

# Deriving cool flame propagation speeds by means of an ozone-seeded, stagnation plate burner configuration

Thomas Panaget, Pierre Bragança, Bertrand Lecordier, Amaury Lahccen, Christophe Cuvier, Sébastien Batut, Yann Fenard, Guillaume Vanhove, Laure Pillier

## ► To cite this version:

Thomas Panaget, Pierre Bragança, Bertrand Lecordier, Amaury Lahccen, Christophe Cuvier, et al.. Deriving cool flame propagation speeds by means of an ozone-seeded, stagnation plate burner configuration. Fuel, 2024, 362, pp.130766. 10.1016/j.fuel.2023.130766 . hal-04376944

## HAL Id: hal-04376944 https://hal.science/hal-04376944

Submitted on 9 Jan 2024

**HAL** is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

# **Deriving Cool Flame Propagation Speeds by Means of an Ozone-Seeded, Stagnation Plate Burner Configuration**

### Thomas Panaget<sup>*a,b,e*</sup>, Pierre Bragança<sup>*c*</sup>, Bertrand Lecordier<sup>*d*</sup>, Amaury Lahccen<sup>*e*</sup>, Christophe Cuvier<sup>c</sup>, Sébastien Batut<sup>e</sup>, Yann Fenard<sup>e</sup>, Guillaume Vanhove<sup>e</sup> and Laure Pillier<sup>*e*,\*</sup>

<sup>a</sup> Univ. Lille, Inserm, CHU Lille, Institut Pasteur Lille, U1167 – RID-AGE – Facteurs de risque et déterminants moléculaires des maladies liées au vieillissement, F-59000 Lille, France

<sup>b</sup>Junia, Health and Environment, Laboratory of Sustainable Chemistry and Health, F-59000 Lille, France

<sup>c</sup>Univ. Lille, CNRS, ONERA, Arts et Métiers Institute of Technology, Centrale Lille, UMR 9014 - LMFL - Laboratoire de Mécanique des Fluides de Lille - Kampé de Fériet, F-59000 Lille, France

<sup>d</sup>Normandie Univ., UNIROUEN, INSA Rouen, CNRS, CORIA, 76000 Rouen, France

<sup>e</sup>Univ. Lille, CNRS, UMR 8522 - PC2A - Physicochimie des Processus de Combustion et de l'Atmosphère, F-59000 Lille, France

Full length article

#### Abstract

This study aims to investigate the feasibility of experimental determination of DME/O<sub>2</sub>/O<sub>3</sub> cool flame propagation speeds using Particle Image Velocimetry (PIV) in a stagnation plate burner operated at atmospheric pressure. A specific PIV data analysis procedure was developed in order to improve the accuracy of the measurements in this particular configuration. Five flame conditions, with equivalence ratio varying from 0.3 to 0.5 and ozone mole fraction varying from 1.5 to 2% were investigated to compare experimental results with kinetic modeling. Three ozone-submechanisms, respectively from Jian et al., 2022), Halter et al. (Halter et al., 2011) and Zhao et al. (Zhao et al., 2016), were coupled with our previously developed DME mechanism (Panaget et al., 2021) and used to compare experimental and simulated axial velocity profiles. Results show that a thoughtful choice of the ozone-submechanism is of particular importance in predicting an accurate cool flame velocity in these conditions. A numerically assisted non-linear extrapolation method is proposed for the determination of the unstrained cool flame speed  $S_{u,0}$ . Additionally, simulations for which the plate temperature reaches the maximal flame temperature (adiabatic conditions) were performed, demonstrating a negligible effect of the plate temperature on the determined Su.0. A kinetic analysis is also presented to highlight the most sensitive chemical reactions influencing the reference cool flame speed Su, ref, showing the preponderant role of the fuel low temperature chemistry.

Keywords: Cool flame, Propagation speed, Low temperature combustion, Particle Image Velocimetry, Ozone assisted combustion

- \*Corresponding author: laure.pillier@univ-lille.fr

- 47
- 48
- 49
- 50
- 51

#### 1. INTRODUCTION

From their discovery two centuries ago [1] to their recent observation under micro-gravity 54 conditions [2], cool flames raised a number of issues throughout the years [3,4]. They are known 55 56 to play a critical role in advanced combustion technologies [5] as they control both autoignition and assisted-ignition processes in the low-temperature combustion regime. Flame propagation 57 speeds are fundamental parameters in combustion due to their influence on the rate of heat 58 release within the reaction zone of flames. Cool flame speeds were numerically investigated by 59 Ju et al. [6,7] and by Zhao et al. [8]. Using dimethyl ether (DME)/O<sub>2</sub> mixtures in both freely-60 propagating and counter-flow conditions, it was reported that cool flame speeds typically range 61 from 6 to 20 cm.s<sup>-1</sup>, depending on the experimental conditions. Interestingly, they are almost 62 insensitive to the equivalence ratio within their stability range, while their hot flames 63 counterparts are known to be highly dependent on this parameter. Numerical investigations of 64 the effect of ozone on the cool flame speed have shown that it increases as the ozone 65 concentration increases, as in the case of hot flames [9,10]. 66

67 To the best of our knowledge, experimental cool flame propagation speeds were only reported under microgravity conditions [11] or at sub-atmospheric pressure by the Belmont 68 group [12–16]. Foster and Pearlman [11] measured the speed of a propane/O<sub>2</sub> cool flame at 69 70 low-pressure and microgravity conditions, using the spherically-propagating flame method. It was however observed that heat was released by pre-ignition of the mixture, prior to the cool 71 flame formation. Thus, the measurement could not be used to determine the propagation speed 72 of the propane cool flame. Recent work from Belmont group at the University of Wyoming 73 [12–16] showed the feasibility of measuring cool flame speeds using a Hencken Burner 74 75 operated at sub-atmospheric pressure. They reported low pressure data for ozone-seeded cool flames of dimethyl ether, propane and *n*-heptane. This method consists of varying the gas inlet 76 flow rate while keeping the equivalence ratio fixed, and measuring the position of the flame 77

above the burner by excited formaldehyde chemiluminescence or formaldehyde planar laser 78 induced fluorescence (PLIF). Two distinct regimes are then identified: a/ a first regime where 79 the flame remains anchored to the burner by the heat losses, and where the variation of the inlet 80 flow rate causes only a minimal variation of the flame position; b/ a second regime, where the 81 flame detaches from the burner surface and is considered freely-propagating and nearly 82 adiabatic, the heat transfer being considered negligible. In this case, the flame position varies 83 linearly with the inlet flow rate. The transition between these two regimes was suggested to 84 provide a reasonable estimate of the cool flame speed. This method was validated for hot flames 85 by comparing flame speeds measured by Particle Image Velocimetry (PIV) [16,17] and data 86 87 from the literature and simulations. The cool flame speeds obtained experimentally by Hajilou et al. were simulated with different kinetic models [13-15] using freely-propagating flame 88 simulations. 89

