

Graph Neural Network-Based Pipeline for Track Finding in the Velo at LHCb

Anthony Correia, Fotis I Giasemis, Nabil Garroum, Vladimir Vava Gligorov, Bertrand Granado

▶ To cite this version:

Anthony Correia, Fotis I Giasemis, Nabil Garroum, Vladimir Vava Gligorov, Bertrand Granado. Graph Neural Network-Based Pipeline for Track Finding in the Velo at LHCb. Connecting The Dots 2023 (CTD 2023), Oct 2023, Toulouse, France. pp.PROC-CTD2023-34. hal-04614040

HAL Id: hal-04614040 https://hal.science/hal-04614040v1

Submitted on 17 Jun 2024

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.



Graph Neural Network-Based Pipeline for Track Finding in the Velo at LHCb

Anthony Correia¹, Fotis I. Giasemis^{1,2}, Nabil Garroum¹, Vladimir Vava Gligorov¹, Bertrand Granado²

¹ LPNHE, Sorbonne Université, CNRS/IN2P3, Paris, France

² LIP6, Sorbonne Université, CNRS, Paris, France

On behalf of the LHCb real-time analysis project

ABSTRACT

Over the next decade, increases in instantaneous luminosity and detector granularity will amplify the amount of data that has to be analysed by high-energy physics experiments, whether in real time or offline, by an order of magnitude. The reconstruction of charged particle tracks, which has always been a crucial element of offline data processing pipelines, must increasingly be deployed from the very first stages of the real time processing to enable experiments to achieve their physics goals. Graph Neural Networks (GNNs) have received a great deal of attention in the community because their computational complexity scales nearly linearly with the number of hits in the detector, unlike conventional algorithms which often scale quadratically or worse. This paper presents ETX4VELO, a GNN-based track-finding pipeline tailored for the Run 3 LHCb experiment's Vertex Locator, in the context of LHCb's fully GPU-based first-level trigger system, Allen. Currently implemented in Python, ETX4VELO offers the ability to reconstruct tracks with shared hits using a novel triplet-based method. When benchmarked against the traditional track-finding algorithm in Allen, this GNN-based approach not only matches but occasionally surpasses its physics performance. In particular, the fraction of fake tracks is reduced from over 2% to below 1% and the efficiency to reconstruct electrons is improved. While achieving comparable physics performance is a milestone, the immediate priority remains implementing ETX4VELO in Allen in order to determine and optimise its throughput, to meet the demands of this high-rate environment.

PRESENTED AT

Connecting the Dots Workshop (CTD 2023) October 10-13, 2023

1 Introduction

The LHCb Run 3 detector [1] is a multi-purpose particle physics detector at the Large Hadron Collider (LHC). Proton bunches collide every 25 ns within its Vertex Locator (Velo). The resulting particles are detected in a forward region near the beamline, specifically within the acceptance region defined by $\eta \in [2, 5]$, where η represents the pseudo-rapidity.

Central to the LHCb is its tracking system, illustrated in Figure 1. This system consists of:

- The Vertex Locator (Velo) [2], surrounding the proton-proton interaction region, encompasses $n_{\text{planes}} = 26$ planes of $55 \times 55 \ \mu\text{m}^2$ silicon pixels.
- The **Upstream Tracker (UT)** [3], placed before the magnet station, includes 4 planes of silicon strips.
- The **Scintillating Fibre Tracker (SciFi)** [3], located after the magnet station, is composed of 12 planes of scintillating fibres.

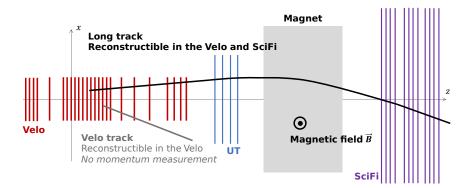


Figure 1: Sketch of the LHCb tracking system in Run 3.

The LHCb subdetectors collectively produce a data rate of up to 5 TB/s. To curtail this before storage during Run 3, LHCb deployed Allen, a GPU-based online trigger [4], which trims the rate to a more manageable 70-200 GB/s. Using around 340 GPUs, Allen partially reconstructs events, achieving better selection efficiency than the FPGA-based hardware trigger used by LHCb during Run 1 and Run 2. The data is then buffered for real-time alignment and calibration before a second, x86-based trigger performs a full event reconstruction and selects events containing physics signals of interest for analysis. This refined data is then stored at a rate of 10 GB/s.

In this environment, Allen and LHCb offers a pragmatic platform for developing Neural Network-based algorithms on GPUs, with a specific emphasis on high-throughput. Using Allen's existing GPU algorithms as a reference, the track-finding algorithms in development can be refined and compared both in terms of physics and throughput performance.

