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### Polarization structure of nanostrip domain intersections in GeTe films

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Ferroelectric germanium telluride is under active consideration for spintronic and thermoelectric applications. The control of the ferroelectric domain walls is a key issue to optimize the electronic and thermal properties of GeTe thin films. Domain walls properties are usually driven by the mechanical and electrostatic compatibility conditions of twin domains. However in dense ferroelectric domain structures these compatibility conditions are hardly fulfilled everywhere. In particular intersection of domains may result in complex lattice relaxations and polarization textures. In this study, we have fabricated GeTe thin films on silicon substrate and elucidated the intersections of a-type domains using 3D reciprocal space maps, scanning tunneling microscopy and second-harmonic microscopy. We demonstrate the presence of complex structural reorganizations, that manifest by the formation of charged domains walls, large lattice rotations and enhanced stretching of the rhombohedral lattice.

### INTRODUCTION I.

Ferroelectric thin films are the object of intense funda-• mental research stimulated by their applications as func-<sup>10</sup> tional materials. The ability to synthesize ferroelectric thin films of high crystalline quality based on layer-by-11 layer growth techniques and strain engineering has made 12 possible to discover novel phenomena based on the inter-13 play between the stress induced by the substrate and the 14 electrostatic boundary conditions. It has been demon-15 strated that flux-closure polar domains [1–3], vortices [4] 16 and 5 and even skyrmions 6 could be obtained in fer-17 roelectric materials. These novel structures can poten-18 <sup>19</sup> tially exhibit enhanced electric conduction as measured at vortex cores in  $BiFeO_3$  [2], high thermal resistance 20 [7], or high Seebeck coefficient at charged domain walls 21 [8]. Such properties could be used in future devices if 22 <sup>23</sup> the local ferroelectric polarization can be controlled. In 24 the quest of enhanced ferroelectric properties, intersections of domain walls are expected to show highly polar-25 ized regions with complex polarization textures resulting 26 from a strong relaxation of the lattice. Among ferro-27 electrics, GeTe has witnessed a sustained boom [9–14]. 28 As a thermoelectrics, it has recently been demonstrated 29 a record figure of merit  $(zT\sim2.4)$  at 330°C for the ferro-30 electric GeTe phase [15]. In the meantime, major results 31 have been obtained on ferroelectric GeTe thin films in 32 the context of spintronic properties based on the Rashba 33 effect [16]. It has been demonstrated the reversal of the 34 ferroelectric polarization under an electric field [17] and a 35 consistent change of the spin chirality of the band struc-36 ture [18 and 19]. Even more fascinating GeTe thin films 37 show remarkable transport properties at room tempera-38 ture such as non-reciprocal charge transport [20] or fer-39 40 roelectric switching of the spin-to-charge conversion [21].

All these results take advantage of the ferroelectric 41 42 43 structure (space group R3m) and bulk Curie temperature 33 chine learning methods, reveals different crossing types

45 spontaneous polarization of  $\alpha$ -GeTe is along the pseu-46 docubic  $\langle 111 \rangle_c$  leading to the formation of 4 ferroelastic 47 variants (c stands for pseudo-cubic coordinates, see sup-<sup>48</sup> plementary materials [22]). As reported by Wang et al. 49 [23]  $\alpha$ -GeTe thin films can be grown with a quasi-single <sup>50</sup> crystalline quality on Si(111) by molecular beam epitaxy <sup>51</sup> using a pre-deposition of 1 monolayer of Sb onto the sub- $_{\tt 52}$  strate. Despite a significant lattice mismatch of  ${\sim}8.5\%$ <sup>53</sup> with the substrate, the GeTe layer is relaxed since the <sup>54</sup> very beginning of growth. Croes et al. [24] have shown 55 that GeTe thin films thicker than 30 nm have a multi-56 ple domain structure with all 4 ferroelastic variants. The 57 main domain has a ferroelectric polarization perpendicso ular to the surface, *i.e.* in the  $[111]_c$  direction, and is 59 called *c*-domain. The three other ferroelectric domains 60 are called hereafter *a*-domains and form  $71^{\circ}$ -type domain  $_{61}$  walls with the *c*-domain. These domain walls ensure me-62 chanical compatibility and neutrality of the interface be-63 tween a- and c-domains. In addition to the a/c twin 64 domains, the simultaneous existence of different variants of a-domains generates inevitably  $a/a 109^{\circ}$ -type intersec-66 tions.

