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1 **Probabilistic multi-objective optimization of wood torrefaction conditions**

2 **using a validated mechanistic model**

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13 **Abstract**

14 This paper uses a comprehensive computational model to propose optimal wood torrefaction conditions
15 by probabilistic optimization. Its main outcome is to propose tailor-made heat treatment conditions
16 (temperature levels-duration of mild pyrolysis at temperature levels ranging from 200 to 300 °C) to meet
17 users' expectations in terms of overall mass loss, duration and homogeneity of treatment. To this
18 purpose, beech wood boards were torrefied with a usual 3-steps treatment schedule (drying, heating and
19 cooling) under contrasting configurations in a well-instrumented device. The heterogeneity of the
20 treatment within the wood sample was assessed through X-ray attenuation profile and water vapour
21 sorption isotherm. These results allowed the model to be validated. In particular, it predicts the evolution
22 of the mass loss and internal temperatures with good accuracy, including the temperature overshoot. The
23 results highlight the need to adjust the heat treatment schedule to each input parameter such as the wood
24 piece dimensions and its initial moisture content or density, in order to limit the effect of exothermic
25 reactions. The torrefaction model was then embedded in a probabilistic optimization process. A case

26 study demonstrates the ability of the model to propose an alternative 3-steps treatment schedule able to
27 reach the target mass loss while controlling the temperature overshoot within the wood piece.

28 Keywords: Wood torrefaction, thermal modification, optimal conditions, treatment heterogeneity,
29 overheating, computational model.

30 **1. Introduction**

31 Torrefaction of wood is a mild pyrolysis treatment at temperature levels ranging from 200 to 300 °C in
32 the absence of oxygen. This induces the thermal alteration of the cell wall constituents of wood, namely
33 hemicelluloses, cellulose and lignin, via a series of thermally activated chemical reactions coupled with
34 heat and mass transfer phenomena. Chemical modification concerns mainly hemicelluloses degradation,
35 lignins reticulation and modification of the crystalline structure of the cellulose [1–7].

36 Over the last 50 years, torrefaction has been used to effectively improve various wood properties such
37 as durability and dimensional stability [8–10]. These studies were intended for solid wood as a material.
38 Later, torrefaction was promoted for other purposes. Current perspectives of this technology aim at
39 taking advantage of renewable resources, to valorize wood and biomass wastes, thus limiting the
40 exploitation of natural resources. For example, in an attempt to replace fossil fuels, a pre-treatment by
41 torrefaction of woody biomass is advised to obtain hydrophobic products with increased specific energy
42 contents and improved grindability [11–14]. Besides, it also leads to increased anti-shrinkage efficiency,
43 which reduces swelling during moisture recovery, which is an interesting feature for wood chips stored
44 in a silo. Furthermore, torrefaction can be advantageous in processing heterogeneous cellulosic
45 feedstock of different density, humidity content and size, such as those from forestry (logs, chips,
46 sawdust, bark, etc.) or agricultural crops [15,16]. These characteristics make torrefaction suitable for
47 integration into existing commercial regimes such as the white wood pellet value chain [15,17].
48 Moreover, end-of-life wooden furniture may be recycled and decontaminated by removing the urea-
49 formaldehyde and melamine-formaldehyde resins through a low temperature pyrolysis [18,19]. This
50 opens the possibility to use recycled wooden furniture materials for energy production. Nonetheless, the
51 introduction of the torrefaction technology in industrial manufacturing processes can pose serious safety
52 issues with regards to fire and injury risks. In this respect, various authors have reported that overheating

53 occurs within wood products induced by the exothermic reactions during torrefaction. Indeed, as wood
54 has a low thermal conductivity, the internal source of heat due to exothermic reactions gives rise to an
55 important temperature gradient needed to drive heat towards the exchange surfaces. The core
56 temperature therefore increases with, and in turn, activates even more, the exothermic reactions [20–
57 22]. A thermal runaway is then likely to occur at the scale of a boards stack or a packed bed of wood
58 chips where a dual-scale interaction occurs. The wood piece supplies the energy to the airflow due to
59 the exothermic reactions, the gas temperature increases along the stack or the packed bed which triggers
60 even more the exothermic reactions along the flow direction [23]. The risk of thermal runaway depends
61 on the size of the wood piece and process conditions (heating rate, airflow velocity, temperature, etc.).
62 In addition to safety issues, this produces also a heterogeneous treatment, both within and between the
63 wood pieces, hence undesirable consequences on the mass yield and product quality. Nowadays,
64 however, torrefaction programs are often empirical and customized according to the wood species
65 (softwood, hardwood, density, etc.), the characteristics of the products to be torrefied (e.g., dimensions,
66 geometry, initial moisture content, etc.) and the user expectations.

67 The motivation for this research arises from the difficulty of determining the optimal torrefaction
68 schedule that could limit the overheating within the wood piece and ensure that products meet quality
69 requirements, for example the hydrophobic character, energy content and grindability for energy
70 purposes, or the anti-shrinkage efficiency, mechanical performance and color for solid wood. Since most
71 of these properties are monotonic functions of the overall mass loss [11,24–28], the latter could therefore
72 be used as a target indicator to fine-tune the torrefaction parameters (duration–temperature levels) in
73 order to meet quality specifications.

74 In the present work, the research approach consists of two complementary parts. In the first, in a series
75 of experiments, beech (*Fagus sylvatica*) wood boards were torrefied using the usual 3-step program
76 (drying, heating at high temperature and cooling) under different conditions in terms of the sample
77 thickness and initial moisture content. The experimental data, including local values of internal sample
78 temperatures and mass loss progression, were then compared with simulations of a torrefaction model
79 [22,29–31]. The comparison between simulation and measurement in contrasting configurations

80 allowed the robustness of the model to be assessed. In the second part, this model was integrated into
81 an optimization algorithm with the purpose of proposing optimized heat treatment schedules
82 (temperature levels and durations), meeting the user expectations in terms of mass loss, duration and
83 homogeneity of treatment, while mitigating the undesirable overheating within the wood piece. A case
84 study was conducted to experimentally validate one of the treatment schedules proposed by the
85 optimization procedure.

86 **2. Measuring the torrefaction kinetics and treatment homogeneity under** 87 **contrasting conditions**

88 *2.1 Materials*

89 In order to focus on the effects of different factors such as the sample thickness and initial moisture
90 content on the homogeneity of the heat treatment, the sampling was designed to limit the effect of the
91 biological variability of wood (Fig. 1a). For that purpose, a green beech (*Fagus sylvatica*) log from the
92 Vosges region in France, with a diameter of about 60 cm, was selected and sawn. Then, two flatsawn
93 boards were selected at least 10 cm far from the bark to keep only the heartwood, and each board was
94 cut into specimens of final dimensions 20 mm (R) x 150 mm (T) x 300 mm (L) and 40 mm (R) x 150
95 mm (T) x 280 mm (L). Note that the large volume/surface ratio of the solid wood samples used here are
96 more demanding as they exacerbate the intra-particle temperature peak due to the importance of internal
97 transfers. Such sizes also ensure the reliability and accuracy of the experimental measurements (mass
98 evolution and internal temperature). Smaller volume/surface ratios encountered in energy applications
99 could be easily predicted by this mechanistic model as these situations limit the coupling due to internal
100 transfers. The boards were pre-conditioned at 12 % of moisture content on dry basis (MC) in a climatic
101 chamber at 40 °C and 75 % of relative humidity.

