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A detonation run-up distance database: data-driven existing models improvement and new model development

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Abstract

A comprehensive database of detonation run-up distances (x_{DDT}) in unobstructed tubes/channels is compiled. Eight fuels are included, i.e., hydrogen, methane, ethane, ethylene, acetylene, propane, butane and carbon monoxide. Oxygen is used as oxidizer with different diluents under a wide range of tube/channel sizes. In total 559 points are collected and analyzed. The global x_{DDT} trends observed in the data as a function of the initial conditions (i.e., fuel type, equivalence ratio (ϕ), hydraulic diameter (D_h), and pressure (p)) reveal that x_{DDT} decreases with increasing p, decreasing D_h , and $\phi \to 1$. The correlation of the normalized run-up distance x_{DDT}/D_h with geometrical parameters and fundamental combustion properties shows that most of the variance in the experimental data can be captured by the ratio of $D_{\rm h}$ to the flame thickness $(D_{\rm h}/\delta_{\rm f})$, the expansion ratio $(\sigma - 1)$ and that of the Chapman-Jouguet to the laminar flame speed $(V_{CI}/\sigma s_L)$. With these, a non-linear (NLM) and a logarithmic model (LM) are proposed using a non-linear least squares regression to fit a user-defined function. The NLM and LM are shown to outperform the widely used Silvestrini and Dorofeev models by a large margin since they are capable of explaining $\sim 70-80\%$ of the variance in the experimental $x_{\text{DDT}}/D_{\text{h}}$ data in contrast to only $\sim 20\%$ of the original Silvestrini and Dorofeev models. The poor performance of the original models is due to the limited amount of data used to determine the models constants. An update to these constants is also carried out using the database collected in this work resulting in a notable improvement of their predictive capabilities over the original models. The database is publicly available so that it can be used freely to guide future research in the combustion community (e.g., by identifying conditions where there is a lack of data), and as a test bed for further data-driven model development.

Keywords: Deflagration-to-detonation transition; detonation run-up distances; data-driven models; flame acceleration; fuel safety

1. Introduction

Under certain conditions, after accidental ignition 2 of a reactive cloud, the initial flame may accelerate 3 and transit to detonation, the so-called, deflagration-4 to-detonation-transition (DDT) phenomenon. Deto-5 nation is a supersonic combustion propagation regime 6 that is much stronger and more destructive than a flame. Although in most cases DDT occurs due to 8 flame/shock/obstacles interactions, it can also occur 9 in unobstructed spaces, such as gas compartments 10 and hoses in fuel cells, battery packs, electrolyzers, 11 12 among others. The determination of the DDT run-up distance x_{DDT} , defined as the distance between igni-13 tion of the flame and detonation onset, is not only im-14 portant for safety but also for the optimal design of 15 pulse detonation engines (PDE) [1]. 16

One way to estimate x_{DDT} is by using experimen-17 tal data together with phenomenological models. For 18 the latter, those proposed by Silvestrini et al. [2] 19 and Dorofeev et al. [3] are the most widely used 20 21 for predicting x_{DDT} in unobstructed channels. In [2] an expression for x_{DDT}/D_h is proposed, where D_h 22 is the hydraulic diameter of the tube/channel; here-23 inafter, the word channel(s) will be used to refer to 24 either. The model assumes that the flame: (i) is ig-25 nited at the closed end and propagates towards the 26 open end; (ii) its speed, $V_{\rm F}$, increases exponentially 27 with the relative axial position of the channel, $x/D_{\rm h}$, 28 i.e., $V_{\rm F} = \mathrm{A}\sigma s_{\rm L} \exp\left[\mathrm{B}(\sigma-1)(x/D_{\rm h})(D_{\rm h}/D_{\rm ref})^n\right]$, 29 30 where $s_{\rm L}$ is the laminar flame speed, σ is the expansion ratio, D_{ref} is a reference diameter, and A, B, and 31 n are constants. 32

To estimate the constants, six $V_{\rm F}(x)$ experimental 33 data for hydrogen, propane, and ethylene in air [4, 5] 34 were used. These tests were performed in 150, 250, 35 and 1400 mm diameter channels. Only one $V_{\rm F}(x)$ 36 profile per mixture was considered during curve fit-37 ting. The criterion to predict $x_{\text{DDT}}/D_{\text{h}}$ is that V_{F} must 38 achieve a critical value suitable to trigger DDT, that 39 is, half of the Chapman-Jouguet detonation velocity, 40 $V_{\rm F} = V_{\rm CJ}/2$. Silvestrini's model is thus 41

$$\frac{x_{\text{DDT}}}{D_{\text{h}}} = \frac{1}{B(\sigma - 1)} \left(\frac{D_{\text{ref}}}{D_{\text{h}}}\right)^n \ln\left(F\frac{V_{\text{CJ}}}{\sigma s_{\text{L}}}\right), \quad (1)$$

where B = 0.0061, n = 0.4, $D_{ref} = 0.15$ m, and 42 F = 0.5/A = 0.077. Since the constants were not 43 determined directly using x_{DDT} data but with V_{F} = 44 f(x) profiles, the model prediction is limited by the 45 $V_{\rm F} = V_{\rm CI}/2$ assumption. 46

