

Plasma-assisted combustion of hydrogen swirling flames: Extension of lean blowout limit and NO_*x* **emissions**

Jean-Baptiste Perrin-Terrin, Nicolas Vaysse, Daniel Durox, Ronan Vicquelin, Sébastien Candel, Christophe O Laux, Antoine Renaud

To cite this version:

Jean-Baptiste Perrin-Terrin, Nicolas Vaysse, Daniel Durox, Ronan Vicquelin, Sébastien Candel, et al.. Plasma-assisted combustion of hydrogen swirling flames: Extension of lean blowout limit and NO_{$_\ x$} emissions. Proceedings of the Combustion Institute, 2024, 40 (1-4), pp.105546. $10.1016/j.proci.2024.105546$. hal-04665064

HAL Id: hal-04665064 <https://hal.science/hal-04665064v1>

Submitted on 30 Jul 2024

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

[Distributed under a Creative Commons Attribution 4.0 International License](http://creativecommons.org/licenses/by/4.0/)

Plasma-assisted combustion of hydrogen swirling flames: extension of lean blowout limit and NO_x emissions.

Jean-Baptiste Perrin-Terrin^a, Nicolas Vaysse^{a,∗}, Daniel Durox^a, Ronan Vicquelin^a, Sébastien Candel^a, Christophe O. Laux^a, Antoine Renaud^a

^a*Laboratoire EM2C, CNRS, CentraleSupelec, Universit ´ e Paris-Saclay, 8-10 rue Joliot Curie, Gif-sur-Yvette 91192, France ´*

Abstract

A key challenge in the use of hydrogen in practical combustors is to stabilize the flame at equivalence ratios close and even below the LBO limit. Plasma-Assisted Combustion (PAC) has been shown to improve the ignition, stabilization, and blowout margins of combustion systems for a great variety of fuels. In this work, Nanosecond Repetitively Pulsed (NRP) discharges are applied to extend the lean blowout limit (LBO) of a partially premixed hydrogen-air combustor atmospheric test rig equipped with a special unit injecting gaseous hydrogen in crossflow into a swirling air stream. The plasma is formed between this injector and an electrode placed in the central recirculation zone. The LBO limit of a 2.2-kW, V-attached flame is extended from 0.220 to 0.177 (20% reduction) using NRP discharges with a plasma power of about 1% of the nominal flame power. Spectroscopic measurements indicate that the plasma operates in the non-equilibrium spark regime: a low ionization degree is observed, and the temperature in the interelectrode gap is moderate (3500 K on average). It is found that plasma discharges increase the OH[∗] concentration at the flame foot, in the vicinity of the plasma location. Burnt gases analyzed at the outlet of the system indicate that low NO_x concentrations are being produced, even at stoichiometric conditions where the Emission Index reaches its maximum value of $1.1 \text{ gNO}_x/\text{kgH}_2$. The application of the NRP discharges increases the NO_x concentration at all equivalence ratios. To minimize the power consumption and the NO_x increase, the NRP discharges are applied with a duty cycle where the plasma is discharged during about half of the time. It is shown that the NO_x concentration scales linearly with the plasma power and thus that NO_x emission induced by the plasma can be mitigated by 60% with this technique while still preserving the LBO extension.

Keywords: Plasma-assisted combustion; Hydrogen swirling flames; Lean blowout; NO_x emissions

Information for Colloquium Chairs and Cochairs, Editors, and Reviewers

1) Novelty and Significance Statement

The novelty of this research lies in the use of plasma discharges in pure hydrogen swirling flames. Extending the lean blow-out limit as well as measuring NO_x emissions of such flames when applying NRP discharges is a novel addition to the existing knowledge in the field of plasma-assisted combustion. It is significant because it provides technological proofs of the capacity to operate hydrogen combustion in very lean conditions. It is apparently the first time that plasma discharges are applied to extend the operability limit of pure hydrogen flames.

2) Author Contributions

- J.-B. P.-T. performed the experiments, processed the data (plasma part) and wrote the paper.
- N.V. performed the experiments, processed the data (combustion part) and wrote the paper.
- D.D. supervised the research, designed the experiments, analyzed the data and edited the paper.
- R.V. supervised the research.
- S.C. supervised the research and edited the paper.
- C.L. supervised the research, analyzed the data, edited the paper and obtained the funding.
- A.R. supervised the research, analyzed the data, edited the paper and obtained the funding.

3) Authors' Preference and Justification for Mode of Presentation at the Symposium

The authors prefer OPP presentation at the Symposium, for the following reasons:

- The audience would not need to be familiar with the experiment to comprehend an oral presentation of this standalone work.
- Both hydrogen and plasma-assisted combustion are topical issues, likely to arouse discussion.
- The topic of hydrogen combustion in ultra-lean conditions is key for the future of decarbonized combustion.

1. Introduction

 Combustion of renewable hydrogen is a potential solution to decarbonize many industrial sectors re-4 quiring high-temperature heating. However, H_2 com- bustion comes with many new challenges for com- bustion chambers. The hydrogen/air laminar burning velocity is higher than for conventional fuels, causing flashback issues depending on the injector, and the adiabatic flame temperature is also augmented, indi-10 cating a risk for higher NO_x production [1, 2]. The high molecular diffusivity of hydrogen makes it prone to thermo-diffusive instabilities whereas hydrogen en- richment may modify the thermo-acoustic coupling in combustion chambers [3]. Extending the operability domain of hydrogen flames to ultra-lean conditions could be a path to safe combustion. However, the proximity with the extinction limit brings up stabil-ity issues.

