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# Molecular gas cloud properties at $z \simeq 1$ revealed by the superb angular resolution achieved with ALMA and gravitational lensing 

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#### Abstract

Current observations favour that the massive ultraviolet-bright clumps with a median stellar mass of $\sim 10^{7} \mathrm{M}_{\odot}$, ubiquitously observed in $z \sim 1-3$ galaxies, are star-forming regions formed in situ in galaxies. It has been proposed that they result from gas fragmentation due to gravitational instability of gas-rich, turbulent, and high-redshift discs. We bring support to this scenario by reporting the new discovery of giant molecular clouds (GMCs) in the strongly lensed, clumpy, main-sequence galaxy, A521-sys1, at $z=1.043$. Its $\operatorname{CO}(4-3)$ emission was mapped with the Atacama Large Millimetre/submillimetre Array (ALMA) at an angular resolution of $0.19 \times 0.16 \mathrm{arcsec}^{2}$, reading down to 30 pc , thanks to gravitational lensing. We identified 14 GMCs, most being virialized, with $10^{5.9}-10^{7.9} \mathrm{M}_{\odot}$ masses and a median $800 \mathrm{M}_{\odot} \mathrm{pc}^{-2}$ molecular gas mass surface density, that are, respectively, 100 and 10 times higher than for nearby GMCs. They are also characterized by 10 times higher supersonic turbulence with a median Mach number of 60 . They end up to fall above the Larson scaling relations, similarly to the GMCs in another clumpy $z$ $\simeq 1$ galaxy, the Cosmic Snake, although differences between the two sets of high-redshift GMCs exist. Altogether they support that GMCs form with properties that adjust to the ambient interstellar medium conditions prevalent in the host galaxy whatever its redshift. The detected A521-sys1 GMCs are massive enough to be the parent gas clouds of stellar clumps, with a relatively high star formation efficiency per free-fall time of $\sim 11$ per cent.


Key words: gravitational lensing: strong - galaxies: high-redshift - galaxies: individual: A521-sys1 - galaxies: ISM - galaxies: star formation.

## 1 INTRODUCTION

The understanding of the process of star formation at high redshift, which drives the stellar mass build-up of galaxies across cosmic time, evolves in synergy with better observational facilities and not only the improvement of their sensitivity, but specifically their spatial resolution. The Hubble Space Telescope (HST) has delivered unprecedented, resolved near-ultraviolet (UV) to near-infrared (IR) images of high-redshift galaxies. They revealed that about 60 per cent of star-forming galaxies around the peak of the cosmic star formation rate density $(1<z<3)$ have perturbed morphologies, dominated by giant UV-bright star-forming knots/clumps (e.g. Cowie, Hu \& Songaila 1995; Conselice et al. 2004; Elmegreen et al. 2007, 2013; Livermore et al. 2012, 2015; Guo et al. 2012, 2015, 2018; Soto et al. 2017; Zanella et al. 2019). The origin and nature of these clumps

[^0]have been debated over two decades now, while their understanding could provide key information on: the mass assembly of galaxies, via mergers or secular evolution, depending on whether the clumps we see are 'ex situ' satellites resulting from a merger event or are formed locally ('in situ') in galaxies; the structural evolution of the host galaxy if clumps contribute to the bulge growth when migrating towards the galactic centre; the star formation process of highredshift galaxies if clumps are star-forming regions formed in situ in galaxies; and the role clumps play in the galactic stellar feedback and Lyman continuum ionizing photons (Dessauges-Zavadsky et al. 2020).

Several observational findings currently support that the observed clumps are star cluster complexes/large star-forming regions formed in situ in high-redshift galaxies. We can cite the study by Shibuya et al. (2016) of 17000 galaxies from the HST legacy surveys, which evidenced that the redshift evolution of the clumpy galaxy fraction differs from the one of both minor and major mergers (Lotz et al. 2011). The same authors also showed that the bulk of the clumpy
galaxies are disc-like systems with a Sérsic index close to 1 . This is consistent with their kinematics found to be dominated by ordered disc rotation with high velocity dispersions, similarly to the majority of star-forming galaxies at $0.8<z<$ (e.g. Förster Schreiber et al. 2009; Wisnioski et al. 2015; Simons et al. 2017; Turner et al. 2017; Übler et al. 2019; Girard et al. 2018, 2020). Moreover, Elmegreen et al. (2017) determined that the scale heights of clumpy galaxies and those of normal spirals when seen edge on are comparable, indicating that clumps are distributed within the disc thickness of the host galaxy (see also Elmegreen \& Elmegreen 2006). Finally, Dessauges-Zavadsky \& Adamo (2018) reported that the stellar mass function of clumps at $1<z<3$ follows a power law with a slope close to -2 , similar to the one of local/nearby star clusters and H II regions (e.g. Adamo et al. 2017; Grasha et al. 2017; Messa et al. 2018), and expected if clumps are formed via the turbulence-driven fragmentation process (Elmegreen et al. 2006; Guszejnov, Hopkins \& Grudić 2018; Ma et al. 2020).

The compilation of UV-bright clumps hosted the HST Ultra Deep Field galaxies and in the strongly lensed galaxies, now also imaged with the JWST, which benefits from the best sensitivity and the best spatial resolution imaging, shows clump sizes $\lesssim 300 \mathrm{pc}$ and stellar masses ranging from $\sim 10^{5}$ to $\sim 10^{9} \mathrm{M}_{\odot}$ with a median of $\sim 10^{7} \mathrm{M}_{\odot}$ (Elmegreen et al. 2013; Dessauges-Zavadsky et al. 2017; Cava et al. 2018; Claeyssens et al. 2022; Messa et al. 2022; Meštrić et al. 2022). These revised clump properties, indicating sizes much smaller than 1 kpc and masses with a median lower than $10^{8.5-9} \mathrm{M}_{\odot}$ initially reported, nevertheless, confirm that the high-redshift clumps remain more massive by $2-3$ orders of magnitude than the local/nearby star clusters (e.g. Bastian et al. 2006; Adamo et al. 2013). They yet have stellar mass surface densities comparable to the average surface density of a nearby massive cluster (Brown \& Gnedin 2021; Claeyssens et al. 2022; Messa et al. 2022). They are very well reproduced by the high-resolution hydrodynamical simulations (e.g. Tamburello et al. 2015; Mandelker et al. 2017; Fensch \& Bournaud 2021), which have proposed that the high-redshift, gas-rich, rotationdominated galaxies, characterized by highly turbulent gas discs, fragment because of violent gravitational instability driven by intense cosmic web cold gas inflows (e.g. Agertz, Teyssier \& Moore 2009; Dekel et al. 2009; Bournaud et al. 2010) and produce gravitationally bound gas clouds, the progenitors of the stellar clumps ubiquitously seen in high-redshift galaxies. If this scenario is correct, one should also observe the parent gas clouds.

The cold molecular gas in nearby galaxies is usually traced by the carbon monoxide ( CO ) and is structured in giant molecular clouds (GMCs). These GMCs with $10^{4}-10^{7} \mathrm{M}_{\odot}$ masses and 5100 pc radii contract and form star clusters (Bolatto, Wolfire \& Leroy 2013). Their detection at such a small scale in distant galaxies is observationally challenging even in interferometric data. Numerous studies searching for these clouds in the far-IR dust-continuum images of high-redshift submillimetre galaxies (SMGs) led to nondetections showing essentially a smooth dust emission (e.g. Hodge et al. 2016, 2019; Gullberg et al. 2018; Rujopakarn et al. 2019; Ivison et al. 2020). Only a few studies reported GMC detections in the CO emission maps of SMGs (Swinbank et al. 2015; Cañameras et al. 2017; Tadaki et al. 2018). We obtained the first detection of GMCs in a clumpy, main-sequence, rotation-dominated galaxy - the strongly lensed Cosmic Snake galaxy at $z=1.036$ - characterized by a stellar mass of $M_{\text {stars }}=(4.0 \pm 0.5) \times 10^{10} \mathrm{M}_{\odot}$, a star formation rate of $\mathrm{SFR}=30 \pm 10 \mathrm{M}_{\odot} \mathrm{yr}^{-1}$, and a molecular gas to stellar mass fraction of $f_{\text {molgas }}=25 \pm 4$ per cent (DessaugesZavadsky et al. 2019). The kinematics, the metallicity, and the radial profiles of surface densities of $M_{\text {stars }}, \mathrm{SFR}$, molecular gas
mass ( $M_{\text {molgas }}$ ), and dust mass of the Cosmic Snake galaxy were studied by Patrício et al. $(2018,2019)$, Girard et al. (2019), and Nagy et al. (2022), respectively. The combination of the superb angular resolution achieved with Atacama Large Millimetre/submillimetre Array (ALMA) and gravitational lensing allowed to map the emission of the $\mathrm{CO}(4-3)$ line of this galaxy at the resolution of nearby galaxies (Sun et al. 2018; Rosolowsky et al. 2021), reading down to 30 pc , and to perform the GMC search in the velocity space (in channel intensity maps). We identified 17 GMCs with on average 100 times higher $M_{\text {molgas }}$ and 10 times higher $M_{\text {molgas }}$ surface densities than for most of the local/nearby GMCs (Dessauges-Zavadsky et al. 2019). The high masses of the identified GMCs are close to the stellar masses of the UV-bright clumps detected by Cava et al. (2018) in comparable numbers in the HST images of the Cosmic Snake galaxy at a similar spatial resolution to the $A L M A$ images. In DessaugesZavadsky et al. (2019), we concluded that this corroborates the in situ formation of high-redshift stellar clumps. Moreover, we proposed that the physical properties derived for the Cosmic Snake GMCs (high-mass, high-density, and high internal turbulence) suggest that, also at high redshift, GMCs seem to form with properties that adjust to the host galaxy's ambient interstellar medium (ISM) conditions (pressure, turbulence, density, etc.), as observed for nearby GMCs (Hughes et al. 2013; Sun et al. 2018, 2020).

In this work, we study another clumpy, main-sequence, prototypical Milky Way galaxy - the A521-sys1 galaxy at $z=1.043-$ strongly lensed by the galaxy cluster Abell 521. Its kinematics is characteristic of rotation-dominated galaxies at cosmic noon, with a high velocity dispersion and a low rotation velocity over velocity dispersion ratio of $\sim 2$ (Patrício et al. 2018; Girard et al. 2019). Resembling the Cosmic Snake galaxy, in terms of redshift, $M_{\text {stars }}$ $=(7.4 \pm 1.2) \times 10^{10} \mathrm{M}_{\odot}, \mathrm{SFR}=26 \pm 5 \mathrm{M}_{\odot} \mathrm{yr}^{-1}$ (Nagy et al. 2022), and $f_{\text {molgas }}=14 \pm 3$ per cent (this work), we seek to test and generalize the results found for the Cosmic Snake GMCs. A detailed analysis of the HST near-UV to near-IR images by Messa et al. (2022) allowed to identify 18 UV-bright clumps with stellar masses of $1.5 \times 10^{6}-6 \times 10^{8} \mathrm{M}_{\odot}$. Here, we analyse the ALMA $\mathrm{CO}(4-3)$ observations obtained at a spatial resolution close to the HST images, which we use to search for GMCs down to a physical scale of $\sim 30 \mathrm{pc}$.

