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Article

T_c saturation and possible electronic phase separation in strongly overdoped cuprates

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Abstract: In order to elucidate the unusual superconducting properties of cuprates in the strongly overdoped region, i.e. at hole doping levels $p \gtrsim 0.4/\mathrm{Cu}$ in the $\mathrm{CuO_2}$ plane, we study the structural and superconducting properties of a series of $\mathrm{Cu_{0.75}Mo_{0.25}Sr_2YCu_2O_{7+x}}$ powder samples oxygenated under high pressure using different concentrations of KClO₃ up to 35 mol %. The analysis of x-ray diffraction data indicates a high purity $\sim 90\%$ of all samples for nominal molar concentrations of KClO₃ in the 5-30 % range and suggests that the concentration, x, of extra oxygen atoms increases with increasing KClO₃ concentration. Surprisingly, the T_c values remains nearly constant within the 80-85 K range independent of KClO₃ concentration, which suggests a scenario of T_c saturation. In order to account for this unexpected behaviour, we put forward the hypothesis that overdoping enhances the density of unpaired holes, which is supported by the observation of large values of the Sommerfeld coefficient in all samples. We therefore propose a scenario of electronic phase separation between normal and superconducting holes.

Keywords: Superconducting cuprates; overdoping; electronic phase separation.

1. The unexpected finding of high- T_c superconductivity in strongly overdoped cuprates

The discovery of high-temperature superconductivity (HTSC) in cuprates by G. Bednorz and K.-A. Müller in 1986 has revolutionised the field of superconductivity and driven research on condensed matter and materials physics towards new and totally unexpected directions. Indeed, in these materials, superconductivity occurs in presence of sizeable electronic correlations upon electronically doping a pristine charge-transfer antiferromagnetic (AFM) insulating phase associated with Cu²⁺ ions in the CuO₂ plane, as shown in Fig. 1a. This situation, which was never envisaged before, differs radically from that of metallic systems described by conventional BCS theory of electron-phonon pairing. This has lead to unprecedented theoretical efforts to develop a suitable microscopic theory of HTSC. A clear indication of unconventional superconducting behaviour is given by early observations in the most studied systems, such as La₂CuO₄ (La214) and Bi2212 (see Figure 1b), of a characteristic dome-like dependence of the superconducting critical temperature, T_c , on the excess holes, p, on the planar Cu ions in the Cu2 site in Fig. 2. Specifically, superconductivity appears at $p \sim 0.05$ hole/Cu concomitant to the suppression of the AFM state, reaches a maximum at $p \sim 0.15$ -0.17 hole/Cu and then decreases until it vanishes at $p \sim 0.26$ -0.27 hole/Cu.

Such a dependence has been widely accepted as a universal feature of cuprates [1,2]; the resulting phase diagram shown in Fig. 1a has therefore served as the phenomenological basis for the development of any microscopic HTSC theory for more than three decades. Although the microscopic theory remains highly controversial - a point that goes beyond

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the frame of the present paper - a consensus exists as to a phenomenological scenario where pairing in the CuO_2 plane requires sizeable AFM correlations. As a consequence, research on cuprates has been hitherto focused on the underdoped and optimally doped regions of the electronic phase diagram, where unconventional normal state - or 'strange metal' - properties are found. The overdoped region has remained little studied, possibly because it is widely accepted that, upon approaching the regime of high carrier density in the overdoped region at p > 0.26-0.27 hole/Cu where superconductivity disappears, the properties are expected to become conventional, i.e. Fermi-liquid (FL) like.

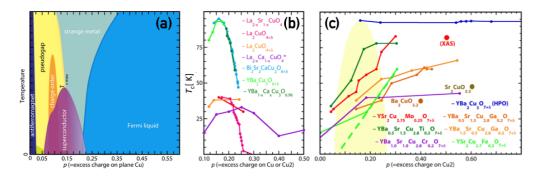


Figure 1. (a) Schematic T-p phase diagram of cuprates showing the existence of a characteristic dome-like p dependence of the superconducting critical temperature, T_c , in the p=0.05-0.27 hole/Cu range, where the hole density, p refers to unit of the a CuO₂ plane. **(b)** Experimental diagram showing the above dome-like dependence for a number of cuprate families. Note the recent data on heavily Ca-substituted epitaxial La_{2-x}Ca_xCuO₄ thin films showing an extended dome up to p=0.4 and beyond [3]. **(c)** T_c vs. p dependence of high-pressure oxygenated cuprates showing that T_c levels off or continues to slowly increase in the strongly overdoped region up to p=0.6 (from [4] and references therein).

