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Article SigML++: Supervised Log Anomaly with Probabilistic Polynomial Approximations

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- + This paper is an extended version of our paper published in the 7th International Symposium on Cyber Security, Cryptology and Machine Learning (CSCML 2023) on June 29-30, 2023.

Abstract: Security log collection and storage is essential for organizations worldwide. Log analysis 1 can help recognize probable security breaches and is often required by law. However, many organizations commission log management to Cloud Service Providers (CSPs), where the logs are collected, 3 processed, and stored. Existing methods for log anomaly detection rely on unencrypted (plaintext) 4 data, which can be a security risk. Logs often contain sensitive information about an organization 5 or its customers. A more secure approach is always to keep logs encrypted (ciphertext). This paper 6 presents "SigML++," an extension of the "SigML" for supervised log anomaly detection on encrypted 7 data. SigML++ uses Fully Homomorphic Encryption (FHE) by the Cheon-Kim-Kim-Song (CKKS) scheme to encrypt the logs and then uses an Artificial Neural Network (ANN) to approximate the 9 sigmoid ($\sigma(x)$) activation function probabilistically for the intervals [-10, 10] and [-50, 50]. This 10 allows SigML++ to perform log anomaly detection without decrypting the logs. Experiments show 11 that SigML++ can achieve better low-order polynomial approximations for Logistic Regression (LR) 12 and Support Vector Machines (SVM) than existing methods. This makes SigML++ a promising new 13 approach for secure log anomaly detection. 14

Keywords: sigmoid function approximation; private machine learning; fully homomorphic encryption; log anomaly detection; supervised machine learning; probabilistic polynomial approximation

1. Introduction

Information security tools like Intrusion Detection Systems (IDS), Intrusion Prevention 18 Systems (IPS), and Security Information and Event Management (SIEM) are designed to 19 help organizations defend against cyberattacks. A Security Operations Center (SOC) uses 20 these security tools to analyze logs collected from endpoints, such as computers, servers, 21 and mobile devices. The logs can contain information about system events, user activity, 22 and security incidents. The SOC uses this information to identify anomalies and potential 23 threats. The SOC may generate an alert to notify the appropriate personnel if an anomaly 24 is detected. The logs collected from endpoints are typically unstructured textual data. This 25 data can be challenging to analyze manually. SIEM tools can help automate the analysis 26 of these logs and identify potential threats. SIEM tools collect logs from various sources, 27 known as Security Analytics Sources (SAS). SAS can be a mobile or stationary host or an 28 information and data security tool such as an IDS. SIEM tools use this data to monitor for 29 security threats in near real-time. If a threat is detected, the SIEM tool can generate an alert 30 and take appropriate action, such as blocking traffic or isolating an infected system. 31

As shown in Figure 1, a typical corporate network is connected to the Internet behind a firewall, which is divided into a Local Area Network (LAN), Wide Area Network (WAN), and Demilitarized zone (DMZ). A SAS client is typically a LAN or WAN endpoint that transmits security or audit logs to a SIEM. A SIEM could be placed in the network along

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Figure 1. A typical corporate network architecture.

Figure 2. Security Analytics Sources (SAS) of a SIEM.

with IDS/IPS or placed externally out of the network and connected via the Internet. There are three types of endpoints in any organization based on the isolation from the Internet: (i) Edge nodes or gateways or machines with public IP, (ii) Machines on LAN or WAN like high-power consumption devices like Servers and Laptops, mid-power devices like Smartphones, and low-power Internet of Things (IoT) or embedded devices and (iii) Machines on a Demilitarized zone (DMZ) like Email or FTP servers.

A Firewall is typically the first line of defense in a network, and an IDS or IPS can 42 accompany it. IPS is placed between the firewall and switch to detect and prevent threats, 43 while IDS is connected to the switch to monitor network activity passively to detect 44 attacks. Additionally, we can have antivirus software running on endpoints. An Advanced 45 Persistent Threat (APT) attacker is assumed to be outside the network and compromises 46 and gains unauthorized access to one of the endpoints. Log anomaly detection aims to 47 trace the trail left behind by the APT attacker while gaining unauthorized access. This trail is called IoC and is identified from the device logs. Logs from different devices are 49 collected and fed to a central SIEM server outside the corporate network for storage and 50 anomaly detection. These logs are collected, parsed, and correlated to generate alerts if 51 anomalies are detected. An example of correlation in logs is to detect new DHCP servers 52 that use UDP protocols on specific ports. 53

Besides the logs collected from network devices, application servers, and end-user systems, SIEM may collect other confidential organization information (Figure 2), such as business locations, active directory information, and ERP server data. These SAS inputs contain a lot of sensitive data, so protecting the security and privacy of data collected for anomaly detection is imperative.

As shown in Figure 3, a typical log anomaly (or intrusion) detection scheme consists of the following components:

- 1. A "Log Collector" to collect logs from diverse applications operating on an SAS.
- 2. A "Transmitter" to send logs to SIEM, which is usually encrypted to safeguard against eavesdropping in the communication channel.
- 3. A "Receiver" to amass, store, decrypt, and ascertain the transmitted logs' integrity.
- 4. A "Parser" to convert the data in a structured form used by the SIEM vendor to process the decrypted logs for storage and analysis.

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5. An "Anomaly Detector" uses proprietary algorithms to render parsed logs and transmit alerts for anomalies. 67

SOCs use a variety of storage options for their SIEM databases, depending on their specific needs and requirements, including (i) servers located on-premises, (ii) Storage Area Network (SAN) or Network Attached Storage (NAS), or (iii) cloud-based storage service, such as Amazon S3 [1] or Azure Blob Storage [2].

In a SOC, the relative jitter for the Log Collector (LC), Transmitter (TX), Receiver 73 (RX), Parser (PA), and Anomaly Detector (AD) is the variation in the time it takes for each 74 component to process a log event. Various factors, such as network latency, hardware 75 performance, and software complexity, can cause this jitter. The AD has the highest relative 76 jitter, followed by the PA, RX, TX, and LC. The AD is the most complex component, requiring more time to analyze each log event. The relative jitter of each component can 78 significantly impact the overall performance of the SOC. For example, if the AD has a 79 high relative jitter, detecting anomalies in the log data may take longer. This can lead to 80 increased security risks. The relative jitter of each component can be reduced by (i) using 81 high-performance hardware, (ii) optimizing the software, (iii) reducing network latency, 82 and (iv) using load-balancing techniques in a SOC to improve overall performance and 83 reduce security risks. 84

Enterprises frequently employ a third-party cloud vendor for SOC. Third-party cloud 85 services lessen complexity and deliver flexibility for organizations. Nonetheless, Cloud 86 Service Consumers (CSCs) must commission their data - and their customer's data - to 87 Cloud Service Providers (CSPs), who are often incentivized to monetize these data. Meanwhile, ordinances such as the US Consumer Online Privacy Rights Act (COPRA) [3], the US 89 State of California Consumer Privacy Act (CCPA) [4], and the EU General Data Protection Regulation (GDPR) [5] strive to safeguard consumers' privacy. Non-compliant institutions 91 are subjected to stringent fines and deteriorated reputations. This outcome is a tradeoff 92 between data utility and privacy. 93

Exporting log data to an SIEM deployed on a third-party CSP is perilous, as the CSP requires access to plaintext (unencrypted) log data for alert generation. Moreover, the CSP may have adequate incentives to accumulate user data. These data are stored in the CSP's servers and thus encounter diverse privacy and security threats like data leakage and misuse of information [6–11]. Thus, shielding these logs' privacy and confidentiality is crucial. We present the use of Fully Homomorphic Encryption (FHE) to permit CSC to ensure privacy without sabotaging their capability to attain insights from their data.