102 Subsequently, the specimens were instrumented with thermocouples of 1 mm diameter with a gas-tight
103 *Swagelok* connector to link the board to the probe. As illustrated in Figure 2, they were placed half-
104 length and mid-width of the boards, 75 mm deep from the lateral surface (RL plan). One was inserted
105 at the core (half thickness) and the second at about 2 mm from the surface (TL plan). Finally, the

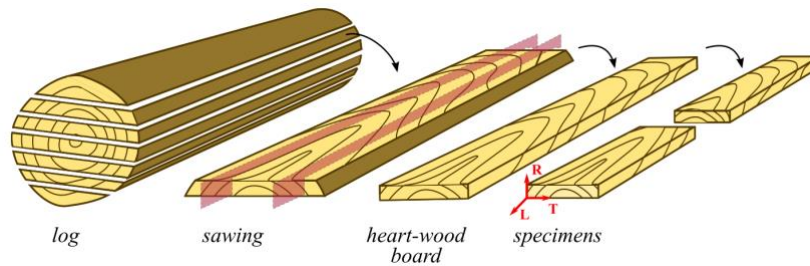
106 endpieces of the boards were coated with a silicone film maintained by two metallic parts strongly tied
107 (see Fig. 2), to prevent mass transfer in the longitudinal direction and avoid any gas leakage due to
108 overpressure during the treatment. This leads the boards to have a behavior similar to that of long boards
109 with transfers mainly in the radial and tangential directions.

110 2.2 *Methods*

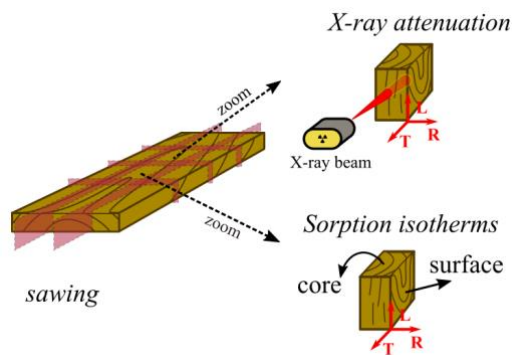
111 2.2.1 *Experimental setup*

112 The heat treatment experiments were carried out in an experimental reactor designed for this purpose
113 (Fig. 2), inspired by Colin's thesis work [32]. It consists of an oven Memmert UF110 plus equipped
114 with four polished stainless-steel heating walls (top, bottom, and sides) heated by electric resistances,
115 two temperature probes placed in the middle and top of the oven chamber, and a tangential fan on the
116 back wall. The maximum working temperature is 300 °C (setting accuracy of 0.5 °C) and the heating
117 rate can be precisely tuned in the range of 1 to 10 °C min⁻¹. The fan ensures the circulation of the gases,
118 and its velocity, adjustable in 10 % steps, was set at 40 % for all experiments. The complex air velocity
119 inside the chamber is not known, but, as explained below, the heat transfer coefficient, the pertinent
120 parameter, has been determined experimentally. Below the reactor, a digital balance is placed in a
121 hermetic chamber, which communicates with the reactor chamber through a glass tube (inner diameter
122 of 12 mm) embedded under the reactor bottom wall. Glass is chosen here because of its lower thermal
123 conductivity compared to metal. The wood specimen is attached to a sample holder, placed in the reactor
124 chamber, that stands directly on a tripod resting on the balance, both of which are clamped to the ends
125 of a glass rod (8 mm diameter) passing through the glass tube. The system is continuously swept by a
126 nitrogen flow (5 L min⁻¹) at room temperature and fed into the weighing chamber. To prevent cooling
127 of the reactor chamber by the flow of nitrogen, an aluminum plate (3 mm thick) was placed 3 cm above
128 the bottom wall of the oven, thus creating a preheating chamber that retains and heats the entering gas
129 before letting it flow through the main chamber. The volatile products are exhausted from the side of
130 the reactor. The oxygen level is continuously measured at the outlet flow by using an oxygen analyzer
131 with a zirconium oxide sensor (ZOA 100). The whole system was remotely controlled and monitored

132 by a home-made software developed on LabView. The oven temperature distribution was measured
 133 during torrefaction and only small differences of about 3 °C were recorded between the middle and top
 134 of the chamber. The middle temperature was lower than the set point by 2 °C.



a) *Sampling pre-treatment*



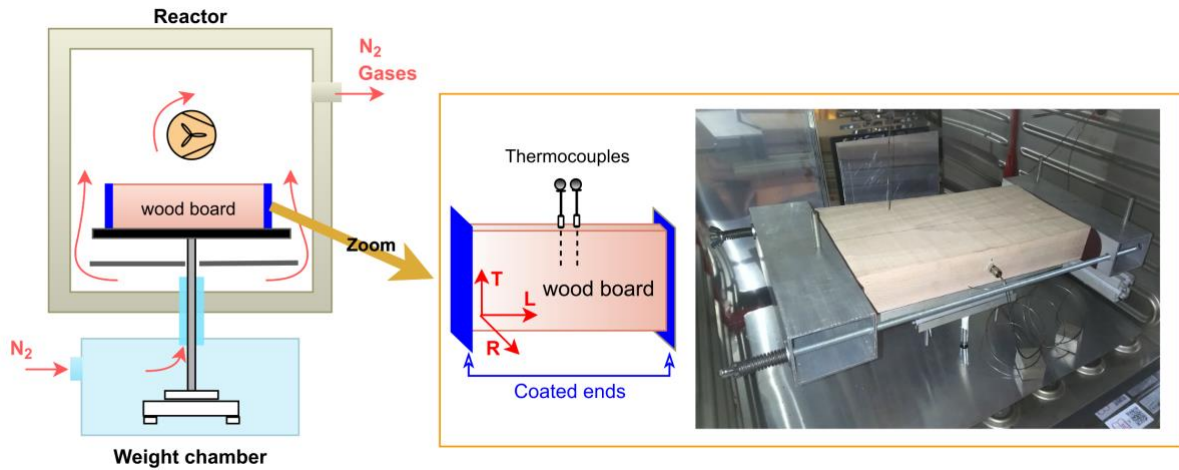
b) *Post-treatment of torrefied samples*

135 **Fig. 1.** Overview of the experimental study: (a) sampling pre-treatment of the wood boards and (b) post-
 136 treatment analysis of heat-treated boards.

137 The overall external heat transfer coefficient of the reactor was determined by considering the
 138 contribution of the convective and radiative transfers. On the one hand, the convective heat transfer
 139 coefficient was assessed experimentally by the sponge method [33] at a temperature of 50 °C, for which
 140 radiation is low, and under flow conditions similar to those used for the torrefaction experiments. A
 141 value of about 12 W m⁻² K⁻¹ was determined for this parameter. On the other hand, the contribution of
 142 the heat transfer by emitted radiation, from the oven surfaces to the boards, was estimated according to
 143 the Stefan–Boltzmann law. The radiative heat transfer at the torrefaction temperature (i.e., 230 °C) was

144 estimated about $13 \text{ W m}^{-2} \text{ K}^{-1}$. In this work, the overall external heat transfer coefficient of the
 145 torrefaction reactor was found to be of the order of $35 \text{ W m}^{-2} \text{ K}^{-1}$.

146



147

148 **Fig. 2.** Reactor device for wood torrefaction treatment and photo of one instrumented board.

149 **2.2.2 Torrefaction conditions**

150 The course of the torrefaction was monitored in real time through the following parameters:
 151 temperatures of the reactor chamber (middle and top) and board (core and subsurface), oxygen level at
 152 the outlet flow (e.g., less than 2 %) and mass loss. The experimental conditions of the heat treatment
 153 (HT) schedules performed on the four single board specimens are detailed in Table 1. The usual 3-phase
 154 schedule was applied on these boards: (1) a drying period at $110 \text{ }^\circ\text{C}$ for at least 1 hour; (2) heating at a
 155 rate of $7 \text{ }^\circ\text{C min}^{-1}$ until the treatment temperature of $230 \text{ }^\circ\text{C}$; then maintained at this level for 3 hours;
 156 (3) and finally cooled down at a rate of $2 \text{ }^\circ\text{C min}^{-1}$ until the temperature decreases to $150 \text{ }^\circ\text{C}$ in the reactor.
 157 Samples "d" were oven-dried at $110 \text{ }^\circ\text{C}$ during 24 to 48 hours just before the torrefaction test.

