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Multi-UAVs end-to-end Distributed Trajectory Generation over Point Cloud Data

Antonio Marino, Claudio Pacchierotti, Paolo Robuffo Giordano

Abstract—This paper introduces an end-to-end trajectory planning algorithm tailored for multi-UAV systems that generates collision-free trajectories in environments populated with both static and dynamic obstacles, leveraging point cloud data. Our approach consists of a 2-fork neural network fed with sensing and localization data, able to communicate intermediate learned features among the agents. One network branch crafts an initial collision-free trajectory estimate, while the other devises a neural collision constraint for subsequent optimization, ensuring trajectory continuity and adherence to physical actuation limits. Extensive simulations in challenging cluttered environments, involving up to 25 robots and 25% obstacle density, show a collision avoidance success rate in the range of 100 – 85%. Finally, we introduce a saliency map computation method acting on the point cloud data, offering qualitative insights into our methodology.

Index Terms—distributed control, graph neural network, trajectory generation

I. INTRODUCTION

The domain of multi-agent Unmanned Aerial Vehicle (UAV) trajectory planning has garnered significant attention, given its diverse range of applications [1]–[3]. In these settings, planning algorithms play a pivotal role in calculating trajectories that are both safe and directed towards a defined goal. These algorithms have to consider the dynamic state of the environment and the presence of neighbouring agents. In practical applications involving drones, trajectory planning is crucial to navigate around obstacles and accommodate limitations in the drone’s actuators [4]–[6].

Despite possessing more theoretical guarantees, centralized approaches are often less appealing than decentralized counterparts due to their computationally intensive nature and the dependence on full-state information of each robot at every algorithm iteration which renders them impractical for real-world execution [7]. In contrast, decentralized planning not only demonstrates enhanced scalability but also provides robustness against potential failures in a centralized architecture [8].

For more effective coordinated planning, the planning algorithm must consider not only local sensing data but also the planning decisions of a few neighbouring team members [9]. Thus, communication emerges as a critical element in realizing distributed solutions for multi-agent systems. Within this context, one of the focuses of this article

is to integrate local sensing and communication strategies to achieve end-to-end distributed multi-UAV motion planning.

For UAV navigation, learning-based control generated from point clouds or images was shown in [10]–[12], emphasising the computational advantages of such approaches. Recently, distributed learning-based methods have started to appear for multi-agent scenarios proposing reinforcement learning approaches [13]–[15] and Graph Neural Networks (GNNs) ones [16], [17]. In particular, since GNNs exploit the communication graph by construction, they show remarkable performances in encoding distributed policies as shown by Blumenkamp et al. [18], who were the first to demonstrate multi-robot coordination for navigating narrow passages using GNNs on real robots. However, the use of learning for control mandates additional safety guarantees, due to its limitation in predicting control commands beyond the distribution of the scenarios on which they were trained. Addressing this concern, GLAS [19] introduces a local safety function, which, in conjunction with control prediction, ensures stability and safety for both single and double integrators. Nonetheless, these results primarily hold in static environments without considering the actuation limits of actual robots and real robot dynamics. A more recent work [20] emphasised the combination of safety control strategies and learning over a graph of agents and obstacles. The authors propose a GNN-based neural network to predict an initial control estimate. They also propose a constraint function characterizing the forward invariant set of a Control Barrier Function (CBF) optimization from LiDAR sensing data.

However, all these methods are susceptible to trapping robots in local minima as they compute only a local control action. To explicitly tackle this problem, a contribution of this work is to propose a trajectory planning algorithm that takes into account spatio-temporal predictions and can avoid local minima. Planning for multi-drone coordination inherently poses a high-dimensional challenge, even when safety is the sole requirement. Moreover, planning algorithms often necessitate access to map data for obstacle information, as noted in prior work [21]. This map should be updated online to tackle environmental changes which in large-scale environments can become cumbersome, bringing a computational bottleneck. Furthermore, optimization-based approaches may need to relax collision constraints as team density increases. Potentially, this relaxation leads to collisions, as discussed in [22] which reports real-time motion planning for a swarm up to 20 drones. The recent literature [23]–[26] has presented notable results for robust multi-drone large-space travelling

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that take into account physical size, actuator limitations, alongside tracking disturbances, communication delay, and asynchronous communication. However, these algorithms typically rely on a perfect knowledge of the environment, i.e., shape, position, and trajectory of all obstacles at all times, which generally is unavailable in real-world scenarios. Moreover, these algorithms need to tune the map grid size to reach the target and avoid collisions and, although implementing a decentralized algorithm, every drone needs to communicate with all the other drones in the team at the expense of less scalability. Addressing these challenges is critical for the deployment of multi-drone systems.

