

Physics-augmented neural networks for constitutive modeling: training with the modified Constitutive Relation Error

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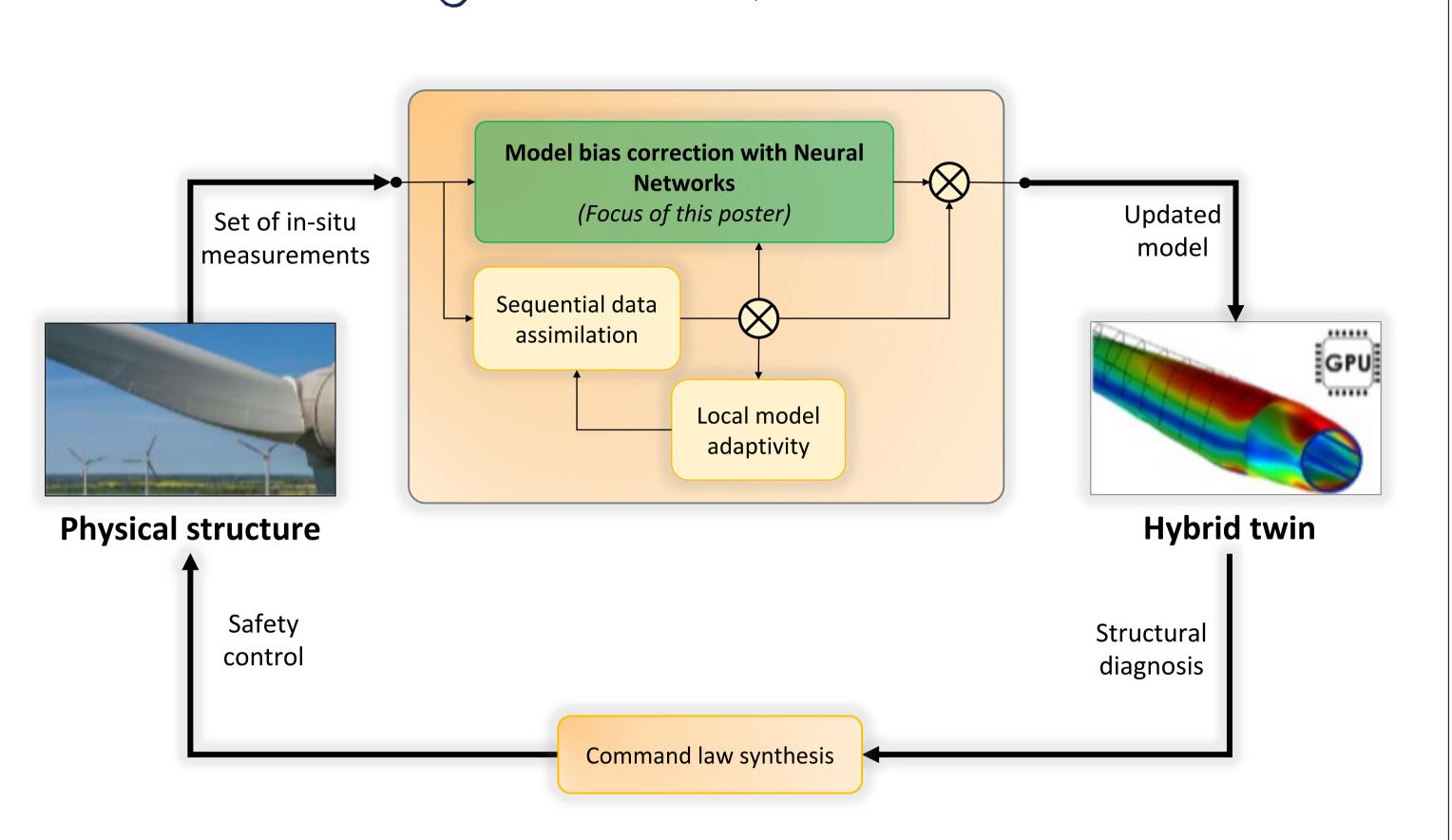
PHYSICS-AUGMENTED NEURAL NETWORKS FOR CONSTITUTIVE MODELING: TRAINING WITH THE MODIFIED CONSTITUTIVE RELATION ERROR (MCRE)

