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Quantifying Flare Combustion Efficiency using an Imaging Fourier Transform Spectrometer

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1 Abstract

2 Mid-wavelength infrared (MWIR) imaging Fourier transform spectrometers (IFTSs) are a 3 promising technology for measuring flare combustion efficiency (CE), defined as the fraction of 4 carbon supplied to the flare as fuel that is converted into carbon dioxide. These devices generate 5 spectrally-resolved intensity images of the flare plume, which may then be used to infer column 6 densities of relevant species along each pixel line-of-sight. In parallel, a 2D projected velocity field 7 may be inferred from the apparent motion of flow features between successive images. Finally, 8 the column densities and velocity field are combined to estimate the mass flow rates for the species 9 needed to calculate the CE. Since the MWIR IFTS can measure all carbon-containing species in 10 the flare plume, it is possible to measure CE without knowing the fuel flow rate, which is important 11 for fenceline measurements.

This work demonstrates this approach on a laboratory heated vent, and then deploys the technique on two working flares: a combustor burning natural gas at a known rate, and a steamassisted flare at a petrochemical refinery. Analysis of the IFTS data highlights the potential of this approach, but also areas for future development to transform this approach into a reliable technique for quantifying flare CE.

17 **1. Introduction**

18 The petrochemical industry uses flaring to transform high global warming potential (GWP) 19 hydrocarbons (HCs) into CO₂, principally to mitigate the impact of these emissions on climate 20 change. In the case of upstream oil and gas extraction, for example, simple flares are used to 21 dispose of natural gas as a by-product of oil extraction (so-called "associated gas"), while 22 downstream flaring often involves a wider range of hydrocarbon species and more costly and 23 sophisticated flare designs. Globally, 144 billion cubic meters of gas was flared in 2021 [1]. 24 Recovery and reuse processes exist (gas to power, gas to hydrogen, gas reinjection [2]), but their 25 feasibility is subject to favorable economic and technical conditions. Consequently, vast amounts 26 of HCs will continue to be flared for the foreseeable future.

27 The performance of a flaring process may be quantified by its combustion efficiency (CE), 28 defined as the ratio of the mass flow rate of carbon affixed to carbon dioxide leaving the flare 29 plume to the mass flow rate of carbon affixed to fuel entering the flare stack. While CE is usually 30 assumed to be close to 100% [3], external factors may reduce this number significantly. 31 Crosswinds, for example, can induce an aerodynamic fuel steeping mechanism [4] that removes 32 the fuel from the combustion zone; while steam-assisted and air-assisted flows, which are intended 33 to suppress soot formation, can also cause excess HC emissions [5, 6]. Given the large volumes of 34 HCs flared annually, the impact of flaring on climate change is very sensitive to seemingly small 35 variations on CE. For example, Plant et al. [7] recently determined an average CE for lit flares 36 from upstream processing in Bakken, Eagle Ford, and Permian basins of 95% based on airborne 37 measurements, as opposed to the nominal value of 98% [3]. When unlit flares are considered, the 38 average CE drops to 91%; this 7% difference corresponds to the annual CO₂ emissions of between

2.9-8 million cars [7], with the higher number corresponding to methane having a CO₂(e) of 86
over a 20-year span.

41 This result highlights the importance of quantifying flare combustion efficiency. In situ 42 approaches like extractive gas sampling are viable in laboratory measurements [6, 8] but mostly 43 infeasible on operating flares. A further challenge is that, particularly in the case of fenceline 44 measurements, the fuel flow rate entering the flare is often unknown. Several studies have relied 45 on aerial mass balance measurements by flying an aircraft equipped with gas-analyzers to measure 46 CH_4 and CO_2 concentrations along a helical trajectory surrounding the plume [7, 9, 10]. Species 47 mass fluxes may be obtained by combining concentration measurements with wind speeds, and 48 the fuel supply rate is inferred through a carbon mass balance. While this approach is appropriate 49 for developing an overall sense of flare emissions, e.g., to develop an emissions inventory over a 50 large area, it is not suitable for assessing the performance of individual flares under specific 51 operating conditions.

52 Accordingly, flare operators, regulators, and equipment manufacturers urgently need 53 diagnostics that can quantify flare CE rapidly through optical standoff measurements. Normal 54 quantitative optical gas imaging (QOGI) cameras are not up to this task, since they cannot 55 distinguish multiple carbon-containing species in the plume. One of the earliest standoff 56 approaches is passive Fourier transform infrared spectroscopy (PFTIR) [11], in which an FTIR is 57 used to measure the spectral intensity emitted by the hot combustion products along a single line-58 of-sight (LOS) through the plume. A spectroscopic model is then inverted to infer the species 59 concentrations, which are then related to a "local" combustion efficiency averaged along the LOS. 60 A major drawback of this approach is that assumes that the plume is homogeneous in composition,

61 which is often not the case, and the CE estimate may vary considerably based on the LOS. 62 Consequently, an optical technique that provides both spectral and spatial resolution is desirable. Zeng et al. [12], adapted a multispectral (MS) camera to visualize the radiant intensity emitted 63 64 by CO₂, CO, and unburned HCs in the flare plume; the spectral intensity measured by the camera 65 is then related to the relative concentrations of these species through a rudimentary spectroscopic 66 model, providing a local CE for each pixel. Finally, an overall CE for the flare is obtained by 67 averaging the CE for a subset of pixels outside of the combustion zone. While most MS cameras 68 generate images using filter wheels mounted external to the cold shield, these are generally 69 unsuitable for this application since the blackbody emission from the filters dominates the signal 70 component arising from thermal emission by the flare products. Instead, the specialized camera 71 used by Zeng et al. [12] features a microlens array that images the scene onto a number of 72 subdivided regions of the focal plane array (FPA), each of which is equipped with a distinct 73 broadband filter that is cooled along with the FPA. This amounts to a trade-off between spatial 74 and spectral resolution, and typically the number of spectral channels is 10 or smaller. 75 Unfortunately, since the detected spectral intensity is influenced both by species concentration and 76 temperature, it is necessary to measure both these quantities simultaneously, and the number of 77 channels in the MS camera may be inadequate to obtain robust estimates of all the parameters 78 needed to define the gas state within the flare plume.