In fact, the above FL scenario for the strongly overdoped region was never verified experimentally in a systematic manner possibly owing to the difficulty of overdoping the CuO₂ plane, which typically requires high-pressure oxygenation. Available data on a number of high-pressure oxygenated cuprates, initially studied by T. H. Geballe and M. Marezio, rather point at a completely different scenario [4–11]. Fig. 1c shows that, in these systems, T_c levels off or continues to slowly increase past the upper limit of the dome of p = 0.26–0.27 hole/Cu, up to the maximum amounts of excess oxygen corresponding to p values ranging from 0.3 up to 0.6. These reports have been met with disinterest or disregard until recent studies confirmed that high- T_c superconductivity is a bulk property of such strongly overdoped phases. To the best of our knowledge, a first confirmation of bulk superconductivity has been given by some of us [12]. Using high-pressure synthesis, we achieved strong overdoping with p = 0.46 hole/Cu, well beyond the superconducting dome of Figure 1a, in high-purity powder samples of the Cu_{0.75}Mo_{0.25}Sr₂YCu₂O_{7+x} system, commonly known as $YBa_2Cu_3O_{7-x}(YBCO)$ (see Figure 2). To facilitate the insertion of extra oxygens x, we replaced the Ba $^{2+}$ ion for the smaller Sr $^{2+}$ one and partially substituted Cu for Mo at the CuO (Cu1) chain site. Previous XANES spectroscopy [7] and bond valence sum analysis of high-resolution neutron diffraction data [12] consistently indicate that the above substitution is effective in increasing the oxygen concentration up to x = 054. Surprisingly, the resulting phase $Cu_{0.75}Mo_{0.25}Sr_2YCu_2O_{7+x}$ displays bulk superconductivity at $T_c \sim 84$ K for x = 0.54 (see [12] and Figure 4). This unexpected scenario has been confirmed two years later in the strongly overdoped cuprate $Ba_2CuO_{4-\nu}$ [13] and, very recently, in heavily Ca-substituted La₂CuO₄ epitaxial thin films [3]. In conclusion, all these data consistently show a much wider superconducting region than previously believed, as apparent from Figures 1b-c.

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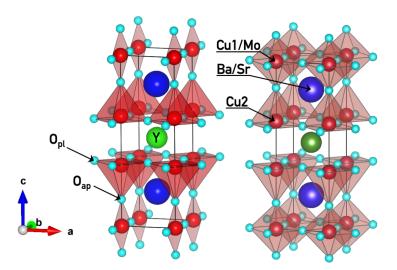


Figure 2. Crystal structures of orthorhombic $YBa_2Cu_3O_{7-x}$ for x=1 (left) and tetragonal $Cu_{0.75}Mo_{0.25}Sr_2YCu_2O_{7+x}$ (right), where Mo partially substitutes the copper Cu1 chain site. Note the distinct planar (pl) and apical (ap) oxygen sites. In the second structure, Sr substitutes the larger Ba ion, thus leaving more room for the extra oxygen atoms.

2. Open questions about the strongly overdoped region of cuprates

The observation of high- T_c superconductivity at doping levels $p \gtrsim 0.4$ put into question the current phenomenological description of cuprates and also the validity of the microscopic theories hitherto developed based on the dome-like phase diagram of Fig. 1a. This prompts us to investigate further the properties of strongly overdoped cuprates. We single out the following research directions:

The possibility of a novel superconducting branch and multiband superconductivity. The high T_c value of 84 K in the Cu_{0.75}Mo_{0.25}Sr₂YCu₂O_{7+x} system is much higher than that of the pristine undoped YSr₂Cu₃O_{7-x}(YSCO) phase, where $T_c \sim 65$ K [14]. This observation rules out the possibility of secondary superconducting phases in the samples and clearly suggests the existence of a second or much more extended superconducting dome, as pointed out by Scalapino *et al.* [15]. Indeed, the larger valence v = 2 + p of the Cu atom in the CuO₂ plane corresponds to record short Cu-apical oxygen distances [12]. Hence, both $x^2 - y^2$ and z^2 orbitals of the Cu^{(2+p)+} ion are expected to be active [16], which suggests that one-band theories in two dimensions are unsuitable.

