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# Real-time collision avoidance based on optic flow divergence onboard an underwater vehicle

Lucia Bergantin<sup>1</sup>, Christophe Viel<sup>2</sup>, Luc Jaulin<sup>1</sup>

**Abstract**—Obstacle avoidance is a major challenge for underwater robot navigation, especially in cluttered environments where sonars are subject to reverberation and noise. Optic flow cues are widely used for aerial drone navigation, as they can be measured with broadly available sensors such as monocular cameras. In this study, we investigate the use of optic flow divergence for real-time collision avoidance onboard a Remotely Operated Underwater Vehicle (ROV) equipped with monocular cameras. The measured optic flow divergence was first used to trigger an autonomous emergency braking response, then to estimate the relative distance of the underwater vehicle from the detected obstacle using an Extended Kalman Filter. This relative distance was used to maintain a predefined safe distance from the obstacle. Tests were first carried out in a pool, then in a harbour and a lake.

**Index Terms**—Obstacle avoidance, underwater navigation, optic flow

## I. INTRODUCTION

Obstacle avoidance is a major challenge for the navigation of Unmanned Underwater Vehicles (UUVs). The robot must first be able to detect obstacles and then avoid them. In the underwater environment, limited visibility generally favours the use of sonar for obstacle detection. However, high-performance sonars are expensive, and can be particularly prone to interference in cluttered environments or near walls due to reverberation and noise. The resulting acoustic image is still useful for remote operators, but distance measurements are often very noisy and too unstable for automated position control systems in these conditions. In addition, the use of sonar is not always authorised (in the vicinity of military installations or near the coast, for example). Therefore, other solutions need to be considered.

Several approaches for UUV navigation involving the use of ArUco markers [27], acoustic systems [20], Simultaneous Localisation and Mapping (SLAM) methods [29, 28] or feature detection [5] have been proposed. Many of these approaches, however, require the fusion of outputs from several sensors. In cluttered environments, short-distance detection can be performed using electric sense [4] or vision.

Optic flow is a visual cue representing the apparent motion

of objects, surfaces, and edges caused by the relative motion between an observer and a scene [6]. Optic flow cues are widely used for Unmanned Aerial Vehicle (UAV) navigation. Translational optic flow has been employed for controlled landing [22], uneven terrain following [9] and localization [14, 15]. Optic flow divergence has been used for visually controlled landing [11, 24, 8, 12], honeybee-inspired visual odometry [1] and obstacle avoidance [21, 26]. Methods for measuring optic flow divergence were tested onboard UAVs with a monocular camera [8, 12] and optic flow sensors [1]. The optic flow divergence was also used to estimate the relative distance between a UAV and the ground using an Extended Kalman Filter (EKF) [1]. Some studies have explored the possibility of using optic flow cues for UUV navigation as well. A synthetic database of underwater scenes was presented to train deep neural networks for optic flow estimation [10]. Optic flow divergence resulting from depth variations has been employed to evaluate the scale factor of observed scenes to perform visual odometry onboard a Remotely Operated Vehicle (ROV) [7].

ROVs are UUVs remotely controlled by operators on the surface. They are connected via a tether and can be equipped with cameras and other sensors for tasks like underwater inspections, data collection, and maintenance in deep and hazardous environments. Their field of application is vast, from dam inspection, offshore platform, and pipeline maintenance to marine research and underwater archaeology. Since ROV operators face practical challenges in maneuvering due to complex underwater conditions (currents, lack of visibility,...), most works try to make robot control easier, more intuitive, and safer [23, 25].

In this study, we investigate the use of optic flow divergence for real-time minimalistic underwater collision avoidance onboard an ROV (referred to here as BlueBee robot). The presented approach is particularly suited for obstacles in close proximity. Optic flow divergence was measured using a monocular camera, based on the method presented in [12]. The occurrence of an optic flow divergence measured during remote-controlled navigation was used to detect the presence of an obstacle and thus trigger an autonomous emergency braking response. The measured optic flow divergence was then used to estimate the relative distance of the BlueBee robot from the detected obstacle using an EKF. The estimated relative distance was employed to reach a predefined safe distance from the obstacle. Optic flow divergence was then continuously measured thanks to an imposed small oscillation, allowing the robot to maintain the predefined safe distance. To evaluate the proposed method under different conditions, tests

