$.³³ PSF in (a) and (d) stands for “pre-spike feature”.

The typical results shown in full details in Figs. 5 and 6 validate the application of the extraction procedure to experimental amperometric spikes. In addition, Fig. 5c and 6c confirm that the

exchange between the fast and slow domains may begin only when substantial amounts (ca. 50%) of NT cations initially present in the fast domain have been released. This validates *a fortiori* the fact that the transfer of NT is considered to be irreversible (Eq.(11a)) in our model. To conclude, it must be emphasized that the present model makes it possible for the first time to quickly analyze all amperometric spikes of the first category within a time interval (a few seconds) compatible with the analysis of complete amperometric traces containing hundreds of peaks or more. This model is fundamentally based on the coexistence and kinetic interaction of two types of intravesicular domains. This central hypothesis is not only in agreement with the physicochemical behavior predicted for the condensation of polyelectrolytes similar to chromogranins^{16,17,35,36} but has recently received experimental support from the nanoSIMS experiments reported by Ewing's group.¹⁵

Quantitative kinetic analysis of a full amperometric trace data

The ca. 3-minute long amperometric trace recorded from a single PC12 cell shown in Fig.1¹² contains 106 analyzable spikes of the first category (i.e. 84% of all individual events), of which 97 spikes had two-exponential tails and a very few ones (9) with single-exponential tails. One may be surprised by the very large proportion of spikes with two-exponential tails, but as will be clear in what follows, several of these would have appeared upon visual inspection to display single-exponential tails because their second exponential component was comparatively faint and would have been dismissed without plotting them in semi-logarithmic scales (compare Fig. 2). For this reason, considering that such situation may happen often unnoticed, all peaks of the first category were analyzed by the present procedure and their parameters extracted without any distinction.

Table 1 summarizes the results of this analysis for PC12 spikes¹² with two-exponential decay tails, namely those whose analysis yielded $q_f^0 > q_s^0$ and $k_1 q_f^0 < k_{max}^{diff}$ within the precision of the determinations. The values in Table 1 are the median values of the reconstructed parameters for the 97 analyzed spikes with two-exponential tails whose distributions obeys log-normal statistics (see plots in Fig. 7). The total released amount of neurotransmitter q_0 given in the Table 1 is somewhat higher than those reported in the literature for PC12 cells³⁰ but fully agrees with our previous report.¹²

Table 1. Median values of the parameters characterizing all the 97 current spikes belonging to the first category and exhibiting two-exponential tails present in the experimental amperometric trace shown in Fig.1b recorded at a single PC12 cell.¹² Values shown between parentheses correspond to the first and third quartiles.

Q_0 / pC	q_0 ^(a) / amol	q_f^0/q_0	q_s^0/q_0	k_{max}^{diff} / s^{-1}	$k_1 q_f^0 / s^{-1}$
0.10	0.52	0.81	0.19	720	180
(0.07; 0.16)	(0.35; 0.81)	(0.76; 0.86)	(0.14; 0.24)	(510; 1100)	(110; 280)

(a) median total releasable amount of transmitter per vesicle. q_0 is computed from Q_0 using Faraday law $Q_0[\text{pC}] = 10^{-6} \times nFq_0[\text{amol}]$, with $n = 2$,³¹ $F = 96485.33 \text{ C/mol}$.

Concerning the quantities q_0 , q_f^0 and q_s^0 shown in Table 1 is important to recall that they represent the median amounts of neurotransmitter released during spontaneous exocytotic events and not at all the total quantities stored in the vesicles before exocytosis occurs. Indeed, as release proceeds,

the NT partition coefficient from the intravesicular matrix to the cell-electrode gap environment, $P_{ves \rightarrow gap}^{NT}$, must necessarily decrease to keep the vesicle integrity. On the one hand, $P_{ves \rightarrow gap}^{NT}$ is initially very large to account for the extremely high initial values of intravesicular NT concentration.^{2,4,28,55,56} On the other hand, as the release progresses, the matrix/NT assembly is continually losing its initial structure due to the replacement of the NT cations by hydrated extracellular cations.³ The ensuing increase in the internal pressure of the vesicle necessarily causes a thermodynamic destabilization of the intravesicular matrix structure which should ultimately lead to its swelling^{41,55} as soon as it can no longer be compensated by the increase of the surface tension of the vesicular membrane.⁵⁷⁻⁵⁹ Therefore, in order to avoid possible membrane rupture or a complete fusion,^{28,60} the excess internal energy must be dissipated provoking a decrease of $P_{ves \rightarrow gap}^{NT}$ while release proceeds with the consequence that release will stop before all initially stored NT quantities have been released. Note the release may stop before this situation is reached if the fusion pore closes although this seems quite rare except for intrasynaptic release.^{5,6,61} Consequently, to satisfy the intravesicular thermodynamics and maintain the vesicular structural integrity, a significant amount of NT remains inside the vesicle as already shown at several instances which evidenced that ca. 40 to 60% of the stored molecules remained stored inside vesicles at the end of release.^{6,14,44,55,62,63}

The values in Table 1 need to be compared to those of q_0 (0.27 amol) and k_{max}^{diff} (570 s^{-1}) obtained for the 9 spikes exhibiting a single-exponential tail. Interestingly, upon assuming an identical NT concentration in both cases this population corresponds to vesicles with volumes being ca. half those of vesicles giving rise to a double-exponential behavior. This suggests that in order to structure into slow and fast domains the vesicles need to be sufficiently large. Hence, below a threshold size a single compartment is formed with structural properties lying presumably in

between those of the fully compact and less compact domains. This is in full agreement with the fact that the value k_{max}^{diff} (570 s^{-1}) for vesicles giving rise to spikes with single-exponential tails is less than that (720 s^{-1}) determined for those leading to double-exponential release tails.