 The flame stability can be improved by the ap- plication of plasma in burnt or fresh gases. This tech- nique is called Plasma-Assisted Combustion (PAC). Various methods can be used to generate plasma, and one of the most power-effective is the Nanosec- ond Repetitively Pulsed (NRP) discharge. These dis- charges use 1-25 kV amplitude voltage pulses lasting a few nanoseconds and repeated at frequencies of the order of 10-100 kHz. Depending on these parameters, several plasma regimes can be reached with NRP dis- charges [4, 5]. For PAC applications, a spark regime is preferred due to its hydrodynamic, chemical, and 31 thermal effects that enhance combustion [6].

 Many PAC experiments using NRP discharges were conducted during the last two decades show- ing various combustion enhancements. The ignition delay can be reduced [7], thermo-acoustic instabili- ties can be controlled and mitigated [8–10] and lean blow-out limits can be extended [11–13]. These ef- fects were observed not only on lab-scale burners but also on semi-industrial scale combustors (70 kW [10], 100 kW [14]). They were also demonstrated on a wide variety of fuels: propane [8], methane [8, 9, 11– 13], liquid heptane and dodecane [13], kerosene [15], and ammonia [16].

 Regarding hydrogen, plasma-assisted combus- tion of pure H₂ has focused mostly on the ignition enhancement [17], in supersonic conditions [18], at low pressure (0.2 bar) [19] and at high pressure (1-12 bar) [20]. A recent study also focused on the defla- gration to detonation transition using NRP discharges and showed that the plasma accelerates the hydro- gen combustion [21]. Despite these promising effects of NRP discharges on H_2 /air combustion, to the au- thors' knowledge no studies have focused on the ex-tension of the lean blow-out limit.

 Lean combustion is interesting to reduce the burnt gases temperature, and thus mitigate NO_x emis- sions. This subject is of particular importance for hy- drogen combustion since the H₂ adiabatic flame tem- perature is, as already mentioned, substantially higher than for conventional fossil fuels at the same equiva-

 lence ratio [1]. Exploring ultra-lean conditions is the first step to reducing flame temperature. Among the studies of LBO limit extension using NRP discharges, Lacoste et al. compared the NO_x emissions of a propane/air flame with and without the plasma at dif- ferent equivalence ratios [22]. When the plasma was applied, they measured an increase in NO_x emissions with the plasma power, a conclusion also mentioned with the plasma power, a conclusion also mentioned by [10]. More recently, Choe et al. [16] applied NRP discharges in ammonia/air flame and showed that the plasma can reduce by 30% the NO_x levels at the exit of the burner. More surprisingly, they observed a de- crease in NO_x when the deposited energy increased. This change in the NO_x emissions trends suggests that the effect of PAC on NO_x emissions highly depends on the fuel.

 In this work, NRP discharges are applied in a swirl-stabilized H₂/air burner, the SICCA-H2 config- uration. The LBO limit is measured with different NRP parameters and the burnt gases are analyzed at 81 the outlet of the burner. An extension of the LBO limit to ultra-lean conditions is shown with a limited NO_x penalty.

2. Experimental setup

2.1. The SICCA-H2 PAC facility

Fig. 1: Left : Schematic view of the SICCA-H2 experimental setup. Right: Schematic view of the CFI-X3 cross-flow injector, equipped with a 1-mm diameter tungsten electrode for NRP discharges.

 The experimental configuration is derived from the SICCA-H2 burner presented in [23] which com- prises an air plenum, a tangential swirler, a cross- flow injector for gaseous hydrogen (denoted CFI-X) and a cylindrical combustion chamber. In this work, the hydrogen injection head is longer and has a trun- cated conical shape as presented in Fig. 1. The hy- drogen is injected in cross-flow in the swirled air flow through 6 radial holes of 1.2 mm in diameter. In this work, the swirl number is kept constant at a value $S = 0.60$, determined from laser Doppler velocime-try axial and tangential velocity profiles. The quartz

 chamber is 150-mm long and surmounted by a 41-mm high 15° converging nozzle that reduces recirculation effects when measuring exhaust gas composition. Air and hydrogen mass flow rates are controlled by two *Bronkhorst* EL-FLOW meters with full-scale capac- ities of 210 NL/min for air and 20 NL/min for hydrogen and a typical relative accuracy of 0.8%. The hydrogen mass flow rate is kept constant and thus the flame thermal power is fixed at $P_{th} = 2.2$ kW. The equivalence ratio is varied through the air flow rate while keeping a constant fuel flow rate. Thus, the Reynolds number varies between 8,000 and 36,000.

 NRP discharges are applied with a 1-mm diameter 14 tungsten electrode with an end located at $D = 2.3$ mm above the injector tip, in the central recirculation zone. The plasma is formed in this area, between the electrode (anode) and the injector (grounded cath- ode). Pulses of a fixed duration of 10 ns are gener- ated by an FPG 30-100MC4K pulse generator (FID Technology). The generator is externally triggered by a Pulse-and-Delay BNC model 574, enabling fre- quency control and time delay adjustment with other devices. The NRP discharges have a positive polar- ity and their frequency and incident voltage are var- ied throughout this study in the range 15-30 kHz and 0.5-1.5 mJ.