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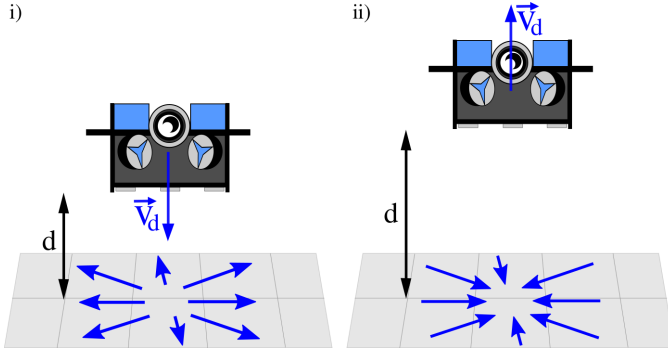


Fig. 1. An expansion of the optic flow vector field is observed when a robot approaches a surface (i), while a contraction is observed when the robot moves away from it (ii).

were carried out in a pool, a harbour and a lake.

## II. MEASUREMENT OF THE OPTIC FLOW DIVERGENCE

An expansion of the optic flow vector field is observed when approaching a surface, while a contraction is observed when moving away from it (see Figure 1). This series of expansions and contractions can be defined as the optic flow divergence  $\omega_D$ . If we consider a robot equipped with a camera looking straight towards a surface,  $\omega_D$  can be expressed as the ratio of the robot's velocity in the direction of the surface  $V_d$  to the robot's distance from the surface  $d$ :

$$\omega_D = \frac{V_d}{d} \quad (1)$$

In this study, we built on a method presented by previous authors to measure optic flow divergence with a monocular camera [8, 12, 13]. Images were first converted from RGB to greyscale. Features were detected with the Scale-Invariant Feature Transform (SIFT) algorithm [18, 17] and tracked to the next image with the Pyramidal Lucas Kanade method [3]. After calculating the image distances  $d_t$  in the frame taken at time  $t_i$  and  $d_{(t+\Delta t)}$  in the next frame at time  $t_{i+1} = t_i + \Delta t$  (with  $\Delta t > 0$  a chosen time interval), we computed the ratios  $(d_t - d_{(t+\Delta t)})/d_t$  and took their average divided by  $\Delta t$ .

To compensate for the presence of underwater currents and orientation instabilities due to remote operation, the highest component of the rotational optic flow given either by the rotation around axis  $y$  or  $z$  of the camera (see Figure 2.ii), was subtracted from the optic flow divergence. Let us call them  $\omega_{R,y}$  and  $\omega_{R,z}$  respectively. Since each component of the rotational optic flow depends on the robot's speed of rotation, we can roughly approximate (for reasons of calculation time)  $\omega_{R,y}$  and  $\omega_{R,z}$  using angular velocities given by the Inertial Measurement Unit (IMU) of the robot. Note that  $\omega_{R,y}$  and  $\omega_{R,z}$  depend on the camera position and orientation on the robot. For example, on a downward-facing camera,  $\omega_{R,y}$  and  $\omega_{R,z}$  can be approximated as the derivative of the robot's pitch and roll respectively. A more complete estimate in real time of  $\omega_{R,y}$ ,  $\omega_{R,z}$  and possibly  $\omega_{R,x}$  (expressed according to [16]) will be the subject of future studies.

The measured optic flow divergence was filtered to remove outliers.

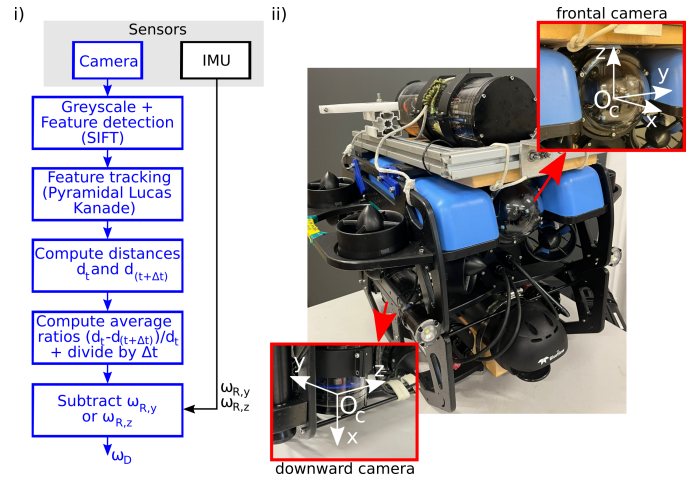


Fig. 2. i) Schema of the method used for measuring the optic flow divergence  $\omega_D$ . ii) The BlueBee robot is equipped with a frontal monocular camera and a downward monocular camera (with their respective coordinate systems  $\{O_c, \vec{x}, \vec{y}, \vec{z}\}$ ).

