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New mixed inhomogeneous phase in vortical gluon plasma: first-principle results from rotating SU(3) lattice gauge theory

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Using first-principle numerical simulations, we find a new spatially inhomogeneous phase in rigidly rotating $N_c = 3$ gluon plasma. This mixed phase simultaneously possesses both confining and deconfining phases in thermal equilibrium. Unexpectedly, the local critical temperature of the phase transition at the rotation axis does not depend on the angular frequency within a few percent accuracy. Even more surprisingly, an analytic continuation of our results to the domain of real angular frequencies indicates a profound breaking of the Tolman-Ehrenfest law in the vicinity of the phase transition, with the confining (deconfining) phase appearing far (near) the rotation axis.

Introduction. The experimental observation of quark-gluon plasma (QGP) produced in non-central heavy-ion collisions has ignited intense theoretical interest in these highly vortical, strongly interacting systems. The plasma droplets are created in a state possessing a nonzero net angular momentum with the vorticity of the plasma estimated to reach the enormous value of [1]

$$\Omega \simeq (9 \pm 1) \times 10^{21} \text{ s}^{-1} \sim 0.03 \text{ fm}^{-1} c \simeq 7 \text{ MeV}. \quad (1)$$

The rapid rotation, which is revealed experimentally via the global polarization measurements of produced hyperons [1–3], is analytically predicted to have a significant impact on the phase structure of QGP [4–19].

It must be noted that *all* theoretical approaches to the QGP thermodynamics are performed under the condition of the rigid rotation of the system [4–27]. In a rigidly rotating fluid, the uniformity of vorticity implies the absence of the viscous component of the stress tensor [28], indicating no internal friction and no entropy production, thereby representing a thermodynamic ground state of the system. Although this simplification is not an accurate approximation of an off-equilibrium state of the QGP produced in heavy-ion collisions, it drastically simplifies the theoretical analysis and makes predictions on the consequences of rotating QCD much easier. Despite the would-be simplicity of the rigid rotation, it reveals profound disagreement between the results coming from analytical [4–16] and numerical [22–27] simulations (see also [19]), implying that our understanding of the rotating QGP is far from satisfactory.

The controversy is further augmented by two independent numerical observations in finite-temperature Yang-Mills theory, made in both rotating [26] and static [29] systems, which revealed that the moment of inertia of the gluon plasma takes a negative value in a range of temperatures starting from a temperature slightly below the deconfining phase transition $T_{c0} \equiv T_c(\Omega = 0)$, identified in a non-rotating system, up to the “supervortical” temperature $T_s \simeq 1.5T_{c0}$ [26, 29, 30]. This exceptional

phenomenon, which has no analogs in ordinary fluids, was shown to occur due to thermal evaporation of the chromomagnetic condensate [26]. The negative moment of inertia was argued to emerge from the negativity of a gluonic Barnett effect, which implies a negative coupling of the gluon spin polarization with vorticity [31].

Below, we deepen this mystery even further. We reveal, using first-principle lattice simulations, a new mixed structure of confining (hadron) and deconfining (quark-gluon plasma) phases that co-exist simultaneously in a rotating hot gluon matter. Although the existence of a confining-deconfining phase was proposed some years ago [12] (see also the holographic study [16]) and was evidenced in lattice calculations with a *kinematically* defined order parameter [32] we show that the *dynamical* structure of the plasma is surprisingly different from all existing theoretical predictions.

Lattice set up for rotating gluodynamics. Rigid rotation with a fixed angular velocity Ω can be conveniently described by setting a relevant system in curved spacetime endowed with the metric [33]:

$$g_{\mu\nu} = \begin{pmatrix} 1 - r^2\Omega^2 & \Omega y & -\Omega x & 0 \\ \Omega y & -1 & 0 & 0 \\ -\Omega x & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}, \quad (2)$$

where $r = \sqrt{x^2 + y^2}$ is the distance from the axis of rotation set to be along the z direction. Consequently, a rotating gluon system is described by Yang-Mills action

$$S = -\frac{1}{2g^2} \int d^4x \sqrt{-g} g^{\mu\nu} g^{\alpha\beta} F_{\mu\alpha}^a F_{\nu\beta}^a, \quad (3)$$

where $F_{\mu\nu}^a$ is the field-strength tensor of the gluon field.