Are strongly overdoped cuprates Fermi liquids? The observation of FL behaviour would lead to the surprising conclusion of high- T_c superconductivity arising from a FL, in full contradiction with the current understanding of superconductivity in cuprates. The opposite finding of non-FL behaviour would also be interesting since we could establish whether this unconventional behaviour is similar to that found in the optimally doped or underdoped regions. We expect that either case would drive the field toward a new direction.

Electronic phase separation. Our specific heat results on $\text{Cu}_{0.75}\text{Mo}_{0.25}\text{Sr}_2\text{YCu}_2\text{O}_{7+x}$ for x=0.54 unveil a significant fraction of normal electrons, as indicated by a sizeable Sommerfeld coefficient $\gamma\sim 10$ mJ Cu mol $^{-1}$ K $^{-2}$ [12]. Notably, a similar result has previously been reported on overdoped La214 samples [17], while a vanishing γ is found in optimally Y123 (YBCO) [18]. Considering the high purity of our $\text{Cu}_{0.75}\text{Mo}_{0.25}\text{Sr}_2\text{YCu}_2\text{O}_{7+x}$ samples and that neutron diffraction and muon-spin relaxation results rule out the presence of chemical inhomogeneities within a scale larger than the London penetration depth, $\lambda\sim 1000$ Å, the observation of normal electrons in the superconducting phase suggests

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a scenario of electronic phase separation between normal and superconducting phases within the intermediate scale ~ 100 Å between λ and the superconducting coherence length, $\xi \sim 10$ Å [4,12].

Previously, the scenario of nanoscale phase separation has been proposed by several authors not only for cuprate superconductors [19–24], but also for other strongly correlated electron systems, such as manganites and cobaltites [25–27]. Indeed, it has been theoretically argued that electronic phase separation can be stabilised by a the competition between long-range Coulomb and short-range magnetic interactions [19], ubiquitous in all the above transition metal oxides. Various experimental techniques, such as nuclear magnetic resonance, Mössbauer spectroscopy, scanning tunneling microscopy and, more recently by time-resolved or space-resolved synchrotron radiation techniques [28] have been successfully employed to probe dynamical phase separation in a variety of systems.

Beyond the adiabatic approximation. Recently, the local structure and dynamical properties of the strongly overdoped cuprates $Cu_{0.75}Mo_{0.25}Sr_2YCu_2O_{7+x}$ and Ba_2CuO_{4-y} were studied by means of Extended X-ray Absorption Fine Structure (EXAFS) spectroscopy [29,30]. The data analysis unveils huge (~ 1 Å) dynamical distortions of the lattice at T_c that involve the apical oxygen, which suggests the existence of a lattice-driven change of the electronic structure in the superconducting state.

In the present paper, we focus on the possibility of an inhomogeneous superconducting phase, as suggested by the observation of a large γ in superconducting Cu_{0.75}Mo_{0.25}Sr₂YCu₂O_{71.54} In order to elucidate this point, we have prepared and studied a series of powder samples of Cu_{0.75}Mo_{0.25}Sr₂YCu₂O_{7+x}with varying the concentration $x \sim p$ of the extra oxygen atoms in the basal plane of the Cu1 chain site (see Figure 2). In the following, we report selected results regarding the structural and superconducting properties of the samples. The new data enable us to draw more precisely the tentative electronic phase diagram of the strongly overdoped region (Fig. 1c). Our objective is to cover the widest possible range of doping from the tail of the dome at $p \sim 0.3$ hole/Cu ideally up to the maximum doping, $p \sim 1$ corresponding to Cu³⁺.