90 Ozone has been widely used in experimental cool flames studies [15,18] as its thermal decomposition releases highly reactive oxygen atoms at temperatures close to 450 K at the 91 92 atmospheric pressure, facilitating the initiation of low-temperature reactivity [19]. Several 93 ozone specific submechanisms have been developed in the past years, and are commonly coupled with hydrocarbon mechanisms to describe the decomposition of ozone and its impact 94 95 on combustion [20–22]. Knowing the important influence of ozone on the combustion process, it is important to wisely choose the ozone submechanism when simulating the behaviour of 96 ozone-seeded cool flames. 97

In this work, we investigated the feasibility of measuring atmospheric pressure lean DME/O<sub>2</sub>/O<sub>3</sub> cool flames propagation speeds from the measurements of the axial velocity profiles using PIV in a newly implemented stagnation plate burner [23]. A specific PIV data analysis procedure, developed in order to improve the accuracy of the measurements, is presented. Five different flames conditions have been studied with equivalence ratio varying

from 0.3 to 0.5 and  $O_3$  mole fraction from 1.5 to 2%. Comparison with simulations is performed using three different  $O_3$ -submechanims from the literature [20–22] coupled to a detailed kinetic mechanism recently developed in our group [23] for DME low temperature combustion. The performance of the coupled mechanisms is first assessed in predicting experimental axial velocity profiles in the strained cool flames, then a method to extract the unstrained propagation speed is proposed. Finally, a kinetic analysis is performed to highlight the most sensitive chemical reactions influencing the cool flame speed.

- 110
- 111

#### 2. EXPERIMENTAL AND NUMERICAL METHODS

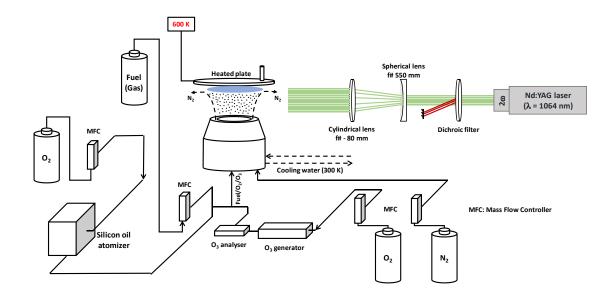
112 113

## 2.1. Experimental setup for PIV measurements

The stagnation plate burner used in the present study has already been extensively 114 115 described in a previous study [23], and will therefore only briefly be presented in the present work (Figure 1). It consists of a stainless-steel body, with a coaxial converging nozzle of an 116 117 inner diameter of 10 mm for the DME/O<sub>2</sub>/O<sub>3</sub> mixture. This mixture is injected through four orthogonal inlets and flows through a stainless-steel porous disc before entering the convergent 118 119 section of the burner. This geometry is chosen as it provides a laminar and uniform flow at the 120 burner exit. A N<sub>2</sub> co-flow exits through a 20 mm internal diameter co-axial nozzle also equipped 121 with a stainless-steel porous section to protect the cool flames from external perturbations. The burner body is kept at a constant temperature of 300 K by a temperature-regulated water 122 123 circulation system, and is operated at atmospheric pressure. A cylindrical heated plate, with a diameter of 65 mm and a thickness of 8 mm, is placed at 13 mm from the burner nozzle, with 124 a strictly parallel geometry, and is heated at  $600 \pm 0.1$  K. Gas flow rates are controlled by 125 Bronkhorst mass flow controllers, whose calibration was performed using DryCal DC-Lite 126 Primary Flow Meters. Part of the O<sub>2</sub> flows through two ozone generators (BMT Messtechnik 127 128 GMBH) arranged in parallel. The ozone mole fraction is measured at the entrance of the burner

with a Teledyne API 452 ozone analyser, the relative uncertainty on the reported ozone concentrations being  $\pm 0.02\%$  for every studied condition. The ozone mole fraction at the burner outlet has been measured both in reactive and non-reactive conditions using an Omnistar GSD 301 O<sub>2</sub> Pfeiffer Vacuum mass spectrometer, showing no ozone reactivity or decomposition before the burner outlet.

Measurements of the axial velocity profiles between the burner and the plate are 134 performed using the PIV technique which is based on the diffusion of illuminated particles 135 seeded in the flow. In our case, part of the oxygen flows through a liquid atomizer, allowing 136 137 the seeding of small particles in the flow. Silicon oil, provided by Chem-Lab, is chosen for its 138 well-defined properties (viscosity, surface tension, etc.) and its high vaporization temperature, around 600 K. In the studied conditions, the temperature does not exceed 900 K downstream 139 from the flame, and the temperature in the flame front is around 600 K [23]. The particle 140 diameter is estimated to be in the range  $1-5 \mu m$ , as usually met for this kind of atomizer [24]. 141 The flame position did not change with the addition of particles, demonstrating that the seeding 142 143 by silicon oil droplets does not affect the cool flame speed. The use of silicon oil is therefore well adapted for such PIV measurements, as will be demonstrated further later in this 144 manuscript. 145





148 **Figure 1.** Schematic diagram of the experimental setup.

Particles are illuminated by a dual cavity Nd:YAG Splitlight Compact laser from 150 Innolas, delivering a 50 mJ pulse at 532 nm, at a frequency of 10 Hz. The laser sheet, centred 151 on the burner, is generated using spherical (f# 550 mm) and cylindrical (f# - 80 mm) lenses. 152 153 The laser sheet dimensions are  $\sim 12$  mm height x 600 µm thick. The particles displacement 154 between two laser pulses is captured using a LaVision Scmos camera of 2560 by 2160 pixels, equipped with a 105 mm Nikkor lens at an aperture of f#8, the resulting magnification being 155 equal to 20  $\mu$ m per pixel. The time between two pulses ( $\Delta t$ ) was fixed to 220  $\mu$ s, in order to 156 record a 10-pixel displacement between the pulses at the lowest flow rate. A total of 1000 157 images were recorded for each condition. 158

In the vicinity of the flame, the particle concentration is estimated to 0.005 particle per pixel. Such a low concentration is caused by the difficulties of effectively seeding the flow, as the oxygen flow rate had to be split between the ozone generators and the atomizer. For conventional PIV, this very low concentration requires a minimum interrogation window size (IWS) of 32 x 32 pixels (0.64 x 0.64 mm<sup>2</sup>), which leads in our conditions to an insufficient spatial resolution for accurate measurements. To tackle this difficulty, a more advanced and adapted post-processing approach has been specifically developed at the CORIA laboratory,and is detailed below.