Traditional cloud storage and computation approaches using contemporaneous cryptography mandate that customer data be decrypted before operating on it. Thus, security policies are deployed to avert unauthorized admission to decrypted data. CSCs must entrust the Access Control Policies (ACP) incorporated by their CSPs for data privacy (Figure 4). With FHE, data privacy is accomplished by the CSC via cryptography, leveraging rigid mathematical proofs. Consequently, the CSP will not be admitted to unencrypted customer data for computation and storage without a valid Secret Key (SK).



Figure 4. Traditional cloud model (left) v/s FHE cloud model (right).

FHE allows calculations to be performed on encrypted data without decrypting it first. The results of these computations are stored in an encrypted form. Still, when decrypted, they are equivalent to the results that would have been obtained if the computations had been performed on the unencrypted data. Plaintexts are unencrypted data, while ciphertexts are encrypted data. FHE can enable privacy-preserving storage and computation and process encrypted data in commercial cloud environments. It is a promising technology with a wide range of potential applications.

For privacy-preserving log anomaly detection, we can use a hardware-based solution 115 (e.g., Trusted Execution Environment (TEE)) or a software-based approach (e.g., FHE). 116 SGX-Log [12] and Custos [13] showed private log anomaly detection using TEE with Intel 117 SGX. However, TEEs have limitations on how much data can be stored. For example, Intel 118 SGX has a limit of 128 MB. Hence, bit-wise FHE schemes like TFHE [14] or word-wise 119 FHE schemes like BFV [15,16] and CKKS [17] are better for larger data. Concrete-ML from 120 Zama [18] uses TFHE, which is efficient for smaller arithmetic. Still, it is inefficient for 121 larger arithmetic operations (while amortized performance in CKKS can be improved 122 with batching). For word-wise FHE schemes, we have BFV for integers and CKKS for 123 approximate arithmetic. Hence, for Machine Learning (ML) tasks, CKKS is a better choice. 124 Aymen et al. [19] used BFV for SVM with linear kernel. They experimentally calculate 125 the best scaling factor value to convert floats to integers for better accuracy, which is not 126 required in CKKS. SigML [20] used CKKS for LR and SVM. 127

Our contributions can be summarized as follows:

- First, we formulate a supervised binary classification problem for log anomaly detection and implement it with the CKKS cryptosystem (in section §4).
- Second, we propose novel ANN-based third-degree Sigmoid approximations in the intervals [-10, 10] and [-50, 50] (in section §5).
- Third, we evaluate the performance of various Sigmoid approximations in the encrypted domain, and our results show better accuracy and sum ratio (in section §6).

1.2. Organization

This paper is organized as follows:

- First, we describe the building blocks of our protocols in section §2, where we review FHE in section §2.1 and present polynomial approximations for the $Sigmoid(\sigma(x))$ activation function in section §5.
- Next, we review the previous work in section §3.
- Then, we describe our methodology in section §4.
- Finally, we discuss our experimental results in section §6.

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2. Background

This section details CKKS, a Fully Homomorphic Encryption scheme, and determinis-145 tic and probabilistic polynomial approximation schemes.

2.1. Fully Homomorphic Encryption

This work utilizes the CKKS [17] as a fully homomorphic encryption scheme. CKKS 148 varies from other FHE schemes (such as BFV [15,16], BGV [21], and TFHE [14]) in the 149 way that it interprets encryption noise. Indeed, CKKS treats encryption noise as part of 150 the message, similar to how floating-point arithmetic approximates real numbers. This 151 means the encryption noise does not eliminate the Most Significant Bits (MSB) of the 152 plaintext *m* as long as it stays small enough. CKKS decrypts the encryption of message *m* 153 as an approximated value m + e, where e is a slight noise. The authors of CKKS suggest 154 multiplying plaintexts by a scaling factor Δ prior to encryption to lessen precision loss 155 after adding noise during encryption. CKKS also sustains batching, a process for encoding 156 many plaintexts within a single ciphertext in a Single Instruction Multiple Data (SIMD) 157 fashion. We describe CKKS as a set of probabilistic polynomial-time algorithms regarding 158 the security parameter k. 159

The algorithms are:

- CKKS.Keygen: Generates a key pair.
- CKKS.Enc: Encrypts a plaintext.
- CKKS.Dec: Decrypts a ciphertext.
 - CKKS.Eval: Evaluates an arithmetic operation on ciphertexts.

The level of a ciphertext is *l* if it is sampled from $\mathbb{Z}_{q_l}[X]/(X^N+1)$. Let *L*, q_0 and Δ be 165 integers. We set $q_1 = \Delta^l \cdot q_0$ for any *l* integer in [0, L].

 $(evk, pk, sk) \leftarrow \mathsf{CKKS.Keygen}(1^k, L)$: generates a secret key (sk) for decryption, a public 167 key (pk) for encryption, and a publicly available evaluation key (evk). The secret key 168 (*sk*) is a sample from a random distribution over $\mathbb{Z}_3[X]/(X^N+1)$. The public key (*pk*) 169 is computed as: 170

$$pk = ([-a \cdot sk + e]_{q_L}, a) = (p_0, p_1)$$

where *a* is sampled from a uniform distribution over $\mathbb{Z}_{q_L}[X]/(X^N+1)$, and *e* is sam-171 pled from an error distribution over $\mathbb{Z}_{q_L}[X]/(X^N+1)$. *evk* is utilized for relinearisation 172 after the multiplication of two ciphertexts. 173

 $c \leftarrow \mathsf{CKKS.Enc}_{pk}(m)$: encrypts a message *m* into a ciphertext *c* utilizing the public 174 key (*pk*). Let *v* be sampled from a distribution over $\mathbb{Z}_3[X]/(X^N + 1)$. Let e_0 and e_1 be 175 small errors. Then the message *m* is encrypted as: 176

$$c = [(v \cdot pk_0, v \cdot pk_1) + (m + e_0, e_1)]_{aL} = (c_0, c_1).$$

- $m \leftarrow \mathsf{CKKS.Dec}_{sk}(c)$: decrypts a message c into a plaintext m utilizing the secret key . 177 (*sk*). The message *m* can be recovered from a level *l* ciphertext thanks to the function 178 $m = [c_0 + c_1 \cdot sk]_{q_l}$. Note that with CKKS, the capacity of a ciphertext reduces each 179 time a multiplication is computed. 180
- $c_f \leftarrow \mathsf{CKKS.Eval}_{evk}(f, c_1, \ldots, c_k)$: estimates the function f on the encrypted inputs 181 (c_1, \ldots, c_k) using the evaluation key evk. 182