To study this system, we follow lattice methods used in Refs. [22–26, 29–31, 33]. In particular, within lattice simulations, one studies the system with the action (3) in thermodynamic equilibrium. The partition function of this system can be written as the path integral over gluon fields with the weight e^{-S_E} , where S_E is the

Euclidean lattice action of rotating Yang-Mills theory. Unfortunately, this action is a complex-valued function that leads to a sign problem and does not allow to apply lattice methods directly to this theory. To overcome this obstacle, we carry out lattice simulation with imaginary angular velocity $\Omega_I = -i\Omega$ and then analytically continue the results to real values of Ω through the identification: $\Omega_I^2 \rightarrow -\Omega^2$.

The temperature of a system in the thermodynamic equilibrium in an external static gravitational field depends on the coordinates \mathbf{r} and obeys the well-known Tolman-Ehrenfest (TE) law [34, 35]: $\sqrt{g_{00}(\mathbf{r})}T(\mathbf{r}) = T_0 = \text{const}$. For a rotating system (2), the TE law gives:

$$T(r) = \frac{T_0}{\sqrt{1 - \Omega^2 r^2}} = \frac{T_0}{\sqrt{1 + \Omega_I^2 r^2}}, \quad (4)$$

where T_0 is the temperature at the rotation axis ($r = 0$). The last equality in Eq. (4) corresponds to the case of imaginary rotation. In our numerical simulations, we fix the on-axis temperature parameter T_0 and call it, unless stated otherwise, the temperature T of gluon plasma.

Lattice setup. To construct the lattice form of the continuum action (3), we discretize the terms, which are coupled with the angular velocity, following Refs. [23, 33], whereas for the remaining (non-rotating) terms, we use tree-level improved Symanzik gauge action [36, 37]. The explicit form of the used lattice action may be found in Ref. [26]. The simulations were performed on the lattices of size $N_t \times N_x \times N_y \times N_z \times N_s^2$ ($N_x = N_y = N_s$), and the rotation axis passes through the lattice site in the center of xy -plane. To study in detail the non-trivial dynamics of gluons induced by the rotation, we use the lattices with a large extension in transversal space directions: $4 \times 24 \times 145^2$, $5 \times 30 \times 181^2$ and $6 \times 36 \times 217^2$.

We applied open boundary conditions [23] in the directions that are orthogonal to the rotation axis and used conventional periodic boundary conditions in the directions along the rotation axis and the Euclidean time. While the choice of the boundary conditions in transversal directions warrants some discussion, the previous study [23] indicates that a type of spatial boundary does not produce an important impact on the bulk of the system due to strong screening. Nonetheless, to validate the correctness of this approach, we reproduced some of our results with periodic boundary conditions in xy -plane.

Slow rotation and analytic continuity. We carry out simulations at imaginary angular frequencies and then perform analytic continuation to real rotations. It is convenient to describe the results in terms of the imaginary velocity $v_I = \Omega_I R$ at the QGP boundary, $v_I^2 = -v_R^2$, where the velocity v_I is taken for the middle of the boundary side, i.e., at the distance $R = a(N_s - 1)/2$ from the axis of rotation. The analytic continuation is only possible if at any point of the system $|\Omega_I| r < 1$ so that the real solid rotation does not violate causality

with a corresponding theorem proven in Ref. [38]. In our paper, we respect the causality bound.

Another important and, perhaps, not intuitively clear statement is that the thermodynamical properties of the rotating plasma, which has the shape of a cylinder, depend on the angular frequency Ω only in the combination $v_R = \Omega R$ which is nothing but the (imaginary) velocity of the system at the boundary v_R [26, 29, 31].

Confining and deconfining phases. In this paper, we concentrate on a pure gluon SU(3) system, which constitutes the most important component of the QGP and determines all its nontrivial properties. At vanishing rotation, thermal gluon matter emerges in two phases: it resides either in the confinement phase, in which all color degrees of freedom are bounded into colorless states, or the deconfinement phase, in which the asymptotic physical states are colored objects. These pure-gluon phases are precursors of the low-temperature hadronic and high-temperature QGP phases, respectively.

Confining and deconfining phases can be distinguished with the help of the expectation of the Polyakov loop,

$$L(\mathbf{r}) = \text{Tr} \mathcal{P} \exp \left(\oint_0^{1/T} d\tau A_4(\tau, \mathbf{r}) \right), \quad (5)$$

where \mathcal{P} is the path-ordering operator and the integral goes over the timelike component A_4 of the matrix-valued gluon field A_μ along the compactified Euclidean time τ .