158 **Table 1.** Samples and conditions of the torrefaction experiments

Specimen name	Board thickness (mm)	Initial MC (%)	Heat treatment schedule
HT20d	20	Oven-dry (d)	usual
HT40d	40	Oven-dry (d)	usual

HT40m	40	12 % MC (m)	usual without drying
HT40d-opt	40	Oven-dry (d)	optimized

159

160 In total, four specimens were heat-treated. For the study of the effect of the thickness, two of the boards,
 161 namely HT20d and HT40d, were oven-dried at 103 °C to remove the residual water before torrefaction
 162 with the usual schedule. Then, the third sample, named HT40m and having an initial moisture content
 163 of 12 %, was directly heated at 230 °C by omitting the first drying step to study the effect of the residual
 164 water on the treatment. The fourth sample, denoted as HT40d-opt, was oven-dried at 103 °C and
 165 torrefied with an optimized treatment schedule proposed later in this work.

166 The overall mass loss (ML) due to thermal degradation should be determined as follows:

$$167 \quad ML = \left[\frac{M_o - M_t}{M_o} \right] 100\% \quad (1)$$

168 where M_o is the mass at the anhydrous state and M_t is the mass at a time t during thermal treatment.
 169 However, in this work, the experimental measurements of mass loss do not distinguish between moisture
 170 evaporation and wood degradation. Thus, this mass loss is named apparent mass loss (ML_{app}), which is
 171 defined by the following equation:

$$172 \quad ML_{app} = \left[\frac{M_{init} - M_t}{M_{init}} \right] 100\% \quad (2)$$

173 where M_{init} is the mass of the board in either the moist or dry state, according to the initial conditions at
 174 the beginning of the experiment.

175 2.2.3 Assessing the final density profile and hygroscopicity

176 The density profiles of the heat-treated boards were scanned by using X-ray attenuation with a Dax5000
 177 from Fagus-GreCon. Samples with dimensions of 50 mm x 50 mm were sawn from the geometric centre
 178 of the boards and subsequently dried at 103 °C until reaching constant mass before analysis (Fig. 1b).
 179 Besides, the differences in water adsorption capacity between the core and the surface of the torrefied
 180 boards (Fig. 1b) were assessed by dynamic vapour sorption (DVS), using a DVS intrinsic apparatus

181 from Surface Measurement Systems. Samples with 30 to 40 mg mass were subjected to an isothermal
182 cycle at 23 °C of humidification by increasing the relative humidity of the surrounding atmosphere from
183 0 % up to 90 %, in steps of 15 %. The change in sample mass was followed at regular time intervals
184 (1 point/min). Equilibrium moisture content (EMC %) was considered as established when the change
185 in the sample mass was less than 0.0005 %/min for a given relative humidity level, where this slope is
186 evaluated over a time window of 10 min.

187 **3. Optimization of torrefaction conditions**

188 In this work, a program has been developed to determine tailor-made wood torrefaction conditions to
189 meet the user expectations. The overall mass loss (ML) of the sample is a synthetic indicator of the
190 treatment intensity [24], and it can be used to determine some properties of the torrefied products such
191 as the hygroscopicity, anti-swelling efficiency (ASE), color, grindability and energy content. Just as the
192 final MC is the target of drying, the final ML can be defined as the target of wood torrefaction on the
193 basis of the end user applications. The methodology implemented for the development of the program
194 consists of three complementary parts:

- 195 • A torrefaction model computes the ML field over time and the temperature overshoot in the
196 board for a given treatment schedule,
- 197 • An objective function is defined to describe the output targets that meet the user expectations,
- 198 • A metamodel calls the torrefaction model, starts with a given schedule and modifies it to
199 minimize the objective function.

200 Each step is presented in detail in the following section.

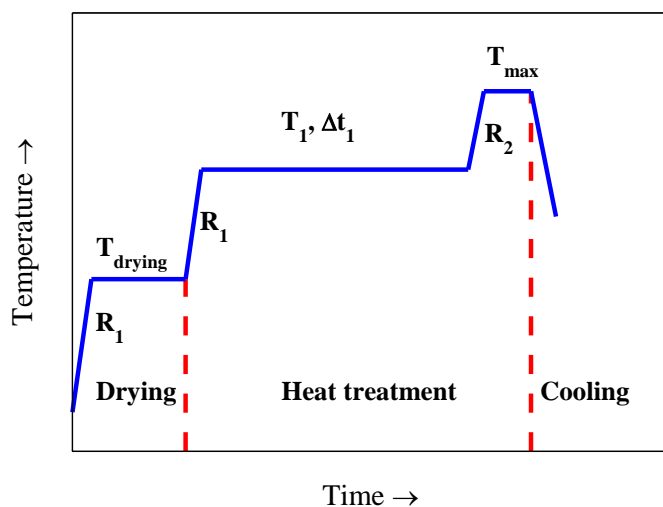
201 *3.1 Torrefaction model*

202 The 2-D version of the computational model *TransPore*, developed in previous works [22,29–31], was
203 used in this work. This computational model accounts for the thermal decomposition kinetics of the
204 main components of the cell wall (cellulose, hemicelluloses and lignin) via a series of parallel,
205 consecutive or competitive chemical reactions. Enthalpy values are associated with these reactions,

206 which allows a two-way spatio-temporal coupling between heat and mass transfer and kinetics to be
 207 considered: activation of chemical reactions by the local temperature value and evolution of the
 208 temperature fields by the cumulative effect of the local heat source due to reactions. In this respect, the
 209 temperature computed by *TransPore*, for each control volume of the wood piece, is used to estimate the
 210 rate of the chemical reactions and their related heat sources (or sinks) and the production of volatiles.
 211 For a better understanding of the intricate two-way coupling between the heat and mass transfer and
 212 chemical mechanisms, the formulation of the model at the board scale is summarized in Annex B, and
 213 it is presented in more details in the work of Rémond et al. (2010) and Turner et al. (2010) [22,30]. In
 214 this work, the initial MC, dimensions and wood density measured on the board samples from our
 215 experiments are the input data for the computational model. Additional model parameters come from
 216 the literature [22,30]. Finally, the board section is discretized by a set of 41×21 control volume, in the
 217 radial and tangential directions respectively.

218 3.2 Module for generating the torrefaction conditions to reach the target ML

219 A simple module written in Fortran has been developed to generate a wide variety of treatment
 220 schedules. This module is integrated in the *TransPore* model, in which the generated schedules are used
 221 as boundary conditions of the wood piece, which allows the ML to be computed versus time. In the
 222 following, the usual 3-step schedule is generated:



223

224 **Fig. 3.** Example of the torrefaction schedule that can be proposed by the module. This includes a first
225 drying step and two subsequent steps for wood torrefaction.

- 226 • Step 1 is a drying stage at a level ranging from 110 °C to 130 °C, maintained until the computed
227 average MC reaches 1%.
- 228 • Step 2 is the heat treatment stage itself with two temperature plateaus, the intermediate
229 temperature (T_I) and the maximum torrefaction temperature (T_{max}). The temperature change
230 between plateaus is defined by the heating rate (R_I) and the duration of the intermediate plateau
231 is Δt_I . Step 2 ends as soon as the target ML is reached.
- 232 • Step 3 is the cooling stage, which lasts until the reactor temperature drops to 80 °C.

233 By defining the heating rate (R_I), the parameters of the intermediate plateau (T_I , Δt_I) and the maximal
234 temperature (T_{max}) as variables of the module, it is already possible to generate a wide variety of
235 torrefaction schedules to reach the target ML (Fig. 3).