In this paper, we present a novel data-driven approach for distributed trajectory generation and safety collision avoidance under LiDAR-based observations. Our main contributions are in proposing:

- A decentralized and asynchronous planning of coordinated trajectories from point cloud data is deployed on each drone, by using a neural network architecture leveraging attention-based GNN to learn a decentralized policy.
- An optimization that generates a collision-free trajectory by utilizing a predicted collision constraint derived from the point cloud data and communication between the drones.
- An algorithm for computing the point cloud saliency map due to the predicted trajectory and collision constraint as an analysis tool for neural network performances.

II. PROBLEM STATEMENT

Consider a distributed trajectory generation problem for a set of N UAVs modelled in $SO(3)$ with second-order dynamics. The UAV team (V) operates within a three-dimensional workspace containing static and dynamic obstacles \mathcal{O}_k . The dynamic obstacles are akin to non-cooperative agents, lacking communication capabilities with the drones. Each drone’s objective is to navigate the environment toward its target without colliding with other agents. A team mission is the collective traversing of the space such that every drone satisfies its objective. We make the following assumptions

Assumption 1. *Each drone is controlled via a trajectory-tracking algorithm and equipped with a 3D range sensor, such as a LiDAR.*

Assumption 2. *At time t , we assume the orientation $quat_i(t)$ and the triplets of position $r_i(t)$, velocity $v_i(t)$ in world frame are available to agent i .*

Assumption 3. *Each drone can communicate with a limited number of neighbours at a given frequency without communication loss*

The observation data for a drone i is denoted by $pc_i \in R^{m \times 3}$, which includes the relative positions of the m “hit” points in the scanned environment. The trajectory generated must comply with the following constraints:

- **collision avoidance:** each pair of drones and drone-obstacle maintains a safety distance of $2d$ throughout the whole trajectory, where $d > 0$ is the radius of a circle that can contain the entire physical body of each agent.
- **limited sensing and communication:** each agent has a limited sensing and communication range radius R . We define the neighbours of agent i as $\mathcal{N}_i = \{j \in V \mid \|r_i - r_j\|_2 \leq R, j \neq i\}$; therefore, the agents can only sense other agents or obstacles inside a sphere of radius R originating on the agent.
- **physical limitations:** The generated trajectory must satisfy the drone’s velocity and acceleration limits and must be smooth and continuous relative to the actual state.

III. METHOD

This section presents the proposed policy as a neural network that fulfils the above requirements. We start by presenting the trajectory encoding used by the proposed approach. Then, we present the privileged expert used for training and how we process the input features. Subsequently, we describe the neural network architecture depicted in Fig. 1 and deployed on the drone composed of input features processing, communicated variables aggregation and the optimization layer to cope with physical limitations. Finally, we describe the algorithm to compute the saliency map, used to analyze the neural network behaviour in the results.

A. Trajectory Representation

The trajectory used by each drone is a polynomial-based curve, e.g., B-Splines, which allows us to impose velocity and higher derivatives limitation through linear constraints on the trajectory control points (CP). In fact, the convex hull of the curve CP leads to the representation of the outer trajectory polyhedron and, by imposing constraints on the CP, we ensure they are satisfied throughout the trajectory.

In this paper, we adopted a MINVO basis [27] expression for the curve. MINVO bases are recently introduced in the literature and, compared to B-spline or Bernstein bases, form a simplex \mathcal{M} enclosing the given polynomial curve with minimum volume by construction. Hence, these bases lead to less conservative polyhedron representations. Given a polynomial order, we can pass from MINVO to B-Spline CP and vice-versa by a linear transformation. For these reasons, it is ideal to generate and apply constraints on MINVO CP for trajectory descriptions. In particular, we define two linear mappings, $h_v(\cdot)$ and $h_a(\cdot)$, to pass from MINVO CPs to their velocity and acceleration, respectively.

B. Privileged Expert

Our trajectory planner is trained via privileged learning [28]. Specifically, we generate a dataset from an expert controller: MADER [23]. MADER employs a decentralized and asynchronous approach to generate feasible and safe trajectories, leveraging a combination of path planning and Quadratic Programming (QP) optimization. We can consider