## III. COLLISION AVOIDANCE

### A. Hypotheses

In this study, we propose controls for a robot of type ROV. Let us define  $\mathcal{R}_c = \{O_c, \vec{x}, \vec{y}, \vec{z}\}$  the frame of reference of the camera, where  $O_c$  is the center of the camera and  $\vec{x}$  corresponds to the optical axis of the camera (see Figure 2.ii).  $\vec{x}$  represents the direction in which the optic flow divergence is measured. Let  $V_x$  be the velocity of the robot in the direction  $\vec{x}$ . Since ROVs are holonomic, we consider here that the robot has already a low-level control allowing it to be driven directly in translation on  $\vec{x}$ : we define  $u_x$  the control input in the direction  $\vec{x}$ . When the autonomous controls described below are not activated, a manual control  $u_{x,operator}$  given by an operator (from a joystick, for example) is applied.

### B. Emergency braking response

To detect obstacles in an underwater environment, we continuously measured optic flow divergence while an operator remotely controlled the BlueBee robot. When the measured optic flow divergence was lower than an experimentally defined threshold  $\omega_{D,lim} < 0$  (see Appendix A), we considered that an obstacle was detected and an autonomous emergency braking response was automatically activated. A strong impulse in the opposite direction to the obstacle was imposed on the robot to avoid it. When the obstacle was no longer detected, the robot stopped the motors and then gave back the control to the operator. The robot can so be in three different modes: operator control (mode = 0), obstacle repulsion (mode = 1), and stop repulsion (mode = 2).

The emergency braking control can be expressed as:

$$u_x = \begin{cases} -k_v V_x^* & \text{if mode} = 1, \\ 0 & \text{if mode} = 2, \\ u_{x,operator} & \text{if mode} = 0, \end{cases} \quad (2)$$

where  $V_x^* = V_x$  if  $V_x$  can be measured or  $V_x^* = 1$  otherwise,  $k_v > 0$  a design parameter whose value can be high if  $V_x$  is unknown, and mode a discrete memory variable such that:

$$\text{mode}(k) = \begin{cases} 1 & \text{if } \omega_D \leq \omega_{D \text{ lim}} \\ 2 & \text{if } (\omega_D > \omega_{D \text{ lim}}) \text{ and } (\text{mode}(k-1) = 1) \\ 0 & \text{else} \end{cases} \quad (3)$$

Note that the knowledge of the velocity  $V_x$  is not necessary in the control (2). However, if  $V_x$  is known, this information allows a smoother speed-proportional control. Otherwise, a chosen motor impulse strong enough to stop the robot must be chosen.

### C. Safe-distance maintenance control

Previous authors demonstrated that thanks to the optic flow divergence the state vector  $X = [d, V_d]^T$  is locally observable [12, 2]. As a consequence, we can use the measured optic flow divergence to estimate the relative distance  $d_{est}$  of the BlueBee robot from the obstacle using an EKF. The EKF receives the optic flow divergence as measurement and the acceleration  $a_d$  of the BlueBee robot (given by its IMU) in the direction of the obstacle as input (see Appendix B). In this study, we use the measured optic flow divergence to estimate the relative distance  $d_{est}$  of the BlueBee robot from the obstacle after an emergency braking response.  $d_{est}$  is then used to maintain a predefined safe distance.

The safe-distance maintenance control can be expressed as:

$$u_x = -\text{sign}(d_{est} - d^*) u_{x, \text{min}} \quad (4)$$

where  $d^* > 0$  is the desired distance from the obstacle and  $u_{x, \text{min}} > 0$  is a control value for a small displacement (see an example for our experiment in Section IV). Note that  $d^*$  must be chosen such that optic flow divergence can be measured stably. It can be observed that the control does not use proportional or derivative terms but a constant term. This prevents the robot from converging to the desired distance, thus imposing a small oscillation to continuously measure optic flow divergence and so continuously estimate the relative distance of the BlueBee robot from the obstacle.

## IV. THE BLUEBEE ROBOT

A BlueROV2<sup>1</sup> was used for tests in a pool, a harbour and a lake. BlueROV2 are equipped by standard with a frontal monocular camera, two lights facing forward, a barometer, and an IMU. The BlueBee robot was also equipped with a second monocular camera and two extra lights facing downwards to measure  $\omega_D$  in that direction and thus use the barometer as ground truth. Both monocular cameras are Low-Light HD USB Camera<sup>2</sup> (standard cameras on BlueROV2), developed for underwater vision with excellent low-light performance, good color handling, and onboard H.264 video compression. An image of size  $800 \times 600$  was chosen for the transmission. An acoustic camera Blueview<sup>3</sup> was also equipped in the frontal

direction to obtain a 2D imaging sonar easy for humans to interpret. Distance extraction is not possible directly on this model.