The paper is organized as follows. In Section 2, the lens model of Abell 521 is presented. Section 3 describes the $A L M A$ observations, and the data reduction and imaging. In Section 4, we explain how the search for the molecular clouds was performed and how their physical properties were derived. We discuss the GMC physical properties and their implications in Section 5. Our conclusions can be found in Section 6. We adopt the $\Lambda$-CDM cosmology with $H_{0}=$ $70 \mathrm{~km} \mathrm{~s}^{-1} \mathrm{Mpc}^{-1}, \Omega_{\mathrm{M}}=0.3, \Omega_{\Lambda}=0.7$, and the Salpeter (1955) initial mass function.

## 2 LENS MODEL

Lensed by the galaxy cluster Abell 521, the targeted galaxy A521sys1 is multiply imaged as illustrated in Fig. 1. There is one isolated and uniformly lensed image of the entire galaxy, magnified by a factor $\mu=2-6$, observed in the north-east; and five strongly magnified and stretched images, covering about 55 per cent of the galaxy, which form a wide arc in the western direction of 11 arcsec in length from north to south, with high $\mu$ ranging from 3 to $>50$ and even $>100$ in subregions close to the critical line (see Nagy et al. 2022, fig. 2 for a magnification map). The former image reveals the spiral structure of the galaxy with two spiral arms, while the latter images provide a zoom-in on the internal structure of less than half of the galaxy


Figure 1. HST RGB-colour composite image (red filter: F160W; green: F105W; blue: F606W) of the multiply imaged A521-sys1 galaxy together with the foreground Abell 521 galaxy cluster. The black crosses mark the cluster members. The critical line of our lens model at $z=1.043$, the redshift of the A521-sys1 galaxy, is shown by the red solid line. The entire A521-sys1 galaxy can be seen in the north-east isolated and uniformly lensed image, which reveals the spiral structure of the galaxy with two spiral arms. The 11 arcsec-long arc in the western direction is a fivefold multiple image of the A521-sys1 galaxy, with two main mirrored images encompassing the critical line, and the remaining multiple images covering a small region around the closed critical line in the north of the arc. Only about 55 per cent of the galaxy, including less than half of the galactic central region and one spiral arm (the western arm of the isolated counter-image), is multiply imaged along the arc, as shown by the cyan dashed line that delimits southward the zone of multiple images. The overlaid white contours correspond to the $A L M A \operatorname{CO}(4-3)$ velocity-integrated intensity in levels of $4 \sigma, 5 \sigma, 6 \sigma, 7 \sigma, 8 \sigma, 10 \sigma, 12 \sigma$, and $14 \sigma$, with the RMS noise of $0.01 \mathrm{Jy} \mathrm{beam}^{-1} \mathrm{~km} \mathrm{~s}^{-1}$. The ALMA synthesized beam with a size of $0.19 \times 0.16 \operatorname{arcsec}^{2}$ at the position angle of $-74^{\circ}$ is represented by the white ellipse. We give a reference scale of 2 arcsec. The left inset shows the HST RGB-colour composite source-plane reconstruction of the lensed isolated image with the source-plane reconstructed $\mathrm{CO}(4-3)$ velocity-integrated intensity $4 \sigma$ contours (in white) detected in the arc. The 14 identified GMCs are not resolved in the source-plane image, they are distributed within the $\mathrm{CO}(4-3) 4 \sigma$ contours.
including the western spiral arm of the former image. We use the tailored lens model of the A521 cluster from Richard et al. (2010), which was refined to better match the arc at $z=1.043$ by using seven multiply imaged UV-bright clumps as constraints (see Messa et al. 2022, for details). The resulting root-mean-square (RMS) noise between the observed and predicted locations measured in the imageplane is 0.08 arcsec, and $\mu$ is determined with a typical uncertainty of the order of $\sim 10-20$ per cent. The reconstructed source-plane image of the A521-sys1 galaxy is shown in the left inset of Fig. 1.

## 3 ALMA OBSERVATIONS, DATA REDUCTION, AND IMAGING

The A521-sys1 galaxy was observed in Cycle 4 (2016.1.00643.S) in band 6 with 41 ALMA 12 m antennas in the C40-6 configuration (maximum baseline of 3.1 km ) during 89 min of on-source time. The redshifted $\mathrm{CO}(4-3)$ line frequency at 225.6685 GHz was used to tune the spectral window 2 , whose spectral resolution was set to $7.8125 \mathrm{MHz}\left(10.3782 \mathrm{~km} \mathrm{~s}^{-1}\right)$. We used the remaining three 1.875 GHz spectral windows for continuum emission. As described in Girard et al. (2019), the ALMA data were reduced following the reduction pipeline distributed within the Common Astronomy Software Application (CASA; McMullin et al. 2007). For the CO(43) line imaging, we used a pixel size of 0.03 arcsec and the

Briggs weighting with the robust factor of 0.5 , and we cleaned all channels until convergence using the clean routine in CASA with a custom mask. According to the ALMA Technical Handbook, the adopted weighting scheme is known to deliver low sidelobe levels for $\sim 1 \mathrm{~h}$ observations and to give a reasonable balance between spatial resolution and sensitivity. We finally applied the primary beam correction. The synthesized beam size of the resulting $\mathrm{CO}(4-$ 3) line data cube is $0.19 \times 0.16 \operatorname{arcsec}^{2}$ at the position angle of $-74^{\circ}$. The cube has an RMS noise of $0.2 \mathrm{mJy} \mathrm{beam}^{-1}$ per $10.3782 \mathrm{~km} \mathrm{~s}^{-1}$ channel. The calibrated visibilities of continuum over the four spectral windows, when excluding channels where the $\mathrm{CO}(4-3)$ emission was detected, were also imaged, but no 1.3 mm continuum was detected.

The immoments routine in CASA was used to obtain moment maps of the $\mathrm{CO}(4-3)$ emission. The threshold was fixed to $4 \sigma$ RMS when computing the velocity first-moment and the velocity dispersion second-moment. We used the same routine to extract 12channel intensity maps (zero-moment maps), at the native spectral resolution of $10.3782 \mathrm{~km} \mathrm{~s}^{-1}$, of the $\mathrm{CO}(4-3)$ emission covering the velocity range from -41 to $+73 \mathrm{~km} \mathrm{~s}^{-1}$; the zero velocity was set to $z=1.043425$. The respective channel maps are plotted in Fig. A1.

In Fig. 1, we overlay the contours of the $\mathrm{CO}(4-3)$ velocityintegrated intensity on the HST RGB-colour composite image of the A521-sys1 galaxy. The two spiral arms nicely visible in the HST
near-UV to near-IR images of the north-east isolated and uniformly lensed image are also detected in the $\mathrm{CO}(4-3)$ emission, together with the CO-bright galactic central region. The western spiral arm is clearly more gas-rich than the eastern spiral arm. By chance, the western spiral arm is the arm that is multiply imaged over the arc, where it benefits from high magnification factors. Nagy et al. (2022) showed that the $\mathrm{CO}(4-3)$ emission extends out to the galactocentric radius of $\sim 6 \mathrm{kpc}$ in the A521-sys 1 source galaxy. This corresponds to $\sim 1 / 3$ of the radial extent of the stellar emission ( $\sim 20 \mathrm{kpc}$ ) in the restframe optical HST F160W filter. Asymmetries in the molecular gas distribution between two spiral arms and in scale lengths of the stellar and molecular gas emission radial profiles are common in galaxies: they can be inherited from the cosmic web accretion pattern, but they can also be due to internal instabilities and the fact that dark matter haloes are not spherical and can produce warps, bending modes, etc. Finally, asymmetries can be induced by interactions with (big) satellites. In the case of the A521-sys1 galaxy, there is no evidence of a massive satellite at small projected distance.

## 4 ANALYSIS

### 4.1 Search for molecular clouds

To search for GMCs in the A521-sys1 galaxy, we considered only the multiple images within the arc, because there the magnification factors are the higher (yielding to a better spatial resolution) and the arc is located close to the phase centre, such that the RMS noise over the arc's $\mathrm{CO}(4-3)$ emission is almost constant, affected by less than 4 per cent by the primary beam attenuation. We followed the methodology developed in Dessauges-Zavadsky et al. (2019) for the Cosmic Snake galaxy, which consisted in exploiting the three dimensions of the $\mathrm{CO}(4-3)$ data cube by searching for emission peaks of the molecular clouds in the 12-channel intensity maps extracted over the $\mathrm{CO}(4-3)$ emission (Fig. A1). The reliability of an emission detection against noise was evaluated by computing the fidelity of the detection at a given significance:
fidelity $(\mathrm{S} / \mathrm{N})=1-\frac{N_{\mathrm{neg}}(\mathrm{S} / \mathrm{N})}{N_{\mathrm{pos}}(\mathrm{S} / \mathrm{N})}$,
where $N_{\mathrm{pos}}$ and $N_{\text {neg }}$ are, respectively, the number of positive and negative emission detections with a given signal-to-noise ratio ( $\mathrm{S} / \mathrm{N}$ ) in the primary beam (Walter et al. 2016; Decarli et al. 2019). In individual channel maps, the fidelity of 100 per cent was reached at $\mathrm{S} / \mathrm{N}=4.8$, thus we first extracted, in the primary beam, all $>4.8 \sigma$ emissions per channel. Then, we considered emissions spatially overlapping in two adjacent $10.3782 \mathrm{~km} \mathrm{~s}^{-1}$ channel maps, for which the fidelity of 100 per cent was reached at $\mathrm{S} / \mathrm{N}=3.9$ per channel (equivalent to $\mathrm{S} / \mathrm{N}=5.5$ for two adjacent channels). Therefore, we also extracted all $>3.9 \sigma$ emissions co-spatial in at least two adjacent channel maps. ${ }^{1}$ All the extracted $\mathrm{CO}(4-3)$ emissions were found to be distributed over the position of the detected $\mathrm{CO}(4-$ 3 ) velocity-integrated intensity of the A521-sys1 multiple images, whose contours are shown in white in Fig. 1. This provided support that the extracted emissions were detected at sufficiently high $\mathrm{S} / \mathrm{N}$ to be real and were not noise peaks since they were not randomly distributed. As an additional test, we also performed the search for cloud's emission peaks in the 'dirty' channel maps (before the

[^1]clean) that gave the same results as the emission search in the cleaned channel maps. This allowed us to establish that the clean did not give rise to noise peaks or artificial cloud detections.