3. Materials and Methods

The (Cu,Mo)1212 powder samples object of this work were newly synthesised using the citrate sol-gel method and a modified oxidation treatment, as described elsewhere [12]. In brief, appropriate amounts of Y_2O_3 , CuO, SrCO₃ and MoO₃ were dissolved in 1M HNO₃ solution. Citric acid and ethylene glycol were added and the solution was heated in oven at 200 °C until a gel was formed. The obtained gel was then dried, powdered and calcined at 600 °C for 12 h. The resulting powder was pressed into a pellet and annealed at 980 °C for 2 \times 24 h with intermediate grinding to obtain the as synthesised product. The oxygenation was carried out by mixing the as synthesised powder with a variable concentration from 5 to 35 mol % of KClO₃. The mixture was then subjected to high pressure treatment in a cubic-anvil type high-pressure apparatus at 4 GPa and 500 °C. The powders were studied by means of x-ray diffraction in a conventional Bragg-Brentano $\vartheta - 2\vartheta$ geometry using a commercial X'pert powder diffractometer equipped with a Co K_{α} anode. The superconducting transition of the powders was studied by means of dc magnetisation measurements as a function of temperature in both zero-field (ZF) and field-cooling (FC) modes at 100 Oe using a commercial SQUID Quantum Design apparatus. A complementary study of the superconducting transition and of the electronic spectrum was carried out by means of specific heat measurements in the 2-300 K range performed using the relaxation rate method implemented in the same PPMS apparatus. This latter study enables us to estimate the aforementioned Sommerfeld coefficient, γ .

4. Results

The analysis of the x-ray diffraction data indicates for all samples a phase purity better than 90% or better by excluding the inevitable residual KCl phase arising from the decomposition of KClO₃ at high temperature during synthesis. In Figure 3, we show

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a representative x-ray diffraction pattern of the 30% sample and compare it with the calculated pattern using the tetragonal P4/mmm symmetry reported earlier. Although the above good purity level concerns the limited volume fraction probed by x-rays, it is plausible that we would obtain a similar purity level using neutron diffraction. Indeed, in a previous neutron diffraction study [12], we found a phase purity of 94% in a 35% sample prepared under the same conditions. In conclusion, we believe that secondary phases, if any, do not affect significantly the superconducting properties.

In Figure 5, we note that, in the 5-35 % range of KClO₃ molar concentration studied, the c-axis parameter decreases monotonically by about 0.02 Å, while the a-axis parameter remains constant within the experimental error. Such a decrease of c-axis parameter is comparable to that obtained on YBa₂Cu₃O_{7-x}[31], where a decrease of 0.4 Å was reported upon increasing the oxygen concentration x from 0.4 to 0.95. This increase of oxygen concentration is identical to that obtained in our Cu_{0.75}Mo_{0.25}Sr₂YCu₂O_{7+x} system, so the present results therefore suggest that, in first approximation, the amount of extra oxygen atoms incorporated in the structure is proportional to the KClO₃ concentration. Future neutron diffraction studies with enhanced resolution may confirm the above conclusion and also enable a direct measurement of the oxygen concentration. Similar to the aforementioned case of YBa₂Cu₃O_{7-x}, the increase of oxygen concentration in the basal plane of Cu_{0.75}Mo_{0.25}Sr₂YCu₂O_{7+x} does not seem to change appreciably the a-axis parameter, for the latter is mainly determined by the Cu-O distance in the CuO₂ plane.

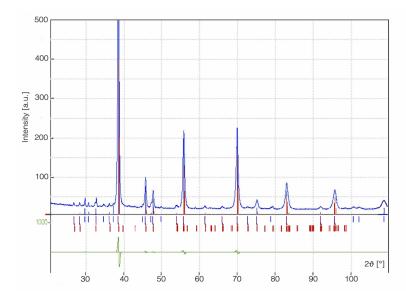


Figure 3. Co K_{α} X-ray diffraction pattern of the sample prepared with 30 mol % of KClO₃. This pattern confirms the purity of the $Cu_{0.75}Mo_{0.25}Sr_2YCu_2O_{7+x}$ phase up to sizeable concentrations of KClO₃. The experimental profile is indicated by the solid blue line. Experimental and calculated Bragg peaks are indicated by vertical red and blue ticks, respectively. The extra peaks that do not match the $Cu_{0.75}Mo_{0.25}Sr_2YCu_2O_{7+x}$ peaks are attributed to the residual KCl and KClO₃ phases. The green curve represents the difference between experimental and calculated pattern.