2.2. Diagnostics

 The voltage and the current delivered by the pulses are monitored with voltage (Lecroy PPE20kV) and current (Pearson 6585) probes placed in the mid- dle of the 5-m cables connecting the pulser and the electrode. The time-integration of the product of the voltage by the current gives the energy deposited by each pulse in the interelectrode gap. Then, the prod- uct of the frequency by the energy gives the plasma power. More details on these electrical measurements can be found in the appendix of [11]. In the rest of this work, each plasma configuration will be desig- nated by its frequency and the energy deposited per pulse.

 The spectra of the flame and the plasma- assisted flame are recorded using an OceanOptics Maya2000Pro deep-UV spectrometer. A Princeton Instruments PI-MAX4 intensified camera equipped with an Asahi Spectra XBPA310 optical bandpass fil- ter centered on 310 nm is used to capture OH $*$ chemi- luminescence images of the flame. The exhaust gas composition is measured using an ECOM J2KN ana- lyzer. The sample probe is placed at the center of the conical exit nozzle, as illustrated in Fig. 1. A non- heated 4-m hose links the sample probe to the gas an-alyzer.

2.3. Protocol

 In this part, the different experimental protocols used in this work are described.

Determination of the equivalence ratio at the LBO limit

 A K-type thermocouple placed on the external quartz tube surface measures the wall temperature 30 mm above the backplane. When thermal equilibrium is reached at the combustor wall, the LBO limit is mea- sured by increasing the air flow rate at a rate of 0.1 (NL/min)/s, resulting in an equivalence ratio vari- ation of 0.01 min⁻¹. To detect the blowout two meth- ods are tested. The first consists in recording the time evolution of the air flow rate value and the output sig- nal of a microphone placed at the chamber outlet. The abrupt change in the microphone signal indicates the extinction. Then, the equivalence ratio at the LBO limit is determined via postprocessing of the recorded signals. The second method consists in a direct acoustic detection of the extinction by the experimenter and a direct reading of the air flow value on the controller. Both methods are in good agreement and feature a constant uncertainty of 1% on the air flow rate value at extinction. Thus, the typical uncertainty on the gain in LBO is 4%, computed as a combination of the latter reading uncertainty and statistical uncertainties. In the present work, the results are obtained with the sec-ond method.

Measurement of the OH[∗] *chemiluminescence* ⁸² To measure the OH^{*} chemiluminescence when the NRP discharges are applied, the camera is externally 84 triggered by the BNC generator to adjust the time de- lay with the plasma emission. For the non-assisted flame, the camera is internally triggered.

Application of the NRP discharges

 In this work, NRP discharges are applied in two modes:

- The continuous mode, which is the most com-monly used in the literature.
- The duty-cycle mode, used in [14, 24].

 The pulsing pattern of the duty-cycle mode is de- scribed in Fig. 2. This mode consists in repetitively applying bursts of NRP discharges. At a given fre- quency, the duty-cycle is described by the number of 97 pulses ON in the burst (N_{ON}) and the number of fol-98 lowing pulses OFF (N_{OFF}). In Fig. 2, $N_{\text{ON}} = 6$ 99 and $N_{\text{OFF}} = 5$. The duty-cycle ratio is defined as 100 $r_{\rm DC} = N_{\rm ON}/(N_{\rm ON} + N_{\rm OFF})$ and corresponds to the fraction of the cycle during which the plasma is on. The continuous mode corresponds to the limit case 103 where $r_{\text{DC}} = 1$. In the duty-cycle mode, the plasma 104 power is $P_{\text{plasma}} = f \times E_p \times r_{\text{DC}}$. Thus, the lower the duty-cycle ratio, the lower the plasma power.

Burnt gases analysis

 After each variation of the experimental conditions, a few minutes are necessary for the measured dry con- centration to stabilize. Once stabilized, their values are noted. The analysis of the dry gases composition gives, among others, the dry mole fractions of O_2 ,

Fig. 2: Timing diagram of NRP discharges applied with a duty-cycle, here with $N_{\text{ON}} = 6$ and $N_{\text{OFF}} = 5$.

 $_{1}$ NO, NO₂ and H₂. Because the unburnt H₂ rapidly sat-² urates the ECOM analyzer (the mole fraction limit is $3\quad 23000$ ppm), $H₂$ cannot be measured when the com-

⁴ bustion efficiency is not close to unity. The follow-⁵ ing global chemical equation is used for the post-

⁶ processing of the dry mole fractions:

$$
\phi H_2 + \frac{1}{2} (O_2 + \beta N_2) \rightarrow
$$

$$
\eta \phi H_2 O + \frac{1 - \eta \phi}{2} O_2 + \frac{\beta}{2} N_2 + \phi (1 - \eta) H_2
$$

where $\beta = n'_{N_2}/n'_{O_2} = 3.76$ is the nitrogen-tos oxygen ratio in fresh air and $\eta = n''_{H_2O}/n'_{H_2}$ is the 9 combustion efficiency. The number of moles n'_i and 10 n''_i respectively stand for the reactants and the prod- 11 ucts of species i. The mole fraction of oxygen under 12 dry conditions can be expressed as:

$$
X_{O_2}^m = \frac{n_{O_2}''}{n_{O_2}'' + n_{N_2}'' + n_{H_2}''} = \frac{1 - \eta \phi}{1 + \beta + (2 - 3\eta)\phi}
$$