Similarly to the analysis performed for the Cosmic Snake galaxy (Dessauges-Zavadsky et al. 2019), we adopted the same definition of molecular clouds by considering $\mathrm{CO}(4-3)$ emissions as belonging to distinct clouds when their $4 \sigma$ contours were not spatially overlapping in the same channel map, or when their $4 \sigma$ contours were co-spatial, but not in adjacent channel maps (i.e. when separated by at least one channel). This allows clouds to overlap in either velocity or physical space, but not both. Following the above definition, with the help of the lens model, we could group the extracted $\mathrm{CO}(4-3)$ emissions spread over the A521 arc in 24 multiple images of 14 distinct GMCs. We found no GMCs overlapping along the same line of sight, and almost all GMCs (except the GMCs with IDs 1 and 2) were multiply imaged (two to three times) in the 12-channel intensity maps analysed, as shown in Fig. A1. In fact, all the GMCs identified in one single channel map (the GMCs with IDs 7, 9, and 12), except GMC 6, are detected in the two multiple images predicted by the lens model in the arc. The detection of these respective multiple images at the predicted locations reinforces the reliability of these GMCs, since it is unlikely to find two noise features sitting at these predicted locations. In the case of the GMC 6, we detect only one multiple image, which, in reality, is a blend (within the synthesized beam) of two predicted multiple images because it is located almost on the critical line (see Fig. A1; same for the GMC 13). The detection of multiple images also enables us to alleviate the caveat of the possible effect of the Gibbs phenomenon, which is known to produce a non-trivial correlation across two adjacent channels resulting from the post-processing smoothing (e.g. Hanning; see the ALMA Technical Handbook). Again, all the GMCs identified over less than three adjacent channel maps, which could be affected by the Gibbs phenomenon (the GMCs with IDs 10 and 14), are detected in two multiple images. Finally, in Appendix B, we discuss the results of the CASA visibility simulations we performed, excluding the possibility that the identified GMCs are artificial clumpy features produced by lensing and interferometric effects out of a smooth exponential disc of $\mathrm{CO}(4-3)$ emission.

The significance level of the 14 identified GMCs ranges between $\sim 5 \sigma$ and $\sim 14 \sigma$ (Table 1 ) when integrated over their extent in velocity space from one to five adjacent $10.3782 \mathrm{~km} \mathrm{~s}^{-1}$ channels. The GMCs with IDs $10-14$ are found near the galactic centre, and the GMCs with IDs $1-10$ are spread along the spiral arm (the western arm of the uniformly lensed image; see Fig. 1).

The 14 GMCs are spatially offset from the 13 UV-bright stellar clumps detected over the arc by Messa et al. (2022, see their fig. 2). The closest GMC/stellar clump pairs, located both near the galactic centre and in the spiral arm, have a separation which ranges between $\sim 110$ and $\sim 980 \mathrm{pc}$, with a median $/ \mathrm{mean}$ of $\sim 590 \mathrm{pc}$. This represents quite a large drift for the young stars from their birth place given the estimated ages of the stellar clumps $<100 \mathrm{Myr}$ (the majority even have best-fitting ages close to 10 Myr , although with large uncertainties), much shorter than the dynamical time of the host galaxy (Messa et al. 2022). The association between the identified GMCs and stellar clumps can thus be questionable. Considering the typical lifetime of GMCs in local galaxies ( $\sim 10-30 \mathrm{Myr}$; Kruijssen et al. 2019; Chevance et al. 2020; Kim et al. 2021), we can also wonder if the stellar clumps we are observing in A521-sys1 are not already old enough to have destroyed/dispersed their parent GMCs after the episode of star formation, unless high-redshift GMCs are more long-lived than the local ones given their different physical properties (see Section 5).

Table 1. Physical properties of the 14 GMCs identified in the A521-sys1 galaxy. The description of their measurements can be found in Section 4.2. $M_{\text {molgas }}$ is the GMC lensing-corrected molecular gas mass obtained by adopting the CO-to- $\mathrm{H}_{2}$ conversion factor, $\alpha_{\mathrm{CO}}=1.9 \pm 0.4 \mathrm{M}_{\odot}\left(\mathrm{K} \mathrm{km} \mathrm{s}^{-1} \mathrm{pc}^{2}\right)^{-1}$, derived in Section 4.3, $R$ is the GMC lensing-corrected beam-deconvolved circularized FWHM radius, $\sigma_{v}$ is the GMC interval velocity dispersion, and $\mu$ is the GMC mean magnification factor. The listed values were measured on the multiple images with the less blended $\mathrm{CO}(4-3)$ emissions in channel intensity maps (see Fig. A1). The GMCs with IDs $1-10$ are spread along the spiral arm, and the GMCs with IDs 11-14 are located near the galactic centre. The letters are used to refer to the different multiple images of a given GMC, labelled following the nomenclature explained in Appendix A and shown in Fig. A1.

| GMC | $M_{\text {molgas }}$ <br> $10^{6} \mathrm{M}_{\odot}$ | $R$ <br> pc | $\sigma_{v}$ <br> $\mathrm{~km} \mathrm{~s}^{-1}$ | $\mu$ | Detection <br> significance |
| :--- | :---: | :---: | :---: | :---: | :---: |
| 1N | $77 \pm 11$ | $166 \pm 16$ | $21 \pm 4$ | $18 \pm 4$ | $10.7 \sigma$ |
| 2N | $66 \pm 12$ | $129 \pm 21$ | $17 \pm 4$ | $24 \pm 3$ | $12.0 \sigma$ |
| 3CS | $44 \pm 7$ | $144 \pm 37$ | $17 \pm 3$ | $26 \pm 4$ | $9.7 \sigma$ |
| 4CS | $18 \pm 4$ | $89 \pm 42$ | $11 \pm 4$ | $66 \pm 14$ | $8.5 \sigma$ |
| 5N | $37 \pm 5$ | $104 \pm 38$ | $25 \pm 8$ | $30 \pm 3$ | $9.0 \sigma$ |
| 6C | $0.8 \pm 0.1$ | $31 \pm 6$ | $20 \pm 6$ | $366 \pm 38$ | $4.8 \sigma$ |
| 7S | $28 \pm 5$ | $107 \pm 15$ | $16 \pm 4$ | $9 \pm 2$ | $6.8 \sigma$ |
| 8N | $61 \pm 10$ | $117 \pm 19$ | $12 \pm 5$ | $16 \pm 3$ | $9.4 \sigma$ |
| 9S | $6 \pm 1$ | $94 \pm 14$ | $8 \pm 2$ | $48 \pm 7$ | $7.2 \sigma$ |
| 10S | $32 \pm 5$ | $112 \pm 19$ | $5 \pm 2$ | $20 \pm 4$ | $7.5 \sigma$ |
| 11S | $41 \pm 5$ | $94 \pm 25$ | $16 \pm 4$ | $78 \pm 24$ | $13.9 \sigma$ |
| 12S | $15 \pm 2$ | $102 \pm 23$ | $11 \pm 3$ | $33 \pm 5$ | $6.9 \sigma$ |
| 13NS | $6 \pm 1$ | $28 \pm 7$ | $15 \pm 4$ | $428 \pm 147$ | $12.4 \sigma$ |
| 14S | $22 \pm 3$ | $140 \pm 29$ | $14 \pm 4$ | $35 \pm 5$ | $6.7 \sigma$ |

### 4.2 Physical properties of molecular clouds

The molecular gas mass of each multiple image of a given GMC was derived by summing the lensing-corrected line-integrated fluxes of all the $\mathrm{CO}(4-3)$ emissions extracted for that image over a number of adjacent channels. To measure the fluxes, we used custom apertures per channel, large enough to include for each emission, all the signal above the local RMS noise level (no aperture correction was needed as the apertures used were all larger than the synthesized beam). To correct for the lensing, we considered the mean magnification factor computed over the area subtended by the $4 \sigma$ intensity contour of each emission per channel ${ }^{2}$; the standard deviation of the $\mu$ values within the $4 \sigma$ intensity contour was used as the uncertainty on the mean magnification factor. When the $\geq 3 \sigma$ intensity contours of emissions associated with different multiple images were spatially blended in a channel map, we tried at the best effort to deblend the signal by redistributing the blended flux among images proportionally to their respective fluxes measured above the threshold at which they were unblended. The lensing-corrected $\mathrm{CO}(4-3)$ line-integrated fluxes $\left(F_{\mathrm{CO}(4-3)}\right)$ derived for the different multiple images of the same GMC were reassuring, as they agreed within less than a factor of $2(1-2 \sigma$ flux error). We also extracted for each GMC image the integrated $\mathrm{CO}(4-3)$ line spectrum and performed a Gaussian function fit to the line profile, as illustrated in Fig. A2 for a subset of $\mathrm{CO}(4-3)$ line spectra. For the same GMC image, the corresponding flux was found in agreement, within measurement errors, with $F_{\mathrm{CO}(4-3)}$ derived from

[^2]channel intensity maps. A large flux difference (close to a factor of 3 ) was only obtained for two GMCs with IDs 6 and 7 that we detected at 100 per cent fidelity in one channel map. In what follows, we considered for these two clouds the lower $F_{\mathrm{CO}(4-3)}$ values measured from the channel maps.

Adopting the CO luminosity correction factor $r_{4,1}=$ $L_{\mathrm{CO}(4-3)}^{\prime} / L_{\mathrm{CO}(1-0)}^{\prime}=0.33$, as inferred for the Cosmic Snake galaxy (Dessauges-Zavadsky et al. 2019), and assuming a CO-to- $\mathrm{H}_{2}$ conversion factor ( $\alpha_{\mathrm{CO}}$ ), $M_{\text {molgas }}$ of each multiple image of a given GMC was then calculated following:
$M_{\text {molgas }}=\left(\frac{\alpha_{\mathrm{CO}}}{\mathrm{M}_{\odot}\left(\mathrm{K} \mathrm{km} \mathrm{s}^{-1} \mathrm{pc}^{2}\right)^{-1}}\right)\left(\frac{L_{\mathrm{CO}(4-3)}^{\prime} / 0.33}{\mathrm{~K} \mathrm{~km} \mathrm{~s}^{-1} \mathrm{pc}^{2}}\right) \mathrm{M}_{\odot}$,
where the $\mathrm{CO}(4-3)$ luminosity $\left(L_{\mathrm{CO}(4-3)}^{\prime}\right)$ was derived from $F_{\mathrm{CO}(4-3)}$ measured for that image (Solomon et al. 1997).