In Figure 4 we show the temperature-dependent susceptibility curves for a few representative $Cu_{0.75}Mo_{0.25}Sr_2YCu_2O_{7+x}$ samples prepared with different concentrations of KClO₃ oxidant. The curves were obtained from the zero-field-cooling magnetisation data taken at a 100 Oe field. Note that the onset T_c values vary modestly within the 80-85 K range as better seen in Figure 5. Taking into account the data scattering, we conclude that T_c does not appreciably change with the concentration of oxidant, with the exception of the 20% sample which seems to exhibit an anomalous decrease of T_c . The volume fraction falls in the 15-25% range for all samples, except for the above anomalous sample. This indicates that the observed superconductivity is a bulk property of the $Cu_{0.75}Mo_{0.25}Sr_2YCu_2O_{7+x}$ phase and that the T_c seems to saturate independent of the hole doping level. In Figure 5,

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note a similar behaviour of the Sommerfeld coefficient, γ , as estimated by extrapolating the C/T vs. T^2 curves down to zero temperature (see Figure 6). Note in all samples a large residual γ in the 5 – 20 mJ K $^{-2}$ mol Cu range. This confirms previous findings in a x=0.54 sample of Cu_{0.75}Mo_{0.25}Sr₂YCu₂O_{7+x} [12] and in overdoped La_{2-x}Sr_xCuO₄ single crystals with vanishing T_c or even beyond in the metallic non-superconducting phase, where γ probes the density of states of *normal* electrons [17]. Similar values have been reported on optimally doped Bi₂Sr₂CaCu₂O₈ [32] and overdoped Tl₂Ba₂CuO_{6+ δ} [33] as well. Note that smaller - still not vanishing - values have been reported on the above optimally doped systems [18], which supports a scenario of unpaired carriers in the overdoped region of cuprates. Further evidence of this scenario has recently been provided by optical conductivity measurements on overdoped La214 films, showing a wide Drude-like peak in the zero-temperature limit, well inside the superconducting phase [34].

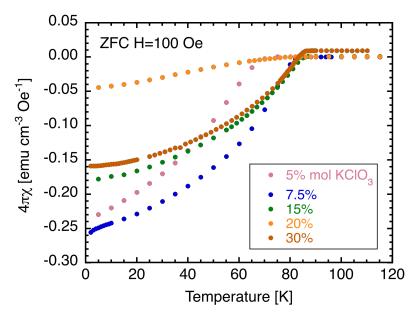


Figure 4. Zero-field-cooling (ZFC) magnetisation curves measured at a field of 100 Oe on a series of $Cu_{0.75}Mo_{0.25}Sr_2YCu_2O_{7+x}$ samples prepared with different molar concentrations of KClO₃ oxidant indicated in the legend.

5. Discussion

The present systematic study carried out on a series of Cu_{0.75}Mo_{0.25}Sr₂YCu₂O_{7+x} powder samples prepared under high pressure with different nominal concentrations of extra oxygen atoms, x, confirms the occurrence of bulk superconductivity at 80-85 K in the strongly overdoped region, corresponding to hole concentrations $p \gtrsim 0.4$ in the CuO_2 plane. The above T_c values are significantly higher than those of the pristine unsubstituted $YSr_2Cu_3O_{7-x}$ phase, which rules out the possibility that superconductivity in $Cu_{0.75}Mo_{0.25}Sr_2YCu_2O_{7+x}$ is associated with a secondary phase. This conclusion is in agreement with the high purity of the samples, typically 90% or better, as determined by x-ray diffraction and with the sizeable magnitude of the superconducting fraction, typically in the 15-25% range, estimated by means of susceptibility measurements. The monotonic decrease of the c-axis parameter with the nominal molar concentration of KClO₃ used during the high pressure synthesis suggests an increasing amount of extra oxygens, x, in the 5-35 mol % range of KClO₃ concentration investigated. A striking result is the nearly constant T_c values, which suggests a quick saturation of superconductivity with oxygen overdoping. This observation is consistent with the large and nearly x-independent values of the Sommerfeld coefficient, γ , which points at a sizeable fraction of unpaired carriers that coexist in the superconducting state. In order to account for this unusual observation, we put forward the hypothesis that overdoping would mainly enhance the density of holes