The Bluerov already has translation commands provided by the MAVROS package. A pwm input must be provided between 1000 and 2000, where 1500 is the neutral input, and 1000 and 2000 are the maximum power in one direction or the other. The pwm input was so expressed as  $u_{pwm, x} = u_x + 1500$ . Note that motors have a dead-band such that they are inactive if the input is in the interval  $u_{pwm, x} \in [1450, 1550]$ : we can so choose  $u_{x, \text{min}} = 60$ . The ROV's downward speed can be accurately measured using the barometer, but the ROV's IMU is not accurate enough to provide forward speed. Thus, we take  $V_x^* = V_x$  during downward and  $V_x^* = 1$  during frontal testing. We take  $\omega_{D \text{ lim}} = -0.05 \text{ rad/s}$ ,  $k_v = 400$  and  $d^* = 0.7 \text{ m}$ . Optic flow divergence and control input were calculated with a frequency of  $f = 15 \text{ Hz}$  and so  $dt = \frac{1}{f}$ . The ROV was controlled in depth and heading to keep them constant when the operator did not control them.

## V. EXPERIMENTAL RESULTS

### A. Tests carried out in a pool

Tests were carried out in the pool of ENSTA Bretagne (in Brest, Brittany, France; shown in Figure 3.i ). In order to use the output of the barometer as the ground truth, tests were performed using the monocular camera facing downwards and the bottom of the pool was considered as the obstacle. The downward-facing lights of the BlueBee robot were switched on at maximum.

An example of real-time emergency braking response is shown in Figure 3.iii. The blue section of the curves correspond to the remote operation phase, during which an operator controlled the BlueBee robot with a joystick to descend towards the

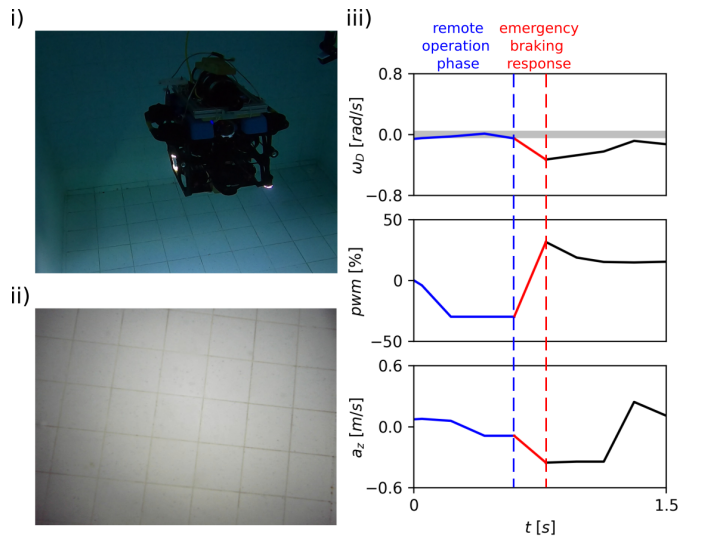


Fig. 3. i) The BlueBee robot in the ENSTA Bretagne pool (in Brest, Brittany, France). ii) View of the bottom of the pool from the downward camera. iii) Example of emergency braking response: the BlueBee robot was remotely controlled (in blue) until an optic flow divergence  $\omega_D$  below the threshold  $\omega_{D \text{ lim}} = -0.05 \text{ rad/s}$  (gray area) was measured and the autonomous emergency braking response was triggered (in red).

<sup>1</sup><https://bluerobotics.com/store/rov/bluerov2/>

<sup>2</sup><https://bluerobotics.com/store/sensors-cameras/cameras/cam-usb-low-light-r1/>