The size of each multiple image of a given GMC was determined by first measuring in each channel map the radius of all the $\mathrm{CO}(4-3)$ emissions encompassed by that image. We then adopted the radius of the emission with the highest significance level (i.e. highest $\mathrm{S} / \mathrm{N}$ ) among the $10.343 \mathrm{~km} \mathrm{~s}^{-1}$ channels as the radius of that image, and we used the standard deviation of all measured radii, added in quadrature to the measurement error, as the error on the radius. To derive the radius, we applied the method used for the Cosmic Snake GMCs (Dessauges-Zavadsky et al. 2019). As a first step, we measured the major (a) and minor (b) semi-axes of the elliptical region, which best fits the area subtended by the $4 \sigma$ intensity contour of the emission associated with a given multiple image, and obtained the equivalent circularized radius, $R_{\text {circ }}^{4 \sigma}=\sqrt{a b}$. Considering a 2 D Gaussian distribution of the $\mathrm{CO}(4-3)$ emission, as it is generally assumed, we then derived the circularized radius at the full width halfmaximum (FWHM) as $R_{\text {FWHM }}=R_{\text {circ }}^{4 \sigma} \sqrt{\ln (2) / \ln \left(F_{\text {peak }} / \mathrm{RMS} / 4\right)}$, where $F_{\text {peak }}$ is the peak flux. Finally, to obtain the physical radius $(R)$, we deconvolved $R_{\text {FWHM }}$ from the beam and corrected the deconvolved $R_{\text {FWHM }}$ from the lensing using the same $\mu$ as for the lensingcorrection of the corresponding $F_{\mathrm{CO}(4-3)}$. In the case of emissions, associated with different multiple images, having their $4 \sigma$ contours spatially blended in a channel map, $R_{\text {FWHM }}$ was derived by using the unblended higher $\mathrm{S} / \mathrm{N}$ intensity contours. The resulting $R$ we measured for the different multiple images of the same GMC ended up to globally agree within less than a factor of 2 ( $1-2 \sigma$ radius error).

The velocity dispersion of each multiple image of a given GMC was estimated by measuring in the $\mathrm{CO}(4-3)$ velocity dispersion second-moment map the mean velocity dispersion over the area subtended by the $4 \sigma$ intensity contours of all the $\mathrm{CO}(4-3)$ emissions encompassed by that image. We adopted the largest velocity dispersion measured as the velocity dispersion ( $\sigma_{v}$ ) of the image, and we used the standard deviation of all velocity dispersions, added in quadrature to the measurement error, as the error on $\sigma_{v}$. Here again, we got an agreement between $\sigma_{v}$ derived for the different multiple images of the same GMC within less than a factor of $2(1-2 \sigma$ velocity dispersion error). However, as these $\sigma_{v}$ were relying on the global second-moment map integrated over the whole (12-channels) A521-sys1 CO(4-3) emission, and not over the specific channels of the CO emission of the respective GMCs (which would have generated noisy second-moment maps), we also inferred the GMC $\sigma_{v}$ measurements from the line FWHM obtained from the Gaussian fit of the integrated $\mathrm{CO}(4-3)$ line spectrum extracted for each GMC image (see a subset of those spectra and fits in Fig. A2), and corrected for the final channel spacing (see the ALMA Technical Handbook). We found consistent $\sigma_{v}$, within measurement errors, for the two methods. This consistency suggested that the $\sigma_{v}$ measurements were not too affected by the beam smearing; as further supported by the
fact that the GMCs with IDs $10-14$, located near the galactic centre where the beam smearing effect is expected to be the largest, were not found to be biased towards high $\sigma_{v}$.

The adopted physical properties $-\mu, F_{\mathrm{CO}(4-3)}, M_{\text {molgas }}, R$, and $\sigma_{v}-$ of the 14 GMCs identified in the A521-sys1 galaxy are listed in Table 1; we chose the measurements obtained for the less blended multiple images in channel maps of each GMC. The corresponding $\mathrm{CO}(4-3)$ emission line spectra are shown in Fig. A2. No specific difference is found between the physical properties of the GMCs located near the galactic centre and those located in the spiral arm. The two sets of GMCs encompass the same range of $M_{\text {molgas }}, R$, and $\sigma_{v}$ values.

The 14 GMCs are spatially resolved, as their radii and masses are larger than, respectively, the magnification-dependent equivalent circularized beam resolution limit and the magnification-dependent $4.8 \sigma$ flux detection limit (corresponding to the 100 per cent fidelity), as shown in Fig. 2. Nevertheless, we cannot exclude that some of the identified GMCs are not GMC associations, composed of several GMCs superposed along the line of sight that only observations with better spectral resolution ( $\ll 10 \mathrm{~km} \mathrm{~s}^{-1}$ ) will resolve. Projection effects are indeed likely given the inclination of $72^{\circ}$ of the A521-sys1 galaxy (Patrício et al. 2018). Therefore, we should remember that the inferred GMC masses and radii can still be upper limits.

Altogether the 14 GMCs (corrected for lensing) account for about 11 per cent of the total lensing-corrected $\mathrm{CO}(4-3)$ velocity-integrated flux we measured in the A521-sys1 arc, where the GMCs were searched for and identified; about 55 per cent of the A521-sys1 source galaxy is imaged in the arc. This means there still is a substantial amount of $\mathrm{CO}(4-3)$ molecular gas in the galaxy beside the detected GMCs, which is an unresolved 'background'. This gas can be in a diffuse phase, but we consider it is mostly made of subclouds, which are not resolved due to our limited angular resolution with ALMA. A hierarchical fragmentation over several orders of magnitude and well below $\sim 10 \mathrm{pc}$ is indeed expected, and is believed to result from the hierarchical nature of turbulence (Elmegreen \& Efremov 1997; Padoan \& Nordlund 2002; Hopkins 2013a, b). As a result, the molecular gas follows a quasi-hierarchical structure, containing subclouds, clouds, and subclouds inside clouds. Therefore, in the same way as proceeded by Solomon et al. (1987) for local GMCs where they took all the mass above a certain level of integrated intensity, no background was subtracted when we measured the mass of GMCs in order to take all the mass within the boundary of a GMC including all subclumps.

Finally, we would like to stress that we did not find much smooth emission in our high-resolution ALMA data of A521-sys1. This is not due to the filtered out large-scale $\mathrm{CO}(4-3)$ emission, since the total integrated $A L M A \operatorname{CO}(4-3)$ emission flux ${ }^{3}$ agrees with the fluxes inferred from the $\mathrm{CO}(2-1)$ and $\mathrm{CO}(3-2)$ lines detected with the IRAM 30 m single-dish antenna (Boone, private communication), for a CO spectral-line energy distribution typical of galaxies at $z \sim 1-2$ (Daddi et al. 2015; Dessauges-Zavadsky et al. 2015).

### 4.3 Virial equilibrium and CO -to- $\mathrm{H}_{\mathbf{2}}$ conversion factor

A way to give credit to the identified GMCs in the A521-sys1 galaxy is to determine whether they are gravitationally bound structures in virial equilibrium. Most of the GMCs in local/nearby galaxies, as well as in the Cosmic Snake galaxy at $z \simeq 1$, are indeed virialized

[^3]

Figure 2. The top and bottom panels show, respectively, the lensingcorrected $\mathrm{CO}(4-3)$ luminosities and beam-deconvolved circularized FWHM radii of the A521-sys1 GMCs plotted as a function of their mean lensing magnification factor. The solid line (top panel) defines the magnificationdependent $4.8 \sigma$ flux detection limit, converted to the $\mathrm{CO}(4-3)$ luminosity limit, corresponding to the 100 per cent fidelity (see Section 4.1). The dashed line (bottom panel) defines the magnification-dependent equivalent circularized beam resolution limit. The 14 identified GMCs are spatially resolved with their $L_{\mathrm{CO}(4-3)}^{\prime}$ and $R$ lying above the respective detection limits.
(Heyer et al. 2009; Sun et al. 2018; Dessauges-Zavadsky et al. 2019; Rosolowsky et al. 2021). A way to determine the dynamical state of GMCs is to consider the size-velocity dispersion coefficient ( $C=$ $\left.\sigma_{v}^{2} / R\right)$ that is linearly proportional to the gas mass surface density ( $\Sigma_{\text {molgas }}$ ) for a virialized GMC. In Fig. 3, we show that within a factor of 3,11 out of the 14 A521-sys 1 GMCs are distributed around the one-to-one $C-\Sigma_{\text {molgas }}$ relation, independently of the $\alpha_{\mathrm{CO}}$ considered between the Milky Way value of $4.36 \mathrm{M}_{\odot}\left(\mathrm{K} \mathrm{km} \mathrm{s}^{-1} \mathrm{pc}^{2}\right)^{-1}$ and the starburst value of $1 \mathrm{M}_{\odot}\left(\mathrm{K} \mathrm{km} \mathrm{s}^{-1} \mathrm{pc}^{2}\right)^{-1}$ (Bolatto et al. 2013). The factor of 3 uncertainty in this parameter space corresponds to the


Figure 3. Size-velocity dispersion coefficients plotted as a function of molecular gas mass surface density. The solid line shows the expected one-to-one relation for virialized GMCs, $\Sigma_{\text {molgas }} \approx 330 \sigma_{v}^{2} / R$, with the dashed lines marking the mean spread $(\sim 0.4-0.5$ dex) of GMCs hosted in local quiescent galaxies [grey dots (Bolatto et al. 2008), triangles (Heyer et al. 2009), squares (Donovan Meyer et al. 2013), crosses (Colombo et al. 2014), and stars (Corbelli et al. 2017)], and nearby starbursting/merger galaxies [black filled circles (Wei et al. 2012; Leroy et al. 2015)]. The orange data points correspond to the A521-sys1 GMCs with the dotted lines showing the range of possible $\Sigma_{\text {molgas }}$ determined with two different $\alpha_{\mathrm{CO}}$, the Milky Way and starburst values of 4.36 and $1.0 \mathrm{M}_{\odot}\left(\mathrm{K} \mathrm{km} \mathrm{s}^{-1} \mathrm{pc}^{2}\right)^{-1}$, respectively. Eleven out of the 14 A521-sys1 GMCs (orange filled circles) are virialized, since located within a factor of 3 from the one-to-one $C-\Sigma_{\text {molgas }}$ relation (dashed lines), independently of $\alpha_{\mathrm{CO}}$. For comparison, we also show the 17 GMCs identified in the Cosmic Snake galaxy (magenta data points), among which 14 are found to be virialized [magenta filled circles (DessaugesZavadsky et al. 2019)].
standard deviation of the local GMC distribution ( $\sim 0.4-0.5 \mathrm{dex}$ ) and to measurement errors. Therefore, within this uncertainty, GMCs are usually assumed to be in virial equilibrium, although some of them can be transient structures or collapsing.

