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WEAK FORM-BASED OBJECTIVE FUNCTIONS IN HYDROLOGY APPLICATION TO A 1D TRANSPORT/DEGRADATION MODEL



Context and Objective Weak form-based objective functions (WOF) can be a good alternative to the classical distance-based functions (DOF) for model calibration [1]. WOF are monotone with respect to a given parameter when – The calibration problem is changed from an optimization problem into a root finding problem contaminant concentration: C– WOF are less prone to local extrema (when one parameter is to be calibrated, they have a single opdegradation coefficient: k– When several parameters are calibrated, their redundancy can be assessed by superimposing the flow velocity: u=QThe objective is to apply WOF to the calibration of the degradation coefficient (k(t) depending on Application Calibration process Requires observations / measurements $C(x,0) = C_0$ - The primary variable C(x,t) cannot be measured easily $u(x,t) = u_{\mathrm{in}}$ - Use of a secondary variable: C(L,t) at the outlet $C(0,t) = C_{\rm in}$ Model output «as close as possible» to the data k(t) = K– Classical measures of closeness (DOF): $D_p = \sum |e|^p$ Calibration of 3 $k_{\rm m}$: – Weak form-based (monotone wrt k): $W_p = \sum e|e|^p$ $k(t) = \sum k_n \epsilon_n$ Model error: $e = (C_{\rm sim} - C_{\rm obs})$ C(x, 0) = 0.1 g/l $u(x,t) = 25 \pm 10\%$ (m/day) ∂k_n $k_n = \{0.02; 0.05; 0.06; 0.04\}$ W_{p} $_{n}C(x,t)$ $C_{\rm out} (g/l)$ 0.11 k optimal 0.02 *HydroSciences Montpellier UMR 5569

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the sensitivity of the model output keeps a constant sign; then:

- timum)
- contour lines of different WOF.

time) of a 1D pollutant transport/degradation model.



Calibration of 1 parameter k_{m} with WOF:

– Choose a value for p and solve $W_{p}(k_{p})$ =0 using e.g. Newton's algorithm :

$$k_{i+1}=k_i-rac{W_p}{W_p'}$$
 with $W_p'=p|e|^{p-1}\chi_n$ and $\chi_n=$

With χ_n obtained by solving the sensitivity equation:

$$\frac{\partial \chi_n(x,t)}{\partial t} + u(x,t)\frac{\partial \chi_n(x,t)}{\partial x} = -k(t)\chi_n(x,t) - \epsilon_n$$

Calibration of n parameters k_n with WOF

- Find the intersection of n WOF with n values for p.











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