¹³ thus the combustion efficiency can be deduced from

¹⁴ $X_{O_2}^m$ and the global equivalence ratio ϕ :

$$
\eta \phi = \frac{(\beta + 1 + 2\phi)X_{O_2}^m - 1}{3X_{O_2}^m - 1}
$$

¹⁵ One retrieves the limit case of no combus-¹⁶ tion, for which $X_{O_2}^m = 1/(1 + 2\phi + \beta)$ leads to $17 \eta = 0$, and the case of complete combustion where 18 $X_{O_2}^m = (1 - \phi)/(1 - \phi + \beta)$ leads to $\eta = 1$.

¹⁹ One can then derive the wet mole fractions by ²⁰ multiplying the measured dry mole fractions by a dry- 21 to-wet correction factor C , defined as:

$$
C=\frac{n_{O_2}^{\prime\prime}+n_{N_2}^{\prime\prime}+n_{H_2}^{\prime\prime}}{n_{H_2O}^{\prime\prime}+n_{O_2}^{\prime\prime}+n_{N_2}^{\prime\prime}+n_{H_2}^{\prime\prime}}.
$$

²² After some algebra one finds that:

$$
C = \frac{\phi + \beta/2 - 1}{\phi + \beta/2 - X_{O_2}^m (1 + \beta + 2\phi)}
$$

 which gives, in the limit case of no combustion, $C = 1$ which is consistent with the fact that no water is produced. In the complete combus- tion assumption, one retrieves the classical formula $C = (\beta + 1 - \phi)/(\beta + 1 + \phi).$

$$
28
$$
 The evolution of *C* is shown in Fig. 3.

Fig. 3: Abacus giving the correction factor C linking dry and wet mole fractions, as a function of the measured O_2 dry mole fraction and the equivalence ratio.

²⁹ *Electrode erosion*

 Electrode erosion was observed both when operat- ing the flame with and without plasma. The erosion speed was about 0.5 mm/h with the flame alone and 0.6 mm/h with the flame and plasma at 40 kHz and 1.5 mJ. For this reason, the electrodes were replaced after each hour of operation to prevent a variation of more than 0.6 mm in the interelectrode gap dis- tance during experiments. Additionally, to minimize this uncertainty for each operating point, several elec-trodes with different erosion states are used.

⁴⁰ 3. Experimental conditions

⁴¹ *3.1. Flame structure*

Fig. 4: Line-of-sight integrated OH^{*}chemiluminescence images of the flame without plasma, at thermal power P_{th} = 2.2 kW and equivalence ratio $\phi = 0.231$, (left) without and (right) with the electrode outlined with white dashes.

 The observed LBO equivalence ratio of the 43 flame at thermal power $P_{th} = 2.2$ kW is $\phi = 0.220$. 44 At $\phi = 0.231$, corresponding to 105% of the LBO limit, the flame is V-shaped and is attached to the injector flat tip. The OH[∗] ⁴⁶ chemiluminescence images of Fig. 4 show that the presence of the electrode brings minimal changes to the flame shape (the electrode can be seen in the right image of Fig. 4).

⁵⁰ *3.2. Characterization of the plasma*

⁵¹ NRP discharges are generated with frequencies 52 in the range of $15 - 30$ kHz and with incident voltages 1 in the range of $1.5 - 3$ kV. The typical shapes of the ² voltage and current traces are shown in Fig. 5. The 3 interelectrode distance is $D = 2.3 \pm 0.6$ mm. The energy is deposited during the initial pulse and the se-⁵ ries of reflected pulses (as shown in blue in Fig. 5) and 6 varies between 0.5 mJ and 1.5 mJ, with an uncertainty

 τ of $\pm 100 \mu$ J. In these conditions, according to [4], the plasma is formed in the spark regime.

Fig. 5: Typical traces of voltage (black) and current (red) of a pulsed discharge. The energy (blue) is the integration over time of the product of the voltage by the current. In this case, the incident voltage is 2.8 kV, and the deposited energy is 1.42 mJ after 1800 ns.

 The optical emission spectroscopy measure- ments shown in Fig. 6 are used to measure the tem- perature in the plasma region from the rotational tem-12 perature of $N_2(C)$ in the range 360 – 390 nm using 13 Specair [25]. A temperature of 3500 ± 300 K is 14 found for the 15 kHz $-$ 1.5 mJ plasma (applied con-15 tinuously and with duty-cycle) and 3800 ± 400 K for 16 the 30 kHz – 0.75 mJ plasma. Additionally, an up- per bound of the electron number density can be esti-18 mated from the broadening of the H_β line at 486 nm [26]. The total broadening observed in Fig. 6 is 1.5 nm. Taking into account the instrumental broad- ening of about 1 nm, we obtain an upper bound of the ionization degree of less than about 0.2%. Consider- ing the relatively low heating and ionization degree, the plasma is in the non-equilibrium spark regime [5]. The spectrum of the flame without plasma is dominated by the black-body emission of the heated electrode. In particular, the broadband blue emis- sion characteristic of the hydrogen flames is not vis- ible. The absorption caused by the water vapor pro- duced by the combustion appears around 950 nm. At 31 310 nm, OH^{*} emission is not intense because the field of view of the spectrometer is centered on the dis-charge which produces intense emission via the sec-

³⁴ ond positive system of nitrogen.