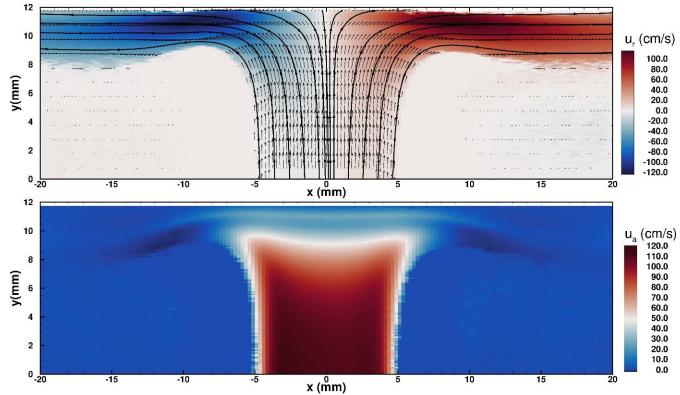
167

### 2.2. Particle Image Velocimetry (PIV) images post-processing

Before applying the PIV image processing, an advanced background correction is 168 performed from conditioned averaged images, one at t and one at t +  $\Delta t$ . A standard background 169 correction is not adapted in the case of low-densities due to the difficulty to remove the 170 171 individual particle signal on averaged images, even when 1000 images are considered. In our approach, the conditioned background images are then obtained by averaging all the 172 instantaneous images but without integrating the signal of particles in the process using a 173 174 Kuwahara filter. This specific image processing improves the estimation of background images in particular in low density regions. Following the background correction, only the particle 175 176 signal remains on the corrected images. Then, the spatial calibration is done with a well-defined target (0.977 x 0.977 mm), and is used to estimate a polynomial camera model of 3<sup>rd</sup> order used 177 178 to dewarp each image, ensuring a perfect alignment of both wall and burner axes within the (x, 179 y) frame. This step also corrects any image distortion induced by the camera lens. From this 180 step, PIV processing starts by an extraction of the particles position in the images using a 2D correlation pattern recognizing technique. Between 1500 and 3500 particles are detected on 181 182 each image, depending on the experimental conditions. The vector calculation is then initiated at the particle location, and not on a regular mesh as it is usually performed when the particles 183 density is higher. This calculation is based on an iterative continuous window shift technique 184 [25,26], starting with an interrogation window size (IWS) of 64 x 64, and reaching an IWS of 185  $8 \times 8$  pixels (0.16 x 0.16 mm<sup>2</sup>) in the final pass. This results in a series of non-regular velocity 186 187 fields which are validated with a rate higher than 85%. The scaling in the real coordinated system is realized with the burner plate as reference, with an accuracy of  $\pm 20 \,\mu\text{m}$ . The final 188 step consists in computing a mean velocity field on a regular mesh by averaging every 189

instantaneous vector in small cells at each mesh node, the cell size being compatible with the
PIV resolution of 8 x 8 pixels. This processing method allows a significant improvement in the
particle detection in the area close to the flame front. A comparison of the axial velocity profiles
determined using a conventional image processing method, i.e., with an IWS of 32 x 32 pixels,
and the present one is presented in Figure S1 of the Supplementary Material.

195 Axial velocity profiles are finally extracted from the mean velocity field by averaging 196 on a radial width of  $\pm 1$  mm around the centre of the burner. A two-dimensional velocity field in reactive conditions is shown in Figure 2. It demonstrates that the radial (u<sub>r</sub>) distribution of 197 198 the velocities is axisymmetric, and that the axial velocity (u<sub>a</sub>) profile at the burner exit is almost 199 uniform over the entire diameter of the burner (10 mm). The flat cool flame front, stabilized two millimetres under the heated plate, can be distinguished on the axial velocity profile. This 200 confirms the efficiency of the converging nozzle geometry, and constitutes further justification 201 of the averaging process over a region of  $\pm 1$  mm used in the image post-processing, as the axial 202 velocity can be considered constant over a significant portion of the burner diameter. From 203 204 Root Mean Square (RMS) analysis, the uncertainty on the determination of the axial velocity with the PIV technique is estimated to be  $\pm$  5%. This lead to an uncertainty in the flame speed 205 determination lying between 0.83 and 1.05 cm.s<sup>-1</sup>, depending on the value of the reference axial 206 velocity S<sub>u,ref</sub> (minimum velocity upstream of the flame front, as shown in Figure 3), which has 207 been averaged at  $\pm 1 \text{ cm.s}^{-1}$ . 208



**Figure 2.** Radial velocity streamlines (top) and axial velocity profile (bottom) of a DME/O<sub>2</sub>/O<sub>3</sub> cool flame at  $\phi = 0.4$  and  $x_{O3} = 1.9\%$ . u<sub>r</sub> represents the radial velocity, u<sub>a</sub> the axial velocity, y the Height Above the Burner (HAB) and x the burner radius.

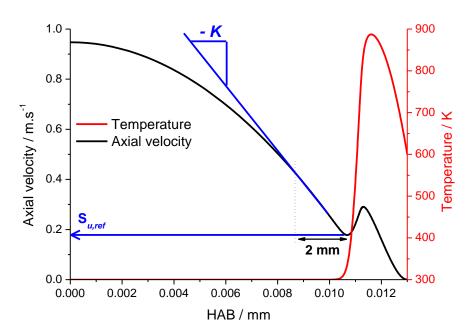


Figure 3. Simulated temperature (red) and axial velocity (black) profiles of a cool flame. Determination
 of the couple (S<sub>u,ref</sub>, K) is also shown.

#### 220 **2.3. Flame conditions**

Five stable cool flame conditions were selected for the measurement of cool flame 221 speeds, and are summarized in Table 1. Note that the inlet velocity (uin) range is limited as it is 222 constrained by the stability domain of the cool flames, which is known to be narrower than for 223 hot flames. Furthermore, at high inlet velocity (and strain rate, usually calculated as the ratio 224 between the flow velocity and the burner/plate distance), the cool flames tend to stabilize closer 225 to the stagnation plate, leading to difficulties in resolving the entire velocity profile. On the 226 contrary, at low inlet velocity, the particle seeding is not sufficient to provide accurate 227 measurement of the velocity field in the burner. 228

229

The detailed flames conditions are provided in the Supplementary Material (Table T1).

ф	x <sub>03</sub> * / %	u <sub>in</sub> / cm.s <sup>-1</sup>
0.5	1.5	65 - 80
0.45	1.7	75 – 110
).4	1.7	65 – 85
).4	1.9	75 – 110
).3	2.0	65 – 95

\*The indicated values correspond to the ozone mole fraction in the DME/O<sub>2</sub>/O<sub>3</sub> mixture

**Table 1.** Experimental conditions for the investigated  $DME/O_2/O_3$  cool flames.

232

233

## 2.4. Flame simulations

The axial velocity profiles for all flames conditions were simulated with multicomponent transport using the Pre-Mixed Burner Stagnation Flame module of Chemkin-Pro 2021 [27]. The size of the simulation domain (see Table T1 in Supplementary Material) was varied depending on the studied conditions, as detailed later. The GRAD and CURV parameters were fixed at 0.03 each, resulting in ~ 450 points per simulation, which is sufficient to ensure accurate simulations of the reference axial velocity  $S_{u,ref}$  within a 1% uncertainty, as demonstrated in the Supplementary Material (Figure S2). The Soret effect option was disabled for the axial velocity profiles simulations as it did not significantly modify the reference axial velocity and allowed a drastic reduction of the computational time. The energy equation was solved for simulation; hence the experimental temperature profile was not used as an input. The experimental and simulated temperature profiles of lean DME/O<sub>2</sub>/O<sub>3</sub> cool flames were compared in our previous study [23] and showed an excellent agreement.

