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► **To cite this version:**

T. Okumura, T. Azuma, D. A. Bennett, I. Chiu, W. B. Doriese, et al.. A Proof-of-Principle Experiment for Testing Strong-Field Quantum Electrodynamics with Exotic Atoms: High Precision X-Ray Spectroscopy of Muonic Neon. *Physical Review Letters*, 2023, 130 (17), pp.173001. 10.1103/physrevlett.130.173001 . hal-04293221

**HAL Id: hal-04293221**

**<https://hal.science/hal-04293221v1>**

Submitted on 18 Nov 2023

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# A Proof-of-Principle Experiment for Testing Strong-Field Quantum Electrodynamics with Exotic Atoms: High Precision X-ray Spectroscopy of Muonic Neon

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To test bound-state quantum electrodynamics (BSQED) in the strong-field regime, we have performed high-precision x-ray spectroscopy of the  $5g\text{-}4f$  and  $5f\text{-}4d$  transitions (BSQED contribution of 2.4 eV and 5.2 eV, respectively) of muonic neon atoms in the low-pressure gas phase without bound electrons. Muonic atoms have been recently proposed as an alternative to few-electron high- $Z$  ions for BSQED tests by focusing on circular Rydberg states where nuclear contributions are negligibly small. We determined the  $5g_{9/2}\text{-}4f_{7/2}$  transition energy to be  $6297.08 \pm 0.04$  (stat.)  $\pm 0.13$  (syst.) eV using superconducting transition-edge sensor microcalorimeters (5.2-5.5 eV FWHM resolution), which agrees well with the most advanced BSQED theoretical prediction of 6297.26 eV.

Quantum electrodynamics (QED) is one of the most precisely examined theories in physics. In hydrogen, the QED correction to the  $1s\text{-}2s$  transition energy is 8172770.4(2.1) kHz corresponding to 3.3 ppm of the total energy [1], which was measured with  $\sim 10$  Hz accuracy [2, 3]. The calculated value is in excellent agreement with experiment, the difference being 0.1(2.1) kHz. The QED contribution to the transition energy increases in general with  $Z^2$  ( $Z$ : nuclear charge). However, it is known that the theoretical approach using a perturbative expansion with  $\alpha Z$  ( $\alpha \approx 1/137$ : fine-structure constant) does not converge at high  $Z$ . Thus, a comparison between experimental and theoretical bound-state QED (BSQED) under strong fields is of utmost necessity. It has been explored intensively with highly-charged ions (HCIs); see Ref. [4] for a recent review. The most precise measurement of the ground state Lamb shift in high- $Z$  systems is so far limited to an accuracy of 1% [5]. Moreover, HCI studies face a severe difficulty, i.e., the non-negligible contribution of the finite nuclear size (FNS), and its uncertainties often overwhelm the second-order BSQED contribution [4, 6]. Thus tests of BSQED

in the strong-field regime are still in their infancy.

Muonic atoms, where a negative muon is captured onto the atomic orbitals, replacing an electron, provide a unique window into strong electric field atomic physics because muons are 207 times closer to the nucleus than electrons and thus probe high Coulomb fields. When a muon is captured by an atom, it experiences a cascading deexcitation process by Auger electron emission, which results in the peeling-off of the bound electrons of the atom. The cascade is followed by photon emission in the x-ray regime [7]. Muonic atoms have been of great interest for measuring fundamental physics parameters and searching for beyond-Standard-Model physics [8–12].

A negative muon in a muonic atom with a high- $Z$  nucleus is exposed to the strong electric field of the nucleus, which also makes it a good probe to explore BSQED in the strong fields. In this simple exotic atom, the leading-order BSQED correction to the x-ray transitions is the vacuum polarization (VP), i.e., polarization of virtual electron-positron pairs in the muon-nucleus field, followed by the self-energy, which is the reverse order compared to ordinary atoms consisting of an electron and a

nucleus. This is because, when the muon comes so close to the nucleus, generally less than the electron's Compton wavelength, the muon would feel "bare" nuclear charge freeing from "polarization" charge, resulting in enhanced VP [13]. As the ensemble of atomic states in muonic atoms are found in a higher field regime than their normal electronic counterparts, and this simple two-body system can be calculated with high precision, these systems are ideal probes of BSQED and particularly of the VP effect. Recently, we theoretically proposed the advantages of exotic atoms over HCIs for BSQED tests in Ref. [14]. A region of suitable transitions may be found between high- $n_\mu$  circular Rydberg states ( $n_\mu$ : the principal quantum number of the muon orbitals) where nuclear contributions to the transition energies are vanishing, while BSQED contributions remain large, creating a unique opportunity to cleanly probe strong-field BSQED.