Mid-wavelength infrared hyperspectral (MWIR-HS) imaging using imaging Fourier transform spectrometers (IFTSs) combine the spectral resolution of PFTIR with the spatial resolution of the MS camera to provide a detailed map of both temperature and species concentration within the flare plume [13]. IFTSs use interferometry to generate a data cube of thousands of nearsimultaneous images, leading to a spectral resolution that far exceeds what is possible using a MS camera without sacrificing spatial resolution, although at the expense of temporal resolution. The spectroscopic data may be inverted to solve for the temperature and species concentration fields simultaneously; these concentrations are then combined with a 2D map of intensity-weighted velocities inferred from a sequence of raw broadband images in the interferogram to produce mass flow rates.

89 This instrument has been used to measure gaseous emissions from a variety of industrial 90 combustion processes, including smoke stacks [14] and engine exhausts [15]. In the context of 91 emissions monitoring, key advantages of this approach include: (1) the spectral and spatial 92 resolution is generally sufficient to obtain the concentration and temperature gradients, which are 93 important in heterogenous plumes; (2) the spectral resolution may be further used to fingerprint 94 species when the plume has an uncertain chemical composition; and, in the case of emission 95 spectroscopy, (3) measurements may be carried out in day or night, and are not as sensitive to 96 nonuniform background illumination as are techniques based on absorption spectroscopy, e.g., 97 using the sun or a cloud layer.

Savary et al. [16] were the first to use IFTSs to infer flare CE. In their work, the plume temperature and species concentrations are assumed to be homogeneous along each LOS in order to simplify the spectroscopic model. However, Grauer et al. [17] and Miguel et al. [18] used CFD simulations to demonstrate that Gaussian distributions are more appropriate in the case of flare plumes. Miguel et al. [18] also conducted several proof-of-concept measurements on lab scale heated vents and a lab-scale steam and air-assist flare.

This work applies the technique developed by Grauer et al. [17] and Miguel et al. [18] to conduct benchmarking experiments on a heated vent under conditions representative of a flare plume, and then measure the combustion efficiency of a portable combustor (enclosed flare)

107 operating at as known firing rate and a steam-assisted flare at an oil refinery burning an unspecified 108 fuel at an unknown rate. In the case of the combustor, the carbon mass flow rate in the plume is consistent with the estimated fuel supply rate, and the overall combustion efficiency is nearly 109 110 100%. The refinery flare, in contrast, is over-assisted and a significant quantity of unburned 111 hydrocarbons are visible in the plume. The paper concludes with an assessment of the strengths 112 and weaknesses of this approach, and areas for improvement. In particular, while the IFTS 113 provides rich spectral data, a major challenge concerns the inference procedure and the model 114 errors that are made to reduce the ill-posed problem. Overall, however, these results highlight the 115 promise of this technique, and its potential to reduce greenhouse gas emissions from flaring.

116

117 **2. Flare combustion efficiency**

Flare combustion efficiency is defined as the mass flow rate of the carbon affixed to CO_2 leaving the flare plume divided by the mass flow rate of carbon entering the flare stack. Since the latter quantity may not be readily available, particularly for fenceline monitoring, it may instead be inferred from a mass balance of all carbon-containing species in the flare plume

122
$$CE = \frac{\dot{m}_{C,CO_2}}{\dot{m}_{C,fuel}} \approx \frac{\dot{m}_{C,CO_2}}{\sum \dot{m}_{C,plume}}$$
(1)

As shown in Figure 1, the mass flow rate of the *k*th species in the plume is found by integrating the product of the corresponding species column density (kg/m^2) with the normal component of the 2D projected velocity along a control line that transects the plume in the image plane

126
$$\dot{m}_{\mathrm{C},k} = \frac{M_{\mathrm{C}}}{M_{k}} \dot{m}_{k} = \frac{M_{\mathrm{C}}}{M_{k}} \int_{\Theta} \rho_{k} \left(\theta\right) \mathbf{u} \left(\theta\right) \cdot \hat{\mathbf{n}} \, d \, \theta \tag{2}$$

where the mass flow rate is adjusted by the ratio of the carbon molar mass, $M_C = 12$ atomic mass units (amu), and the *k*th species molecular molar mass, M_k , to obtain the mass flow rates of carbon. The pixel column density of the *k*th species for the LOS at a location θ along the control line is

130
$$\rho_{k}\left(\theta\right) = \frac{M_{k}p}{k_{B}N_{A}} \int_{\text{LOS}(\theta)} \frac{\chi_{k}\left(s,\theta\right)}{T\left(s,\theta\right)} ds$$
(3)

where *p* is the atmospheric pressure, k_B is Boltzmann's constant, N_A is Avogadro's number, and $T(s,\theta)$ and $\chi_k(s,\theta)$ are the temperature and mole fraction of the *k*th species evaluated at a location *s* along an LOS for a pixel located at θ on the control line. The procedures for calculating the species concentration, the plume temperature and the projected velocity field are described in the Sec. 4. In principle the denominator of Eq. (1) could include soot, although the contribution of soot to the overall carbon balance is usually negligible [19].