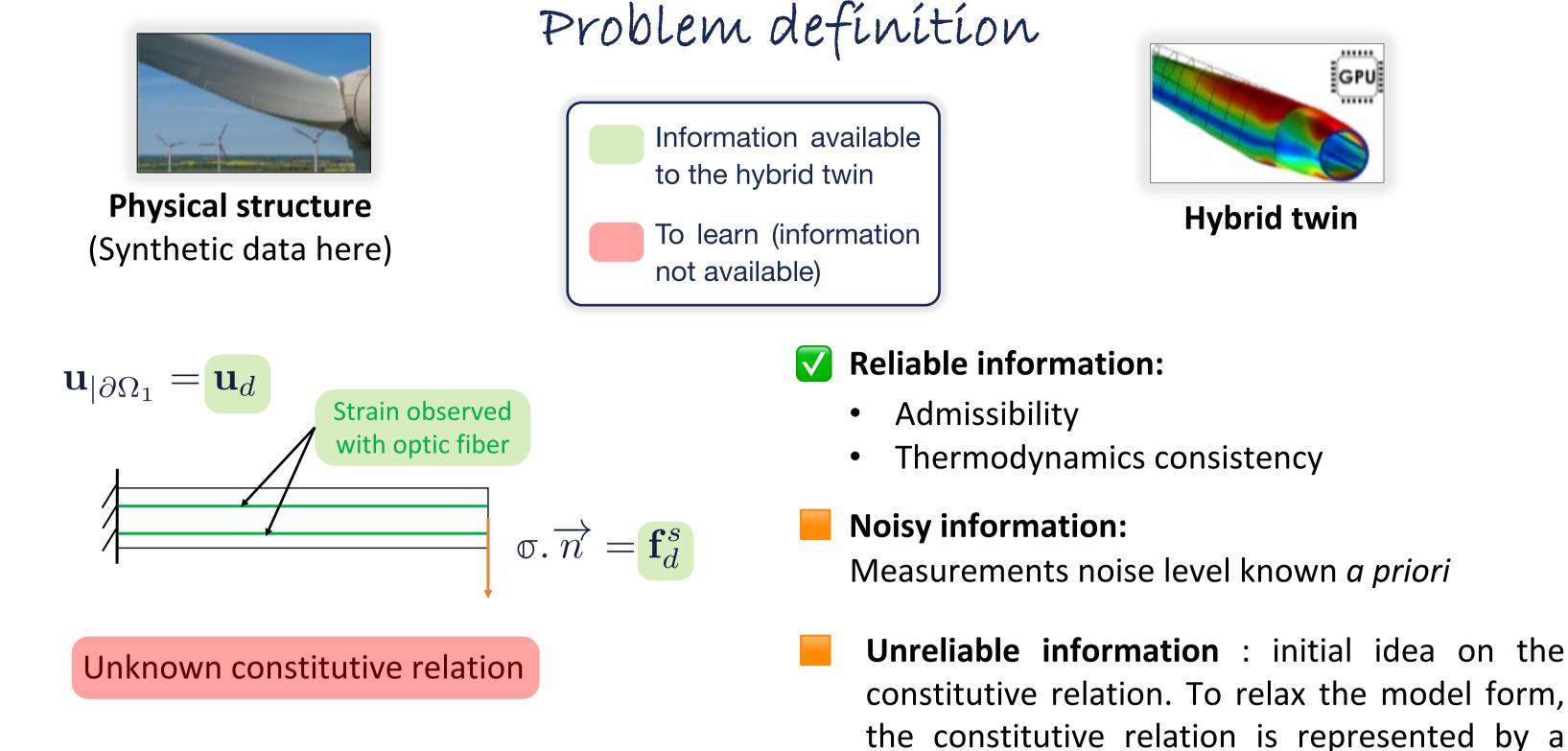
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Keywords: Constitutive modeling, Physics-augmented Neural Network, Unsupervised learning, Constitutive relation error, Plasticity