In this article we address the intersection of *a*-domains 67 68 in GeTe thin films and explore the formation of non- $_{69}$  trivial polarization configurations. Since *a*-domains are <sup>70</sup> already constrained by the interaction with the major-<sup>71</sup> ity c-domain that is in epitaxy with the Si substrate,  $\tau_2$  the crossing of *a*-domains generates major problems of 73 mechanical and electrical compatibilities. We show that 74 a huge structural lattice reorganization occurs and new 75 domain walls are formed. In particular the rhombohe-<sup>76</sup> dron lattice angle decreases by 1°, the lattice rotates by  $_{77}$  more than  $4^\circ$  and a periodic network of charged domain 78 walls is formed perpendicular to the surface plane. These 79 results, addressed by 3D reciprocal space maps and scan-<sup>80</sup> ning tunneling microscopy, point to a complex polarizaso tion texture of GeTe thin films at a/a intersections while property of  $\alpha$ -GeTe. This phase has a rhombohedral second-harmonic generation (SHG), supported by mawell above room temperature ( $T_c \sim 650 - 700$  K). The  $_{84}$  and an unchanged symmetry at the intersection regions.

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Si(111) wafers (Siltronix; 550  $\mu$ m -thick;  $\rho$ =1-10  $\Omega$ cm) 86 are first cleaned by acetone and ethanol rinsing before introduction in ultra-high vacuum (UHV,  $10^{-8}$  Pa). Then <sup>146</sup> domain variants as detailed in Ref. [27]. 87 88 the substrates are degassed at 1000 K during 12 h followed by repeated high temperature annealing (1500 K)90 during a few minutes in order to obtain a clean  $7 \times 7$  surface reconstruction. First a deposition of 1 monolayer of Sb is performed on the Si(111) surface, forming the 148 so-called Si(111)- $\sqrt{3} \times \sqrt{3}$ -Sb reconstruction that greatly is grown on Si(111)- $\sqrt{3} \times \sqrt{3}$ -Sb surface shows needle shape 95 96 97 98 99 100 101 102 103 104 a 105 106 107 108 109 110 111 112 113 114 115 <sup>110</sup> during sample transfer to the ESRF UHV chamber, a Te <sup>171</sup> lines correspond to atomic steps. The *a*-domains appear <sup>117</sup> capping was used. The capping is removed in UHV first <sup>172</sup> as needles with a grey contrast due to the tilt angle of 118 119 120 121 Second-harmonic generation (SHG) microscopy and po- 176 face morphology with a typical period of 30-50 nm along 122 123 124 125 800 nm. The sample is illuminated at normal incidence 181 claims for a change of domain walls. 126 with a time-averaged power of about 10 mW. The SHG 182 127 128 129 130 131 132 133 134 137 <sup>133</sup> analysis workflow presented in this study is implemented <sup>193</sup> by reducing the iso-intensity surface of the 3D recipro-<sup>139</sup> using Python 3. The program allows us to load and pre-<sup>194</sup> cal space map around *a*-domain Bragg peaks, we observe 140 process the SHG data cube (stack of images recorded 195 some diffuse scattering at this reciprocal space coordi-141 at different polarizer and analyzer configurations) and 196 nate [figure 2(e)]. Even more, the 3D reciprocal space

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<sup>142</sup> display the results. The K-means and Non-negative Ma-<sup>143</sup> trix Factorization (NMF) algorithms are implemented via <sup>144</sup> open-access Python packages [28] and applied to the SHG 145 polarimetry data for the automatic determination of the