Figure 1: Schematic of a flare combustion efficiency measurement using an IFTS: (a) temperature and species concentration distributions are inferred from a spectroscopic model, Eq. (4); (b) these distributions are then used to derive column densities along a control line through Eq. (3), which is combined with a 2D intensity-weighted velocity map to obtain mass flow rates via Eq. (2).

137 **3. Measurement model**

The measurement model connects the quantities-of-interest, in this case the temperature and concentration distribution along each line of sight within the plume, to the spectral intensity measured by the IFTS. It is composed of a spectroscopic model, describing the intensity emitted by the scene that is incoming to the camera aperture, and a camera response model, describing the effect of the instrument on the incident scene intensity.

143

144 3.1. Spectroscopic model

145 The spectral intensity at wavenumber η entering the camera aperture, $I_{\eta,L}$, is defined by the 146 radiative transfer equation (RTE) along each pixel line-of-sight

147
$$I_{\eta,L} = I_{\eta,bg} \exp\left(-\int_{0}^{L} \kappa_{\eta}(s) ds\right) + \int_{0}^{L} \kappa_{\eta}(s) I_{\eta,b} \left[T(s)\right] \exp\left(-\int_{s}^{L} \kappa_{\eta}(s') ds'\right) ds$$
(4)

148 where *L* is the length of line-of-sight from behind the plume to the camera aperture, $I_{\eta,bg}$ is the 149 background intensity, $I_{\eta,b}$ is the blackbody intensity, and κ_{η} is the spectral absorption coefficient. 150 The background intensity may be determined from a pixel outside of the flare plume, although 151 its contribution to $I_{\eta,L}$ is usually small compared to the emission term over the vibrational-152 rotational (V-R) bands of the species in the plume. For N_s participating species (e.g., CO₂, CO, 153 H₂O, and various HCs) the spectral absorption coefficient is given by

154
$$\kappa_{\eta}(s) = \sum_{k=1}^{N_s} \kappa_{\eta,k} \left[\chi_k(s), T(s) \right]$$
(5)

155 The spectral absorption cross-sections of individual species may be found using a spectral line 156 database (e.g. HITRAN [20]) or from empirical spectra. In the case of HITRAN-derived spectra, the absorption coefficients of common species are precomputed for given concentrations andtemperatures, assuming air broadening:

159
$$\kappa_{\eta,k} \left[\chi_k(s), T(s) \right] = \sum_{ij} S_{k,ij} \left[T(s) \right] f \left[\eta, \eta_{ij}, T(s), p \right] \frac{\chi_k(s)p}{k_{\rm B}T(s)}$$
(6)

where $S_{k,ij}$ is the species spectral line intensity for the transition between the *i*th and *j*th energy states, and *f* is the Lorentz line shape function. (Doppler broadening is negligible at the temperatures and pressures relevant to flare plumes.)

163

164 *3.2.Camera response model*

165 Hyperspectral imaging is done using a Telops MW HyperCam IFTS with a detection spectrum of 1900-3400 cm⁻¹, which includes V-R bands of CO₂, H₂O, CO, and most HCs, and a maximum 166 167 spectral resolution of 0.25 cm⁻¹. The focal plane array (FPA) is composed of 320×256 pixels with 168 an instantaneous field-of-view (IFOV) of 0.35 mrad per pixel. The FPA is made of InSb sensors, 169 which records the interferogram image generated by a Michelson interferometer as shown in Figure 170 2 (a). As the moving mirror move across its range, an interferogram Y_{cam} is formed, as shown in 171 Figure 2 (b). The mirror position defines the optical path difference (OPD), which characterizes the 172 difference in pathlengths travelled by the two light beams generated by the beam-splitter. The beams 173 are then recombined, generating interferences that are measured by the FPA to form an interferogram. 174 A Fourier transform is performed on the interferogram in counts to obtain an intensity spectrum with 175 arbitrary units. Finally, an absolute intensity spectrum is obtained by calibrating using a two-point 176 calibration method [21] using two built-in blackbodies maintained at different temperatures.

177 The IFTS camera response model, referred to as the instrument line shape (ILS) function, 178 relates the scene intensity entering the camera aperture $I_{\eta,L}$ to the measured intensity, and describes



Figure 2: IFTS measurement process. (*a*) The scene radiation $I_{\eta,L}$ enters the camera aperture and traverses the Michelson interferometer, generating interferences measured by the FPA InSb sensors for successive mirror position. (*b*) The measured raw signal is the interferogram Y_{cam} . Finally, (*c*) the interferogram is Fourier transformed and calibrated by a two-point calibration method to produce the absolute intensity spectra $I_{\eta,\text{cam}}$.

how the IFTS mirror position limited range affects the measurement. In theory, the interferogram $Y_m(x)$ is defined for $x \in \mathbb{R}$. However, the range of the moving mirror in the camera is limited to a maximum OPD, x_{MOPD} , which is related to the spectral resolution by $\delta\eta_{res}=1.20671/2x_{MOPD}$. The measurement model accounts for the finite range of the mirror and relates the intensity $I_{\eta,L}$ to the modelled measurement, $I_{\eta,m}$, by the convolution product:

184
$$I_{\eta,m} = \mathcal{F}\left[Y_{m}\left(x\right)B\left(x,x_{\text{MOPD}}\right)\right] = \mathcal{F}\left[Y_{m}\left(x\right)\right] * \mathcal{F}\left[B\left(x,x_{\text{MOPD}}\right)\right] = I_{\eta,L} * ILS\left(\eta,x_{\text{MOPD}}\right)$$
(7)

where *B* is the boxcar function that characterized the finite OPD and becomes the ILS when the Fourier transformation is applied. Modelling the measured intensity then comes down to a convolution product between the intensity spectra, given by Eq. (4), and the ILS, which is ILS(η , *x*_{MOPD}) = 2*x*_{max}sinc(2 πx _{MOPD}· η). One of the challenges inherent to hyperspectral measurements of turbulent flows are rapid variations in intensity caused by fluctuations in the species concentration and temperature, which occur over a much shorter time scale than the time needed for the mirror to traverse its entire OPD range. These intensity fluctuations manifest as "scene change artifacts" (SCAs) in the transformed intensity spectrum [15]. Indeed, the interferogram model assumes that the intensity field remains constant as the interferogram is assembled:

195
$$Y_{\rm cam}(x) = \int_{-\infty}^{+\infty} \frac{1}{2} S_{\eta} \left[1 + \cos\left(2\pi\eta x\right) \right] d\eta$$
(8)

where S_{η} is the intensity entering the interferometer, representing the scene intensity $I_{\eta,L}$ and the camera self emission. The turbulent fluctuations of the flare plumes are expressed in Eq. (8) through the time dependence of the intensity field $S_{\eta} \equiv S_{\eta}(t)$. Following the hypothesis that the true intensity field is stationary but fluctuating, SCAs may be suppressed by using a high band pass filter to isolate the low frequency intensity variations, Fig. 3 (*a*), and then removing them from the



Figure 3: The raw interferograms $Y_{cam}(x)$ (a) are contaminated by scene change artifacts caused by turbulent fluctuations in the flow field as the mirror traverses through its OPD. These can be removed through a filtering procedure (b).

201 measured interferogram to obtain a new filtered interferogram, Fig. 3 (*b*). The filtered raw 202 spectrum *Y*, cleared from the intensity fluctuations, is then transformed to obtain a raw intensity 203 spectrum, S_{η} . An alternative approach, used in this work, consists of estimating a median 204 interferogram from a large set of raw datacubes.

205

206 **4. Inferring the mass flow rates**

Calculating the species mass flow rates from Eq. (2) relies on solving the column densities and the projected velocity profile along the control line. The column densities are obtained from the species mole fractions and plume temperature distributions along the LOS of each pixel on the control line; these quantities, in turn, are found by inverting the spectroscopic measurement model. The image projected velocity field is found from the apparent motion of pixels between sequential broadband images.

213

214 *4.1.Inferring the mole fractions and plume temperature*

215 Inferring the species mole fractions and the temperature profiles along a pixel LOS amounts to 216 minimizing the residual between the measured and modeled spectral intensities for each LOS. This 217 inversion problem is mathematically ill-posed since an infinite combination of $\chi_k(s)$ and T(s) could 218 be substituted into Eq. (4) to generate a given spectral intensity. Accordingly, it is necessary to 219 parameterize the distributions along the pixel LOS to reduce the ill-posedness of the problem. 220 Following the work of Miguel et al. [18], and Grauer et al. [17], we assume Gaussian profiles inside 221 the plume along the LOS, which are appropriate for free turbulent plumes, and constant values for 222 the atmospheric layer between the plume and the camera aperture:

223
$$\phi(s) = \phi_{amb} + (\phi_{max} - \phi_{amb}) \exp\left[-\frac{(s - s_{pc})^2}{2\sigma_p^2}\right]$$
(9)

224 where $\phi = \chi_k$ or T, σ_p is the characteristic plume thickness, and s_{pc} is the location of the plume 225 center. The ambient concentrations and temperature may be derived from meteorological data, or 226 determined by examining the spectra from a pixel outside of the flare plume, e.g., the flare stack. 227 The plume thickness is assumed to be the same for all parameters and is estimated from the plume 228 image, assuming that the plume is axisymmetric. The plume center is determined by the measured 229 distance between the camera and the flare stack. Therefore, the number of unknown parameters to 230 be solved for is N_s+1 , corresponding of the peak concentration of each species and the peak 231 temperature; these are stored in the vector \mathbf{x} . The maximum likelihood estimate is then found for 232 each pixel/LOS by

233
$$\mathbf{x}_{\text{MLE}} = \arg\min_{\mathbf{x}} \left\{ \left[\mathbf{m}(\mathbf{x}) - \mathbf{b} \right]^{\mathrm{T}} \mathbf{\Gamma}_{\mathrm{b}}^{-1} \left[\mathbf{m}(\mathbf{x}) - \mathbf{b} \right] \right\}$$
(10)

where **m** is the measurement model, defined in Sec. 2, **b** contains the set of spectral intensities at each wavelength { $I_{\eta,cam}$ }, and Γ_b is the measurement error covariance matrix, which is assumed to be diagonal and is computed from the measurement variance for each IFTS spectral bin. Minimization is carried out using the nonlinear least-squares solver in MATLAB[®] with a function tolerance of 10^{-9} and a step tolerance of 10^{-9} [22]. In some cases, the spectral range of the data is restricted to a subset of the detection spectrum that contains species-of-interest, in order to reduce computational time and exclude features that are not included in the model, such as background intensity from the atmosphere.

243 *4.2.Inferring the velocity field*

The time-resolved 2D velocity field, $\mathbf{u} = [u, v]^{T}$, is derived from a set of successive raw interferometer images via either the Horn-Schunk [23] or Lucas-Kanade optical flow algorithms [24]. The intensity of each image is first normalized and the mean pixel intensity field is subtracted to remove the stationary features. Optical flow is based on the hypothesis that any change in pixel brightness between successive images is due entirely to advection. Accordingly, pixel intensity becomes a conserved quantity and the velocity field is obtained by solving

250
$$\frac{DE}{DT} = \frac{\partial E}{\partial x}u + \frac{\partial E}{\partial y}v + \frac{\partial E}{\partial t} = 0$$
(11)

where *E* is the modified broadband pixel intensity and the derivatives are found from finite difference approximations. Solving for the 2D velocity field requires additional information to close the problem. In the Horn-Schunk algorithm, this is done by assuming that the velocity components vary smoothly in space, which correspond to Tikhonov first-order regulation:

255
$$\begin{cases}
\nabla^2 u = \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \\
\nabla^2 v = \frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2}
\end{cases}$$
(12)

The Lucas-Kanade algorithm adopts a weighted window scheme to filter the velocity field calculation, thereby suppressing noise amplification by the numerical derivative. In that case, the weighting term is the equivalent to first-order Tikhonov regularization. The regularization parameters are usually chosen heuristically, as is done here.