This paper introduces ETX4VELO, a Graph Neural Network (GNN)-based track-finding pipeline for the Velo. It is based on the Exa.TrkX collaboration's approach [5], which was originally tailored for 4π tracking detectors in a magnetic field, akin to ATLAS and CMS, in the context of the High-Luminosity upgrade of the LHC (HL-LHC). Crucially, the Exa.TrkX pipeline exhibited a near-linear relationship between throughput and hit count, contrasting with the quadratic nature of conventional algorithms. This is of particular interest in the context of LHCb's upcoming upgrades, which will enhance instantaneous luminosity and detector granularity.

2 Track Topologies in the Velo

In simulation, there are, on average, 150 particles in the Velo acceptance to reconstruct, and 2,200 hits per event. Around 15% of the hits are spilled over from prior events and are therefore noise.

The Velo tracks exhibit the following key characteristics:

- Linear Trajectories: The tracks are straight lines as there is no magnetic field within the Velo.
- Reconstructibility Criterion: A track is deemed reconstructible in the Velo if it leaves hits in at least three Velo layers [6].
- Forward Orientation: The tracks to be reconstructed are forward-oriented, with $\eta \in [2, 5]$, for interaction with subsequent LHCb subdetectors. Although backward-oriented tracks (with negative η) are also relevant, particularly for primary vertex reconstruction, they are not evaluated in this paper.
- Skipped Plane: In simulations, a particle may skip a plane in 1% of cases, attributed to the inefficiency of the detector plane.
- Multiple Hits per Plane: A track can generate more than one hit per plane.*
- Shared Hits: Tracks may intersect, leading to a shared hit.
- **Positron-Electron Pairs:** Material interactions frequently produce positron-electron pairs, resulting in two tracks that initially share hits before diverging.

Given these characteristics, an effective track-finding algorithm for the Velo should be capable of reconstructing the particle tracks illustrated in Figure 2.

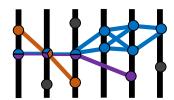


Figure 2: Simplified example of tracks to be reconstructed in the Velo. The blue and purple tracks share three hits prior to diverging. The purple track jumps from plane 3 to 5, missing 4. The orange track intersects the blue and purple tracks. Dark points represent hits unassociated with any particle. When considering the hits as graph nodes, lines between hit nodes represent the genuine edges, as defined in this work.

3 ETX4VELO Pipeline

This section outlines ETX4VELO, a five-step track-finding pipeline, as illustrated in Figure 3.

- 1. Hit Graph Construction: A preliminary directed graph of connected hits $G_{\text{rough}}^{\text{hit}}$ is built. The target edges are connections between hits from the same particle on adjacent planes. The hit coordinates are embedded using a Dense Neural Network (DNN) and the edges are built by local k-Nearest Neighbours (k-NN) applications. Further details are in Section 3.1.
- 2. Edge Classification: A GNN scores the edges in $G_{\text{rough}}^{\text{hit}}$ between 0 (fake) and 1 (genuine). Those below $s_{\text{edge, min}}$ are discarded, forming the purified hit graph $G_{\text{purified}}^{\text{hit}}$. Further details are in Section 3.2.
- 3. Edge Graph Construction: An edge graph, G^{edge} , is derived from $G^{\text{hit}}_{\text{purified}}$. Here, nodes of G^{edge} are edges from $G^{\text{hit}}_{\text{purified}}$ and two edges connect if they share a hit. The edge-edge connections, are called *triplets* since they involve three hits. Further details are in Section 3.3.
- 4. **Triplet Classification**: Triplets within G^{edge} undergo classification. Those scoring below $s_{\text{triplet, min}}$ are removed, producing the purified edge graph $G^{\text{edge}}_{\text{purified}}$. Further details are in Section 3.4.
- 5. Track Construction: The tracks are reconstructed from the purified edge graph $G_{\text{purified}}^{\text{edge}}$ through an algorithm involving a Weakly Connected Component (WCC) stage, as detailed in Section 3.5.

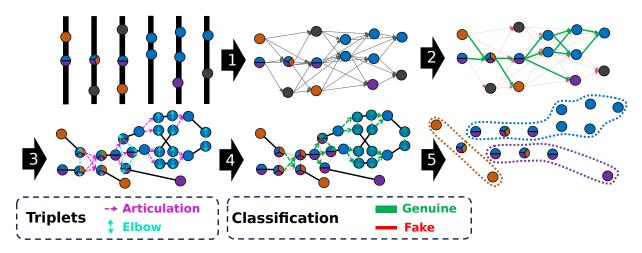


Figure 3: Illustration of the pipeline's 5 stages, beginning with hits from the minimalist example in Figure 2. Steps entail (1) building a rough hit graph, (2) classifying its edges and discarding fakes (in red), (3) constructing the edge graph with edge-to-edge connections called triplets, (4) classifying and removing fake triplets, and finally, producing the tracks.