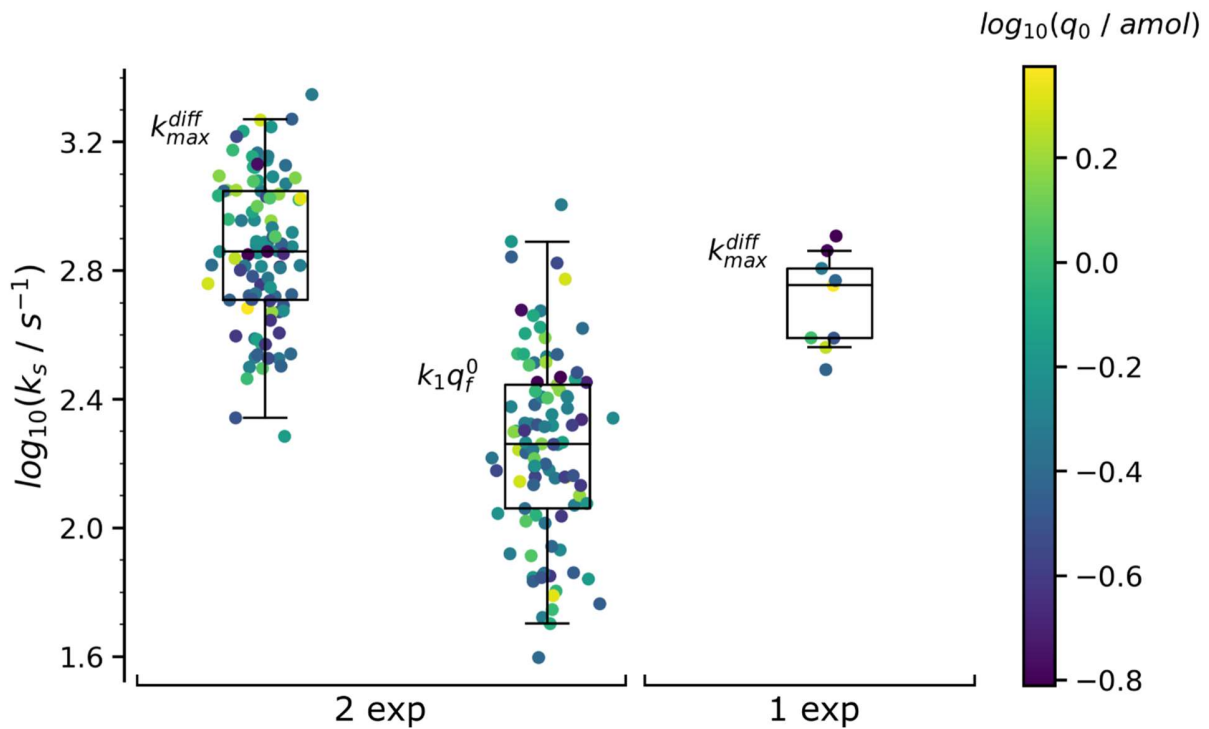


Fig. 7. Box and whisker plots of the reconstructed k_{max}^{diff} and $k_1 q_f^0$ values for the 97 spikes with two exponential decay and k_{max}^{diff} for the 9 spikes with single exponential decay (spikes from the trace in Fig.1b). The color of each dot refers to the reconstructed releasable content of a vesicle q_0 (in amol) as indicated by the color bar on the side. The different horizontal segments in each box and whisker plot represent, from top to bottom, the upper extreme (90%), upper quartile (75%), median (50%), lower quartile (25%) and lower extreme (10%) probabilities.

The distributions of the values reconstructed from spikes with one and two exponential decays as well as their statistics are plotted in Fig.7. The color of each marker refers to the scale of the

releasable NT content determined for the same vesicle, q_0 , shown on the right of the box and whisker plots. It is noted that the sampling time (0.1 ms^{12}) used to record the amperometric trace in Fig. 1b was sufficiently small to record with sufficient accuracy the decay tails of all spikes including those with the largest k_{max}^{diff} values (ca. $2.2 \cdot 10^3 \text{ s}^{-1}$). On the other hand, the mean time separation between two successive spikes of each group of K^+ -elicited events was sufficiently wide (ca. 300 ms^{12}) to allow recording the whole decay tail of each current spike even those with the largest time constants (ca. 30 ms). Hence the only possible experimental limitation which defined the set of 106 analyzed spikes was due to the background noise limit (0.3 pA^{12}) with the smallest peak intensity (ca. $5\text{-}7 \text{ pA}$) but that was taken care of by the extrapolation of the current tails which was used in evaluating q_0 by Eq. (10) (compare the outcome in Figs. 5 and 6). It may then be safely concluded that the distributions of k_{max}^{diff} and $k_1 q_f^0$ values are not limited by the experimental recording of the amperometric traces and that they reflect biological properties characterizing each exocytotic event.

Figure 8a suggests the existence of a correlation between the pairs of values k_{max}^{diff} and $k_1 q_f^0$ determined for each of the 97 amperometric peaks presenting two exponential tails recorded in the trace shown in Figure 1b. (note that $k_{max}^{diff} > k_1 q_f^0$ by definition so all datapoints lie below the first bisector shown by the dashed line). Figure 9 (top) provides a quantitative confirmation of the correlation suggested in Fig. 8a by displaying a cumulative projection of all datapoints onto the axis perpendicular to the bisector (as shown by the black arrow in Fig. 8a). This projection gives strength to the correlation in Fig. 8a since it evidences that almost all datapoints fall within a relatively narrow interval centered around the relationship $k_1 q_f^0 \approx 0.25 k_{max}^{diff}$. Moreover, it is noted that using a different experimental approach, Ewing et al.²¹ also hinted to the existence of a

biologically-based relationship between two time constants that they used to characterize spikes decay tails in their investigation and which are somewhat related to $1/k_{max}^{diff}$ and $1/(k_1q_f^0)$. So let's examine the logic behind this correlation to recognize its biological significance, if any.