³⁵ 4. Results

³⁶ *4.1. Influence of frequency and deposited energy per* ³⁷ *pulse on LBO extension*

³⁸ In a first set of experiments, the frequency is

 is acquired with the 30 kHz - 0.75 mJ plasma applied con- tinuously and with a duty-cycle ratio of 0.45. The blue line with the 15 kHz – 1.5 mJ plasma, applied respectively con- without the plasma. The red and orange lines are acquired 0.4 tinuously. ^{1.2} $P_{th} = 2.2$ kW and $\phi = 0.231$. Spectra are acquired dur ing 50 ms and averaged 40 times. The black line is acquired Fig. 6: Typical emission spectra acquired in the H_2 flame at

 kept equal to 30 kHz and the deposited energy per pulse varies with values 500 µJ, 750 µJ, 1 mJ, and 1.5 mJ. Fig. 7 shows that the gain in LBO compared to the non-assisted case increases linearly with the en- ergy, with values of 6%, 11%, 19%, and 23%. Then, measurements are performed at a lower frequency, $f = 15$ kHz, and show that the gain in LBO also in-46 creases with the frequency at $E_p = 0.75$ mJ (from 7%) 47 to 11%) and $E_p = 1.5$ mJ (from 20% to 23%). It is interesting to compare in Fig. 7 two experiments with 49 the same average plasma power. The $f = 15$ kHz - $E_p = 1.5 \text{ mJ}$ and the $f = 30 \text{ kHz} - E_p = 0.75 \text{ mJ}$ plasmas are on the 22.5-W line (corresponding to 1% of the flame thermal power) but it is shown in Ta- ble 1 that the former extends the LBO limit by up to 19.5% while the latter only to 10.9%. This indi- cates that in these conditions, increasing the energy extends the LBO limit more efficiently than increasing the repetition frequency at constant plasma power. Because of its larger improvement in LBO limit, the $f = 15$ kHz - $E_p = 1.5$ mJ plasma will be studied in more detail in the rest of this work.

Fig. 7: Mapping of the LBO gain as a function of the repetition frequency and the average energy deposited per pulse. Dashed lines represent isolines of plasma power, expressed as a percentage of the thermal power.

Table 1: LBO measurements for a flame at $P_{th} = 2.2 \text{ kW}$

Frequency [kHz]	\sim	15	15	30	30
Energy [mJ]		0.75	15	0.75	15
ϕ at LBO	0.220	0.204	0.177	0.196	0.170
Gain in LBO [%]	0	73	19.5	10.9	22.6
Plasma power [W]	$_{0}$	11.25	22.5	22.5	45

 The effect of the plasma pulses on the chemistry of the flame is analyzed through phase-averaged OH[∗] chemiluminescence imaging presented in Fig. 8. The images are recorded during the time separating two pulses and show that the plasma locally increases the OH[∗] radical concentration near the foot of the flame front, where it is applied. Right after the discharge, ⁸ the OH^{*} signal is intense in the vicinity of the elec- trode. Then, the intensity monotonically decreases until the following pulse. This effect is emphasized in the bottom row of Fig. 8, which isolates the con-12 tribution of plasma to the OH^{*} signal by subtracting the OH[∗] image of the flame without plasma shown in Fig. 4 from the phase-averaged images. It also high- lights that the effect of the plasma on the flame is ¹⁶ local and does not increase the OH^{*} chemilumines-cence elsewhere in the flame.

4.2. Combustion efficiency

 The values of the combustion efficiency pre- sented in Fig. 9 include the flame without plasma and the plasma-assisted flame in the three investi-22 gated plasma cases: $f = 15$ kHz - $E_p = 1.5$ mJ, $f = 30$ kHz - $E_p = 0.75$ mJ and $f = 15$ kHz - $E_p =$ 24 1.5 mJ applied with a duty-cycle ratio $r_{\text{DC}} = 0.45$. At first, the combustion efficiency increases with the 26 equivalence ratio. Then, a plateau value of $92\% \pm 8\%$ 27 is reached above $\phi = 0.5$. However, the measured mole fraction of H_2 is 0 ppm in this domain, indi- cating that combustion is complete. In stoichiometric conditions, the efficiency is close to 100%. No clear effect of the plasma on the combustion efficiency of the flame is visible in Fig. 9.