2.2. Polynomial Approximations

This section describes commonly used function interpolation techniques like (i) Taylor, 184 (ii) Fourier, (iii) Pade, (iv) Chebyshev, (v) Remez, and (vi) probabilistic ANN scheme. 185

2.2.1. Taylor

The Taylor series (Eq. (1)) is a mathematical expression approximating a function as 187 an infinite sum of terms expressed in terms of the function's derivatives at a single point 188 *a*, called the center of the Taylor series. The Maclaurin series is a particular case of the 189

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Taylor series where the center of the series is a = 0. In other words, a Maclaurin series is a Taylor series centered at zero. It is a power series that permits the calculation of an approximation of a function f(x) for input values near zero, given that the values of the successive derivatives of the function at zero are known. The Maclaurin series can be used to find the antiderivative of a complicated function, approximate a function, or compute an uncomputable sum. In addition, the partial sums of a Maclaurin series provide polynomial approximations for the function.

$$\sum_{n=0}^{\infty} f^{(n)}(a) \frac{(x-a)^n}{n!} = f(a) + f'(a)(x-a) + \frac{f''(a)}{2!}(x-a)^2 + \ldots + \frac{f^{(k)}(a)}{k!}(x-a)^n + \ldots$$
(1)

2.2.2. Fourier

The Fourier series can be represented in sine-cosine, exponential, and amplitude-phase forms. For a sine-cosine form, coefficients are

$$A_{0} = \frac{1}{P} \int_{-P/2}^{P/2} f(x) dx$$

$$A_{n} = \frac{2}{P} \int_{-P/2}^{P/2} f(x) \cos\left(\frac{2\pi nx}{P}\right) dx$$

$$B_{n} = \frac{2}{P} \int_{-P/2}^{P/2} f(x) \sin\left(\frac{2\pi nx}{P}\right) dx$$
(2)

With these coefficients, the Fourier series is

$$f(x) \sim A_0 + \sum_{n=1}^{\infty} A_n \cos\left(\frac{2\pi nx}{P}\right) + B_n \sin\left(\frac{2\pi nx}{P}\right)$$
(3)

For an exponential form, coefficients are

$$c_{0} = A_{0}$$

$$c_{n} = (A_{n} - iB_{n})/2, \quad \text{for } n > 0$$

$$c_{n} = (A_{-n} + iB_{-n})/2, \quad \text{for } n < 0$$
(4)

By substituting Eq. 2 into Eq. 4

$$c_n = \frac{1}{P} \int_{-P/2}^{P/2} f(x) e^{-\frac{2\pi i n x}{P}} dx$$
(5)

With these definitions, we can write Fourier series in exponential form

$$f(x) = \sum_{n = -\infty}^{\infty} c_n \cdot e^{\frac{2\pi i n x}{p}}$$
(6)

2.2.3. Pade

Given a function f and two integers $m \ge 0$ and $n \ge 1$, the Pade approximant of order [m/n] is the rational function 203

$$R(x) = \frac{\sum_{j=0}^{m} a_j x^j}{1 + \sum_{k=1}^{n} b_k x^k} = \frac{a_0 + a_1 x + a_2 x^2 + \ldots + a_m x^m}{1 + b_1 x + b_2 x^2 + \ldots + b_n x^n}$$
(7)

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which agrees with f(x) to the highest possible order, which amounts to

$$f(0) = R(0),$$

$$f'(0) = R'(0),$$

$$f''(0) = R''(0),$$
 (8)
:

$$f^{(m+n)}(0) = R^{(m+n)}(0)$$

Equivalently, if R(x) is expanded in a Taylor series at 0, its first m + n terms would 204 cancel the first m + n terms of f(x), and as such 205

$$f(x) - R(x) = c_{m+n+1}x^{m+n+1} + c_{m+n+2}x^{m+n+2} + \dots$$
(9)

2.2.4. Chebyshev

The Chebyshev polynomial of degree *n* is denoted $T_n(x)$, and is given by the formula 207

$$T_n(x) = \cos\left(n \arccos x\right) \tag{10}$$

The first few Chebyshev polynomials of the kind are

$$T_{0}(x) = 1$$

$$T_{1}(x) = x$$

$$T_{2}(x) = 2x^{2} - 1$$

...

$$T_{n+1}(x) = 2xT_{n}(x) - T_{n-1}(x)$$
(11)

If f(x) is an arbitrary function in the interval [-1,1], and if N coefficients $c_i, j =$ 208 $0, \ldots, N-1$, are defined by 209

$$c_j = \frac{2}{N} \sum_{k=1}^{N} f(x_k) T_j(x_k) = \frac{2}{N} \sum_{k=1}^{N} f\left[\cos\left(\frac{\pi(k - \frac{1}{2})}{N}\right) \right] \cos\left(\frac{\pi j(k - \frac{1}{2})}{N}\right)$$
(12)

Then, we get the approximation formula

$$f(x) \approx \left[\sum_{k=0}^{N-1} c_k T_k(x)\right] - \frac{1}{2}c_o$$
(13)

2.2.5. Remez

Given a function f(x) to be approximated and a set *X* of n + 2 points $x_1, x_2, ..., x_{n+2}$ in 212 the approximation interval, usually the extrema of Chebyshev polynomial linearly mapped 213 to the interval. The Remez algorithm is the following: 214

- 1. Solve the system of linear equations
 - $b_0 + b_1 x_i + \ldots + b_n x_i^n + (-1)^i E = f(x_i); i = 1, 2, \ldots, n+2$ (14)

for the unknowns b_0, b_1, \ldots, b_n and *E*.

- 2. Use the b_i as coefficients to form a polynomial P_n .
- 3. Find the set *M* of points of local maximum error $|P_n(x) - f(x)|$. 218
- 4. If the errors at every $m \in M$ are alternate in sign (+/-) and of equal magnitude, then 219 P_n is the minimax approximation polynomial. If not, replace X with M and repeat the 220 abovementioned steps. 221

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Figure 5. Polynomial approximation using ANN.