Context: hybrid-twin for real-time control

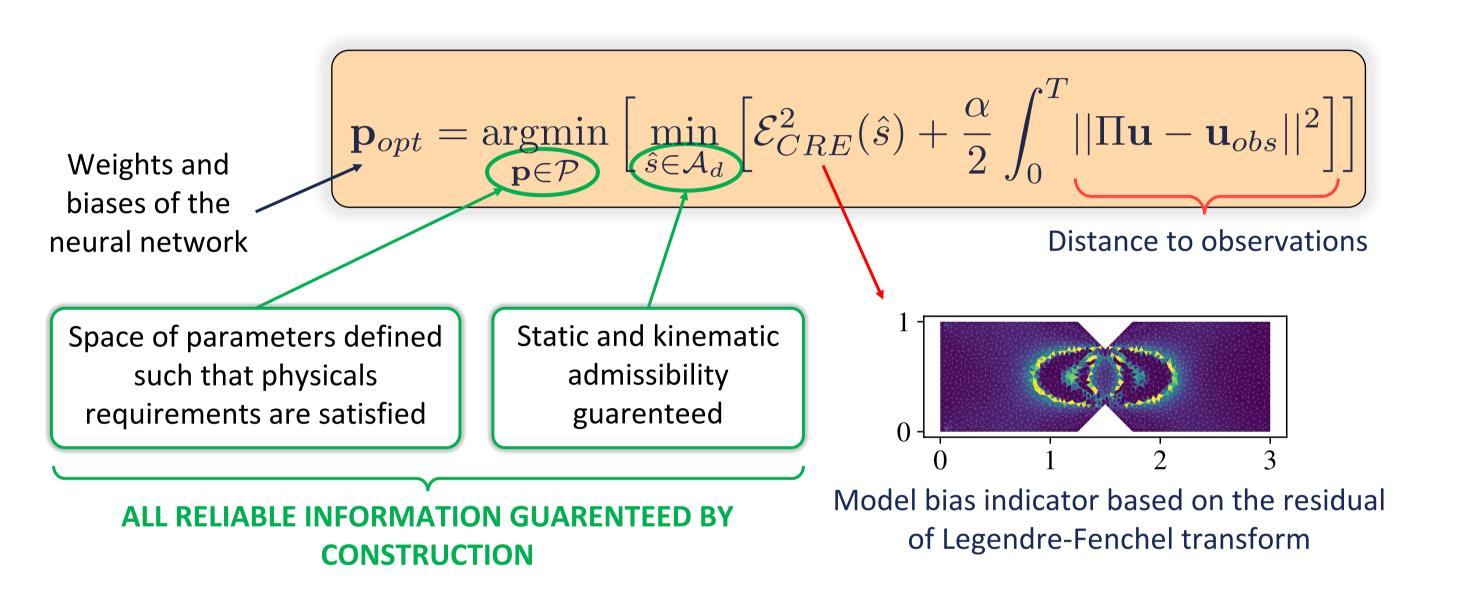




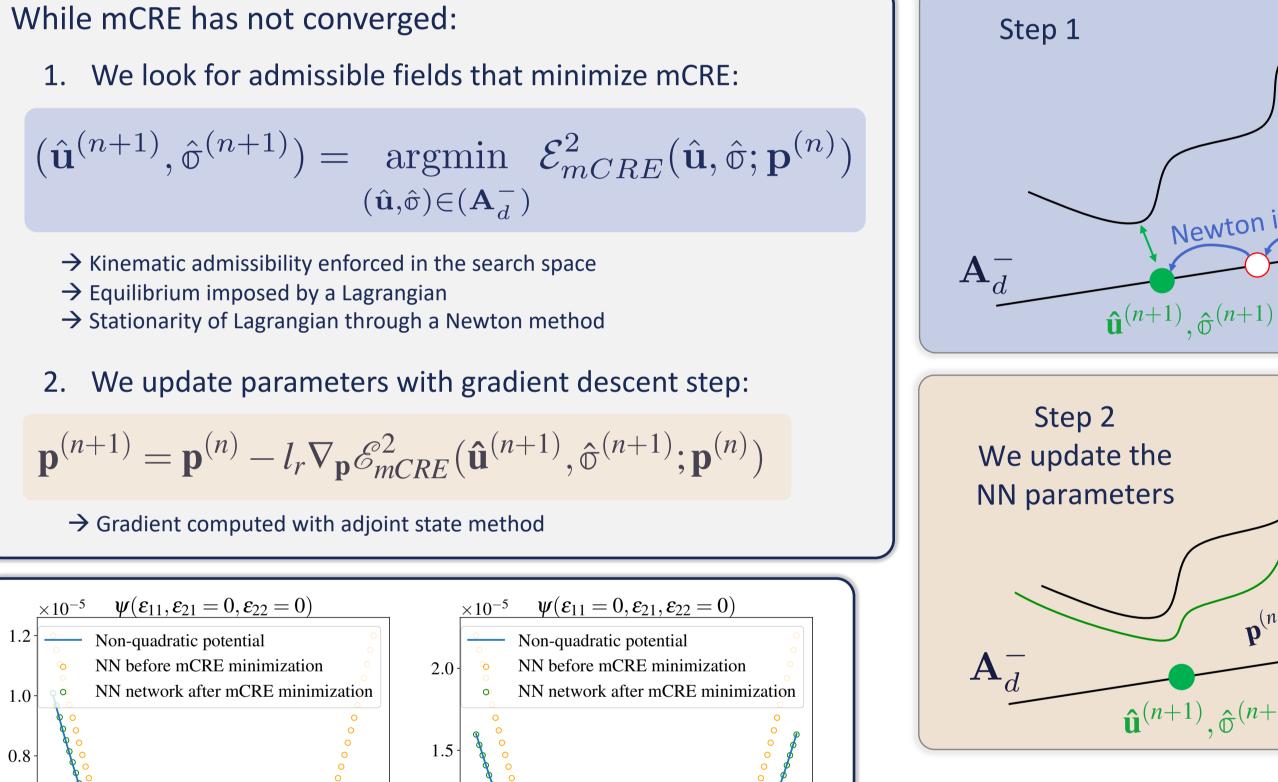
A copyex Helmholtz free energy $\sqrt{2}$ involved in set the state laws