#### **RESULTS AND DISCUSSION** III.

The surface morphology of a 800 nm-thick GeTe film improves the crystalline quality of the GeTe film [23]. 150 structures [figure 1(a)] crossing the surface over several The GeTe thin films are grown by co-deposition of Ge  $_{151}$  microns in the  $\langle 1\overline{10} \rangle_c$  directions. These needles are a few (1175 °C) and Te (310 °C) in UHV on a sample main- 152 hundreds of nanometer wide and show a slightly tilted tained at 275°C. In these conditions the flux ratio be- 153 surface plane with respect to the main surface. These tween Ge: Te is fixed at 2:5 in order to compensate for the 154 needles point out the presence of ferroelectric a-domains high desorption rate of Te [25]. All the deposition sources 155 whereas the flat layer is made of the c-domain [24]. The are effusion cells from MBE-Komponenten Gmbh. After 156 corresponding 3D reciprocal space map around the symgrowth, the samples are transferred under UHV condi- 157 metric Bragg peak of GeTe, perpendicular to the surface tions thanks to a homemade transfer suitcase and char- 150 plane, shows indeed four contributions [see figure 1(d)]. acterized by scanning tunneling microscopy (STM) with 150 The main one labeled  $222_c$ , at low  $q_z$ , is due to the ma-VT-STM (Scienta Omicron Gmbh). STM images were 100 jority c-domain with a rhombohedron axis of the unit cell obtained at room temperature in constant current mode 161 normal to the surface. The three other Bragg peaks  $22\overline{2}_c$ , with typical imaging conditions (U=-1 V, I= 20 pA, W  $_{102}$   $2\overline{2}2_c$  and  $\overline{2}22_c$  at higher  $q_z$  and slightly off the specular tip). The internal structure of thick GeTe films (>40 nm) 103 rod by 1.4°, are due to three a-domains variants with has been studied by x-ray diffraction at BM32 beamline  $_{104}$  axes of the rhombohedron unit cell tilted by  $\sim 71^{\circ}$  with (ESRF). X-ray diffraction data have been measured at 18 105 respect to the normal to the surface. As can be seen on keV [ $\lambda$ =0.06888 nm] with a beam size of 200 × 300  $\mu$ m<sup>2</sup> 166 figure 1(a), the density of *a*-domains in thick GeTe films and collected onto a 2D detector. The data have been 107 is such that crossing of a-domains frequently occurs. Figconverted from the detector coordinates (pixel index) to 100 ure 1(b) shows a close view of the GeTe surface by STM. diffraction angles and then to reciprocal space coordi- 109 The derivative of the surface morphology highlights spenates. To protect the GeTe surface from contamination 170 cific surface structures [figure 1(c)]. The thinnest dark by a mild Ar ion bombardment at room temperature (1 173 the surface plane. Their typical width is 100-200 nm. keV, 10  $\mu$ A) to remove the top most oxidized layers then 174 In this region all three variants of a-domains exist and by annealing at 220 °C to desorb the complete Te layer. 175 when two a-domains intersect they form a staircase surlarimetry measurements are conducted in an inverted op- 177 the  $\langle 1\overline{10} \rangle_c$  direction [see figures 1(b)-(c)]. The morpholtical microscope. The fundamental wave is provided by 178 ogy of the intersection is translation-invariant along the a laser source emitting pulses of 100 fs duration at a rep- 179  $\langle 11\bar{2} \rangle_c$  direction, i.e. along the bisector of the intersectetition rate of 80 MHz, centered at a wavelength  $\lambda = 100$  ing a-domains. This local change of surface morphology

To address these changes we have characterized the images are obtained by scanning the sample with respect 183 surface topography by STM in combination with 3D reto the focused laser beam (objective  $\times 60$ , 0.85 numeri- 184 ciprocal space map analysis. The height profile of the cal aperture) using computer-controlled stepping motors. 185 intersecting area along the translation-invariant 211 The output intensity is spectrally filtered and collected  $_{186}$  direction shows a small angle of  $0.8^{\circ} \pm 0.1^{\circ}$  of the surface into a photomultiplier. Polarimetry measurements are 187 plane with respect to the flat c-domain [figure 2(b)]. This performed by recording the SHG images at different po- 100 angle corresponds to the angle of the intersecting line of larizer and analyzer angles ( $\phi$  and  $\alpha$ , respectively) [26]. 189 two tilted surface planes of two a-domains with respect to The automatic polarimetry data analysis is supported by 100 the c-domain surface  $(1.4^\circ \times \cos (60^\circ) = 0.7^\circ)$ . In recipromachine learning methods [27] for fast and efficient de- 191 cal space such a tilted surface should give a contribution tection of the nanostrip domain crossing regions. The 102 in-between the Bragg peaks of two a-domains. Indeed



FIG. 1. (a) STM image of a 800 nm-thick GeTe thin film grown on Si(111)- $\sqrt{3} \times \sqrt{3}$ -Sb (U=-1 V, I=20 pA). The arrows show needle-shape a-type domains at the surface. The colors indicates the three variants of a-domains. (b) Close view of three domains crossing showing the staircase morphology (black arrows). (c) Derivative of STM image (b) to highlight the morphological slopes at the surface corresponding to a-domains surface and a/a crossings. (d) 3D reciprocal space map of  $222_c$ ,  $22\overline{2}_c$   $2\overline{2}2_c$  and  $\overline{2}22_c$  GeTe Bragg peaks.  $q_x$ ,  $q_y$  and  $q_z$  are the reciprocal space coordinates that are aligned respectively along  $[\overline{110}]_c$ ,  $[\overline{112}]_c$  and  $[111]_c$  directions. The main peak at  $(0, 0, 35.40 \text{ nm}^{-1})$  coordinate arises from the major c-domain (rhombohedron axis perpendicular to surface) and the three other Bragg peaks, at higher  $q_z$  [(0, -0.96, 36.73 nm<sup>-1</sup>), (-0.80,  $0.46, 36.72 \text{ nm}^{-1}$ ) and  $(0.70, 0.50, 36.71 \text{ nm}^{-1})$ ], result from the three a-domains with rhombohedron axis nearly in-plane. The surface planes of the *a*-domains are tilted by  $1.4^{\circ}$  with respect to the Si(111) surface.