The history of BSQED tests using muonic and other exotic atoms can be traced back to the 1970's [13]. Unfortunately, all of these experiments employed solid-state targets, and the resulting screening effects from unavoidable recaptured electrons, in addition to the use of low- $n_\mu$  transitions with large FNS corrections, limited the sensitivity to BSQED effects in the transition energies. After the recognition of the electron refilling problem, particularly in  $\pi$ Mg measurements [15, 16], muonic x-ray measurements using gas targets were explored. Pressure effects on the muon cascade and the transition energies were intensively studied by [17–22]. Kirch *et al.* concluded that a pressure below 0.1 atm is necessary to completely isolate  $\mu$ Ne during the muon cascade [22], where such low-target-density conditions preclude the use of a crystal spectrometer.

Precision measurements of pionic x rays with gas targets employing a cyclotron trap and a crystal spectrometer have been carried out at relatively high pressures around 1 atm [23]. In the updated experiment by Trassinelli *et al.* [24], the pionic x rays from  $\pi$ N were measured together with the muonic x rays from  $\mu$ O, which were located close to the target pionic line and used as a reference for energy calibration under the assumption that the calculated BSQED contribution was correct. They could, in principle, achieve a QED test with a 1%-level accuracy by calibrating the  $\mu$ O lines against the Cu  $K\alpha$  line, which was measured simultaneously as a stability monitor, although they didn't discuss this aspect.

We aim to test strong-field BSQED by muonic x-ray spectroscopy with high resolution under the condition that there are no remaining electrons in the muonic atoms. To prepare the clean two-body system, two requirements are crucial. First, one must be sure of the full stripping of bound electrons via the Auger process during the muon deexcitation, which requires a nucleus of relatively low atomic number  $Z$ . Furthermore, electron refilling from neighboring atoms or molecules has to be avoided, leading to the second requirement of the

isolated condition of the muonic atom, i.e., formation in a low-pressure gas.

To achieve a high-resolution and high-detection-efficiency for the muonic x-ray detection under such a low-pressure condition, we took full advantage of multi-pixel transition-edge-sensor (TES) superconducting x-ray calorimeters. The broadband feature of the TES detector makes it possible to measure different muonic x-ray peaks simultaneously. This allowed us to measure both the targeted peak energy for the BSQED test and other peak energies for directly evaluating the number of the remaining electrons in the muonic atom.

The Materials and Life Science Experimental Facility (MLF) at J-PARC provides the necessary intense pulsed negative muon beams with energies down to 58 keV (3.5 MeV/ $c$ ) [25]. This enables us to stop isolated muons directly at high rates in low-density gas targets. We already have demonstrated excellent performance of the TES detector for accelerator-based experiments [26–28].

In this letter, using the TES detector, we report precision measurements of muonic x rays from completely ionized  $\mu$ Ne isolated in a dilute gas and compare the results with updated stringent BSQED theory. We selected the muonic x rays of the  $5g-4f$  and  $5f-4d$  transitions of  $\mu$ Ne as targets for measurements because 1) the transitions include 2.4 and 5.2 eV BSQED contributions ( $4-8 \times 10^{-4}$  relative to the transition energy) which are resolvable by the TES detector at the 0.1 eV level, 2) the FNS contribution is negligibly small, and 3) bound electrons are absent. We also exploit a muonic x-ray peak from  $7h-5g$  and  $7g-5f$  transitions, which was measured simultaneously with the target peak owing to the broad dynamic range of the TES detector, to confirm the absence of remaining  $K$ -shell electrons at  $n_\mu = 5$ .

The experiment was carried out at the D2 beamline of the MLF at J-PARC [25]. Details of the setup were described in previous papers [27, 29, 30]. The major differences from the previous experiment using a metal-foil target [27] are that a gas target was used, and careful calibration procedures were implemented notably to correct the small but significant temporal energy shifts under the pulsed-mode operation of the muon beam. We prepared the low-pressure Ne gas target as low as 0.1 atm at room temperature and studied the pressure dependence. The neon gas contained  $^{20}\text{Ne}$  and  $^{22}\text{Ne}$  with the natural isotopic abundances of 90.48% and 9.25%. The muons were delivered in a double-pulse structure containing  $\sim 10^4$  muons per double pulse with a repetition rate of 25 Hz. The muon momentum values were optimized to 20.5, 20.5, and 21.5 MeV/ $c$  at neon pressures of 0.1, 0.4, and 0.9 atm, respectively, to maximize the number of stopped muons within the field of view of the detector. Typical count rates of muonic x rays on the whole detector array were 1-3 counts per second. We employed a 240-pixel TES array developed by the National Institute

of Standards and Technology (NIST) [31]. For accurate online energy calibration, we simultaneously monitored characteristic  $K$  x rays from Cr, Co, and Cu produced by an x-ray generator [27]. Energy calibration of each TES pixel was carried out by following the procedure of Refs. [32, 33].