2.2.6. ANN

While Artificial Neural Networks (ANNs) are known for their universal function 223 approximation properties, they are often treated as black boxes and used to calculate the 224 output value. We propose to use a basic 3-layer Perceptron (Figure 5) consisting of an 225 input layer, a hidden layer, and an output layer; both hidden and output layers having 226 linear activations to generate the coefficients for an approximation polynomial of a given 227 order. In this architecture, the input layer is dynamic, with the input nodes corresponding 228 to the desired polynomial degrees. While having a variable number of hidden layers is 229 possible, we fix it to a single layer with a single node to minimize the computation. We 230 show coefficient calculations for a third-order polynomial (d = 3) for a univariate function 231 f(x) = y for an input x, actual output y, and predicted output y_{out} . Input layer weights are 232

$$\{w_1, w_2, \dots, w_d\} = \{w_1, w_2, w_3\} = \{x, x^2, x^3\}$$

and biases are $\{b_1, b_2, b_3\} = b_h$. Thus, the output of the hidden layer is

$$y_h = w_1 x + w_2 x^2 + w_3 x^3 + b_h$$

The predicted output is calculated by

$$y_{out} = w_{out} \cdot y_h + b_{out} = w_1 w_{out} x + w_2 w_{out} x^2 + w_3 w_{out} x^3 + (b_h w_{out} + b_{out})$$
(15)

where the layer weights $\{w_1w_{out}, w_2w_{out}, w_3w_{out}\}$ are the coefficients for the approximating polynomial of order-3 and the constant term is $b_hw_{out} + b_{out}$.

Since the predicted output (y_{out}) is probabilistic, it must be fine-tuned with hyperparameter tuning, as incorrect results lead to erroneous (inefficient) approximations. 238

3. Related Work

This section discusses previous research on privacy-preserving log management ar-240 chitectures. Zhao et al. [22] proposed a system called Zoo to minimize latency in data 241 processing and reduce the amount of raw data exposed to the Cloud Service Provider 242 (CSP). Zoo is deployed on Customer-owned Edge Devices (CEDs) rather than on the cloud, 243 and it supports the composition, construction, and easy deployment of Machine Learning 244 (ML) models on CEDs and local devices. Zoo is implemented in the OCaml language on 245 top of the open-source numerical computing system Owl [23]. In addition to CEDs, Zoo 246 can be deployed on cloud servers or a hybrid of both. This can further reduce the data 247

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exposed to the CSP and its communication costs. Repositioning ML-based data analytics to edge devices from the cloud poses hurdles such as resource limitations, scarcity of usable models, and difficulty deploying user services. Additionally, deploying services on a CED environment introduces problems for the CSP, as the privacy of ML models (weights) must be shielded from the CED.

Ray et al. [24] proposed a set of protocols for anonymous upload, retrieval, and deletion of log records in the cloud using the Tor [25] network. Their scheme addresses integrity and security issues throughout the log management, including log collection, transmission, retrieval, and storage. However, their logging client is operating systemspecific, and privacy is not guaranteed because logs can be identified by their tag values. 254 255 256 257 256 257 257 258 259 259 250 257 259

Zawoad et al. [26,27] presented Secure Logging as a Service (SecLaaS), which stores 258 and provides access to logs generated by Virtual Machines (VMs) running in the cloud. 259 SecLaaS ensures the confidentiality and integrity of these logs, which the CSCs own. 260 SecLaaS encrypts some of the Log Entry (LE) information utilizing a shared public key of 261 the security agents to ensure confidentiality. The private key to decrypt the log is shared 262 among the security agents. An auditor can verify the integrity of the logs utilizing the Proof 263 of Past Log (PPL) and the Log Chain (LC). However, SecLaaS cannot encrypt all the fields 264 of the LE, as the CSP needs to be able to search the storage by some fields. Additionally, using a shared public key violates the CSC's data privacy. 266

Rane and Dixit [28] presented BlockSLaaS, a Blockchain-assisted Secure Logging-267 as-a-Service system for cloud environments. BlockSLaaS aims to make the cloud more 268 auditable and forensic-friendly by securely storing and processing logs while tackling multi-269 stakeholder collusion problems and ensuring integrity and confidentiality. The integrity 270 of logs is assured by utilizing the immutable property of blockchain technology. Cloud 271 Forensic Investigators (CFIs) can only access the logs for forensic investigation through 272 BlockSLaaS, which preserves the confidentiality of logs. To ensure the privacy of the CSC, 273 the Node Controller (NC) encrypts each log entry utilizing the CFI's public key, CFI_{PK} . The 274 CFI can then utilize its secret key, CFI_{SK} , to decrypt the logs, preserving the confidentiality 275 of the CSC's logs. However, this scheme utilizes the CFI's public key, which violates the 276 data privacy of the CSC. A more privacy-preserving scheme would use a different keying 277 mechanism, such as a private blockchain or a Trusted Execution Environment (TEE). 278

Bittau et al. [29] presented a principled systems architecture called Encode, Shuffle, Analyze (ESA) for performing large-scale monitoring with high utility while safeguarding user privacy. ESA guarantees the privacy of monitored users' data by processing it in a three-step pipeline:

- 1. Encode: The data is encoded to control its scope, granularity, and randomness.
- 2. Shuffle: The encoded data is shuffled to break its linkability and guarantee that individual data items get "lost in the crowd" of the batch. 285
- 3. Analyze: The anonymous, shuffled data is analyzed by a specific analysis engine that averts statistical inference attacks on analysis results. 287

The authors implemented ESA as a system called PROCHLO, which develops new techniques to harden the three steps of the pipeline. For example, PROCHLO uses the Stash Shuffle, a novel, efficient, and scalable oblivious-shuffling algorithm based on Intel's SGX, a TEE. TEEs provide isolated execution environments where code and data can be protected from the host system. However, using a TEE like Intel SGX may only be practical for some devices and infeasible for legacy and low-resourced systems. Additionally, TEEs limit the amount of data that can be secured.

Paul et al. [30] presented a Collective Learning protocol, a secure protocol for sharing classified time-series data within entities to partially train the parameters of a binary classifier model. They approximated the Sigmoid activation function ($\sigma(x)$) to a polynomial of degree 7. They presented a Collective Learning protocol to apply Homomorphic Encryption (HE) to fine-tune the last layer of a Deep Neural Network (DNN) securely. However, the degree-7 approximation using an HE method is counterproductive for resource-constrained machines, such as wireless sensors or Internet-of-Things (IoT) devices.

The most comparative work to ours on log confidentiality during transmission and 302 analysis using FHE techniques is presented by Boudguiga et al. [19]. In their scheme, 303 the authors examine the feasibility of using FHE to furnish a privacy-preserving log 304 management architecture. They utilize Support Vector Machines (SVMs) with a linear 305 kernel to assess the FHE classification of Intrusion Detection System (IDS) alerts from 306 the NSL-KDD dataset. In their scheme, they encrypt the input data from SAS using the 307 BFV scheme and perform FHE calculations on the encrypted data using the SIEM weights 308 in plaintext. The encrypted results for each log entry are then sent back to the SAS for 309 decryption. However, this approach can be vulnerable to inference attacks by malicious 310 SAS, such as attribute inference, membership inference, and model inversion attacks. Our 311 "Aggregate" scheme helps prevent most of these attacks, as it only sends a total anomaly 312 score (sum) per block instead of predictions or labels per input, thus minimizing the data 313 inferred by the attacker. 314

SigML, proposed by Trivedi et al. [20], uses the CKKS scheme and presents:

- Ubiquitous configuration: This is similar to other works and sends an encrypted result 1. 316 for every log entry. 317
- Aggregate configuration: This reduces communication and computation requirements 2. 318 by sending a single result for a block of log entries. 319