On the other hand, the model proposed in [3] is de-47 rived via a mass balance considering that the flame 48 99 propagation speed is affected by the hydrodynamic 100 49 boundary layer (BL) growth in the channel whose 101 50 relative thickness is denoted by Δ . To estimate Δ , 102 51 the BL is assumed to grow linearly with the chan-103 52 nel's wall roughness, d and axial position, x, i.e., 104 53 $x/\Delta = [\ln(\Delta/d)/\kappa + K]/C$, where C, κ and K are 105 54 constants. x_{DDT}/D_h is obtained upon substitution of 55 106 56 the latter expression into the mass balance, and as-107

suming that DDT occurs when $V_{\rm F}$ reaches the sound 57 speed in burnt gases, i.e., $V_{\rm F} = c_{\rm b}$. Dorofeev's model 58 59

$$\frac{x_{\text{DDT}}}{D_{\text{h}}} = \frac{\Gamma}{C} \left[\frac{1}{\kappa} \ln \left(\Gamma \frac{D_{\text{h}}}{d} \right) + K \right], \qquad (2)$$

where
$$\Gamma = \left[\frac{c_{\rm b}}{\zeta(\sigma-1)^2 s_{\rm L}} \left(\frac{\delta_{\rm f}}{D_{\rm h}} \right)^{\xi} \right]^{rac{1}{2m+7/3}},$$

and $\delta_{\rm f} = \alpha/s_{\rm L}$ is the laminar flame thickness with α denoting the mixture thermal diffusivity; ζ and mare additional constants. To estimate the constants, nine $V_{\rm F}(x)$ data from [6–10] were used, of which eight were H₂-O₂/air mixtures, and one a hydrocarbon (HC)/air mixture. Four of these were performed using channels with blockage ratio ≈ 0.1 , which is known to modify the DDT behavior compared with unobstructed channels. The $D_{\rm h}$ range considered was $D_{
m h}~\in~[15,520]~{
m mm}$ resulting in $C~=~0.2,\kappa~=$ $0.4, K = 5.5, \zeta = 2.1, \xi = 1/3$ and m = -0.18.

It is evident that the models performance hinges on the appropriate determination of the constants. The limited data used in [2] and [3] did not account for a wide range of fuels, diluents, compositions/equivalence ratios (ϕ) and $D_{\rm h}$, so their predictions are expectedtly restricted. Indeed in [11], Silvestrini's model was evaluated against data from [12, 13] showing poor performance for all the experimental conditions tested. For DDT predictions, large amounts of data are required to account for the variability of the process.

To fill this gap, here, a large database is compiled using all the x_{DDT} data for unobstructed channels available in the literature. In total, 559 tests were collected, including both HCs and hydrogen over a wide range of experimental conditions ($D_{\rm h}$, ϕ , pressure (p) and temperature (T)). The constants of the Silvestrini and Dorofeev models are updated resulting in a significant improvement of their predictive capabilities. Furthermore, two additional simpler expressions that outperform the original Silvestrini and Dorofeev models by a large margin are proposed.

2. Database description

To collect the data a systematic search was performed in Scopus. As criteria, only scientific papers reporting experimental x_{DDT} values obtained in unobstructed channels using weak ignition sources to avoid direct detonation initiation were considered. x_{DDT} is compiled together with the mixture initial conditions, i.e., T, p, and ϕ . Geometrical information such as D_h , length (L), cross-section (CS) and boundary conditions (BC) are also included. The latter refers to channels with Closed/Closed (C/C) or Closed/Opened ends (C/O). Table 1 summarizes the data collected. A total of 36 references were reviewed. The data are split into C/O and C/C channels, and ordered according to the fuel used. Experi-

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1 mental data obtained for the current work in the two-

² directional schlieren visualization set-up described in

³ [14, 15] are included as well.