A detailed kinetic mechanism recently developed in our group [23] has been used, it is 246 based on the AramcoMech1.3 mechanism [28] with reassessed reaction pathways and modified 247 248 Arrhenius parameters. It was validated on the prediction of the mole fraction profiles of intermediates species above the burner for DME/O<sub>2</sub>/O<sub>3</sub> cool flames. Three different O<sub>3</sub>-249 submechanims from the literature, respectively from Jian et al. [20], Zhao et al. [21] and Halter 250 et al. [22], were coupled to the aforementioned mechanism [23]. A summary of the different 251 reactions and their associated modified Arrhenius reaction rate coefficients is given in the Table 252 253 T2 of the Supplementary Material. Note that these three O<sub>3</sub>-submechanisms have been very 254 recently [20] compared to experimental data on  $O_3$  decomposition,  $O_3/O_2$  flame speeds and  $H_2/O_2/O_3$  reaction in a flow reactor, showing satisfactory predictions in these experimental 255 256 conditions.

257

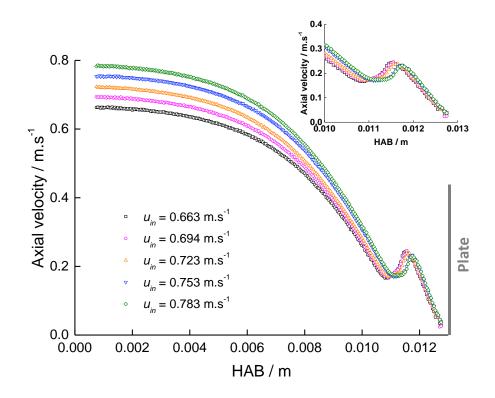
#### 258

259 260

### 3. RESULTS AND DISCUSSION

**3.1. Axial velocity profiles** 

The axial velocity profile measured for the strained cool flame at  $\phi = 0.5$ ,  $x_{O3} = 1.5\%$  is pictured for five different inlet velocities  $u_{in}$  (and strain rates) as an example of the obtained results in Figure 4. The increase of velocity upstream of the flame front due to thermal expansion is less pronounced than in hot flame cases since the heat release of cool flames is significantly lower. The entire velocity profile is well defined in each condition supporting the use of silicon oil droplets and the applied PIV image processing. As the inlet velocity (and strain rate) increases, the flame moves towards the stagnation plate and the acceleration observed in the flame front is reduced in accordance with a decrease of the maximum flame temperature.



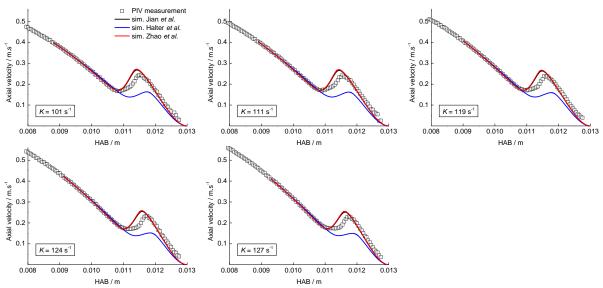
269

**Figure 4**. Axial velocity profiles as a function of the Height Above the Burner (HAB) of a DME/O<sub>2</sub>/O<sub>3</sub> cool flame at  $\phi = 0.5$ ,  $x_{O3} = 1.5\%$ , for five different inlet velocities  $u_{in}$ .

The measured axial velocity profiles in the strained cool flames were compared with 273 simulations performed with the Pre-Mixed Burner Stagnation Flame module of Chemkin-Pro, 274 following the methodology proposed in [29–31]. It consists in imposing the exact boundary 275 conditions inferred from the PIV experiments, as it is recognized that the experimental flow 276 277 field in stagnation plate burner configuration is usually neither a plug flow nor a potential flow [32] and that 1D approaches typically fail in providing accurate prediction of the corresponding 278 velocity profile [33]. In this work, the inlet position of the simulation domain was fixed two 279 280 millimetres before the minimum velocity upstream of the flame front position (defined as Su,ref).

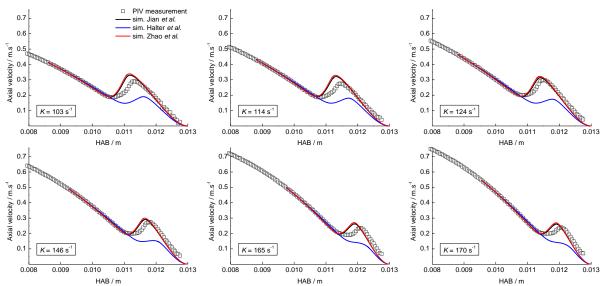
Experimental strain rates K and inlet velocities were inferred from the axial velocity profile 2 281 282 mm upstream from S<sub>u.ref</sub>, as pictured in Figure 3. The effect of the domain size on the accuracy of the velocity profile, targeting both the reference velocity S<sub>u,ref</sub> and its position above the 283 burner, was studied and the results are pictured in Figures S3 and S4 of the Supplementary 284 Material. Results showed that the simulated S<sub>u,ref</sub> were similar within 1% for domain sizes 285 below 8 mm, but that selecting a too small domain size, here less than 3.2 mm, led to a greater 286 deviation. The computational domain length therefore lies between 3.05 and 4.45 mm, 287 depending on the flame conditions. To ensure reproducible determination of the experimental 288 K, the experimental axial velocity profile was fitted using a 2<sup>nd</sup>-order polynomial function 289 beforehand. 290

The axial velocity profiles simulated using the three aforementioned ozone-291 submechanisms [20-22] were compared to the experimental ones. Two flame conditions at 292  $\phi = 0.5$ ,  $x_{O3} = 1.5\%$  and  $\phi = 0.3$ ,  $x_{O3} = 2.0\%$  are presented in Figure 5 and Figure 6 respectively. 293 294 For the sake of brevity, the same comparisons for other flame conditions are presented in Figures S5 to S7 in the Supplementary Material, and the exact boundary conditions used for the 295 simulation are given in the Table T1 of the Supplementary Material. Comparing the three 296 297 different O<sub>3</sub>-submechanims, large variations in the prediction of the velocity profile can be observed between the Halter et al. model and the two other models, with an important 298 299 underprediction of the minimum velocity S<sub>u,ref</sub> for the Halter et al. model. It should be noted that in the case  $\phi = 0.3$ ,  $x_{03} = 2\%$  (Figure 6), the Halter et al. model predicts almost no minimum 300 301 velocity for higher strain rates, but only an inflection of the axial velocity curve upstream of the flame front. The predictions from the Jian et al. and Zhao et al. models are comparable, as both 302 models accurately describe the overall velocity profile. 303



**Figure 5.** Comparison between experimental axial velocity profiles measured by PIV ( $\Box$ ) and simulated

- 306 ones with different O<sub>3</sub>-submechanisms, respectively from Jian et al., Halter et al. and Zhao et al., for the
- 307 cool flame at  $\phi = 0.5$ ,  $x_{O3} = 1.5\%$ , at different strain rates.



**Figure 6**. Comparison between experimental axial velocity profiles measured by PIV ( $\Box$ ) and simulated ones with different O<sub>3</sub>-submechanisms, respectively from Jian et al., Halter et al. and Zhao et al., for the cool flame at  $\phi = 0.3$ ,  $x_{O3} = 2.0\%$ , at different strain rates.