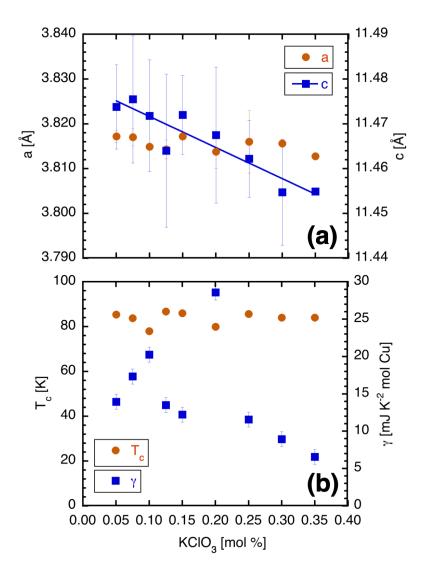


Figure 5. (a) Dependence of the a- and c-axis parameters on KClO₃ oxidant concentration for a series of Cu_{0.75}Mo_{0.25}Sr₂YCu₂O_{7+x} powder samples. Solid lines are linear fits to the experimental points. (b) Same as above for the T_c and the Sommerfeld coefficient, γ . The latter is obtained by extrapolating the C/T vs. T^2 curves shown in Figure 6 down to zero temperature. The data of the 35% sample is taken from Ref. [12].

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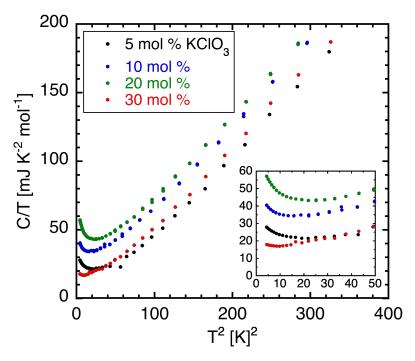


Figure 6. Low-temperature behaviour of the specific heat of four representative $Cu_{0.75}Mo_{0.25}Sr_2YCu_2O_{7+x}$ samples prepared using different concentration of KClO₃ oxidant indicated in the legend. Inset: detail of the data in the zero-temperature limit.

with local a_1 symmetry, formed by the hybridisation of the $3d_{z^2}$ orbitals of the Cu ions in the CuO₂ plane. According to a theoretical model proposed by Di Castro, Feiner and Grilli [20], these holes do not contribute to superconductivity and T_c scales with the density of holes with local b_1 symmetry, formed by the hybridisation of the $3d_{x^2-y^2}$ orbitals. We argue that this scenario is suitable to the present case, for the record short distance between the apical oxygen and the Cu ion in the CuO₂ plane characteristic of the Cu_{0.75}Mo_{0.25}Sr₂YCu₂O_{7+x} phase [12] is expected to significantly enhance the occupancy of the $3d_{z^2}$ orbital, as pointed out above [16]. Further experiments on other strongly overdoped cuprate system would be required to corroborate this scenario and to explore the normal state and superconducting properties in the strongly overdoped region at even higher doping levels, up to p=1.

Author Contributions: Conceptualization, A.G., S.D.C. and M.K.; methodology, A.G. and M.K.; writing and editing, A.G.; experiments, A.H., E.M., L.D., B.P., Y.K. and D.H.; supervision, A.G.; funding acquisition, A.G. and M.K. All authors have read and agreed to the published version of the manuscript.

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Conflicts of Interest: The authors declare no conflict of interest.

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