4 2.1. Geometrical parameters

The ranges of L and D_h for which data were found are $L \in [0.4, 40]$ m and $D_h \in [0.6, 406]$ mm, and $L \in [0.8, 24]$ m and $D_h \in [0.5, 159]$ mm for C/O and C/C channels, respectively. The minimum and maximum L/D_h ratios in the dataset are $L/D_h = 6$ and 4000.

11 2.2. Mixtures and initial conditions

A total of eight fuels are included, i.e., hydro-12 gen (H_2) , methane (CH_4) , ethane (C_2H_6) , ethylene 13 (C₂H₄), acetylene (C₂H₂), propane (C₃H₈), butane 14 (C_4H_{10}) , and carbon monoxide (CO). Almost all are 15 fuels of a single component, except for some in [30] 16 that correspond to CH_4/C_2H_6 , some in [26] that used 17 18 H_2/C_3H_8 , and some measured by the current authors using H_2/CH_4 blends. Oxygen (O₂) is the oxidizer 19 whereas nitrogen (N_2) , helium (He), argon (Ar) and 20 carbon dioxide (CO₂) are used as diluents. The ini-21 tial conditions ranges are $T \in [298, 473]$ K, $p \in$ 22 [0.1, 25] bar, and $\phi \in [0.2, 5.8]$. 23

24 2.3. Number of data points and distribution

Table 1 also shows the number of data points (DP) 25 per fuel. 202 and 357 DP were collected for C/O and 26 C/C which correspond to a total of 559 tests. H_2 and 27 C_2H_4 are the most often used fuels, with 193 and 191 28 DP, respectively. These are followed by C_3H_8 (95) 29 DP), and CH₄ (29 DP). The least used are C_2H_2 (18 30 DP), CO (15 DP), C₂H₆ (9 DP), and C₄H₁₀ (9 DP). 31 Figure 1 shows the D_h , Φ and p histograms for 32 (a) C/O, and (b) C/C. Tests carried out with H₂ and 33 HC are plotted with different colors; the 15 DP with 34 CO are not included. The histograms reveal that for 35 both BCs most of the tests were performed in chan-36 nels with $D_{\rm h} \leq 50$ mm. 37 Regarding mixture compositions, the normalized 38 equivalence ratio, $\Phi = \phi/(1 + \phi)$ is used to center 39 the distribution at $\phi = 1.0$ (i.e., $\Phi = 0.5$), thereby 40 lengthening the axis for $\phi < 1$ and shortening it for 41 42 $\phi > 1$. For C/O, most of the tests are performed with HC fuels of which 81 DP correspond to stoichiomet-43 ric ($\Phi\,=\,0.5$), 28 to lean ($\Phi\,<\,0.5$), and 37 to rich 11 $(\Phi > 0.5)$ conditions. For H₂, 29 DP correspond to 45 $\Phi = 0.5, 11$ to $\Phi < 0.5$, and 16 to $\Phi > 0.5$. For C/C, 46 the data is distributed as follows: 171 DP at $\Phi = 0.5$, 47 14 at $\Phi < 0.5$, and 20 at $\Phi > 0.5$ for HC mixtures. 48 For H₂ mixtures, 81 DP correspond to $\Phi = 0.5, 29$ 49 to $\Phi < 0.5$, and 27 to $\Phi > 0.5$. Finally, the p his-50 togram shows, expectedly, that all the tests with C/O 51 channels are performed at atmospheric pressure, i.e., 52 $p \approx 1$ bar. For C/C, most of the tests are carried out 53 at p < 1 bar with 157 and 14 DP for HC and H₂ mix-54 55 tures, respectively. For p > 1.0 bar, 21 (HC) and 92



Fig. 1: Histograms for D_h , Φ and p. (a) Closed/Open; (b) Closed/Closed channels.

(H₂) DP were found, and at p = 1.0 bar, 27 (HC) and 31 (H₂) DP were collected

This visualization allows to identify regions where there is little to no data available in the literature, and may serve as a guide for future DDT research. As an example, only 9 data points were collected at 473 K for C/C channels [22]. The remaining were obtained at room temperature, i.e., ≈ 298 K (not shown). This shows high research potential of the effect of T on x_{DDT} in unobstructed channels since most of the industrial processes where DDT may occur are either at high T, e.g., electrolyzers and nuclear reactors, or low T, e.g., cryogenic fuel or oxidizer transportation. Additionally, the lack of data for $D_{\rm h} > 50$ mm is evident, which corresponds to most of the industrial pipelines in service. Data is missing for C_2H_2 , C_2H_6 , and C₄H₁₀, HC extensively used in many industries. Likewise for CO, which is of interest because it is one of the main components of Syngas and it is expected to play an important role in the energy transition. Finally, note that most data exist at stoichiometric conditions but many accidents are the result of accidental ignition of a reactive cloud after leakage/mixing of fuel/oxidizer effectively resulting in scenarios where lean/rich mixtures are present.