SigML compares three approximations of the sigmoid function: $\sigma^1(x), \sigma^3(x), \sigma^5(x)$. 320 These approximations are used for a Logistic Regression (LR) and Support Vector Machine 321 (SVM) model. The authors observed that the LR and SVM models trained from scikit-learn 322 [31] did not perform well with the sigmoid activation for the "Aggregate" configuration. 323 Therefore, they designed Sigmoid-LR (σ_{LR}) to improve performance. Sigmoid-LR uses a 324 kernel $A = X \cdot W + b$ to reduce the errors of Sigmoid(a) with the learning rate r_{learn} and 325 the number of iterations r_{iter} . The inputs and labels are $X, Y \in [0, 1]$. This paper presents 326 "SigML++," an extension of SigML [20]. SigML++ improves the results of SigML with LR 327 and SVM models using a novel ANN approximation. SigML++ also evaluates third-order 328 polynomials in the [-10, 10] and [-50, 50]. 329

4. Proposed Solution

Our threat model considers SAS (CSC) and SIEM (CSP) for simplicity. SAS is the client 331 that wants to generate anomaly alerts from logs while preserving its privacy. Consequently, 332 the SIEM server should be oblivious to the data received and refrain from comprehending 333 the log information. On the other hand, SIEM also desires to shield the weights and 334 coefficients of the ML model used to detect intrusion anomalies and generate alerts. Thus, 335 SAS should not learn about the model information. For log analysis using FHE, log parsing 336 shifts from SIEM to SAS. Instead of SIEM decrypting and parsing the logs, SAS collects and 337 parses unstructured logs to a structured form and normalizes the data. Data normalization 338 helps to enhance ML model prediction.

SAS uses FHE to generate an encryption key (pk/sk), a decryption key (sk), and an 340 evaluation key (evk). The parsed log inputs are encrypted using the public key (pk) or 341 secret key (*sk*). We use the CKKS scheme for FHE, which is better suited for floating-point 342 value calculations. CKKS is more suited for arithmetic on real numbers, where we can have 343 approximate but close results, while BFV is more suited for arithmetic on integers. The 344 SIEM performs homomorphic computations on the encrypted inputs and the ML model's 345 coefficients in plaintext, using the evaluation key (evk) generated by SAS. The encrypted 346 result(s) are then passed to SAS. SAS decrypts the result(s) with the secret key (*sk*), infers whether there was an anomaly, and generates an alert accordingly. 348

We present (i) "Ubiquitous" and (ii) "Aggregate" configurations similar to SigML. While 349 the "Ubiquitous" configuration is similar to prevalent research works, the "Aggregate" 350 configuration reduces the computation and communication requirements of the SAS. 351 Both configurations differ in how SIEM results are generated and processed at SAS:

1. Ubiquitous - SIEM sends one encrypted result per encrypted user input. 330

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Figure 6. Encrypted log anomaly detection in Ubiquitous and Aggregate configurations. (The dashed block is an extra component in Aggregate mode for encrypted additions.)

Aggregate - Only one result is sent in the encrypted domain for all inputs. This technique helps reduce communication costs and uses much fewer resources on SAS to decrypt a single encrypted result than one encrypted result per encrypted input.

In the "Ubiquitous" configuration (Figure 6), SAS sends encrypted parsed inputs to SIEM for analysis, and SIEM performs homomorphic calculations on encrypted inputs and unencrypted weights. SIEM sends one encrypted result for every encrypted log entry in the received block to SAS. SAS decrypts all the results and evaluates the labels for all the individual log entries. In this configuration, the disadvantage is leaking the data used for training or the model weights, as a dishonest client can perform inference attacks. 360

In the "Aggregate" configuration (Figure 6), SAS sends a block of encrypted parsed inputs as before. SIEM performs homomorphic computation with plaintext model weights for each input in the received block, applies Sigmoid approximation on individual encrypted results, and sums (homomorphic additions) all encrypted results.

The sigmoid activation is a mathematical function that approximates the outputs 367 of a machine learning model in the [0,1] range. In log anomaly detection, a label of 0 368 corresponds to a "normal" class, and a 1 corresponds to an "anomalous" class. In the 369 proposed procedure, the SAS receives only one result per block of messages. This saves 370 network bandwidth, as the SAS does not need to receive individual ciphers (encrypted 371 labels) for each message. Additionally, the SAS only needs to decrypt one cipher (encrypted 372 total) per block, which saves storage and computation overhead. The SAS decrypts the 373 result and assesses the sum for the block of messages. If there are no abnormalities in the 374 block, the totality should be 0. Otherwise, it should be the count of anomalous inputs. 375

Another advantage of this configuration is that it utilizes an anomaly score per block of log entries and functions as a litmus test for log anomalies. For example, a SOC engineer may prefer to examine the block of logs with a higher anomaly score than a block with a much lower score. Furthermore, if there are successive blocks with higher than usual anomaly scores, it may function as an IoC. The drawback of this configuration is that SAS can not pinpoint which entry in the block is anomalous.

As shown in Table 1, *n* is the number of logs, $T_E(p)$ is the time taken to encrypt a single message, $S_E(p)$ is bytes occupied by a single ciphertext, $T_D(c)$ is the time taken to 383

Configuration	Encry	ption	Decryption		
Configuration	Time	Size	Time	Size	
Ubiquitous	n T(n)	$n \cdot S_{-}(n)$	$n \cdot T_D(c)$	$n \cdot S_D(c)$	
Aggregate	$n \cdot r_E(p)$	$n \cdot S_E(p)$	$T_D(c)$	$S_D(c)$	

Table 1. Comparing "Ubiquitous" and "Aggregate" configurations.

5. Sigmoid Approximation

Barring message expansion and noise growth, implementing the Sigmoid activation 390 function is a substantial challenge in implementing ML with FHE. Sigmoid is used in LR 391 and SVM during classification, so we determined to make it homomorphic. We further 392 describe techniques to approximate this activation function with a polynomial for word-303 wise FHE and compare various polynomial approximations in terms of Accuracy, Precision, 394 Recall, F1-Score, and the Σ -Ratio of the predicted sum from Sigmoid values to the sum of 395 all actual binary labels for the test dataset. We denote \mathbf{M}_{i}^{d} , where **M** is an approximation 396 method like Taylor (T), Remez (R), Chebyshev (C), or ANN (A). d is degree and i is 397 the interval $[-\mathbf{i},\mathbf{i}]$ of the polynomial. We approximate the class C[a,b] of continuous 398 functions on the interval [a, b] by order-n polynomials in \mathcal{P}_n using the L^{∞} -norm to measure 399 fit. This is directed to as minimax polynomial approximation since the best (or minimax) 400 approximation solves: 401

$$p_n^* = \arg \min_{p_n \in \mathcal{P}_n} \max_{a \le x \le b} |f(x) - p_n(x)|$$
 (16)