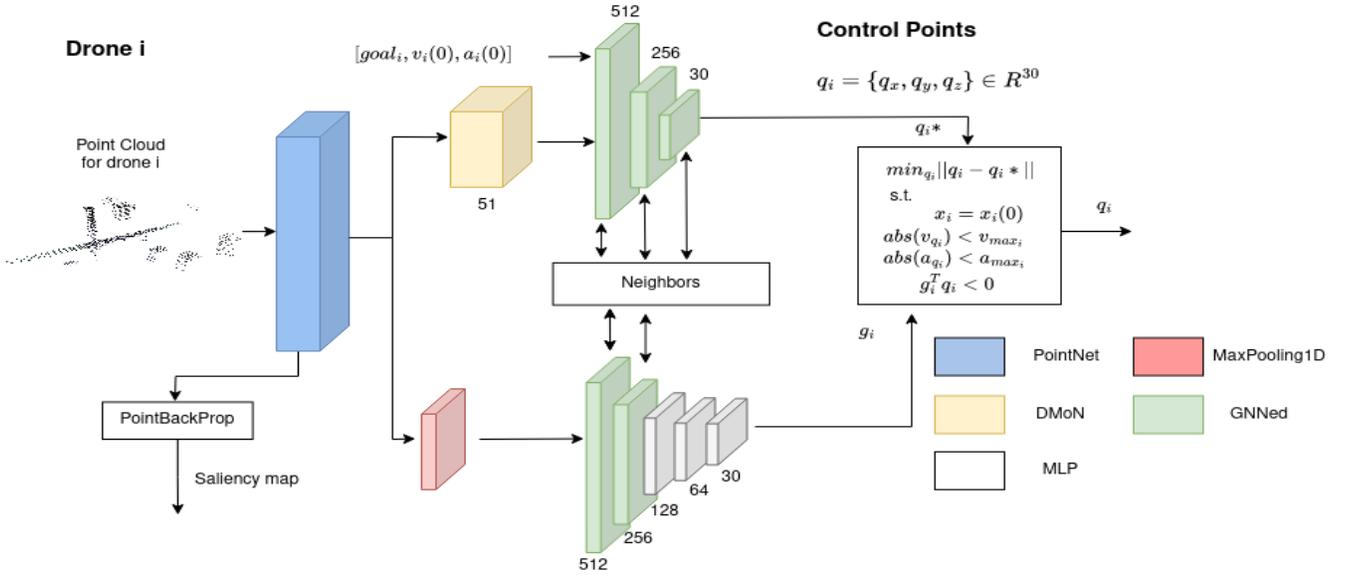


Fig. 1: neural network architecture deployed on each drone.

this algorithm as a privileged expert for two reasons: first, MADER exploits comprehensive knowledge of the physical dimensions of obstacles and drones, as well as the trajectories of both, which is an information typically unavailable in real-world scenarios; second, MADER ensures to find feasible trajectories only for unlimited time budget available in simulation. The optimization proposed by MADER focuses on determining the separation planes between the drone and potential obstacles throughout the trajectory, facilitating motion within a safe region. Moreover, the same reasoning is applied to trajectories committed by the other drones, leveraging the trajectory outer simplex as a cluttered area. However, the growth of the decision variables is proportional to the number of obstacles and other drones within the decision horizon. This renders the optimization more difficult to solve within a limited time budget, leading to potential infeasibility and hazardous halts. However, in simulation where full obstacle information is available and no time constraints are present, we can fully exploit MADER to generate a dataset of safe trajectories.

In our approach, to construct a dataset, we chose MADER over centralized alternatives as its features of asynchrony and decentralization align well with the objectives of our trajectory planner. Moreover, learning over an already decentralized expert policy eases the training process. After the training process, at execution time, the learned policy does not rely on any privileged information and synthesizes the trajectory from sensor inputs only.

C. Neural Network Input Features

Every drone i in the team shares the same neural network architecture that accepts as input raw point clouds normalized in a unitary sphere and projected into the world frame using $quat_i$. To enhance the representation of the sensed environment, we manually augment the point cloud by incorporating safety boxes around drones entering the sensing range, sized

50% larger than the dimensions of the agent. This strategic addition enables the encoding of an extra safety margin for drone-to-drone collision avoidance, leveraging only point cloud information.

Additionally, the proposed neural network uses also the current velocity, v_i , and the current desired acceleration, a_i , divided respectively by the maximum velocity v_{max} and the maximum acceleration a_{max} allowed. We also include the goal location ($goal_i$) in the drone i frame, projected on the sensing sphere with radius R if the distance to the goal is greater than R . Then, the $goal_i$ is divided by R to have coordinates in the range $[-1, 1]$. Drone i can communicate intermediate neural network features with drones in its neighbourhood \mathcal{N}_i . We enclose the drone initial conditions in $x_{i0} = [0_3, v_i, a_i]$ for a generated trajectory starting from the ego location, $0_3 = [0, 0, 0]$. In the final deployment, we add to the learnt control point q the current drone location $r_i(t)$ to track the trajectory.