2.4. Preprocessing of database

Three conditions were identified for which the DP follow different trends compared to most of the tests in the database: (i) channels with $D_h < 3$ mm; 123 DP from [23–25, 33–35, 41, 42]. These include tests with both H₂ and HC for C/O and C/C at $\phi \in [0.7, 1.7]$, and $p \in [0.1, 2.4]$ bar performed mostly in spiral channels or with central ignition. (ii) channels with non-unity aspect ratio (AR); 119 DP from [27, 36] with AR ranging from 1:1.5 to

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Table 1: Database summary.									
Fuel	BC	ϕ	Diluents	D _h [mm]	L [m]	p [bar]	CS	DP	References
H_2	C/0	0.25 - 2.1	N ₂ , Ar, He	3 - 406	1 - 40	1	Cir.; Sqr.	56	[5, 11, 12, 14, 16–21], CW
	C/C	0.2 - 2.8	N_2 , Ar, He, CO_2	0.5 - 159	0.8 - 24	0.1 - 25	Cir.; Rec.	137	[6, 7, 13, 22–29]
CH_4	C/O	1.0	N_2	10 - 50	1 - 11	1	Cir.; Sqr.	12	[11, 15, 18, 30], CW
	C/C	0.35 - 2.0	N_2	15 - 20	1.5 - 2.9	0.3 - 25	Cir.; Sqr.	17	[22, 31]
C_2H_2	C/O	_	_	_	_	_	_	_	_
	C/C	0.27 - 5.8	N_2	15	2.9	1 - 5	Cir.	18	[22]
C_2H_4	C/O	0.63-1.7	N_2	0.6 - 406	0.4 - 40	1	Cir.; Sqr.	55	[5, 11, 18, 32–35]
	C/C	0.35 - 2.7	N_2	10 - 127	1 - 6	0.1 - 1.7	Cir.; Rec.	136	[7, 28, 36–39]
C_2H_6	C/O	1.0	N_2	26 - 50	2 - 11	1	Cir.	9	[18, 30]
	C/C	_	_	_	_	_	_	_	-
C_3H_8	C/O	0.5 - 1.7	N_2	25.4-406	0.5 - 40	1	Cir.	61	[5, 11, 30, 32, 40]
	C/C	1.0	N_2	0.5 - 3	2	0.1 - 1	Cir.	34	[26, 41]
C_4H_{10}	C/O	1.0	N_2	50.8	11	1	Cir.	9	[30]
	C/C	_	_	_	_	_	_	—	-
СО	C/O	_	_	_	_	_	_	_	_
	C/C	0.4 - 2.0	—	50	2.9	5 - 25	Cir.	15	[22]

Legend: current work (CW); circular (Cir.); square (Sqr.); rectangular (Rec.). Refs. [27, 36] include channels with $AR \neq 1$.

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1:30. These include tests with stoichiometric H_2 and 1 C_2H_4 at p < 0.7 bar. (iii) the use of CO as fuel, 2 with 15 DP from [22]; these tests were carried out 3 at high pressure, i.e., $p \in [5-25]$ bar. Only data 4 that did not meet the conditions above are considered 5 in the analysis that follows. A total of 302 DP are 6 thus retained after filtering: 132 for H_2 and 1707 for HC mixtures. The final experimental ranges are 8 $D_{\rm h} \in [3, 406] \text{ mm}, \phi \in [0.2, 5.8], p \in [0.12, 25] \text{ bar},$ 9 and $T \in [298, 474]$ K. 10 11

The database and scripts are made publicly available as a github repository (https://github.com/
MejiaBotero/DDTdatabase).

15 3. *x*DDT trends

16 3.1. x_{DDT} vs. D_h , Φ , and p

17 It is of practical interest (safety/propulsion) to identify/verify the general dependence of x_{DDT} on ge-18 ometrical and initial conditions. Figure 2 shows these 19 trends as a function of D_h , Φ , and p. For ease of visu-20 alization, selected cases were taken from the database 21 to isolate the effect of the respective variable on x_{DDT} , 22 however, the trends hold for all mixtures considered. 23 Concerning $D_{\rm h}$, stoichiometric ($\Phi = 0.5$) H₂/air and 24 C_2H_4/air at p = 1 bar from [5, 16, 32]. The plot 25 shows that x_{DDT} increases almost linearly with D_h 26 for both mixtures. Regarding Φ , H₂/air and C₃H₈/air 27 mixtures from [16, 32] tested in $D_{\rm h} = 50$ mm chan-28 29 nels at p = 1 bar. A U-shape curve is observed with x_{DDT} exhibiting a minimum around $\Phi = 0.5$. Fi-30 nally for p, part of the experiments presented in [22] 31 for H_2/O_2 and CH_4/O_2 in $D_h = 15$ mm channels at 32 33 $\Phi = 0.5$ are shown. There is a pronounced decrease