A minimax approximation is a technique to discover the polynomial *p* in Eq. (16), i.e., the Remez algorithm [32] is an iterative minimax approximation and outputs the following results [33] for the interval [-5,5] and order 3:

$$\mathbf{R}_5^3(\mathbf{x}) = 0.5 + 0.197x - 0.004x^3 \tag{17}$$

Taylor series (around point 0) of degree 3 is given by

$$\mathbf{T}^{3}(\mathbf{x}) = 0.5 + 0.25x - 0.0208333x^{3} \tag{18}$$

Chebyshev series of degree 3 for the interval [-10, 10] is

$$0.5 + 0.139787x + (3.03084e - 26)x^2 - 0.00100377x^3$$

We omit the term for x^2 to get

$$\mathbf{C_{10}^3}(\mathbf{x}) = 0.5 + 0.139787x - 0.00100377x^3 \tag{19}$$

Similarly, we obtain the Chebyshev series of degree 3 for the interval [-50, 50]

$$C_{50}^{3}(\mathbf{x}) = 0.5 + 0.0293015x - (8.65914e - 6)x^{3}$$
⁽²⁰⁾

We derive the ANN polynomials of degree 3 for [-10, 10]

$$\mathbf{A_{10}^3}(\mathbf{x}) = 0.49961343 + 0.12675145x - 0.00087002286x^3 \tag{21}$$

and for the interval [-50, 50]

$$\mathbf{A_{50}^3}(\mathbf{x}) = 0.49714848 + 0.026882438x - (7.728304e - 06)x^3 \tag{22}$$

We compared *Chebyshev* and *ANN* approximations for the *Sigmoid* functions as shown in Table 2. We calculate Mean Absolute Error (*MAE*), Mean Squared Log Error (*MSLE*), *Huber*, *Hinge*, and *Logcosh* losses [34,35] for *Chebyshev* polynomials described in equations 19, 20 and *ANN* polynomials from equations 21, 22. E.g., A³₁₀ recorded a MAE loss of 0.0691 compared to 0.0793 for C³₁₀. The lower losses (closer to 0) reflect

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Interval	Method	MAE	MSLE	Huber	Hinge	Logcosh
[-10, 10]	C_{10}^{3}	0.0793	0.0020	0.0039	0.5593	0.0039
	$A_{10}^{3^{\circ}}$	0.0691	0.0024	0.0031	0.5646	0.0031
[-50, 50]	C_{50}^{3}	0.1363	0.0115	0.0138	0.5475	0.0136
	A_{50}^{3}	0.1255	0.0124	0.0132	0.5534	0.0131

Table 2. Polynomial approximation losses for the intervals [-10, 10] and [-50, 50].

fewer errors and show a better approximation using our approach. Comparing their ratios 416 $\frac{0.0691}{0.0793} = 0.8712$, we observe $\approx 14\%$ improvement (Figure 7). 417

6. Experimental Analysis

The experiments were conducted on a 2.4 GHz Quad-Core MacBook Pro with an Intel 419 Core i5 processor and 2133 MHz 8 GB LPDDR3 memory. We used the SEAL-Python [36] 420 library for Python3 to furnish CKKS encryption. Moreover, we have used sklearn [37] APIs 421 for binary classifiers. 422

6.1. Evaluation Criteria

We compared the performance of the models using the following metrics: Precision, 121 Recall, Accuracy, and F1-score for the "Ubiquitous" configuration and Σ -Ratio for the 425 "Aggregate" configuration. We repeated the experiments on both the NSL-KDD and the 426 balanced HDFS datasets.

- Precision is the proportion of correctly predicted positive results (True Positives, TP) • 428 to the total predicted positive results (TP + False Positives, FP). It is also known as 429 positive predictive value. 430
- Recall is the proportion of correctly predicted positive results (TP) to the total actual 431 positive results (TP + False Negatives, FN). It is also known as sensitivity or specificity. 432
- Accuracy is the proportion of all correct predictions (TP + TN) to the total number of 433 predictions made (TP + FP + TN + FN). It can be calculated as "Precision" divided by 434 FalseNegativeRate(FNR) "Recall" or 1 -435 FalsePositiveRate(FPR)
- F1-Score is a measure that considers both "Precision" and "Recall." It is calculated as 436 the harmonic mean of "Precision" and "Recall."
- Sum ratio is a measure used for the Sigmoid activation function with binary outcomes. 438 It is calculated as the sum of all predicted labels to the sum of all actual labels. 439



Figure 7. ANN losses relative to *Chebyshev* for the intervals [-10, 10] and [-50, 50].

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Dataset	Туре	Accuracy	Precision	Recall	F1-Score	Σ-Ratio
NSL-KDD	Full (100%)	0.4811	0.4811	1.0000	0.6497	2.0782
	Test (20%)	0.4832	0.4832	1.0000	0.6515	2.0695
HDFS	Full (100%)	0.4999	0.4999	1.0000	0.6666	2.0000
	Test (20%)	0.5016	0.5016	1.0000	0.6681	1.9934

Table 3. Return-1 model performance for NSL-KDD and HDFS.

$$Precision = \frac{TP}{TP + FP}$$
(23)

$$Recall = \frac{TP}{TP + FN} \tag{24}$$

$$Accuracy = \frac{TP + TN}{TP + FP + TN + FN}$$
(25)

$$F1 - Score = 2 * \frac{Precision * Recall}{Precision + Recall}$$
(26)

$$\Sigma - Ratio = \frac{\sum_{i=1}^{n} \text{Predicted } y_i}{\sum_{i=1}^{n} \text{Actual } y_i}, \text{ where } y_i \in \{0, 1\}$$
(27)

6.2. Datasets

Log datasets are often imbalanced, with most samples belonging to one class. This can lead to overfitting and a "pseudo-high" accuracy for the trained model. To avoid this, we 446 propose to use balanced datasets. We first used a "Return-1 Model" to verify the balance of 447 classes in our log anomaly datasets. This model always classifies samples as "anomalous." 448 We achieved an Accuracy of 48.11% and a Σ -ratio of 2.07 for the NSL-KDD dataset and an 449 Accuracy of 49.99%, and a Σ -ratio of 2.00 for the HDFS dataset. We also achieved a Recall 450 of 100% for both datasets, as the model always outputs 1 for "anomaly." The NSL-KDD [38] 451 dataset is a modified version of the KDD'99 [39] dataset that solves some of its intrinsic 452 problems. It contains 148,517 inputs with 41 features and two observations for Score and 463 Label. We modified the labels to make it a binary classification problem, with all attack 454 categories consolidated into label-1. This resulted in 77,054 inputs with label-0 ("normal") 455 and 71,463 inputs classified to label-1 ("anomalous"). The testing set comprised 29,704 456 inputs, with 14,353 of label-1 and 15,351 of label-0. The HDFS_1 [40] labeled dataset from 457 Logpai is 1.47 GB of HDFS logs forged by running Hadoop-based map-reduce jobs on 458 over 200 Amazon EC2 nodes for 38.7 hours. Hadoop domain experts labeled it. Of the 459 11,175,629 log entries accumulated, 288,250 (~ 2.58%) data are anomalous. We used Drain [41], a log parser, to convert our unstructured log data into a structured format. For brevity, 461 we skip the details of textual log data parsing. We created a more undersized, balanced 462 dataset of 576,500 inputs with seven observations equally distributed among the "normal" 463 and "anomaly" classes. We used 20% of the total dataset as testing data, with 115,300 inputs, out of which 57,838 inputs belonged to label-1 and 57,462 belonged to label-0. 465

6.3. Test Results

Foremost, we constructed baselines with plain (unencrypted) data, and the results are exhibited in Table 4. For the NSL-KDD dataset, we accomplished 93.52% Accuracy, 95.02% Precision, and 0.99 Σ -Ratio with LR and 93.30% Accuracy, 95.50% Precision, and 1.06 Σ -Ratio with SVM. Likewise, for the HDFS (balanced) dataset, we accomplished 96.83% Accuracy, 94.12% Precision, and 1.00 Σ -Ratio with LR and 96.81% Accuracy, 94.02% Precision, and 0.86 Σ -Ratio with SVM.