For virialized GMCs, their virial mass is expected to be linearly proportional to CO luminosity (Bolatto et al. 2008; Bolatto et al. 2013). Therefore, we can obtain $\alpha_{\mathrm{CO}}$ measurements from the GMC internal kinematics. As done for the Cosmic Snake GMCs (Dessauges-Zavadsky et al. 2019), to compute the virial mass ( $M_{\text {virial }}$ ), we assumed GMCs to be spherical and have their density profile inversely proportional to radius (Solomon et al. 1987; Hughes et al. 2013):
$M_{\text {virial }}=1040\left(\frac{\sigma_{v}}{\mathrm{~km} \mathrm{~s}^{-1}}\right)^{2}\left(\frac{R}{\mathrm{pc}}\right) \mathrm{M}_{\odot}$.
In Fig. 4, we show $M_{\text {virial }}$ as a function of $L_{\mathrm{CO}(1-0)}^{\prime}$ (lensing-corrected) of the 14 A521-sys1 GMCs at $z \simeq 1$. The 11 GMCs, found in virial equilibrium (Fig. 3), are distributed about the mean $\alpha_{\mathrm{CO}}=$ $1.9 \mathrm{M}_{\odot}\left(\mathrm{K} \mathrm{km} \mathrm{s}^{-1} \mathrm{pc}^{2}\right)^{-1}$ with a standard deviation of $0.4 \mathrm{M}_{\odot}$ $\left(\mathrm{K} \mathrm{km} \mathrm{s}^{-1} \mathrm{pc}^{2}\right)^{-1}$. This suggests a lower $\alpha_{\mathrm{CO}}$ than in the Cosmic Snake galaxy, where we determined, also from the GMC internal kinematics, $\alpha_{\mathrm{CO}}=3.8 \pm 1.1 \mathrm{M}_{\odot}\left(\mathrm{K} \mathrm{km} \mathrm{s}^{-1} \mathrm{pc}^{2}\right)^{-1}$ (DessaugesZavadsky et al. 2019). Both galaxies at $z \simeq 1$ yet have a solar metallicity (Patrício et al. 2018) and a comparable SFR of $\sim 26-$


Figure 4. Virial masses of the A521-sys1 GMCs plotted as a function of their lensing-corrected $\mathrm{CO}(1-0)$ luminosity (derived from the measured $\mathrm{CO}(4-3)$ luminosity assuming $r_{4,1}=0.33$ ). The orange filled circles correspond to the 11 GMCs found in virial equilibrium (Fig. 3). They are distributed about the mean CO-to- $\mathrm{H}_{2}$ conversion factor of $\alpha_{\mathrm{CO}}=1.9 \mathrm{M}_{\odot}\left(\mathrm{K} \mathrm{km} \mathrm{s}^{-1} \mathrm{pc}^{2}\right)^{-1}$ (dashed line) with a standard deviation of $0.4 \mathrm{M}_{\odot}\left(\mathrm{K} \mathrm{km} \mathrm{s}^{-1} \mathrm{pc}^{2}\right)^{-1}$ (grey shaded area).
$30 \mathrm{M}_{\odot} \mathrm{yr}^{-1}$ (Nagy et al. 2022), what changes is the median $\Sigma_{\text {molgas }}$ of their respective GMCs. The significantly higher SFR of these $z \simeq 1$ galaxies than of the Milky Way galaxy implies a stronger photodissociating radiation and explains their globally lower $\alpha_{\mathrm{CO}}$ with respect to the Milky Way value. However, in the case of the Cosmic Snake galaxy, the GMC $\Sigma_{\text {molgas }}$ happen to be so high, with a median value of $\sim 2300 \mathrm{M}_{\odot} \mathrm{pc}^{-2}$ (for the above cited $\alpha_{\mathrm{CO}}$ ), that the GMCs are shielded from the ambient radiation. This is less in the case for the A521-sys1 GMCs, which have a median $\Sigma_{\text {molgas }}$ $\sim 800 \mathrm{M}_{\odot} \mathrm{pc}^{-2}$ (for the derived $\alpha_{\mathrm{CO}}$ ), and therefore the CO-to$\mathrm{H}_{2}$ conversion factor in A521-sys1 could have ended up to be lower. However, globally, the factor of two difference in the $\alpha_{\mathrm{CO}}$ values derived for the two galaxies at $z \simeq 1$, both with about solar metallicities, is within the spread of the $\alpha_{\text {CO }}$ measurements obtained for nearby solar metallicity galaxies (e.g. Leroy et al. 2011; Sandstrom et al. 2013).

## 5 DISCUSSION

### 5.1 Larson scaling relations

The GMCs hosted in the A521-sys1 galaxy have high $M_{\text {molgas }}=$ $8.2 \times 10^{5}-7.7 \times 10^{7} \mathrm{M}_{\odot},{ }^{4}$ with a median of $3.0 \times 10^{7} \mathrm{M}_{\odot}$. This is 2 orders of magnitude higher than the median $M_{\text {molgas }}$ of GMCs found in the Milky Way, local dwarf galaxies, and nearby spirals $\left(2.9 \times 10^{5} \mathrm{M}_{\odot}\right.$; Bolatto et al. 2008; Heyer et al. 2009; Donovan Meyer et al. 2013; Colombo et al. 2014; Corbelli et al. 2017). With their $R=28-166 \mathrm{pc}$, they also have a high median $\Sigma_{\text {molgas }}$ (see Section 4.3), almost 10 times higher than local GMCs ( $\Sigma_{\text {molgas }} \sim$

[^4]$100 \mathrm{M}_{\odot} \mathrm{pc}^{-2}$ ). Their $\sigma_{v}=5-25 \mathrm{~km} \mathrm{~s}^{-1}$ are large enough to enable them to be in virial equilibrium.

These measurements, together with the physical properties derived for the Cosmic Snake GMCs, confirm that GMCs hosted in main-sequence galaxies at $z \simeq 1$ differ from GMCs in the local Universe. This is very well assessed when considering the Larson scaling relations, used as the benchmark for the typical local GMC population (Larson et al. 1981; Bolatto et al. 2008). In Fig. 5, we plot, respectively, the first Larson scaling relation $M_{\text {molgas }}-R$ that shows a constant $\Sigma_{\text {molgas }}$ at $\sim 100 \mathrm{M}_{\odot} \mathrm{pc}^{-2}$ for local GMCs (grey data points; top panel), and the second Larson scaling relation $\sigma_{v}-R$ that calibrates $\Sigma_{\text {molgas }}$ of virialized local GMCs (grey data points; bottom panel). The GMCs at $z \simeq 1$ are clearly offset from these two relations. On the other hand, as already suggested in Dessauges-Zavadsky et al. (2019), the high-redshift GMCs very much resemble GMCs hosted in the antennas galaxy merger (Wei et al. 2012) and the NGC 253 nuclear starburst (Leroy et al. 2015), which are also offset from the Larson relations, because immersed in an ISM characterized by an enhanced SFR per unit mass of molecular gas and a strong ambient pressure (see also the GMCs hosted in the starburst galaxy NGC 4826; Rosolowsky \& Blitz 2005; Rosolowsky et al. 2021). It has now been evidenced by a number of studies of GMCs in nearby galaxies that the physical properties of GMCs are indeed dependent on their surrounding local environment (e.g. Hughes et al. 2013; Sun et al. 2018, 2020). The A521-sys1 GMCs further support the strong influence of the ambient ISM, which, at $z \simeq 1$, clearly differs from the ISM of nearby quiescent galaxies as discussed in the next Section 5.2.

### 5.2 Pressure equilibrium

The internal kinetic pressure ( $P_{\text {int }} / k_{\mathrm{B}}$ ) of the A521-sys1 GMCs can be determined following Hughes et al. (2013):
$\frac{P_{\text {int }}}{k_{\mathrm{B}}}=1176\left(\frac{M_{\text {molgas }}}{\mathrm{M}_{\odot}}\right)\left(\frac{R}{\mathrm{pc}}\right)^{-3}\left(\frac{\sigma_{v}}{\mathrm{~km} \mathrm{~s}^{-1}}\right)^{2} \mathrm{~cm}^{-3} \mathrm{~K}$.
As shown in Fig. 6, we found strong $P_{\text {int }} / k_{\mathrm{B}}$ between $10^{5.7}$ and $10^{7.8} \mathrm{~cm}^{-3} \mathrm{~K}$, comparable to the distribution of the values determined for the Cosmic Snake GMCs at their low-pressure end. The $P_{\text {int }} / k_{\mathrm{B}}$ measurements in the $z \simeq 1$ GMCs show a dependence on $\Sigma_{\text {molgas }}$, which very well extends, towards higher $\Sigma_{\text {molgas }}$, the $P_{\text {int }} / k_{\mathrm{B}}-\Sigma_{\text {molgas }}$ correlation reported for typical local GMCs (Hughes et al. 2013; Sun et al. 2018).

In Swinbank et al. (2015) and Dessauges-Zavadsky et al. (2019), it was argued that the strong $P_{\mathrm{int}} / k_{\mathrm{B}}$ of high-redshift GMCs is linked to the strong hydrostatic pressure at the disc mid-plane $\left(P_{\text {ext }} / k_{\mathrm{B}}\right)$ observed in their host galaxies, which was suggested to approximate the pressure at the boundary of molecular clouds (Elmegreen 1989; Blitz \& Rosolowsky 2004). For a two-component disc of gas and stars, $P_{\text {ext }} / k_{\mathrm{B}}$ can be estimated as:
$\frac{P_{\text {ext }}}{k_{\mathrm{B}}} \approx \frac{\pi G}{2} \Sigma_{\text {gas }}\left(\Sigma_{\text {gas }}+\frac{\sigma_{\text {gas }}}{\sigma_{\text {stars }}} \Sigma_{\text {stars }}\right) \mathrm{cm}^{-3} \mathrm{~K}$,
where $G$ is the gravitational constant, and $\Sigma_{\text {gas }}, \Sigma_{\text {stars }}$, and $\sigma_{\text {gas }}$, $\sigma_{\text {stars }}$, respectively, are the neutral (atomic + molecular) gas and stellar mass surface densities and velocity dispersions (Elmegreen 1989; Blitz \& Rosolowsky 2004). Similarly to Dessauges-Zavadsky et al. (2019) and Swinbank et al. (2015), we assumed the neutral gas of high-redshift galaxies to be dominated by the molecular gas, and $\sigma_{\text {gas }} \approx \sigma_{\text {stars }}$. We derived $\Sigma_{\text {gas }}$ and $\Sigma_{\text {stars }}$ from the total molecular gas and stellar masses, respectively, measured in the uniformly lensed image of the A521-sys1 galaxy (see Fig. 1). This gave us $P_{\text {ext }} / k_{\mathrm{B}} \sim$