The expectation value of the Polyakov loop operator (5), $\langle L \rangle = e^{-F_Q/T}$, is interpreted via the free energy F_Q of an infinitely heavy test quark Q . In the confinement phase, the free quarks do not exist as they possess infinite energy, implying that $\langle L \rangle = 0$. In the deconfinement phase, on the contrary, $\langle L \rangle \neq 0$, the quark's free energy is finite, $F_Q \neq 0$, and the quarks can exist as free states. The expectation value of the Polyakov loop serves as a reliable order parameter that distinguishes two phases in a static, non-rotating SU(3) gluon plasma.

Emergence of the inhomogeneity. Quark-gluon plasma, slightly above the deconfining phase transition, resembles more a liquid than a gas. Our experience tells us that if a liquid is rotated –think about a rotating glass of water– then it becomes inhomogeneous due to the centrifugal force, which literally pushes the liquid outwards the axis of rotation. Therefore, we suspect that the gluon plasma develops inhomogeneity in a rotating state, and this inhomogeneity has an imprint on its phase structure, with the phases close to the axis of rotation and far from the axis of rotation being different.

In Fig. 1, we show a local structure of the Polyakov loop in the gluon plasma for a fixed temperature and various values of Ω_I . The lattice data demonstrates that gluodynamics subjected to imaginary rotation generates an inhomogeneous two-phase structure in thermal equilibrium. There are three notable features of the system:

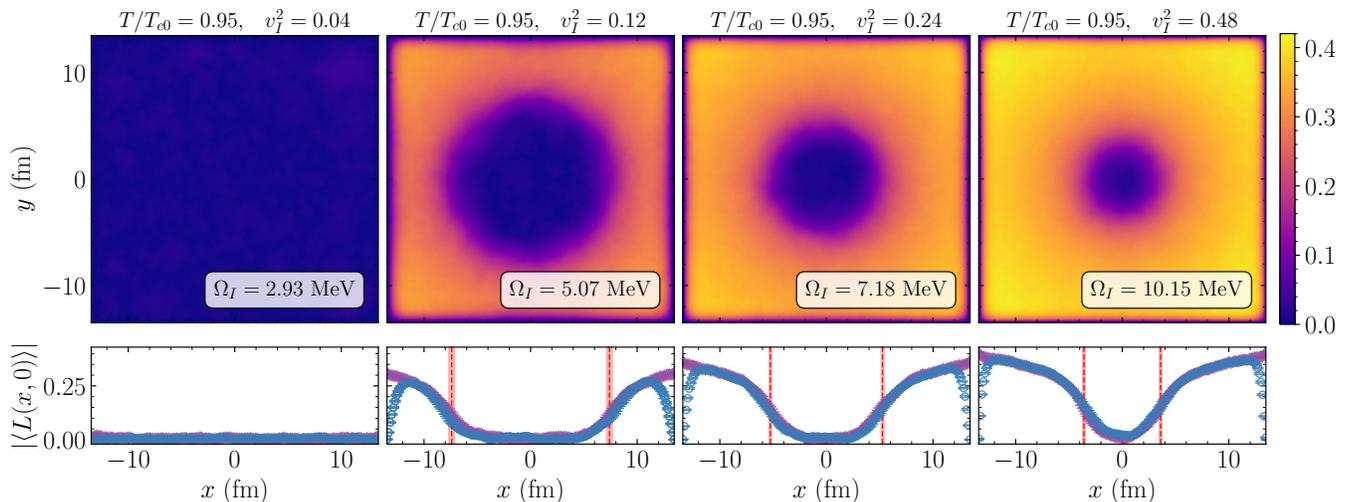


FIG. 1. (top) The distribution of the local Polyakov loop in x, y -plane for lattice of size $5 \times 30 \times 181^2$ with open boundary conditions at the fixed on-axis temperature $T = 0.95 T_{c0}$ and different imaginary angular frequencies (also shown as imaginary velocities at the boundary, $v_I^2 \equiv (\Omega_I R)^2 = 0.04, 0.12, 0.24, 0.48$) with $R = 13.5$ fm. (bottom) The Polyakov loop at the x axis. The vertical lines mark the phase boundaries with shaded uncertainties. The violet (blue) data points correspond to periodic (open) boundary conditions. Movies on the phase evolution with increasing Ω_I are available as ancillary files [39].