D. Neural Network Structure

The neural network consists of two main branches that process the point cloud pc_i , combine it with localization data $[goal_i, v_i, a_i]$, and communicate features to compute a trajectory guess q_i^* (described by MINVO CPs) and a vector of collision coefficients g_i for drone i . This latter is used to define a linear combination of CPs composing q_i , thereby classifying its safety. Specifically,

Definition III.1. The scalar value $g_i^T q_i$ is $g_i^T q_i < 0$ if and only if q_i belongs to the safe set \mathcal{S}_i , where $\mathcal{S}_i = \{q_i \mid \|v_i - pc_i\|_2^2 > 2d, v_i \in \mathcal{M}(q_i)\}$ and $\mathcal{M}(q_i)$ is the outer simplex of q_i .

By introducing the collision coefficients g_i , we aim to increase the robustness of q_i found by leveraging imitation learning on the collected dataset. The term $g_i^T q_i$ can be used as a linear constraint to generate a safe trajectory. Leveraging

the initial guess \mathbf{q}_i^* and the collision coefficient \mathbf{g}_i , we formulate a Quadratic Programming (QP) layer as the final stage within the neural network. This QP layer optimizes \mathbf{q}_i to closely align with the initial guess \mathbf{q}_i^* , while concurrently ensuring adherence to predefined maximum drone velocity (v_{max}) and acceleration (a_{max}) constraints. This combination not only refines trajectory predictions but also strengthens the system’s resilience in navigating complex environments. The QP formulation is the following:

$$\begin{aligned} & \min_{\mathbf{q}} \|\mathbf{q}_i - \mathbf{q}_i^*\|_2^2 \\ \text{s.t.} & \\ & \mathbf{x}_i(\mathbf{t}_0) = \mathbf{x}_{i0} \\ & \text{abs}(\mathbf{v}) \leq v_{max} \leftarrow \forall \mathbf{v} \in h_v(\mathbf{q}_i) \\ & \text{abs}(\mathbf{a}) \leq a_{max} \leftarrow \forall \mathbf{a} \in h_a(\mathbf{q}_i) \\ & \mathbf{g}_i^T \mathbf{q}_i \leq 0 \end{aligned} \quad (1)$$

The point cloud is processed by a PointNet layer [29] comprising three filters of 64, 128, 256, respectively. PointNet employs sequences of point transformations through a compact transformation network and MLP to generate spatially-permutation invariant features. The output of this layer, $m \times 256$ with m points, forks to serve distinct purposes within the collision coefficients branch and the trajectory generation branch. To generate \mathbf{g}_i , i.e., assigning a safety score to trajectories crossing the environment, we require global features extracted from the point cloud. Consequently, the PointNet output is transformed into a 256-dimensional vector through global max pooling over the features.

Conversely, within the trajectory generation branch, our approach involves further clustering of the point cloud based on the features learned by PointNet. Clusters prove advantageous in classifying spatial regions that hold crucial information for trajectory generation. Clustering was already adopted in the design of PointNet++, which consists of spatial clusterization coupled with smaller PointNet modules. We adopted DMoN [30], a clustering methodology based on a graph neural network, approximating spectral modularity maximization to recover high-quality features and spatial-based clusters. Unlike PointNet++, DMoN’s approach does not solely rely on spatial displacement and does not require a nested architecture of PointNets. The adjacency matrix required by DMoN is represented as a binary sparse map encoding the spatial proximity of the points. This strategic combination of PointNet and DMoN very well captures intricate spatial structures for trajectory generation tasks, as we show in the results of Sec. V. We chose a number of clusters (51) that, together with the localization data, form a 64-dimensional vector for the next layer.

Both branches exchange the local features with the neighbouring agents using a message-aware graph attention network (MAGAT) [16]. Assuming that each drone i can communicate with its set of neighbours \mathcal{N}_i , the communication graph can be represented by a binary sparse matrix \mathcal{S} . We let $\mathbf{A} = \mathcal{S} \in \mathbb{R}^{N \times N}$ be the adjacency matrix of the communication graph. Given a graph signal $\mathbf{x} \in \mathbb{R}^{N \times F}$

distributed over the drones, we can define a graph filter as

$$H_{\mathbf{A}}(\mathbf{x}) = \sum_{k=0}^K \mathbf{A}^k \mathbf{x} \mathbf{H}_k. \quad (2)$$

which combines the elements of \mathbf{x} over the adjacency matrix of the communication graph and applies the graph filter weights $\mathbf{H}_k \in \mathbb{R}^{F \times F'}$. The quantity $K > 1$ represents the filter length, which implies repeated 1-hop communications over the graph. Therefore, the filter can be executed distributively over the graph. The filter in eq. (2) transforms the graph signal from an F -features space into a signal of an F' -features space. MAGAT enhances this framework by incorporating an attention mechanism to weigh the relative importance of drone features. Specifically:

$$\begin{aligned} H_{\mathbf{A}\mathcal{E}}(\mathbf{x}) &= \sum_{k=0}^K (\mathcal{E} \circ \mathbf{A})^k \mathbf{x} \mathbf{H}_k. \\ \mathcal{E} &= \left[\frac{\exp(\text{LeakyReLU}(x^{iT} W x^j))}{\sum_{\mathcal{N}_i} \exp(\text{LeakyReLU}(x^{iT} W x^j))} \right]_{x^i, x^j \in \mathbf{x}} \end{aligned} \quad (3)$$

where \mathcal{E} is the matrix of attention weights. Considering the need to communicate graph signals over the network, the size of F affects network congestion. To address this, we extend the scheme by introducing an encoding-decoding mechanism to compress the graph signal before communication and reconstruct its original dimension afterwards. This involves point-wise learnable encoding and decoding functions, denoted as $e_{\theta}(\cdot) : \mathbb{R}^F \rightarrow \mathbb{R}^G$ and $d_{\theta}(\cdot) : \mathbb{R}^G \rightarrow \mathbb{R}^F$, respectively:

$$H_{\mathbf{A}ed}(\mathbf{x}) = \sum_{k=0}^K d_{\theta}((\mathcal{E} \circ \mathbf{A})^k e_{\theta}(\mathbf{x})) \mathbf{H}_k. \quad (4)$$

Here, $G \ll F$ reduces the number of communicated variables, with e_{θ} and d_{θ} functions implemented as MLP with ReLU activation functions. The resulting GNNed layer,

$$\mathbf{x} = \text{ReLU}(H_{\mathbf{A}ed}(\mathbf{x})) \quad (5)$$

is employed 3 times in the trajectory generation branch (with filter dimensions 512, 256, 30) and twice in the collision branch (with filter dimensions 512, 256), totalling $L = 5$ layers. Set parameters include $K = 1$ and $G = 5$. We can use the unit-delay communication model [31] and communicate unit-time delayed signals to compute the graph filters in (4) in one shot, by sending $[x_i(t), \dots, A_i^{K-1} x_i(t - K - 1)]$ for each agent. This model allows releasing a new output at each communication iteration but at the cost of more communicated variables. Therefore, each drone communicates $L G K$ variables, i.e. 25 in our implementation.

E. Point Cloud Saliency Map

A saliency or attention map, denoted as $s = [0, 1]^m$, serves as a feature map unveiling the relevance of input data in the decision-making process. This map is instrumental in inspecting and interpreting neural networks, particularly under distribution shifts. Existing studies on point cloud

Algorithm 1 PointBackProp

Require: point cloud (pt), model
 $\bar{h}_1, \bar{h}_2, \dots, \bar{h}_P \leftarrow$ compute average maps from model
 $s := \bar{h}_P$
for $i = N-1 \dots 1$ **do**
 $s := \bar{h}_i \cdot s$
 Normalize s between $\{0, 1\}$
end for
compose point cloud values $\{s, pt\}$

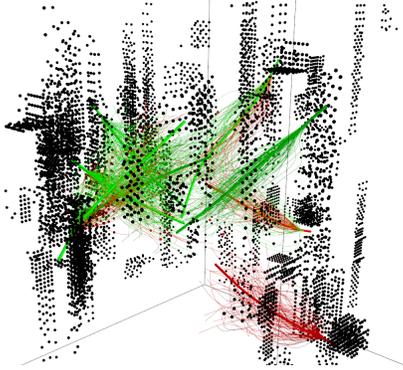


Fig. 2: Sample trajectory generation for collision dataset. The trajectories starting from the drone location are coloured in red if they are colliding and in green if they are safe.

saliency maps [32], [33] predominantly rely on gradient-based methods or incorporate additional neural network architectures. As highlighted by the authors of VisBackProp [34], for autonomous navigation, it is convenient to dispose of a gradient-free method that can be evaluated online. Addressing this gap, we introduce PointBackProp, which we apply to the PointNet layer in our architecture. Notably, PointNet can be conceptualized as a sequence of 1D-CNNs with a unitary kernel size and variable filter dimensions, drawing a direct parallelism with VisBackProp and 2D-CNNs. We focus on the PointNet layer in our architecture, as it processes the point cloud and dynamically shapes itself during training to enhance the representation of points for trajectory generation. Having a PointNet made of P sequences of matrix transformations and 1D-CNN, we save the average map \bar{h}_i computed over the features generated after each sequence in one evaluation round of the neural network in Fig. 1. Starting from \bar{h}_P , we loop over the list of \bar{h}_i by multiplying the actual element with previous element of the list and normalize between $[0, 1]$ after each multiplication. The algorithm is summarized in Algorithm 1.