in x_{DDT} as p increases. The trends reveal that the use of pure O_2 as oxidizer significantly decreases x_{DDT} for H_2 and HC mixtures. Based on the database collected, for PDE design where short x_{DDT} values are desirable, small D_h channels at high pressure and under stoichiometric conditions using pure O_2 as oxidizer are advised; the opposite holds for safety applications.



Fig. 2: x_{DDT} trends vs. D_h , Φ , and p for selected cases.

3.2. x_{DDT}/D_h vs. fundamental combustion properties

The effect on x_{DDT} of the (ratios of) fundamental combustion properties (i.e., $V_{\text{CJ}}/\sigma s_{\text{L}}$, c_{b}/s_{L} , and $\sigma-1$) and that of the channel size to the laminar flame thickness (i.e., D_{h}/δ_f) used in the Silvestrini and Dorofeev models is evaluated next to assess whether the dependencies assumed hold, and to identify potentially overlooked relevant variables. The analysis is carried out on $x_{\text{DDT}}/D_{\text{h}}$ to absorb channel size effects

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1 on the output variable. The hydraulic diameter to detonation induction length ratio, $D_{\rm h}/l_{\rm ind}$, the Zel'dovich 2 number, $\beta = E_{a}(T_{b} - T_{u})/(RT_{b}^{2})$, and the heat ca-3 pacity ratio, $\gamma = c_{\rm p}/c_{\rm v}$, are also evaluated. $E_{\rm a}$ is the 4 effective activation energy, $T_{\rm b}$ and $T_{\rm u}$ are the burnt 5 and unburnt/fresh gases temperature, respectively; cp 6 and $c_{\rm v}$ are the heat capacity at constant pressure and 7 volume. All properties were computed with Can-8 tera using GRI 3.0 chemical mechanism, except for 9 C_4H_{10} for which the San Diego mechanism was used. 10 Figure 3 shows the Pearson autocorrelation matrix for 11 the properties considered which measures colinearity 12 13 between two sets of data. Values close to unity indicate a strong correlation, and suggest that these vari-14 ables capture the $x_{\text{DDT}}/D_{\text{h}}$ dependencies observed in 15 16 the data.



Fig. 3: Pearson autocorrelation matrix for $x_{\text{DDT}}/D_{\text{h}}$.

The most correlated with $x_{\text{DDT}}/D_{\text{h}}$ are $D_{\text{h}}/\delta_{\text{f}}$ and 17 $D_{\rm h}/l_{\rm ind}$, both with correlation coefficients of 0.79. 18 Note however that these two variables are also corre-19 lated with each other indicating that they provide sim-20 ilar statistical information about x_{DDT}/D_h . D_h/δ_f is 21 retained since for flame propagation and acceleration 22 δ_f is a more sensible length scale to consider. No-23 tably, the latter ratio is included in Dorofeev's and not 24 25 in Silvestrini's model. The next in line is $\sigma - 1$ which was found to have a strong effect on the x_{DDT}/D_h pre-26 dictions that will be presented in section 5, and to be 27 highly correlated to γ ; both Silvestrini and Dorofeev 28 include $\sigma - 1$ and omit γ in their models. The fol-29 lowing is $V_{\rm CJ}/\sigma s_{\rm L}$ (used in Silvestrini) which in turn 30 is correlated to c_b/s_L (used in Dorofeev). The former 31 ratio is retained because of its higher correlation with 32 $x_{\text{DDT}}/D_{\text{h}}$. In addition, β exhibits a correlation coeffi-33 cient of 0.41. While similar to that of c_b/s_L , it does 34 not seem to be correlated to any of the other variables 35 considered. The addition of this property to the mod-36 37 els proposed in section 5 had a very modest effect on their performance, consequently, it was not consid-38 ered further. Finally, the high correlations between (i) 39 $V_{\rm CJ}/\sigma s_{\rm L}$ and $c_{\rm b}/s_{\rm L}$, and (ii) $D_{\rm h}/\delta_{\rm f}$ and $D_{\rm h}/l_{\rm ind}$, are 40 worth mentioning. While (i) is not surprising because 41

 $c_b \approx V_{\text{CI}}/2$, (ii) is not so straightforward since these two lengths are governed by different physics. The latter observation may warrant a deeper analysis but it is beyond the scope of the current work.

