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1 Influence of experimental boundary conditions on the  
2 calibration of a ductile fracture criterion

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6 **Abstract**

7 Hybrid experimental-numerical approach is the commonly used technique  
8 to identify the material parameters of ductile fracture criteria. In this work,  
9 attention is paid to the precise definition of the Finite Element (FE) model  
10 of fracture tests by applying real boundary conditions coming from the lo-  
11 cal displacement field. The aim is to investigate the effect of the way to  
12 reproduce experimental boundary conditions on the accuracy of the hybrid  
13 experimental-numerical approach. A stress triaxiality and Lode angle based  
14 ductile fracture criterion is used to predict the onset of ductile fracture for  
15 AA6061-T6 aluminum alloy sheets. To calibrate this criterion, a series of  
16 fracture tests is carried out up to fracture. Notched tensile specimens with  
17 different radius, tensile specimens with a central hole and shear specimens  
18 are used to cover a wide range of stress states. Strain distribution over the  
19 surface is measured with digital image correlation technique. Two numeri-  
20 cal models are defined for each geometry type, a first one constrained with  
21 real experimental boundary conditions and a second one with ideal boundary  
22 conditions, to predict stress and strain distributions. By comparing results of  
23 both approaches with experiments, it is shown that the model constrained by

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1 local experimental boundary conditions provides a better agreement with the  
2 experiments than the simplified model does, which underlines the sensitivity  
3 of the hybrid method to the adopted boundary conditions. **Furthermore,**  
4 **several fracture test combinations are used to calibrate the ductile criterion**  
5 **and the effect of the calibration tests is discussed.**

6

7 *Keywords:* Ductile fracture criterion, Hybrid experimental-numerical  
8 approach, Boundary conditions, AA6061-T6

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9

## 10 **Nomenclature**

11  $C_1, C_2, C_3$  material parameters

12  $D$  failure indicator

13  $D_{cri}$  critical value of  $D$

14  $D_{pred}$  predicted value of  $D$  in the critical element at the fracture stroke

15  $E$  Young's modulus

16  $Erf$  error function

17  $f$  weighting function of the stress state

18  $L$  Lode parameter

19  $L_{avg}$  average value of Lode parameter

20  $LE11$  longitudinal logarithmic strain

- 1  $r_0, r_{45}, r_{90}$  plastic anisotropy coefficients
- 2  $\bar{r}$  normal anisotropy coefficient
- 3  $t_f$  fracture time
- 4  $u_{avg}$  average value of displacement at fracture
- 5  $u_f$  displacement at fracture
- 6  $UTS$  ultimate tensile strength in RD
- 7  $YS$  yield strength at 0.2% plastic strain in RD
- 8  $\delta$  error indicator
- 9  $\Delta r$  planar anisotropy coefficient
- 10  $\varepsilon_1, \varepsilon_2$  logarithmic in-plane principal strain components
- 11  $\varepsilon_{eq}$  equivalent strain
- 12  $\bar{\varepsilon}_f$  equivalent plastic strain at fracture or fracture strain
- 13  $\bar{\varepsilon}_p$  equivalent plastic strain
- 14  $\bar{\varepsilon}_{t0}, \bar{\varepsilon}_{s0}, \bar{\varepsilon}_{p0}$  fracture strains in uniaxial tension, pure shear and plane strain  
15 conditions, respectively
- 16  $\dot{\varepsilon}$  strain rate
- 17  $\eta$  stress triaxiality
- 18  $\eta_{avg}$  average value of stress triaxiality

- 1  $\nu$       Poisson's ratio
- 2  $\boldsymbol{\sigma}$     Cauchy stress tensor
- 3  $\bar{\sigma}$       von Mises equivalent stress
- 4  $\sigma_1, \sigma_2, \sigma_3$  principal stresses of the stress tensor
- 5  $\sigma_m$     mean stress or hydrostatic stress
- 6  $\tau_{max}$     maximum shear stress

7 **1. Introduction**

8      Ductile fracture criteria are widely used to predict failure during manu-  
 9      facturing process and service. These criteria characterize the damage state in  
 10     the material and when a critical value of these criteria is reached, they lead  
 11     to the onset of macroscopic fracture. These criteria are expressed according  
 12     to the following general form:

$$D = \int_0^{\bar{\epsilon}_f} f(\boldsymbol{\sigma}) d\bar{\epsilon}_p \quad (1)$$

13     where  $D$  is a **failure indicator** that indicates the onset of fracture in a given  
 14     finite element when it reaches unity.  $\bar{\epsilon}_p$  is the equivalent plastic strain,  $\bar{\epsilon}_f$  is  
 15     the equivalent plastic strain at fracture (or fracture strain) and  $f$  is a weight-  
 16     ing function of the stress state represented by the Cauchy stress tensor  $\boldsymbol{\sigma}$ .

17

18      Several ductile fracture criteria have been developed to predict the duc-  
 19      tile fracture of materials by using different weighting functions. Cockroft and  
 20      Latham [1] proposed a fracture criterion weighted by the maximum principal

1 stress. Oh et al. [2] normalized the maximum principal stress in the crite-  
2 rion of Cockcroft-Latham by the equivalent stress. Clift et al. [3] introduced  
3 equivalent stress into the weighting function instead of maximum principal  
4 stress. Brozzo et al. [4] modified the Cockcroft and Latham fracture crite-  
5 rion to incorporate an explicit dependence of the mean stress on the fracture  
6 strain. Rice and Tracey [5], Oyane [6], Ayada et al. [7] and Ko et al. [8] pro-  
7 posed fracture criteria that consider stress triaxiality. All these mentioned  
8 ductile fracture criteria have only one parameter requiring few tests to be  
9 calibrated which justifies their intensive use in industrial applications [9, 10].  
10 However, the use of only one material parameter limits the flexibility of  
11 these criteria. Moreover, a comparative study of some ductile fracture crite-  
12 ria mentioned above conducted by Bao et al. [11] showed that none of them  
13 can accurately describe the fracture behavior of a given material over a large  
14 range of stress triaxialities. Barsoum and Faleskog [12] argued that the stress  
15 triaxiality is insufficient to characterize the stress state in ductile fracture.  
16 Wierzbicki et al. [13] and Gao and Kim [14] observed that predictions of duc-  
17 tile failure can be improved by introducing the Lode parameter. To predict  
18 fracture strain with high accuracy under a wide range of loading conditions,  
19 Bai and Wierzbicki [15, 16] have modified the Mohr–Coulomb fracture model  
20 to propose a criterion based on stress triaxiality and Lode angle. Mohr and  
21 Marcadet [17] developed the Hosford-Coulomb model accounting also for the  
22 effects of the stress triaxiality and the Lode angle. Lou et al. [18] developed a  
23 ductile fracture criterion inspired from the micro-mechanisms of ductile frac-  
24 ture that occurs mainly due to void nucleation, growth and finally coalescence  
25 into microcracks. It was assumed that void nucleation is proportional to the

1 equivalent plastic strain, void growth is controlled by the stress triaxiality  
 2 and coalescence of void is dominated by the shear-linking up of voids gov-  
 3 erned by the maximum shear stress. This criterion is defined as follows:

$$D(\bar{\varepsilon}_p) = \frac{1}{C_3} \int_0^{\bar{\varepsilon}_f} \left( \frac{2\tau_{max}}{\bar{\sigma}} \right)^{C_1} \left( \frac{\langle 1 + 3\eta \rangle}{2} \right)^{C_2} d\bar{\varepsilon}_p \text{ with } \langle x \rangle = \begin{cases} x & \text{when } x \geq 0 \\ 0 & \text{when } x < 0 \end{cases} \quad (2)$$

4 where  $\tau_{max}$  is the maximum shear stress,  $\bar{\sigma}$  is von Mises equivalent stress.  
 5  $C_1$ ,  $C_2$  and  $C_3$  are three material parameters that need to be calibrated by  
 6 at least three different tests.  $\eta$  is the stress triaxiality defined as follows:

$$\eta = \frac{\sigma_m}{\bar{\sigma}} \quad \text{with} \quad \sigma_m = \frac{\text{Tr}(\boldsymbol{\sigma})}{3} \quad (3)$$

7 where  $\sigma_m$  is the hydrostatic stress and  $\sigma_1$ ,  $\sigma_2$  and  $\sigma_3$  are the principal stresses  
 8 of the stress tensor, such that  $\sigma_1 \geq \sigma_2 \geq \sigma_3$ . Lou and Huh [19] correlated the  
 9 normalized maximum shear stress to the Lode parameter, to transform the  
 10 criterion into a Lode parameter dependent form:

$$D(\bar{\varepsilon}_p) = \frac{1}{C_3} \int_0^{\bar{\varepsilon}_f} \left( \frac{2}{\sqrt{L^2 + 3}} \right)^{C_1} \left( \frac{\langle 1 + 3\eta \rangle}{2} \right)^{C_2} d\bar{\varepsilon}_p \quad (4)$$

11 where  $L$  is the Lode parameter defined as follows:

$$L = \frac{2\sigma_2 - \sigma_1 - \sigma_3}{\sigma_1 - \sigma_3} \quad (5)$$

12 It should be emphasized that the three fracture parameters  $C_1$ ,  $C_2$  and  $C_3$   
 13 should be positive as reported by Lou [20]. The fracture parameter  $C_1$  which  
 14 modulates the effect of the Lode parameter on shear coalescence of voids  
 15 should have a positive value to make sure that at a constant stress triaxiality,  
 16 the fracture strain in uniaxial tension ( $L = -1$ ) is greater than those in plane

1 strain and pure shear ( $L=0$ ). The fracture parameter  $C_2$  modulates the  
 2 effect of the stress triaxiality on void growth and should also have a positive  
 3 value. That is because  $C_2$  is calculated as follows [20]:

$$C_2 = \frac{\log(\bar{\varepsilon}_{s0}) - \log(\bar{\varepsilon}_{p0})}{\log(1 + \sqrt{3})} \quad (6)$$

4 where  $\bar{\varepsilon}_{s0}$  and  $\bar{\varepsilon}_{p0}$  are fracture strains respectively in pure shear and plane  
 5 strain conditions. According to Eq. 6, a positive value of  $C_2$  is guaranteed if  
 6  $\bar{\varepsilon}_{s0} > \bar{\varepsilon}_{p0}$  which is true since both conditions have the same Lode parameter  
 7 ( $L=0$ ) but the lower triaxiality in pure shear than that in plane strain raises  
 8 the fracture strain.