260

262 **5. Experimental analysis**

263 The technique is demonstrated by conducting measurements on a laboratory-scale heated vent,264 combustor, and a steam-assisted petrochemical flare.

265 5.1.Laboratory-scale heated vent

The performance of this technique is first benchmarked using the heated vent apparatus shown in Figure 4 (*a*), consisting of a 1.9 cm diameter nozzle positioned in front of four aluminum plates (30 cm \times 30 cm each), coated with matte black paint (Krylon k01602 Ultra-flat black) and maintained at a set-point temperature of 281 K by a water/ethylene glycol mixture. A specified 47:53 vol. mixture of CH₄ (53%) and CO₂ (47%) is generated using mass flow controllers (Brooks SLA5850 for CO₂ and Brooks GF40 for CH₄) at a total flow rate of 25.5 standard litres per minute



Figure 4: (*a*) laboratory scale apparatus, the hyperspectral camera is aiming at the gas plume. (*b*) The camera generates infrared images of the emitted radiation from the plume. The analysis is conducted over two control lines, Cl-1 near the stack exit and Cl-2 located 6.6 cm above the stack exit.

272 (SLPM). The gas mixture then flows through a heated hose before it is discharged from the nozzle. 273 The gas temperature is maintained at 350 K via a K-type thermocouple located at the nozzle exit. 274 Hyperspectral measurements were conducted with the camera aperture located 420 cm away 275 from the plume, using a 128 px ×128 px subdomain of the FPA. The detection spectrum was set between 1,900 cm⁻¹ and 3,400⁻¹ with a spectral resolution of 4 cm⁻¹ and a fixed integration time of 276 277 100 μ s. However, during the inference, only a subset of the spectrum was used, containing the 278 species-of-interests absorption spectral ranges, from 2200 to 2470 cm⁻¹ for CO₂ and from 2800 to 3300 cm⁻¹ for CH₄. The ambient CO₂ concentration was assumed to be 420 ppm and the 279 280 temperature of the atmospheric layer between the plume and the camera was measured at 295 K. Inferring the ambient temperature from background pixels led to $T_{amb} = 297$ K, which is in good 281 282 agreement with the measurement.

283 The control line Cl-1was positioned near the stack exit, as shown in Figure 4 (b), so the gas 284 velocities could be estimated from the known mass flow rates and nozzle dimensions. Because the 285 control line is located above the stack exit, the velocity and concentration profiles are assumed to 286 be uniform along the control line region covering the stack nozzle. The absence of turbulent flow 287 features at the nozzle exit precludes calculating the gas velocity from optical flow, so the gas exit 288 velocity is estimated to be 1.5 m/s from the known mass flow rate and the nozzle diameter. 289 Therefore, calculating the mass flow rate at this position provides a means to isolate how 290 uncertainty in the spectroscopic model impacts the mass flow rate.

Figure 5 (*a*) shows the column density profiles for CO₂ and CH₄, as well as the inferred plume temperature for the control line "CL-1" in Fig. 4 (*b*). The inferred ambient temperature (297 K) was used for this calculation. The plume temperature inferred from the IFTS data is around 400 K instead of the measured 350 K at the stack exit. The column density profiles of CO₂ and CH₄ show



Figure 5: (a) Column densities and temperatures inferred from the IFTS camera data for the integration line Cl-1 shown in Fig. 4 (b). (b) Comparison of modeled and measured spectra at the pixel location shown in Fig. 4 (b).

295 spikes at the extremities of the control line, which is due to the fact that the contribution of thermal 296 emission from the gases to the detected intensities is small at this location, and the inference 297 becomes dominated by measurement noise and model error. Since the values do not cover the 298 plume, they are excluded from the mass flow rate estimations, which is conducted from $\theta = 0.7$ 299 cm to $\theta = 2.9$ cm. Figure 5 (b) shows that the modeled spectrum at the sample point indicated in 300 Fig. 4 (b) closely matches the measured intensity. Features for both CO_2 and CH_4 are visible at 2,200-2,400 cm⁻¹ and 2,800-3,200 cm⁻¹, respectively. The measured emission spectra from the 301 plume reveals two CO₂ emission "spikes" at 2,250 ("red spike") and 2,400 cm⁻¹ ("blue spike"). 302 303 This feature arises from the fact that a portion of emission from 001 fundamental CO₂ band in the 304 plume is absorbed by the ambient CO_2 between the plume and the camera, only leaving the hot 305 lines at the wings of the band.

306	The control line Cl-2 was positioned 6.6 cm above the stack exit, as shown in Figure 4 (<i>b</i>), so
307	the gas velocities are inferred from the Horn-Schunk optical flow algorithm. Gaussian profiles for
308	the plume concentrations and temperature are assumed due to the turbulent nature of the plume at
309	that location (see Eq. (9)). The inferred column density profile for CO_2 and CH_4 are shown in
310	Figure 6 (a), as well as the maximum temperature distribution along Cl-2. Figure 6 (b) shows the
311	corresponding velocity profile used to estimate CO ₂ and CH ₄ mass flow rates. The mass flow rates
312	are computed from $\theta = 0.6$ cm to $\theta = 5$ cm to exclude the background pixels from the mass flow
313	rate calculation.
314	Table 1 shows that the inferred mass flow rate for CO ₂ and CH ₄ , along Cl-1 and Cl-2, are in
315	good agreement with the mass flow controller settings.