Figure 5. The top panel shows the first Larson scaling relation with the molecular gas masses plotted as a function of radius for the GMCs hosted in the A521-sys1 galaxy at $z=1.043$ (orange data points), the Cosmic Snake galaxy at $z=1.036$ [magenta data points (Dessauges-Zavadsky et al. 2019)], local quiescent galaxies [grey dots (Bolatto et al. 2008), triangles (Heyer et al. 2009), squares (Donovan Meyer et al. 2013), crosses (Colombo et al. 2014), and stars (Corbelli et al. 2017)], and nearby starbursting/merger galaxies [black filled circles (Wei et al. 2012; Leroy et al. 2015)]. The lines correspond to the median molecular gas mass surface densities of $100 \mathrm{M}_{\odot} \mathrm{pc}^{-2}$ (solid line), $800 \mathrm{M}_{\odot} \mathrm{pc}^{-2}$ (orange dashed line), and $2300 \mathrm{M}_{\odot} \mathrm{pc}^{-2}$ (magenta dotted line) as measured for, respectively, the local GMCs, the A521-sys1 GMCs, and the Cosmic Snake GMCs. The GMCs at $z \simeq 1$ are clearly much denser than typical local GMCs, but have comparable $\Sigma_{\text {molgas }}$ to those of GMCs hosted in nearby starbursting/merger galaxies. The bottom panel shows the second Larson scaling relation with the internal velocity dispersions plotted as a function of radius for the same GMC populations as in the top panel. We plot the $\sigma_{v} \propto R^{0.5}$ relation for the three median $\Sigma_{\text {molgas }}$ values derived in the top panel. The internal velocity dispersions of $z \simeq 1$ GMCs are on average larger than those of typical local GMCs to enable them to remain in virial equilibrium despite their higher $\Sigma_{\text {molgas }}$. The adopted $\alpha_{\mathrm{CO}}$ for the A521-sys1 and Cosmic Snake GMCs are given in Section 4.3.


Figure 6. Internal kinetic pressures plotted as a function of molecular gas mass surface density for the same GMC populations as in Fig. 5. The GMCs at $z \simeq 1$ (orange and magenta data points) extend the $P_{\text {int }} / k_{\mathrm{B}}-\Sigma_{\text {molgas }}$ correlation of typical local GMCs over 3 orders of magnitude in $\Sigma_{\text {molgas }}$. The adopted $\alpha_{\text {CO }}$ are given in Section 4.3.
$10^{7.2} \mathrm{~cm}^{-3} \mathrm{~K}$, namely a factor of $\sim 7$ weaker than in the Cosmic Snake galaxy (Dessauges-Zavadsky et al. 2019), but a factor of $\sim 100-1000$ stronger than the hydrostatic pressure of nearby quiescent galaxies, including the Milky Way disc (Hughes et al. 2013).

The results obtained for the A521-sys1 galaxy, showing a weaker $P_{\text {ext }} / k_{\mathrm{B}}$ (mostly because of the lower molecular gas mass surface density of A521-sys1; Nagy et al. 2022) together with slightly more moderate GMC physical properties (density, turbulence, and internal pressure) than in the Cosmic Snake galaxy (see Figs 5 and 6), bring an additional evidence that GMCs form with properties adjusted to the ambient ISM conditions particular to the host galaxy, and this is not only in local galaxies but also in high-redshift galaxies. In summary, the GMCs of main-sequence galaxies at $z \simeq 1$ show variations in their properties from galaxy to galaxy. Their properties resemble those of local GMCs hosted in starbursting media, where the ambient pressure is comparable to the one observed in the ISM of high-redshift galaxies (Rosolowsky \& Blitz 2005; Hughes et al. 2013; Leroy et al. 2015; Sun et al. 2020). However, they are different from the properties of typical local GMCs, because the strong $P_{\text {ext }} / k_{\mathrm{B}}$ of distant galaxies exceeds the self-gravity of these local GMCs that would be rapidly compressed.

### 5.3 Efficiency of star formation

The Cosmic Snake GMCs at $z \simeq 1$ were found to be highly supersonic, with a median Mach number $(\mathcal{M})$ of $80 \pm 13$ (DessaugesZavadsky et al. 2019), almost 10 times higher than that of typical local GMCs (Leroy et al. 2015). We suggested that such a highly supersonic turbulence may imply a particularly efficient formation of stars in these GMCs, given that star clusters form by gravitational collapse of shock-compressed density fluctuations generated from the supersonic turbulence in GMCs (McKee \& Ostriker 2007; Brunt, Heyer \& Mac Low 2009). And, indeed, we estimated the GMC star formation efficiency $(\epsilon)$ to be as high as $\sim 26-34$ per cent from the


Figure 7. Molecular gas mass distribution of 14 GMCs (orange histogram) versus stellar mass distribution of 11 stellar clumps [grey histogram; Messa et al. (2022)] hosted in the A521-sys1 galaxy and all imaged over the arc within regions where the magnification factor is larger than 4 . The solid vertical lines show the respective medians of $3.0 \times 10^{7} \mathrm{M}_{\odot}$ for the GMCs and $1.2 \times 10^{7} \mathrm{M}_{\odot}$ for the stellar clumps. Their comparison suggests a fairly high efficiency of star formation as discussed in Section 5.3. The adopted $\alpha_{\mathrm{CO}}$ is derived in Section 4.3.
simple comparison of the mass distribution of GMCs and stellar clumps identified in the Cosmic Snake galaxy (Dessauges-Zavadsky et al. 2019). This is sensibly higher than $\epsilon \lesssim 6$ per cent reported in nearby galaxies (Evans et al. 2009; Chevance et al. 2020; Kim et al. 2021), but consistent with the $\epsilon-\Sigma_{\text {molgas }}$ scaling-relation predicted for molecular clouds by numerical simulations (Grudić et al. 2018, 2023).

The A521-sys1 GMCs discussed here and the stellar clumps analysed by Messa et al. (2022) offer a new opportunity to investigate $\epsilon$ in a galaxy at $z \simeq 1$. We derived the GMC Mach number ( $\mathcal{M}$ ) following the prescriptions of Leroy et al. (2015):
$\mathcal{M}=\frac{\sqrt{3} \sigma_{v}}{c_{\mathrm{s}}}$,
where $c_{\mathrm{s}}=0.45 \mathrm{~km} \mathrm{~s}^{-1}$ is the sound speed estimated for molecular hydrogen at $20-50 \mathrm{~K}$. We derived a high median $\mathcal{M}=60 \pm 11$ for the 14 A521-sys 1 GMCs, showing they are highly supersonic, as are the Cosmic Snake GMCs, and may hence potentially experience a high $\epsilon$.

In Fig. 7, we compare the distributions of masses of the 14 GMCs and the 11 stellar clumps (Messa et al. 2022) identified in the A521sys1 galaxy, all imaged over the arc within regions where $\mu>4$. $^{5}$ This comparison can be used to estimate $\epsilon$ in the same way as for local galaxies via $\epsilon=M_{\text {stars }} /\left(M_{\text {molgas }}+M_{\text {stars }}\right)$ (Evans et al. 2009) given that the identified stellar clumps are young, with ages mainly $<100 \mathrm{Myr}$, i.e. likely tracing the recent star formation episodes as do the GMCs (Messa et al. 2022), and the stellar clumps and GMCs were identified at a similar spatial resolution, throughout, respectively, the

[^5]HST near-UV to near-IR images (with the PSF varying from 0.10 to 0.24 arcsec; Messa et al. 2022) and the ALMA images (with the synthesized circularized beam of 0.17 arcsec$)$. It appears that the most massive GMCs are only slightly more massive than the most massive stellar clumps, which suggests a relatively high $\epsilon$. Considering the median values of the molecular gas masses of the GMCs and the stellar masses of the stellar clumps, we get $\epsilon \sim 29$ per cent in this $z \simeq 1$ galaxy, provided that the observed massive stellar clumps (star cluster complexes/associations) were formed within GMCs with comparable physical properties to those we identified.

We also estimated the star formation efficiency per free-fall time $\left(\epsilon_{\mathrm{fff}}\right)$ :
$\epsilon_{\mathrm{ff}}=\frac{\mathrm{SFR}}{M_{\mathrm{molgas}}} t_{\mathrm{ff}}$.
$t_{\mathrm{ff}}$ is the free-fall time defined as $t_{\mathrm{ff}}=\sqrt{3 \pi /(32 G \rho)}$, where $\rho$ is the volume gas density, and $t_{\mathrm{ff}}$ is considered as the characteristic time-scale for the GMC gravitational free-fall collapse inducing the formation of stars (Federrath \& Klessen 2012; Krumholz, Dekel \& McKee 2012). A theoretical value of $\epsilon_{\mathrm{ff}} \sim 1$ per cent is commonly accepted in the literature (especially in numerical simulations), meaning that each free-fall time a galaxy typically converts about 1 per cent of its dense gas into stars (e.g. Krumholz \& Tan 2007; McKee \& Ostriker 2007; Krumholz et al. 2012). This value is globally supported by observations, although important $\epsilon_{\mathrm{ff}}$ deviations exist among different environments of nearby galaxies (e.g. Leroy et al. 2017; Ochsendorf et al. 2017; Utomo et al. 2018; Schruba, Kruijssen \& Leroy 2019; Kim et al. 2021).