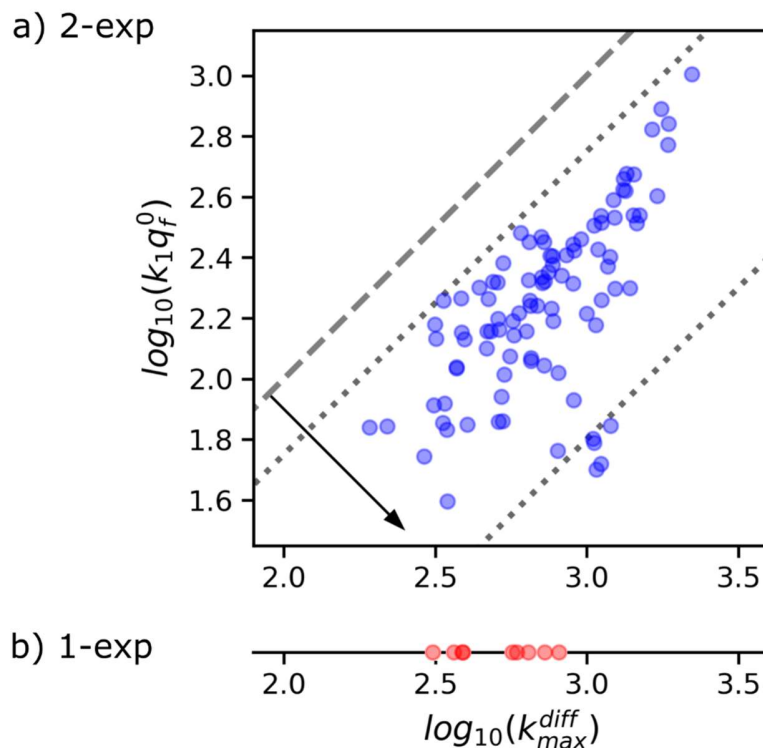


Fig.8. (a) Correlation between k_{max}^{diff} and $k_1q_f^0$ values characterizing each of the 97 spikes exhibiting two-exponential tails analyzed from the amperometric trace in Fig. 1b. These are put in perspective with the k_{max}^{diff} values (b) determined for the 9 spikes displaying a single-exponential tail recorded in the same amperometric trace. Slanted dotted lines delimit the region in which the spikes with two exponential tails may be quantitatively analyzed owing to the experimental constraints (see text and Fig 9).

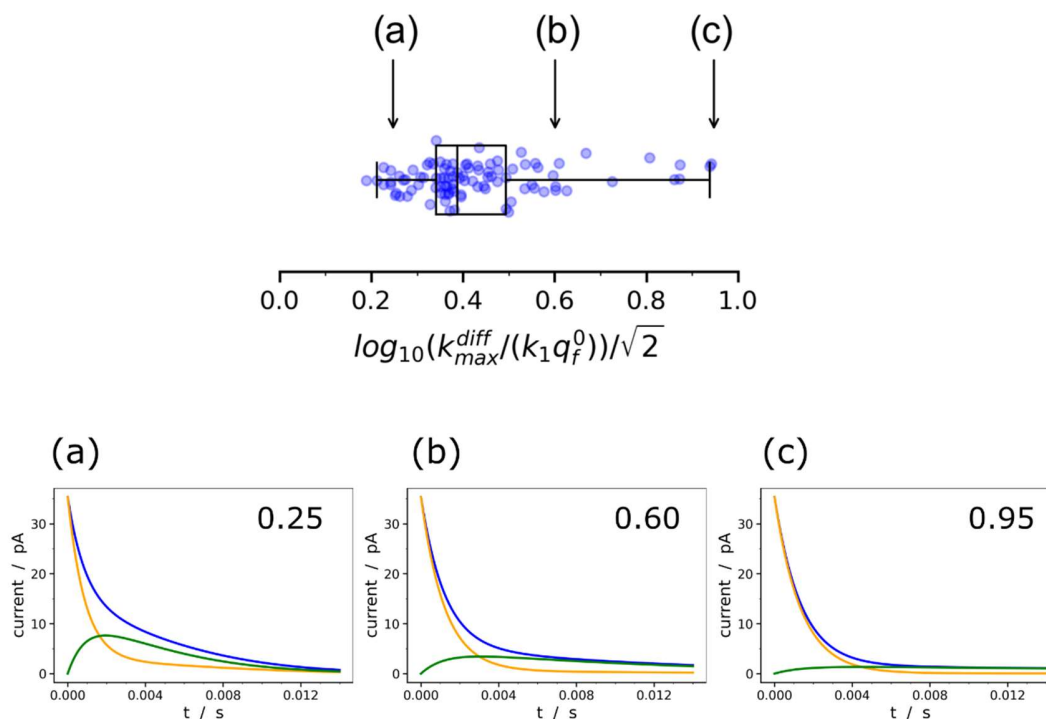


Fig. 9. Box and whisker plot together with the underlying distribution of the projections of the data points shown in Fig.8a onto an axis perpendicular to the line with a unit slope (black arrow in Fig.8a). The whiskers correspond to 1 and 99 percentiles. The total currents and its components are simulated for $\log_{10}(k_{max}^{diff}/(k_1q_f^0))/\sqrt{2}$ values shown in the sub-plots (a-c) as well as in box and whisker plot, for more details see text. Simulations in (a-c) were performed by imposing an instant fusion pore opening at $t = 0$ s in order to emphasize the effect of the intravesicular kinetics on the tail shapes.