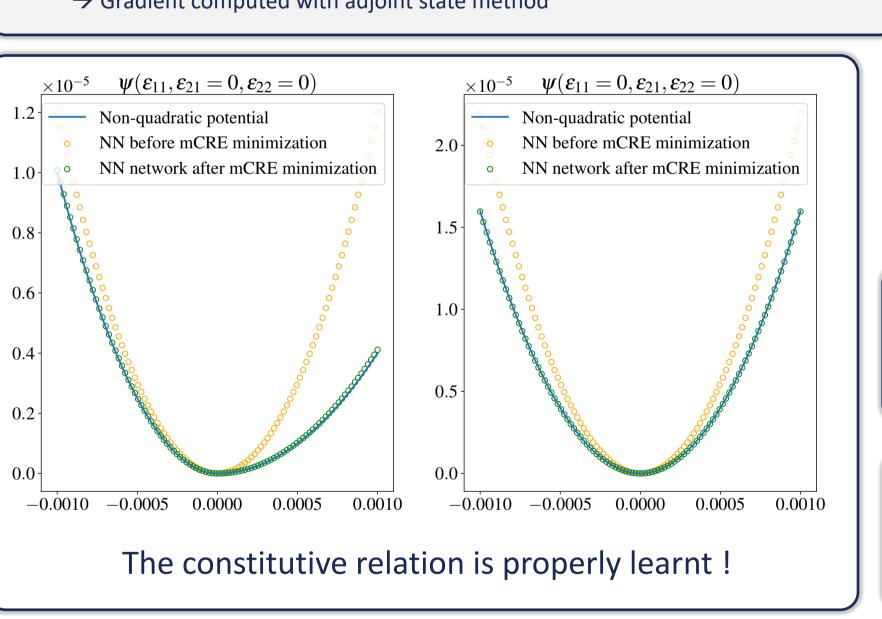
A convex Helmholtz free energy ψ involved in set the state laws, A convex, non-negative, zero at origin pseudo-potential φ involved in the set of evolution laws.