199 200 201 202 203 204 205 should give x-ray diffuse scattering contributions along 222 scattering tails. 206 the connecting arc [figure 2(c)]. Let us note that the 207 <sup>223</sup> The volution of the lattice <sup>224</sup> map passing through two Bragg peaks of *a*-type domains <sup>225</sup> using a lower iso-intensity value brings additional inforprovide a local characterization with a few measured tilt 211

197 map shows an arc of diffuse scattering that connects each 213 complete, let us not that figure 2(e) shows also diffuse Bragg peak of a-domains. This signal suggests a strong 24 scattering rods connecting a- and c-domains Bragg peaks. interaction between intersecting a-domains that can be 215 As shown by Croes et al. [24] this diffuse scattering origiassigned to a lattice relaxation process. In particular the  $_{210}$  nates from the facetted interface associated with a/c dodiffuse scattering arc suggests not only a mean lattice ro- 217 main walls (71°-type domain wall). The domain walls tation towards the  $\langle \overline{112} \rangle_c$  direction by  $\beta = 0.8^{\circ}$  but also 218 generate diffuse scattering rods, called crystal truncation towards the  $\langle \overline{1}10 \rangle_c$  direction [angle  $\alpha$ , see figures 2(d)- <sup>219</sup> rods for surfaces, starting on each Bragg peaks of the (e)]. Indeed the STM height profile of the staircase mor- 220 corresponding a- and c-domains and extending perpenphology shows large slope variations of the surface that 221 dicular to the domain wall, forming the measured diffuse

223 The vertical cross-section of the 3D reciprocal space relaxations at domain intersections whereas STM images 226 mation on the crossings [see figure 3(a)]. It shows that <sup>227</sup> the diffuse scattering arc is not simply connecting the two angles corresponding to a local relaxation state. To be  $\frac{227}{228}$  Bragg reflections. It is in fact composed of two diffuse



FIG. 2. (a) STM image of an intersection area of two a-domains. (b) Line profile along the  $[\overline{2}11]_{c}$  direction [along red dashed line in (a)] showing a slight tilt angle of the edge. (c) Line profile along the  $\left[0\overline{1}1\right]_{c}$  direction [along dark dashed line in (a)] showing a staircase morphology of the surface. (d) Schematic view of the GeTe film, c- and a-type ferroelastic domains as well as a a/a intersection. The rhombohedron unit cell is given in the c-domain and in a a-domain. The two a-domains extend as stripes elongated along  $\begin{bmatrix} 10\overline{1} \end{bmatrix}_c$  and  $\begin{bmatrix} 1\overline{1}0 \end{bmatrix}_c$  directions. Their crossing forms a staircase morphology (black lines) along  $\begin{bmatrix} 01\overline{1} \end{bmatrix}_c$ that is translation invariant along  $\left[2\overline{11}\right]_c$  direction.  $\alpha$  represents the tilt angle of the surface with respect to  $[111]_c$  and oriented in  $[01\overline{1}]_c$  direction.  $\beta$  represents the tilt angle of the surface with respect to  $[111]_c$  and oriented in  $[2\overline{11}]_c$  direction. (e) 3D reciprocal space maps around  $222_c$ ,  $22\overline{2}_c$   $2\overline{2}_c$  and  $\overline{2}22_c$  GeTe Bragg peaks: the x-ray scattered intensity arising from the intersections is expected to be in-between 2 Bragg peaks. The corresponding diffuse scattering is tilted by an angle  $\beta$  with respect to the c-axis in the  $\left|\overline{112}\right|_c$  direction and the staircase morphology generates a diffuse arc tilted by an angle  $\alpha$  in the  $[\overline{1}10]_{c}$  direction.

230 231 continuing even further away forming an arc of a cir- 248 face reconstructions with large unit cells designed as row 232 233 234 235 236 237 239 240 241 242 24 3 244