Compared to the Exa.TrkX pipeline, which directly follows its first two stages with a WCC algorithm, ETX4VELO introduces three additional stages to handle tracks with shared hits.

3.1 Rough Graph Construction

To limit the graph size, edges created during the graph construction stage are permitted to skip at most one plane. Edges are also directed towards increasing plane number (and z-coordinate).

Initially, the hit coordinates $(r, \phi, z, \text{plane number})^{\dagger}$ are normalised and input into a DNN. This DNN embeds hits into a n_{dim} -dimensional space, set as $n_{\text{dim}} = 4$, designed to bring connected hit pairs closer while distancing disconnected ones. The embedding DNN comprises 3 hidden layers of 128 hidden units with hyperbolic tangent activation, each followed by a normalisation layer, and an output layer without activation. In total, the network has approximately 35,000 parameters.

The rough graph $G_{\text{rough}}^{\text{hit}}$ is built by identifying the k_{max} -nearest neighbours (in the embedding space) of every hit in plane $p \in [\![1,n_{\text{planes}}-1]\!]$, constrained within the subsequent two planes p+1 and p+2, and a maximum squared distance of d_{max}^2 . Practically, a k_{max} -Nearest Neighbour (k_{max} -NN) algorithm implemented in faiss [7] determines hits' neighbours between plane p and planes p+1 and p+2. Only neighbours within the d_{max}^2 boundary are retained. The values of k_{max} and d_{max}^2 are optimisable parameters.

For training the DNN, a dataset consisting of (1) random hit pairs, (2) all edge-connected hit pairs, and (3) challenging fakes identified by the 25 local k_{max} -NN procedure with $k_{\text{max}} = 50$ and $d_{\text{max}}^2 = 0.015$, is utilised. This results in a dataset of n_{genuine} connected hits and n_{fake} disconnected ones. The distances $\{d_{\text{genuine},i}, \forall i \in [\![1,n_{\text{genuine}}]\!]\}$ and $\{d_{\text{fake},j}, \forall j \in [\![1,n_{\text{fake}}]\!]\}$ between the embedded genuine and fake hit pairs, respectively, are then computed.

The DNN training minimises a pairwise hinge embedding loss defined as

$$\mathcal{L} = \mathcal{L}_{\text{fake}} + w_{\text{genuine}} \times \mathcal{L}_{\text{genuine}}, \tag{1}$$

with a weight $w_{\text{genuine}} = 3$ to emphasise genuine edge inclusion over fake edge exclusion. The optimization of hyperparameters such as m and w_{genuine} will be pursued in future work.

^{*}A Velo plane consists of four overlapping sensor layers, displaced in z, collaboratively covering the desired acceptance in the (x, y) plane. Multiple hits on a plane primarily arise from different overlapping sensor layers within a plane.

[†]Later analyses showed omitting the plane number from DNN input did not affect performance.

The objective of the following loss equations is to reduce the distance between connected hits and increase the distance (up to a threshold m) between disconnected ones:

$$\mathcal{L}_{\text{genuine}} = \frac{1}{n_{\text{genuine}}} \sum_{i=1}^{n_{\text{genuine}}} d_{\text{genuine},i}^2 \quad \text{and} \quad \mathcal{L}_{\text{fake}} = \frac{1}{n_{\text{fake}}} \sum_{j=1}^{n_{\text{fake}}} \max \left(0, m - d_{\text{fake},j}^2\right), \tag{2}$$

with the margin m fixed at 0.010.

3.2Edge Classification

The edges are classified using a GNN that incorporates a 6-step message passing mechanism. Notably, the message-passing aggregation scheme has been updated from the original Exa. TrkX pipeline. The architecture of this GNN is illustrated in Figure 4.

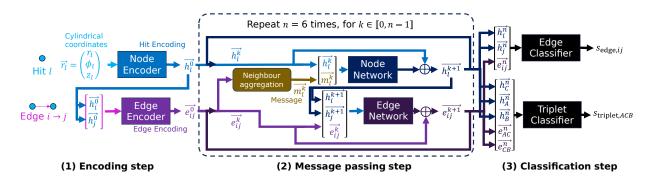


Figure 4: Schematic of the GNN architecture, highlighting: (1) hit and edge encodings, (2) iterative message passing refinement, and (3) subsequent edge and triplet classifications. The node and edge encoders and networks and the edge and triplet classifiers are DNNs.

