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A Unified and General Framework for Argumentation-based Negotiation

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ABSTRACT

This paper proposes a unified and general framework for argumentation-based negotiation, in which the role of argumentation is formally analyzed. The framework makes it possible to study the outcomes of an argumentation-based negotiation. It shows what an agreement is, how it is related to the theories of the agents, when it is possible, and how this can be attained by the negotiating agents in this case. It defines also the notion of concession, and shows in which situation an agent will make one, as well as how it influences the evolution of the dialogue.

Categories and Subject Descriptors

I.2.3 [Deduction and Theorem Proving]: Nonmonotonic reasoning and belief revision
I.2.11 [Distributed Artificial Intelligence]: Intelligent agents

General Terms

Human Factors, Theory

Keywords

Argumentation, Negotiation

1. INTRODUCTION

Roughly speaking, negotiation is a process aiming at finding some compromise or consensus between two or several agents about some matters of collective agreement, such as pricing products, allocating resources, or choosing candidates. Negotiation models have been proposed for the design of systems able to bargain in an optimal way with other agents for example, buying or selling products in e-commerce.

Different approaches to automated negotiation have been investigated, including game-theoretic approaches (which usually assume complete information and unlimited computation capabilities) [11], heuristic-based approaches which try to cope with these limitations [6], and argumentation-based approaches [2, 3, 7, 8, 9, 12, 13] which emphasize the importance of exchanging information and explanations between negotiating agents in order to mutually influence their behaviors (e.g. an agent may concede a goal having a small priority), and consequently the outcome of the dialogue. Indeed, the two first types of settings do not allow for the addition of information or for exchanging opinions about offers. Integrating argumentation theory in negotiation provides a good means for supplying additional information and also helps agents to convince each other by adequate arguments during a negotiation dialogue. Indeed, an offer supported by a good argument has a better chance to be accepted by an agent, and can also make him reveal his goals or give up some of them. The basic idea behind an argumentation-based approach is that by exchanging arguments, the theories of the agents (i.e. their mental states) may evolve, and consequently, the status of offers may change. For instance, an agent may reject an offer because it is not acceptable for it. However, the agent may change its mind if it receives a strong argument in favor of this offer.

Several proposals have been made in the literature for modeling such an approach. However, the work is still preliminary. Some researchers have mainly focused on relating argumentation with protocols. They have shown how and when arguments in favor of offers can be computed and exchanged. Others have emphasized on the decision making problem. In [3, 7], the authors argued that selecting an offer to propose at a given step of the dialogue is a decision making problem. They have thus proposed an argumentation-based decision model, and have shown how such a model can be related to the dialogue protocol.

In most existing works, there is no deep formal analysis of the role of argumentation in negotiation dialogues. It is not clear how argumentation can influence the outcome of the dialogue. Moreover, basic concepts in negotiation such as agreement (i.e. optimal solutions, or compromise) and concession are neither defined nor studied.

This paper aims to propose a unified and general framework for argumentation-based negotiation, in which the role of argumentation is formally analyzed, and where the existing systems can be restated. In this framework, a negotiation dialogue takes place between two agents on a set \( O \) of offers, whose structure is not known. The goal of a negotiation is to find among elements of \( O \), an offer that satisfies more or less
the preferences of both agents. Each agent is supposed to have a theory represented in an abstract way. A theory consists of a set \( A \) of arguments whose structure and origin are not known, a function specifying for each possible offer in \( O \), the arguments of \( A \) that support it, a non specified conflict relation among the arguments, and finally a preference relation between the arguments. The status of each argument is defined using Dung’s acceptability semantics. Consequently, the set of offers is partitioned into four subsets: acceptable, rejected, negotiable and non-supported offers. We show how an agent’s theory may evolve during a negotiation dialogue. We define formally the notions of concession, compromise, and optimal solution. Then, we propose a protocol that allows agents i) to exchange offers and arguments, and ii) to make concessions when necessary. We show that dialogues generated under such a protocol terminate, and even reach optimal solutions when they exist.

This paper is organized as follows: Section 2 introduces the logical language that is used in the rest of the paper. Section 3 defines the agents as well as their theories. In section 4, we study the properties of these agents’ theories. Section 5 defines formally an argumentation-based negotiation, shows how the theories of agents may evolve during a dialogue, and how this evolution may influence the outcome of the dialogue. Two kinds of outcomes: optimal solution and compromise are defined, and we show when such outcomes are reached. Section 6 illustrates our general framework through some examples. Section 7 compares our formalism with existing ones. Section 8 concludes and presents some perspectives. Due to lack of space, the proofs are not included. These last are in a technical report that we will make available online at some later time.