Table 1: CO₂ and CH₄ carbon mass flow rates inferred from the heated vent.

	IFTS (Cl-1)	IFTS (Cl-2)	MFC	% diff. (Cl-1)	% diff. (Cl-2)
$\dot{m}_{c,co2}$ (×10 ² g/s)	8.9	8.4	8.37	5.9	0.3
$\dot{m}_{\rm C,CH4}~(\times 10^2~{\rm g/s})$	8.1	9.6	9.45	-13.9	1.6



Figure 6: (a) Column densities and temperatures inferred from the IFTS camera data for the integration line Cl-2 shown in Fig. 4 (b). (b) Velocity profile inferred from the Horn-Schunk optical flow algorithm.

319 5.2. *IFTS measurement of a combustor*

Figure 7 (*a*) shows a Questor Q100 combustor that was operated at Carbon Management Canada's Newall County Research Station. The combustor was supplied with natural gas (~94.2% CH₄, 3.4% C₂H₆, 1.1% C₃H₈, and 1.3% minor components by volume) at approximately 42.5 standard cubic meters per hour. Local meteorological conditions (windspeed, wind direction, and temperature) were measured by a Davis onsite weather station, while ambient CO₂, CH₄, and H₂O concentrations were measured by a Picarro cavity ringdown spectrometer.

Figure 7 (b) shows the spectral intensity map at $\eta = 2283$ cm⁻¹, corresponding to the CO₂ "red 326 327 spike." Measurements were conducted at a distance of 150 m from the combustor stack exit, using a 128 px×128 px subdomain of the FPA, corresponding to a (6.6×6.6) m^2 area of the scene. The 328 detection spectrum was set between 1900 cm⁻¹ and 3400⁻¹ with a spectral resolution of 4 cm⁻¹ and 329 330 a fixed integration time of 50 µs. Figure 8 shows the intensity spectra for pixels "A" above, "B" 331 within, and "C" beneath the plume, along with the absorption coefficients of species that may be 332 in the plume (H₂O, CO, CO₂, CH₄). The spectra for pixels "A" and "B" show blackbody-like 333 behavior at low wavenumbers corresponding to an average temperature of approximately 255 K 334 under clear conditions. As one would expect, the spectral intensity for the plume pixel "B" is much 335 larger than those of "A" and "C" due to the thermal emission of the hot species. The intensity 336 spectra indicate the presence of CO₂, H₂O, CO, but shows no detectable CH₄, suggesting that the 337 combustor is operating with a high CE. Note also that the red and blue CO_2 spikes are more 338 pronounced compared to Fig. 5, due to the greater column density of ambient CO_2 between the 339 camera and the plume.



Figure 7: (a) Questor Q100 combustor; and (b) the intensity map at $\eta = 2283$ cm⁻¹, corresponding to the CO2 red spike. Spectra for locations A, B, and C along the integration line are shown in Fig. 8. Lens flare artifacts extend diagonally from the region of peak intensity.



Figure 8: Spectra for pixels "A", "B", and "C" shown in Fig. 7. Note the difference in scale between the top and the bottom plots.

341 The infrared intensity map in Fig. 7 (b) also reveals lens flare artifacts, which extend diagonally 342 from the brightest spot on the image. These artifacts affect all of the broadband images used to construct the interferogram, and are therefore difficult to remove through image post-processing. 343 344 The impact of lens flare on the recovered spectrum is highlighted in the bottom panel of Figure 8, 345 where the spectra from pixels "A" and "C" are superposed. The intensity spectra from pixel "C" 346 shows two small CO_2 spikes, as we would expect inside the plume but not outside the plume. It also shows an increase of intensity at 2,150 cm⁻¹ corresponding to CO emission lines. From the 347 348 spectra at pixel "C", it is difficult to identify that those spectral signatures come from an optical 349 artifact and not from species emissions. This artifact will cause the CO and CO₂ column densities 350 of these pixels to be over-estimated.

351 The "hole" between the red and blue CO₂ spikes for highlights the importance of accounting 352 for the atmospheric layer between the flare plume and the camera in the spectroscopic model. 353 Ambient conditions can often be inferred from the hyperspectral data by selecting pixels from the 354 flare stack region. In this particular measurement, however, the stack pixels are strongly affected 355 by the lens flare, so onsite concentrations of CO₂ and H₂O and temperature are used instead (Table 356 2). Given the long pathlength between the flare plume and the camera, it is crucial to include the $^{13}C^{16}O_2$ isotopologue, which has a natural abundance of approximately 1% and a red-shifted 357 358 absorption spectrum compared to that of the main ${}^{12}C^{16}O_2$ isotopologue.

359

Table 2: Ambient conditions set for the combustor hyperspectral measurement

Parameter	Onsite measured values
CO ₂	426 ppm ¹
H ₂ O	2914 ppm $(RH = 44\%)^1$
$T_{\rm amb}$ (K)	289 K ²

¹Picarro station ²Davis weather station Figure 9 shows the column density profiles for of CO_2 and CO, inferred using Eq. (3), the plume temperature, as well as the velocity profile found from the Lucas-Kanade algorithm. Since there were no CH_4 features in the intensity spectra, a subregion of the detection spectrum, between 2000 and 2470 cm⁻¹, was used for the inference, and a blackbody spectrum corresponding to 255 K is assumed for the background.