236 3.3 *Objective function and variables*

237 An objective function has been built up from three output targets defining the user expectations. The
238 first can be defined by the heterogeneity of the ML field within the wood sample at the end of the
239 treatment, since it is sought to perform a homogeneous treatment of the sample. The second concerns
240 the treatment duration, as good homogeneity should not be sought at the expense of longer durations.
241 The third and last output target intends to limit the exothermic peak which is at the origin of the thermal
242 runaway, hence heterogeneity, observed in industrial ovens. Accordingly, each of the objective variables
243 can be defined as follows:

244 Firstly, the standard deviation of the ML at the end of the treatment, which is given as a fraction of its
245 mean value \overline{ML} ,

$$246 Z_1 = \sigma / \overline{ML} \quad (3)$$

247 with σ defined as:

248
$$\sigma = \sqrt{\frac{1}{ncv} \sum_{j=1}^{ncv} (ML(j) - \overline{ML})^2}$$
 (4)

249 In the above expression, ncv is the total number of control volumes in the board section, and $ML(j)$ is
 250 the local ML at the control volume j .

251 Secondly, the rate of torrefaction progression establishes the relationship between the duration of the
 252 treatment t_{end} and the maximum duration t_{target} accepted by the user:

253
$$Z_2 = \max\left(0 ; \frac{t_{end} - t_{target}}{t_{target}}\right)$$
 (5)

254 Thirdly, the term considering the temperature overshoot, which can be considered as a safety factor to
 255 reduce the risk of the thermal runaway, is defined by:

256
$$Z_3 = \max\left(0 ; \frac{T_{in} - T_{sp}}{T_{sp}}\right)$$
 (6)

257 where $T_{in} = \max(T(j)_{j=1,ncv})$ during the treatment period, and T_{sp} is the gas temperature around the
 258 board surface.

259 The difficulty remains in finding the right compromise between a short treatment and a homogeneous
 260 treatment, while limiting the temperature overshoot. Finally, the global objective function is given as a
 261 weighting average of all sub-functions:

262
$$g = w_1 \cdot Z_1 + w_2 \cdot Z_2 + w_3 \cdot Z_3$$
 (7)

263 where w_i is the weighting factor, such as $w_1 + w_2 + w_3 = 1$, whose value is chosen by the decision
 264 maker according to his own constraints.

265 3.4 Minimization of the objective function

266 For given torrefaction conditions, the *TransPore* code predicts the values of the objective variables (Z_1 ,
 267 Z_2 , Z_3). A metamodel, developed here in the versatile language Python, calls *TransPore* code by using
 268 the F2PY package (*TransPore* being written in the very fast Fortran language) and estimates the value

269 of the objective function (Eq. 7) [34]. Simulated annealing (SA) has been adopted in the metamodel to
270 minimize this function. We used the dual annealing function included in the SciPy Python Package. A
271 compromise between the quality of the objective function minimum and the number of calls of such
272 function was looked for to limit the time and resource consumption of the SA (Annex A). The program
273 takes 5 minutes for the whole optimization procedure, with two Xenon W cores at 3.5 GHz. The
274 parameters of the SA function were set at the default values [35]: the initial artificial temperature value
275 was 5230, the value of the parameter for visiting distribution was 2.62, the value of the parameter for
276 acceptance distribution was -5, the value of the ratio triggering the restart of the process was $2 \cdot 10^{-5}$, and
277 the local search strategy was deactivated.

278 Finally, by fixing a target ML, the torrefaction conditions defined by R_I , T_1 , Δt_I , and T_{max} can be tuned
279 by the metamodel to find the best compromise between the three sub-criteria to minimize the objective
280 function.

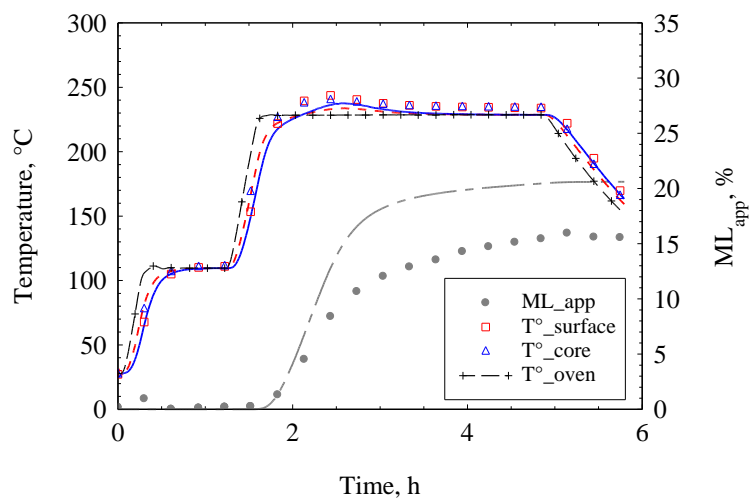
281 **4. Results and discussion**

282 *4.1 Experimental and simulated results*

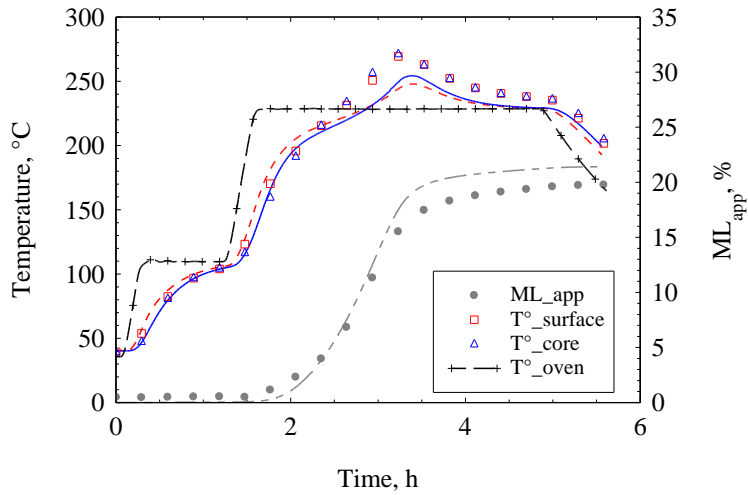
283 *4.2.1 Dynamics of torrefaction treatment*

284 Figures 4a and 4b present the experimental results for the temporal evolution of the core and subsurface
285 temperatures, as well as the ML_{app} for the HT20d and HT40d boards. Both cases were conducted with
286 the usual 3-step schedule (i.e., drying, heating at 230 °C and cooling). It can be observed that at the end
287 of the drying plateau, the core (blue triangle markers) and subsurface (red square markers) temperatures
288 of both boards reach the dry bulb temperature, and the moisture is almost completely removed, as
289 evidenced by the unchanging ML_{app} (grey circle markers). At this point, the remaining MC is almost
290 zero, as shown in Table 2. Subsequently, during heating to the treatment plateau at 230 °C, the
291 temperature in the core exceeds the one at the subsurface of the boards, and both exceed the reactor
292 temperature (black cross markers) until reaching a maximum peak. As is well known, this phenomenon
293 is attributed to the exothermicity of the chemical reactions activated by the rapid increase of the internal
294 temperature of the boards. On the other hand, when the board thickness is doubled, the onset of the

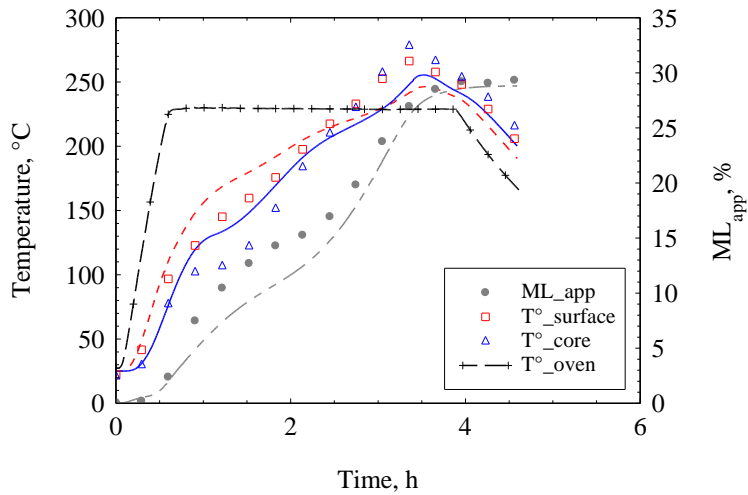
295 exothermic peak is delayed and its intensity is greater. This is due to a longer time for heat conduction
296 towards the core of the board, and then, when exothermic reactions are activated, the thermal insulation
297 ensured by the sample thickness limits the cooling of the product by the exchange surfaces. Nonetheless,
298 it was also observed that the differences between the core and subsurface temperatures were the same,
299 about 2 °C, for both specimens. This result is unexpected since a greater difference is likely to be
300 observed by doubling the board thickness. This may be attributed to the internal location of the
301 subsurface thermocouple, which was placed 6 mm under the surface of the thickest board, instead of 2
302 mm as for the thinnest one. Table 2 details the characteristics of the exothermic peaks in terms of the
303 onset time, maximum core and subsurface temperatures, as well as the final ML and ML_{app} of each
304 experiment.