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Dataset	Model	Scale	Method	Accuracy	Precision	Recall	F1-Score	Σ-Ratio
NSL-KDD	LR		Plain	0.9352	0.9502	0.9138	0.9317	0.9966
			R ₅ ³	0.7923	0.9272	0.6186	0.7421	0.6336
		2 ³⁰	T ³	0.3865	0.3083	0.2167	0.2545	-2.1720
			C ³ ₁₀	0.9330	0.9486	0.9108	0.9293	1.0633
			C_{50}^{3}	0.9351	0.9498	0.9139	0.9315	1.0753
			A_{10}^{3}	0.9342	0.9502	0.9116	0.9305	1.0667
			A_{50}^{3}	0.9120	0.9213	0.8942	0.9076	1.0666
		240	T ³	0.3870	0.3087	0.2169	0.2548	-2.1649
			C_{10}^{3}	0.9341	0.9501	0.9115	0.9304	1.0634
			$C_{50}^{\bar{3}}$	0.9352	0.9502	0.9138	0.9317	1.0752
			A_{10}^{3}	0.9341	0.9501	0.9115	0.9304	1.0668
			A_{50}^{3}	0.9350	0.9537	0.9096	0.9311	1.0660
	SVM		Plain	0.9330	0.9550	0.9039	0.9287	1.0614
			R ₅ ³	0.9326	0.9550	0.9031	0.9283	1.0993
		2 ³⁰	T ³	0.7743	0.9262	0.5790	0.7126	0.7872
			C_{10}^3	0.9312	0.9522	0.9029	0.9269	1.1190
			$C_{50}^{3^{\circ}}$	0.8426	0.8194	0.8649	0.8649	1.0569
			A_{10}^{3}	0.9239	0.9407	0.8993	0.9195	1.1110
			$A_{50}^{3^{\circ}}$	0.9311	0.9574	0.8974	0.9264	1.0489
		240	T ³	0.7762	0.9302	0.5804	0.7148	0.7876
			C_{10}^3	0.9330	0.9550	0.9039	0.9287	1.1189
			$C_{50}^{3^{\circ}}$	0.9330	0.9550	0.9039	0.9287	1.0566
			A_{10}^{3}	0.9329	0.9551	0.9036	0.9287	1.1111
			A_{50}^{3}	0.9318	0.9604	0.8958	0.9270	1.0489
HDFS	LR		Plain	0.9683	0.9412	0.9992	0.9693	1.0001
			R ₅ ³	0.5308	0.5167	0.9992	0.6812	292.6803
		2 ³⁰	T ³	0.3616	0.4178	0.6928	0.5213	1545.6206
			C_{10}^{3}	0.5561	0.5306	0.9993	0.6931	71.6765
			$C_{50}^{3^{\circ}}$	0.8899	0.8203	0.9995	0.9011	0.7862
			A_{10}^{3}	0.5560	0.5305	0.9994	0.6931	62.0974
			A_{50}^{3}	0.8932	0.8249	0.9992	0.9037	0.7784
		240	T ³	0.3616	0.4178	0.6927	0.5212	1542.8804
			C_{10}^{3}	0.5564	0.5307	0.9992	0.6932	71.5496
			C_{50}^{3}	0.8908	0.8216	0.9992	0.9018	0.7835
			A ³ ₁₀	0.5565	0.5308	0.9992	0.6933	61.9845
			A_{50}^3	0.8930	0.8247	0.9992	0.9036	0.7794
	SVM		Plain	0.9681	0.9402	1.0000	0.9692	0.8649
			R ₅ ³	0.5605	0.5330	1.0000	0.6953	36.6039
		2^{30}	T ³	0.5513	0.5278	1.0000	0.6910	198.8704
			C_{10}^{3}	0.6356	0.5793	0.9988	0.7333	8.5442
			C_{50}^{3}	0.9263	0.9385	0.9130	0.9256	0.6254
			A_{10}^3	0.6397	0.5820	1.0000	0.7358	7.4514
			A_{50}^3	0.9682	0.9406	0.9998	0.9693	0.6478
		2^{40}	T ³	0.5518	0.5281	1.0000	0.6912	198.5042
			C ³ ₁₀	0.6357	0.5793	1.0000	0.7336	8.5288
			C ³ ₅₀	0.9681	0.9402	1.0000	0.9692	0.6253
			A_{10}^{3}	0.6399	0.5821	1.0000	0.7359	7.4376
			A_{50}^{3}	0.9682	0.9404	1.0000	0.9693	0.6482

 Table 4. Comparing performance metrics for sigmoid approximations.