Under the simple assumption that the detected high-redshift A521sys1 GMCs are spherical (see also Section 4.3), their $t_{\mathrm{ff}}$ range between 1 and 6 Myr , with a median value of $\sim 3 \mathrm{Myr}$, comparable to the free-fall times measured for GMCs in nearby galaxies (see references above). We carried out the estimation of $\epsilon_{\mathrm{ff}}$ in the A521-sys1 galaxy for three cases: (1) considering the total $\mathrm{SFR}=26 \pm 5 \mathrm{M}_{\odot} \mathrm{yr}^{-1}$ and the total $M_{\text {molgas }}=(1.2 \pm 0.2) \times 10^{10} \mathrm{M}_{\odot}{ }^{6}$ integrated over the entire galaxy; (2) considering the radial $\Sigma_{\text {SFR }} / \Sigma_{\text {molgas }}$ measurements from Nagy et al. (2022), inferred in concentric elliptical rings centred on the galaxy center; and (3) considering the total galactic SFR, but the $M_{\text {molgas }}$ contribution from the 14 GMCs only that means considering only the compact/dense CO gas that drives most of the star formation of the galaxy. For case (1), we found a low $\epsilon_{\mathrm{ff}} \sim 0.8$ per cent, and for case (2), $\epsilon_{\mathrm{ff}}$ ranged between 0.9 and 4.3 per cent. For case (3), we obtained a much higher $\epsilon_{\mathrm{ff}} \sim 11$ per cent, which is more in line with the $\epsilon$ estimation above. While the $\epsilon_{\mathrm{ff}}$ derived for cases (1) and (2) are in line with most of the measurements reported for nearby galaxies (Utomo et al. 2018, and references above), $\epsilon_{\mathrm{ff}}$ for case (3) stands out of the range. The difference between cases (1) $+(2)$ and case (3) comes from the fact that the compact/dense molecular gas found in GMCs represents a small fraction of about 11 per cent in mass of the total molecular gas that is observed in the A521-sys1 galaxy (Section 4.2). In the definition of $\epsilon_{\mathrm{ff}}$ [equation (7)], the molecular gas mass precisely refers to the dense gas mass that is available for the star formation (Kim et al. 2021). Therefore, we believe that our estimate of $\epsilon_{\mathrm{ff}} \sim 11$ per cent for case (3) is most likely characterizing
${ }^{6}$ Derived from the $\mathrm{CO}(4-3)$ line emission and calculated by adopting $r_{4,1}=$ 0.33 and $\alpha_{\mathrm{CO}}=1.9 \pm 0.4 \mathrm{M}_{\odot}\left(\mathrm{K} \mathrm{km} \mathrm{s}^{-1} \mathrm{pc}^{2}\right)^{-1}$ determined in Section 4.3. As mentioned in Section 4.2, the $\mathrm{CO}(2-1)$ and $\mathrm{CO}(3-2)$ emission lines, detected with the IRAM 30 m single-dish antenna, give comparable total molecular gas mass estimates (Boone, private communication).
the more efficient star-formation process taking place in the $z \sim 1$ A521-sys1 galaxy compared to nearby galaxies.

## 6 CONCLUSIONS

We present the analysis of the $\mathrm{CO}(4-3)$ molecular gas emission of the A521-sys 1 main-sequence star-forming galaxy at $z=1.043$. In the $H S T$ rest-frame UV to optical images, the galaxy is clumpy, showing several UV-bright clumps (Messa et al. 2022), and has a nice spiral structure, also traced by the $\mathrm{CO}(4-3)$ emission (see Fig. 1) that even exhibits a surface over-density of molecular gas mass in the galaxy radial profile at the location of the spiral arms (Nagy et al. 2022). The kinematics of both ionized ([O II] emission) and molecular (CO(4-3) emission) gas reveals a rotating disc, with an inclination-corrected rotation velocity of $v_{\text {rot }}=130 \pm 5 \mathrm{~km} \mathrm{~s}^{-1}$ (Patrício et al. 2018; Girard et al. 2019). The respective velocity dispersions significantly differ between $\sigma_{0}=54 \pm 11 \mathrm{~km} \mathrm{~s}^{-1}$ for the ionized gas and $11 \pm 8 \mathrm{~km} \mathrm{~s}^{-1}$ for the molecular gas (Girard et al. 2019). We can determine the Toomre stability parameter (Toomre 1964) for a constant rotation velocity as follows:
$Q_{\text {gas }}=\sqrt{2} \frac{\sigma_{0}}{v_{\text {rot }} f_{\text {gas }}}$,
where $f_{\text {gas }}$ is the molecular gas mass to total (including gas, stars, and dark matter) mass fraction (Escala \& Larson 2008; Genzel et al. 2011). With $M_{\text {stars }}=(7.4 \pm 1.2) \times 10^{10} \mathrm{M}_{\odot}$ and $M_{\text {molgas }}=$ $(1.2 \pm 0.2) \times 10^{10} \mathrm{M}_{\odot}$, the A521-sys1 galaxy has $f_{\text {gas }}$ smaller than 14 per cent as one also needs to account for the dark matter mass. The dynamical mass estimate, obtained under the disc-like potential hypothesis, does not show evidence for a large amount of dark matter ( $\$ 5$ per cent). Moreover, given that $\sigma_{0}$ has not to be isotropic, $Q_{\text {gas }}$ is likely close to 1 for the molecular gas disc, as expected since once disc fragmentation occurred, $Q_{\text {gas }}$ should become $\geq 1$ to regulate the system. Numerical simulations indeed show that the UV-bright stellar clumps, ubiquitously observed in galaxies at cosmic noon (e.g. Guo et al. 2015; Dessauges-Zavadsky et al. 2017; Cava et al. 2018; Zanella et al. 2019), form in gas clouds produced from the fragmentation process of high-redshift gas-rich, turbulent discs (e.g. Dekel et al. 2009; Tamburello et al. 2015; Mandelker et al. 2017; Renaud, Romeo \& Agertz 2021). Feedback and molecular gas fraction play a key role here, since to undergo the phase of violent disc instability the feedback is not to be too strong (Mayer et al. 2016) and $f_{\text {gas }}$ has to be at least $40-50$ per cent for fragmentation to happen and the formation of long-lived clouds (Tamburello et al. 2015; Fensch \& Bournaud 2021).

By combining the ALMA high angular resolution imaging capability with gravitational lensing, our study of the A521-sys1 strongly lensed galaxy led to the second observational discovery of GMCs in a proto-Milky Way galaxy at $z \simeq 1$, after the Cosmic Snake galaxy (Dessauges-Zavadsky et al. 2019). Fourteen GMCs were identified, with 11 found to be gravitationally bound structures in virial equilibrium. They provide additional clues that GMCs hosted in typical high-redshift main-sequence galaxies are different from local GMCs. They have, on average, 100 times higher $M_{\text {molgas }}$, 10 times higher $\Sigma_{\text {molgas }}$, almost 100 times stronger internal kinetic pressures, and 10 times enhanced supersonic turbulence, resulting in being located above the Larson scaling relations for local GMCs (Larson et al. 1981; Bolatto et al. 2008). Only GMCs hosted in nearby starbursting and merger galaxies (e.g. Wei et al. 2012; Leroy et al. 2015; Rosolowsky et al. 2021), sometimes considered as the high-redshift galaxy analogues, show comparable physical properties. These findings support that, now and at other look-back
times, GMCs form with properties that adjust to the ambient ISM conditions (pressure, turbulence, density, etc.) prevalent in the host galaxy.

This picture is further validated by the variations in the physical properties we observe among local GMCs (Hughes et al. 2013; Sun et al. 2018, 2020), as well as among high-redshift GMCs hosted in different galaxies. Indeed, we may see that the seven times weaker hydrostatic pressure that we estimated at the disc mid-plane of the A521-sys1 galaxy, in comparison to the one of the Cosmic Snake galaxy, seems to impact in cascade all the properties of the A521sys1 GMCs with respect to those of the Cosmic Snake GMCs: it first implies a weaker GMC internal kinetic pressure, which yields, on the one hand, (i) a lower gas mass surface density (Fig. 6), and, on the other hand, (ii) a less extreme supersonic turbulence given the lower internal velocity dispersion [equation (6)]. Because of (i), GMCs result in being less shielded from the ambient photodissociating radiation, and therefore we measured a smaller CO-to- $\mathrm{H}_{2}$ conversion factor from the virialized clouds (Section 5.2), and because of (ii), GMCs are found to be slightly less efficient in forming stars (Section 5.3).

In summary, the GMCs, detected in the A521-sys1 galaxy and the Cosmic Snake galaxy, have masses high enough to support the in situ formation of the massive stellar clumps (star cluster complexes/associations) we see in comparable numbers in the HST restframe UV to optical images of these two $z \simeq 1$ galaxies (Cava et al. 2018; Messa et al. 2022), as well as in up to $\sim 60$ per cent of galaxies at $z \sim 1-2$ (Guo et al. 2015). Their similar molecular gas and stellar mass distributions suggest a relatively high star-formation efficiency of $\sim 30$ per cent in these $z \simeq 1$ GMCs. We estimated the star formation efficiency per free-fall time to be $\sim 11$ per cent in the A521-sys1 galaxy. To confirm the possible trend of an enhanced star formation efficiency in GMCs of high-redshift galaxies, high-resolution $\mathrm{H} \alpha$ observations, tracing the very recent ( $\lesssim 10 \mathrm{Myr}$ ) star formation are needed, as motivated by the studies of GMC star formation timescales and efficiencies led in nearby galaxies (e.g. Kruijssen et al. 2019; Chevance et al. 2020), based on the statistical framework developed by Kruijssen \& Longmore (2014) and Kruijssen et al. (2018), built on the spatial correlation/decorrelation of GMCs and young stars on small scales. Planned JWST Cycle $1 \mathrm{H} \alpha$ integral-field NIRSpec observations of the Cosmic Snake galaxy will help to shed light on this important physical parameter so far usually fixed to $\epsilon_{\mathrm{ff}} \sim 1$ per cent as measured in nearby galaxies (Krumholz et al. 2012).

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## DATA AVAILABILITY

The data underlying this article will be shared on reasonable request to the corresponding author.

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## APPENDIX A: MOLECULAR CLOUD IDENTIFICATION IN CHANNEL MAPS

In Section 4.1, we describe how we performed the search for the GMCs in the ALMA 12-channel intensity maps extracted over the $\mathrm{CO}(4-3)$ line emission. In total, 24 counter-images of 14 GMCs were identified, with most GMCs having two to three multiple images. Their respective $\mathrm{CO}(4-3)$ emission encompasses between one and five adjacent $10.3782 \mathrm{~km} \mathrm{~s}^{-1}$ channels, as shown in Fig. A1. Similarly to the definition applied for the GMCs hosted in the Cosmic Snake galaxy (Dessauges-Zavadsky et al. 2019), the detected $4 \sigma$ $\mathrm{CO}(4-3)$ emission peaks per channel were considered as belonging to images of distinct clouds when their $4 \sigma$ contours were not spatially overlapping in the same channel map, or when their $4 \sigma$ contours were co-spatial, but not in adjacent channel maps (that is, when separated by at least one channel). This definition of clouds, although at first sight appearing as arbitrary, is a possible way of defining clouds. We consider that the essential point is to describe our method clearly to ensure that our results are reproducible, but, of course, a different cloud definition can be adopted using the same ALMA data. Globally, we acknowledge that our definition of clouds depends on, and is limited by, our spatial resolution and our beam size. We labelled the identified multiple images with ' N ', ' S ', and ' C ' letters; they denote the respective emission peaks found in the northern $(\mathrm{N})$ mirrored image and the southern (S) mirrored image of the arc, and the central (C) north (CS) and south (CS) images around the closed critical line in the northern part of the arc. The numbers enumerate the 14 distinct GMCs.

In Fig. A2, we show the individual integrated $\mathrm{CO}(4-3)$ emission line spectra extracted for the 14 GMCs. We plot the spectra obtained for the less blended multiple images in channel maps of each GMC, and that was adopted to estimate the GMC physical properties listed in Table 1.