9 The material constant  $C_3$  modulates the magnitude of the constructed  
 10 fracture locus with no influence on the shape.  $C_3$  is positive since it corre-  
 11 sponds to the fracture strain in uniaxial tension  $\bar{\varepsilon}_{t0}$ . It is worth noting that  
 12  $\bar{\varepsilon}_{t0}$ ,  $\bar{\varepsilon}_{s0}$  and  $\bar{\varepsilon}_{p0}$  are fracture strains corresponding to ideal cases which cannot  
 13 be achieved in practical experiments.

14 Lou's ductile fracture criterion have been successfully applied for pre-  
 15 dicting fracture of several metals: Dual Phase steels DP780 [18, 21] and  
 16 DP980 [22], fully martensitic steel (Docol 1400M) [23], TWIP steel [24], SUS304  
 17 steel [25] and aluminum alloys AA1050 [26], AA6082-T6 [27], AA6016-T4 [28],  
 18 AA2024 [18, 29] and AA7075-T6 [30, 31].

19

20 The hybrid experimental-numerical approach is widely used to calibrate  
 21 the material parameters of ductile fracture criterion. In a first step, experi-  
 22 ments are carried out using various specimen shapes to determine the instant  
 23 of fracture over a wide range of stress states. Then, FE simulations of these  
 24 tests are conducted to obtain the strain field and record the evolution of the



1 stress state during the deformation process. The fracture strain is taken as  
2 the numerical equivalent plastic strain at the displacement at rupture, com-  
3 ing from the experiment, and usually at the location of the maximum value,  
4 that can be within the thickness or on the surface. Due to the variation of  
5 the stress state during the test, the corresponding parameters (e.g: stress  
6 triaxiality and Lode parameter) are generally averaged. The obtained values  
7 of fracture strain and the evolution of the variables of stress state are taken  
8 thereafter to calibrate the fracture model.

9  
10 A reliable FE model of experimental ductile fracture test that repro-  
11 duces accurately the deformation process is strongly recommended for this  
12 approach. This can be achieved by accurately modeling the material be-  
13 havior and the boundary conditions. In most of research carried out so  
14 far, efforts are focused mainly on improving the description of the material  
15 response [32, 27, 33] but no previous study has focused on the analysis of  
16 the influence of taking real boundary conditions into account in FE simu-  
17 lations on the calibration of fracture criterion parameters. Indeed, in most  
18 of the previous work, classical symmetrical boundary conditions was used  
19 by neglecting some effects that are likely to occur in experiments involving  
20 large deformations such as misalignment of specimen during test. Lou and  
21 Huh [22] observed that the strain distribution obtained experimentally from  
22 plane strain tensile specimens is not symmetric. Tang et al. [34] also ob-  
23 served that the strain distribution obtained experimentally is asymmetrical  
24 whatever the specimen shape. They claimed that it is impossible to ensure  
25 a complete alignment during the tensile test, and even a slight misalignment

1 will cause great rotation and asymmetry in the process of large plastic defor-  
2 mation. An asymmetrical strain distribution is also observed experimentally  
3 for notched specimen in the works of Lou et al. [27] and Deole et al. [23] and  
4 for plane strain tensile specimen in the work of Gruben et al. [35]. In all these  
5 cited works, authors neglected the misalignment of specimen by considering  
6 symmetric boundary conditions.

7  
8 Therefore, the main objective of this work is to investigate the effect of  
9 boundary conditions on the prediction efficiency of the hybrid experimental-  
10 numerical approach. Lou's ductile fracture criterion is used to construct  
11 the fracture locus of AA6061-T6 aluminum alloy. The ductile fracture crite-  
12 rion is calibrated by the hybrid experimental-numerical approach. Two FE  
13 models are defined: a model constrained by reproducing the real experimen-  
14 tal boundary conditions and a classical simplified model in which the ideal  
15 boundary conditions are applied. The effect of boundary conditions is inves-  
16 tigated by comparing the accuracy of the parameters of the ductile fracture  
17 criterion obtained by both models. **Furthermore, three sets of experiments**  
18 **are used to calibrate the fracture criterion. The influence of the calibration**  
19 **tests on the prediction accuracy is also investigated in this study.**

## 21 **2. Material and methods**

### 22 *2.1. Material*

23 Aluminum alloy sheet AA6061-T6 with a thickness of 1 mm is considered  
24 in this work. This material is widely used in automotive applications due to

1 its good strength to weight ratio. AA6061-T6 fails as ductile fracture with  
2 slight necking. Therefore, ductile fracture criteria based on negligible necking  
3 such as Lou’s ductile fracture criterion are more suitable to predict failure of  
4 this material [22].

5

### 6 *2.2. Tensile test*

7 To determine the mechanical properties, monotonic tensile tests are car-  
8 ried out on dog-bone specimens. Samples are designed according to ISO  
9 6892-1 standard and manufactured using water jet cutting machine. The  
10 load is measured by a load cell of 50 kN capacity. Cauchy stress is calcu-  
11 lated by the ratio of the load over the current section of the sample before  
12 necking. The logarithmic strain is measured by a field measuring system by  
13 3D Digital Image Correlation (DIC) software, Aramis [36]. **To prepare spec-**  
14 **imens for DIC, the sample surface is cleaned and spray-painted with a white**  
15 **and black stochastic pattern. Two high speed cameras equipped with 50 mm**  
16 **lenses are used to acquire the images for the DIC.** Tensile tests are conducted  
17 under extensometer-based strain control at a constant **technical** strain rate  
18 of  $\dot{\epsilon} = 10^{-3} \text{ s}^{-1}$ . To this end, an extensometer with a 25 mm gauge length is  
19 also used. To determine the material anisotropy, tensile tests are performed  
20 in the rolling direction (RD) as well as at  $45^\circ$  and  $90^\circ$  to RD.

### 21 *2.3. Ductile fracture tests*

22 Four types of specimens illustrated in Fig.1 are designed to obtain differ-  
23 ent stress states. Notched specimens with small (N-R5) and large (N-R15)  
24 notch radii are considered to achieve a high stress triaxiality [37]. Specimen

1 with a central hole (H-R4) is designed to obtain a stress state close to the  
2 uniaxial tensile test but with minor necking [38]. Finally, shear specimen  
3 (SH) is designed to achieve a low stress triaxiality [39].

4

5 All specimens are manufactured along RD using the same cutting pro-  
6 cedure as applied for the tensile test specimens. To check the machining  
7 quality, the dimensions of specimens are measured before performing tests.  
8 Low dimensional error of about 0.02 mm is found so that the effect of  
9 the real specimen geometry can be neglected. To assess the repeatability  
10 of the experiments, three samples are prepared for each geometry. All ex-  
11 periments are carried out using a universal testing machine INSTRON 5969  
12 under displacement control at a constant crosshead velocity. For each type  
13 of specimen, the crosshead speed is set to obtain an average strain rate of  
14 about  $\dot{\epsilon} = 10^{-3} \text{ s}^{-1}$ , which is the same value as in uniaxial tensile test. It  
15 should be emphasized that strain rate control can not be used in ductile  
16 fracture test since the deformation is not homogeneous in the gauge length  
17 area of the extensometer. The deformation evolution during experiments is  
18 recorded using the DIC Aramis, with the same parameters as in the tensile  
19 test. The three tests for each type of specimen lead to at least two ones  
20 with quite similar results. One test is selected for each specimen geometry  
21 to determine the corresponding fracture strain and stress state. It should be  
22 noted that in real experimental situations, the common practice is to choose  
23 the test showing the least source of error. In this work, the same practice is  
24 adopted to show that even when working in real experimental conditions the  
25 misalignment may affect the obtained results.