229 tails that start at each Bragg peak and extend towards 246 structure [figure 3(b)]. As shown by Croes and coworkers the neighboring Bragg peak, passing slightly above and 247 [29], the surface termination of a-domains displays surcle (green and blue dashed lines). This surprising result 249 and scale structures. One can observe in the intersection shows that huge rotations of the GeTe lattice occur in 250 area that the slope change of the staircase morphology the intersection zone. As the diffuse tail from one Bragg 251 is associated with a change of orientation of the surface peak extends to the neighboring Bragg peak (and vice- 252 reconstruction. If we associate the surface reconstruction versa), then we can say that the surface planes of two 253 with each a-domain we observe that the surface normal of intersecting a-domains rotate so much that they appear 254 a a-domain alone (without intersection) is tilted by  $\alpha =$ to exchange their surface tilt angles in the crossing area. 255  $1.1^{\circ}$  in the  $[01\overline{1}]_{c}$  direction as expected from mechanical As this diffuse scattering is measured even further away  $_{256}$  compatibility with the c-domain  $[-1.2^{\circ}=-1.4^{\circ}\times\cos(30^{\circ})]$ from the neighboring Bragg peak, this indicates that the  $_{257}$  whereas it is tilted by  $\alpha = +3.2^{\circ}, +2.0^{\circ}$  and  $+2.7^{\circ}$  in the surface angle of one a-domain can be more tilted than the  $_{258}$  a/a intersection area. Similarly the other a-domain is neighboring a-domain (away from the intersection area). 259 tilted by  $\alpha = +1.1^{\circ}$  in the  $[01\overline{1}]_c$  direction as expected This x-ray diffraction result is corroborated by high res- 260 from mechanical compatibility with the c-domain but olution STM images. A close view of the intersecting 261 tilted by -0.5° in the intersection area. In figure 3(c) are 245 area of two a-domains shows the details of the surface 262 schematically shown the expected positions of the x-ray



FIG. 3. (a) Cross-section of the 3D reciprocal space map passing through the Bragg peaks of two *a*-domains. Evidence of two crossing diffuse tails are highlighted by dashed lines. (b) Close STM view of the surface reconstruction of intersecting domains (inset: large view of the surface and corresponding imaged area). The dashed lines separate the areas with specific surface reconstructions and thus identify different *a*domain type. The indicated surface angles along  $[01\overline{1}]_c$  direction are indicated in blue or green depending on the *a*-domain [values extracted from the height profile of figure 2(c)]. (c) 3D reciprocal space maps and schematic representation of the corresponding expected x-ray scattered intensity from typical measured surface tilt angles by STM.

<sup>263</sup> scattering signal on the 3D-reciprocal space map assum-<sup>264</sup> ing similar lattice rotations. They perfectly fit on the <sup>265</sup> diffuse scattering arc.

To interpret this result let us study the mechanical 266 compatibility conditions of two intersecting *a*-domains. 267 At first, i.e. away from a/a intersection, both *a*-domains 268 <sup>269</sup> form 71°-type domain walls with the majority c-domain [24]. Assuming that the *c*-domain keeps a planar in-270 terface with the Si(111) substrate then the  $(111)_c$  sur-271 face planes of *a*-domains are expected to be tilted by 272  $1.39^{\circ}$  as deduced from the rhombohedral angle (58.3°) 273 of GeTe and mechanical compatibility conditions at 71°-274 type domain walls. This is indeed confirmed by STM 275 observations and x-ray diffraction ( $\sim 1.4^{\circ}$ ). The theo-276 retical  $1.39^{\circ}$  tilt angle [24] can be decomposed in a ro-277 tation of the lattice  $(2.08^{\circ})$  and a pure shear compo-278 nent  $(-0.69^{\circ})$ . This geometrical result is schematically 279 illustrated in figures 4-(a)-(b) showing the tilt angles of 280  $(111)_c$  surface planes of two *a*-domains with rhombohe-281 dron axes along  $[11\overline{1}]_c$  and  $[\overline{1}11]_c$  (the coordinates refer 282 to the *c*-domains pseudo-cube). However in the intersection area, a staircase morphology is observed. This indi-284 cates a local rearrangement of polarization and the exis-285 <sup>286</sup> tence of additional domain patterns separated by domain walls. From the symmetry properties of rhombohedral 287 288 GeTe and translation-invariance of the staircase morphol-289 ogy along  $\langle 11\overline{2} \rangle_c$  we can estimate that a/a domain walls



FIG. 4. (a) Schematic representation of two intersecting adomains. Considering pseudo-cubic unit cells, the  $(111)_c$  surface planes and the  $(101)_c$  domain wall planes are represented with their rotations (without intersection). The  $(111)_c$  surface plane of a-domains is expected to be tilted by  $2.08^{\circ}$ - $0.69^{\circ} = 1.39^{\circ}$  with respect to Si(111) surface (2.08° from lattice rotation and  $-0.69^{\circ}$  from shear). The  $(101)_c$  domain wall plane of a-domains is expected to be tilted by  $1.80^{\circ}+0.60^{\circ}=2.40^{\circ}$ with respect to  $Si(\overline{1}01)_c$  plane  $(1.80^\circ \text{ from lattice rotation})$ and  $+0.60^{\circ}$  from shear. (b) Same as (a) but representing the pseudo-cubic unit cells for two a-domains elongated along  $[\overline{1}11]_c$  and  $[11\overline{1}]_c$ . The filled areas (blue and green) represent the  $(111)_c$  surface plane that tilts due to the stretching of the rhombohedron. (c) Same as (b) but considering the tilt of the  $(\overline{1}01)_c$  plane corresponding to the domain wall generated by the a/a intersection.