IV. TRAINING

Our model training dataset \mathcal{D} encompasses UAV trajectories under the control of the expert controller within a simulated environment.

The simulation environment incorporates a 10% obstacle density confined within a sphere of 10m radius centred in the world origin. The obstacles are partitioned equally into static

Algorithm 2 Training Algorithm

Require: \mathcal{D} batch size b
for point cloud in \mathcal{D} **do**
 Combine point clouds of the N drones
 Generate random of trajectories \hat{q}
 Solve QP to constraints \hat{q} with the initial conditions and physical limitations
 Calculate collision indexes C for \hat{q}
 Append trajectories and collision indexes to the dataset
 $\hat{\mathcal{D}} \leftarrow \hat{\mathcal{D}} \cup \{\hat{q}, C\}$
end for
calculate adjacency matrix of drones A \triangleright This step is only needed in centralized training
calculate adjacency of point clouds A_{pt}
for $i = 1 \dots$ epochs **do**
 collect b batches $\{pt, v, a, quat, goal, q\} \leftarrow \mathcal{D}$
 compute $q^*, g \leftarrow$ model
 if $i > epochs_i$ **then**
 prepare QP in eq (1) with constraint $g^T q^* < 0$
 Solve QP $\rightarrow q$
 if QP feasible **then**
 $q \rightarrow q^*$
 end if
 end if
 extract $\{\hat{q}, C\}$ in $\hat{\mathcal{D}}$
 Compute constraint $L_g(g, \hat{q}, C)$ using eq (7)
 Compute loss $L_q(q, q^*)$ in eq (6)
 Update model weights
end for

and dynamic elements, with the dynamic obstacles following a three-dimensional trefoil knot motion spanning a width of 1m. The obstacle trajectories reach a maximum speed of 2m/s. For each mission, we randomly placed 8 drones around the surface of the 10-m sphere, with each drone target located on the opposite side of the sphere surface, forcing the traversal of the sphere centre. The drones move with a maximum velocity of 3.5m/s in all directions, a maximum planar acceleration of 20m/s² and a vertical acceleration of 9.6m/s². Moreover, we assume their size to be confined in a sphere of radius $d = 0.15m$ and having a sensing/communication radius of $R = 4$ m. At a sampling rate of 15Hz, we capture point cloud data, localization information, and current control trajectory in MINVO control points, starting from the current drone location. The saved trajectory has 10 equally spaced time knots for each axis starting from the current timestamp t_0 to one second. We consider that one second offers a good compromise between knots resolution and prediction horizon. Therefore, the trajectories are defined solely by 10 CPs for each axis for segment polynomials of order 3. This helps the training process by focusing on learning the control points. In addition, we generate random trajectories \hat{q} offline, originating from the initial robot location, and categorize them as successful or unsuccessful based on definition III.1 within the joint point cloud space,

i.e. successful if the trajectory does not collide with obstacles or agent, as depicted in Figure 2. Moreover, we introduce a diminishing safety distance d along the trajectory, ranging from the drone’s actual size at the trajectory’s initiation to 0 at its termination. This approach optimizes the safe set by progressively reducing conservatism, thereby prioritizing the safety of the trajectory’s initial location:

$$L_q = \sum_{i \in V} \frac{1}{30} \|q_i - q_i^*\|_2^2 \quad q_i \in \mathcal{D}, \quad (6)$$

$$L_g = \sum_{i \in V} \sum_{\hat{q}_i \in \mathcal{S}_i} [g_i^T \hat{q}_i]^+ \sum_{\hat{q}_i \notin \mathcal{S}_i} [-g_i^T \hat{q}_i]^+, \quad (7)$$

where $[\cdot]^+ = \text{Softplus}(\cdot)$ stands for a continuous ReLU function ensuring strict constraint satisfaction. We solve the imitation learning problem using the ADAM algorithm [35] with a learning rate $1e-3$ and forgetting factors 0.9 and 0.999. We trained for 200 epochs of which in the first 50 the loss of eq. (6) is computed on the trajectory guess, without solving the QP. This solution helps to ease the learning and predict a good initial guess. If the QP is unfeasible, we used the initial guess to train our neural network. We exploit OptNet [36] to realize a differentiable quadratic programming layer and use classic backpropagation methods during training. We summarize the training algorithm in 2.

V. EXPERIMENTS

To test the validity of our approach, we conducted two sets of experiments for the mission described in the Section IV. The communication between the drones is employed through ROS with a communication rate of 100Hz while a new trajectory is calculated when a new point cloud is sensed at 15Hz . As specified in the assumption, we do not consider communication loss but, being the trajectory computation at a lower rate, we can guarantee a communication loss margin of 0.056s .