Figure A1. In each row, the left-hand panel shows the velocity first-moment map, with the magenta/violet colours corresponding to $-70 \mathrm{~km} \mathrm{~s}^{-1}$ and the red colours to $+90 \mathrm{~km} \mathrm{~s}^{-1}$. The critical line of our lens model at the redshift of the A521-sys1 galaxy, $z=1.043$, is represented by the red solid line. The middle and right-hand panels show the channel intensity maps of the $\mathrm{CO}(4-3)$ line emission at the native spectral resolution of $10.3782 \mathrm{~km} \mathrm{~s}{ }^{-1}$. The overlaid gold contours start at $\pm 3 \sigma$, in steps of $1 \sigma\left(\mathrm{RMS}=0.0027 \mathrm{Jy} \mathrm{beam}^{-1} \mathrm{~km} \mathrm{~s}^{-1}\right)$; dashed gold contours for negative values. The ellipses, colour-coded, following the velocity map at their location, are the best fits of the extracted $4 \sigma$ intensity contours [sometimes the $3 \sigma$ intensity contours (for labels in parenthesis) if clearly identified, or higher intensity contours, if the $4 \sigma$ intensity contours are blended] of the 24 counter-images of the 14 GMCs. The $3 \sigma$ intensity contours, with equivalent circularized radii bigger than the equivalent circularized radius of the beam, are marked with capital letters (if smaller they are marked with small letters). The $A L M A$ synthesized beam with a size of $0.19 \times 0.16 \operatorname{arcsec}^{2}$ at the position angle of $-74^{\circ}$ is shown by the gold filled ellipse. We give a reference scale of 1 arcsec.


Figure A1 - continued


Figure A2. ALMA integrated $\mathrm{CO}(4-3)$ emission line spectra (plotted at the spectral resolution of $10.3782 \mathrm{~km} \mathrm{~s}^{-1}$ ) of the 14 GMCs detected in the A521-sys1 galaxy, extracted from the less blended multiple images in channel maps (Fig. A1) of each GMC. The cyan shaded regions represent channels over which the $\mathrm{CO}(4-3)$ emission is detected above the RMS noise of $0.2 \mathrm{mJy} \mathrm{beam}^{-1}$ (orange dashed line). The best Gaussian fits of the $\mathrm{CO}(4-3)$ line profiles are shown by the red solid lines. The zero velocity is fixed at $z=1.043425$.


Figure B1. ALMA visibility simulations of a lensed smooth exponential disc with the Sérsic index of 1, characterized by the total CO(4-3) line-integrated flux multiplied by 20, the effective radius, and the rotation velocity measured for the A521-sys1 galaxy. The left-hand panel shows an example of the channel intensity map of $10.3782 \mathrm{~km} \mathrm{~s}^{-1}$ of the central bright region of the smooth disc model located close to the critical line. The other panels show the corresponding CASA simulated intensity maps in three consecutive channels with the RMS noise comparable to the real ALMA observations of A521-sys1. Only with the flux boost by a factor of 20 , the $\operatorname{CO}(4-3)$ emission of the smooth disc model is detected at $4-6 \sigma$ above the RMS noise in the simulated channel maps and appears structured in clumpy features as shown by the overlaid gold contours starting at $\pm 3 \sigma$, in steps of $1 \sigma$ (RMS $=0.003 \mathrm{Jy} \mathrm{beam}^{-1} \mathrm{~km} \mathrm{~s}^{-1}$ ); dashed gold contours for negative values. The clumpy features mimic the GMCs we identified in channel maps (see Fig. A1), but remain fundamentally different because they are found at random locations from channel to channel and they change for different noise realizations. The critical line of our lens model at the redshift of the A521-sys1 galaxy, $z=1.043$, is shown by the red solid line. The $0.18 \times 0.15 \operatorname{arcsec}^{2}$ synthesized beam of the simulated data at the position angle of $-89^{\circ}$ is represented by the white filled ellipse. We give a reference scale of 1 arcsec.

## APPENDIX B: CASA VISIBILITY SIMULATIONS

To validate the existence of the detected GMCs (see Section 4.1) against artificial clumpy features produced by lensing and interferometric effects out of a smooth exponential disc of $\mathrm{CO}(4-3)$ emission, we followed the methodology of Hodge et al. $(2016,2019)$, Gullberg et al. (2018), and Ivison et al. (2020) who evidenced the presence of artificial clumpy features in lensed interferometric data. We performed CASA visibility simulations with the CASA simobserve routine by setting up the frequency, the bandwidth, the ALMA configuration, the precipitable water vapour, and the exposure time to the real ALMA observations of A521-sys1. For the $\mathrm{CO}(4-3)$ line imaging, we used the CASA simanalyze routine, and we applied the same pixel size and weighting scheme as for real visibilities using Briggs and the robust factor of 0.5 . The generated RMS noise per beam in the simulated channel intensity maps is comparable within about 10 per cent to the RMS noise measured in the real channel intensity maps for the same synthesized beam size. We considered two input sky models.

In the first sky model, we distributed the total lensing-corrected $\mathrm{CO}(4-3)$ line-integrated flux of $1.5 \pm 0.2 \mathrm{Jy} \mathrm{km} \mathrm{s}{ }^{-1}$ measured in the A521-sys1 galaxy in a smooth exponential disc with the Sérsic index of 1 in the source plane, characterized by the rotation velocity and the effective radius determined for the A521-sys1 galaxy (Girard et al. 2019; Nagy et al. 2022). This smooth exponential disc was then lensed with the tailored lens model using Lenstool (see Section 2) to obtain the corresponding $\mathrm{CO}(4-3)$ emission data cube in the image plane, for which we adopted a channel sampling of $10.3782 \mathrm{~km} \mathrm{~s}^{-1}$
as in the real data cube. The simulated channel intensity maps showed no $\mathrm{CO}(4-3)$ emission detection of the smooth disc model. Only after increasing the measured total $\mathrm{CO}(4-3)$ line-integrated flux by a factor of 20 , the $\mathrm{CO}(4-3)$ emission of the smooth disc model was detected at $4-6 \sigma$ above the RMS noise in the simulated channel maps; albeit only in the central bright regions of the disc located close to the critical line. The detected $\mathrm{CO}(4-3)$ emission is indeed structured in clumpy features as shown in Fig. B1 for three consecutive channels encompassing the central bright region of the smooth disc. However, we noticed that these clumpy features change for different noise realizations in our CASA visibility simulations; as a result, the corresponding CO emission peaks, which mimic the GMC search undertaken per channel map, have random locations, and are thus never detected over two and more adjacent channels at the same location and do not show multiple images as predicted by the lens model, while the GMCs identified in the real channel maps do (see Section 4.1 and Fig. A1). Moreover, and most importantly, it is difficult to explain how we could have missed 20 times of the $\mathrm{CO}(4-3)$ line-integrated flux of A521-sys1, and even more that, in addition to the ALMA observations, we have IRAM 30 m singledish observations that do not suffer of large-scale $\mathrm{CO}(4-3)$ emission filtering.

In the second sky model, we created a data cube with also a $10.3782 \mathrm{~km} \mathrm{~s}^{-1}$ sampling, and we placed in the channel intensity maps $\mathrm{CO}(4-3)$ clumps at the locations of the GMGs identified in the A521-sys1 galaxy and with their measured properties (fluxes and $a$, $b$ elliptical sizes) in the image plane. The modelled $\mathrm{CO}(4-3)$ clumps are detected at $>4-6 \sigma$ above the RMS noise in the simulated channel intensity maps, namely at similar significance levels as the GMCs


Figure B2. ALMA visibility simulations of $\mathrm{CO}(4-3)$ clumps placed in the channel intensity maps of $10.3782 \mathrm{~km} \mathrm{~s}^{-1}$ at the locations of the GMGs identified in the A521-sys1 galaxy and with their measured properties (fluxes and $a, b$ elliptical sizes). We show the corresponding sky model on the left, and the cASA simulated intensity maps with the RMS noise comparable to the real ALMA observations on the right for three consecutive channels encompassing the central region of the A521-sys1 galaxy. The modelled $\mathrm{CO}(4-3)$ clumps are detected at $>4-6 \sigma$ above the RMS noise in the simulated channel maps, namely at similar significance levels as the GMCs detected in the real channel maps (see Fig. A1). For different noise realizations, the clumps remain detected in the simulated channel maps at comparable significance levels. The overlaid gold contours start at $\pm 3 \sigma$, in steps of $1 \sigma$ (RMS $=0.003 \mathrm{Jy} \mathrm{beam}^{-1} \mathrm{~km} \mathrm{~s}^{-1}$ ); dashed gold contours for negative values. The critical line of our lens model at the redshift of the A521-sys1 galaxy, $z=1.043$, is shown by the red solid line. The $0.18 \times$ $0.15 \operatorname{arcsec}^{2}$ synthesized beam of the simulated data at the position angle of $-89^{\circ}$ is represented by the white filled ellipse. We give a reference scale of 1 arcsec.
detected in the real channel intensity maps as shown in Fig. B2. For different noise realizations in our CASA visibility simulations, the clumps remained detected in the simulated channel maps at comparable significance levels.

These two sets of CASA visibility simulations demonstrate that clumps that benefit from a high $\mathrm{CO}(4-3)$ surface brightness can be detected in channel intensity maps. This is not the case if the
measured total $\mathrm{CO}(4-3)$ line-integrated flux is distributed in a smooth exponential disc that globally suffers from a much lower surface brightness than clumps.

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[^1]:    ${ }^{1}$ We considered two $\mathrm{CO}(4-3)$ emissions as co-spatial in two adjacent channel maps when their respective $4 \sigma$ contours were overlapping over at least three pixels of 0.03 arcsec.

[^2]:    ${ }^{2}$ Given the small sizes of the $4 \sigma$ intensity contours of the $\mathrm{CO}(4-3)$ emissions per channel, barely more extended in surface than the synthesized beam (at most by a factor of 1.7; see Table 1 and Fig. A1), the effect of differential magnification is negligible and is eventually accounted in the uncertainty on $\mu$.

[^3]:    ${ }^{3}$ We integrated the ALMA $\operatorname{CO}(4-3)$ emission over all A521-sys1 multiple images, since they were all covered by the large IRAM 30 m beam.

[^4]:    ${ }^{4}$ Obtained by adopting $\alpha_{\mathrm{CO}}=1.9 \pm 0.4 \mathrm{M}_{\odot}\left(\mathrm{K} \mathrm{km} \mathrm{s}^{-1} \mathrm{pc}^{2}\right)^{-1}$ derived in Section 4.3.

[^5]:    ${ }^{5}$ We focused only on stellar clumps imaged over the arc and that benefit from high $\mu>4$ (Messa et al. 2022).