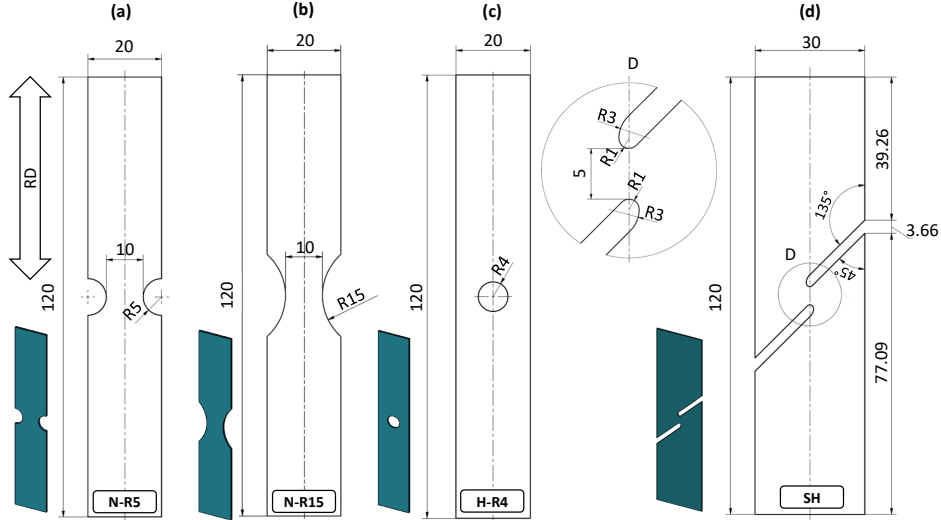


Figure 1: Geometry and dimensions (in mm) of the four specimens designed to obtain different stress states: (a) notched specimen with  $R = 5$  mm (N-R5) (b) notched specimen with  $R = 15$  mm (N-R15) (c) specimen with a central hole with  $R = 4$  mm (H-R4) (d) shear specimen (SH).

2 In order to quantify the misalignment of the sample during the test likely  
 3 to occur in this kind of experiments, by Aramis, five virtual extensometers  
 1 with a gauge length of 15 mm are defined at different positions and the evolu-  
 2 tion of the displacements of these extensometers in function of the normalized  
 3 time is recorded. A representative result is shown in Fig.2 for the testing of  
 4 a specimen with a central hole. It can be seen that the displacement at  
 5 fracture  $u_f$  strongly depends on the position of the extensometer. Therefore,  
 6 the values are averaged and the displacement at fracture  $u_f$  corresponds to  
 7 the averaged displacement  $u_{avg}$  at the fracture time  $t_f$ . It is worth noting  
 8 that the fracture time is identified as the time when a sudden drop in the

9 measured load-displacement curve is recorded.

10

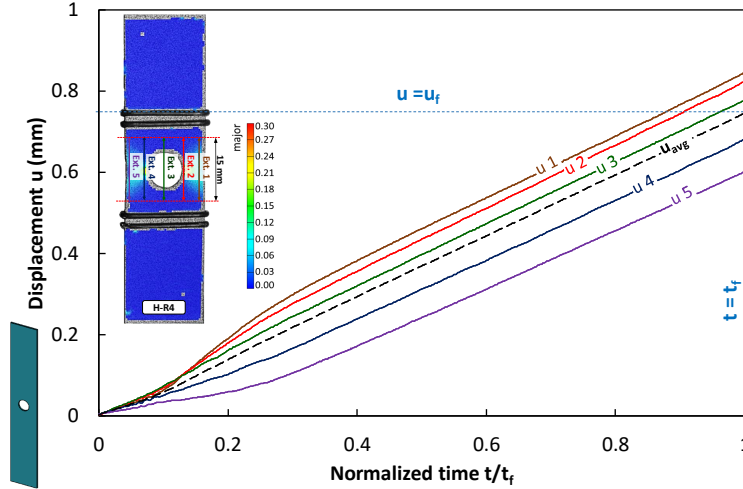


Figure 2: Evolution of displacement of the five virtual extensometers (gauge length of 15 mm) defined at different positions with Aramis as a function of time  $t$  normalized by the fracture time  $t_f$ , for a specimen with central hole H-R4.

#### 1 2.4. FE modeling

2 Numerical simulations of the different fracture ductile tests and the ten-  
3 sile test are performed in 3D with the FE code Abaqus/Standard. Attention  
4 is paid to develop a FE model as close as possible to the experimental con-  
5 ditions. For that reason, a full model of the specimen is defined to account  
6 for all possible displacements of specimen during the test. In addition, only  
7 the part of the specimen between the grips of the tensile machine is modeled  
8 in such a way that the length of the specimen in the FE model is almost  
1 equal to the distance between the grips of the tensile machine as shown in  
2 Fig.3. The specimens are discretized by 3D solid hexahedral elements with

3 reduced integration (C3D8R). Since reduced integration is used, the hour-  
4 glass control based on the total stiffness approach used by default in Abaqus  
5 is employed. Mesh with a size of approximately 0.2 mm in the local zone  
6 where strain localization is likely to occur (see the zooms in Fig.3), and with  
7 larger size at sections away from this zone is used. Since the local zone of  
8 the shear specimen is smaller than that of the other geometries, a smaller  
9 mesh size of about 0.1 mm is used for this specimen. All the models have  
10 6 elements through the thickness. Dunand and Mohr [38] have shown that  
11 the prediction of force–displacement relationship is approximately mesh size  
12 independent, but the mesh density has a noticeable effect on the predicted  
13 fracture strain. Therefore, the size of elements is determined based on con-  
14 vergence of the fracture strain. Indeed, simulation are carried out with 2,  
15 4, 6 and 8 elements through the thickness. It is found that results converge  
16 when the element number is larger than 6. For the tensile test, since experi-  
17 mentally the fracture was initiated from the edge, a tiny imperfection (0.03  
18 mm) has been done in the FE model geometry to trigger numerically the  
19 deformation localization also on the edge.

20

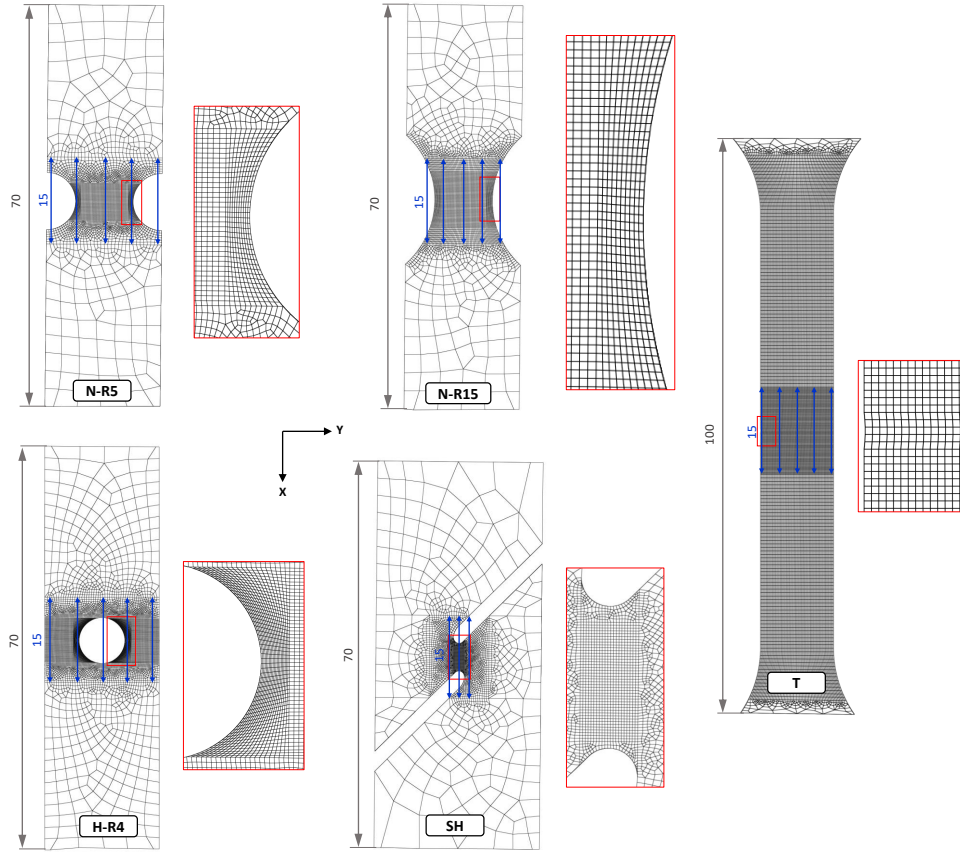


Figure 3: Meshes used for the four ductile fracture tests and the tensile test. In red, zooms on the meshes in zones where strain localization is likely to occur. The blue dimension lines highlight the position of the virtual extensometers with gauge length of 15 mm used for local displacement measurement.

1 The boundary conditions are applied in two different ways. For the first  
 2 case (model M1), non-zero displacements ( $U_x$ ,  $U_y$  and  $U_z$ ) are imposed on  
 3 the lower and upper sides of specimen as shown in Fig.4-a. These values are  
 1 obtained from the displacement field recorded by Aramis on the specimen  
 2 surface. An automatic procedure is developed to apply the experimental lo-



3 cal displacements to the FE model with a Python script. Such a procedure  
4 leads to a more realistic model, in which the misalignment of the specimen  
5 during the test is reproduced. For the second case (model M2), the nodes  
6 located on the lower side are clamped while those located on the upper side  
7 are moved along  $X$  axis with a smooth increasing displacement as shown in  
8 Fig.4-b. In this case, the model is simplified by assuming a perfect alignment  
9 of the specimen during the test and considering the conditions of a homoge-  
10 neous tensile test. For both models, five virtual extensometers with a gauge  
11 length of 15 mm are defined at the same positions of those used with Aramis  
12 as explained before, to output a local displacement used to plot the load  
13 evolution. Note that only three virtual extensometers are defined for shear  
14 specimen as shown in Fig.3.