We observed the energy shift originating from the pulsed-mode operation of the muon beam, which can be understood by thermal crosstalk resulting from high-energy charged particles accompanying the muon beam injection [30]. When charged particles, produced by muon decay or nuclear capture, or scattered by the Ne gas, hit the TES pixel array, a large fraction of the deposited energy is converted into heat in the Si frame of the TES pixel, causing a change in the raw TES waveform that results from the x-ray detection. The energy shifts in the observed region were roughly 0.3, 0.4, and 0.5 eV at pressures of 0.1, 0.4, and 0.9 atm. These shifts are corrected by measuring the peak-energy deviation of the calibration  $K$  x-ray peaks as a function of the detection time with respect to the pulsed muon beam injection, as well as employing a small temperature rise observed in the surrounding TES pixels (see the details in the Supplementary Material (SM)). We evaluated the accuracy of this correction from experimental results using a Fe foil target. From a comparison of peak positions of Fe  $K\alpha$  x rays, which are emitted only at the muon-beam injection and affected by the crosstalk effect, to the reference value [34, 35], we confirmed that the energy shifts are properly corrected with an error below 0.11 eV.

We obtained x-ray spectra by summing up those from all TES pixels under normal operation after selecting the events within a specific time window to extract the muon-beam induced signals [29]. The x-ray spectrum at a pressure of 0.9 atm after correction for the thermal crosstalk is shown in Fig. 1. A muonic x-ray peak from the 5-4 transition of  $\mu\text{Ne}$  is clearly seen at around 6300 eV. The 7-5 transition peak of  $\mu\text{Ne}$  is also identified at 5480 eV.

The typical expanded spectrum of the 5-4 transition peak at a pressure of 0.1 atm is shown in Fig. 2. To determine the transition energies, the muonic x-ray peaks were fitted with the curves obtained by a convolution of the line-shape model with the TES response function using the maximum likelihood method. We also employed a Bayesian analysis program [36, 37] to check correlations between the fitting parameters. The TES response function is a Gaussian function accompanied by a low-energy tail, which originates from the trapping of heat carriers in the Bi absorber [38]. The function has three parameters: the energy resolution and the fraction and length of the low-energy tail. The energy resolution was evaluated by fitting the  $\mu\text{Ne}$  peak. We fixed the two tail parameters obtained from the calibration  $K$  x-ray peaks under the off-beam condition.

The observed  $\mu\text{Ne}$  peak is a sum of contributions from two isotopes,  $^{20}\text{Ne}$  and  $^{22}\text{Ne}$ . Each isotopic component

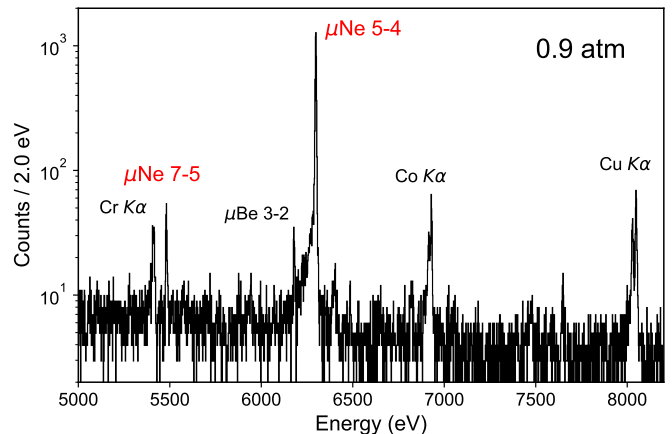


FIG. 1. An x-ray spectrum from 5-4 and 7-5 transitions of  $\mu\text{Ne}$  at a pressure of 0.9 atm. A muonic x-ray peak from  $\mu\text{Be}$  produced at the Be x-ray window in front of the TES detector, along with small calibration x-ray peaks, are also identified.