<sup>3</sup><http://www.teledynemarine.com/blueview/>

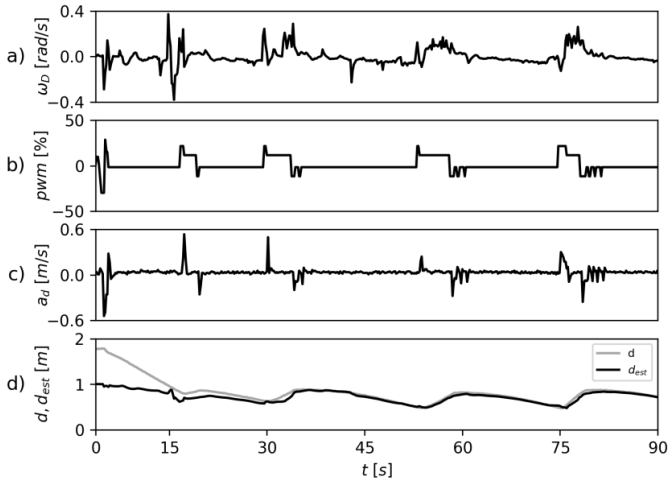


Fig. 4. Example of collision avoidance carried out in the ENSTA Bretagne pool (in Brest, Brittany, France): a) measured optic flow divergence  $\omega_D$ , b) pwm command given to the BlueBee robot, c) acceleration  $a_d$  in the direction of the obstacle given by the Inertial Measurement Unit (IMU) of the robot, d) comparison of the estimated relative distance  $d_{est}$  with the ground truth  $d$  given by the barometer. A video of the tests is available at <https://youtu.be/qSBWyW11wX0>.

bottom of the pool. As soon as an optic flow divergence below the given threshold  $\omega_{D \text{ lim}}$  was measured, the emergency braking response (red section of the curves) was automatically activated and the BlueBee robot autonomously moved away from the detected obstacle.

We then tested the real-time safe-distance maintenance algorithm under the same conditions. In the example shown in Figure 4, the obstacle was detected at  $1.8m$  from the bottom of the pool and thus the BlueBee robot performed an emergency braking stop within  $3s$ . The EKF was initialized at  $1m$  (see Appendix A) and the estimated relative distance  $d_{est}$  converged to the ground truth  $d$  given by the barometer within  $11s$  from the emergency braking response. The average percentage error after convergence  $d - d_{est}$  was  $5.3\%$ , with a minimum value of  $-9.52\%$  and a maximum value of  $26.84\%$ .  $d_{est}$  was used to maintain the BlueBee robot at a predefined safe distance of  $0.7m$  from the bottom of the pool. The imposed oscillations (see Figure 4.d) had an average amplitude of approximately  $0.2m$ .

Similar results were obtained by performing preliminary tests with the frontal camera and considering the side of the pool as an obstacle. Due to the lack of reliability of the equipped sonar in such a confined environment, we lacked a ground truth to validate our results.

### B. Tests carried out in harbour and lake

Real-time safe-distance maintenance tests were carried out in the Moulin Blanc harbour (in Brest, Brittany, France) in salt water. Experiments were performed with the downward camera under the same conditions as those carried out in the ENSTA Bretagne pool, with similar results (as shown in Figure 5.A i and ii). The bottom of the harbour was considered as the obstacle to avoid and was detected at a relative distance of about  $1.3m$ . An emergency braking

response was triggered within  $3s$ , after which the BlueBee robot maintained a safe distance of  $0.7m$  from the obstacle. Preliminary tests with the frontal camera in fresh water were also carried out in the Guerlédan lake (in Guerlédan, Brittany, France; see Figure 5.B.i and ii). Here, the EKF was initialized at  $1.5m$  and  $d^*$  was  $0.8m$ . Due to the high turbidity of the water, a Gaussian blur was applied to each frame before measuring the optic flow divergence and no further outlier filtering was performed. Although we had no ground truth to validate our results, the real-time safe-distance maintenance algorithm allowed the robot to avoid small and hollow obstacles and maintain a safe distance of  $0.8m$ . Tests with the downward camera were also performed, but the method was not effective since the engine's propulsion created dense clouds of particles when the BlueBee robot was close to the bottom of the lake. However, an emergency braking stop could still be performed.

A video of the tests carried out in the pool, harbor and lake are available at <https://youtu.be/qSBWyW11wX0>.

## VI. CONCLUSIONS

While optic flow cues are widely exploited for applications involving UAVs, only a small number of studies have explored their potential for underwater navigation. This is particularly interesting as previous authors have shown that optic flow cues can be measured with commonly available sensors such as monocular cameras [19, 24, 8, 12].

In this study, we present a real-time underwater collision avoidance method based on the optic flow divergence cue measured with a monocular camera. This method was tested onboard an ROV (here referred to as BlueBee robot) in a pool, a harbour and a lake to avoid downward and forward obstacles. The measured optic flow divergence was used to initiate an emergency braking response and then fused with low-cost IMU's outputs to estimate the relative distance of the BlueBee robot from the detected obstacle with an EKF. The estimated relative distance was used to reach a predefined safe distance from the obstacle. The optic flow divergence was then continuously measured thanks to a small imposed oscillation, allowing the robot to maintain the predefined safe distance.