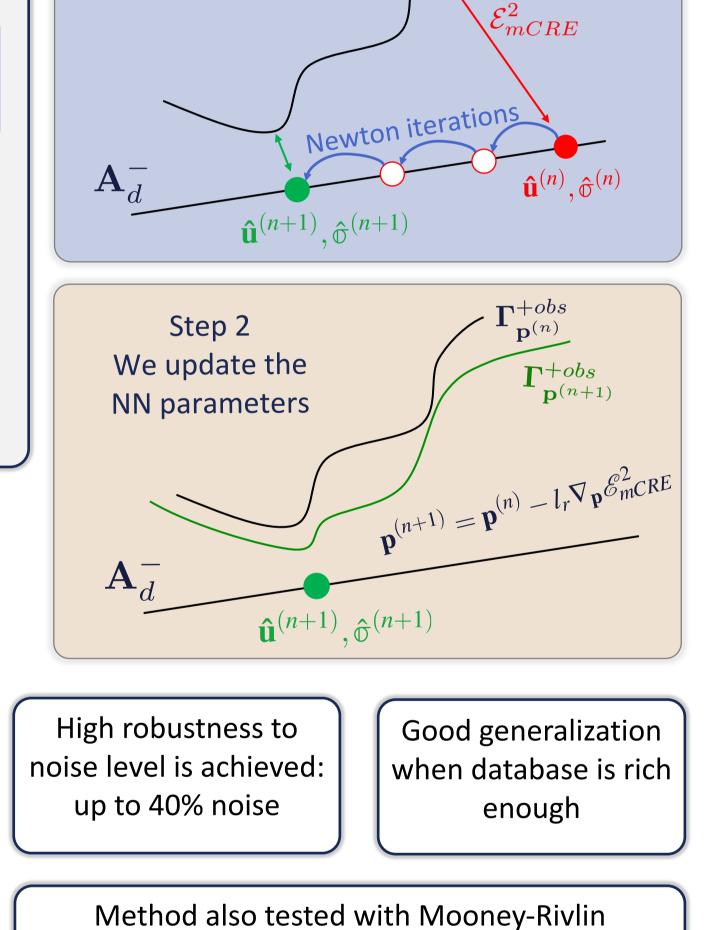
The modified Constitutive Relation Error (mCRE)