1. Imaginary rotation produces the deconfinement phase outside of the rotation axis while the region near the axis stays in the confinement phase. The deconfinement region approaches the rotation axis with the increase of Ω_I ;
2. The outer, deconfining region appears even if the temperature at the rotation axis, T , is lower than the deconfining temperature T_{c0} of a non-rotating gluon matter, $T < T_{c0}$ (so that the whole non-rotating system would reside in the confining phase at this temperature);
3. As the on-axis temperature increases, the radius of the inner confining region shrinks.

On the contrary, if the on-axis temperature T is higher than the deconfining temperature of a non-rotating system, $T > T_{c0}$, then the two-phase structure does not emerge, and the whole imaginary-rotating system resides in the deconfinement phase.

Finalizing this section, we stress that the central confining regions in Fig. 1 have the form of a disk, despite the lattice having a square shape, thus signaling the expected restoration of the rotational symmetry and implying that we work in the physical domain of lattice coupling close to the continuum limit. Moreover, the boundary conditions affect the local phase structure only very near the boundary. The latter property is a result of the short-range nature of the screening, which implies that the boundary effects on the phase structure are negligible [23].

Size of the inhomogeneity. In order to quantitatively study the inhomogeneous phase, it is convenient to introduce the local (pseudo)critical temperature on the

rotation axis $T_c(r)$ for which the system undergoes confinement/deconfinement phase transition at a distance r . One has a confinement phase at distances smaller than r and a deconfinement phase at distances larger than r . The local (pseudo)critical temperature is associated with the position of the peak of the Polyakov loop susceptibility, $\chi_L = \langle |L|^2 \rangle - \langle |L| \rangle^2$ in the parameter space.

At a fixed distance r from the rotation axis, the expectation value of the Polyakov loop and its susceptibility can only be evaluated at a finite number of spatial points proportional to the lattice extension L_z . Since our calculations are performed at finite L_z , a small volume of this lattice submanifold leads to high uncertainty in the determination of the critical temperature. To reduce the associated statistical error, we calculated the mentioned quantities within a thin cylinder $(r - \delta r/2, r + \delta r/2)$. We justified our approach by demonstrating numerically that the finiteness of δr brings only a minor systematic error to the estimation of the critical temperature [40].

In Fig. 2, we present the local (pseudo)critical temperature $T_c(r)$ as a function of distance to the rotation axis for various imaginary angular frequencies, obtained for the averaging width $\delta r \cdot T = 3$ on the lattice with $N_t = 5$. In the absence of rotation, at $\Omega_I = 0$ (not shown in the figure), there is no dependence of the critical temperature at the center on r since the transition appears simultaneously in the whole system. At any nonzero value of Ω_I , the critical temperature at the rotation axis diminishes with the increase of the distance r from the axis of rotation, implying that the imaginary rotation facilitates the transition to the deconfined phase outside of the rotation axis. The stronger the imaginary rotation, the lower the on-axis temperature should be to produce

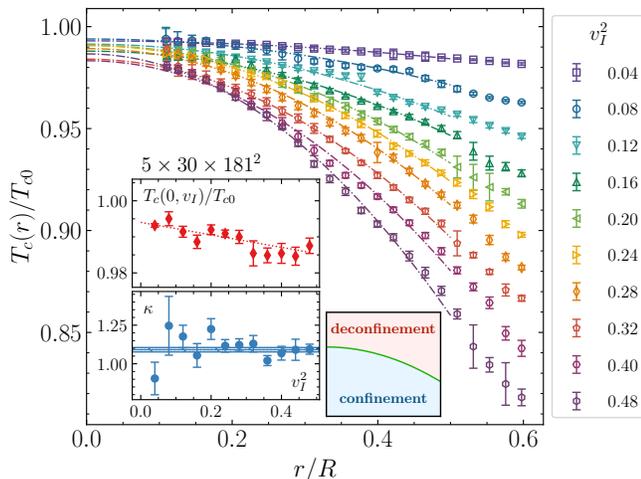


FIG. 2. Temperature $T_c(r)$, shown in units of the $\Omega = 0$ critical temperature T_{c0} of the non-rotating system, which should be imposed at the axis of rotation ($r = 0$) in order to produce the deconfinement phase transition at the distances larger than r from the rotation axis for the gluonic system rotating at various values of the imaginary angular velocity $v_I = \Omega_I R$. The dashed lines are the best quadratic fits by Eq. (6). The insets show the arrangement of the phases for each fixed v_I and the best-fit parameters vs. v_I .