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Figure 4 shows the trends of x_{DDT}/D_h with D_h/δ_f , $V_{\rm CJ}/\sigma s_{\rm L}$, and $\sigma - 1$. The BC type does not seem to have an important effect on $x_{\text{DDT}}/D_{\text{h}}$ since both C/O and C/C follow the same behavior. $D_{\rm h}/\delta_{\rm f}$ is inversely proportional to $x_{\text{DDT}}/D_{\text{h}}$. Large $D_{\text{h}}/\delta_{\text{f}}$ values indicate that the flame is thin compared to the channel dimensions, which in turn favors the development of surface instabilities and large flame surface area. This results in increased flame acceleration leading to a decrease in $x_{\text{DDT}}/D_{\text{h}}$. On the other hand, $x_{\text{DDT}}/D_{\text{h}}$ is directly proportional to $V_{\rm CJ}/\sigma s_{\rm L}$. A mixture with high $V_{\rm CJ}$ must be accelerated more prior to transition, and a low $\sigma s_{\rm L}$ is representative of mixtures with slow laminar flame speeds. It is thus expected that a large $V_{\rm CJ}/\sigma s_{\rm L}$ ratio results in large $x_{\rm DDT}/D_{\rm h}$ values. Finally, of interest is that $\sigma - 1$, exhibits different slopes for H2 and HC while both being inversely proportional to $x_{\text{DDT}}/D_{\text{h}}$. The latter observation stems from the fact that there is a large difference in σ between both fuel types. For the conditions at hand (i.e., flame acceleration in channels ignited at the closed end), higher σ values lead to increased acceleration rates during the early stages of flame propagation.



Fig. 4: x_{DDT}/D_h vs. ratios of fundamental combustion properties.

4. Existing model evaluation

4.1. Silvestrini and Dorofeev vs. database

Figure 5 compares the models predictions against the experimental database. A 45° line showing the ideal performance is added as a visual aid. That is, values that are predicted well by the models are expected to fall on this line. Most references do not report the standard deviation of their x_{DDT} data, hence an arbitrarily defined deviation band of $\pm 15\%$ (blue shading) is plotted to account for experimental uncertainties. The coefficient of determination (R²) is used as our metric to assess the models performance. It was computed using standard functions from the scikitlearn package [43]. The best possible score is R² = 1

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and it can be negative. A negative R² implies that a
model fits the data worse than a horizontal line at a
height equal to the mean of the observed data. This
occurs when a wrong model is chosen or nonsensical
constraints are inadvertently applied.

Both models performed poorly with R^2 of -0.886 and 0.23 for Silvestrini and Dorofeev, respectively. 7 8 R^2 was also computed for H_2 and HC mixtures separately. The scatter is higher for H₂ mixtures ($R_{H2}^2 =$ 9 -3.5 (Silvestrini) and -0.05 (Dorofeev)) than with 10 HCs ($R_{HC}^2 = 0.54$ (Silvestrini) and 0.37 (Dorofeev)). 11 Note that there are outliers present in the evalua-12 13 tion of the models. These are simply a reflection of their (poor) performance against our database, and 14 a consequence of the limited amount of data used 15 to determine the original models constants. Ulti-16 mately, this prevents them from properly reproduc-17 ing the $x_{\rm DDT}/D_{\rm h}$ trends with fundamental combus-18 tion properties over the wide range of experimental 19 conditions considered. In subsection 4.2 the original 20 constants are updated. 21



Fig. 5: Original models performance against database: a) Silvestrini and b) Dorofeev.

22 4.2. Updated Silvestrini and Dorofeev constants

An update to Silvestrini and Dorofeev model con-23 stants was done using the database collected in this 24 work which includes a much wider range of oper-25 ating conditions and fuels. As the fitting target is 26 x_{DDT} rather than $V_{\text{F}} = f(x)$ data, it allows for 27 a direct prediction/estimate of the variable of inter-28 80 % of the data were used as the training est. 29 set and 20 % as the test set. That is, 242 DP 30 were used to determine the constants and 60 DP to 31 evaluate the performance of the models. To select 32 these data, the train_test_split() function of scikit-33 learn [43] was used. It splits the data randomly 34 by selecting a user-defined percentage. The initial 35 conditions ranges for the training data are $D_{\rm h} \in$ 36 $[3, 406] \text{ mm}, \phi \in [0.2, 5.8], p \in [0.12, 25]$ bar, 37 and $T \in [298, 474]$ K, and for the test data $D_{\rm h} \in$ 38 $[3, 406] \text{ mm}, \phi \in [0.21, 2.8], p \in [0.21, 25]$ bar, and 39 $T \in [298, 474]$ K. The fitting was carried out using 40 41 the *optimize.curve_fit(*) function of SciPy which

essentially uses a non-linear least squares regression method to fit a function. The updated constants are listed in Table 2.