a) 20 mm, dry, HT20d



b) 40 mm, dry, HT40d



c) 40 mm, moist, HT40m

305 **Fig. 4.** Temporal evolution of the ML_{app} (grey circles and dot/dashed curves), core (blue triangles and
 306 solid curves) and subsurface (red squares and dashed curves) board temperatures of the samples: (a)
 307 HT20d, (b) HT40d and (c) HT40m. Model predictions are represented by the curves and experimental
 308 data by the markers.

309 The subsequent comparison case, shown in Fig. 4c, concerns the evolution of the thermal treatment of
 310 the 40 mm thick board with an initial MC at 12 %, which was directly heated at 230 °C for 200 min
 311 (without previous drying). Due to the high initial MC, the internal temperature of the board is delayed
 312 from the oven temperature, as much of the energy of the system is used to supply the latent heat of

313 evaporation required to remove the moisture. Thus, because of the massive and sudden water
 314 evaporation, the profile of the core temperature exhibits a plateau at 100 °C followed by a sharp increase
 315 up to 280 °C after 200 min of heating. Regarding the ML_{app} , as expected, it is higher for the moist board
 316 (30 %), but with a true value of ML of the order of 18 %, which is comparable to the dry board (as
 317 shown in Table 2), regardless of the differences in the initial MC.

318 **Table 2.** Experimental characteristics of the exothermic peaks (onset time, core and subsurface
 319 temperatures, T°), and overall mass loss (ML_{app} and ML) of the heat-treated boards.

Specimen name	MC (after drying step) (%)	Maximum of the exothermic peak				
		Time (after drying step) (min)	Core_ T° (°C)	Subsurface_ T° (°C)	ML_{app} (%)	ML (%)
HT20d	0	75	239	237	-	16.6
HT40d	0.7	120	271	269	19.8	19.1
HT40m	12.1 ^a	215	280	266	30.0	17.8
HT40d-opt	1.5	245	238	238	13.3	11.8

320

321 In addition to the results from the three torrefaction experiments presented here, additional experiments
 322 (from reference [22] and several unpublished data) using different temperature-levels, duration and
 323 heating rates, were tested for model validation. The model predictions for each board are compared to
 324 the respective experimental data and plotted as solid lines in Fig. 4. In all the presented cases, the actual
 325 temperature in the reactor chamber is used as a boundary condition in the computational model
 326 *TransPore*. As can be seen, the model succeeds in predicting with good accuracy the internal board
 327 temperatures (core and subsurface) for the very contrasting experimental conditions of sample thickness
 328 and initial MC. Regarding the ML_{app} progression, the comparisons are correct for the thickest boards,
 329 but it is less good for the HT20d one, since the model seems to overestimate the ML_{app} with a more
 330 advanced degradation kinetics. For the three different experimental configurations, the occurrence of
 331 the exothermic peak is captured well by the model, but its intensity is under-estimated, notably for the

332 40 mm thick boards. In the case of the moist board (HT40m), the observed over-predictions on
333 temperature evolution may be related to the local pressure at the internal position of the probes, which
334 seems to be at atmospheric pressure with a plateau at 100°C despite the intense evaporation of the bound
335 water, while the model predicts a local overpressure of about 2.5 bar. A possible cause would be a
336 leakage around the tight connector that links the board to the probe.

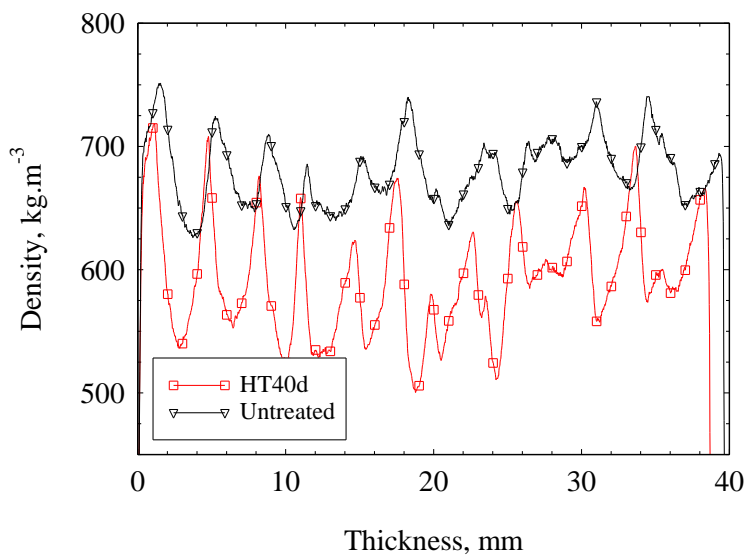
337 *4.2.2 Heterogeneity of treatment intensity across the sample thickness*

338 The intensity of the different heat treatments was then experimentally compared by measuring the
339 changes in the density profile and water sorption capacity of the beech boards before and after
340 torrefaction. The ability of the Grecon X-ray beam to detect density changes after heat treatment was
341 first verified using a series of homogeneously heat-treated thin beech specimens with different mass
342 losses. It was found that the Grecon analyzer is capable of accurately measuring small changes in mean
343 density, even as little as 10 kg/m³. Figure 5a compares the density profile of the HT40d specimen with
344 the untreated reference, both of which have the same pattern of annual growth rings. Since the X-ray
345 beam scans were performed in the radial direction, i.e., the X-ray passes through the sample in the
346 tangential direction, the growth rings were highlighted, and the alternation between earlywood (EW,
347 lower density) and latewood (LW, higher density) was distinguished by the lowest and the highest
348 density values of each peak, respectively.

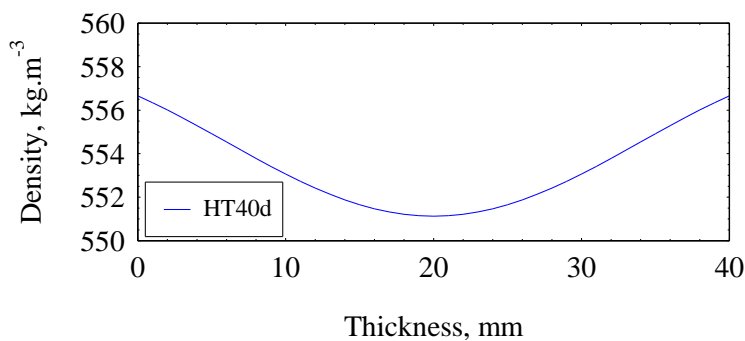
349 As can be seen, the case corresponding to the heat-treated specimen displays more pronounced and
350 narrower peaks that are positioned at lower density values than the untreated reference, due to the
351 degradation and shrinking of the cell wall during torrefaction. At the same time, the density reduction
352 seems to be greater in earlywood than in latewood, as evidenced by the decrease of the respective peaks,
353 notably those placed at the half-length of the board, where the highest temperature overshoot was
354 recorded. These results are consistent with studies performed on different wood species [36,37]. The
355 higher susceptibility of earlywood to thermal degradation can be attributed to a lower proportion of the
356 cellulose content, since its S2 layer is thinner, thus increasing the proportion of the more thermally
357 sensitive components, namely hemicelluloses and lignin, to heat degradation, while cellulose remains

358 stable at the recorded temperatures. In addition, greater shrinkage of LW compared to EW due to cell
359 wall component degradations could also explain this observation, since shrinkage increases density,
360 hence counterbalancing the mass loss per unit volume.