Learning of nonlinear state laws





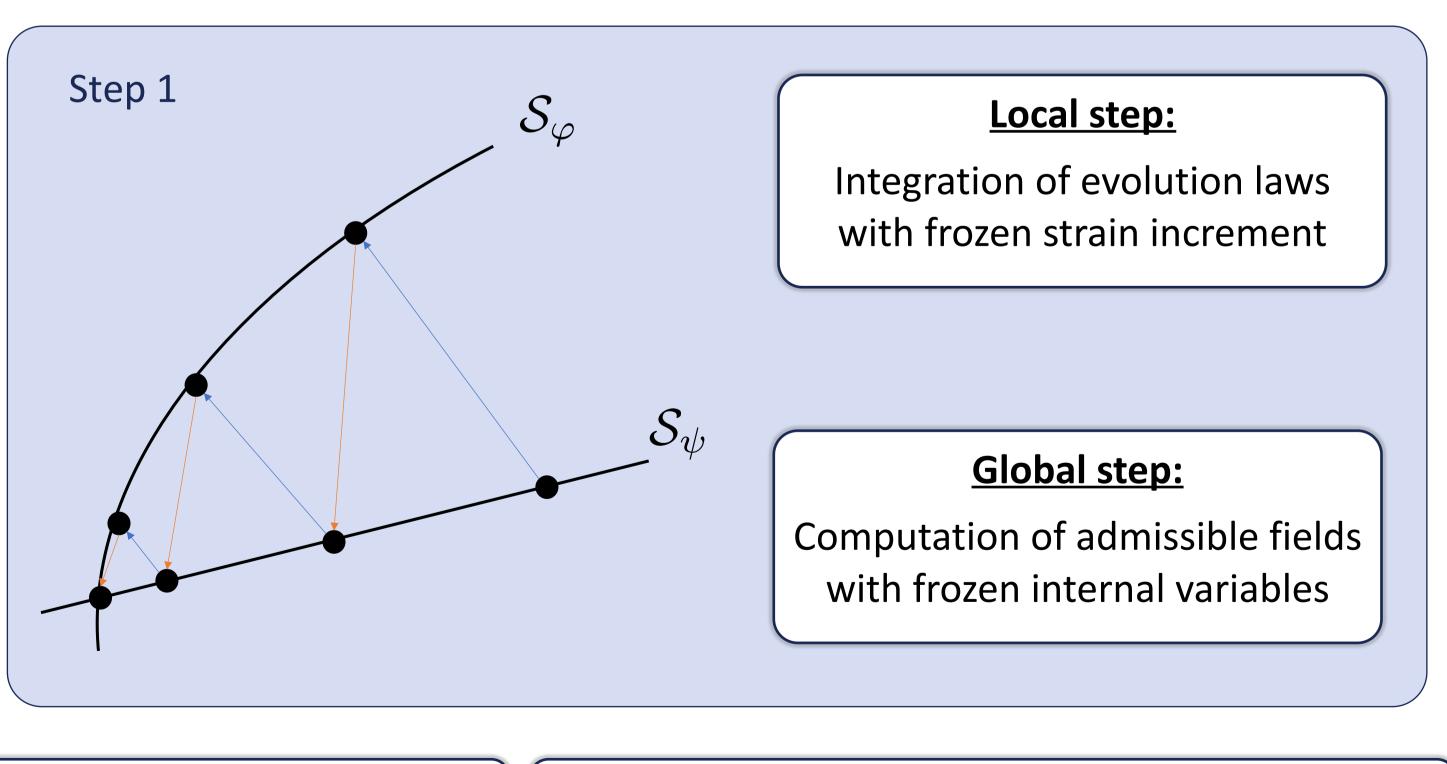


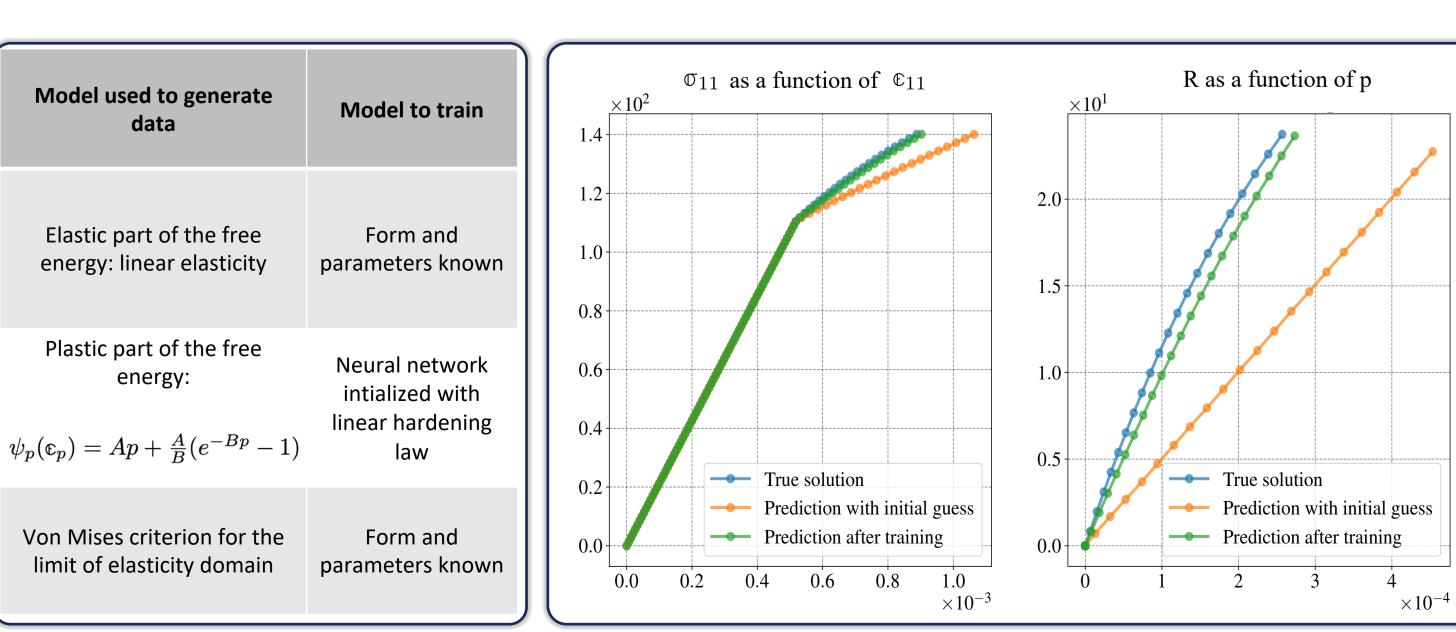
thermodynamics consistent neural network.