It is important to recall in this respect that in order to extract both values of k_{max}^{diff} and $k_1q_f^0$ from a single amperometric spike, its decay tail must display clear components of the first and second

exponential behaviors or at least a recognizable kinetic mixture of these allowing their deconvolution with sufficient precision. However, such deconvolution process may be hampered at short time by a mixing of the fusion pore opening kinetics with the first exponential decay mode (compare Figs 4a, b). Since the opening dynamics of the fusion pores being a priori unknown, the recording of a sufficient time trace linked to the first exponential mode is necessary. On the other hand, at large times, the second exponential behavior must give rise to a current flow large enough to be identified with sufficient precision from the background noise (compare Figs. 2Ba,b). This is easily understood by examining the decay tails shown in Figs.9a-c which were simulated using the following parameters: $q_0 = 0.52$ amol, $q_s^0 = q_f^0 = q_0/2$, $\log_{10}(k_{max}^{diff}/s^{-1}) = 2.85$ (i.e. $k_{max}^{diff} = 710$ s⁻¹, see Table 1), for three different values of $\log_{10}(k_1 q_f^0/s^{-1}) = 2.5, 2.0, 1.5$ (i.e. $k_1 q_f^0 = 316, 100, 32$ s⁻¹) corresponding to the markers (a-c) shown in Fig. 9 (top) and assuming that the fusion pore opened instantly at $t = 0$ (assuming the same values as above, i.e., $D_{ves}/r_{ves}^2 = 5.8 \times 10^3$ s⁻¹,³³ $r_{ves} = 95$ nm;³³ note that the radius of the instantly opened pore deduced from k_{max}^{diff} is then $r_{pore}^{max} = 11$ nm). This series of simulated current spikes shows that to extract both k_{max}^{diff} and $k_1 q_f^0$ values from a single amperometric decay tail, these values must necessarily be commensurable. This is precisely what is observed experimentally in Figs. 8 and 9. Moreover, the current trace in Fig. 9a would evidently be strongly altered at short times by the fusion pore opening kinetics (compare Fig. 4a,b) so only $(k_1 q_f^0)$ would be accessible. Likewise, the second exponential mode in Fig. 9c would be difficult to analyze due to the background noise (compare Figs. 2B), so only k_{max}^{diff} may be measurable.

This analysis actually requires that data points featuring all measurable $|k_{max}^{diff}, k_1 q_f^0|$ pairs must fall within the area delimited by the two dotted lines parallel to the first bisector drawn in Figure

8a as observed experimentally. It is therefore impossible to conclude with certainty whether this correlation has a biological significance or whether it is simply an artifact linked to the experimental impossibility of measuring datapoints located outside this area. However, given that less than 10% of the current spikes exhibited mono-exponential behavior while the remaining 90% could be analyzed with high accuracy in the double-exponential mode predicted by our theoretical model, we are inclined to consider this correlation as having a biological importance.

Conclusion

In this work, a novel theoretical model was proposed to take into account and analyze amperometric spikes corresponding to unique vesicular exocytotic events comprising decay tails obeying two exponential modes, which represent one of the main types of spikes. This model is based on an original concept according to which vesicular release involves a simultaneous exchange of the neurotransmitter between two types of intravesicular domains whose formation arises from the entropic constraints of condensation of polyelectrolytes by mono-charged ions such as most neurotransmitters.

The predictive value of the present model and its importance in solving the inverse problem – namely the quantitative deconvolution of key physicochemical factors that determine the shape of amperometric spikes – have been carefully validated using theoretical and experimental data taken from our published work. This made it possible to design a robust automatic computational procedure to extract extremely rapidly the values of the main kinetic parameters that govern the release as well as the final fusion pore size and opening kinetics from the most common experimental amperometric spikes featuring single exocytotic release events from large amperometric datasets.

The present theoretical and computational framework can be formally generalized to the case of vesicular matrices containing more than the two condensed domains considered in this study, namely either “fully condensed” or “weakly condensed”. Indeed, even if the results of molecular dynamics simulations suggest that this is a simple but rather good description, formally there may exist a gradient of “more and more condensed” domains leading to amperometric spikes with more than two exponential decay tails. The corresponding amperometric spikes would then be analyzed through simple extensions of the current model, provided that their decay tail components could be deconvolved. However, this will be limited by the accuracy of the spike current numerical recordings and the relative amount of background noise, as has been highlighted here.

Data availability section

This work is entirely theoretical and devoted to the analyses of previously published experimental data by some of us, as indicated whenever needed. We can confirm that no new experimental data was generated during this study. The only data gathered as the outcome of our theory is the set of statistical values reported in Table 1.

Conflict of interest

The authors declare no conflict of interest.

Authors contribution:

R.D. – Investigation (theoretical), Software, Formal Analysis; R.H. – Investigation (experimental); L.H. – Investigation (experimental); Z.Q.T. – Funding acquisition, Supervision; I.S. – Formal

Analysis; W.H.H. – Funding acquisition, Supervision; C.A. – Conceptualization, Supervision, Writing – review & editing; A.O. – Conceptualization, Funding acquisition, Supervision, Software, Writing – review & editing.

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Vesicular Neurotransmitters Exocytosis Monitored by Amperometry: Theoretical Quantitative Links Between Experimental Current Spikes Shapes and Intravesicular Structures.

Supporting Information

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Content:

- A. Extraction procedure of the main parameters shown in Table 1.
- B. Distribution of k_1 values.
- C. General case of reversible exchange between intravesicular domains.

A. Extraction procedure of the main parameters shown in Table 1.

The main objectives of this work were: (i) to propose a realistic model accounting for the existence of amperometric spikes displaying one or two exponential decay tails; (ii) to use this model to extract the parameters which govern the shape and intensity of the current of each amperometric spike (see Table 1). Point (i) has been described in detail in the main text, so this section is devoted to describe the principle of the computation procedure developed to answer point (ii).

The script performing the extraction procedure described in the main text and hereafter was implemented in Python 3.8 and ran in Spyder 5.5. The script implementing the extraction procedure developed here and illustrated in section A of Supporting Information is available from the authors on reasonable request.