4.3. NO^x emissions

 The measured dry NO_x mole fractions are multi- plied by the dry-to-wet correction factor C introduced in Fig. 3 to obtain their wet values in the flame. This is essential to derive an emission index based on the 38 mass flow rate ratio between NO_x and injected H_2 . 39 The evolution of this NO_x Emission Index, plotted 40 in Fig. 10, shows that the NO_x emissions of the non-41 assisted flame remain lower than 1.1 g/kgH_2 on the whole investigated operability domain of the flame. This value corresponds to the lower end of the typ- ical Emission Indexes reported in the literature (1- 20 g/kgH_2 for jet and coaxial flames [27–29]). The NO_x emissions increase with the equivalence ratio af- ter a slight decrease in the leanest range. An opti-48 mum for NO_x emissions is found around $\phi = 0.4$ for all conditions. All plasma pulses investigated in

 this work induce an increase of the NO_x emissions by 0.5 to 1.5 g/kgH² . However, applying a duty-cycle 52 (green diamonds in Fig. 10) to the $f = 15$ kHz - E_p = 1.5 mJ plasma reduces the NO_x emissions at all equivalence ratios, up to 60% in the leanest do- main, while still extending the LBO limit. The one- sigma error bars are fairly large because all sources of error are taken into account. The main uncertain- ties arise when the oxygen mole fraction is close to zero near stoichiometry or at very low equivalence ra- tios (especially in Fig. 10). However, the measured mean values still clearly support the reduction of NO_x emissions in duty cycle mode, which is the intended point of Fig. 10. The effect of this technique on the NO_x emissions is further investigated in the following section.

4.4. Influence of the pulsing pattern : effect of the duty-cycle on flame stability and NO^x emissions

 To decrease the plasma power without reducing the effect of the plasma on the flame, the NRP dis- charges are applied in the duty-cycle mode at $f =$ 15 kHz and $E_p = 1.5$ mJ. This method was already tested by [14, 24] and the energy was reduced with- out losing the stabilizing properties of the plasma. The power consumption is thus directly multiplied by $r_{\rm DC}$. The equivalence ratio is fixed at 105% of the 76 LBO limit obtained with this plasma $(1.05\phi_{LBO}^p =$ 0.186). To determine the lowest duty-cycle ratio al- lowing the stabilization of a flame at this equivalence 79 ratio, N_{ON} is fixed and N_{OFF} is progressively in- creased until the flame is blown off. The gas is sam- pled in the process. The results are shown in Fig. 11. The extinction limit is drawn as a dotted line and presents the same V-shape as found in [14], with a 84 minimum reached around $N_{ON} = 100$. During the ON phase, the pulses generate a stabilizing kernel, enhancing the combustion. During the OFF phase, the enhancement of the flame fades until the next 88 ON phase. For the low N_{ON} , the aforementioned combustion-stabilizing kernel is not strong enough and the enhancement fades before the next ON phase. 91 When N_{ON} increases, the kernel is stronger, and thus 92 the maximum r_{DC} is larger. As N_{ON} is further increased, for a given $r_{\rm DC}$, the OFF phase is also longer 94 and the contribution of the additional pulses to the kernel is not sufficient to sustain the combustion on kernel is not sufficient to sustain the combustion on this longer OFF phase: the flame extinguishes.

 Two key plasma-induced reactions must be con-98 sidered to interpret the results on NO_x emissions pre- sented in Fig. 11: the beneficial radical production (1) and the detrimental NO formation (2).

$$
N_2^* + O_2 \to N_2 + 2 O \tag{1}
$$

$$
N_2^* + O \to NO + N \tag{2}
$$

101 where N_2^* stands for excited electronic states of nitro- gen. The flame is stabilized when successive pulses have produced enough radicals through reaction (1).

Fig. 8: Phase-averaged OH[∗] chemiluminescence images of the flame between two plasma pulses. The phase number is indicated in the top diagram. The $f = 15$ kHz - $E_p = 1.5$ mJ plasma is applied. Top: line-of-sight integrated images of the flame. Bottom: Images of the difference between these phase-averaged images and the image of the flame without plasma, presented in Fig. 4. The electrode is added in white on the second row. The exposure time is 5 µs. Twelve phases are recorded, only the even phases are shown.

Fig. 9: Evolution of the combustion efficiency as a function of the equivalence ratio, for the flame without plasma, and the three different discharges applied. The efficiency is computed from the dry O_2 mole fraction measurement and the equivalence ratio. Uncertainties are propagated starting from the accuracy and resolution of the mass flow meters and the gas analyzer.

Fig. 10: Evolution of the NO_x Emission Index as a function of the equivalence ratio, for the flame without plasma, and for the three different discharges applied. The $EINO_x$ is computed from the dry NO_y mole fractions, corrected to wet conditions using O_2 measurements. Uncertainties are propagated starting from the accuracy and resolution of the mass flow meters and the gas analyzer.

- ¹ Above this threshold, additional pulses do not further
- ² improve stabilization, but they increase NO through
- ³ reaction (2). Thus, the duty cycle mode allows to keep

Fig. 11: Map of the NO_x Emission Index as a function of the duty-cycle ratio r_{DC} and the number of pulses in each cycle, at an equivalence ratio of $1.05\phi_{LBO}^p = 0.186$. The $f = 15$ kHz - $E_p = 1.5$ mJ plasma is applied. The dashed line shows the minimal duty-cycle ratio required to stabilize the flame.

Fig. 12: Evolution of the NO_x Emission Index as a function of the plasma power at an equivalence ratio of $1.05\phi_{LBO}^p =$ 0.186. The $f = 15$ kHz - $E_p = 1.5$ mJ plasma is applied. The colors correspond to the duty-cycle ratio. The down triangle corresponds to the measured emissions at the minimal $r_{\rm DC}$ value and the circle to the value obtained for continuous plasma operation. N_{ON} is varied between 10 and 500.