During the field trial wind speed was approximately 2.5 m/s during the measurement period, which is in good agreement with the peak velocity inferred from the optical flow algorithm. The velocities and column densities along the control line are used to infer the species mass flow rate, Eq. (2), and then multiplied by their respective carbon mass ratios (CO₂: 12/44, CO: 12/28) to obtain the carbon mass flow rate and estimate the combustion efficiency via Eq. (1). Figure 9 shows that the column densities increase drastically outside the plume compared to their densities



Figure 9: Column densities and peak temperature inferred from the spectroscopic model, and velocity profile inferred from the optical flow algorithm, for the combustor shown in Fig. 6. The shaded regions are excluded from the mass flow rate calculation.

371 inside the plume (0.7 m $< \theta < 1.9$ m). This behaviour is caused by the lens flare effects depicted in 372 Fig. 7 (b), and of the mischaracterization of the background intensity when modelled by Eq. (4). 373 Ouantification of the species mass flow rate and of combustion efficiency is therefore conducted 374 only for pixels covering the plume. Results are summarized in Table 3. When only considering the 375 part of the control line that crosses the plume (0.7 m $< \theta < 1.9$ m), as labeled in Fig. 9, the 376 combustor carbon mass flow rate is estimated at $\dot{m}_{\rm C} = 5.8$ g/s, which is in good agreement with the 377 known natural gas input carbon mass flow rate of 6.1 g/s (42.5 SCM of natural gas per hour). This 378 corresponds to a CE greater than 99%.

- 379
- 380

Table 3: CO₂ and CO mass flow rates of the combustor, inferred using the IFTS.

Species, k	$\dot{m}_{\mathrm{C},k}$ (g/s)
CO_2	5.8
CO	~ 0

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382 5.3.IFTS measurement of a steam-assisted flare at a refinery

A key application for this technique lies in conducting fenceline measurements on flares that burn unknown fuel compositions and at unknown rates, as is the case of a steam-assist flare at a petrochemical refinery in Southern Ontario, shown in Fig. 10.

A 128 px ×128 px subdomain of the FPA was used to image the flare, which corresponds to a (22.4×22.4) m² area for a measurement distance of 580 m. The spectral resolution was set to 4 cm⁻¹. With these parameters and an integration time of 100 μ s per image, the imaging framerate was 747 Hz, which required 3.17 s to form a complete interferogram. Figure 11 (*a*) shows the spectral intensity map for 2960 cm⁻¹, a part of the spectra that contains features corresponding to the principle C-H stretching mode of many hydrocarbons, while Figure 11 (*b*) shows the spectral



Figure 10: Steam assisted flare at a refinery. Measurements were carried out at a standoff distance of approximately 580 m.

intensity map for another wavenumber, $\eta = 2224$ cm⁻¹, corresponding to the combustion products 392 393 CO and CO₂. For that wavenumber, the map illustrates the lense flare artefacts and the flare halo 394 that affect the infrared image. As the lens flare transects the control line pixels, this artifact will 395 interfere with the inversion procedure and the column densities estimates. 396 Figure 12 (b) shows the intensity spectra for pixels above and within the plume ("A", "B") and 397 for a pixel at the plume extremity ("C"), along with absorption coefficients for H₂O, CO₂, and CO, 398 all of which are expected to be in the flare plume. The intensity spectra indicate the presence of CO₂, H₂O, CO, while the feature between 2800-3000 cm⁻¹ visible in the spectra for pixels "B" and 399 400 "C" indicates the presence of an unknown hydrocarbon. In the case of flares used to dispose of 401 process gas for upstream oil and gas production this signal would likely be CH₄, but the absence 402 of the R-branch lines at higher wavenumbers indicates the presence of a heavier hydrocarbon. The



Figure 11: (a) Intensity map at 2224 cm⁻¹ of the flare shown in Fig.10; this wavenumber corresponds to CO and CO₂ emission lines. For that wavenumber, lens flare and glowing of the flare is observed on the image. (b) Intensity map at 2960 cm⁻¹ of the flare shown in Fig. 10; this wavenumber corresponds to the principle C-H stretching mode of hydrocarbons. The National Pollution Release Inventory suggests that the flare is likely burning butane, which is consistent with the detected spectra (Fig. 12 (b)).

403 National Pollutant Release Inventory for this facility [25] suggests that the HC is butane, C_4H_{10} . 404 Like many heavier hydrocarbons, line parameters for butane are not available in the HITRAN 405 database. Instead, a comparison of the experimentally-derived molecular absorption cross-section 406 [20, 26] and the IFTS emissions spectrum confirms that this emission feature likely corresponds 407 to butane. This empirically-derived absorption spectrum is incorporated into the spectroscopic 408 model. This result highlights the importance of spectral and spatial resolution when calculating 409 flare CE, particularly for downstream oil and gas operations since the absorption cross-sections of 410 hydrocarbons generally do not scale with the number of carbons per molecule.