Detesat	Madal	Carla	Mathad	Average			Total (CPU)	
Dataset		Scale	Method	Encryption	Decryption	Sigmoid	User	System
NSL-KDD	LR	2 ³⁰	T ³	15.9451	1.2736	25.0283	21229.5304	31.1183
			C_{10}^{3}	15.8492	1.2750	24.8478	14151.9965	21.6079
			C_{50}^{3}	16.3591	1.3128	25.6645	57907.9974	192.8575
			A_{10}^{3}	15.9845	1.2882	25.1456	7098.8882	12.2847
			A_{50}^{3}	16.4581	1.3294	25.8525	50652.5642	173.5452
		240	T ³	16.5453	1.3044	26.1130	21864.5342	86.9118
			C_{10}^3	16.3382	1.2872	25.6880	14527.2336	63.9331
			$C_{50}^{3^{\circ}}$	16.2095	1.2866	25.3791	72326.0694	229.5827
			A_{10}^{3}	16.4056	1.2930	25.8025	7249.1064	44.1778
			$A_{50}^{3^{\circ}}$	16.2132	1.2683	25.5183	65122.4439	209.3589
	SVM	2 ³⁰	T ³	15.9461	1.2854	25.1386	21342.9889	37.2623
			C_{10}^3	16.0024	1.2769	25.1158	14240.9221	27.7670
			$C_{50}^{\bar{3}}$	16.3930	1.3225	25.7013	34780.6294	69.3801
			A_{10}^{3}	16.1102	1.2971	25.3295	7138.4435	17.5237
			A_{50}^{3}	16.0584	1.2954	25.1713	79472.3131	241.1018
		240	T ³	16.0374	1.2567	25.0808	43369.0540	144.5788
			C_{10}^3	15.9906	1.2657	25.0830	36270.2810	133.6592
			$C_{50}^{\bar{3}}$	16.1845	1.2751	25.3623	41969.1462	86.2903
			A_{10}^{3}	16.4235	1.3000	25.8985	29143.3392	110.3346
			A_{50}^{3}	15.9473	1.2531	25.1184	93679.2789	260.7503
HDFS	LR	2 ³⁰	T ³	16.3908	1.2578	25.4707	28191.8944	96.0272
			C_{10}^3	16.4117	1.2704	25.3694	56176.0993	249.5097
			C_{50}^{3}	16.2385	1.3113	25.1131	83989.0793	355.9741
			A_{10}^{3}	16.1082	1.2582	24.9673	27724.1933	75.9279
			A_{50}^{3}	15.9611	1.2891	24.7696	55177.6614	119.2686
		240	T ³	16.0785	1.1416	24.8503	27533.3271	43.9969
			C_{10}^{3}	16.1325	1.1467	24.6902	28002.8715	42.0600
			C_{50}^{3}	16.1544	1.1475	24.7477	55939.1609	88.9075
			A ³ ₁₀	16.0655	1.1504	25.0016	82767.8606	171.9368
			A_{50}^{3}	16.4731	1.1875	25.5487	110748.7027	309.8314
	SVM	2^{30}	T ³	16.3642	1.2677	25.4733	82902.0987	212.2604
			C ³ ₁₀	16.0238	1.2588	24.7493	27494.7062	61.8813
			C_{50}^{3}	15.9412	1.2864	24.7108	54953.8687	107.4183
			A ³ ₁₀	16.1825	1.2757	25.0942	138438.5341	379.7756
			A_{50}^{3}	16.3706	1.3089	25.4166	35159.2336	121.3245
		240	T ³	16.6737	1.1933	25.8361	83201.7236	274.1485
			C ³ ₁₀	15.9010	1.1333	24.5346	27335.2857	46.0062
			$C_{50}^{\bar{3}}$	16.0024	1.1422	24.6981	54971.1042	97.4169
			A_{10}^{3}	15.9279	1.1375	24.6168	27384.4133	46.0062
			$A_{50}^{\bar{3}}$	15.9141	1.1383	24.5868	27388.0323	43.6415

 Table 5. Time taken in seconds for sigmoid approximations.

Next, we compare third-order sigmoid approximations as shown in Equations 17, 18, 473 19, 20, 21, and 22 in terms of performance metrics and execution time. We empirically show 474 that our *ANN*-based polynomials performed better in most instances. For the NSL-KDD 475 dataset and LR model with a CKKS scaling factor of 2^{30} , the Chebyshev polynomial C_{10}^{30} 476 in the range [-10, 10] (Eq. 19) yielded 93.30% Accuracy, 94.86% Precision, 91.08% recall, 477 92.93% f1-score and 1.06 Σ -ratio. While *ANN* approximation A_{10}^3 in the same range (Eq. 478 21) had 93.42% accuracy, 95.02% precision, 91.16% recall, 93.05% f1-score and 1.06 Σ -ratio. 479 Thus, A_{10}^3 resulted in 0.13% improvement in accuracy and 0.17% in precision over C_{10}^3 .

We also experimented with different scaling factors of 2^{30} and 2^{40} . While it did not significantly impact the NSL-KDD dataset, we observed improvements for HDFS. For C_{50}^{3} with the SVM model, Accuracy improved from 92.63% to 96.81%, Precision from 93.85% to 94.02%, Recall from 91.30% to 100%, and f1-score also improved from 92.56% to 96.92% when increasing scaling factor. We also observed improvements for Σ -ratio, for A_{10}^{3} it reduced from 7.45 to 7.43 (ideal value is close to 1).

We also improve the results reported in SigML. For instance, A_{10}^3 performed much better than R_5^3 . For NSL-KDD, with LR, Accuracy was improved from 79.23% to 93.42%, precision from 92.72% to 95.02%, recall from 61.86% to 91.16%, f1-score from 74.21% to 93.05% and Σ -ratio from 0.63 to 1.06. However, like SigML, our approximations did not yield good results for HDFS datasets, specifically for Σ -ratio. It would be interesting to approximate sigmoid in the [-20, 20] and [-30, 30] to get better results.

We also measured the average time taken for encryption, decryption, and sigmoid operations, as shown in Table 5. We did not see any significant impact of different datasets, models, scales, or methods on average time taken in seconds. We also measured the total User CPU and System CPU time for different configurations for completeness. A³₁₀ was observed to be faster than other methods.

7. Discussion

This section briefly compares the proposed solution and the most closely related supervised machine learning technique for regression and classification tasks. While Support Vector Machines (SVM) ensures classification by identifying a hyperplane that maximizes the margin between data points of different classes, Gaussian Process Regression (GPR) adopts a generative approach using a Gaussian process to model data distributions, enabling predictions and uncertainty estimations.

In the context of (encrypted) anomaly detection, SVM is often preferred over GPR for two main reasons. First, GPR tends to be computationally intensive, mainly when dealing with high-dimensional data. In contrast, SVM is known for its efficiency in training and evaluation, making it highly suitable for handling large datasets. Second, GPR requires careful selection of kernel functions and other hyperparameters, which can be challenging. SVM is less sensitive to these choices, which makes it easier to use.

8. Conclusions

We implemented an FHE-based solution for supervised binary classification for log anomaly detection. FHE is a cryptographic technique that allows computations on encrypted data without decrypting it. This makes it a promising approach for privacypreserving machine learning applications, such as log anomaly detection.

In our solution, we used the CKKS algorithm, which is a popular FHE scheme. We 516 also approximated the *Sigmoid* activation function, a commonly used function in machine 517 learning, with novel low-order polynomials. This allowed us to reduce the communication 518 and computation requirements of our solution, making it more suitable for wireless sensors 519 and IoT devices. *Chebyshev* approximations of low order for FHE are widely used in many 520 privacy-preserving tasks. We compared our ANN-based polynomials with Chebyshev 521 regarding performance metrics and timings. We empirically show that our polynomials 522 performed better in most cases for the same amount of computation and multiplication 523 depth. However, comparing our approximations with composite (iterative) polynomials 524

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[42,43] would make an interesting study. Iterative polynomials have the advantage of generating optimal approximations for the same multiplicative depth, with the drawback of extra noise and processing due to more multiplications.

Our evaluation of FHE for supervised binary classification was limited to linearly separable problems. In future work, we plan to implement FHE with other ML models, such as Recurrent Neural Networks (RNN) and Random Forests (RF). We also plan to use Chimera [44] and combine TFHE/BFV for assessing the Sigmoid activation function by approximating it by the *Signum(Sign)* operation furnished by the TFHE bootstrapping.

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