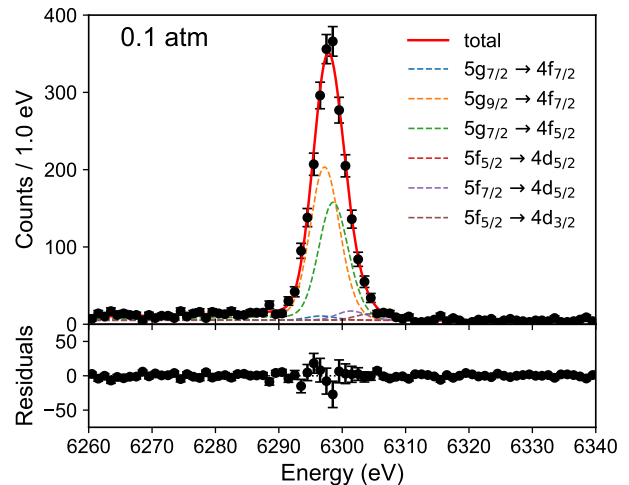


FIG. 2. X-ray spectra from 5-4 transitions of  $\mu\text{Ne}$  at a pressure of 0.1 atm. The fitted profiles obtained by summing up  $\mu^{20}\text{Ne}$  and  $\mu^{22}\text{Ne}$  contributions are also shown with residual errors. The fitting is carried out by using three spectra at pressures of 0.1, 0.4, and 0.9 atm simultaneously, and the reduced  $\chi^2$  (ndf: 284) for the total fitting is evaluated to be 1.26.

contains three  $5g-4f$  and three weaker  $5f-4d$  transitions. The theoretical values of the transition energies, QED, FNS, and recoil shifts, and relative intensity of  $\mu^{20}\text{Ne}$  are listed in Table I (transition energies for  $\mu^{22}\text{Ne}$  are found in the SM). These results were obtained by BSQED calculations that include first- and second-order QED corrections, the full Breit interaction, all-order retardation effects, and the FNS contributions using the MultiConfiguration Dirac Fock and General Matrix Elements (MCD-FGME) code [39–42]. This code can compute the above

TABLE I. Theoretically calculated energies of the  $\mu^{20}\text{Ne}$  5-4 transitions with BSQED (vacuum polarization from Uehling effect, self-energy, and higher-order contributions), FNS and recoil contributions, and relative intensities among fine-structure-resolved transition. The total transition energies contain all BSQED, FNS, and recoil shifts. The relative intensities are obtained assuming statistical distribution among fine-structure levels. We also list the energy shifts due to one  $K$ -shell electron screening. The uncertainties of the calculations are in the order of the last digit of each value.

Initial state	Final state	Transition energy (eV)						Relative intensity	one $K$ -shell $e^-$ energy shift (eV)
		Total transition energy	Vacuum polarization	Self-energy	QED order $\geq \alpha^2$	FNS	Recoil		
$5g_{9/2}$	$4f_{7/2}$	6297.26191	2.33803	-0.00152	0.02297	0.00031	0.00495	1.0000	-1.25198
$5g_{7/2}$	$4f_{7/2}$	6296.66427	2.33775	-0.00291	0.02297	0.00031	0.00497	0.0286	-1.25163
$5g_{7/2}$	$4f_{5/2}$	6298.61192	2.34051	0.00160	0.02295	0.00031	0.00491	0.7715	-1.25196
$5f_{7/2}$	$4d_{5/2}$	6301.43265	5.14445	-0.00345	0.04456	0.00137	0.00516	1.0000	-1.61866
$5f_{5/2}$	$4d_{5/2}$	6300.43536	5.14301	-0.00574	0.04455	0.00137	0.00519	0.0503	-1.61805
$5f_{5/2}$	$4d_{3/2}$	6304.34099	5.15641	0.00323	0.04461	0.00145	0.00507	0.6991	-1.61876

effects for muonic atoms with an arbitrary number of remaining electrons. The energy shifts due to the one  $K$ -shell electron screening are -1.25 and -1.62 eV for the  $5g$ - $4f$  and  $5f$ - $4d$  transitions, respectively. As seen in Table I, the theoretical calculation predicts that vacuum polarization dominates the shifts for all transitions that contribute to the observed line. Other contributions are more than two orders of magnitude smaller than vacuum polarization. The transition energy differences within the fine-structure-resolved levels are mainly explained by the spin-orbit interaction in the Dirac equation.