361 These trends obviously cannot be captured by the model, which considers a homogeneous density in the
362 board at the initial state (here 698 kg m^{-3} for the untreated 40 mm thick board). Fig. 5b shows that the
363 model simulates a parabolic density profile at the end of the treatment, with a slightly lower density at
364 the core than at the surface.



a) experiments



b) model

365 **Fig. 5.** Density profile across the thickness (radial direction on the RT plan) of the HT40d board (a)
366 measured before and after heat treatment and (b) predicted by the model after treatment.

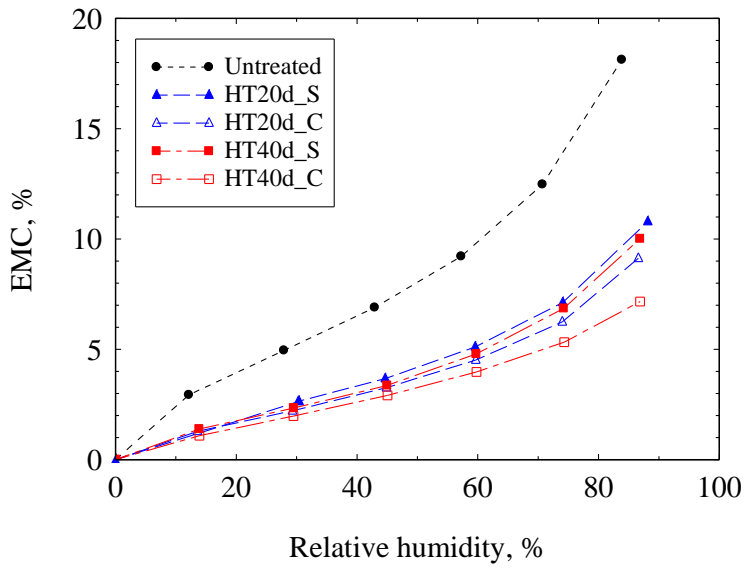
367 For all other specimens, the changes in their density profile are not presented here because the pattern
 368 of the annual rings was very different from the untreated reference, making it difficult to draw
 369 conclusions about the extent of the local degradation. The mean density of all heat-treated specimens is
 370 shown in Table 3.

371 **Table 3.** Mean density of heat treated and untreated beech wood measured by tomography. Two
 372 specimens were analysed at each time.

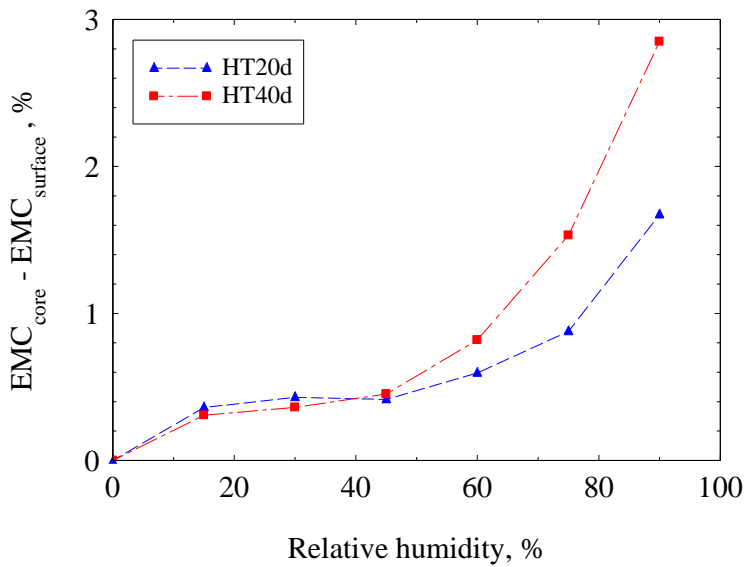
Specimen	Mean density (kg m ⁻³)	Standard deviation (kg m ⁻³)
Untreated, 20 mm	671.8	26.1
HT20d	558.6	54.1
Untreated, 40 mm	698.5	34.4
HT40d	580.2	8.7
HT40m	575.0	3.0
HT40d_opt	604.1	7.0

373

374 Fig. 6 shows the changes in hygroscopicity after the heat treatment, as well as the differences in the
 375 adsorption isotherms between the core (C, solid marks) and the outer surface layer (S, empty marks) of
 376 the dry boards, namely HT20d and HT40d. In both cases, the EMC of the untreated beech decreases
 377 over the analyzed range of relative humidity (i.e., 0 % to 90 %). It is well known that heat treatment
 378 reduces the sorption isotherms. The measurement presented here perfectly confirms this: first, a slight
 379 reduction at the surface, in agreement with the density and temperature evolution; second, a larger
 380 reduction at the core due to the overshoot in temperature, which triggers kinetics; third, an effect of the
 381 thickness, which exacerbates the overshoot due to a thicker insulation.



a) isotherms



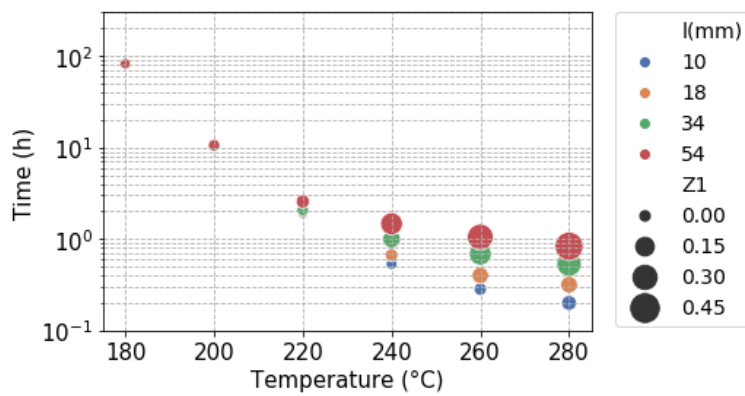
b) core-surface isotherms differences

382 **Fig. 6.** Effect of treatment on water adsorption capacity: untreated (black dots) and torrefied samples
 383 from core (C, solid dots) and outer surface layer (S, empty dots) of the boards of different thicknesses.
 384 a) Sorption isotherms and b) Isotherm differences between core and surface.

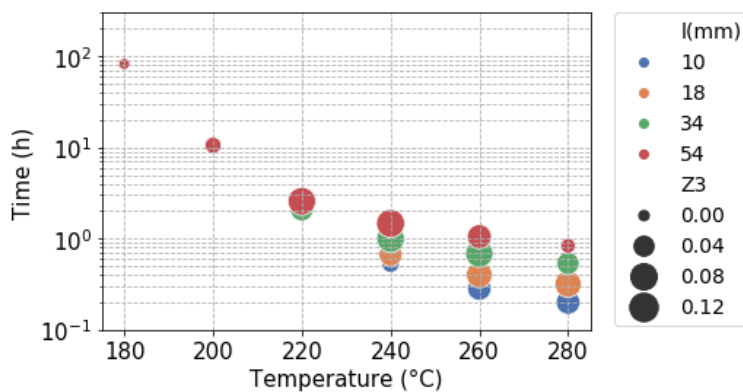
385

386 4.2 Numerical analysis of the time–temperature couples for a single step treatment

387 From the above, it becomes evident that the intensity of the heat treatment is very sensitive to the wood
 388 properties and initial conditioning, hence the need to adapt the treatment schedule to each particular
 389 case. To further investigate the effect of board thickness on the time–temperature couple, when a single
 390 temperature step treatment is applied, a series of simulations were carried out for varying the board
 391 thickness, namely 10 mm, 18 mm, 34 mm and 54 mm (in the radial (R) direction of the wood), for a
 392 150 mm wide board (in the tangential (T) direction) and for a target ML equal to 15 %. At the beginning
 393 of the treatment, the boards are assumed to be anhydrous and at a temperature of 100 °C. Subsequently,
 394 these are subjected to a single-step schedule at constant temperature, for an undefined period of time
 395 until the desired ML is reached.