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Figure 6 shows the fitting results with the training data and the performance with the test data for the updated a) Silvestrini, and b) Dorofeev. The improvement is evident with R² values of 0.74 and 0.73 for the respective models with the train data. Their performance with the test data have \mathbb{R}^2 values of 0.7 and 0.71, respectively. Again, this represents significant improvements compared to the original models, and indicates that $\sim 70\%$ of the variance in $x_{\rm DDT}/D_{\rm h}$ can now be explained by the updated models. The remaining $\sim 30\%$ can be attributed to unknown lurking variables or inherent variability. Note that the model's underlying assumptions were carefully verified to ensure that the updated constants values did not lead to non-physical flame velocities (Silvestrini) or unreasonable BL growth (Dorofeev) as a function of the axial position in the channel. Silvestrini/Dorofeev resulted in a measurable/modest increase/decrease compared to that originally obtained. The revised $V_{\rm F}(x)$ and $\Delta(x)$ dependence better reflects the experimentally observed trends (not shown).



Fig. 6: Updated a) Silvestrini and b) Dorofeev performance for training and test data.

5. Proposed models

Two additional simpler models are proposed, i.e., non-linear (NLM) and logarithmic (LM), that leverage the learnings from the data analysis carried out in the previous sections. The expressions are shown in Equation 3, and Equation 4, respectively.

$$\frac{x_{\text{DDT}}}{D_{\text{h}}} = \frac{a_0}{(\sigma - 1)^{a_1}} \left(\frac{D_{\text{h}}}{\delta_{\text{f}}}\right)^{-a_2} \left(\frac{V_{\text{CJ}}}{\sigma s_{\text{L}}}\right)^{a_3}, \quad (3)$$

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$$\frac{x_{\text{DDT}}}{D_{\text{h}}} = \frac{b_0}{(\sigma - 1)^{b_1}} \ln \left[b_2 \left(\frac{D_{\text{h}}}{\delta_{\text{f}}} \right)^{-1} \left(\frac{V_{\text{CJ}}}{\sigma s_{\text{L}}} \right) \right].$$
(4)

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NLM considers the influence of the most important 1 2 variables discussed in subsection 3.2 to estimate four constants: a_0 , a_1 , a_2 , and a_3 . Note that this expression is general and does not take into account any in-4 formation regarding the $x_{\text{DDT}}/D_{\text{h}}$ trends observed in 5 Figure 4. On the other hand, LM accounts for the log-6 arithmic trend that $x_{\text{DDT}}/D_{\text{h}}$ exhibits when plotted as 7 a function of $D_{\rm h}/\delta_{\rm f}$ and $V_{\rm CJ}/\sigma s_{\rm L}$. Three constants 8 need being estimated: b_0 , b_1 , and b_2 . The constraint $b_2 > (D_h/\delta_f)(V_{CI}/\sigma s_L)^{-1}$ was enforced during the 9 10 11 regression so that the argument of the natural logarithm is always greater than unity thereby ensuring 12 that all the $x_{\text{DDT}}/D_{\text{h}}$ estimates are positive; Table 2 13 lists the fitting results. Note that although these are 14 data driven models, the choice of variables is based 15 16 on lower/upper bounds for combustion wave steady propagation speeds (i.e., $s_{\rm L}$ and $V_{\rm CJ}$), length scales 17 (i.e., $\delta_{\rm f}$ and $D_{\rm h}$), first order approximations of the 18 flow induced ahead of the flame (i.e., $(\sigma - 1)s_{\rm L}$), 19 and the flame speed in the laboratory frame (i.e., 20 $V_{\rm F} = \sigma s_{\rm L}$). All of them have physical significance 21 and are relevant to the FA process. Therefore, these 22 are semi-empirical models that take into account the 23 phenomenology of the process. 24