Each hit, denoted as l, is encoded from its normalised cylindrical coordinates $r_l = (r_l, \theta_l, z_l)$ through a 3-layer DNN (hit encoder) into a 256-dimensional representation, denoted as h_l^0 .

For every edge connecting hits i and j, its 256-dimensional encoding e_{ij}^0 is formed by concatenating the associated hit encodings h_i^0 and h_i^0 , which is then processed through a 3-layer DNN (edge encoder).

During the n-step message passing phase, with n=6, at each step $k \in [0, n-1]$, a message vector m_l^k is derived for every hit l. The message vector aggregates encodings from both its preceding (left, $q_L \to l$) and succeeding (right, $l \to q_R$) edges. Specifically:

$$m_l^k = \left[\max\left(\left\{ e_{q_L l}^k \right\}_l \right), \, \operatorname{sum}\left(\left\{ e_{q_L l}^k \right\}_l \right), \, \max\left(\left\{ e_{l q_R}^k \right\}_l \right), \, \operatorname{sum}\left(\left\{ e_{l q_R}^k \right\}_l \right) \right]. \tag{3}$$

This distinct aggregation for preceding and succeeding planes enhances performance. After message derivation, the hit encodings h_l^k upgrade to h_l^{k+1} using a 3-layer DNN (node network). This network features a residual connection and ingests the current hit encoding h_l^k and the message m_l^k . Similarly, edge encodings e_{ij}^k are refined using a 6-layer DNN (edge network) with a residual connection, from the refined hit encodings h_i^{k+1} and h_j^{k+1} alongside the current edge encoding e_{ij}^k .

After message passing, each edge between hits i and j is scored between 0 (indicative of fakeness) and 1 (indicative of genuineness) by a 3-layer DNN (edge classifier) using the refined hit encodings h_i^n and h_i^n and edge encodings e_{ij}^n . Only those surpassing the score threshold, $s_{\rm edge,\; min}$, persist in the purified hit graph $G_{\text{purified}}^{\text{hit}}$.

All the DNNs have 256 hidden units per layer and use the SiLU activation [8], each followed by a normalisation layer. The output layers of the classifiers deploy a sigmoid activation.

The GNN training encompasses the triplet classifier, which is detailed further in Section 3.4. In total, it has approximately two million parameters.

3.3 Edge Graph Construction

Applying a WCC algorithm directly to the hit graph results in tracks that share common hits being merged. This is particularly detrimental for positron-electron pairs that share their first hits before diverging, as detailed in Section 2. This leads to an unsatisfactory electron track-finding performance.

The hit graph, by its construction, only encodes hit-to-hit connections and lacks the capability to disentangle tracks that share hits. Transitioning to connections between the edges themselves offers a solution. Thus, we introduce the edge graph G^{edge} , where nodes correspond to the edges from the hit graph, and connect if their corresponding edges share a common hit.

An edge-edge connection in this graph represents a set of two edges connected by a shared hit C, and is therefore called triplets [9]. Considering the directionality of these edges (towards increasing plane numbers), the triplets in the edge graph can be categorised into three types, visually depicted in Figure 5:

- Articulation: Two sequential edges $A \to C$ and $C \to B$, maintaining the order plane_A < plane_C < plane_B.
- Left Elbow: Two edges $C \to A$ and $C \to B$ emanating from a common left hit C.
- Right Elbow: Two edges $A \to C$ and $B \to C$ converging at a common right hit C.

For scenarios with tracks sharing a hit S, not all triplets with the common hit C = S will be genuine. Such ambiguous triplets necessitate classification and potential exclusion, as elaborated in the next section.

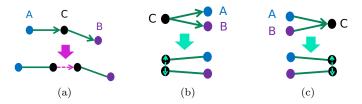


Figure 5: Visual representation of the three triplet configurations in the edge graph: (a) the articulation, (b) the left elbow and (c) the right elbow.

3.4 Triplet Classification

To classify the triplets in the edge graph G^{edge} , the node and edge encodings from the GNN-based edge classifier described in Section 3.2 are utilised instead of invoking another GNN inference.

For a triplet defined by hits (C, A, B), where C is the common hit, the encodings of these hits and of the edges $A \leftrightarrow C$ and $B \leftrightarrow C$ are input to a deep neural network (DNN), termed the *triplet classifier*. This DNN outputs a score between 0 (fake) and 1 (genuine). For left and right elbows, which lack a strict hit order between A and B, the triplet score is the average of the two scores for both possible orderings. Triplets are then filtered based on a threshold score $s_{\text{triplet, min}}$ to exclude the non-genuine ones.