Our experimental results show that the optic flow divergence cue can be used to avoid underwater collisions in real-time to facilitate remote control of an ROV. This method relies solely on the use of a monocular camera and an IMU, two sensors commonly available on off-the-shelf ROVs. No transformation of the perceived image is necessary to compensate for camera rotation movements: only a rough approximation of the highest component of the rotational optic flow is subtracted from the optic flow divergence. The method presented in this study is better suited to obstacles in close proximity and can therefore be considered as complementary to sonar in the distance range where sonar could be too affected by reverberation.

Future work will include a further analysis of each component of the rotational optic flow (expressed according to [16]) to improve their estimates and thus better measure the optic flow divergence. As the optic flow divergence allows the BlueBee robot to maintain a safe distance from the obstacle in order to



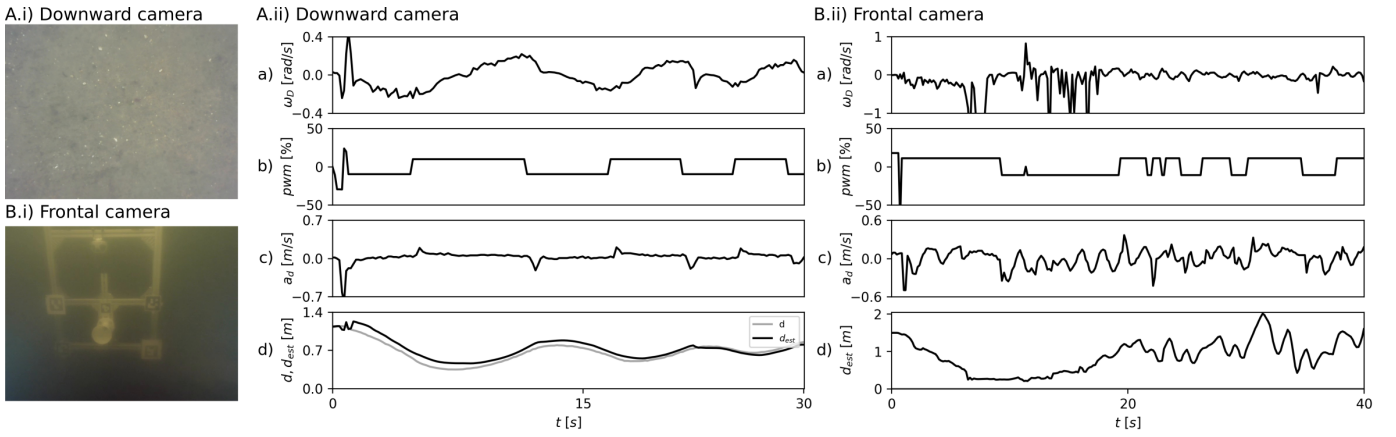


Fig. 5. A) Test carried out in the Moulin Blanc harbour (in Brest, Brittany, France): A.i) view from the downward camera, A.ii) a) measured optic flow divergence  $\omega_D$ , b) pwm command given to the robot, c) acceleration  $a_d$  in the direction of the obstacle given by the Inertial Measurement Unit (IMU) of the robot, d) comparison of the estimated relative distance  $d_{est}$  with the ground truth  $d$  given by the barometer. B) Test carried out in the Guerlédan lake (in Guerlédan, Brittany, France): A.i) view from the frontal camera, showing a hollow obstacle; A.ii) preliminary results. A video of the tests is available at <https://youtu.be/qSBWYwI1wX0>.

avoid collisions, we could consider using a similar technique to detect and follow a surface at a given distance based solely on optic flow cues (for dam inspection, for example). Future work will also include testing this approach for an Unmanned Surface Vehicle to perform avoidance of both fixed and moving obstacles.

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#### APPENDIX A VISIBILITY THRESHOLD

A test was carried out in the ENSTA Bretagne pool to determine the threshold below which the measured optic flow divergence can be considered an indicator of the presence of an obstacle. The BlueBee robot moved from the bottom of the pool to the surface and the barometer was used to measure its relative distance  $d$  from the bottom of the pool. The optic flow divergence was measured using the downward monocular camera with the robot's downward-facing lights switched on at maximum. Figure 6.a shows that from a distance  $d$  of about  $1m$  from the bottom of the pool the measured optic flow divergence ranges around  $0rad/s$ , indicating that the obstacle is no longer detected under these conditions. A test in which the robot descended from the surface to the bottom of the pool showed similar results (see Figure 6.b). To increase the robustness to noise, we chose a threshold  $\omega_{D \lim} = -0.05rad/s$ .