A.1. Theoretical framework

As follows from our previous work¹ and the discussion in the main text the function $k_{\rho}^{diff}(t)$, is very important in shaping the monitored spikes. For single exponential spikes these functions reach their plateaus rather quickly after the spike peak, a mandatory behavior for the observation of one exponential spikes.¹⁻³ However, as was discussed in the main text, during the second mode of a two-exponential spike the kinetics of release is essentially governed by $k_1 q_f^0$. This means that the fusion pore size does not contribute directly in sustaining the spike current time variations during this second mode of release. For simplicity it is thus assumed that the pore keeps its maximal size that it achieved at the end of the first exponential mode (see main text). Note that would the pore close during this phase this would lead to a sudden and easily observable decrease of the current as reported in a few instances by Ewing et al.⁴

This allows to formalize the extraction procedure as the optimization problem defined by:

$$\min_{q_0, q_f^0, k_1} \Phi \quad (\text{A.1})$$

$$\Phi = \frac{1}{k_\rho^{diff,av^2}} \int_{t_{1exp}^{start}}^{t_{2exp}^{fin}} (k_\rho^{diff}(\tau) - k_\rho^{diff,av})^2 d\tau$$

subject to:

$$q_0, q_f^0, k_1 > 0, q_0 \geq q_f^0$$

where Φ is the objective function indicating deviation of $k_\rho^{diff}(t)$ from its average value $k_\rho^{diff,av}$ during the time range of the first and second exponential regimes:

$$k_\rho^{diff,av} = \frac{1}{t_{2exp}^{fin} - t_{1exp}^{start}} \int_{t_{1exp}^{start}}^{t_{2exp}^{fin}} k_\rho^{diff}(\tau) d\tau$$

where t_{1ex}^{start} and t_{2exp}^{fin} are the times reflecting beginning of the first and end of the second exponential regimes, correspondingly. It should be noted that we found the average value $k_\rho^{diff,av}$ worked well for most of the cases. However, for some noisy spikes an average value was too sensitive to some too large or too small values imposed by noise. In that cases (and in general) using a median value instead of average one provided very good results since it is more robust with respect to outliers.

A.2. Numerical details of the procedure

A.2.1. Algorithm

The Nelder-Mead method was used to solve the optimization problem given above. In order to start optimization procedure, one has to supply initial approximations of the unknown parameters as detailed in the left branch in algorithm shown in Fig.A1.

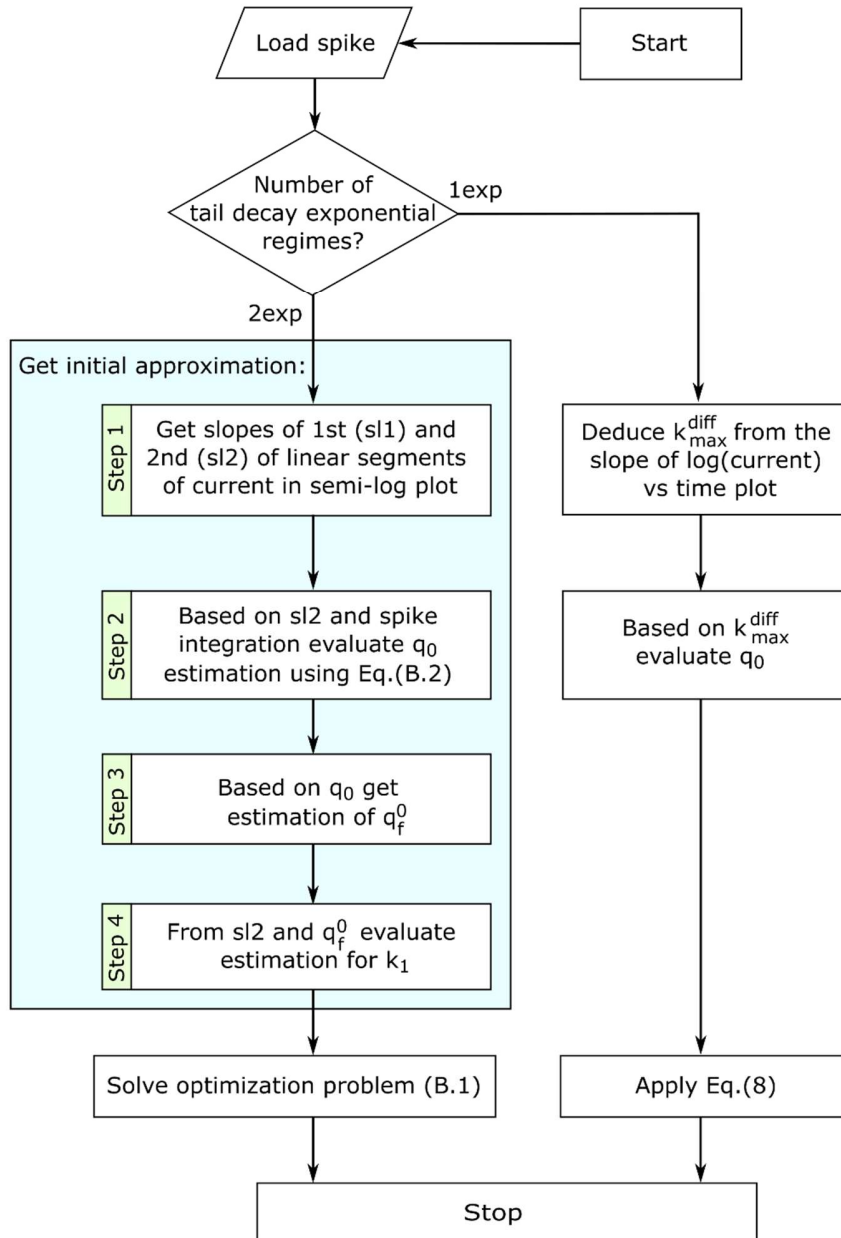


Fig.A1. Algorithm for parameter evaluation required for quantitative treatment of one- and two-exponential spikes with procedures developed here and in previous work.¹

A.2.2. Description of the steps in the algorithm in Fig.A1 for the two-exponential problem

Step 1. The ranges of the first and second exponential regimes were automatically identified. For this the derivative of the spike was obtained and the width of the minimum well at the level of 75% of its amplitude $[t_{1ex}^{st}, t_{1exp}^{fin}]$ was selected as a duration of the first exponential regime (see Fig.A2). The slope sl_1 was then evaluated from the linear regression of the spike in this range. In principle, the boundaries of the second exponential range can be defined from the signal derivative. However, practically this part is generally saturated with a noise which is amplified even more by differentiation. Thus, we used an alternative approach by performing continuation of the first exponent and noting where it drops to negligible level (ca. 1% of the spike peak) allows to obtain beginning of the second exponential regime, t_{2exp}^{st} (Fig.A2a,b). A t_{2exp}^{fin} value was then defined as

$$t_{2exp}^{fin} = t_{2exp}^{st} + 0.8 \cdot (t_{spike} - t_{2exp}^{st})$$

where t_{spike} is the duration of the spike, in order to reduce the influence of the noise generally encountered at the very end of the signal. The sl_2 value was then computed from a linear regression of the spike at the $[t_{2exp}^{st}, t_{2exp}^{fin}]$ range.