The overall GNN aims at both edge and triplet classification, by minimising the combined loss: $\mathcal{L} = \mathcal{L}_{\text{edges}} + \mathcal{L}_{\text{triplets}}$. During training, edges with scores below 0.5 are discarded prior to triplet construction, concentrating on challenging triplet cases. Both edge and triplet losses employ the sigmoid focal loss [10] to address the genuine-fake imbalance. The loss, for a score $s \in [0, 1]$ and target $t \in \{0, 1\}$, is:

$$\mathcal{L}_{\text{focal}} = -\begin{cases} (1 - \alpha)s^{\gamma} \log (1 - s) & \text{for } t = 1\\ \alpha (1 - s)^{\gamma} \log (s) & \text{otherwise} \end{cases}, \tag{4}$$

where the hyperparameter γ is set to 2 and α is set to the proportions of fake examples (edges or triplets) in a given graph. The overall edge and triplet loss $\mathcal{L}_{\text{edges}}$ and $\mathcal{L}_{\text{triplets}}$ for the given graph are computed as their respective averages.

3.5 Track Construction

 ${\it Track construction from the purified edge graph } \ G^{\rm edge}_{\rm purified} \ {\it consists of four sequential steps}, \ depicted in Figure 6:$

- 1. Connect left and right elbows. This action eliminates forks (two articulations sharing the same initial or terminal edge) related to a single particle. The residual forks represent two particles that start by sharing hits but later diverge.
- 2. Apply a WCC algorithm on the edge graph, excluding the articulations associated with forks.
- 3. Label each remaining link (which corresponds to articulations engaged in forks) as a unique track.
- 4. Convert sets of connected edges into corresponding sets of connected hits, representing the tracks.

The initial two steps discern tracks that might intersect. The third step distinguishes tracks that share their first hits but later diverge. By presupposing that tracks sharing multiple successive hits diverge solely once, this method averts sequential iterations within connected components.

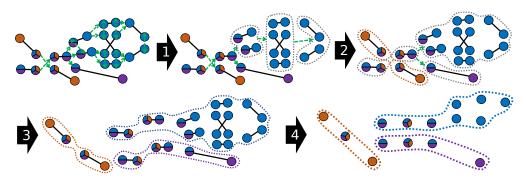


Figure 6: Illustration of the four phases of track construction from the purified edge graph: (1) Connecting left and right elbows, (2) applying a WCC while omitting articulations with shared edges, (3) designating each residual link as a unique track, and (4) substituting edges with hits.

4 Performance

4.1 Definitions and Conventions

The conventions and definitions for track-finding performance in LHCb are outlined in [6]. A track is matched to a particle when at least 70% of its hits are associated with that particle, forming a set of *matching candidates* (track, particle). The metrics used to assess the track-finding performance are presented in Table 1. The uncertainties associated with track-finding efficiency are determined via the Bayesian method with a uniform prior [11] and computed using the ROOT software [12].

Within the Velo's track-finding context, Figure 1 illustrates two primary particle categories:

- Velo-only particles: particles whose tracks are reconstructible in the Velo but not in the SciFi.
- Long particles: particles whose tracks are reconstructible both in the Velo and in the SciFi.

Long track trajectories are bent between the UT and the SciFi due to the magnetic field, which enables momentum measurements. Consequently, reconstructing these tracks is crucial for LHCb physics analyses. The aforementioned categories can be further broken down into three sub-categories:

- No electrons: All particles except for electrons.
- **Electrons**: Only electrons, which are more challenging to reconstruct due to a higher chance of scattering or photon radiation (bremsstrahlung).
- From strange: Non-electron particles in a decay chain with an s-quark hadron, excluding electrons.
 These typically represent tracks originating near the end of the VELO detector, making them harder to reconstruct.

Metric	Definition	Formula
Efficiency	Proportion of matched particles	# matched particles # particles
Clone rate	Proportion of redundant candidates	# candidates - # matched particles # candidates
Ghost rate	Proportion of unmatched tracks	# unmatched tracks # tracks
Hit efficiency	Average proportion of matched hits per particle	$\left\langle \frac{\# \text{ matched hits}}{\# \text{ hits on particle}} \right\rangle_{\text{candidates}}$
Hit purity	Average proportion of matched hits per track	$\left\langle \frac{\text{\# matched hits}}{\text{\# hits on track}} \right\rangle_{\text{candidates}}$

Table 1: Metrics for track-finding performance. Efficiency, clone rate, and ghost rate encompass all events, while hit efficiency and hit purity are averaged across matching candidates.

4.2 Training datasets

This study utilises LHCb Run 3 simulation minimum-bias samples of p-p collisions, which include overlapping event effects. "Minimum-bias" indicates that no specific decay is targeted in the simulation. p-p collisions are generated using PYTHIA [13]. The interaction of the generated particles with the detector, and its response, are implemented using the Geant4 toolkit [14] as described in [15].