Transitions with different total angular momenta for the  $5g$ - $4f$  and  $5f$ - $4d$  transitions are not resolved by the detector. Thus, to fit the data, we allowed the energy of the most intense transition, i.e.,  $5g_{9/2}$ - $4f_{7/2}$ , to vary, and fixed the transition energy differences between the fine-structure levels and between  $5g$ - $4f$  and  $5f$ - $4d$  transitions to the calculated values in Table I. The relative intensities of the fine-structure levels are fixed to their statistical population. On the other hand, the intensity ratio between the  $5f$ - $4d$  and  $5g$ - $4f$  transitions,  $R_{5f-4d}$ , is affected by the details of the cascade deexcitation process. By also allowing  $R_{5f-4d}$  to vary, we arrived at five fitting parameters:  $5g_{9/2}$ - $4f_{7/2}$  transition energy for  $\mu^{20}\text{Ne}$ , intensity ratio  $R_{5f-4d}$ , total intensity, a constant background, and the energy resolution. Note that we fixed the energy differences and the relative intensities between  $\mu^{20}\text{Ne}$  and  $\mu^{22}\text{Ne}$  to the calculated values and the natural isotope abundance, respectively. The fitted result is shown in Fig. 2 with the residual error. With regard to the energy resolution, the experimental widths (FWHM) are 5.18(14), 5.50(12), and 5.51(11) eV at pressures of 0.1, 0.4, and 0.9 atm, respectively, whereas the resolutions for the beam-off condition are 5.0-5.2 eV at the Co  $K\alpha$  peak. The obtained  $R_{5f-4d}$  is 0.059(9), which is consistent with the well-known behavior that the deexcitation cascade dominantly proceeds via the transitions between the levels of  $\ell_\mu = n_\mu - 1$ .

The experimental  $5g_{9/2}$ - $4f_{7/2}$  transition energies for  $\mu^{20}\text{Ne}$  are given in Table II and shown in Fig. 3. As-

TABLE II. The experimental  $5g_{9/2}$ - $4f_{7/2}$  transition energies for  $\mu^{20}\text{Ne}$  and associated uncertainties.

Transition energy and uncertainties (eV)	$5g_{9/2}$ - $4f_{7/2}$		
	0.1 atm	0.4 atm	0.9 atm
measured energy	6297.13	6297.06	6297.05
statistical error	0.07	0.06	0.06
systematic error: total	0.13	0.13	0.13
1) calibration	0.07	0.07	0.07
2) low-energy tail	0.01	0.02	0.01
3) thermal crosstalk	0.11	0.11	0.11

sociated uncertainties are also listed in Table II. We consider three sources of systematic uncertainties: energy calibration, estimation of the low-energy tail of the TES response function, and the thermal crosstalk correction. 1) The calibration uncertainty of the TES detector is mainly determined by errors accompanying the interpolation between the anchor points. We evaluated the net uncertainty of our calibration by evaluating the peak energy of the Fe  $K\alpha$  line. Our obtained energy is 6404.01(7) eV, and we employed 0.07 eV as the net uncertainty. The peak energy agrees well with the reported energy of 6404.0062(99) eV, which was determined more precisely with a single-crystal diffractometer [35]. 2) The tail parameters might change from the off-beam values due to the thermal crosstalk. We tried fitting without fixing them and obtained the related errors. 3) Uncertainty due to the crosstalk correction is below 0.11 eV as already described. Thus, the total systematic errors were 0.13 eV, which were governed mainly by the calibration uncertainty and the crosstalk correction.

In order to evaluate contribution from remaining  $K$ -shell electrons in  $\mu\text{Ne}$ , we monitored the muonic x rays from the 7-5 transitions at around 5480 eV. In a sharp contrast to the 5-4 transitions, their energy shift due to the  $K$ -shell-electron screening is expected to be much larger, i.e., -6.93 eV and -7.68 eV for  $7h$ - $5g$  and  $7g$ - $5f$  transitions, respectively, while the BSQED contribution



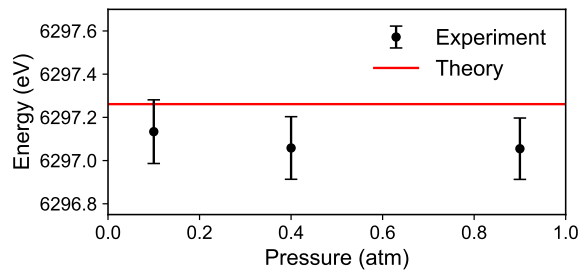


FIG. 3. Comparison of the obtained  $\mu^{20}\text{Ne } 5g_{9/2}-4f_{7/2}$  transition energies at pressures of 0.1, 0.4, and 0.9 atm with the theoretical value (red solid line).

is about six times smaller (see the SM). If  $\mu\text{Ne}$  with one  $K$ -shell electron at  $n_\mu = 7$  exists, the satellite structure would appear at the low-energy side of the main peak. We fitted the observed 7-5 spectrum considering the satellite contribution with a new fitting parameter  $f_{1e}$ , a fraction of  $\mu\text{Ne}$  with one  $K$  electron. The low number of counts in the peak prevents a determination of the relative intensity between the  $7g-5f$  and  $7h-5g$  peaks,  $R_{7g-5f}$ , by fitting. We employed instead the values,  $0.20 \leq R_{7g-5f} \leq 0.37$ , obtained from a muon cascade simulation by the Akylas-Vogel code [43]. Details of the simulation are discussed in the SM. The fitting result for the  $K$ -electron contribution is  $f_{1e} = 0.00^{+0.08}_{-0.00}$  for all  $R_{7g-5f}$  values considered here, which means that the  $\mu\text{Ne}$  atoms can be considered to be fully ionized. This result is also consistent from the viewpoint of the timescale of the relevant processes; the muon cascade proceeds within  $10^{-10}$  s at largest [20], while the time between charge transfer collisions of  $\mu\text{Ne}$  with the surrounding Ne is in the range of  $10^{-9}$  s [44].