2. THE LOGICAL LANGUAGE

In what follows, \( \mathcal{L} \) will denote a logical language, and \( \equiv \) is an equivalence relation associated with it. From \( \mathcal{L} \), a set \( O = \{o_1, \ldots, o_n\} \) of \( n \) offers is identified, such that \( \exists o_i, o_j \in O \) such that \( o_i \equiv o_j \). This means that the offers are different. Offers correspond to the different alternatives that can be exchanged during a negotiation dialogue. For instance, if the agents try to decide the place of their next meeting, then the set \( O \) will contain different towns. Different arguments can be built from \( \mathcal{L} \). The set \( \text{Args}(\mathcal{L}) \) will contain all those arguments. By argument, we mean a reason in believing or of doing something. In [3], it has been argued that the selection of the best offer to propose at a given step of the dialogue is a decision problem. In [4], it has been shown that in an argumentation-based approach for decision making, two kinds of arguments are distinguished: arguments supporting choices (or decisions), and arguments supporting beliefs. Moreover, it has been acknowledged that the two categories of arguments are formally defined in different ways, and they play different roles. Indeed, an argument in favor of a decision, built both on an agent’s beliefs and goals, tries to justify the choice; whereas an argument in favor of a belief, built only from beliefs, tries to destroy the decision arguments, in particular the beliefs part of those decision arguments. Consequently, in a negotiation dialogue, those two kinds of arguments are generally exchanged between agents. In what follows, the set \( \text{Args}(\mathcal{L}) \) is then divided into two subsets: a subset \( \text{Args}_a(\mathcal{L}) \) of arguments supporting offers, and a subset \( \text{Args}_b(\mathcal{L}) \) of arguments supporting beliefs. Thus, \( \text{Args}(\mathcal{L}) = \text{Args}_a(\mathcal{L}) \cup \text{Args}_b(\mathcal{L}) \).

As in [5], in what follows, we consider that the structure of the arguments is not known. Since the knowledge bases from which arguments are built may be inconsistent, the arguments may be conflicting too. In what follows, those conflicts will be captured by the relation \( \mathcal{R}_c \), thus \( \mathcal{R}_c \subseteq \text{Args}(\mathcal{L}) \times \text{Args}(\mathcal{L}) \). Three assumptions are made on this relation: First the arguments supporting different offers are conflicting. The idea behind this assumption is that since offers are exclusive, an agent has to choose only one at a given step of the dialogue. Note that, the relation \( \mathcal{R}_c \) is not necessarily symmetric between the arguments of \( \text{Args}_b(\mathcal{L}) \). The second hypothesis says that arguments supporting the same offer are also conflicting. The idea here is to return the strongest argument among these arguments. The third condition does not allow an argument in favor of an offer to attack an argument supporting a belief. This avoids wishful thinking. Formally:

**Definition 1.** \( \mathcal{R}_c \subseteq \text{Args}(\mathcal{L}) \times \text{Args}(\mathcal{L}) \) is a conflict relation among arguments such that:

- \( \forall a, a' \in \text{Args}_a(\mathcal{L}), \) s.t. \( a \neq a' \), a \( \mathcal{R}_c a' \)
- \( \exists a \in \text{Args}_a(\mathcal{L}) \) and \( a' \in \text{Args}_b(\mathcal{L}) \) such that a \( \mathcal{R}_c a' \)

Note that the relation \( \mathcal{R}_c \) is not symmetric. This is due to the fact that arguments of \( \text{Args}_a(\mathcal{L}) \) may be conflicting but not necessarily in a symmetric way. In what follows, we assume that the set \( \text{Args}(\mathcal{L}) \) of arguments is finite, and each argument is attacked by a finite number of arguments.

3. NEGOTIATING AGENTS THEORIES AND REASONING MODELS

In this section we define formally the negotiating agents, i.e. their theories, as well as the reasoning model used by those agents in a negotiation dialogue.

3.1 Negotiating agents theories

Agents involved in a negotiation dialogue, called negotiating agents, are supposed to have theories. In this paper, the theory of an agent will not refer, as usual, to its mental states (i.e. its beliefs, desires and intentions). However, it will be encoded in a more abstract way in terms of the arguments owned by the agent, a conflict relation among those arguments, a preference relation between the arguments, and a function that specifies which arguments support offers of the set \( O \). We assume that an agent is aware of all the arguments of the set \( \text{Args}(\mathcal{L}) \). The agent is even able to express a preference between any pair of arguments. This does not mean that the agent will use all the arguments of \( \text{Args}(\mathcal{L}) \), but it encodes the fact that when an agent receives an argument from another agent, it can interpret it correctly, and it can also compare it with its own arguments. Similarly, each agent is supposed to be aware of the conflicts between arguments. This also allows us to encode the fact that an agent can recognize whether the received argument is in conflict or not with its arguments. However, in its theory, only the conflicts between its own arguments are considered.

**Definition 2.** (Negotiating Agent Theory). Let \( O \) be a set of \( n \) offers. A negotiating agent theory is a tuple \( \langle A, \mathcal{F}, \succeq, (R, \text{Def}) \rangle \) such that:

- \( A \subseteq \text{Args}(\mathcal{L}) \).
The function $F$ offer is not supported at all by arguments, thus for simplicity reasons, in this paper we consider only arguments supporting it, called arguments PRO, and arguments others.