312

In order to evaluate the capabilities of these models to predict cool flame speeds, the Root-Mean-Square Error (RMSE) between experimental and simulated  $S_{u,ref}$  was calculated over the investigated strain rate range, for the five flames conditions. The RMSE data are summed up in the Table 2, for each  $O_3$ -submechanism. One can see that the Halter et al. submechanism constantly underestimates the value of  $S_{u,ref}$ , while the two other models yield similar performance.

	Root-Mean-Square Error (RMSE)		
Condition	Jian et al.	Halter et al.	Zhao et al.
$\phi = 0.3, x_{O3} = 2.0\%$	0.5	4.7	0.5
$\phi = 0.4, x_{O3} = 1.9\%$	1.2	5.9	0.7
$\phi = 0.4, x_{O3} = 1.7\%$	0.2	3.8	0.3
$\phi = 0.45, x_{O3} = 1.7\%$	0.2	4.5	0.4
$\phi = 0.5,  x_{O3} = 1.5\%$	0.2	3.1	0.2

Table 2. Root Mean-Square Error (RMSE) calculated for each flame condition with the different O<sub>3</sub> submechanisms

321

A possible explanation for the constant underestimation of the flame speed by the model of 322 Halter et al. is the definition of the ozone decomposition within the model, where only N<sub>2</sub>, O<sub>2</sub> 323 and  $O_3$  are declared as collision partners in the  $O_3 + M \Leftrightarrow O_2 + \ddot{O} + M$  reaction, in contrast with 324 the other two mechanisms (for which all species are considered with a collision efficiency of 1, 325 except if specified). In our experimental conditions, the fuel mole fraction lies between 10 and 326 15% of the mixture. The absence of DME as a third-body in the ozone decomposition reaction 327 328 can therefore lead to a lowered reactivity of the Halter et al. model (see Table T2 in the Supplementary Material). This aspect has been tested by replacing the O<sub>3</sub>+M decomposition 329 reactions of the model of Jian et al. by the O<sub>3</sub>+M reactions of Halter et al., showing a 330 331 deterioration in the prediction of the axial velocity profile, as seen in Figure S8 in the Supplementary Material. 332

For the following sections, the Jian et al. submechanism will be used solely, because of its more recent rate constants data and its good performance in predicting  $S_{u,ref}$ .

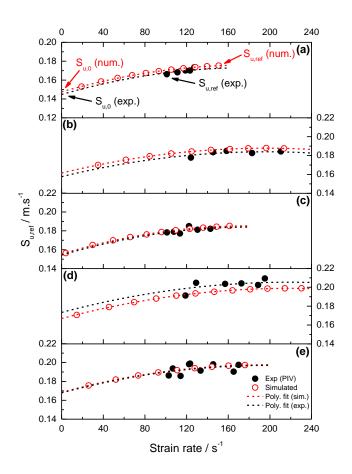
### **3.2.** Determination of the unstrained cool flame speed S<sub>u,0</sub>

A well-established method [34] has been widely used to derive the unstrained flame speed  $S_{u,0}$  of hot flames. It consists of measuring the axial velocity profiles for different strain rates (K) and determining the reference velocity ( $S_{u,ref}$ ) as represented in Figure 3. From the plot of  $S_{u,ref} = f(K)$ , the extrapolation to strain rate K = 0 returns the unstrained laminar flame speed  $S_{u,0}$ .

Both linear [35] and non-linear [36] extrapolation methods have been used in the past. 341 Vagelopoulos et al. [34] and Chong and Hochgreb [37] have demonstrated that for low-strain 342 rate hot flames (50 - 250 s<sup>-1</sup>), the linear extrapolation method yields accurate results within a 343 reported uncertainty of ~ 1-2 cm.s<sup>-1</sup>. In the case of cool flames, for which the speed is 344 significantly smaller, this added uncertainty might however be problematic. The issue of non-345 linear extrapolation was revisited by Egolfopoulos et al. [38-41] with a computational 346 approach, where the simulated S<sub>u,ref</sub> at various K (using a counter-flow flame code) and the 347 simulated  $S_{u,0}$  at K = 0 (using the freely propagating flame module of the PREMIX code) are 348 349 fitted using a polynomial function. This computed curve is vertically translated to best fit the experimental data and the experimental flame speeds are derived from this non-linear 350 extrapolation [40]. This method however requires using a kinetic mechanism that yields an 351 352 accurate value of S<sub>u.0</sub>.

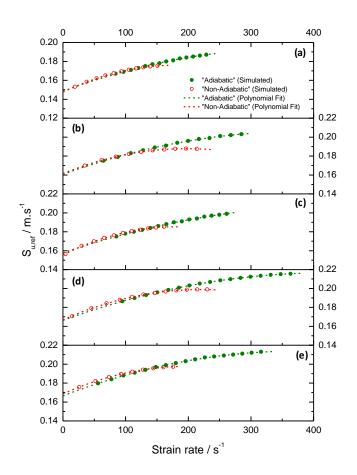
In the present work, a similar approach has been applied but without using the  $S_{u,0}$ calculated from a freely-propagating flame module. Axial velocity profiles were simulated using the Pre-Mixed Burner Stagnation Flame module of Chemkin-Pro by progressively decreasing the strain rate, from which a numerical curve  $S_{u,ref} = f(K)$  was extracted, as shown in Figure 7. The simulated curve  $S_{u,ref} = f(K)$  is then fitted using a 2<sup>nd</sup> order polynomial and vertically translated to best fit the experimental results [37-40]. The experimental unstrained cool flame speed  $S_{u,0}$  is then considered at K = 0. Figure 7 shows the application of this method for the five  $DME/O_2/O_3$  cool flames conditions. As seen in Figure 7, the numerical and experimental  $S_{u,0}$  lie very close to each other (those values are given in Table 3 for the five flames studied, columns 2 and 3).

Limitations of this method should however be considered. First, unlike hot flames, the 363 fuel conversion is only partial in a cool flame. Therefore, thermochemical equilibrium is not 364 reached in the post flame region. This causes non-zero temperature and velocity gradients in 365 the downstream area of the flame. Such results can therefore not be considered as laminar 366 burning velocities, nor modelled using a freely propagating flame module. Secondly, since the 367 stagnation plate temperature (600 K) is below the measured flame peak temperatures of about 368 369 900 K [23], such flames are not adiabatic. To assess the effect of this non-adiabaticity on the determined unstrained cool flame speeds S<sub>u,0</sub>, additional simulations were carried out. The 370 stagnation plate module of Cantera 2.6 [42] was used in the same domain width and input 371 compositions as in the simulations of Figures 5-6, and the stagnation plate temperature was 372 progressively increased until it reached a temperature identical to the maximal flame 373 374 temperature within a 0.01% tolerance. The strain rate was varied, and the  $S_{u,ref} = f(K)$  results were fitted to a  $2^{nd}$  order polynomial leading to  $S_{u,0}$  values at K=0 reported in Figure 8 and Table 375 3 (column 4). Because these cool flames are below 1000 K and sufficiently lifted to neglect 376 377 heat losses to the exit burner nozzle, they can be considered adiabatic, as for example in the well-known heat flux method [43]. The adiabatic  $S_{u,0}$  results (Table 3) are identical within the 378 uncertainty of the experiments to the simulated values at a plate temperature of 600 K, 379 380 demonstrating a negligible effect of the plate temperature on the measured unstrained cool flame velocities. 381



383

**Figure 7.** Variations of  $S_{u,ref}$  with K and determination of  $S_{u,0}$  using a numerically assisted non-linear extrapolation. Flame conditions:  $\phi = 0.5$ ,  $x_{O3} = 1.5\%$  (a),  $\phi = 0.45$ ,  $x_{O3} = 1.7\%$  (b),  $\phi = 0.4$ ,  $x_{O3} = 1.7\%$ (c),  $\phi = 0.4$ ,  $x_{O3} = 1.9\%$  (d) and  $\phi = 0.3$ ,  $x_{O3} = 2.0\%$  (e).