Step 2. Knowing sl_2 value Q_0 was evaluated by using exponential continuation of the spike as it was done for single exponential spikes, but now applied to a second exponential regime.

$$\begin{aligned} Q_0 &= \int_0^\infty i(t) dt = \int_0^{t_{spike}} i(t) dt + \int_{t_{spike}}^\infty i(t) dt = \\ &= \int_0^{t_{spike}} i(t) dt + \frac{1}{sl_2} \cdot e^{-sl_2 t_{spike} + b_2} = nFq_0 \end{aligned} \quad (A.2)$$

where $(-sl_2 t_{spike} + b_2)$ is the equation of the linear fit of second exponential segment in semi-log plot. Thus, initial approximation for q_0 is obtained.

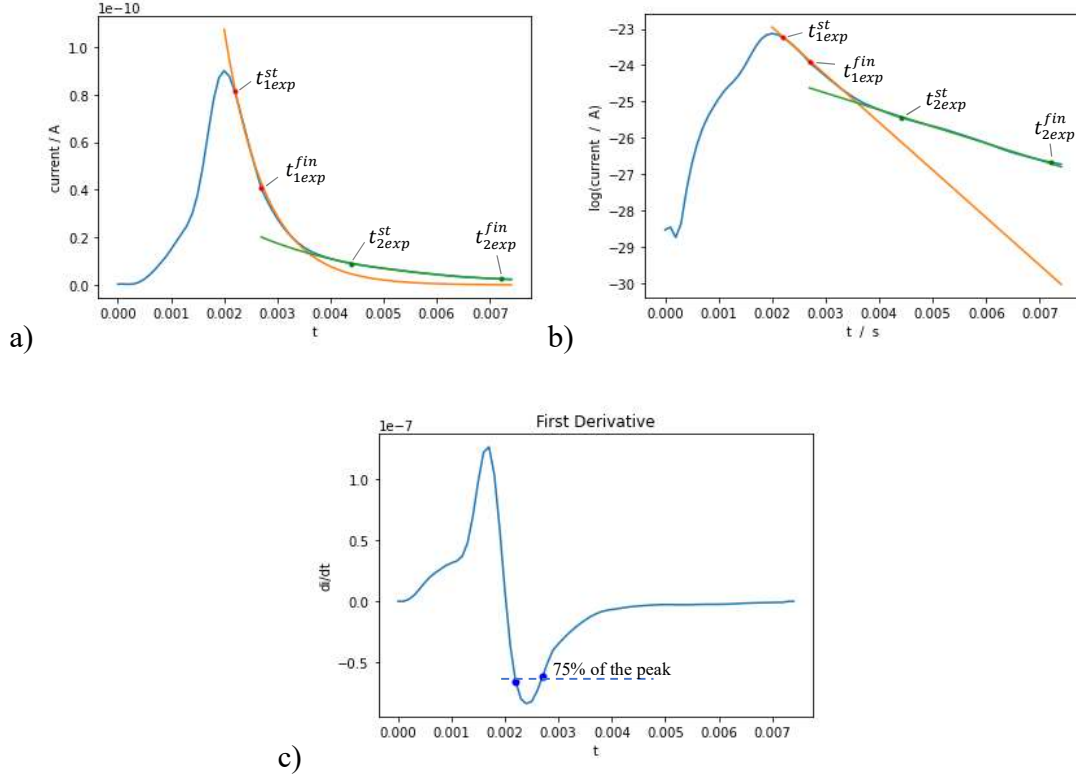


Fig.A2. Automatic determination of the first and second exponential regimes ranges. (a) Current spike; (b) current spike in a semi-log scale; (c) the first derivative of the current.

Step 3. Initial approximation for q_f^0 can then be set based on q_0 value, e.g. $q_f^0 = a \times q_0$, where $a < 1$ and whose value may depend on a dataset to be analyzed.

Step 4. As discussed in the main text the asymptotic value for the slope during second exponential regime in a semi-log plot is $sl_2 = k_1 q_f^0$, hence, initial value of the parameter k_1 was set as $k_1 = -sl_2/q_f^0$.

For making the extraction procedure more robust with respect to experimental noise inevitably present in the analyzed signal, we used in step 3 a set of initial approximations for q_f^0 (and hence of k_1 in step 4 which is evaluated from q_f^0) in the range $0.4q_0 - 0.85q_0$ with the step of $0.05q_0$. Optimization procedure was repeated for each of the set of initial approximations and the outcome with the smallest Φ value was then selected.

It worth to note that the last term in Eq.(12b), i.e. $k_\rho^{diff}(t) q_f$, is the flux of the neurotransmitter flowing through the vesicle pore (see definition in Eq.(12c)). Hence for the reconstruction procedure one may substitute experimental current directly into Eq.(12b) removing the necessity of providing unknown function $k_\rho^{diff}(t)$.

A.2.3. Schematics representation of the procedures for analysis of one- and two-exponential spikes

The essence of the one- and two-exponential spike procedures corresponding to the algorithm are shown below in Figs.A3 and A4.