Following theory is the theory of agent for computing the status of arguments. These are based on two basic concepts, defence and conflict-free, defined as follows:

**Definition 4** (Defence/conflict-free). Let $S \subseteq A$.

- $S$ defends an argument $a$ iff each argument that defeats $a$ is defeated by some argument in $S$.
- $S$ is conflict-free iff there exist no $a, a' \in S$ such that $a \text{ Def } a'$.

**Definition 5** (Acceptability semantics). Let $S$ be a conflict-free set of arguments, and let $T: 2^A \rightarrow 2^A$ be a function such that $T(S) = \{a | a$ is defended by $S\}$.

- $S$ is a complete extension iff $S = T(S)$.
- $S$ is a preferred extension iff $S$ is a maximal (w.r.t set $\subseteq$) complete extension.
- $S$ is a grounded extension iff it is the smallest (w.r.t set $\subseteq$) complete extension.

Let $E_1, \ldots, E_x$ denote the different extensions under a given semantics.

Note that there is only one grounded extension. It contains all the arguments that are not defeated, and those arguments that are defended directly or indirectly by non-defeated arguments.

**Theorem 1.** Let $\langle A, \text{Def} \rangle$ the argumentation system defined as shown above.

1. It may have $x \geq 1$ preferred extensions.

2. The grounded extensions is $S = \bigcup_{i=1}^{x} T(\emptyset)$.

From the above definition of agent theory, the following hold:

**Property 1.**

- $\forall a, a' \in F(o_i), a \text{ R } a'$

### 3.2 The reasoning model

From the theory of an agent, one can define the argumentation system used by that agent for reasoning about the offers and the arguments, i.e. for computing the status of the different offers and arguments.

**Definition 3** (Argumentation system). Let $\langle A, F, \geq, R, \text{Def} \rangle$ be the theory of an agent. The argumentation system of that agent is the pair $\langle A, \text{Def} \rangle$.

In [5], different acceptability semantics have been introduced for computing the status of arguments. These are based on two basic concepts, defence and conflict-free, defined as follows:

**Definition 4** (Defence/conflict-free). Let $S \subseteq A$.

- $S$ defends an argument $a$ iff each argument that defeats $a$ is defeated by some argument in $S$.
- $S$ is conflict-free iff there exist no $a, a' \in S$ such that $a \text{ Def } a'$.
• The offer \( o \) is negotiable if and only if \( \forall a \in \mathcal{F}(o), a \) is undecided.

\[ \mathcal{O}_n = \{ o_i \in \mathcal{O}, \text{ such that } o_i \text{ is negotiable} \} \]

• The offer \( o \) is non-supported iff it is neither acceptable, nor rejected or negotiable. \( \mathcal{O}_{ns} = \{ o_i \in \mathcal{O}, \text{ such that } o_i \text{ is non-supported offers} \} \).

**Example 4.** In example 1, the two offers \( o_1 \) and \( o_2 \) are acceptable since they are supported by accepted arguments, whereas the offer \( o_3 \) is non-supported since it has no argument in its favor.

From the above definitions, the following results hold:

**Property 2.** Let \( o \in \mathcal{O} \).

• \( \mathcal{O} = \mathcal{O}_a \cup \mathcal{O}_r \cup \mathcal{O}_n \cup \mathcal{O}_{ns} \).

• The set \( \mathcal{O}_a \) may contain more than one offer.

From the above partition of the set \( \mathcal{O} \) of offers, a preference relation between offers is defined. Let \( \mathcal{O}_a \) and \( \mathcal{O}_r \) be two subsets of \( \mathcal{O} \). \( \mathcal{O}_a \triangleright \mathcal{O}_r \) means that any offer in \( \mathcal{O}_a \) is preferred to any offer in the set \( \mathcal{O}_r \). We can write also for two offers \( o_i, o_j \), \( o_i \triangleright o_j \) iff \( o_i \in \mathcal{O}_a, o_j \in \mathcal{O}_r \) and \( \mathcal{O}_a \triangleright \mathcal{O}_r \).

**Definition 8.** (Preference between offers) Let \( \mathcal{O} \) be a set of offers, and \( \mathcal{O}_a, \mathcal{O}_r, \mathcal{O}_n, \mathcal{O}_{ns} \) its partition. \( \mathcal{O}_a \triangleright \mathcal{O}_r \triangleright \mathcal{O}_n \triangleright \mathcal{O}_{ns} \).

**Example 5.** In example 1, we have \( o_1 \triangleright o_3 \), and \( o_2 \triangleright o_3 \). However, \( o_1 \) and \( o_2 \) are indifferent.

### 4. The Structure of Negotiation Theories

In this section, we study the properties of the system developed above. We first show that in the particular case where \( A = \mathcal{A}_O \) (ie. all of the agent’s arguments refer to offers), the corresponding argumentation system will return at least one non-empty preferred extension.

**Theorem 2.** Let \( \langle A, \text{Def} \rangle \) an argumentation system such that \( A = \mathcal{A}_O \). Then the system returns at least one extension \( \mathcal{E} \), such that \( |\mathcal{E}| \geq 1 \).

We now present some results that demonstrate the importance of indifference in negotiating agents, and more specifically its relation to acceptable outcomes. We first show that the set \( \mathcal{O}_a \) may contain several offers when their corresponding accepted arguments are indifferent w.r.t the preference relation \( \succeq \).