389

**Figure 8.** Simulated variations of  $S_{u,ref}$  with K using a non-linear extrapolation in adiabatic and nonadiabatic conditions. Flames conditions:  $\phi = 0.5$ ,  $x_{O3} = 1.5\%$  (a),  $\phi = 0.45$ ,  $x_{O3} = 1.7\%$  (b),  $\phi = 0.4$ ,  $x_{O3} = 1.7\%$  (c),  $\phi = 0.4$ ,  $x_{O3} = 1.9\%$  (d) and  $\phi = 0.3$ ,  $x_{O3} = 2.0\%$  (e).

393

394

Flame conditions	S <sub>u,0</sub> / cm.s <sup>-1</sup>			
	Experimental	Simulated	Simulated Adiabatic	
$\phi = 0.5, x_{O3} = 1.5\%$	$14.5 \pm 1 \text{ cm} \cdot \text{s}^{-1}$	14.7	14.8	
$\phi = 0.45, x_{O3} = 1.7\%$	15.8	16.1	16.1	
$\phi = 0.4, x_{O3} = 1.7\%$	15.4	15.6	15.8	
$\phi = 0.4, x_{O3} = 1.9\%$	17.3	16.7	16.6	
$\phi = 0.3, x_{O3} = 2.0\%$	16.8	16.9	16.6	

**Table 3.** Experimental and simulated unstrained cool flame speeds  $S_{u,0}$  for all the cool flames conditions.

396

By comparing both flames at  $x_{03} = 1.7\%$ , one can see that the cool flame speed increases moderately as the equivalence ratio increases from 0.4 to 0.45. This effect is captured by the simulation. A comparison of both flames at  $\phi = 0.4$  ( $x_{03} = 1.7\%$  and 1.9%) demonstrates the important effect of ozone addition on the cool flame speed, which increases by about 2 cm.s<sup>-1</sup>
(experimentally) when the ozone mole fraction increases only from 1.7% to 1.9%. This effect
is also captured in the simulation, yet underestimated.

403

404

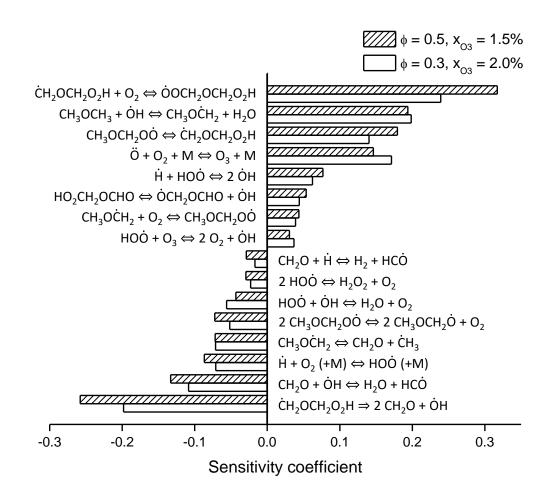
## **3.3. Kinetic analysis**

A brute-force sensitivity analysis was performed on the experimental reference axial 405 velocity S<sub>u,ref</sub>, using the Jian et al. O<sub>3</sub>-submechanism [20] in conjunction with our previously 406 published DME sub-mechanism [23], with the stagnation flame module of the Cantera 2.6 407 solver [42]. To do so, the domain size and input conditions were chosen as in the experiments 408 409 and simulations of Figures 5-6, and the sensitivity coefficients of the reactions on the minimum of axial velocity associated with the cool flame were evaluated from a positive and negative 410 variation of the frequency factor of each reaction by 5%. A positive sensitivity coefficient 411 412 therefore means that increasing the reaction rate constant for the associated reaction increases the reference cool flame velocity S<sub>u,ref</sub>, and vice versa. The two most extreme conditions were 413 selected for the sensitivity analyses, respectively the flame at  $\phi = 0.3$ ,  $x_{03} = 2.0\%$ , which 414 contains the highest ozone mole fraction in this study, and the flame at  $\phi = 0.5$ ,  $x_{O3} = 1.5\%$ , 415 which contains the lowest. The results are displayed for the 16 reactions with the highest 416 417 absolute sensitivity coefficients in Figure 9.

In both conditions, it is observed that the simulated  $S_{u,ref}$  is strongly dependent on the branching between the decomposition of the QOOH into two molecules of formaldehyde and an OH radical, which tends to decrease the cool flame velocity, and the addition of QOOH to  $O_2$ , which will lead to indirect chain-branching. Among the other important features is the competition between the ROO  $\Leftrightarrow$  QOOH pathway, and the 2 ROO  $\Leftrightarrow$  2 RO +  $O_2$  route. The latter is traditionally associated with atmospheric conditions, but was previously observed to be

significant in our conditions [23]. To a more reduced extent, the branching of R radical between 424 addition to O<sub>2</sub> or direct scission into formaldehyde and a methyl radical is also of importance. 425 One can however note the large sensitivity coefficient of the H-atom abstraction reaction on 426 DME by OH. A striking feature of these results is that, in contrast with hot flames burning 427 velocities, the most sensitive reactions are all directly part of the fuel submechanism, the  $O_3$  + 428  $M \Leftrightarrow O_2 + \ddot{O} + M$  reaction only ranking as the fourth most sensitive reaction. This is a strong 429 argument in favour of these experimental data as potential targets for the validation of kinetic 430 models in the low-temperature domain. 431

432



433

434 **Figure 9.** Brute-force sensitivity analysis performed on the reference cool flame  $S_{u,ref}$ , at  $\phi = 0.5$ ,  $x_{O3} =$ 435 1.5% and at  $\phi = 0.3$ ,  $x_{O3} = 2.0\%$ .