 5 The effect of the pulsing pattern on NO_x emissions is expressed in Fig. 12 as a function of the ⁷ average plasma power, computed as the product ⁸ of the duty-cycle ratio with the continuous plasma 9 power. The NO_x emissions decrease linearly with the plasma power as the duty-cycle ratio is decreased.

This is consistent with the results found in methane

flames [10, 14, 22].

5. Conclusion

 A V-attached hydrogen flame of 2.2 kW is studied. Its equivalence ratio at the lean blow-out limit equals 0.22. NRP discharges are applied to this flame to extend the LBO limit. Various couples of repetition frequencies and deposited energy are tested. In all NRP conditions, the plasma is in the non-equilibrium spark regime, inducing moderate heating (a few thou- sand kelvins) and a low ionization degree (less than 0.2%). The effect of the plasma on the flame is ob-14 served using OH^{*} chemiluminescence. During the 15 pulse, the plasma locally increases the OH^{*} signal. The increase is confined to the vicinity of the plasma and slowly decays between two pulses. The main findings of this work are:

- The LBO limit can be extended from 0.22 to 20 0.177 (20% gain) with the $f = 15$ kHz -21 $E_p = 1.5 \text{ mJ plasma.}$
- ²² The plasma power required to extend the LBO limit with continuously applied NRP discharges is about 1% of the flame thermal power.
- ²⁵ The plasma power can be reduced to 0.45% of the flame thermal power by applying the NRP discharges with a duty-cycle ratio of 0.45.
- 28 From $\phi = 0.22$ to 1 (lean operation) the nonassisted flame emits less than $1.1 \text{ gNO}_x/\text{kgH}_2$.
- The NRP discharges applied continuously in- $_{31}$ crease the NO_x emission by 0.5 to 1.5 g/kgH₂.
- The NRP discharges applied with a duty-cycle ratio of 0.45 increase the NO_x emission by 0.2 $_{34}$ to 0.9 g/kgH₂.

Declaration of competing interest

 The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence this work.

Acknowledgments

 This work was partially supported by the FlyHy project of the Agence Nationale de la Recherche (ANR-21-CE05-0008), the European Research Coun- cil (ERC) under the European Union's Horizon 2020 research and innovation program (GreenBlue project under grant agreement No.101021538) and by the Fondation Simone and Cino Del Duca through a sci- entific grant attributed to the project PLATHON. For open access purposes, a CC-BY license has been ap- plied by the authors to this document and will be ap- plied to any subsequent version up to the author's manuscript accepted for publication resulting from this submission. The authors would like to thank Yan- nick Le Teno and the support team of EM2C lab for their technical assistance.