**Theorem 3.** Let \( o_1, o_2 \in \mathcal{O} \). \( o_1, o_2 \in \mathcal{O}_a \) iff \( \exists a_1 \in \mathcal{F}(o_1), \exists a_2 \in \mathcal{F}(o_2), \text{ such that } a_1 \text{ and } a_2 \text{ are accepted and are indifferent w.r.t } \succeq \) (i.e. \( a \succeq b \text{ and } b \succeq a \)).

We now study acyclic preference relations that are defined formally as follows.

**Definition 9.** (Acyclic relation) A relation \( R \) on a set \( A \) is acyclic if there is no sequence \( a_1, a_2, \ldots, a_n \in A \), with \( n > 1 \), such that \( (a_i, a_{i+1}) \in R \) and \( (a_n, a_1) \in R \), with \( 1 \leq i < n \).

We note that acyclicity prohibits pairs of arguments \( a, b \) such that \( a \succeq b \text{ and } b \succeq a \), ie., an acyclic preference relation disallows indifference.

**Theorem 4.** Let \( A \) be a set of arguments, \( R \) the attacking relation of \( A \) defined as \( R \subseteq A \times A \), and \( \succeq_1 \) an acyclic relation on \( A. \) Then for any pair of arguments \( a, b \in A \), such that \( (a, b) \in R \), either \( (a, b) \in \text{Def} \text{ or } (b, a) \in \text{Def} \) (or both).

The previous result is used in the proof of the following theorem that states that acyclic preference relations sanction extensions that support exactly one offer.

**Theorem 5.** Let \( A \) be a set of arguments, and \( \succeq_1 \) an acyclic relation on \( A. \) If \( \mathcal{E} \) is an extension of \( \langle A, \text{Def} \rangle \), then \( |\mathcal{E} \cap \mathcal{A}_O| = 1 \).

An immediate consequence of the above is the following.

**Property 3.** Let \( A \) be a set of arguments such that \( A = \mathcal{A}_O \). If the relation \( \succeq_1 \) on \( A \) is acyclic, then each extension \( \mathcal{E}_i \) of \( \langle A, \text{Def} \rangle \), \( |\mathcal{E}_i| = 1 \).

Another direct consequence of the above theorem is that in acyclic preference relations, arguments that support offers may participate in only one preferred extension.

**Theorem 6.** Let \( A \) be a set of arguments, and \( \succeq_1 \) an acyclic relation on \( A. \) Then the preferred extensions of \( \langle A, \text{Def} \rangle \) are pairwise disjoint w.r.t arguments of \( \mathcal{A}_O \).

Using the above results we can prove the main theorem of this section that states that negotiating agents with acyclic preference relations do not have acceptable offers.

**Theorem 7.** Let \( \langle A, \mathcal{F}, R, \succeq, \text{Def} \rangle \) be a negotiating agent such that \( A = \mathcal{A}_O \) and \( \succeq_1 \) is an acyclic relation. Then the set of accepted arguments w.r.t \( \langle A, \text{Def} \rangle \) is empty. Consequently, the set of acceptable offers, \( \mathcal{O}_a \) is empty as well.

### 5. Argumentation-Based Negotiation

In this section, we define formally a protocol that generates argumentation-based negotiation dialogues between two negotiating agents \( P \) and \( C \). The two agents negotiate about an object whose possible values belong to a set \( O \). This set \( O \) is supposed to be known and the same for both agents. For simplicity reasons, we assume that this set does not change during the dialogue. The agents are equipped with theories denoted respectively \( \langle \mathcal{A}^P, \mathcal{F}^P, \succeq^P, R^P, \text{Def}^P \rangle \), and \( \langle \mathcal{A}^C, \mathcal{F}^C, \succeq^C, R^C, \text{Def}^C \rangle \). Note that the two theories may be different in the sense that the agents may have different sets of arguments, and different preference relations. Worst yet, they may have different arguments in favor of the same offers. Moreover, these theories may evolve during the dialogue.

#### 5.1 Evolution of the theories

Before defining formally the evolution of an agent’s theory, let us first introduce the notion of dialogue moves, or moves for short.

**Definition 10.** (Move) A move is a tuple \( m = \langle p_i, a_i, o_i, t_i \rangle \) such that:

- \( p_i \in \{ P, C \} \)
- \( a_i \in \text{Args}(\mathcal{L}) \cup \emptyset \)

1In what follows \( \emptyset \) denotes the fact that no argument, or no offer is given.
The function Player (resp. Argument, Offer, Target) returns the player of the move \(i.e., p_i\) (resp. the argument of a move, \(i.e., a_i\), the offer \(o_i\), and the target of the move, \(t_i\)). Let \(M\) denote the set of all the moves that can be built from \(\{P, C\}, \text{Arg}(L), O\).