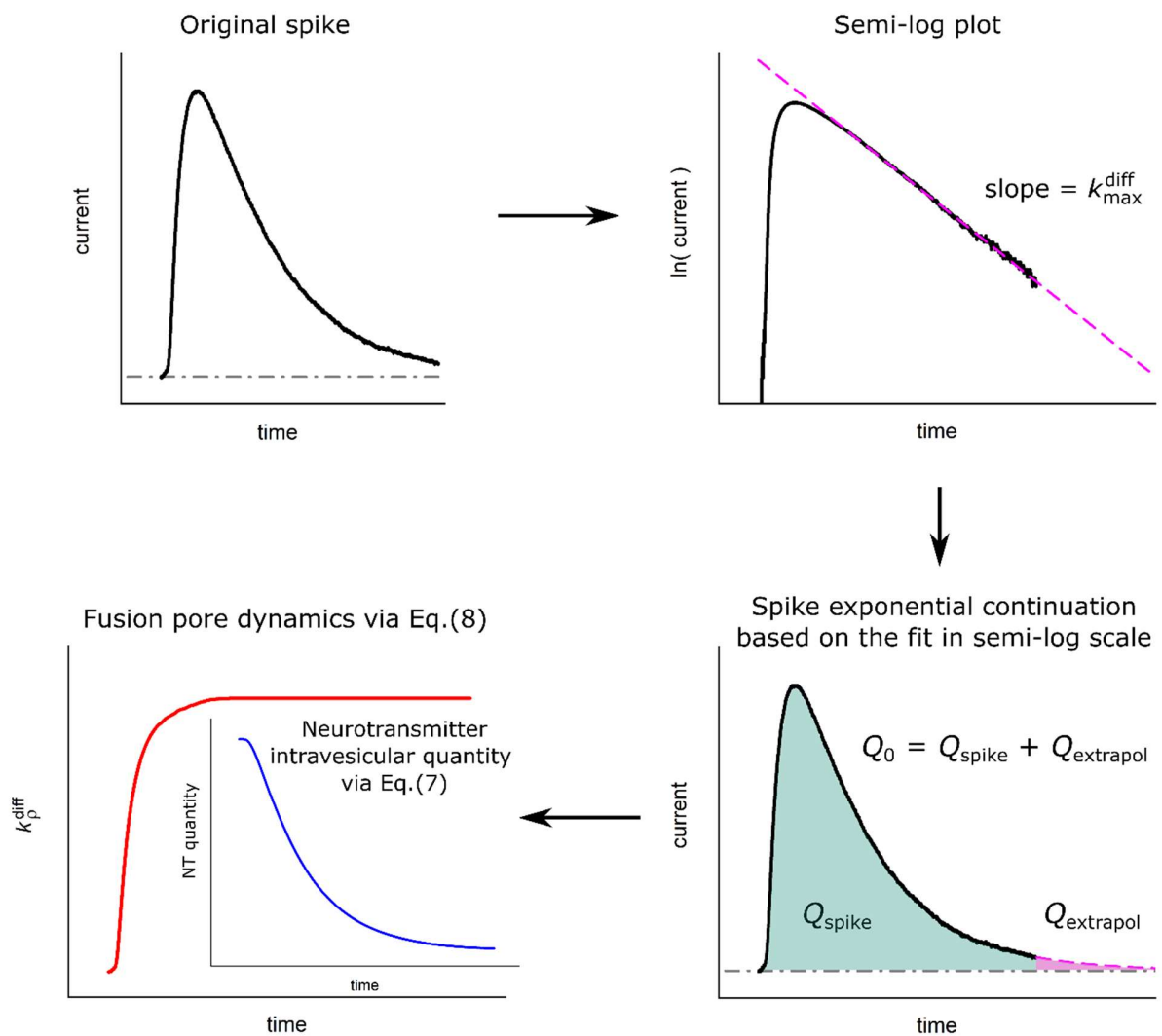


Fig.A3. Schematic depiction of the procedure used to analyze the spikes with one-exponential decay tail.

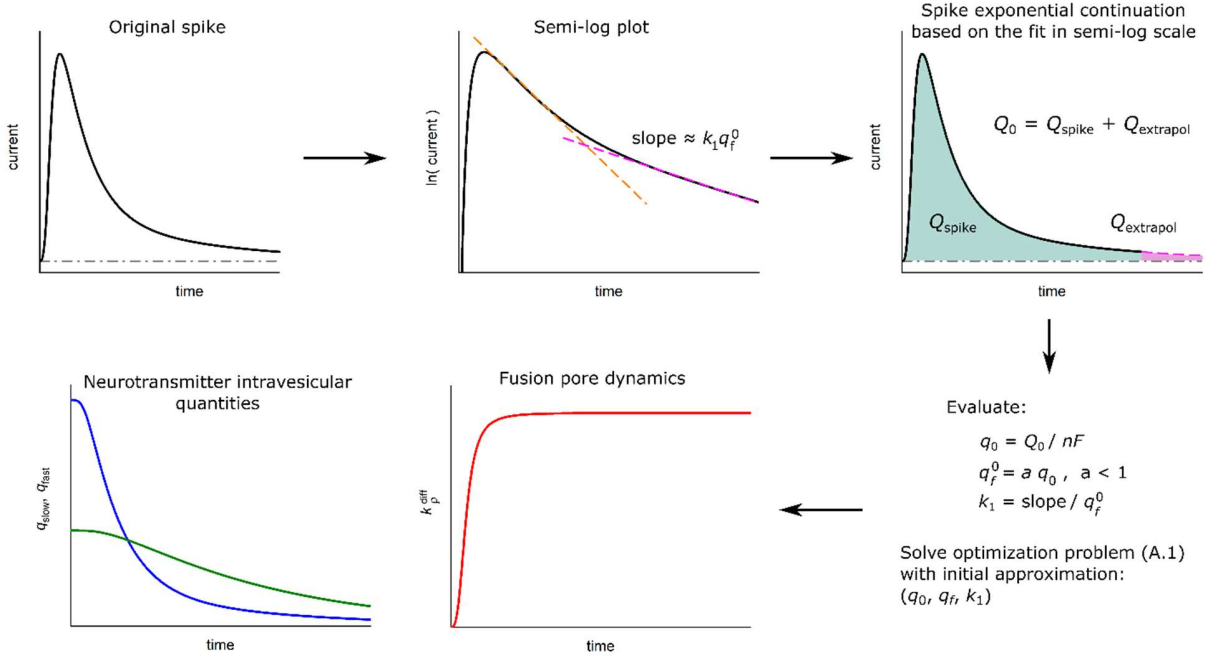


Fig.A4. Schematic depiction of the procedure used to analyze the spikes with two-exponential decay tail.