15

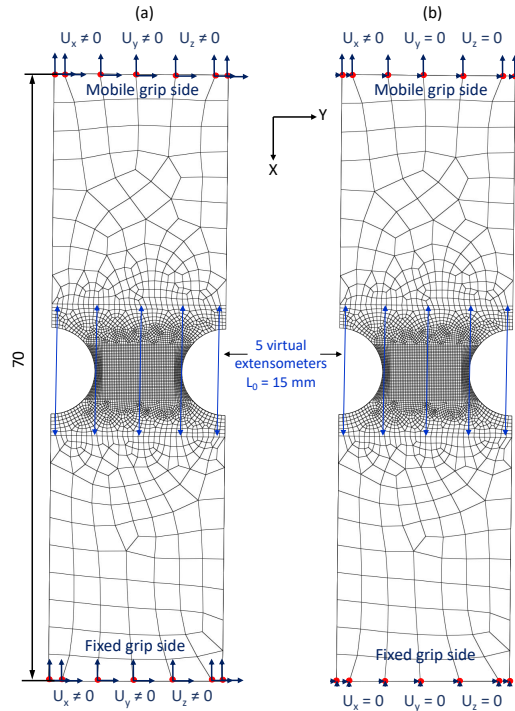


Figure 4: Boundary conditions used for (a) the representative experimental conditions test (Model M1) and (b) assuming a perfect alignment of specimen (Model M2). Red dots represent nodes where boundary conditions are applied.

1 To model the mechanical behavior, the aluminium alloy is assumed to  
 2 have an elastic-plastic behavior with an isotropic hardening rule. The anisotropy  
 3 is neglected in a first step. The material is assumed to be isotropic and to  
 4 obey the von Mises yield criterion. Before necking, the hardening curve is  
 5 obtained from the uniaxial tension test detailed in section 2.2. After necking,  
 6 the hardening curve is described by a linear piecewise relation identified by  
 7 a manual inverse method that consists of manually adjusting the hardening  
 8 curve while visually inspecting the agreement between the experimental and

9 predicted results as detailed in section 3.1. Indeed, the hardening curve is  
10 adjusted so that the simulation provides an accurate prediction of the exper-  
11 imentally measured force-displacement curve, as described by Dunand and  
1 Mohr [38] and Kacem et al. [40]. The material model is already implemented  
2 in Abaqus, with the hardening law defined in a tabular form, and the failure  
3 criterion is not incorporated in a first step.

#### 4 2.5. Calibration methodology

5 The hybrid experimental-numerical method is applied to calibrate the  
6 fracture model. Normally the fracture strain is defined as the equivalent  
7 plastic strain in the first element (integration point) with a failure indicator  
8  $D$  reaching the unity. However, the failure indicator is affected by fracture  
9 parameters  $C_1$ ,  $C_2$  and  $C_3$  which are to be identified from experimental re-  
10 sults first. This element cannot be located since the fracture parameters have  
11 not been identified yet. Therefore, it is assumed that the fracture initiates  
12 in the element with the highest equivalent plastic strain at the instant of  
13 fracture  $t_f$  (critical element). The fracture strain  $\bar{\epsilon}_f$  corresponds thus to the  
14 maximum equivalent plastic strain at the fracture stroke  $u_f$ . This assumption  
15 has been proved in previous works. Talebi-Ghadikolaee et al. [41] have shown  
16 that for sheet notched specimens the position of the element with the highest  
17 equivalent plastic strain is the same as that of the element with highest fail-  
18 ure indicator value. Lou and Huh [22] found that for specimen with central  
19 hole and shear specimen the element with the maximum fracture indicator is  
20 close to that with the largest equivalent plastic strain. They also claimed that  
21 identification method based on this assumption provides sufficient approxi-  
22 mation of fracture parameters. Therefore, to determine the fracture strain,

23 the displacement at fracture  $u_f$  is first determined experimentally. Then, the  
 24 maximum equivalent plastic strain is extracted from the numerical simula-  
 25 tion of ductile fracture test at the corresponding experimental fracture stroke  
 1  $u_f$ . Simultaneously, evolution of stress triaxiality  $\eta$  and Lode parameter  $L$  is  
 2 obtained from the numerical analysis. Although, specimens are designed to  
 3 achieve a constant stress state,  $\eta$  and  $L$  may vary during test. Therefore, to  
 4 assign a specific stress to each fracture test it is convenient to calculate the  
 5 average of stress triaxiality  $\eta_{avg}$  and Lode parameter  $L_{avg}$  by the following  
 6 relations:

$$\eta_{avg} = \frac{1}{\bar{\varepsilon}_f} \int_0^{\bar{\varepsilon}_f} \eta d\bar{\varepsilon}_p \quad \text{and} \quad L_{avg} = \frac{1}{\bar{\varepsilon}_f} \int_0^{\bar{\varepsilon}_f} L d\bar{\varepsilon}_p \quad (7)$$

7 A Python script is developed for the presented methodology. It makes it pos-  
 8 sible to determine  $(\bar{\varepsilon}_f, \eta_{avg}, L_{avg})$  for each specimen in the post-processing  
 9 phase.

10

11 The failure indicator  $D$  at the critical element can be calculated for each  
 12 test through Eq.4 by using the loading history extracted from the numerical  
 13 simulation of the tests and the fracture strain  $\bar{\varepsilon}_f$  determined by the hybrid  
 14 approach. Therefore, to calibrate the fracture criterion, the fracture param-  
 15 eters are optimized using a generalized reduced gradient (GRG) algorithm  
 16 tool by minimizing the following error function defined in the least square  
 17 sense.

18

$$Erf = \sum_{i=1}^{N_s} (1 - D_i)^2 \quad (8)$$

19 where  $N_s$  denotes the number of samples used for the calibration and  $D_i$   
 20 corresponds to the failure indicator of the  $i^{th}$  test which is calculated numer-

21 ically through Eq.4.

22

1 Three sets of experimental data are used to calibrate the fracture crite-  
2 rion: set 1 (SH, H-R4 and N-R5), set 2 (SH, H-R4 and N-R15) and set 3 (SH,  
3 H-R4, N-R15 and N-R5). For sets 1 and 2 the minimum number of tests  
4 ( $N_s = 3$ ) required to identify the fracture parameters is used whereas for set  
5 3 all fracture specimens ( $N_s = 4$ ) are employed for calibration. It should  
6 be noted that dog-bone specimen is not utilized for calibration and serves  
7 mainly the purpose of validation.

8

### 9 **3. Results and discussion**

#### 10 *3.1. Mechanical behavior in uniaxial tension and hardening*

11 Fig.5 shows the Cauchy stress-logarithmic strain curves obtained in uni-  
12 axial tension, with dog-bone specimen. It can be seen that there is no signifi-  
13 cant difference on the stress level according to the different orientations of the  
14 tensile test compared to RD. The mechanical properties are given in Tab.1.  
15 The measurement of both transverse and longitudinal strains leads to the  
16 plastic anisotropy coefficients  $r_\alpha$ , for  $\alpha = 0, 45, 90^\circ$ , also given in Tab.1. It  
17 can be seen that the normal anisotropy coefficient  $\bar{r}$  is significantly different  
18 from 1 but the planar anisotropy coefficient  $\Delta r$  is rather weak.

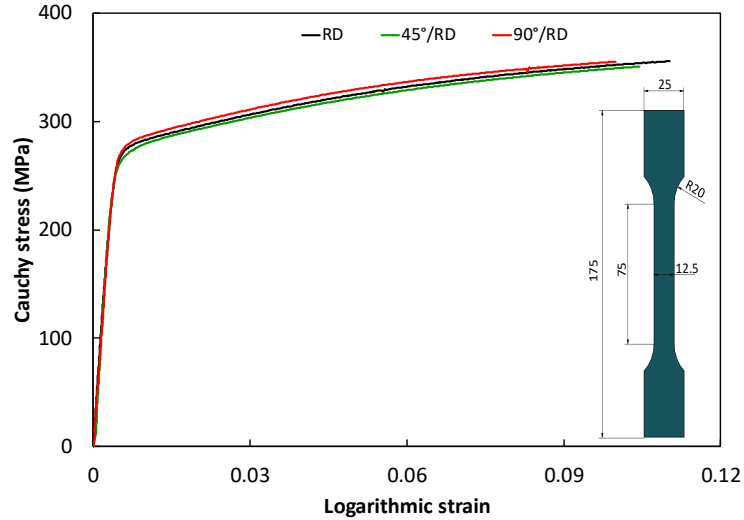


Figure 5: Cauchy stress-logarithmic strain curves in uniaxial tension obtained with dog-bone specimen up to the point of necking at 0°, 45° and 90° to the RD. Sample dimensions are given in mm.

E (GPa)	$\nu$	YS (MPa)	UTS (MPa)	$r_0$	$r_{45}$	$r_{90}$	$\bar{r}$	$\Delta r$
70	0.33	270	318	0.59	0.78	0.81	0.74	-0.08

YS Yield Strength at 0.2% plastic strain in RD UTS Ultimate Tensile Strength in RD

Table 1: Mechanical properties and anisotropy coefficients of AA6061-T6.

1 Fracture usually occurs at high strain levels, well beyond necking. There-  
2 fore, an accurate description of hardening after necking and up to fracture is  
1 fundamental in the hybrid experimental-numerical approach. Tarigopula et  
2 al. [42] claimed that the shear specimen is more suitable to determine strain  
3 hardening for large strains since it could undergo large deformation without  
4 necking. For this, the hardening curve is extrapolated manually using the

5 shear specimen which was also used by Lou and Huh [22], Tang et al. [34] and  
6 Quach et al. [43]. Indeed, the stress-strain curve used as material input is  
7 continually adjusted until the numerical and experimental load-displacement  
8 curves obtained with the shear specimen (SH) show good agreement. The  
9 finally determined stress-strain curve is utilized to describe the strain hard-  
10 ening behavior beyond necking in the FE models of all specimens. Though  
11 the comparison between tension and shear stress levels may depend on an  
12 anisotropic yield criterion, it is observed that this choice, associated to von  
13 Mises yield criterion, gives a good description of the fracture test load level.  
14 Fig.6 shows the hardening curve beyond necking modulated by the manual  
15 inverse engineering method.