Note that the set \(M\) is finite since \(\text{Arg}(L)\) and \(O\) are assumed to be finite. Let us now see how an agent’s theory evolves and why. The idea is that if an agent receives an argument from another agent, it will add the new argument to its theory. Moreover, since an argument may bring new information for the agent, thus new arguments can emerge. Let us take the following example:

**Example 6.** Suppose that an agent \(P\) has the following propositional knowledge base: \(\Sigma_P = \{x, y \rightarrow z\}\). From this base one cannot deduce \(z\). Let’s assume that this agent receives the following argument \(\{a, a \rightarrow y\}\) that justifies \(y\). It is clear that now \(P\) can build an argument, say \(\{a, a \rightarrow y, y \rightarrow z\}\) in favor of \(z\).

In a similar way, if a received argument is in conflict with the arguments of the agent \(i\), then those conflicts are also added to its relation \(R^i\). Note that new conflicts may arise between the original arguments of the agent and the ones that emerge after adding the received arguments to its theory. Those new conflicts should also be considered. As a direct consequence of the evolution of the sets \(A^i\) and \(R^i\), the defeat relation \(\text{Def}^i\) is also updated.

The initial theory of an agent \(i\), (i.e. its theory before the dialogue starts), is denoted by \(\langle A^0_i, F^0_i, \geq^0_i, R^0_i, \text{Def}^0_i, a, n, r, ns \rangle\), with \(i \in \{P, C\}\). Besides, in this paper, we suppose that the preference relation \(\geq^i\) of an agent does not change during the dialogue.

**Definition 11 (Theory evolution).** Let \(m_1, \ldots, m_t, \ldots, m_i, \ldots, m_j\) be a sequence of moves. The theory of an agent \(i\) at a step \(t > 0\) is: \(\langle A^t_i, F^t_i, \geq^t_i, R^t_i, \text{Def}^t_i, a, n, r, ns \rangle\) such that:

- \(A^t_i = A^0_i \cup \{a_i, i = 1, \ldots, t, a_i = \text{Argument}(m_i)\} \cup A^t_i \not\subseteq A^t_i \cup \text{Arg}(L)\)
- \(F^t_i = O \rightarrow 2A^t_i\)
- \(\geq^t_i = \geq^0_i\)
- \(R^t_i = R^0_i \cup \{\{a_i, a_j\} \mid a_i = \text{Argument}(m_j), a_j = \text{Argument}(m_i), i < j \leq t, \text{and } R^i \subseteq R^j \}\)
- \(\text{Def}^t_i \subseteq A^t_i \times A^t_i\)

The above definition captures the monotonic aspect of an argument. Indeed, an argument cannot be removed. However, its status may change. An argument that is accepted at step \(t\) of the dialogue by an agent may become rejected at step \(t + i\). Consequently, the status of offers also change. Thus, the sets \(O_x, O_1, O_2, O_3\), and \(O_4\) may change from one step of the dialogue to another. That means for example that some offers could move from the set \(O_x\) to the set \(O_1\) and vice-versa. Note that in the definition of \(R^t_i\), the relation \(R^t\) is used to denote a conflict between exchanged arguments. The reason is that, such a conflict may not be in the set \(R^t\) of the agent \(i\). Thus, in order to recognize such conflicts, we have supposed that the set \(R^t\) is known to the agents. This allows us to capture the situation where an agent is able to prove an argument that it was unable to prove before, by incorporating in its beliefs some information conveyed through the exchange of arguments with another agent. This, unknown at the beginning of the dialogue argument, could give to this agent the possibility to defeat an argument that it could not by using its initial arguments. This could even lead to a change of the status of these initial arguments and this change would lead to the one of the associated offers’ status.

In what follows, \(O^t\), \(t \geq 0\), denotes the set of offers of type \(x\), where \(x \in \{a, n, r, ns\}\), of the agent \(i\) at step \(t\) of the dialogue. In some places, we can use for short the notation \(O^t_i\) to denote the partition of the set \(O\) at step \(t\) for agent \(i\). Note that we have: \(\text{not}(O^t_i, x) \subseteq O^t_{i+1, x}\).

### 5.2 The notion of agreement

As said in the introduction, negotiation is a process aiming at finding an agreement about some matters. By agreement, one means a solution that satisfies to the largest possible extent the preferences of both agents. In case there is no such solution, we say that the negotiation fails. In what follows, we will discuss the different kinds of solutions that may be reached in a negotiation. The first one is the optimal solution. An optimal solution is the best offer for both agents. Formally:

**Definition 12 (Optimal solution).** Let \(O\) be a set of offers, and \(o \in O\). The offer \(o\) is an optimal solution at a step \(t \geq 0\) if \(o \in O^t_{i,a} \cap O^t_{j,a}\).

Such a solution does not always exist since agents may have conflicting preferences. Thus, agents make concessions by proposing/accepting less preferred offers.

**Definition 13 (Concession).** Let \(o \in O\) be an offer. The offer \(o\) is a concession for an agent \(i\) iff \(o \in O^t_{i,a}\).