References

- [1] A. L. Sanchez, F. A. Williams, Recent advances in un- ´ derstanding of flammability characteristics of hydro- gen, Progress in Energy and Combustion Science 41 (2014) 1–55.
- [2] P. Palies, Challenges and Outlook for Hydrogen-Based Aviation, AIAA Paper 2022-3378. (2022) 15.
- [3] J. G. Aguilar, E. Æsøy, J. R. Dawson, The influence of hydrogen on the stability of a perfectly premixed com- bustor, Combustion and Flame 245 (112323) (Nov. 2022).
- [4] D. Z. Pai, D. A. Lacoste, C. O. Laux, Transitions between corona, glow, and spark regimes of nanosec- ond repetitively pulsed discharges in air at atmospheric pressure, Journal of Applied Physics 107 (9) (2010) 093303.
- [5] N. Minesi, S. Stepanyan, P. Mariotto, G. D. Stancu, C. O. Laux, Fully ionized nanosecond discharges in air: The thermal spark, Plasma Sources Science and Technology 29 (8) (2020) 085003.
- [6] C. Laux, Applications of Plasma Discharges to Com- bustion, Journal of the Combustion Society of Japan 64 (209) (2022) 257–264.
- [7] Y. Xiong, O. Schulz, C. Bourquard, M. Weilenmann, N. Noiray, Plasma enhanced auto-ignition in a sequential combustor, Proceedings of the Combustion Insti-tute 37 (4) (2019) 5587–5594.
- [8] J. Moeck, D. Lacoste, C. Laux, C. Paschereit, Con- trol of combustion dynamics in a swirl-stabilized com- bustor with nanosecond repetitively pulsed discharges, in: 51st AIAA Aerospace Sciences Meeting Including the New Horizons Forum and Aerospace Exposition, Aerospace Sciences Meetings, 2013.
- [9] L. Yu, B. Aravind, D. A. Lacoste, Mitigating the re- sponse of premixed swirl flames to acoustic excita- tion by nanosecond repetitively pulsed discharges at elevated pressures, Combustion and Flame 256 (2023) 112944.
- [10] B. Dharmaputra, S. Shcherbanev, B. Schuermans, N. Noiray, Thermoacoustic stabilization of a sequential combustor with ultra-low-power nanosecond repet- itively pulsed discharges, Combustion and Flame 258 (2023) 113101.
- [11] N. Q. Minesi, V. P. Blanchard, E. Pannier, G. D. Stancu, C. O. Laux, Plasma-assisted combustion with nanosecond discharges. I: Discharge effects characterization in the burnt gases of a lean flame, Plasma Sources Science and Technology 31 (4) (2022) 103 045029.
- [12] F. Di Sabatino, D. A. Lacoste, Enhancement of the lean stability and blow-off limits of methane-air swirl flames at elevated pressures by nanosecond repeti- tively pulsed discharges, Journal of Physics D: Applied Physics 53 (35) (2020) 355201.
- [13] G. Vignat, N. Minesi, P. R. Soundararajan, D. Durox, A. Renaud, V. Blanchard, C. O. Laux, S. Candel, Im- provement of lean blow out performance of spray and premixed swirled flames using nanosecond repetitively pulsed discharges, Proceedings of the Combustion In-114 stitute 38 (4) (2021) 6559–6566.
- [14] V. P. Blanchard, P. Scouflaire, C. O. Laux, S. Ducruix, Combustion performance of plasma-stabilized lean flames in a gas turbine model combustor, Applications in Energy and Combustion Science 15 (2023) 100158.
- [15] G. Heid, G. Pilla, R. Lecourt, D. Lacoste, As- sisted Combustion Of An Air Kerosene Mixture By Nanosecond Repetitively Pulsed Discharges, in: Inter-
- national Symposium on Air Breathing Engines, American Institute of Aeronautics and Astronautics, Mon-
- treal, Canada, 2009, pp. 474–482.
- [16] J. Choe, W. Sun, T. Ombrello, C. Carter, Plasma assisted ammonia combustion: Simultaneous NOx reduction and flame enhancement, Combustion and Flame 228 (2021) 430-432.
- [17] Y. Ju, X. Mao, J. K. Lefkowitz, H. Zhong, Plasma- Assisted Hydrogen Combustion, in: E.-A. Tingas (Ed.), Hydrogen for Future Thermal Engines, Green Energy and Technology, Springer International Pub-12 lishing, Cham, 2023, pp. 429–458.
- [18] H. Do, M. A. Cappelli, M. G. Mungal, Plasma assisted cavity flame ignition in supersonic flows, Combustion and Flame 157 (9) (2010) 1783–1794.
- [19] A. Dutta, Z. Yin, I. V. Adamovich, Cavity ignition and flameholding of ethylene–air and hydrogen–air flows by a repetitively pulsed nanosecond discharge, Com-
- 19 bustion and Flame 158 (8) (2011) 1564–1576.
20 [20] S. A. Shcherbanev, N. A. Popov, S. M. Starike [20] S. A. Shcherbanev, N. A. Popov, S. M. Starikovskaia, Ignition of high pressure lean H2:air mixtures along the multiple channels of nanosecond surface discharge, Combustion and Flame 176 (2017) 272–284.
- 24 [21] J. A. T. Gray, D. A. Lacoste, Effect of the plasma lo-
25 cation on the deflagration-to-detonation transition of cation on the deflagration-to-detonation transition of a hydrogen–air flame enhanced by nanosecond repeti- tively pulsed discharges, Proceedings of the Combus-tion Institute 38 (3) (2021) 3463–3472.
- [22] D. A. Lacoste, J. P. Moeck, C. O. Paschereit, C. O. Laux, Effect of Plasma Discharges on Nitric Oxide Emissions in a Premixed Flame, Journal of Propulsion 32 and Power 29 (3) (2013) 748–751.
33 [23] N. Vaysse, D. Durox, R. Vicquelin
- [23] N. Vaysse, D. Durox, R. Vicquelin, S. Candel, A. Re- naud, Stabilization and Dynamics of Pure Hydro- gen Swirling Flames Using Cross-Flow Injection, in: ASME Turbo Expo 2023: Turbomachinery Technical Conference and Exposition, American Society of Me-chanical Engineers Digital Collection, 2023.
- [24] A. M. Alkhalifa, A. Alsalem, D. Del Cont-Bernard, D. A. Lacoste, Active control of thermoacoustic fluc- tuations by nanosecond repetitively pulsed glow dis- charges, Proceedings of the Combustion Institute 39 (4) (2023) 5429–5437.
- [25] C. O. Laux, T. G. Spence, C. H. Kruger, R. N. Zare, Optical diagnostics of atmospheric pressure air plas-46 mas, Plasma Sources Science and Technology 12 (2) 47 (2003) 125. (2003) 125.
- 48 [26] N. Konjević, M. Ivković, N. Sakan, Hydrogen Balmer lines for low electron number density plasma diag- nostics, Spectrochimica Acta Part B: Atomic Spec-troscopy 76 (2012) 16–26.
- [27] J. F. Driscoll, R.-H. Chen, Y. Yoon, Nitric oxide levels of turbulent jet diffusion flames: Effects of residence time and damkohler number, Combustion and Flame 88 (1) (1992) 37–49.
- [28] S. Noda, J. Inohae, Z. S. Saldi, NO emission character- istics of confined jet nonpremixed flames, Proceedings of the Combustion Institute 31 (1) (2007) 1625–1632.
- [29] M. Leroy, C. Mirat, A. Renaud, S. Puggelli, S. Zur- bach, R. Vicquelin, Structure and NOx Emissions of Stratified Hydrogen-Air Flames Stabilized on a Coax-
- ial Injector, Journal of Engineering for Gas Turbines and Power 146 (031012) (Nov. 2023).