In the first experiment, we consider a variable number of agents in a range of $[4, 25]$, with dynamic and static obstacle density of 10% of the space. In the second experiment, we fixed the number of agents to 8 but we considered an increasing obstacle density from 5% to 25%. In both experiments, we evaluate the average success rate and average travel time for the agents to reach their respective targets. For each experimental condition (number of drones in team, obstacle density), we carried out 50 repetitions of the travelling mission. We consider a mission to be successful if all the agents reach their target without colliding. We proceeded with an ablation study to evaluate our approach:

- *ours w/o GNN*: we replaced GNN layers with normal MLP, to evaluate the impact of communication over the predictions.
- *ours w/o opt*: we did not use the predicted constraint g to test the impact of this introduced feature.
- *Pointnet++*: we replaced our solution of Pointnet-DMoN with Pointnet++ and max pooling.

- *ours w/o DMoN*: we removed DMoN clustering and used max pooling to predict the trajectory guess, as for the constraint prediction branch.

Additionally, for comparison, we also consider MADER running in real-time, providing full obstacle trajectories but a limited time budget of 0.35s for each optimization. The average computational time of our approach is 1.3ms , even if the real computation time is dependent on the number of points in the point cloud.

A. Results

We present an analysis of the average success rate and average travel time on successful trajectories, as illustrated in Figure 3. Our proposed neural network consistently achieves a remarkable success rate of 100% for obstacle densities up to 15% and 16 robots, gradually decreasing to 85% for the highest obstacle density of 25%. Notably, the effectiveness of our model is closely tied to point cloud processing, as evidenced by the success rates of *Pointnet++* and *ours w/o DMoN*, ranging from 85% to 40%. The clustering capabilities of *Pointnet++* contribute to an average 10.5% higher success rate compared to *ours w/o DMoN*, emphasizing its impact on environment processing.

When the model does not exploit the learnt collision constraint g , it encounters difficulties in finding collision-free trajectories, especially in high-constraint spaces populated by both cooperative and non-cooperative agents where the success rate diminishes to 85% for an obstacle density of 25% and 25 robots. The integration of GNN enhances the model’s resilience to collisions and traversal time as the number of drones increases, showcasing the advantages of cooperative trajectory predictions. Our approach shows advantages also compared to MADER with a high density of obstacles and robots primarily because when the optimization in MADER does not find a feasible trajectory the algorithm keeps using the previously computed trajectory. When the drone reaches the end of the trajectory, it breaks remaining exposed to obstacle collision until the optimization becomes feasible again because of the dynamical changes in the environment. Notably, *ours w/o opt* and MADER reach the same success rate of 85% with 25 drones. We speculate that this result is due to the GNN well imitation of coordinated behaviours.

Our approach exhibits the lowest average travel time of 10.3s with 25 robots even if *ours w/o GNN* and *ours w/o opt* find faster trajectories to traverse the space with fewer drones ($[5 - 10]$) and travel times comparable to *ours* as obstacle density increases. Moreover *ours w/o opt* has the lowest travel time when the obstacle increases with $15\text{s} \pm 0.4$, at the expense of less safe trajectories. In contrast, *Pointnet++* and *ours w/o DMoN* have similar travel times, approximately 16s with a high variance of more than 1s , facing drone deadlock situations or predicting longer paths to reach the goal.

Our approach reaches a similar average time to MADER as we used it to generate the dataset. However, we note that MADER does not generate global optimal time trajectories due to its asynchronous communication strategy, favouring

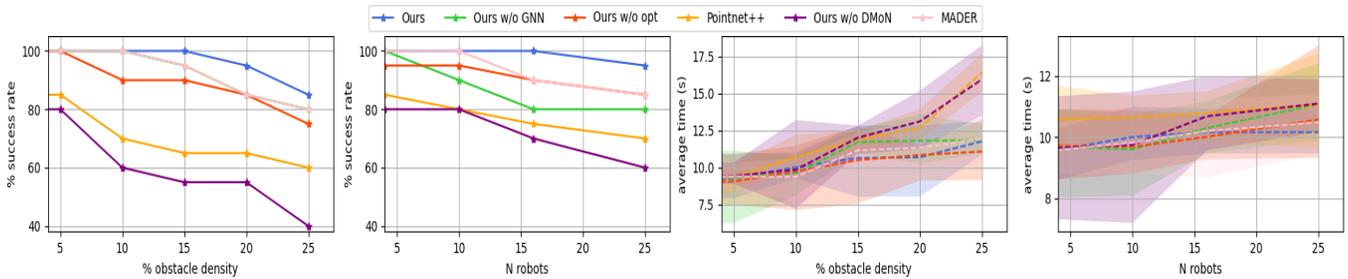


Fig. 3: Success rate and safety rate increasing obstacles and agents in the range of obstacle density [5% – 25%] and number of robots between [5 – 25] for our approach, ours without GNN, ours without collision constraint, ours with Pointnet++, ours without DMoN and MADER algorithm.