The embedding network and GNN are trained on 700,000 events, adhering to these selection criteria[‡]:

- The hits of the particle tracks that are not sufficiently linear are removed. This is assessed by fitting a line to the particle hits and applying an upper limit to the average squared distance between the hits and the line. This criterion excludes 2.5% of the tracks reconstructible in the Velo.
- A minimum of 500 genuine Velo hits is required, to offset the removal of these non-linear tracks.
- Tracks with fewer than 3 hits are excluded.

These criteria are not imposed on the test samples.

4.3 Parameter Choices

In the graph construction phase, two parameters need to be adjusted: the maximal number of neighbours, k_{max} , and the maximal squared distance in the embedding space, d_{max}^2 . k_{max} is fixed to 50, but it could be reduced for quicker inference.

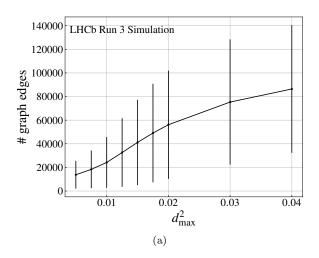
To select an appropriate value for $d_{\rm max}^2$, a natural choice might be the margin of the embedding loss m=0.010. To better grasp its impact on track-finding performance, a hit graph is generated for various $d_{\rm max}^2$ values and then purified by excluding fake edges. Subsequently, a purified edge graph is built, where any fake triplets are discarded. The final tracks emanating from this process provide an upper bound on track-finding performance as a function of $d_{\rm max}^2$.

Figure 7 demonstrates that increasing d_{max}^2 augments graph size (and consequently, inference time), yet can potentially boost performance. Two values are investigated: $d_{\text{max}}^2 = 0.010$ offers a balance between size and performance, while $d_{\text{max}}^2 = 0.020$ elevates efficiency on the challenging long particles from strange decays.

The GNN classifier is trained for each $d_{\rm max}^2$ value. The selection thresholds, $s_{\rm edge,\ min}$ and $s_{\rm triplet,\ min}$, used to filter fake edges and triplets, need to be adjusted. While $s_{\rm edge,\ min}$ is set to 0.4, it could be fine-tuned to balance throughput and performance. As for $s_{\rm triplet,\ min}$, its values are finetuned to ensure a ghost rate below 1% while maximising efficiency for long from strange category. The final thresholds are $s_{\rm triplet,\ min}=0.32$ for $d_{\rm max}^2=0.010$ and $s_{\rm triplet,\ min}=0.36$ for $d_{\rm max}^2=0.020$.

Performance outcomes based on these parameters are discussed in the subsequent section.

 $^{^{\}ddagger}$ Adopting more stringent criteria during the graph construction phase (Section 3.1) may reduce the graph's size without compromising performance.



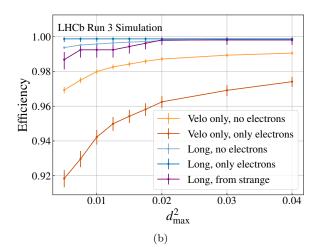


Figure 7: Comparison of optimal track-finding efficiency (a) and hit graph size (b) based on varying d_{max}^2 , for 200 events. The optimal efficiency, derived after purifying the hit and edge graph, represent the efficiency upper limit according to d_{max}^2 . It is shown for 5 different particle categories. Graph sizes (a) feature error bars indicating standard deviation across events, showcasing variability instead of uncertainty.

4.4 Comparison between Allen and ETX4VELO

The search by triplet algorithm in Allen [16] is compared with ETX4VELO using 5,000 simulated events without any selection. Notably, this comparison does not encompass throughput, which is a critical aspect in Allen.

Table 2 illustrates that Allen reconstructs long particles well, especially non-electron ones, with an efficiency surpassing 99%. However, it shows a slight decrease in efficiency for long electrons and for long non-electron particles originating from strange decays. In contrast, with $d_{\text{max}}^2 = 0.010$, ETX4VEL0 exhibits superior track quality across all categories, indicated by higher hit efficiency and purity. Furthermore, Table 3 demonstrates that the GNN-based pipeline has rate of fake tracks which is over 1% lower than Allen. In terms of efficiency, ETX4VEL0 closely matches Allen for the long no electron category, but surpasses it in long electron reconstruction by more than 1.5%. However, ETX4VEL0 is slightly behind Allen by 0.2% for particles from strange decays. When using a larger graph with $d_{\text{max}}^2 = 0.020$, ETX4VEL0's performance improves further, outperforming Allen for long particles from strange decays.

Similar observations are made for the performance in Velo-only categories, as presented in Table 4. Notably, ETX4VELO detects 15% more Velo-only electrons than the traditional Allen algorithm.