Table 2: Models constants.								
Model	Eq.	Constants						
		Original	Updated					
Silvestrini	eq. (1)	B = 0.0061 n = 0.4	B' = 0.0057 n' = 0.07					
	1 \ /	F = 0.077	F' = 0.084					
		C = 0.2	C' = 0.26 c' = 0.13					
5		$\kappa = 0.4$ K = 5.5	K = 0.13 K' = -1.75					
Dorofeev	eq. (2)	$\zeta = 2.1$	$\zeta' = 0.046$					
		$\xi = 1/3$	$\xi' = 1.32$					
		m' = -0.18	m' = 1.46					
		$a_0 =$	= 184					
NLM	ea. (3)	$a_1 = 0.82$						
	1 \ /	$a_2 = a_2 = a_2$	0.11					
		$u_3 =$	0.23					
1.14	eq. (4)	$b_0 =$	= 50					
LM		$b_1 = b_2$	= 0.7 4500					
		$v_2 =$	4000					

Figure 7 shows the fitting with the train, and the 25 evaluation with the test data for a) NLM, and b) LM. 26 Both train and test data are the same sets used in the 27 28 previous sections to enable a meaningful comparison of the models performance. The LM has a better fit to 29 the training data with an \mathbb{R}^2 of 0.78 compared to 0.72 30 for the NLM. This was also reflected in the perfor-31 32 mance with the test data, with a \mathbb{R}^2 of 0.84 for the LM and 0.74 for the NLM. The prediction of both models is much better than that of the original Dorofeev and Silvestrini, and have higher (LM)/similar (NLM) \mathbf{R}^2 values than those obtained with the updated Silvestrini and Dorofeev models. Additionally, note the improvement in the predictions for $x_{DDT}/D_h \text{ Exp} <$ 50 when using the LM. This provides evidence of the value of simple data manipulations (e.g., non-linear regressions) to enhance the predictive capabilities of existing models and/or inform the development of new simpler expressions/correlations with comparable or better performance. The most important aspect is the use of large properly curated data sets covering a wide range of experimental conditions, fuels, and geometries to guide the choice of variables that explain the variance of the experimental measurements. Finally, additional models were also tested in this work (not shown) including but not limited to linear models with dimensional variables, differentiating by BC, type of fuel, etc. However, these resulted in lower performance than the proposed NLM and LM. Strategies such as using data specific to H₂ and HC, as well as assessing kinetic mechanisms induced uncertainties were evaluated and are included as supplementary material for completeness.



Fig. 7: a) Non-linear (NLM) and b) Logarithmic (LM) models performance for training and test data.

6. Conclusions

A large database is compiled using a comprehensive set of x_{DDT} data for unobstructed channels available in the literature. It comprises an extensive range of experimental conditions and mixtures. The global x_{DDT} trends as a function of D_h , ϕ , and p were evaluated. The data shows that x_{DDT} decreases as D_h decreases, p increases, and $\phi \rightarrow 1$. An analysis of the

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effect of the ratios of fundamental combustion proper-56 1 ties on x_{DDT}/D_h revealed that those that most affect 57 2 it are $D_{\rm h}/\delta_{\rm f}$, $V_{\rm CI}/\sigma s_{\rm L}$ and $\sigma - 1$. The most widely 58 3 59 used models for x_{DDT} predictions, i.e., Silvestrini and 60 Dorofeev, were tested against the database perform-5 ing rather poorly. An update to the models con-6 62 stants was carried out via a non-linear least squares 7 63 regression using the large database compiled. This 8 64 resulted in significant improvements in their perfor-9 65 mance. Finally, two simplified models were pro-66 10 posed. Their predictions are significantly better than 67 11 those of the original Silvestrini/Dorofeev models and 68 12 13 higher (LM)/similar (NLM) to those obtained with the 70 updated models. Future work will include the use of 14 71 the database to: (i) train a model that will be tested on 15 72 obstructed channels using an expression that captures 16 73 the experimental dependence of x_{DDT} as a function of 17 74 the blockage ratio; (ii) develop x_{DDT}/D_h models valid 18 19 for $D_{\rm h} < 3$ mm and non-unity AR channels.

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Supplementary material 25

The following is included: 26

- · Original Silvestrini and Dorofeev models per-27 formance against the database without perform-28 ing the data pre-processing discussed in subsec-29 tion 2.4. 30
- The updated Silvestrini and Dorofeev, and pro-31 posed NLM and LM models evaluated on differ-32 ent datasets: (i) against the data excluded after 33 pre-processing, and (ii) against the H₂ and HC 34 data separately. 35
- · New model constants for the updated Silvestrini 36 101 and Dorofeev, and proposed NLM and LM mod-102 37 38 els under three scenarios: (i) without database 103 104 pre-processing, (ii) using the H₂ and HC data 39 105 separately from the pre-processed database, and 40 106 (iii) using the pre-processed database but with 41 107 different kinetic mechanisms (San Diego [44] 42 and FFCM-2 [45]). 43 109

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