a) Z1



b) Z3

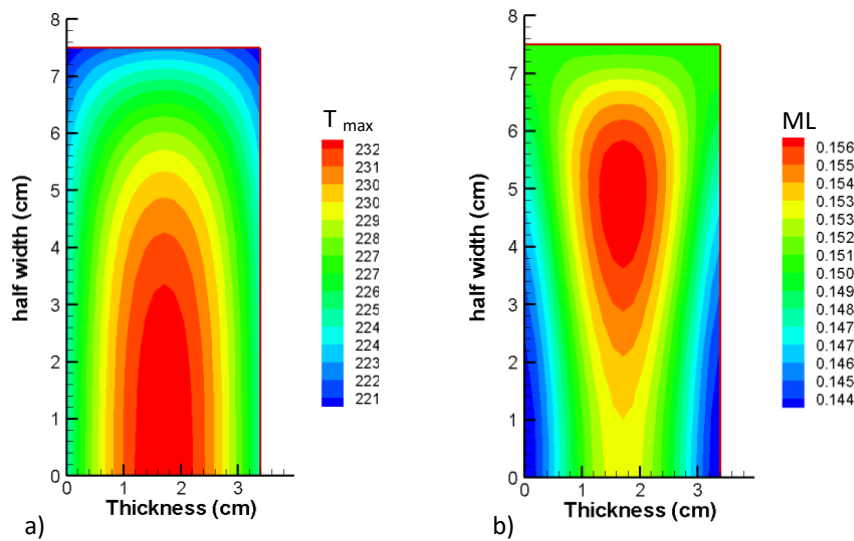
396 **Fig. 7.** Comparison of the time–temperature couples and their respective values of: (a) Z_1 and (b) Z_3 ,
397 for a single-step torrefaction program for boards of different thickness (l) with a target ML of 15 %. The
398 values of the objective variable are represented by the diameter of the circles.

399 Fig. 7 shows the time–temperature couples proposed to reach a target ML of 15 % for each thickness (l ,
400 color of the circles), as well as the values (diameter of the circles) of two objective variables, Z_1 (Fig.
401 7a) and Z_3 (Fig. 7b). Remember that Z_1 (Eq. 3) estimates the relative ML heterogeneity at the end of the
402 thermal treatment and Z_3 (Eq. 6) quantifies the temperature overshoot. These graphs highlight the effect
403 of thermal activation of the exothermic reactions: a clear time–temperature equivalence is revealed by
404 the time–temperature couples. For instance, for a 10 mm thick board, the treatment duration is 82 h at
405 180 °C compared to 0.2 h at 280 °C. In fact, at low temperature levels (e.g., below 200 °C), the duration
406 of the heat treatment is independent of the board thickness: the time required to reach a ML of 15 % is
407 much longer than the characteristic time of heat diffusion in the board thickness. Whatever the thickness,
408 the temperature remains quasi-uniform and the overshoot is low (see Fig. 7a). In contrast, as the
409 temperature rises above 220 °C, the residence time is of the same order of magnitude as the diffusion
410 time constant of the wood piece. Whether during heating or in the exothermic phase, step temperature
411 profiles are established during the process. Consequently, the treatment time and its heterogeneity
412 depend on the board thickness. This is confirmed by the relative heterogeneity at the end of torrefaction,
413 quantified by Z_1 (Fig. 7a).

414 This criterion increases with temperature and, in a more intensive manner, with the sample thickness.
415 Note that the area where the temperature is maximum does not correspond necessarily to greater
416 degradation rates since, as mentioned above, the degradation profile is a result of the history of the
417 temperature profile in time (Fig. 8).

418 Finally, Fig. 7b represents the evolution of the temperature overshoot or Z_3 as a function of temperature,
419 where an inflection point around 220 °C to 240 °C is revealed for the thickest samples. In fact, given
420 that the duration of the treatment is similar to or less than the diffusion constant time, the temperature
421 increase at the core of the board is not high enough to activate the exothermic reactions. In this case, the

422 temperature overshoot is attenuated and the treatment is larger at the surface than in the core of the
423 board.



424
425 **Fig. 8.** (a) Field of the maximum temperature T_{max} reached throughout the process for each location at
426 220 °C of a 35 mm thick board; (b) degradation field at the end of the treatment in the radial (x-axis) –
427 tangential (y-axis) plane. The y-axis represents the distance from the half-width of the board.

428 It is seen here that the impact of the torrefaction conditions on the objective variables is quite subtle.
429 The empirical approach to find the adapted sequence of the temperature levels–duration couples is a
430 very laborious task. Accordingly, the optimisation procedure proposed in this work makes sense to find
431 the most suitable torrefaction conditions to meet the user expectation.

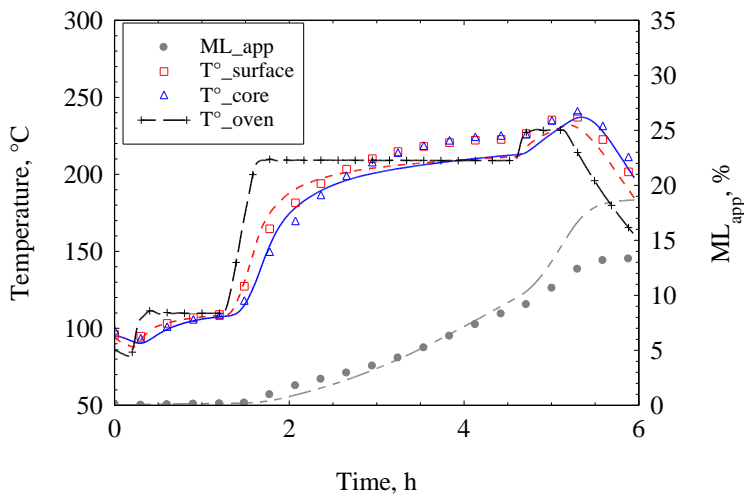
432 4.3 Case study: experimental validation of 4-step torrefaction program proposed by the model

433 In the torrefaction experiments presented above, it seems difficult to limit the magnitude of the
434 exothermic peak with the usual 3-step program. In fact, a gradual temperature increase or the addition
435 of an intermediate step in the treatment program causes the chemical reactions to proceed at a reasonable
436 rate while limiting the thermal runaway. In an attempt to reduce these undesirable effects, which is such
437 a difficult task, the optimization algorithm of the objective function was employed. More specifically,
438 in this case study, the process was optimized only in terms of the duration of the treatment (Z_2) and
439 reduction of the temperature overshoot (Z_3) by fixing, in Eq. (7), $w_1=0$, $w_2=0.3$ and $w_3=0.7$. This choice

440 was made because these two variables can be easily evaluated during the process. In this sense, the
 441 optimization variables considered according to the 4-step treatment schedule, illustrated in Fig. 3, were
 442 T_I and Δt_I , while the values of the other variables were fixed as: $T_{max}=230$ °C; $T_{drying}=110$ °C; $R_I= 5$ °C
 443 min^{-1} ; $t_{target}=5$ h (without the cooling step); for a target ML equal to 15 %. T_I can be tuned by the SA
 444 in the metamodel between 190 °C and 210 °C and Δt_I between 100 min and 240 min.

445 It is interesting to note that the optimal treatment schedule given by the SA method implemented in this
 446 work chooses the maximum temperature allowed for T1 to limit both the residence time at 230 °C and
 447 the duration of the treatment. Moreover, it uses the cooling phase to control the exothermic peak.

448



449

450 **Fig. 9.** Comparison between model predictions and experimental data of heat-treatment progression of
 451 a beech board (40 mm thick, anhydrous) torrefied with the 4-step schedule proposed by the model.
 452 Model predictions are represented by the curves and experimental data by the markers.