#### 4. CONCLUSIONS

The measurement of ozone-seeded dimethyl ether cool flame speeds was successfully 438 realized in a stagnation plate burner for the first time. The PIV technique was used to measure 439 440 the 2-D velocity profiles, from which axial velocity profiles were inferred to measure the unstrained cool flame speeds. For this purpose, an in-house PIV image processing method has 441 been developed and used in order to improve the accuracy of the measurement. Five flame 442 conditions, with equivalence ratios varying from 0.3 to 0.5 and ozone mole fraction varying 443 from 1.5 to 2% were used to compare experimental results with kinetic modeling. Three ozone-444 445 submechanisms, namely from Jian et al., Zhao et al. and Halter et al., were coupled with our previous mechanism validated in DME/O<sub>2</sub>/O<sub>3</sub> cool flames and used to compare experimental 446 and simulated axial velocity profiles, emphasizing the importance of the choice of the O<sub>3</sub>-447 448 submechanism. The Jian et al. submechanism was selected because of its good predictive ability for axial velocity profiles and was used to determine the unstrained cool flame speed S<sub>u,0</sub> for 449 450 each tested condition. A numerical assisted non-linear extrapolation method is proposed for the determination of S<sub>u.0</sub>. Additionally, simulations for which the plate temperature reaches the 451 maximal flame temperature (i.e., adiabatic conditions) were performed, demonstrating a 452 453 negligible effect of the plate temperature on the unstrained cool flame velocity. However, for the purpose of mechanism validation, the direct comparison with the experimental axial 454 velocity profiles should be preferred as it requires no numerical assisted method. Values of Su,0 455 were found to lie between  $\sim 14$  and 17 cm.s<sup>-1</sup> within the range of flame conditions studied here, 456 457 showing a limited effect of the equivalence ratio variations, and a more striking effect of the ozone concentration. Finally, sensitivity analyses performed on the reference axial velocity S<sub>u.ref</sub> 458 in two flame conditions emphasize the importance of the fuel low-temperature chain-branching 459 pathways, over the ozone submechanism. 460

462	Acknowledgements
463	This work is a contribution to the LabEx CaPPA project funded by the French National Agency
464	under contract « ANR-11-LABX-0005-01 », the CPER research project CLIMIBIO funded by
465	the French Ministère de l'Enseignement Supérieur et de la Recherche and the MéOL
466	(Métrologie Optique de Lille) platform. The authors thank the Regional Council « Hauts-de-
467	France » and the « European Regional Development Fund » for their financial support to these
468	projects.
469	
470	Supplementary material
471	Supplementary Material can be found in the attached file.
472	
473	Authors contributions
474	Conceptualization: L. Pillier, G. Vanhove; Data curation: All authors; Formal analysis: T.
475	Panaget, B. Lecordier, Y. Fenard, G. Vanhove, L. Pillier, P. Bragança, C. Cuvier; Funding
476	acquisition: L. Pillier, G. Vanhove; Investigation: T. Panaget, P. Bragança, L. Pillier, C.
477	Cuvier; Methodology: All authors; Project administration: L. Pillier, G. Vanhove; Resources:
478	L. Pillier, G. Vanhove, B. Lecordier, C. Cuvier; Software: T. Panaget, Y. Fenard, G.
479	Vanhove, B. Lecordier, P. Bragança, C. Cuvier; Supervision: L. Pillier, G. Vanhove, Y.
480	Fenard; Validation: All authors; Visualization: All authors; Roles/Writing - original draft: T.
481	Panaget, L. Pillier, G. Vanhove; and Writing - review & editing: All authors
482	
483	
484	
485	
486	
487	
488	
489	

## 490 **REFERENCES**

- 491 [1] Davy H. VIII. Some new experiments and observations on the combustion of gaseous
  492 mixtures, with an account of a method of preserving a continued light in mixtures of
  493 inflammable gases and air without flame. Philos Trans R Soc Lond 1817;107:77–85.
  494 https://doi.org/10.1098/rstl.1817.0009.
- [2] Nayagam V, Dietrich DL, Ferkul PV, Hicks MC, Williams FA. Can cool flames support
  quasi-steady alkane droplet burning? Combust Flame 2012;159:3583–8.
  https://doi.org/10.1016/j.combustflame.2012.07.012.
- 498 [3] Ju Y. Understanding cool flames and warm flames. Proc Combust Inst 2021; 38: 83 119.
   499 https://doi.org/10.1016/j.proci.2020.09.019
- Ju Y, Reuter C, Yehia OR, Farouk TI, Won SH. Dynamics of cool flame. Progress in Energy and Combustion Science 2019; 75:100787.
   https://doi.org/10.1016/j.pecs.2019.100787
- 503 [5] Bhagatwala A, Chen JH, Lu T. Direct numerical simulations of HCCI/SACI with ethanol.
   504 Combust Flame 2014;161:1826–41. https://doi.org/10.1016/j.combustflame.2013.12.027.
- Ju Y, Reuter CB, Won SH. Numerical simulations of premixed cool flames of dimethyl
   ether/oxygen mixtures. Combust Flame 2015;162:3580–8.
   https://doi.org/10.1016/j.combustflame.2015.06.014.
- Ju Y. On the propagation limits and speeds of premixed cool flames at elevated pressures.
   Combust Flame 2017;178:61–9. https://doi.org/10.1016/j.combustflame.2017.01.006.
- [8] Zhao P, Liang W, Deng S, Law CK. Initiation and propagation of laminar premixed cool
  flames. Fuel 2016;166:477–87. https://doi.org/10.1016/j.fuel.2015.11.025.
- 512 [9] Gao X, Zhang Y, Adusumilli S, Seitzman J, Sun W, Ombrello T, et al. The effect of ozone
  513 addition on laminar flame speed. Combust Flame 2015;162:3914–24.
  514 https://doi.org/10.1016/j.combustflame.2015.07.028.
- 515 [10] Ombrello T, Won SH, Ju Y, Williams S. Flame propagation enhancement by plasma
  516 excitation of oxygen. Part I: Effects of O3. Combust Flame 2010;157:1906–15.
  517 https://doi.org/10.1016/j.combustflame.2010.02.005.
- 518 [11] Foster M, Pearlman H. Cool Flame Propagation Speeds. Combust Sci Technol
   519 2007;179:1349–60. https://doi.org/10.1080/00102200601147864.
- 520 [12] Brown MQ, Belmont EL. Effects of ozone on n-heptane low temperature chemistry and
   521 premixed cool flames. Combust Flame 2021;225:20–30.
   522 https://doi.org/10.1016/j.combustflame.2020.10.029.
- [13] Hajilou M, Brown MQ, Brown MC, Belmont E. Investigation of the structure and
  propagation speeds of n-heptane cool flames. Combust Flame 2019;208:99–109.
  https://doi.org/10.1016/j.combustflame.2019.06.020.
- [14] Hajilou M, Belmont E. Characterization of ozone-enhanced propane cool flames at sub atmospheric pressures. Combust Flame 2018;196:416–23.
   https://doi.org/10.1016/j.combustflame.2018.07.001.
- [15] Hajilou M, Ombrello T, Won SH, Belmont E. Experimental and numerical characterization of freely propagating ozone-activated dimethyl ether cool flames.
   Combust Flame 2017;176:326–33. https://doi.org/10.1016/j.combustflame.2016.11.005.
- [16] Belmont E, Ombrello T, Brown M, Carter C, Ellzey J. Experimental and numerical
   investigation of freely propagating flames stabilized on a Hencken Burner. Combust
   Flame 2015;162:2679–85. https://doi.org/10.1016/j.combustflame.2015.03.025.
- [17] Ombrello T, Carter C, Katta V. Burner platform for sub-atmospheric pressure flame
   studies. Combust Flame 2012;159:2363–73.
   https://doi.org/10.1016/j.combustflame.2012.03.010.