<sup>290</sup> are  $(\overline{1}01)_c$  crystallographic planes forming 109°-type do-<sup>291</sup> main wall that are perpendicular to the  $(111)_c$  surface <sup>292</sup> plane. Such domain walls necessitate a reorganization of the crystal lattice to minimize the interfacial strain field 293 at a/a crossing. In particular one can quantify the neces-294 sary rotation to ensure mechanical compatibility at such 295 an interface. Figure 4-(c) shows a schematic representa-296 tion of the tilt angles of  $(\overline{1}01)_c$  crystallographic plane of 297 two *a*-domains with rhombohedron axes along  $[111]_c$  and 298  $[\overline{111}]_c$ . In absence of intersection, the  $(\overline{101})_c$  crystallo-299 graphic planes of two *a*-domains are tilted with respect 300 to the  $[\overline{121}]$  axis in opposed directions by  $+2.4^{\circ}$  and  $-2.4^{\circ}$ 301  $[1.8^{\circ} \text{ arises from the rotation imposed by the } a/c \text{ mechan-}$ 302 ical compatibility and  $+0.60^{\circ}$  from pure shear, see figure 303 4-(a)]. To force the two crystal lattices to mechanically 304 match in the same  $(\overline{1}01)_c$  plane, a rotation of the crys-305 tals towards each other by  $2.4 \times 2 = 4.8^{\circ}$  is necessary. In 306 this circumstance either both domains rotate simultane-307 ously or alternatively. STM image of figure 3(b) shows 308 that both domains rotate alternatively and form a stair-309 case surface morphology. The smallest domain (width) 310 at the intersection undergoes the largest rotation. For 311 instance, outside the intersection area, the surface plane 31 2 313 of the smallest a-domain in figure 3(b) is tilted by  $\alpha = _{314}$  1.1° and in the intersecting area, it can rotate around 315 the  $[\overline{1}2\overline{1}]_c$  axis by +4.3° to reach  $\alpha = +3.2^\circ$  at maximum. The largest a-domain rotates less (-1.6°), from  $\alpha = +1.1^{\circ}$ 316 317 outside the intersecting area to  $\alpha = -0.5^{\circ}$  inside. From these measurements we observe that the rotations of the 318 a-domains in the intersection areas are extremely large but not enough to achieve a complete lattice relaxation 320 at the domain wall  $(4.8^{\circ})$ . This points to a residual stress due to the additional mechanical contributions related to 322 the interface with the *c*-domains and to the epitaxy with 323 the Si substrate. In addition let us note that the observed 324 rotation of the lattices to adjust the  $(\overline{1}01)_c$  domain wall of 325 two intersecting *a*-domains should not occur only around 326 the  $[\overline{1}2\overline{1}]_c$  axis. The  $(\overline{1}01)$  plane is also expected to rotate 327 by  $0.85^{\circ}$  around the surface normal in opposed directions 328 for both *a*-domains to be mechanically compatible. This 329 rotation is however much smaller than around the  $[121]_c$ 330 axis and the generated mechanical stress does not induce 331 a deep restructuring of the lattices. 332

Apart from the lattice rotation a close inspection of the 333 reciprocal space coordinates of the diffuse x-ray scatter-334 ing tails around the Bragg peaks of *a*-domains show that 335 the intereticular distances are also modified at the inter-336 sections. To quantify the induced structural changes we 337 have measured 3D reciprocal space maps around different 338 339 340  $_{344}$  to the normal to the surface. It probes the interesticular  $_{353}$  signed to a rotation of the lattice around  $\overline{[112]}_c$  direction  $_{345}$  distance along the rhombohedron axis of one variant of  $a_{-354}$  as for the  $222_c$  diffuse tail. In figures 5(b)-(ii) and (c)- $_{346}$  domain. As for a-domains Bragg peaks around the  $222_c$ ,  $_{355}$  (ii) are represented the evolution of the modulus of the



FIG. 5. (a) Complete 3D reciprocal space maps around  $\overline{2}22_c$ and  $222_c$  Bragg peaks (*c*-domains is selected as the reference domain for reciprocal space coordinates). (b)-(i) Close view of the 3D reciprocal space map around  $\overline{2}22_c$ . The dashed line illustrates the position of the diffuse tail starting from the a-domain Bragg peak. (b)-(ii) Evolution of the modulus of the scattering vector along the diffuse tail as function of the rotation angle  $\alpha$ . (c) Same as (b) for the 222<sub>c</sub> Bragg peak. (d) Plot of the rhombohedron lattice parameter at the intersection as function of rotation angle  $\alpha$ . (e) Plot of the rhombohedron angle at the intersection as function of rotation angle  $\alpha$ .