16

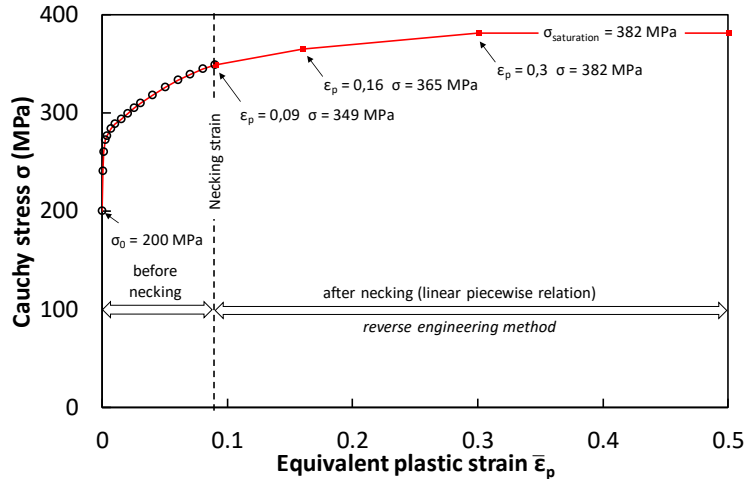


Figure 6: Hardening curve (in red) obtained from stress-strain curve using uniaxial tension of dog-bone specimen before necking and by a reverse engineering method using shear specimen after necking. Black circles represent experimental points obtained from uniaxial tension of dog-bone specimen.

1 3.2. Accuracy of FE model

2 To verify the FE models, Fig. 7 shows the load-local displacement curves  
 3 obtained both numerically with M1 and M2 models and experimentally. The  
 4 local displacement is measured based on the five extensometers with 15 mm  
 5 gauge length as depicted in Fig.4.

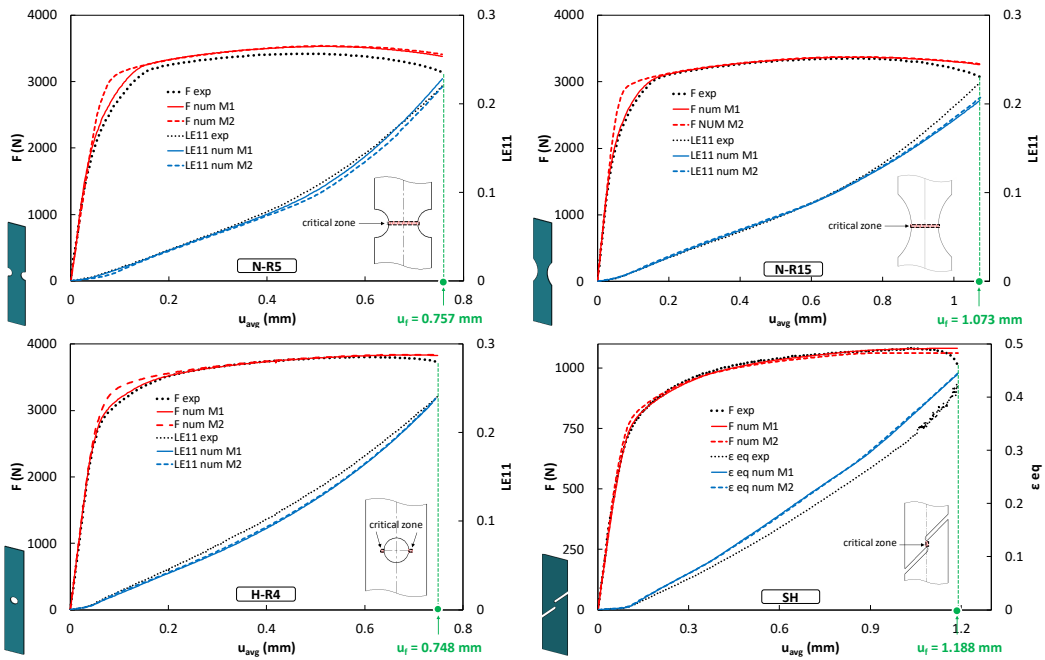


Figure 7: Comparison of the load-local displacement curves and the evolutions of average strain at the critical zone where fracture initiates (longitudinal logarithmic strain LE11 for N-R5, N-R15 and H-R4 specimens and the equivalent strain  $\varepsilon_{eq}$  for SH specimen) between numerical and experimental results. Vertical dashed green lines depict the displacement at fracture  $u_f$ .

1 It can be seen that the numerical results obtained with M1 and M2 models  
 1 fit well the experimental data, not only with the shear test used for hardening



2 extrapolation but also for all other tests. In the case of notched specimen  
 3 N-R5, the numerical simulation overestimates slightly the load. This may  
 4 be due to the dependency of the hardening behavior to the stress state that  
 5 was ignored in the numerical simulation. Fig.7 shows also the numerical and  
 6 experimental evolution of the average longitudinal logarithmic strain LE11  
 7 at the surface of the critical zone for each specimen. For the shear specimen,  
 8 the equivalent strain  $\varepsilon_{eq}$  (Eq.9) is used out of comparison's sake [36].

$$\varepsilon_{eq} = \frac{2}{\sqrt{3}} \sqrt{\varepsilon_1^2 + \varepsilon_2^2 + \varepsilon_1 \varepsilon_2} \quad (9)$$

9 where  $\varepsilon_1$  and  $\varepsilon_2$  are the logarithmic in-plane principal strain components.

10

11 As expected, the load-local displacement responses between M1 and M2  
 12 models show that numerical results with model M1 are closer to the exper-  
 13 imental results than those predicted by model M2. The difference between  
 14 both models is mainly observed for N-R5, N-R15 and H-R4 specimen, at the  
 15 beginning of the test. Indeed, the effect of misalignment on the test kinematic  
 16 is more significant at the early stage of the test, characterized by a different  
 17 velocity between the five extensometers as can be seen in Fig.2. **Moreover,**  
 18 **the misalignment causes higher stress concentration at the beginning of the**  
 19 **test leading to an early onset of plasticity which can be predicted by model**  
 20 **M1. Therefore the linear evolution in the load-displacement curve linked to**  
 21 **the elastic deformation at the beginning of test is more rapidly lost by model**  
 22 **M1.** Comparison also shows that strain evolution predicted by model M1 is  
 23 similar to that predicted by model M2 in the case of specimens N-R15, H-R4  
 24 and SH. For specimens N-R5 a minor difference is observed.

1

2        The numerical simulations are further verified by comparing the experi-  
3        mental and numerical major strain distribution on the specimen surface just  
4        before fracture, as reported in Fig. 8. The misalignment of specimen during  
5        test leads experimentally to an asymmetrical strain distribution that is also  
6        well predicted by the numerical model M1. Even though numerical model  
7        M2 does not consider the misalignment of specimen, it shows a comparable  
8        strain magnitude but the distribution is less well reproduced. For notched  
9        specimens N-R5 and N-R15, the maximum major strain recorded by Aramis  
10       is found between the center of specimen and the edge of the notch. The  
11       maximum value is located closer to the edge for N-R5 specimen and closer to  
12       the center for N-R15 specimen. This observation is also predicted by model  
13       M1 with a slight shift of maximum value towards the center. However, for  
14       model M2 the maximum major strain is usually found at the center for both  
15       specimens. For H-R4 specimen, it is observed that the major strain is more  
16       concentrated on the right side of the hole edge that is also well predicted by  
17       model M1. Note that the large deformation at the edge cannot be calculated  
18       by DIC method so that the maximum value of major strain measured by  
19       Aramis is smaller than that predicted by FE model. For shear specimen,  
20       much higher strain level is obtained. It can be clearly seen that both mod-  
21       els exhibit similar results and are in excellent agreement with experimental  
22       observations. In this case, the maximum major strain is located close to the  
23       edge where fracture experimentally initiates.