the deconfinement in the medium. [41]

For a moderate radius $r \lesssim 0.5R$, the critical temperature can be fitted, as a function of r , by the simple quadratic formula:

$$\frac{T_c(r, \Omega_I)}{T_{c0}} = \frac{T_c(\Omega_I)}{T_{c0}} - \kappa(\Omega_I)(\Omega_I r)^2, \quad (6)$$

where the transition temperature on the rotation axis, T_c , and the dimensionless ‘‘vortical curvature’’ κ [42] serve as the fitting parameters. The best fits for various angular frequencies are shown in the main plot of Fig. 2.

On-axis transition and vortical curvature.

The results for the fit parameters are shown in the inset of Fig. 2, where the systematic uncertainties associated with the averaging width are taken into account. While both fitting parameters of Eq. (6) should, in general, depend on the imaginary frequency Ω_I , our data, shown in the inset of Fig. 2 as functions of the imaginary velocity at the boundary v_I , unexpectedly indicates that this dependence is almost absent. We believe that this tiny dependence –within a few percent of accuracy– might be attributed to finite N_z effects.

Our result is even more surprising given that the critical temperature of the deconfining transition in *all* analytic calculations available so far is predicted to exhibit a significant dependence on rotation [4–16, 19]. In addition, the previous numerical results that have found a dependence of the critical temperature on Ω_I without specifying the distance of the center of rotation [22–27]

should be understood as the bulk-averaged results. We found a minor dependence of our results on the lattice spacing and obtained a value $\kappa = 0.901(32)$ after continuum limit extrapolation using the data for $N_t = 4, 5, 6$.

Violation of the Tolman-Ehrenfest law.

The TE law (4) suggests that real rotation effectively heats the system outside of the rotation axis. This fact led Ref. [12] to conclude –also supported by a calculation in a low-dimensional confining model– that the outer region of the rotating plasma is hotter than its interior (thus, with $\langle L \rangle \neq 0$ far from the axis and $\langle L \rangle = 0$ close to the axis), which naturally leads to the two-phase structure of the rotating plasma in thermal equilibrium. For imaginary rotation, the TE law is represented by the second equality of the equation (4), which leads to the following two-phase structure: deconfinement at the center and confinement close to the boundaries. This theoretically motivated phase structure is in contradiction with the numerical simulations of this paper. Thus the TE law is violated in rotating gluodynamics.

The Tolman-Ehrenfest law is violated since external gravity, generated by centrifugal forces, influences the dynamics of gluon matter and cannot be accounted for by the simple formula (4). We suggest that this effect appears due to conformal anomaly, which is known to affect the temperature distribution in background gravitational field [43, 44]. This suggestion aligns well with the indication that a condensed-matter counterpart of the TE law, the Luttinger relation [45], is violated in certain materials [46, 47] as a result of the conformal anomaly [47]. Strikingly, it is the conformal anomaly, which, according to Refs. [26, 29], might be responsible for the negative moment of inertia of the gluon plasma [31] so that these exotic effects can be related to each other.

Phase diagram for imaginary and real rotation.

We construct the phase diagram in the (Ω, r) plane using the results for local critical temperature extrapolated to the continuum limit. The radius of the spatial boundary between the confining phase close to the axis and the deconfining phase in an outer region depends on temperature and angular frequency, as shown in Fig. 3. As the rotation increases, the radius separating these phases diminishes. This tendency is observed at all studied temperatures for imaginary rotation. The radius of the phase boundary shrinks to zero when the temperature at the center of the rotating plasma reaches the deconfining temperature of the non-rotating plasma.

For the studied range of temperatures and angular frequencies, the phase diagram, shown in Fig. 3, is precisely the same for imaginary and real rotations up to the swap of the phases. This property follows from the quadratic form of the critical curve (6), with the swap of the phases explained in detail in Fig. 4.

The role of fermions.