Bragg peaks. In figure 5(a) is shown a 3D map of GeTe 348 flection shows diffuse scattering tails that can be assigned thin film including the  $222_c$  Bragg peak and also the non- 349 to lattice relaxations. In particular a diffuse tail starting symmetric  $\overline{2}22_c$  Bragg peak (considering as reference for  $_{350}$  from the Bragg peak of the *a*-domain that is stretched reciprocal space coordinates the c-domains). The  $\overline{2}22_c$   $_{351}$  along the probed axis, i.e. the rhombohedron axis, ex-Bragg peak is angularly distant by  $\sim 71^{\circ}$  with respect  $_{352}$  tends far away [see figure 5(b)-(i)]. This tail can be as- $_{347}$  the Bragg peaks of the *a*-domains around  $\overline{2}22_c$  Bragg re-  $_{356}$  scattering vectors as function of the lattice rotation angle 358 Bragg peaks. For the 222<sub>c</sub> diffuse tail, the modulus of the 416 two a-domains forming the intersection. The intersection 359 scattering vector increases from 36.6 nm<sup>-1</sup> and reaches 417 of strip domains can result in either uninterrupted or in-360 a maximum at 37.2 nm<sup>-1</sup> (+1.6%) for  $\alpha \sim 2^{\circ}$  and then 418 terrupted stripes, or a rearrangement of one of the inter-361 362 363 364 365 366 367 368 369 370 371 not detect a change of symmetry and the rhombohedral 430 sections are rhombohedral. 372 structure appears to be present even in the intersection 431 373 374 375  $_{376}$   $a_R = 0.430$  nm and angle  $\theta_R = 58.2^{\circ}$ . In the intersection  $_{434}$  the polarization state of the c-domain and of two needle 377 378 379 380 structural modification is expected to result in a large 438 the *a*-domains is expected to be along  $[11\overline{1}]_c$  and  $[111]_c$ . change of ferroelectric polarization of the material. 381

382 383 local symmetry at the strip-domain (staircase) intersec-384 385 386 intersection regions are first detected using the K-means 387 method applied to the SHG images recorded at differ-388 ent polarizer and analyzer angle settings, following the 389 method reported in [27 and 30] and in the supplementary 390 materials [22]. While the K-means clustering method al-391 lows the determination of the domain variants and infers 392 the position of their intersections, it restricts the assign-393 ment of the data points to only one cluster. To disen-394 tangle the mixed signals from the main c-domain (back-395 ground) and the three different a-domains (nanostrips) 396 in GeTe, especially at the a-domain intersections, we use 397 the Non-Negative Matrix Factorization (NMF) algorithm 398 399 400 401 the laser in nonlinear optical microscopy, the SHG study 402 contains a rather limited number of data points. To in-403 crease the accuracy of the data analysis, we trained the 404 machine learning models on a larger data set, including <sup>461</sup> 405 the data reported in [24 and 27] (see supplementary ma-406 terials for details in [22]). Figure 6 summarizes the dif- 462 407 410 411 412 413 sponding to the contributions from the c-domain (black - 408 the energy cost of these intersections, a complex struc-414 background) and the 3 a-domains variants (RGB colors). 400 tural reorganization occurs as demonstrated by 3D re-

 $_{357} \alpha$  following the diffuse scattering tails for  $222_c$  and  $\overline{2}22_c$  415 All detected crossing regions contain the signatures of the decreases at larger angle. Similarly the modulus of the 410 secting strip domains (e.g., splitting into two parts after scattering vector of the  $\overline{2}22_c$  diffuse tail decreases from 420 crossing another a-domain). However, it is worth noting 35.3 to  $3\overline{4.9}$  nm<sup>-1</sup> (-1.1%) for  $\alpha \sim 2^{\circ}$  and then increases 421 that the interrupted configuration (one of the strip doagain at larger angle. The decrease of the modulus of 422 mains is stopped at the intersection region) is most comthe scattering vector of the  $\overline{2}22_c$  diffuse tail clearly indi- 423 monly observed and occurs systematically in thin films cates an extension of the intereticular distance along the 424 with thicknesses below 400 nm. Decomposing the data rhombohedron axis of the *a*-domain. This result is also 425 into more than four polar plots does not provide relevant corroborated by the decrease of the interesticular distance 420 polar plots (see supplementary materials and figure 8 in deduced from  $222_c$  diffuse tail position. This set of data  $_{227}$  [22]), showing that the intersections do not contain an can be combined to determine the change of structure 428 additional phase. The absence of symmetry variation in of the GeTe lattice in the intersection area. We could 429 the SHG study confirms that the a-domains at the inter-