The elevated clone rate for electrons, particularly for long electrons, arises from electron-positron pairs sharing initial hits. The current 70% matching criterion erroneously matches each track to both particles. Future revisions will refine this criterion for unique track-to-particle matching, thereby better reflecting the algorithm performance.

Long category	Efficiency		Clone rate		Hit efficiency		Hit purity	
	Allen	ETX4VELO	Allen	ETX4VELO	Allen	ETX4VELO	Allen	ETX4VELO
No electrons	99.26	99.28 (99.51)	2.54	0.96 (0.89)	96.46	98.73 (98.90)	99.78	99.94 (99.94)
Electrons	97.11	98.80 (99.22)	4.25	7.42(7.31)	95.24	96.54 (96.79)	97.11	98.46 (98.46)
From strange	97.69	97.50 (98.06)	2.50	0.92(0.81)	97.69	98.22 (98.77)	99.34	99.68 (99.68)

Table 2: Track-finding efficiency (in percentages) of the search by triplet algorithm in Allen versus ETX4VELO for long particles. For ETX4VELO, values for both $d_{\text{max}}^2 = 0.010$ (first) and $d_{\text{max}}^2 = 0.020$ (in parentheses) are presented.

	Allen	ETX4VELO				
	Allell	$d_{\text{max}}^2 = 0.010$	$d_{\rm max}^2=0.020$			
Ghost rate	2.18%	0.76%	0.81%			

Table 3: Ghost rate of the search by triplet algorithm in Allen versus ETX4VELO for two choices of d_{max}^2

Velo-only	Efficiency		Clone rate		Hit efficiency		Hit purity	
category	Allen	ETX4VELO	Allen	ETX4VELO	Allen	ETX4VELO	Allen	ETX4VELO
No electrons	96.84	97.03 (97.86)	3.84	1.08 (1.02)	93.89	97.93 (98.32)	99.50	99.84 (99.82)
Electrons	67.81	85.10 (86.69)	10.27	5.02(4.97)	79.21	93.33 (93.88)	97.35	99.07 (98.99)
From strange	93.53	$93.07 \ (96.05)$	5.60	1.97(1.77)	90.05	93.92 (96.05)	99.36	99.67 (99.64)

Table 4: Track-finding efficiency (in percentages) of the search by triplet algorithm in Allen versus ETX4VELO for Velo-only particles. For ETX4VELO, values for both $d_{\text{max}}^2 = 0.010$ (first) and $d_{\text{max}}^2 = 0.020$ (in parentheses) are presented.

5 Conclusions

This work introduced ETX4VELO, a GNN-based pipeline derived from the foundational Exa.TrkX pipeline as presented in [5]. ETX4VELO has the ability to reconstruct tracks sharing hits through an novel triplet-based approach.

When juxtaposed with the default traditional algorithm, ETX4VELO not only matched its efficiency but in some instances, surpassed it. The GNN pipeline notably excels in two areas: it reduces the ghost rate by over 1% and delivers significantly improved electron reconstruction results.

As the focus shifts to deployment, the immediate priority is to optimise inference time, to accommodate the high-rate environment that LHCb operates in. Integration of the GNN-based pipeline into Allen is in progress, aiming to provide a comprehensive comparison with the default traditional algorithm. This integration is expected to offer insights that will guide the refinement of various hyperparameters — including the DNN architecture, embedding dimension, number of layers, hidden units, and beyond.

Simultaneously, efforts are directed towards adapting this pipeline for other LHCb tracking detectors, starting from the SciFi.

The code for training and testing ETX4VELO is accessible at https://gitlab.cern.ch/gdl4hep/etx4velo/-/tree/ctd2023.

ACKNOWLEDGEMENTS

The authors extend their sincere gratitude to the LIP6 laboratory for granting access to their versatile GPU cluster, where the majority of the trainings were conducted. We are grateful to the ANN4Europe group at Frankfurt Institute for Advanced Studies (FIAS), led by Ivan Kisel, for their insightful discussions. We thank LHCb's Real-Time Analysis project for its support, for many useful discussions, and for reviewing an early draft of this manuscript. We also thank the LHCb computing and simulation teams for producing the simulated LHCb samples used to benchmark the performance of the algorithm presented in this paper. The development and maintenance of LHCb's nightly testing and benchmarking infrastructure which our work relied on is a collaborative effort and we are grateful to all LHCb colleagues who contribute to it. This work is part of the SMARTHEP network and it is funded by the European Union's Horizon 2020 research and innovation programme, call H2020-MSCA-ITN-2020, under Grant Agreement n. 956086. It is also supported by the ANR-BMBF project ANN4EUROPE ANR-21-FAI1-0011, in collaboration with FIAS.