24

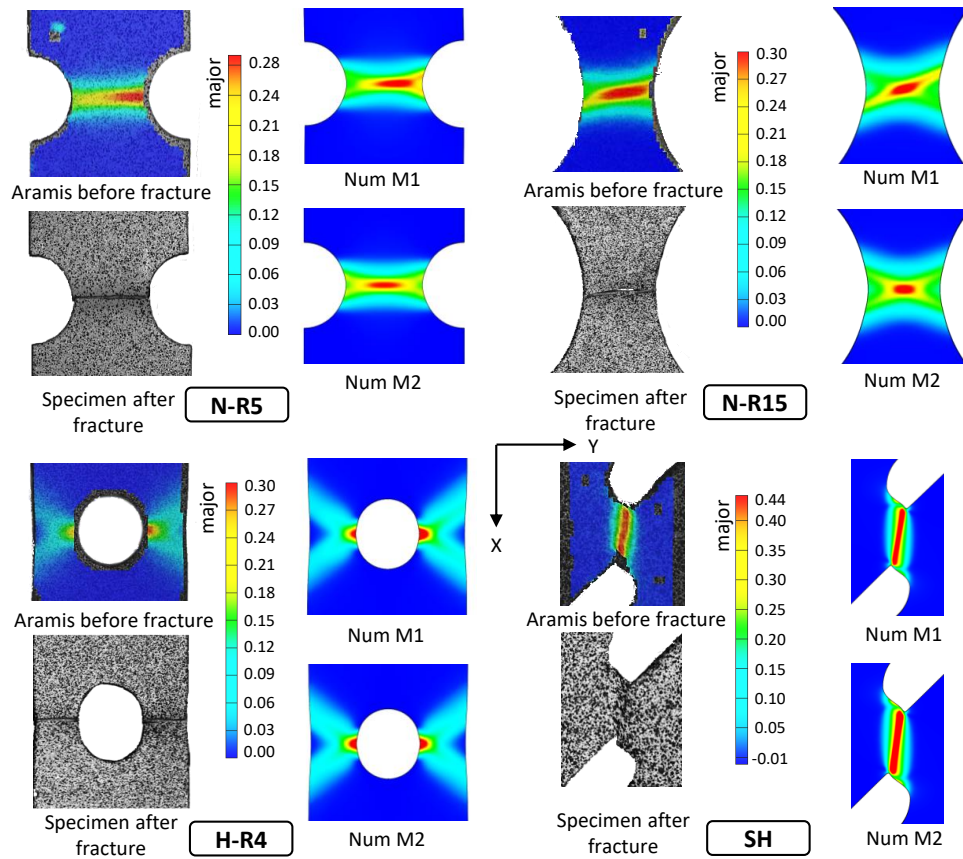


Figure 8: Comparison of major strain distributions on the specimen surface between Aramis and simulation just before fracture and specimens after fracture tests. The fracture strain is located within the thickness for N-R5, N-R15 and H-R4 specimens and at the centre of shear gauge for SH specimen.

1 The reliability of simulation is then quantitatively verified by compar-  
 2 ing the evolution of major strain along longitudinal and transverse directions  
 3 passing through the element with maximum major strain recorded by Aramis  
 1 at fracture, as depicted in Fig. 9. It can be seen that the shape of the nu-  
 2 merical and experimental curves are broadly similar. The simulations with

3 model M1 better correlated with the experiments than those with model M2  
4 for all types of specimen considered. In the case of notched specimens, a  
5 divergence is seen between numerical and experimental results for high val-  
6 ues of displacement  $u$ . At final stage ( $u = u_f$ ), the maximum major strain in  
7 transverse position is located experimentally at 3.24 mm and 0.73 mm away  
8 from the center of N-R5 and N-R15 specimens, respectively. The relative er-  
9 ror in the location of maximum major strain in transverse position predicted  
10 by models M1 and M2 for notched specimen N-R5 is 25 % and 43.5 %, re-  
11 spectively and 12.4 % and 18.8 % for notched specimen N-R15, respectively.  
12 However, in terms of maximum major strain value a good agreement between  
13 experimental and numerical results is observed. The relative error on this  
14 strain value does not exceed 6.5 % and 3.2 % for notched specimens N-R5  
15 and N-R15, respectively. In the case of specimen with central hole, the ma-  
16 jor strain is more rapidly concentrated at the localized zone than the other  
17 specimens. At the early stage ( $u = 1/4 u_f$ ) the difference between the max-  
18 imum and minimum experimental major strain values along the transverse  
19 direction is found about 0.043 which is much higher than those observed for  
20 notched specimens N-R5 and N-R15 of about 0.04 and 0.027, respectively.  
21 Numerically, the relative error on this value predicted at this stage for H-R4  
22 specimen by models M1 of about 2.5 % is lower than that predicted by model  
23 M2 of about 41.9 %. Furthermore, the relative errors on this value predicted  
24 at this stage for N-R5 and N-R15 specimens by model M1 of about 6.5 %  
25 and 22.5 %, respectively are also lower than those predicted by model M2  
1 of about 79.4 % and 67 %, respectively. The large difference between exper-  
2 imental and numerical results with model M2 observed in this case is due

3 to the misalignment of specimen leading to an early strain concentration at  
4 the edge of the notch that cannot be predicted by model M2. In the case of  
5 shear specimen, the major strain values exhibit low variation along the lon-  
6 gitudinal direction. At the half of loading process ( $u = 1/2 u_f$ ), the relative  
7 difference between the maximum and minimum values is found numerically  
8 with models M1 and M2 of about 12 % and 13 %, respectively. At the final  
9 stage ( $u = u_f$ ), the relative difference increases numerically to 30 % and 29 %  
10 for models M1 and M2, respectively but it remains experimentally constant.  
11 The difference between numerical and experimental results observed in this  
12 case may be due to the lack of experimental major strain values at the edge of  
13 the specimen where fracture initiates since Aramis cannot calculate precisely  
14 the strain at this location.

15

16 In conclusion, the comparison between numerical and experimental re-  
17 sults indicate that the numerical simulation is reliable to describe the plastic  
18 deformation of all types of specimens. Besides, as expected, numerical simu-  
19 lations with M1 describe more precisely the deformation distribution of frac-  
20 ture tests and seem therefore more suitable to calibrate the fracture criterion.

21

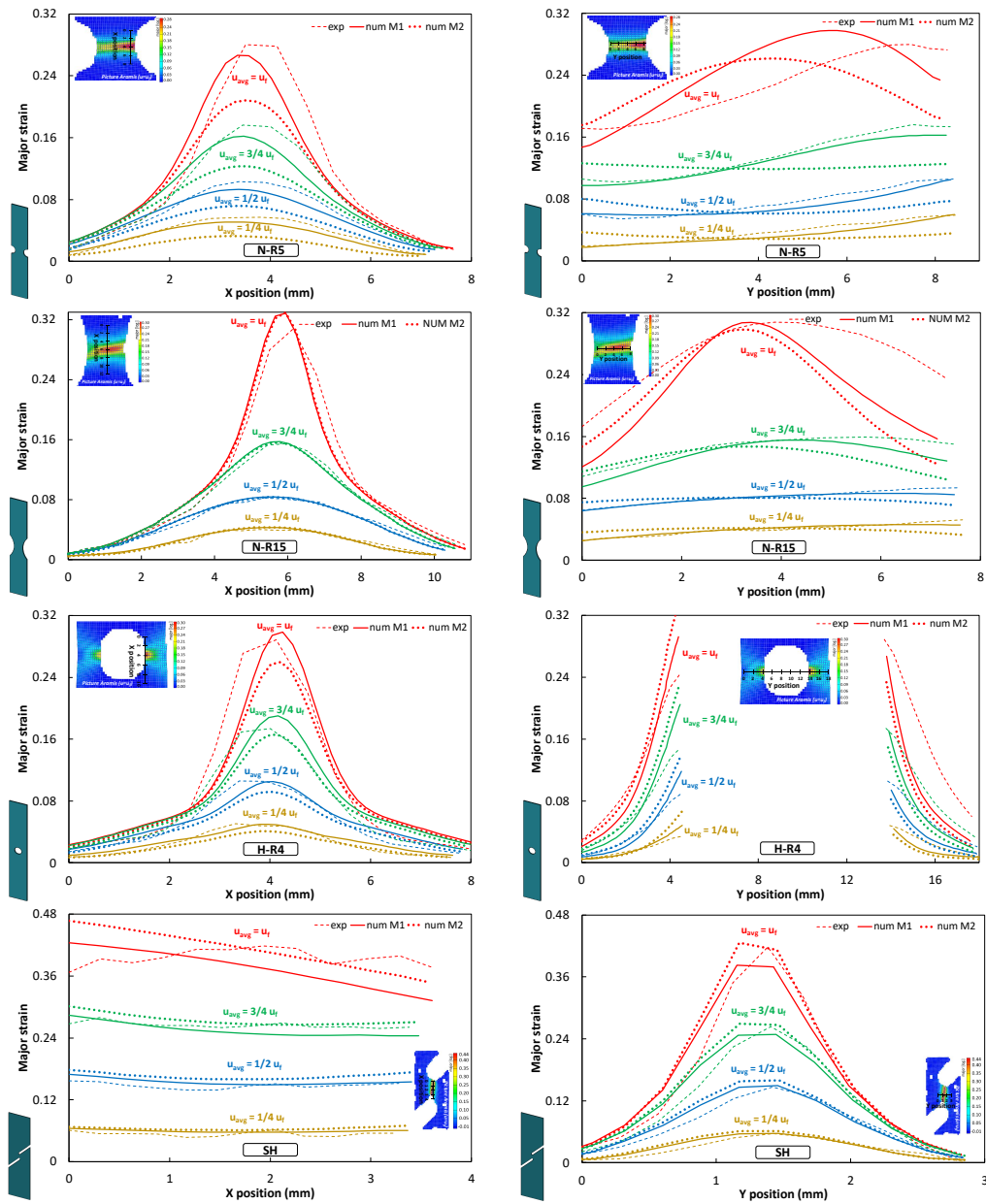


Figure 9: Evolution of major strain with X position along longitudinal direction (left) and Y position along transverse direction (right) for different local displacements, for all fracture tests. Results are taken from the nodes located along longitudinal and transverse directions passing through the element with maximum major strain recorded by Aramis.