During a negotiation dialogue, agents exchange first their most preferred offers, and if these last are rejected, they make concessions. In this case, we say that their best offers are no longer defendable. In an argumentation setting, this means that the agent has already presented all its arguments supporting its best offers, and it has no counter argument against the ones presented by the other agent. Formally:

**Definition 14 (Defendable offer).** Let \(\langle A^t_i, F^t_i, \geq^t_i, R^t_i, \text{Def}^t_i \rangle\) be the theory of agent \(i\) at a step \(t \geq 0\) of the dialogue. Let \(o \in O\) such that \(\exists j \leq t \text{ with } \text{Player}(m_j) = i \text{ and offer}(m_j) = o\). The offer \(o\) is defendable by the agent \(i\) iff:

- \(\exists a \in F^t_i(o), \exists k \leq t \text{ s.t. } \text{Argument}(m_k) = a, \text{ or} \)
- \(\exists a \in A^t_i \setminus F^t_i(o) \text{ s.t. a Def}^t_i b \text{ with} \)
  - \(\text{Argument}(m_k) = b, k \leq t, \text{ and Player}(m_k) \neq i \)
  - \(\exists l \leq t, \text{Argument}(m_l) = a \)

The offer \(o\) is said non-defendable otherwise and \(ND^t_i\) is the set of non-defendable offers of agent \(i\) at a step \(t\).
5.3 Negotiation dialogue

Now that we have shown how the theories of the agents evolve during a dialogue, we are ready to define formally an argumentation-based negotiation dialogue. For that purpose, we need to define first the notion of a legal continuation.

Definition 15 (Legal move). A move \( m \) is a legal continuation of a sequence of moves \( m_1, \ldots, m_i \) iff \( \exists j, k < l \), such that:

- \( \text{Offer}(m_j) = \text{Offer}(m_k) \), and
- \( \text{Player}(m_j) \neq \text{Player}(m_k) \)

The idea here is that if the two agents present the same offer, then the dialogue should terminate, and there is no longer possible continuation of the dialogue.

Definition 16 (Argumentation-based negotiation). An argumentation-based negotiation dialogue \( d \) between two agents \( P \) and \( C \) is a non-empty sequence of moves \( m_1, \ldots, m_i \), such that:

- \( p_i = P \) if \( i \) is even, and \( p_i = C \) if \( i \) is odd
- \( \text{Player}(m_1) = P \), \( \text{Argument}(m_1) = \theta \), \( \text{Offer}(m_1) \neq \theta \), and \( \text{Target}(m_1) = \emptyset \)
- \( \forall m_i, \text{if} \: \text{Offer}(m_i) = \emptyset, \text{then} \: \text{Offer}(m_i) \supset a_j, \forall a_j \in \text{O}(\text{Player}(m_i) \cup \text{ND}^{\text{Player}(m_i)}) \)
- \( \forall i = 1, \ldots, l, m_i \) is a legal continuation of \( m_1, \ldots, m_{i-1} \)
- \( \text{Target}(m_i) = m_j \) such that \( j < i \) and \( \text{Player}(m_i) \neq \text{Player}(m_j) \)
- If \( \text{Argument}(m_i) \neq \emptyset \), then:
  - \( \text{if} \: \text{Offer}(m_i) = \emptyset \) then \( \text{Argument}(m_i) \in \mathcal{F}(\text{Offer}(m_i)) \)
  - \( \text{if} \: \text{Offer}(m_i) = \emptyset \) then \( \text{Argument}(m_i) \in \text{Def}_{\text{Player}(m_i)}^{\text{Target}(m_i)} \)
- \( \exists i, j \leq l \) such that \( m_i = m_j \)
- \( \exists m \in \mathcal{M} \) such that \( m \) is a legal continuation of \( m_1, \ldots, m_i \)

Let \( D \) be the set of all possible dialogues.

The first condition says that the two agents take turn. The second condition says that agent \( P \) starts the negotiation dialogue by presenting an offer. Note that, in the first turn, we suppose that the agent does not present an argument. This assumption is made for strategical purposes. Indeed, arguments are exchanged as soon as a conflict appears. The third condition ensures that agents exchange their best offers, but never the rejected ones. This condition takes also into account the concessions that an agent will have to make if it was established that a concession is the only option for it at the current state of the dialogue. Of course, as we have shown in a previous section, an agent may have several good or acceptable offers. In this case, the agent chooses one of them randomly. The fourth condition ensures that the moves are legal. This condition allows to terminate the dialogue as soon as an offer is presented by both agents. The fifth condition allows agents to backtrack. The sixth condition says that an agent may send arguments in favor of offers, and in this case the offer should be stated in the same move. An agent can also send arguments in order to defeat arguments of the other agent. The next condition prevents repeating the same move. This is useful for avoiding loops. The last condition ensures that all the possible legal moves have been presented.

The outcome of a negotiation dialogue is computed as follows:

Definition 17 (Dialogue outcome). Let \( d = m_1, \ldots, m_i \) be an argumentation-based negotiation dialogue. The outcome of this dialogue, denoted \( \text{Outcome}(d) \), is \( \text{Outcome}(d) = \text{Offer}(m_i) \) iff \( \exists j < l \) s.t. \( \text{Offer}(m_i) = \text{Offer}(m_j) \), and \( \text{Player}(m_i) \neq \text{Player}(m_j) \). Otherwise, \( \text{Outcome}(d) = \emptyset \).