B. Distribution of k_1 values

The volumes of the highly compacted domains are imposed by local competition between free energy and entropic factors,⁵ so they should not vary drastically since the ionic composition of the intravesicular loaded matrices is assumed to be roughly constant. Evaluating analytically their mean volume, $V_{compact}$, hence their number, $N_{compact}$, as may be performed in the conceptually analogous problem of the Debye sphere for colloidal dispersions seems almost impossible except by ad-hoc extended molecular level approaches⁶ because of the length and conformation of the chromogranins and the involvement of ionic and non-ionic interactions such as hydrogen bonds. Nonetheless, as a first approximation $V_{compact}$ can be considered as a constant.

On the other hand, for each of these domains the rate constant of interfacial exchange with the surrounding less compacted compartment has to scale with the domains surface, viz., be proportional to $V_{compact}^{2/3}$. Therefore, k_1 as defined in the main text in Eq.(11a) has to be proportional to $N_{compact} \times V_{compact}^{2/3}$, so within this framework one expects that the distribution of k_1 values represents that of $N_{compact}$.

C. General case of reversible exchange between intravesicular domains

As discussed in the text the exchange between the two compartments in general is reversible and prior to the onset of the release (i.e. formation of an initial fusion pore) the exchange between two compartments is necessarily in dynamic equilibrium, but is progressively displaced while the less compacted compartment NT content is released. Hence the exchange between the two phases and extracellular environment in Eqs.(11a,b) is thus replaced by the following kinetic scheme



where all notations keep their meaning as in the main text and k_2 is the rate constant characterizing reverse exchange from fast to slow compartments. Note that since the interactions between the NT cations and the polyelectrolyte are much stronger in the slow compartment than in the fast one, k_1 features an up-hill reaction while k_2 features down-hill step of the same reaction, hence $k_1 \ll k_2$. In addition, before release one has necessarily $\emptyset_f^0/\emptyset_s^0 = (k_2/k_1) \times (q_f^0/q_s^0)$ in mature vesicles, so

the relatively small amounts of empty sites in the fast and slow compartments are thermodynamically linked to that of NT quantities in each domain.

Within the same framework and assumptions the governing system of differential equations will take the following view:

$$\frac{dq_s}{dt} = -k_1 (q_f^0 - q_f)q_s + k_2 (q_s^0 - q_s)q_f \quad (\text{C.2})$$

$$\frac{dq_f}{dt} = k_1 (q_f^0 - q_f)q_s - k_2 (q_s^0 - q_s)q_f - k_\rho^{diff}(t)q_f \quad (\text{C.3})$$

$$\frac{dq_{out}}{dt} = \frac{i(t)}{nF} = -\left(\frac{dq_s}{dt} + \frac{dq_f}{dt}\right) = k_\rho^{diff}(t)q_f \quad (\text{C.4})$$

associated to the same initial conditions:

$$q_s^{t=0} = q_s^0, \quad q_f^{t=0} = q_f^0, \quad q_{out}^{t=0} = 0 \quad (\text{C.5})$$

Similarly, to the case considered in the main text the system (C.2, C.3) has two limits depending on the time. At short times, $-\frac{dq_f}{dt} \gg -\frac{dq_s}{dt} \approx 0$ and $q_s \approx q_s^0$ and $dq_s/dt \approx 0$ thus, the same limit is attained as in Eq.(13a) in the main text:

$$\frac{dq_{out}}{dt} = -\frac{dq_f}{dt} \approx k_\rho^{diff}(t)q_f \quad (\text{C.6})$$

and the same time constant $\tau_1 = 1/k_{max}^{diff}$ controls the release during first exponential regime.

Conversely, when the fast compartment is almost emptied, viz. when $q_f \ll q_f^0$ and $q_s^0 \gg q_s$, release is essentially commanded kinetically by the transfer of NT molecules from the slow compartment into the fast one in which they rapidly exit the vesicle through the fusion pore. In other words, NT quantity in the fast compartment is under steady state, so that:

$$q_f \rightarrow \frac{k_1 q_f^0}{[k_2 q_s^0 + k_\rho^{diff}(t)]} q_s \quad (C.7)$$

Hence the current at long times:

$$\frac{i(t)}{nF} = \frac{dq_{out}}{dt} \approx -\frac{dq_s}{dt} \approx \frac{k_1 q_f^0 k_\rho^{diff}(t)}{[k_2 q_s^0 + k_\rho^{diff}(t)]} q_s \quad (C.8)$$

controlled by the following time constant $\tau_2 = [k_2 q_s^0 + k_{max}^{diff}]/(k_1 q_f^0 k_{max}^{diff})$. Equation (C.7),

hence also Eq. (C.8), admits two limits depending on the relative magnitude of $k_2 q_s^0$ vs. $k_\rho^{diff}(t)$.

Would $k_2 q_s^0$ be much larger than $k_\rho^{diff}(t)$, the initial equilibrium between the slow and fast compartments would always be maintained during release so that:

$$\frac{dq_{out}}{dt} \approx \frac{k_1 q_f^0}{k_2 q_s^0} k_\rho^{diff}(t) q_s \quad (C.9)$$

However, the latter does not seem to be the case. Indeed, although polyelectrolyte/neurotransmitter condensed state is thermodynamically favorable (as discussed above), this step necessarily requires numerous local molecular rearrangements (e.g. change in polyelectrolyte conformation, expel of the solvent molecules during polyelectrolyte condensation etc.) which might determine the kinetics of the exchange process making diffusion controlled release a prevailing process.

Under these conditions the opposite limiting case likely takes place, i.e. when $k_\rho^{diff}(t) \gg k_2 q_s^0$ and again the limit identical to the one in Eq.(8c) is attained:

$$\frac{dq_{out}}{dt} \approx -\frac{dq_s}{dt} \approx k_1 q_f^0 q_s \quad (C.10)$$

with a time constant $\tau_2 = 1/(k_1 q_f^0)$ controlling the release.

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