- [18] Reuter CB, Won SH, Ju Y. Cool Flames Activated by Ozone Addition. 53rd AIAA
  Aerosp. Sci. Meet., Kissimmee, Florida: American Institute of Aeronautics and Astronautics; 2015. https://doi.org/10.2514/6.2015-1387.
- [19] Liao H, Kang S, Hansen N, Zhang F, Yang B. Influence of ozone addition on the low-temperature oxidation of dimethyl ether in a jet-stirred reactor. Combust Flame 2020;214:277–86. https://doi.org/10.1016/j.combustflame.2019.12.036.
- [20] Jian J, Hashemi H, Wu H, Jasper AW, Glarborg P. A reaction mechanism for ozone dissociation and reaction with hydrogen at elevated temperature. Fuel 2022;322:124138.
  https://doi.org/10.1016/j.fuel.2022.124138.
- [21] Zhao H, Yang X, Ju Y. Kinetic studies of ozone assisted low temperature oxidation of
   dimethyl ether in a flow reactor using molecular-beam mass spectrometry. Combust Flame
   2016;173:187–94. https://doi.org/10.1016/j.combustflame.2016.08.008.
- [22] Halter F, Higelin P, Dagaut P. Experimental and Detailed Kinetic Modeling Study of the
  Effect of Ozone on the Combustion of Methane. Energy Fuels 2011;25:2909–16.
  https://doi.org/10.1021/ef200550m.
- [23] Panaget T, Mokrani N, Batut S, Lahccen A, Fenard Y, Pillier L, et al. Insight into the
  Ozone-Assisted Low-Temperature Combustion of Dimethyl Ether by Means of Stabilized
  Cool Flames. J Phys Chem A 2021;125:9167–79.
  https://doi.org/10.1021/acs.jpca.1c05583.
- [24] Kähler C, Sammler B, Kompenhans J. Generation and control of tracer particles for optical
  flow investigations in air. Exp Fluids 2002;33:736–42. https://doi.org/10.1007/s00348002-0492-x.
- [25] Lecordier B, Demare D, Vervisch LMJ, Réveillon J, Trinite M. Estimation of the accuracy
   of PIV treatments for turbulent flow studies by direct numerical simulation of multi-phase
   flow. Meas Sci Technol 2001;12:1382.
- 563 [26] Balusamy S, Cessou A, Lecordier B. Direct measurement of local instantaneous laminar
  564 burning velocity by a new PIV algorithm. Exp Fluids 2011;50:1109–21.
  565 https://doi.org/10.1007/s00348-010-1027-5.
- 566 [27] Ansys Chemkin Pro, Release 2021 R1 2021.
- [28] Metcalfe WK, Burke SM, Ahmed SS, Curran HJ. A Hierarchical and Comparative Kinetic
   Modeling Study of C<sub>1</sub> C<sub>2</sub> Hydrocarbon and Oxygenated Fuels. Int J Chem Kinet
   2013;45:638–75. https://doi.org/10.1002/kin.20802.
- [29] Durocher A, Meulemans M, Bourque G, Bergthorson JM. Measurements of the laminar
   flame speed of premixed, hydrogen-air-argon stagnation flames. Appl Energy Combust
   Sci 2021;7:100028. https://doi.org/10.1016/j.jaecs.2021.100028.
- [30] Munzar JD, Akih-Kumgeh B, Denman BM, Zia A, Bergthorson JM. An experimental and
   reduced modeling study of the laminar flame speed of jet fuel surrogate components. Fuel
   2013;113:586–97. https://doi.org/10.1016/j.fuel.2013.05.105.
- [31] Bergthorson JM, Salusbury SD, Dimotakis PE. Experiments and modelling of premixed
  laminar stagnation flame hydrodynamics. J Fluid Mech 2011;681:340–69.
  https://doi.org/10.1017/jfm.2011.203.
- [32] Sung CJ, Kistler JS, Nishioka M, Law CK. Further studies on effects of thermophoresis
   on seeding particles in LDV measurements of strained flames. Combust Flame
   1996;105:189–201. https://doi.org/10.1016/0010-2180(95)00189-1.
- [33] Bouvet N, Davidenko D, Chauveau C, Pillier L, Yoon Y. On the simulation of laminar strained flames in stagnation flows: 1D and 2D approaches versus experiments. Combust Flame 2014;161:438–52. https://doi.org/10.1016/j.combustflame.2013.09.010.
- [34] Vagelopoulos CM, Egolfopoulos FN. Direct experimental determination of laminar flame
   speeds. Symp Int Combust 1998;27:513–9. https://doi.org/10.1016/S0082 0784(98)80441-4.

- [35] Davis SG, Law CK. Determination of and Fuel Structure Effects on Laminar Flame
  Speeds of C 1 to C 8 Hydrocarbons. Combust Sci Technol 1998;140:427–49. https://doi.org/10.1080/00102209808915781.
- [36] Tien JH, Matalon M. On the burning velocity of stretched flames. Combust Flame
  1991;84:238–48. https://doi.org/10.1016/0010-2180(91)90003-T.
- [37] Chong CT, Hochgreb S. Measurements of laminar flame speeds of acetone/methane/air
   mixtures. Combust Flame 2011;158:490–500.
   https://doi.org/10.1016/j.combustflame.2010.09.019.
- [38] Veloo PS, Wang YL, Egolfopoulos FN, Westbrook CK. A comparative experimental and computational study of methanol, ethanol, and n-butanol flames. Combust Flame 2010;157:1989–2004. https://doi.org/10.1016/j.combustflame.2010.04.001.
- [39] Ji C, Dames E, Wang YL, Wang H, Egolfopoulos FN. Propagation and extinction of
  premixed C5–C12 n-alkane flames. Combust Flame 2010;157:277–87.
  https://doi.org/10.1016/j.combustflame.2009.06.011.
- [40] Wang YL, Holley AT, Ji C, Egolfopoulos FN, Tsotsis TT, Curran HJ. Propagation and
   extinction of premixed dimethyl-ether/air flames. Proc Combust Inst 2009;32:1035–42.
   https://doi.org/10.1016/j.proci.2008.06.054.
- [41] Egolfopoulos FN, Hansen N, Ju Y, Kohse-Höinghaus K, Law CK, Qi F. Advances and challenges in laminar flame experiments and implications for combustion chemistry. Prog Energy Combust Sci 2014; 43:36–67. https://doi.org/10.1016/j.pecs.2014.04.004.
- 608 [42] D. Goodwin, H. Moffat, R. Speth, Cantera: An Object-oriented Software Toolkit for
- 609 Chemical Kinetics, Thermodynamics, and Transport Processes, 2015.
  610 http://dx.doi.org/10.5281/zenodo.48735
- [43] K.J. Bosschaart and L.P.H. de Goey, The laminar burning velocity of flames propagating
   in mixtures of hydrocarbons and air measured with the heat flux method, Comb. Flame 136
   (2004) 261–269. https://doi.org/10.1016/j.combustflame.2003.10.005.
- 614