Note that when \( \text{Outcome}(d) = \emptyset \), the negotiation fails, and no agreement is reached by the two agents. However, if \( \text{Outcome}(d) \neq \emptyset \), the negotiation succeeds, and a solution that is either optimal or a compromise is found.

Theorem 8. \( \forall d \in D \), the argumentation-based negotiation \( d \), terminates.

The above result is of great importance, since it shows that the proposed protocol avoids loops, and dialogues terminate. Another important result shows that the proposed protocol ensures to reach an optimal solution if it exists. Formally:

Theorem 9 (Completeness). Let \( d = m_1, \ldots, m_i \) be an argumentation-based negotiation dialogue. If \( \exists l \) such that \( \mathcal{O}^i_{t,a} \cap \mathcal{O}^i_{t,b} \neq \emptyset \), then \( \text{Outcome}(d) \in \mathcal{O}^i_{t,a} \). \( \mathcal{O}^i_{t,a} \cap \mathcal{O}^i_{t,b} \).

We show also that the proposed dialogue protocol is sound in the sense that, if a dialogue returns a solution, then that solution is for sure a compromise. In other words, that solution is a “common agreement” at a given step of the dialogue. We show also that if the negotiation fails, then there is no possible solution.

Theorem 10 (Soundness). Let \( d = m_1, \ldots, m_i \) be an argumentation-based negotiation dialogue.

1. If \( \text{Outcome}(d) = \emptyset \), \( \emptyset \neq \theta \), then \( \exists l \leq l \) such that \( \emptyset \in \mathcal{O}^i_{t,x} \cup \mathcal{O}^i_{t,y} \), with \( x, y \in \{a, n, ns\} \).

2. If \( \text{Outcome}(d) = \emptyset \), then \( \forall l \leq l \), \( \mathcal{O}^i_{t,x} \cap \mathcal{O}^i_{t,y} = \emptyset \), \( \forall x, y \in \{a, n, ns\} \).

A direct consequence of the above theorem is the following:

Property 4. Let \( d = m_1, \ldots, m_i \) be an argumentation-based negotiation dialogue. If \( \text{Outcome}(d) = \emptyset \), then \( \forall l \leq l \),

- \( \mathcal{O}^i_{t,x} = \mathcal{O}^i_{t,a} \cup \mathcal{O}^i_{t,n} \cup \mathcal{O}^i_{t,ns} \), and
- \( \mathcal{O}^i_{t,y} = \mathcal{O}^i_{t,a} \cup \mathcal{O}^i_{t,n} \cup \mathcal{O}^i_{t,ns} \).

6. ILLUSTRATIVE EXAMPLES

In this section we will present some examples in order to illustrate our general framework.

Example 7 (No argumentation). Let \( \mathcal{O} = \{o_1, o_2\} \) be the set of all possible offers. Let \( P \) and \( C \) be two agents, equipped with the same theory: \( \langle A, F, \succeq, R, \text{Def} \rangle \) such that \( A = \emptyset \), \( F(o_1) = F(o_2) = \emptyset \), \( \succeq = \emptyset \), \( R = \emptyset \), \( \text{Def} = \emptyset \). In this case, it is clear that the two agents \( o_1 \) and \( o_2 \) are unsupported. The proposed protocol (see Definition 16) will generate one of the following dialogues:
Both dialogues end with failure. Note that in both dialogues, the theories of both agents do not change. The reason is that the exchanged arguments are already known to both agents. The negotiation fails because the agents have conflicting preferences.

Let us now consider an example in which argumentation will allow agents to reach an agreement.

Example 9 (Dynamic theories). Let $O = \{a_1, a_2\}$ be the set of all possible offers. The theory of agent $P$ is $(\mathcal{A}^P, \mathcal{F}^P, \succeq^P, \mathcal{R}^P, \text{Def}^P)$ such that: $\mathcal{A}^P = \{a_1, a_2\}$, $\mathcal{F}^P(a_1) = \{a_1\}$, $\mathcal{F}^P(a_2) = \{a_2\}$, $\succeq^P = \{(a_1, a_2),(a_2, a_1)\}$, $\mathcal{R}^P = \{(a_1,a_2),(a_2,a_1)\}$, $\text{Def}^P = \{(a_1, a_2)\}$. The argumentation system $(\mathcal{A}^P, \text{Def}^P)$ of this agent will return $a_1$ as an accepted argument, and $a_2$ as a rejected one. Consequently, the offer $a_1$ is acceptable and $a_2$ is rejected.

The theory of agent $C$ is $(\mathcal{A}^C, \mathcal{F}^C, \succeq^C, \mathcal{R}^C, \text{Def}^C)$ such that: $\mathcal{A}^C = \{a_1, a_2\}$, $\mathcal{F}^C(a_1) = \{a_1\}$, $\mathcal{F}^C(a_2) = \{a_2\}$, $\succeq^C = \{(a_1, a_2),(a_2, a_1)\}$, $\mathcal{R}^C = \{(a_1,a_2),(a_2,a_1)\}$, $\text{Def}^C = \{(a_1, a_2),(a_3, a_1)\}$. The argumentation system $(\mathcal{A}^C, \text{Def}^C)$ of this agent will return $a_3$ as an accepted argument, and $a_1$ as a rejected one. Consequently, the offer $a_2$ is acceptable and $a_1$ is rejected.