hyperelastic model : $\psi(\mathbf{E})=A(\tilde{\mathbf{I}}_1-3)+B(\tilde{\mathbf{I}}_2-3)+C(\tilde{\mathbf{I}}_1-3)(\tilde{\mathbf{I}}_2-3)$

Learning of history-dependent behavior

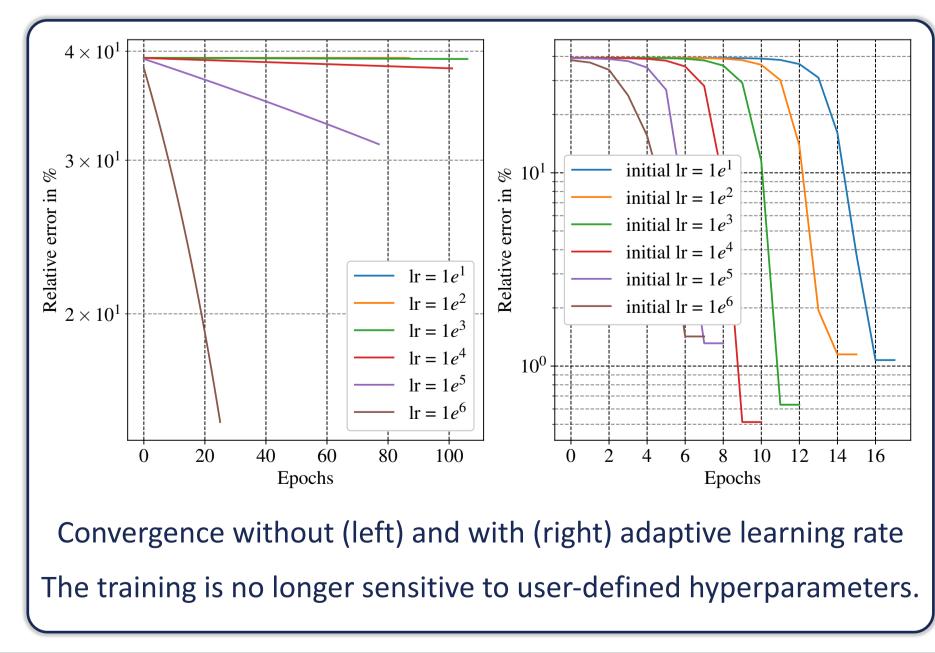
For history-dependent behavior, the minimization of the mCRE is slightly different. The Step 1 is performed with a LATIN-inspired method composed of the alternance of a local step (integration of evolution law) and a global step (computation of admissible fields).





What about hyperparameters tuning?

Parameters	Tuning
Learning rate	Adaptive learning rate during training
Weigthing between losses	Morozov-based automatic tuning
Number of epochs	mCRE-based stop criteria
Network initialization	Initialization with simple model
Batch size	Fixed by mesh



Conclusion

Neural network trained to learn constitutive model with observable data

All reliable information is guarenteed by construction

No need for user to tune hyperparameters