References

- [1] LHCb Collaboration, "Framework TDR for the LHCb Upgrade: Technical Design Report," (2012) CERN-LHCC-2012-007 URL:https://cds.cern.ch/record/1443882.
- [2] LHCb Collaboration, "LHCb VELO Upgrade Technical Design Report," (2013) CERN-LHCC-2013-021 URL:https://cds.cern.ch/record/1624070.
- [3] LHCb Collaboration, "LHCb Tracker Upgrade Technical Design Report," (2014) CERN-LHCC-2014-001 URL:https://cds.cern.ch/record/1647400.
- [4] LHCb Collaboration, "LHCb Upgrade GPU High Level Trigger Technical Design Report," (2020) doi:10.17181/CERN.QDVA.5PIR URL:https://doi.org/10.17181/CERN.QDVA.5PIR.
- [5] X. Ju et al. [Exa.TrkX], "Performance of a geometric deep learning pipeline for HL-LHC particle tracking," Eur. Phys. J. C 81 (2021) no.10, 876 doi:10.1140/epjc/s10052-021-09675-8 [arXiv:2103.06995 [physics.data-an]] URL:https://doi.org/10.1140/epjc/s10052-021-09675-8.
- [6] P. Li, E. Rodrigues and S. Stahl, "Tracking Definitions and Conventions for Run 3 and Beyond," (2021) LHCb-PUB-2021-005 URL:https://cds.cern.ch/record/2752971.
- [7] J. Johnson, M. Douze, and H. Jegou, "Billion-Scale Similarity Search with GPUs," IEEE Transactions on Big Data 7 (2021), 535-547 doi:10.1109/TBDATA.2019.2921572 [arXiv:1702.08734 [cs.CV]] URL:https://doi.org/doi:10.1109/TBDATA.2019.2921572.
- [8] S. Elfwing, E. Uchibe, and K. Doya, "Sigmoid-weighted linear units for neural network function approximation in reinforcement learning," Neural Networks 107 (2018), 3–11 doi:10.1016/j.neunet.2017.12.012 [ArXiv:1702.03118 [cs.LG]] URL:https://doi.org/10.1016/j.neunet.2017.12.012.
- [9] N. Choma *et al.* [Exa.TrkX], "Track Seeding and Labelling with Embedded-space Graph Neural Networks," (2020) [arXiv:2007.00149 [physics.ins-det]] URL:https://arxiv.org/abs/2007.00149.
- [10] T. Y. Lin, P. Goyal, R. Girshick, K. He and P. Dollár, "Focal Loss for Dense Object Detection," (2017) [arXiv:1708.02002 [cs.CV]] URL:https://arxiv.org/abs/1708.02002.
- [11] M. Paterno, "Calculating efficiencies and their uncertainties," (2004) doi:10.2172/15017262 URL:https://lss.fnal.gov/archive/test-tm/2000/fermilab-tm-2286-cd.pdf.
- [12] R. Brun and F. Rademakers, "ROOT: An object oriented data analysis framework," Nucl. Instrum. Meth. A 389 (1997), 81-86 doi:10.1016/S0168-9002(97)00048-X URL:https://doi.org/10.1016/S0168-9002(97)00048-X.
- [13] T. Sjostrand, S. Mrenna and P. Z. Skands, "A Brief Introduction to PYTHIA 8.1," Comput. Phys. Commun. 178 (2008), 852-867 doi:10.1016/j.cpc.2008.01.036 [arXiv:0710.3820 [hep-ph]] URL:https://doi.org/10.1016/j.cpc.2008.01.036.
- [14] J. Allison, K. Amako, J. Apostolakis, H. Araujo, P. A. Dubois, M. Asai, G. Barrand, R. Capra, S. Chauvie and R. Chytracek, et al. "Geant4 developments and applications," IEEE Trans. Nucl. Sci. 53 (2006), 270 doi:10.1109/TNS.2006.869826 URL:https://doi.org/10.1109/TNS.2006.869826
- [15] M. Clemencic et al. [LHCb], "The LHCb simulation application, Gauss: Design, evolution and experience," J. Phys. Conf. Ser. 331 (2011), 032023 doi:10.1088/1742-6596/331/3/032023 URL:https://doi.org/10.1088/1742-6596/331/3/032023
- [16] D. H. Cámpora Pérez, N. Neufeld and A. Riscos Núñez, "Search by triplet: An efficient local track reconstruction algorithm for parallel architectures," J. Comput. Sci. 54 (2021), 101422 doi:10.1016/j.jocs.2021.101422 [arXiv:2207.03936 [hep-ex]] URL:https://doi.org/10.1016/j.jocs.2021.101422.