In summary, we experimentally determined the  $5g_{9/2}-4f_{7/2}$  transition energy of  $\mu^{20}\text{Ne}$  to be  $6297.08 \pm 0.04$  (stat.)  $\pm 0.13$  (syst.) eV by averaging the data at pressures of 0.1, 0.4, and 0.9 atm. The statistical error is evaluated by the weighted average. This value agrees well with the most advanced BSQED theoretical prediction of 6297.26 eV. We also experimentally confirmed full ionization of  $\mu\text{Ne}$  from the 7-5 transition peak, which was possible thanks to the broadband feature of the TES detector. We obtained, for the first time, the QED vacuum polarization contribution to this transition with an accuracy of 5.8%, for the fully ionized exotic hydrogenlike two-body system under such low-pressure conditions free from both the effect of the FNS ( $\sim 0.01\%$  relative to the VP contribution) and the  $K$ -shell electron shift, while previous reports on BSQED tests by muonic atoms in solids have not satisfied these conditions [45–48]. Thus, the present measurement is regarded to be a significant milestone for strong-field BSQED tests. Presently, we are preparing the measurements of larger QED contribution ( $\sim 100$  eV) from the 4-3 transitions (44 keV) of  $\mu\text{Ar}$

by introducing newly-developed TES microcalorimeters covering the energy region up to 50 keV [49] which is not practically accessible with a crystal spectrometer.

We acknowledge Dr. M. Trassinelli for his valuable suggestions. We also acknowledge Dr. H. Tanuma for providing the information on charge exchange cross sections. The muon experiment at the Materials and Life Science Experimental Facility of the J-PARC was performed under a user program (2019MS01). This work was supported by the JSPS KAKENHI (Grant-in-Aid for Scientific Research on Innovative Areas, Toward new frontiers: encounter and synergy of state-of-the-art astronomical detectors and exotic quantum beams 18H05457, 18H05458, 18H05460, 18H05461, 18H05463, and 18H05464, Grant-in-Aid for Scientific Research (A) 18H03713 and 18H03714, and Grant-in-Aid for Young Scientists, 20K15238), and the RIKEN Pioneering Projects. N.P. thanks CNRS Institute of Physics for support and RIKEN for a young scientist fellowship. P.I. is a member of the Allianz Program of the Helmholtz Association, contract no EMMI HA-216 “Extremes of Density and Temperature: Cosmic Matter in the Laboratory”.

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- [1] V. A. Yerokhin, K. Pachucki, and V. Patkóš, *Ann. Phys.* **531**, 1800324 (2019).
- [2] C. G. Parthey, A. Matveev, J. Alnis, B. Bernhardt, A. Beyer, R. Holzwarth, A. Maistrou, R. Pohl, K. Predehl, T. Udem, et al., *Phys. Rev. Lett.* **107**, 203001 (2011).
- [3] A. Matveev, C. G. Parthey, K. Predehl, J. Alnis, A. Beyer, R. Holzwarth, T. Udem, T. Wilken, N. Kolachevsky, M. Abgrall, et al., *Phys. Rev. Lett.* **110**, 230801 (2013).
- [4] P. Indelicato, *J. Phys. B* **52**, 232001 (2019).
- [5] A. Gumberidze, T. Stöhlker, D. Banaś, K. Beckert, P. Beller, H. F. Beyer, F. Bosch, S. Hagmann, C. Kozhuharov, D. Liesen, et al., *Phys. Rev. Lett.* **94**, 223001 (2005).
- [6] A. V. Volotka, D. A. Glazov, G. Plunien, and V. M. Shabaev, *Ann. Phys. (Berlin)* **525**, 636 (2013).
- [7] D. Horváth, in *Handbook of Nuclear Chemistry*, edited by A. Vértes, S. Nagy, Z. Klencsár, R. G. Lovas, and F. Rösch (Springer, Boston, 2011), pp. 1485–1513, 2nd ed.
- [8] R. Pohl, A. Antognini, F. Nez, F. D. Amaro, F. Biraben, J. M. R. Cardoso, D. S. Covita, A. Dax, S. Dhawan, L. M. P. Fernandes, et al., *Nature* **466**, 213 (2010).
- [9] A. Antognini, F. Nez, K. Schuhmann, F. D. Amaro, F. Biraben, J. M. R. Cardoso, D. S. Covita, A. Dax, S. Dhawan, M. Diepold, et al., *Science* **339**, 417 (2013).
- [10] R. Pohl, F. Nez, L. M. P. Fernandes, F. D. Amaro,