The remaining question concerns the charge state of area. Outside the intersections, from the Bragg peak  $_{432}$  the  $(\overline{1}01)_c$  109°-type domain walls formed at these a/apositions, we obtain a rhombohedron lattice parameter 433 domain intersections. Figure 7(a) is a schematic view of area ( $\alpha \sim 2^{\circ}$ ) we obtain a slight increase of the lattice 435 shape a-domains. Since the polarization state of the cparameter  $(a_R = 0.431 - 0.432 \text{ nm})$  and a large decrease 436 domain is along  $[111]_c$ , pointing upward [18], then to have of the rhombohedron angle  $\theta_R = 57.0^{\circ}$ . Such a large 437 a neutral 71°-type domain wall, the polarization state of 439 Therefore the formation of  $(\overline{1}01)_c$  domain walls at a/aSecond-harmonic generation microscopy (SHG) with <sup>440</sup> intersections results in non-compensated charges. The polarimetry analysis is used to examine and compare the 442 alternate a-domains results in head-to-head and tail-to-443 tail polarization configurations at domain walls [figure tect a possible phase change at the intersections. The 444 7(c)]. The formation of charged domain walls in GeTe 445 thin films seems to be driven by mechanical compati-446 bility, the electrostatic part being compensated by the <sup>447</sup> available charges in the materials [31–33]. As proposed <sup>448</sup> by Dangic and co-workers [7], charged domain walls are 449 expected to be easily formed in GeTe. Indeed GeTe can 450 provide free charge carriers to locally screen the accu-<sup>451</sup> mulated charges since it is semiconducting and p-doped 452 (due to the easy formation of Ge vacancies [34]). The <sup>453</sup> positively charged carriers may compensate the accumu-454 lated charge at tail-to-tail domain walls whereas the cor-<sup>455</sup> responding Ge vacancies (negatively charged) could accu-456 mulate at head-to-head domain walls if they are enough <sup>457</sup> mobile [35]. Since screening by free charge carriers is size of the crossings (about 50 nm) and the long acquisition time due to the slow sample scanning with respect to 460 head-to-head domain walls in GeTe.

#### CONCLUSION IV.

In conclusion we have studied the *a*-domain intersecferent types of nanostrip crossings as automatically de- 403 tions in ferroelectric GeTe thin films grown on Si(111)-Sb. rived from the SHG polarimetry analysis using trained 404 Constrained by the mechanical compatibility conditions machine learning methods. Each SHG polarimetry plot 405 between a- and c-domains as well as by the epitaxy of the associated with each pixel of the GeTe film can be decom- 400 thin film with the silicon substrate, the a/a-domain inposed in four components with distinct polar plots corre- 467 tersections are a priori highly mismatched. To minimize

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FIG. 6. Local (a)-(f) different strip domain intersection types derived from SHG microscopy polarimetry analysis assisted by trained K-means (left columns) and NMF algorithms at a-domains intersections. The domain contribution maps derived with NMF are obtained by taking into account four components (domain variants) with respective fractions  $W_i$  corresponding to the polar plots presented in panel (g). The scale bar is common to all images and corresponds to 1  $\mu$ m.

470 ciprocal space maps, scanning tunneling microscopy and 477 ization texture in GeTe thin films. 471 second-harmonic generation. We demonstrate the for- 478 Acknowledgements 472 mation of new domains walls, large lattice rotations, en- 479 473 hanced stretching of the rhombohedral lattice of GeTe. 480 funding from Excellence Initiative of Aix-Marseille Uni-474 We believe that the detailed description of a/a domain 481 versity A\*MIDEX, a french "Investissements d'Avenir" 475 intersections and 109°-type domain wall will motivate 482 programme through the AMUtech Institute. This work 476 further studies for the control of the ferroelectric polar- 483 has also been supported by the ANR grant FETh (ANR-

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FIG. 7. (a) Model of the surface morphology and polarization states of *a*-domains and *c*-domain. (b) STM image of the surface topography of an intersecting area of two *a*-domains. The arrows show the in-plane components of the polarization direction at different places. (c) Corresponding schematic representation of the staircase morphology indicating the presence of charged domain walls.

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