1 *3.3. Prediction of ductile fracture*

2 The hybrid experimental-numerical approach is used to predict the frac-  
3 ture strain and the average triaxiality and Lode parameter for each type of  
4 test. The local displacement at fracture  $u_f$  is first determined experimen-  
5 tally, as shown in Fig.7. Numerically, the element presenting the maximum  
6 equivalent plastic strain at  $u_f$  (critical element) is located in the center of  
7 specimen, within the thickness for N-R5, N-R15 and H-R4 specimens. In the  
8 case of shear specimen, due to edge effect the maximum equivalent plastic  
9 strain at  $u_f$  is found at a point close to the edge rather than at the center.  
10 The critical element cannot be taken at the edge since the stress state is  
11 not a one of shear in this region. Therefore, the equivalent plastic strain at  
12 the center of the shear gauge is chosen as the fracture strain. This assump-  
13 tion was broadly applied in previous works [22]. To avoid edge effect in pure  
14 shear butterfly specimen proposed by Mohr and Henn [44] is recommended.  
15 However, this type of specimen cannot be used for thin sheets since it needs  
16 through-thickness machining. Evolution of stress triaxiality and Lode pa-  
17 rameter at the critical element is obtained from the numerical analysis as  
18 shown in Fig.10.

19

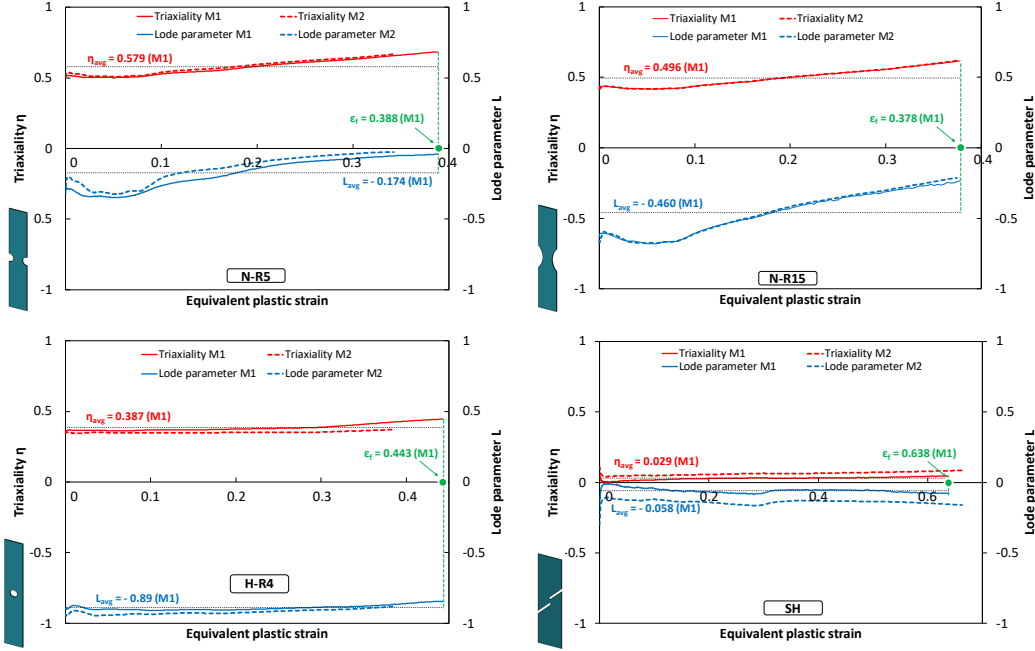


Figure 10: Evolution of stress triaxiality and Lode parameter at the critical element corresponding to the element presenting the maximum equivalent plastic strain at  $u_f$  for N-R5, N-R15 and H-R4 specimens and selected at the center of the shear gauge for SH specimen for models M1 and M2. Horizontal dashed black lines show average triaxiality  $\eta_{avg}$  and Lode parameter  $L_{avg}$  while vertical dashed green line depicts the fracture strain only for model M1 for clarity purpose.

1 It is found that the values of triaxiality and Lode parameter calculated for  
 2 N-R5 and N-R15 specimens are not stable and exhibit significant variation  
 3 during plastic deformation. This is due to the localized necking leading to  
 4 the development of out of plane stress components in the critical zone that  
 5 increases the stress triaxiality and modifies the evolution of Lode parameter.  
 6 In the case of SH and H-R4 specimens small variations of triaxiality and



7 Lode parameter are obtained since these specimens are characterized by mi-  
8 nor necking. For instance, for notched specimen N-R15 the Lode parameters  
9 values predicted by model M1 varies between  $-0.714$  and  $-0.232$  correspond-  
10 ing to an absolute difference of 0.482 while those predicted by the same model  
11 for H-R4 specimen varies between  $-0.911$  and  $-0.845$  corresponding to an  
12 absolute difference of 0.066. The absolute difference in stress triaxiality pre-  
13 dicted by model M1 for N-R15 and H-R4 specimens are respectively  $0.21$  and  
14  $0.087$ .

15

16 Triaxiality and Lode parameter variation obtained by models M1 and M2  
17 are also compared in Fig.10. It can be seen that both variations are similar  
18 in the case of N-R15 specimen but slightly different for other fracture test  
19 specimens. The largest difference is observed in the Lode parameter of SH  
20 specimen.

21

22 The average stress triaxiality  $\eta_{avg}$  and Lode parameter  $L_{avg}$  are then cal-  
23 culated according to Eq.7. The values of fracture strain  $\bar{\epsilon}_f$  and the corre-  
24 sponding average triaxiality  $\eta_{avg}$  and Lode parameter  $L_{avg}$  are listed in Tab.2.  
25 The average triaxiality  $\eta_{avg}$  and Lode parameter  $L_{avg}$  are also included with  
1 dashed lines in Fig.10 only for model M1 for clarity purpose.

2

		$\bar{\epsilon}_f$	$\eta_{avg}$	$L_{avg}$
N-R5	Model M1	0.388	0.579	-0.174
	Model M2	0.342	0.578	-0.148
N-R15	Model M1	0.378	0.496	-0.460
	Model M2	0.372	0.497	-0.455
H-R4	Model M1	0.443	0.387	-0.890
	Model M2	0.387	0.353	-0.920
SH	Model M1	0.638	0.029	-0.058
	Model M2	0.663	0.063	-0.138

Table 2: Fracture strain and the corresponding average stress triaxiality and Lode parameter.

3 It can be seen that fracture strain predicted by model M2 is lower than  
4 that predicted by model M1 for specimens N-R5, N-R15 and H-R4. The  
5 difference is about 13% for specimens N-R5 and H-R4 and 2% for specimen  
6 N-R15. For SH specimen, a minor difference of fracture strain between both  
7 models of about 4% is observed. Regarding the stress state, it is found that  
8  $\eta_{avg}$  and  $L_{avg}$  values are almost similar for both models of specimens N-R5,  
9 N-R15 and H-R4. However, a significant difference is observed in case of  
10 SH specimen. Indeed, the average values obtained from model M1 are closer  
11 to the pure shear state ( $\eta = 0$  and  $L = 0$ ) than those obtained from model M2.

12

### 1 3.4. Determination of fracture locus

2 Since the loading paths are non-linear, the values of  $\bar{\epsilon}_f$ ,  $\eta_{avg}$  and  $L_{avg}$   
3 determined by the hybrid experimental-numerical approach are firstly used  
4 to estimate an initial guess of the material parameters  $C_1$ ,  $C_2$  and  $C_3$  of Lou's  
5 fracture criterion. Then the final values of fracture criterion parameters are  
6 obtained by using the integral expression for the non-linear loading path ac-  
7 cording to Eq.4 to construct the fracture locus of AA6061-T6 aluminum alloy.

8  
9 Three sets of calibration tests are used to calibrate the fracture criterion  
10 as explained in section 2.5. Tab.3 shows the calibration results for models  
11 M1 and M2. It should be noted that results obtained by model M2 with all  
12 sets are not realistic since they lead to negative values of fracture parameters.  
13 For that reason, the calibration for model M2 is performed otherwise by con-  
14 straining  $C_1$ ,  $C_2$  and  $C_3$  to be positive and only set 3 is considered in this case.

15  
16 It is found that the calibration result depends strongly on the set of ex-  
17 periments used for calibration that was also concluded in previous works by  
18 Deole et al.[23] and Yang et al.[30]. The low value of  $C_1$  obtained in most of  
19 the cases means that the Lode parameter has a weak effect on the fracture  
20 strain. This was also observed for DH36 steel [45], 5083-H116 aluminum al-  
21 loy [46] and 5083-O aluminum alloy [47]. Moreover, since the material used  
22 in this work exhibits a weak Lode parameter dependency, the calibration of  
23 a Lode parameter dependent ductile fracture criterion may fail for this ma-  
24 terial mainly when it is used with the ideal model M2. This highlights again  
25 the importance of considering the real boundary conditions in the simulation  
1 of fracture test.

		$C_1$	$C_2$	$C_3$
M1	set 1	0.0538	0.5383	0.4627
	set 2	0.8076	0.6661	0.4768
	set 3	0.1588	0.5725	0.4593
M2	set 3	0	0.7887	0.4306

Table 3: Calibrated fracture parameters with the three sets of experiments for model M1 (set 1 (SH, H-R4 and N-R5), set 2 (SH, H-R4 and N-R15) and set 3 (SH, H-R4, N-R15 and N-R5)) and with set 3 for model M2.

3 An error indicator  $\delta$  is used to evaluate the prediction accuracy of material  
4 parameters obtained by each set:

$$\delta = \frac{|D_{cri} - D_{pred}|}{D_{cri}} \cdot 100\% \quad (10)$$

5 where  $D_{cri}$  is the critical value of  $D$  which is supposed to be unity in this  
6 work and  $D_{pred}$  is the value of  $D$  in the critical element at the fracture stroke.