While dynamical fermions affect the thermodynamics of QGP, it is the dynamics of

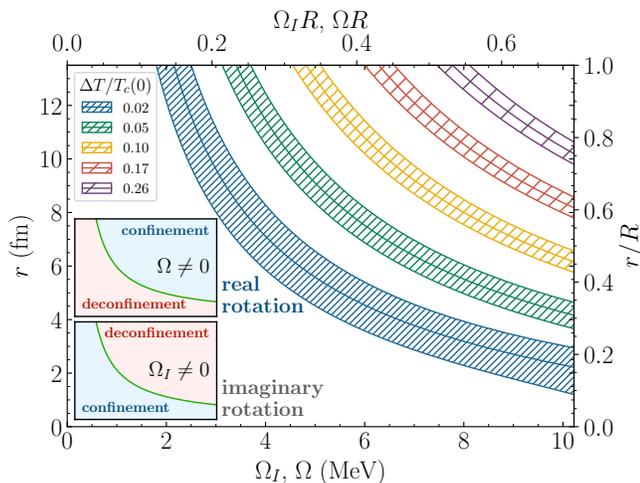


FIG. 3. The critical radius r of the spatial boundary between the confining and deconfining phases for imaginary frequencies Ω_I (at the axis temperature $T = T_{c0} - \Delta T$) and the real frequency Ω (at the axis temperature $T = T_{c0} + \Delta T$) in the experimentally relevant domain of parameters (1) for various temperature offsets $\Delta T > 0$. The size of the system is $R = 13.5$ fm as in Fig. 1. The shading corresponds to a degree of uncertainty around the central curve. The insets show the mutual arrangement of the confining and deconfining phases for real (Ω) and imaginary (Ω_I) angular frequencies, with the details of the analytic continuation given in Fig. 4.

gluons that makes the plasma a perfect fluid possessing an exceptionally low viscosity [48] and determines the hydrodynamics of its evolution. Thus, we expect that the observed inhomogeneous features will also persist in QGP.

Summary and Conclusions. Our results demonstrate that plasma becomes an inhomogeneous medium in which the layers of plasma situated at different distances from the axis of rotation experience the deconfining phase transition at different critical temperatures. Therefore, we conclude that there is no such notion as a single (global) critical temperature for vortical quark-gluon plasma.

One could alternatively try to associate a rotational dependence of the critical temperature with the phase transition at the rotation axis. However, we find the absence of any noticeable dependence of the on-axis critical temperature on the angular frequency with a few percent accuracy. The latter numerical fact poses a delicate question concerning the physical sense of numerous analytical calculations based on different effective models that propose various predictions on the global effect of solid rotation on the critical temperature similar to what happens in the background magnetic field.

We also conclude that the non-perturbative dynamics of the gluon plasma do not comply with the oversimplified picture of the Tolman-Ehrenfest (TE) law, which is based on an analogy with black body radiation.

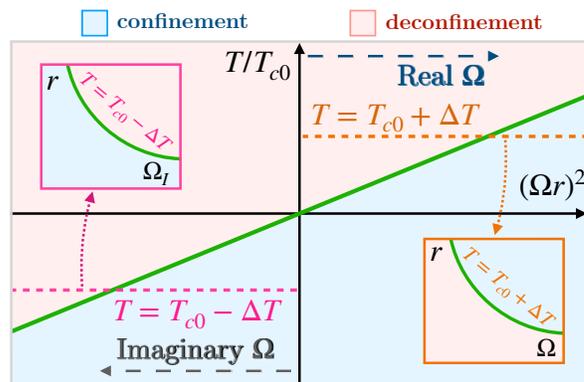


FIG. 4. The analytic continuation for slow rotation, described by Eq. (6), from the imaginary angular frequencies (left) to the real frequencies (right). The insets show how the phase diagrams in, respectively, (Ω_I, r) and (Ω, r) planes look like at a fixed offset $\Delta T > 0$ of the temperature T of rotating plasma with respect to the $\Omega = 0$ critical temperature T_{c0} .

The conventional TE law –the hotter region outside and the colder region closer to the axis of rotation– should work for a non-interacting or weakly interacting gas of particles. The outer regions of the plasma –at least, in the phenomenologically interesting phase-transition region– turned out to be in the confinement phase, which is more appropriate for the colder environment rather than for the hot gas as prescribed by the TE picture. Being cold, the outer region does not essentially rotate.

We claim that the violation of the TE law is a consequence of the conformal anomaly in analogy with a similar effect in condensed matter systems [47]. We suggest that the negative moment of inertia observed in our previous studies [26, 29–31] and the violation of the Tolman-Ehrenfest law found in this paper are linked to each other through a yet-to-be-discovered relationship. This link remains to be explored and is left for future work.

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