- 411 As mentioned for the combustor measurements, the spectra in Fig. 12 (*b*) corresponding to 412 pixels "B" and "C" feature two CO_2 emission "spikes" caused by emission the hot CO_2 in the flare
- 413 plume and its absorption by the ambient CO₂. For each pixel "A", "B" and "C", the spectra show

an increase in intensity around wavenumber 2224 cm⁻¹ that correspond to the halo and lens flare 414 artefacts. For pixels inside the plume like "B" and "C", the model attempt to recover that fictitious 415 416 signal by an increase in the CO_2 concentration. In Figure 12 (a), are represented the column 417 densities and plume maximum temperature along the control line. The CO₂ column density profile is increasing for pixels located at the plume extremities (e.g. pixel "C"), illustrating the effect of 418 419 lens flare and the overcompensation of the model (spectra "C" in Fig. 12 (b)). The CO₂ and C₄H₁₀ 420 spikes at the control line top and bottom pixels can be explained by those artefacts but also by the mischaracterization of the background, as shown by the intensity spectrum "A" in Fig. 12 (b). 421



Figure 12: (a) Column densities and peak temperature inferred along the control line shown in Fig. 11. The spikes in column density at the extreme ends of the integration line are likely caused by lens flare artifacts and mischaracterization of the background. The positions "A", "B" and "C" labeled along the control line correspond to the ones in Fig. 11; (b) Intensity spectra for pixels at positions "A", "B" and "C", along with the absorption coefficient of candidate species. Blue lines for wavenumbers corresponding to Fig. 11 images, show the emission from butane ($\eta = 2960 \text{ cm}^{-1}$) as well as the lens flare and glowing effect on the spectra ($\eta = 2224 \text{ cm}^{-1}$).

422 The ambient CO_2 and H_2O concentration and temperature needed to interpret the spectra are 423 shown in Table 4. Apart from the background and lens artefact, the modeled spectra are in 424 excellent agreement with the measured spectra.

- 425
- 426 Table 4: Ambient conditions during the hyperspectral measurement of the petrochemical flare.

Parameter	Value			
CO ₂	413 ppm ¹			
H ₂ O	$3666 \text{ ppm} (\text{RH} = 60\%^2)$			
$T_{\rm amb}$ (K)	280 K ³ (280.3 K ²)			
¹ Based on average atmospheric abundance				
² Environment Canada				
³ Onboard thermocouple				

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The velocities are found from the Lucas-Kanade algorithm, with a maximum normal velocity of 4.5 m/s. Column densities and velocities are substituted into Eq. (2) to obtain the mass flow rates shown in Table 5. Finally, these mass flow rates are multiplied by their respective carbon mass ratios (CO₂: 12/44, CO: 12/28, C₄H₁₀: 48/58) and then substituted into Eq. (1) to obtain an overall flare combustion efficiency of 97%. Table 5: CO₂, CO, and C₄H₁₀ carbon mass flow rates for the petrochemical flare.

Species, k	$\dot{m}_{\mathrm{C},k}$ (g/s)
CO ₂	27.2
CO	0.5
C_4H_{10}	0.3

434

435 **6.** Conclusions and future work

This study presents a technique for estimating flare combustion efficiency using a MWIR HS
camera. The mass flow rates needed for this calculation are found by combining species column
densities inferred using a spectroscopic model with a 2D velocity field obtained using an optical

439 flow algorithm. Crucially, this technique provides the capacity to infer flow rates and flare 440 efficiency through fenceline measurements, without requiring any knowledge about the fuel flow 441 rate supplied to the flare. This tool may be used by operators, flare equipment manufacturers, and 442 regulators to assess the combustion efficiency of flares in situ through standoff measurements. 443 This information is crucial to understand and minimize the impact of flaring on climate change. 444 While the approach focused on calculating CE, it may also be used to quantify emissions of other 445 types of flare emissions, including black carbon [27] and sulphur dioxide [28]. The combined 446 spectral and spatial resolution afforded by the IFTS is particularly well-suited in cases where the 447 species may be distributed heterogeneously in the flare plume and in cases where the species 448 present in the plume may be unknown or uncertain.

449 Despite the strong potential of this technique, there are a number of challenges that must be 450 overcome in order to improve the reliability of this approach. First and foremost, it is necessary to 451 quantify the uncertainties attached to the column densities and mass flow rates used to estimate 452 the CE, and to carry out benchmark validation measurements using an independent measurement 453 technique. The inversion of the spectroscopic model is deeply ill-posed, since an infinite set of 454 concentration and temperature distributions exist that, when substituted into Eq. (4), could explain 455 the spectroscopic data. The imposition of Gaussian profiles may be reasonable in a time-averaged 456 sense, but the instantaneous intensity field may be influenced strongly by turbulent fluctuations 457 between the concentration and temperature field (so-called "turbulence-radiation interactions" 458 [29]). A second source of model error comes from the use of intensity-weighted projected 459 velocities obtained from the optical flow algorithm. When the intensity variations are caused by 460 the absorption of background radiation it can be shown that the projected velocity field is a "mass-461 weighted velocity", which is appropriate for calculating a mass-flow rate [30, 27]. In this case,

462 however, the intensity variations are due to coupled fluctuations in local temperature and 463 concentration, and the resulting velocity field may not be mass-weighted. In both regards, working 464 with Bayesian inversion methods could help with both of those objectives, as it formalizes the 465 inclusion of prior information and account for quantification of the measurement and model 466 uncertainty propagation to the estimates.

467 There also remain several issues related to hardware implementation. Hyperspectral images of 468 the combustor and petrochemical flares were contaminated with lens flare features, likely caused 469 by coherent scattering of the most intense source of incident intensity (e.g., hot CO₂) by defects in 470 the optics. These artifacts are difficult to remove since they contaminate the broadband images 471 that are Fourier-transformed into the recovered spectra. Turbulence-induced SCAs and lens flare 472 both impact the intensity spectrum, and therefore the inferred temperature and species column 473 densities. While the impact of SCAs may be mitigated through filtering, flare artifacts are 474 considerably more challenging to remove. Future work will focus on developing image processing 475 techniques to remove lens flare, and experimental procedures for avoiding these features in the 476 first place.

477 Data availability statement

The data that support the findings of this study are openly available in "Replication Data for:
Quantifying Flare Combustion Efficiency using an Imaging Fourier Transform Spectrometer" at
https://doi.org/10.5683/SP3/JLMYWE.

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