453 Subsequently, the proposed schedule was performed experimentally on a 40 mm thick dry board named
 454 as HT40d-opt. The comparison of the experimental course of the torrefaction with the predictions of the
 455 model is shown in Fig. 9. The experimental results in terms of the characteristics of the exothermic peak
 456 and the final ML_{app} , as well as the mean density measured by X-ray, are shown in Tables 2 and 3,
 457 respectively. The temperature overshoot at the core is now 8 °C on this optimized schedule, as against
 458 41 °C for the twin board on the first schedule (compare HT40d-opt vs. HT40d, Table 2) for an identical

459 treatment duration (4 h). The overall ML reached experimentally is 11.8 % (Table 3), which is lower
460 than the fixed target of 15 %.

461 From the above, the model proved its ability to propose optimized schedules able to fulfill the desired
462 criteria, but also to correctly predict the experimental behavior for this schedule with 2 treatment
463 plateaus, more demanding than the initial experiments.

464 **5. Conclusions**

465 An optimization program proposing tailor-made torrefaction schedules (temperature levels–duration)
466 has been derived to control the torrefaction process of wood. This opens up the possibility of controlling
467 the ultimate product qualities according to the user expectations. In this regard, the main outcomes of
468 this work can be summarised as follows:

- 469 • A torrefaction device was developed to thermally treat instrumented wood sample under
470 contrasting conditions,
- 471 • Parameters such as sample thickness and initial moisture content influence the temperature
472 overshoot and overall mass loss,
- 473 • The water sorption isotherms are accurate for evaluating the heterogeneity of this treatment,
- 474 • A mechanistic model was used to successfully simulate these experiments,
- 475 • The use of an optimization procedure allows the treatment schedule to be adapted while
476 mitigating the temperature overshoot,
- 477 • The predictive potential of the model has been experimentally validated with this optimized
478 schedule.

479 Discrepancies were evidenced in comparisons between measurements and simulations of the intensity
480 of the exothermic peak and the magnitude of the mass loss. An adjustment of some parameters of the
481 heat treatment model or the implementation of the new model proposed by [38] appears a promising
482 development of this work. Furthermore, this optimization approach, validated at the scale of one board,

483 could be developed in a double-scale modelling of a board stack [23] or a packed bed of chips to optimize
484 the schedules and avoid the thermal runaway in the industrial heat treatment process.

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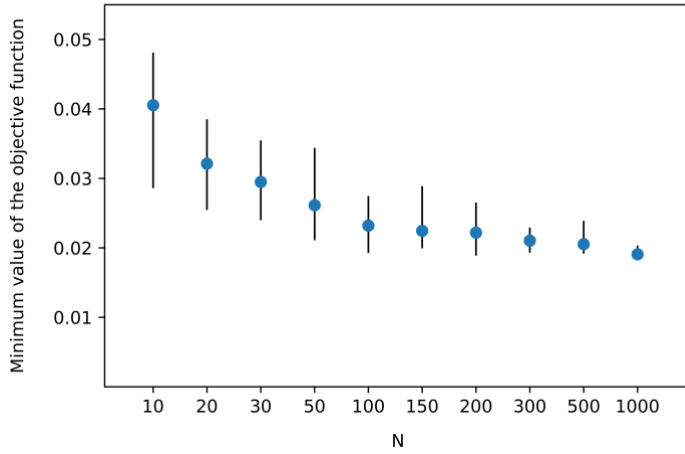
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603

604 **Annex A: SA results by the numbers of calls**

605 Figure A.1 shows the results of the SA with different numbers of calls of the objective function, which
606 is implemented in the code in the "maxfun" parameter. In this paper, this parameter was set to 100 for
607 the search for the optimised thermal treatment schedule.



608

609 **Fig. A.1.** Minimum value of the objective function called by the algorithm: N represents the number of
 610 calls of the objective function. The blue marker is the mean value of 10 numerical tests, and the error
 611 bars represent the difference between the minimum and maximum of the objective function.

612 **Annex B: Formulation of the torrefaction model. Summarized from [22]**

613 The total behaviour of wood is obtained from the evolution of its principal components:

614
$$\text{Wood} = \% \text{ cellulose} + \% \text{ lignin} + \% \text{ hemicellulose}$$

615 The following system of differential equations is used for the degradation of the wood components (the
 616 kinetics parameters are depicted in table A1).

617 - *Hemicellulose*

618
$$\begin{aligned} \frac{d\rho_H}{dt} &= -k_1 \cdot \rho_H, & \frac{d\rho_{G_1}}{dt} &= 0.43 \cdot k_1 \cdot \rho_H, \\ \frac{d\rho_{S_1}}{dt} &= -k_2 \cdot \rho_{S_1} + 0.57 \cdot k_1 \cdot \rho_H, & \frac{d\rho_{G_2}}{dt} &= 0.56 \cdot k_2 \cdot \rho_{S_1}, \\ \frac{d\rho_{S_2}}{dt} &= 0.44 \cdot k_2 \cdot \rho_{S_1}, \end{aligned} \quad (1)$$

619 where ρ_H represents the mass of hemicellulose; k_1 and k_2 the reaction rates and ρ_{S_i} , ρ_{G_i} the
 620 masses of the coal or tar and volatile matters produced during reaction $i = 1, 2$.

621 - *Cellulose*

622
$$\frac{d\rho_C}{dt} = -(k_3 + k_4) \rho_C, \quad \frac{d\rho_{G_4}}{dt} = k_4 \rho_C, \quad (2)$$

623 where ρ_C is the mass of cellulose and k_3 and k_4 are the reaction rates for cellulose.

624 - Lignin

$$625 \quad \frac{d\rho_L}{dt} = -k_5\rho_L, \quad \frac{d\rho_{G_5}}{dt} = k_5\rho_L, \quad (3)$$

626 where ρ_L is the mass of lignin and k_5 is the reaction rate for lignin. In the above equations we

627 model the reaction rates according to the Arrhenius Law $k_i = A_i \exp\left(\frac{-E_i}{RT}\right)$.

628 **Table A1.** Parameters used for the wood pyrolysis model. H, C, L designate respectively
 629 hemicellulose, cellulose, lignin; G_i and S_i designate the products from the reaction i respectively in the
 630 gaseous phase and in the solid phase.

631

632

Component	Models	Kinetics parameters
Hemicelluloses	H $\xrightarrow{1}$ $0,43 G_1 + 0,57 S_1$	$E_1 = 193 \text{ kJ/mol}$ $A_1 = 7,94 \cdot 10^{16} \text{ s}^{-1}$
	$\downarrow 2$ $0,56 G_2 + 0,44 S_2$	$E_2 = 95 \text{ kJ/mol}$ $A_2 = 5,01 \cdot 10^6 \text{ s}^{-1}$
Cellulose	C $\begin{cases} \xrightarrow{3} S_3 \\ \xrightarrow{4} G_4 \end{cases}$	$E_3 = 147 \text{ kJ/mol}$ $A_3 = 2,51 \cdot 10^9 \text{ s}^{-1}$
		$E_4 = 238 \text{ kJ/mol}$ $A_4 = 1,25 \cdot 10^{18} \text{ s}^{-1}$
Lignin	L $\xrightarrow{5}$ $S_5 + G_5$	$E_5 = 124,3 \text{ kJ/mol}$ $A_5 = 2,77 \cdot 10^7 \text{ s}^{-1}$

633

634 The macroscopic conservation equations governing heat and mass transfer phenomena in porous
 635 media during drying [29], [39] were extended in [22] to account for the effects of chemical reactions
 636 (component degradation, heat source, heat sink and volatiles production). The control volume (CV)
 637 method is implemented to discretize the conservation laws. Thereafter, an efficient inexact Newton
 638 method is used to solve the complicated nonlinear system that describes the drying and heat treatment
 639 processes.

640