- F. Biraben, J. M. R. Cardoso, D. S. Covita, A. Dax, S. Dhawan, M. Diepold, et al., *Science* **353**, 669 (2016).
- [11] J.-P. Karr, D. Marchand, and E. Voutier, *Nat. Rev. Phys.* **2**, 601 (2020).
- [12] J. J. Krauth, K. Schuhmann, M. A. Ahmed, F. D. Amaro, P. Amaro, F. Biraben, T.-L. Chen, D. S. Covita, A. J. Dax, M. Diepold, et al., *Nature* **589**, 527 (2021).
- [13] E. Borie and G. A. Rinker, *Rev. Mod. Phys.* **54**, 67 (1982).
- [14] N. Paul, G. Bian, T. Azuma, S. Okada, and P. Indelicato, *Phys. Rev. Lett.* **126**, 173001 (2021).
- [15] B. Jeckelmann, T. Nakada, W. Beer, G. de Chambrier, O. Elsenhans, K. L. Giovanetti, P. F. A. Goudsmit, H. J. Leisi, A. Rüetschi, O. Piller, et al., *Phys. Rev. Lett.* **56**, 1444 (1986).
- [16] B. Jeckelmann, P. Goudsmit, and H. Leisi, *Phys. Lett. B* **335**, 326 (1994).
- [17] P. Ehrhart, F. J. Hartmann, E. Köhler, and H. Daniel, *Z. Phys. A* **311**, 259 (1983).
- [18] R. Bacher, D. Gotta, L. M. Simons, J. Missimer, and N. C. Mukhopadhyay, *Phys. Rev. Lett.* **54**, 2087 (1985).
- [19] R. Jacot-Guillarmod, F. Bienz, M. Boschung, C. Piller, L. A. Schaller, L. Schellenberg, H. Schneuwly, and D. Siradovic, *Phys. Rev. A* **37**, 3795 (1988).
- [20] R. Bacher, P. Blüm, D. Gotta, K. Heitlinger, M. Schneider, J. Missimer, and L. M. Simons, *Phys. Rev. A* **39**, 1610 (1989).
- [21] L. Simons, D. Abbot, B. Bach, R. Bacher, A. Badertscher, P. Blüm, P. DeCecco, J. Eades, J. Egger, K. Elsener, et al., *Nucl. Instrum. Meth. Phys. Res. B* **87**, 293 (1994).
- [22] K. Kirch, D. Abbott, B. Bach, P. Hauser, P. Indelicato, F. Kottmann, J. Missimer, P. Patte, R. T. Siegel, L. M. Simons, et al., *Phys. Rev. A* **59**, 3375 (1999).
- [23] S. Lenz, G. Borchert, H. Gorke, D. Gotta, T. Siems, D. Anagnostopoulos, M. Augsburg, D. Chatellard, J. Egger, D. Belmiloud, et al., *Phys. Lett. B* **416**, 50 (1998).
- [24] M. Trassinelli, D. Anagnostopoulos, G. Borchert, A. Dax, J.-P. Egger, D. Gotta, M. Hennebach, P. Indelicato, Y.-W. Liu, B. Manil, et al., *Phys. Lett. B* **759**, 583 (2016).
- [25] W. Higemoto, R. Kadono, N. Kawamura, A. Koda, K. Kojima, S. Makimura, S. Matoba, Y. Miyake, K. Shimomura, and P. Strasser, *Quantum Beam Sci.* **1**, 11 (2017).
- [26] S. Okada, D. A. Bennett, C. Curceanu, W. B. Doriese, J. W. Fowler, J. D. Gard, F. P. Gustafsson, T. Hashimoto, R. S. Hayano, S. Hirenzaki, et al., *Prog. Theor. Exp. Phys.* **2016**, 091D01 (2016).
- [27] T. Okumura, T. Azuma, D. A. Bennett, P. Caradonna, I. Chiu, W. B. Doriese, M. S. Durkin, J. W. Fowler, J. D. Gard, T. Hashimoto, et al., *Phys. Rev. Lett.* **127**, 053001 (2021).
- [28] T. Hashimoto, S. Aikawa, T. Akaishi, H. Asano, M. Bazzi, D. A. Bennett, M. Berger, D. Bosnar, A. D. Butt, C. Curceanu, et al., *Phys. Rev. Lett.* **128**, 112503 (2022).