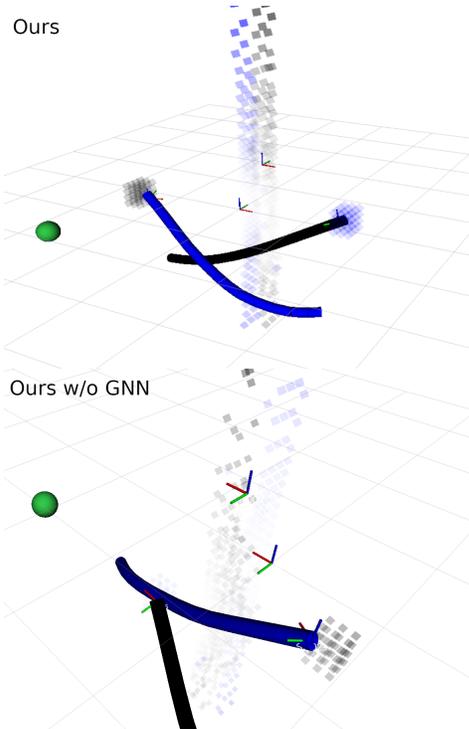


Fig. 4: Saliency map for two drones and one static obstacle for the proposed approach and the proposed without GNN

the first drone committing the trajectory. Subsequently, subsequent drones must adapt to avoid collisions, resulting in non-optimal trajectories.

We use Algorithm 1 to generate saliency maps, enabling interpretation of network behaviour and providing insights into the point cloud’s contribution to trajectory prediction. To emphasize the contribution of different sensing points, we assign distinct colours to points sensed by individual drones, while the alpha channel represents saliency values, with transparent points indicating lesser contributions to predictions. The saliency map allows to make qualitative assessments of the neural network ability to exploit the sensing data to make decisions. We expect that the point distances from the drone affect their relevance as the network tries to predict spatio-temporal commands and possible collisions surrounding the drone, this latter is not dependent

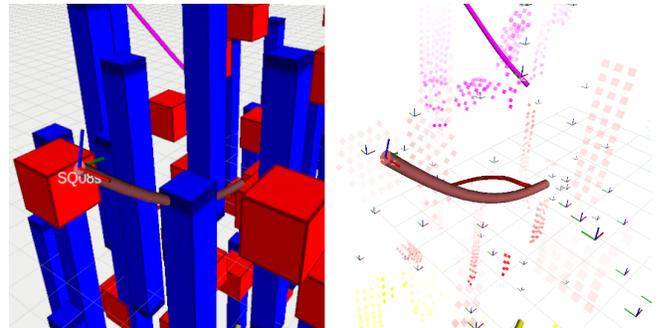


Fig. 5: Saliency map (on the right) of collision case using our approach without the collision constraint for a trajectory starting from the drone and traversing the obstacle.

on the goal location. Initially, we focus our analysis on a scenario involving two drones and a static obstacle, as illustrated in Fig. 4. It is evident from the saliency map that each drone perceives the obstacle from only one side, while mutual sensing occurs between the drones due to added points surrounding them. As expected, the points closer to the drones are more transparent as the first part of the trajectory is predefined by the continuity with the current motion. Compared to *ours w/o GNN*, the saliency map for our approach illustrates a balanced distribution of points between the two drones, resulting in trajectories crossing the environment uniformly. In contrast, when using *ours w/o GNN*, the black drone exhibits a more significant reliance on sensed points compared to the blue drone, leading to non-homogeneous trajectories. This discrepancy indicates potential conflicting behaviours between the drones due to differing perceptions of the environment. Additionally, saliency maps serve as valuable tools for analyzing failure cases. Fig. 5 showcases a collision scenario with *ours*. The trajectory intersects a pillar, with its points appearing transparent in the saliency map, suggesting that the network is “blind” to the obstacle, although perceived through the point cloud. Conversely, other obstacles are clearly visible and incorporated into the trajectory planning.

VI. CONCLUSION

This work presented a decentralized end-to-end trajectory planner that handles static obstacles, dynamic obstacles, and

other agents. By learning a collision constraint alongside the trajectory we can ensure collision-free and dynamic feasibility of the trajectory in a QP. We also introduce an algorithm to compute the saliency map of the point cloud over the neural network. We extensively validate our approach in simulations providing an ablation study and use the saliency map as an interpretation tool for understanding the failure and successful case. Future work includes adding a more general framework to train our model and improve the average flight time, as well as hardware experiments.

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