7

8 Tab.4 shows the prediction error for models M1 and M2. For model M1,  
9 low values of mean error are obtained for all sets of experiments. The min-  
10 imum mean error of 1.91 % is obtained by using the first set of calibration  
11 tests. It is also found that calibration with model M2 leads to an acceptable  
12 mean error of 3.82 % but it remains higher than that predicted by model  
13 M1 using the same set of experiments (2.49 %). It should be noted that the  
14 prediction error for model M2 can be calculated otherwise by setting the real  
15 model M1 as a reference. In this case the failure indicator  $D$  is calculated  
1 by using the FE model of M1 in which the fracture parameters calibrated by

2 model M2 are incorporated. The mean error obtained in this case is 9.39 %  
3 which is very higher than those predicted by model M1. This indicates that  
4 real model M1 should be considered to calibrate ductile fracture criterion  
5 with high accuracy.

6

			N-R5	N-R15	H-R4	SH	T (validation)
M1	set1	$D_{pred}$	1	0.924	1	1	0.984
		error (%)	-	7.64	-	-	1.57
		mean error (%)	1.91				-
	set2	$D_{pred}$	1.12	1	1	1	1.004
		error (%)	12.04	-	-	-	0.43
		mean error (%)	3.01				-
	set3	$D_{pred}$	1.033	0.948	1.013	1.002	1.0002
		error (%)	3.32	5.18	1.3	0.17	<b>0.02</b>
		mean error (%)	<b>2.49</b>				-
M2	set3	$D_{pred}$	1.018	1.033	0.919	1.021	1.072
		error (%)	1.79	3.32	8.07	2.11	7.23
		mean error (%)	3.82				-

Table 4: Failure indicator  $D$  predicted in the critical element at the fracture stroke and prediction errors (Eq.10) of the three sets of experiments for model M1 and of set 3 for model M2.

7 Fig.11 shows the locus of fracture strains in the 2D space  $(\eta, \bar{\epsilon}^p)$  under  
8 the plane stress condition. The  $(\eta_{avg}, \bar{\epsilon}_f)$  points obtained by the hybrid ex-  
9 perimental approach using models M1 and M2 are superimposed in Fig.11.  
10 It can be seen that the fracture locus is strongly dependent on the used  
11 model and calibration tests which witness the high sensitivity of the hybrid

2 experimental-numerical approach to the boundary conditions adopted and  
 3 to the set of tests used for calibration. Comparison between both models re-  
 4 veals that model M1 fits more accurately the results obtained by the hybrid  
 5 approach. Therefore, it can be concluded that model M1 is more suited than  
 6 model M2 for the calibration of ductile fracture criterion.

7

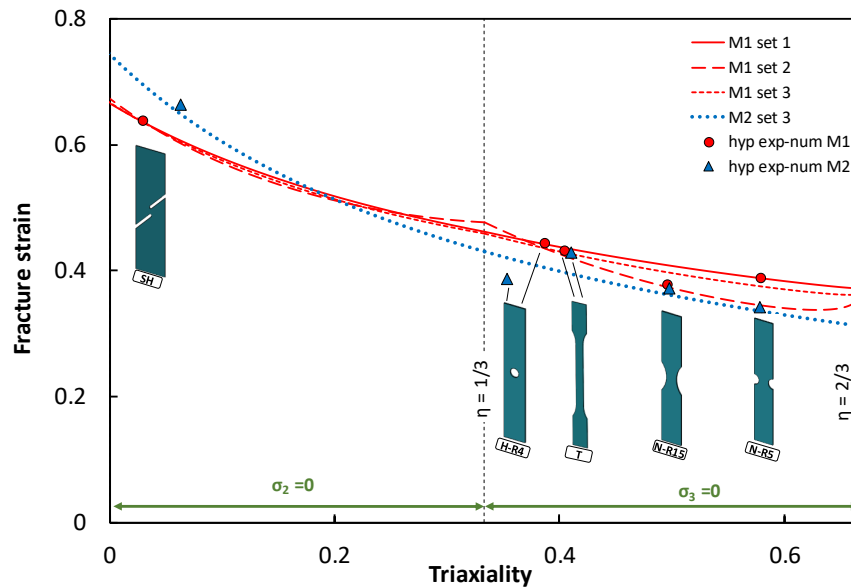


Figure 11: Fracture locus constructed in the space  $(\eta, \bar{\varepsilon}^p)$  under the plane stress condition using model M1 (set 1, set 2 and opt) shown with red lines and model M2 (opt) shown with blue line. The  $(\eta_{avg}, \bar{\varepsilon}_f)$  points obtained by the hybrid experimental-numerical approach using models M1 and M2 are shown with red and blue dots, respectively.

1 It can also be seen that for N-R15 specimen data points obtained by the  
 2 hybrid approach by both models are very close to each other. The effect  
 3 of considering the real boundary conditions in N-R15 specimen seems to be

4 lower than other specimens as can also seen in Fig. 7,9 and 10. Therefore N-  
1 R15 specimen is not really interesting to accurately model the real boundary  
2 conditions and could be replaced by other specimen (e.g N-R10).

### 3 3.5. Validation of fracture locus

4 Tensile tests on dog-bone shaped specimens are used for validation. Fig.12  
5 shows the numerical and experimental force-displacement curves. It should  
6 be noted that both models M1 and M2 predict similar result of the force-  
7 displacement curve. For that reason, only the numerical curve predicted by  
8 model M1 is presented in Fig.12 for clarity purpose. Good agreements be-  
9 tween experimental and numerical results is observed which verified the FE  
10 models. Fig.12 shows also the longitudinal logarithmic strain LE11 distribu-  
11 tions on the specimen surface just before fracture obtained experimentally by  
12 Aramis and numerically by Models M1 and M2. It is obvious that both mod-  
13 els predict accurately the location of necking zone observed in this case at  
14 the edge which demonstrates the reliability of the FE models. It is also found  
15 that the strain distribution predicted by model M1 is closer to the experi-  
16 mental strain distribution than that predicted by model M2 which confirms  
17 once again that model M1 is more suitable to calibrate the fracture criterion.

18  
19 The  $(\eta_{avg}, \bar{\epsilon}_f)$  points obtained by the hybrid experimental approach using  
20 models M1 and M2 are superimposed in Fig.11. The data point obtained by  
21 the hybrid approach using model M1 is closer to the fracture locus than that  
22 obtained using model M2. The prediction errors are reported in Tab.4. For  
23 all sets of experiments the prediction error is smaller than 1.57% for model  
24 M1. The error is close to zero for set 3. However higher prediction error of

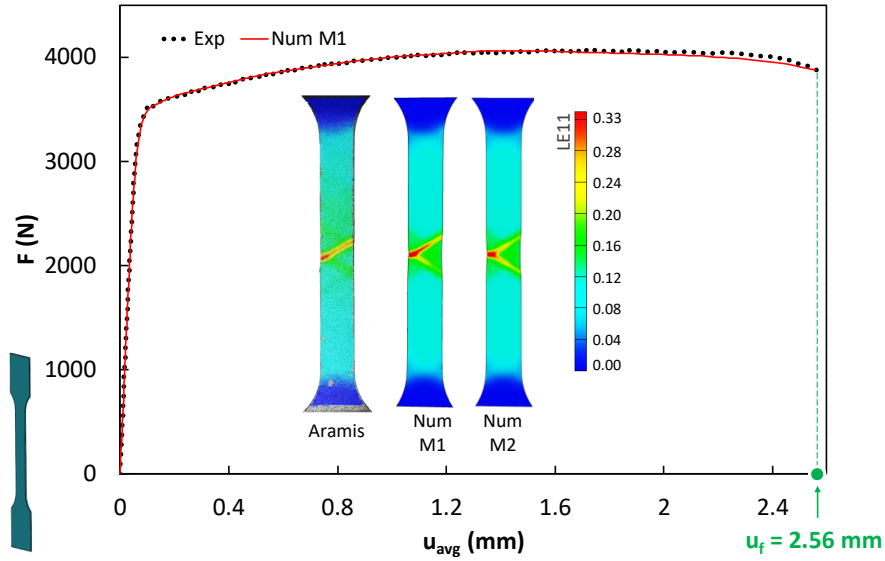


Figure 12: Comparison of the load-local displacement curves and the longitudinal logarithmic strain LE11 distributions on the specimen surface just before fracture for tensile specimen between numerical and experimental results.

25 about 7.23% is found for model M2. This indicates again that model M1 is  
 1 more suited than model M2 for the calibration of ductile fracture criterion  
 2 which further validates the obtained results.

#### 1 4. Conclusion

2 In this study, the hybrid experimental-numerical approach is used to cal-  
 3 ibrate Lou's fracture criterion for AA6061-T6 aluminum alloy. Special em-  
 4 phasis is put on the influence of boundary conditions on the accuracy pre-  
 5 iction of this approach. To this end, numerical simulations are carried out  
 6 with and without considering some experimental aspects like misalignment of  
 7 specimen. The comparison between models and experiments shows that the



8 model constrained by experimental boundary conditions describes more pre-  
9 cisely the deformation processes of the fracture tests. Moreover, it is found  
10 that experimental boundary conditions have a significant effect on the frac-  
11 ture strain and minor influence on the stress states (i.e stress triaxiality and  
12 Lode parameter). **In addition, the effect of the calibration test is investigated.**  
13 **It is found that all sets of fracture tests leads to highly accurate results with**  
14 **model correctly constrained.** The obtained results are verified using tensile  
15 **test performed until fracture which confirms that model correctly constrained**  
16 **is more suited for calibration of ductile fracture criterion.**

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