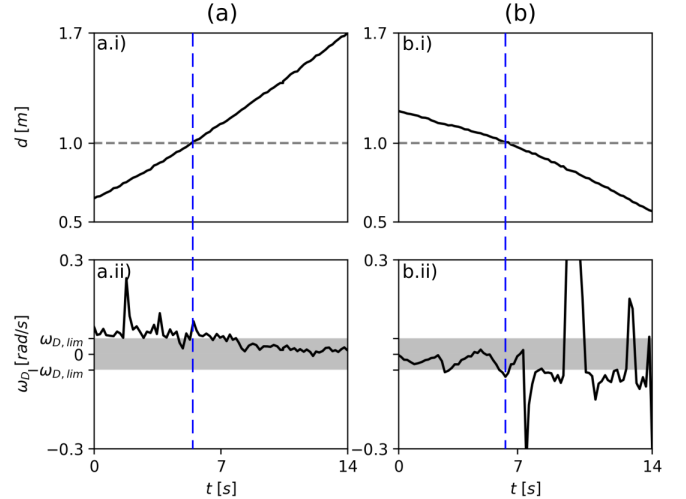


Fig. 6. Tests in which the BlueBee robot moves from the bottom of the pool to the surface (a) and descends from the surface to the bottom of the pool (b) respectively. (a.i and b.i) Distance  $d$  of the robot from the bottom of the pool given by the barometer. Only the time interval between  $0s$  and  $14s$  is shown, corresponding to the robot crossing the  $1m$  threshold (dashed blue line). (a.ii and b.ii) Measured optic flow divergence  $\omega_D$  (in black) and area bounded by the thresholds  $\pm\omega_{D \lim}$  (in grey).

#### APPENDIX B EXTENDED KALMAN FILTER

The BlueBee robot was modeled in the form of a double integrator receiving as input the acceleration in the direction of the obstacle  $a_d$  given by its IMU. The robot's state space representation can therefore be expressed as:

$$\begin{cases} \dot{X} = f(X, a_d) = A \cdot X + B \cdot a_d = \begin{bmatrix} 0 & 1 \\ 0 & 0 \end{bmatrix} \cdot X + \begin{bmatrix} 0 \\ 1 \end{bmatrix} \cdot a_d \\ Y = g(X) = [X(2)/X(1)] = V_d/d = \omega_D \end{cases} \quad (5)$$

where  $X = [d, V_d]^T$  is the ROV's state vector. The discretized model of the BlueBee robot used in the EKF calculations can be expressed as:

$$\begin{cases} X[k+1] = \Phi \cdot X[k] + \Gamma \cdot U[k] \\ Y[k] = C_k \cdot X[k] + D_k \cdot U[k] \end{cases} \quad (6)$$

with

$$\Phi = e^{A \cdot dt} \quad (7)$$

$$\Gamma = \left( \int_0^{dt} e^{A \cdot \tau} d\tau \right) \cdot B \approx dt \cdot B \quad (8)$$

$$C_k = g(X_k) = \begin{bmatrix} X_2[k] \\ X_1[k] \end{bmatrix} = \begin{bmatrix} V_d[k] \\ d[k] \end{bmatrix} \quad (9)$$

$$D_k = 0 \quad (10)$$

where  $dt$  is the discretization time.