The following dialogue may take place between the two agents:

P: $m_1 = \langle P, \theta, o_1, 0 \rangle$
C: $m_2 = \langle C, \theta, o_2, 1 \rangle$
P: $m_3 = \langle P, a_1, o_1, 2 \rangle$
C: $m_4 = \langle C, a_2, o_2, 3 \rangle$

At step 4 of the dialogue, the agent $P$ receives the argument $a_3$ from $P$. Thus, its theory evolves as follows: $\mathcal{A}^P = \{a_1, a_2, a_3\}$, $\mathcal{F}^P = \{(a_1, a_2),(a_2, a_1),(a_3,a_1)\}$, $\text{Def}^P = \{(a_1, a_2),(a_3, a_1)\}$. At this step, the argument $a_1$ which was accepted will become rejected, and the argument $a_2$ which was at the beginning of the dialogue rejected will become accepted. Thus, the offer $a_2$ will be acceptable for the agent, whereas $a_1$ will become rejected. At this step 4, the offer $a_2$ is acceptable for both agents, thus it is an optimal solution. The dialogue ends by returning this offer as an outcome.

7. RELATED WORK

Argumentation has been integrated in negotiation dialogues at the early nineties by Sycara [12]. In that work, the author has emphasized the advantages of using argumentation in negotiation dialogues, and a specific framework has been introduced. In [8], the different types of arguments that are used in a negotiation dialogue, such as threats and rewards, have been discussed. Moreover, a particular framework for negotiation have been proposed. In [9, 13], different frameworks have been proposed. Even if all these frameworks are based on different logics, and use different definitions of arguments, they all have at their heart an exchange of offers and arguments. However, none of those proposals explains when arguments can be used within a negotiation, and how they should be dealt with by the agent that receives them. Thus the protocol for handling arguments was missing. Another limitation of the above frameworks is the fact that the argumentation frameworks they
use are quite poor, since they use a very simple acceptability semantics. In [2] a negotiation framework that fills the gap has been suggested. A protocol that handles the arguments was proposed. However, the notion of concession is not modeled in that framework, and it is not clear what is the status of the outcome of the dialogue. Moreover, it is not clear how an agent chooses the offer to propose at a given step of the dialogue. In [1, 7], the authors have focused mainly on this decision problem. They have proposed an argumentation-based decision framework that is used by agents in order to choose the offer to propose or to accept during the dialogue. In that work, agents are supposed to have a beliefs base and a goals base.

Our framework is more general since it does not impose any specific structure for the arguments, the offers, or the beliefs. The negotiation protocol is general as well. Thus this framework can be instantiated in different ways by creating, in such manner, different specific argumentation-based negotiation frameworks, all of them respecting the same properties. Our framework is also a unified one because frameworks like the ones presented above can be represented within this framework. For example the decision making mechanism proposed in [7] for the evaluation of arguments and therefore of offers, which is based on a priority relation between mutually attacked arguments, can be captured by the relation defeat proposed in our framework. This relation takes simultaneously into account the attacking and preference relations that may exist between two arguments.

8. CONCLUSIONS AND FUTURE WORK

In this paper we have presented a unified and general framework for argumentation-based negotiation. Like any other argumentation-based negotiation framework, as it is evoked in (e.g. [10]), our framework has all the advantages that argumentation-based negotiation approaches present when related to the negotiation approaches based either on game theoretic models (see e.g. [11]) or heuristics ([6]). This work is a first attempt to formally define the role of argumentation in the negotiation process. More precisely, for the first time, it formally establishes the link that exists between the status of the arguments and the offers they support, it defines the notion of concession and shows how it influences the evolution of the negotiation, it determines how the theories of agents evolve during the dialogue and performs an analysis of the negotiation outcomes. It is also the first time where a study of the formal properties of the negotiation theories of the agents as well as of an argumentative negotiation dialogue is presented.

Our future work concerns several points. A first point is to relax the assumption that the set of possible offers is the same to both agents. Indeed, it is more natural to assume that agents may have different sets of offers. During a negotiation dialogue, these sets will evolve. Arguments in favor of the new offers may be built from the agent theory. Thus, the set of offers will be part of the agent theory. Another possible extension of this work would be to allow agents to handle both arguments PRO and CONS offers. This is more akin to the way human take decisions. Considering both types of arguments will refine the evaluation of the offers status. In the proposed model, a preference relation between offers is defined on the basis of the partition of the set of offers. This preference relation can be refined. For instance, among the acceptable offers, one may prefer the offer that is supported by the strongest argument. In [4], different criteria have been proposed for comparing decisions. Our framework can thus be extended by integrating those criteria. Another interesting point to investigate is that of considering negotiation dialogues between two agents with different profiles. By profile, we mean the criterion used by an agent to compare its offers.

9. REFERENCES