- [29] S. Okada, T. Azuma, D. A. Bennett, P. Caradonna, W. B. Doriese, M. S. Durkin, J. W. Fowler, J. D. Gard, T. Hashimoto, R. Hayakawa, et al., *J. Low Temp. Phys.* **200**, 445 (2020).
- [30] T. Okumura, T. Azuma, D. A. Bennett, P. Caradonna, I.-H. Chiu, W. B. Doriese, M. S. Durkin, J. W. Fowler, J. D. Gard, T. Hashimoto, et al., *IEEE Trans. Appl. Supercond.* **31**, 1 (2021).
- [31] W. B. Doriese, P. Abbamonte, B. K. Alpert, D. A. Bennett, E. V. Denison, Y. Fang, D. A. Fischer, C. P. Fitzgerald, J. W. Fowler, J. D. Gard, et al., *Rev. Sci. Instrum.* **88**, 053108 (2017).
- [32] J. W. Fowler, B. K. Alpert, D. A. Bennett, W. B. Doriese, J. D. Gard, G. C. Hilton, L. T. Hudson, Y.-I. Joe, K. M. Morgan, G. C. O'Neil, et al., *Metrologia* **54**, 494 (2017).
- [33] J. W. Fowler, G. C. O'Neil, B. K. Alpert, D. A. Bennett, E. V. Denison, W. B. Doriese, G. C. Hilton, L. T. Hudson, Y.-I. Joe, K. M. Morgan, et al., *Metrologia* **58**, 015016 (2021).
- [34] G. Hölzer, M. Fritsch, M. Deutsch, J. Härtwig, and E. Förster, *Phys. Rev. A* **56**, 4554 (1997).
- [35] R. D. Deslattes, E. G. Kessler, P. Indelicato, L. de Billy, E. Lindroth, and J. Anton, *Rev. Mod. Phys.* **75**, 35 (2003).
- [36] M. Trassinelli, *Nucl. Instrum. Meth. Phys. Res. B* **408**, 301 (2017).
- [37] M. Trassinelli, *Proceedings* **33**, 14 (2019).
- [38] H. Tatsuno, W. B. Doriese, D. A. Bennett, C. Curceanu, J. W. Fowler, J. Gard, F. P. Gustafsson, T. Hashimoto, R. S. Hayano, J. P. Hays-Wehle, et al., *J. Low Temp. Phys.* **184**, 930 (2016).
- [39] J. V. Mallow, J. P. Desclaux, and A. J. Freeman, *Phys. Rev. A* **17**, 1804 (1978).
- [40] J. P. Santos, F. Parente, S. Boucard, P. Indelicato, and J. P. Desclaux, *Phys. Rev. A* **71**, 032501 (2005).
- [41] M. Trassinelli and P. Indelicato, *Phys. Rev. A* **76**, 012510 (2007).
- [42] P. Indelicato, *Phys. Rev. A* **87**, 022501 (2013).
- [43] V. R. Akylas and P. Vogel, *Comput. Phys. Commun.* **15**, 291 (1978).
- [44] K. Suzuki, K. Okuno, and N. Kobayashi, *Phys. Scr.* **T73**, 172 (1997).
- [45] R. Eichler, B. Aas, W. Beer, I. Beltrami, P. Ebersold, T. v. Ledebur, H. J. Leisi, W. W. Sapp, J. C. Dousse, J. Kern, et al., *Phys. Lett. B* **76**, 231 (1978).
- [46] B. Aas, W. Beer, I. Beltrami, P. Ebersold, R. Eichler, T. V. Ledebur, H. J. Leisi, W. Ruckstuhl, W. W. Sapp, A. Vacchi, et al., *Nucl. Phys. A* **375**, 405 (1982).
- [47] W. Ruckstuhl, B. Aas, W. Beer, I. Beltrami, F. W. N. de Boer, K. Bos, P. F. A. Goudsmit, U. Kiebele, H. J. Leisi, G. Strassner, et al., *Phys. Rev. Lett.* **49**, 859 (1982).
- [48] I. Beltrami, B. Aas, W. Beer, P. Ebersold, R. Eichler, P. F. A. Goudsmit, M. Guanziroli, T. v. Ledebur, H. J. Leisi, W. Ruckstuhl, et al., *Nucl. Phys. A* **429**, 381 (1984).
- [49] D. Yan, J. Weber, K. Morgan, A. Wessels, D. Bennett, C. Pappas, J. Mates, J. Gard, D. Becker, J. Fowler, et al., *IEEE Trans. Appl. Supercond.* **31**, 2100505 (2021).