#### REFERENCES

- [1] L. Bergantin et al. “Indoor and outdoor in-flight odometry based solely on optic flows with oscillatory trajectories”. In: *International Journal of Micro Air Vehicles* (2023), p. 15.
- [2] L. Bergantin et al. “Oscillations make a self-scaled model for honeybees’ visual odometer reliable regardless of flight trajectory”. In: *Journal of the Royal Society Interface* 18.182 (2021), p. 20210567.
- [3] J.-Y. Bouguet et al. “Pyramidal implementation of the affine lucas kanade feature tracker description of the algorithm”. In: *Intel corporation* 5.1-10 (2001), p. 4.
- [4] F. Boyer et al. “Underwater pre-touch based on artificial electric sense”. In: *The International Journal of Robotics Research* 39.6 (2020), pp. 729–752.
- [5] A. Bucci et al. “Comparison of feature detection and outlier removal strategies in a mono visual odometry algorithm for underwater navigation”. In: *Applied Ocean Research* 118 (2022), p. 102961. ISSN: 0141-1187.
- [6] A. Burton and J. Radford. *Thinking in perspective: critical essays in the study of thought processes*. Taylor & Francis, 2022.
- [7] V. Creuze. “Monocular odometry for underwater vehicles with online estimation of the scale factor”. In: *IFAC 2017 World Congress*. 2017.
- [8] G. de Croon. “Monocular distance estimation with optical flow maneuvers and efference copies: a stability-based strategy”. In: *Bioinspiration & biomimetics* 11.1 (2016), p. 016004.
- [9] F. Expert and F. Ruffier. “Flying over uneven moving terrain based on optic-flow cues without any need for reference frames or accelerometers”. In: *Bioinspiration and Biomimetics* 10 (2015).
- [10] A. Ferone et al. “A Synthetic Dataset for Learning Optical Flow in Underwater Environment”. In: *Applications of Artificial Intelligence and Neural Systems to Data Science*. Singapore: Springer Nature Singapore, 2023, pp. 147–156.
- [11] B. Herissé et al. “Landing a VTOL unmanned aerial vehicle on a moving platform using optical flow”. In: *IEEE Transactions on robotics* 28.1 (2011), pp. 77–89.
- [12] H. W. Ho, G. de Croon, and Q. Chu. “Distance and velocity estimation using optical flow from a monocular camera”. In: *International Journal of Micro Air Vehicles* 9.3 (2017), pp. 198–208.
- [13] H. W. Ho et al. “Adaptive gain control strategy for constant optical flow divergence landing”. In: *IEEE Transactions on Robotics* 34.2 (2018), pp. 508–516.
- [14] F. Iida. “Biologically inspired visual odometer for navigation of a flying robot”. In: *Robotics and autonomous systems* 44.3-4 (2003), pp. 201–208.
- [15] F. Kendoul, I. Fantoni, and K. Nonami. “Optic flow-based vision system for autonomous 3D localization and control of small aerial vehicles”. In: *Robotics and autonomous systems* 57.6-7 (2009), pp. 591–602.
- [16] J.J. Koenderink and A.J. van Doorn. “Facts on optic flow”. In: *Biological Cybernetics* 56 (1987), pp. 247–254.
- [17] D. G. Lowe. “Distinctive image features from scale-invariant keypoints”. In: *International journal of computer vision* 60 (2004), pp. 91–110.
- [18] D. G. Lowe. “Object recognition from local scale-invariant features”. In: *Proceedings of the seventh IEEE international conference on computer vision*. Vol. 2. Ieee, 1999, pp. 1150–1157.
- [19] B. D. Lucas and T. Kanade. “An iterative image registration technique with an application to stereo vision”. In: *IJCAI’81: 7th international joint conference on Artificial intelligence*. Vol. 2. 1981, pp. 674–679.
- [20] P.A. Miller et al. “Autonomous underwater vehicle navigation”. In: *IEEE Journal of Oceanic Engineering* 35.3 (2010), pp. 663–678.
- [21] R.C. Nelson and J. Aloimonos. “Obstacle avoidance using flow field divergence”. In: *IEEE Transactions on Pattern Analysis and Machine Intelligence* 11.10 (1989), pp. 1102–1106.
- [22] F. Ruffier and N. Franceschini. “Optic flow regulation: the key to aircraft automatic guidance”. In: *Robotics and Autonomous Systems* 50.4 (2005), pp. 177–194.
- [23] H. Teigland, V. Hassani, and M. T. Møller. “Operator focused automation of ROV operations”. In: *2020 IEEE/OES Autonomous Underwater Vehicles Symposium (AUV)*. 2020, pp. 1–7.
- [24] F. Van Breugel, K. Morgansen, and M. H Dickinson. “Monocular distance estimation from optic flow during active landing maneuvers”. In: *Bioinspiration & biomimetics* 9.2 (2014), p. 025002.
- [25] P. Xia, H. You, and J. Du. “Visual-haptic feedback for ROV subsea navigation control”. In: *Automation in Construction* 154 (2023), p. 104987.
- [26] F. Xiao et al. “Optic flow-based reactive collision prevention for mavs using the fictitious obstacle hypothesis”. In: *IEEE Robotics and Automation Letters* 6.2 (2021), pp. 3144–3151.
- [27] Z. Xu et al. “An underwater visual navigation method based on multiple ArUco markers”. In: *Journal of Marine Science and Engineering* 9.12 (2021), p. 1432.
- [28] B. Zhang et al. “Autonomous underwater vehicle navigation: a review”. In: *Ocean Engineering* (2023), p. 113861.
- [29] S. Zhang et al. “Visual SLAM for underwater vehicles: A survey”. In: *Computer Science Review* 46 (2022), p. 100510.