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1 **Rapid detection of co-seismic ionospheric disturbances**
2 **associated with the 2015 Illapel, the 2014 Iquique and**
3 **the 2011 Sanriku-Oki earthquakes**

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7 **Key Points:**

- 8 • A new methodology to rapidly estimate the time and the altitude of detection of
9 co-seismic ionospheric disturbances (CID),
10 • The methodology uses data from near-epicenter seismic stations to calculate the
11 seismic peak time as an alternative to the earthquake onset,
12 • First report on detection of CID as soon as 400 seconds after the earthquake on-
13 set and 250-430 seconds after the seismic peak time,

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Abstract

Co-seismic Ionospheric disturbances (CID, or "ionoquakes") are disturbances in the electron density or total electron content (TEC) of the ionosphere, produced by the ground motion due to earthquakes. Usually, ionoquakes are detected in the near-epicentral region within 8-10 minutes after an earthquake onset time. In this work, we present a new methodology that allows to estimate the CID arrival time based on determining the CID peak time in TEC measurements with respect to the peak time of seismic waves registered by the nearest seismic station. Our methodology also allows to understand the altitude of GNSS detection that otherwise remains ambiguous. We apply the newly developed techniques to detect CID signatures associated with three large earthquakes: the 2015 Illapel, the 2014 Iquique, and the 2011 Sanriku-Oki. We show that for these events, the CID arrive 250-430 seconds after the time of the seismic wave peak, or 350-700 s after the earthquake onset time. Our analysis show that the first CID are detected at the altitudes of 150-180 km (the Sanriku earthquake) and of 200-300 km (the Illapel and the Iquique earthquakes). The disturbances represent high-frequency acoustic oscillations that propagate with a horizontal speed faster than 0.75 km/s.

1 Introduction

It is known that large earthquakes can generate acoustic and gravity waves that further produce disturbances in the ionosphere (Calais & Minster, 1995; Heki & Ping, 2005; Liu et al., 2006; Lognonné, 2009; Astafyeva et al., 2009; Chum et al., 2012; Occhipinti et al., 2013; Afraimovich, E. L. et al., 2013; Cahyadi & Heki, 2015; Thomas et al., 2018; Astafyeva & Shults, 2019; Sanchez et al., 2022; Bravo et al., 2022). Such disturbances are referred to as Coseismic Ionospheric Disturbances (CIDs) or ionoquakes. They usually propagate at horizontal speeds between 600 m/s and 3 km/s (Astafyeva et al., 2009; Rolland et al., 2011; Astafyeva et al., 2014), and their oscillation frequency lies in the range 1-10 mHz (Bagiya et al., 2019; Manta et al., 2020; Sanchez et al., 2022).

The CIDs propagating at the acoustic wave speed (i.e., 600-1000 m/s) are usually detected in the near-epicentral area only 8-10 min after an earthquake (Heki & Ping, 2005; Kherani et al., 2012; Cahyadi & Heki, 2015; Thomas et al., 2018; Astafyeva & Shults, 2019). Such a short timing opens a possibility of use CIDs to enhance the capability of early tsunami warning by using ionospheric data Occhipinti (2015); Astafyeva (2019, 2020).

In recent years, a few studies have reported early and rapid detection of CIDs, i.e. less than the "nominal" 480-600 seconds after an earthquake. For instance, the first CIDs due to the 2011 Tohoku-oki earthquake were detected as early as 420-464 seconds after the earthquake onset time Astafyeva et al. (2011, 2013); Bagiya et al. (2020); Chum et al. (2016). Early CID arrivals (440-480 sec) have also been reported for the Mw7.4 March 9, 2011 Sanriku-oki earthquake in Japan Thomas et al. (2018); Astafyeva and Shults (2019). The phenomenon of early CID arrivals is not well understood yet. In the case of the Tohoku-oki earthquake, they were explained by the generation of large shock-waves Astafyeva et al. (2011), and/or by low LOS elevation angles Astafyeva et al. (2013).

In this work, we present a new methodology allowing to 1) rapidly detect CID in total electron content (TEC) data times series and to estimate the CID arrival time; 2) estimate the altitude of ionospheric detection. We further apply this technique to analyze co-seismic ionospheric signatures due to the Mw8.3 Illapel earthquake of September 16, 2015, the Mw8.2 Iquique earthquake of April 01, 2014, and the Mw7.3 Sanriku-oki earthquake of March 09, 2011.

2 Earthquake events and Seismic and TEC Data

The Illapel and Iquique earthquakes of Mw8.3 and 8.2 respectively were triggered near the Chile subduction zone, in South America. Seismicity in the Chilean region is defined by the subduction of the oceanic Nazca plate under the South American plate. This subduction zone is well known for harboring large EQs (Carrasco et al., 2019). The Illapel earthquake occurred on September 16, 2015, at 22:54:32 UT. According to the U.S. Geological Survey (USGS), this earthquake was generated by thrust faulting, with the epicenter located at latitude = 31.57°S and longitude = 71.67°W, at a depth of 22.4 km (<https://earthquake.usgs.gov/earthquakes/eventpage/us20003k7a/technical>). The Iquique earthquake occurred on April 01, 2014, at 23:46:47 UT as a result of thrust faulting, with the epicenter located at latitude = 19.61°S and longitude = 70.77°W, at a depth of 25.5 km, (<https://earthquake.usgs.gov/earthquakes/eventpage/us20003k7a/technical>). The Sanriku-Oki earthquake of Mw7.4, occurred on March 9, 2011 at 02:45:20 UT at a depth of 32 km, with an epicenter at 38.435°N, 142.842°E (<https://earthquake.usgs.gov/earthquakes/eventpage/usp000hvhj/executive>).

Figure 1 illustrates the epicentral location and the shake map of the peak ground velocity for the Illapel, Iquique, and Sanriku-Oki earthquakes (source: <https://earthquake.usgs.gov/earthquakes>). The present study employs the seismic data derived from seismometers and TEC data derived from GNSS receivers. Figure 1 also illustrates the locations of seismic stations and GNSS receivers for the three earthquake events.

2.1 vTEC estimation from GNSS receivers

For Illapel and Iquique earthquakes, we examine the TEC data with 15 seconds sampling rate, retrieved from GNSS receivers of the permanent ground-based network UNAVCO (<http://www.unavco.org>) and CSN (<http://gps.csn.uchile.cl/>). For the analysis of the Sanriku-Oki earthquake, the original TEC data is with a 1-second sampling rate, retrieved from the GNSS Earth Observation Network System (GEONET). However, we lower the sampling rate from 1 second to 15 seconds in order to have identical data cadences for all events.

During the earthquakes, multiple GNSS satellites were visible by ground-based GNSS receivers. However, here we focus on PRNs = 12 and 24 for the Illapel earthquake, PRNs = 01, 20, and 23 for the Iquique earthquake, and PRN = 07 for the Sanriku-Oki earthquake. We have selected these PRNs since their projected locations at the ionospheric heights i.e., the Sub-Ionospheric Points (SIP) are within ~450 km of the epicentral distance, and the elevation angle is more than 42°, except for the Sanriku-Oki earthquake, where the elevation angle was ~30°.

The slant TEC (sTEC) and vertical TEC (vTEC) are estimated by using the phase and code measurements from ground-based GNSS-receivers (Hofmann-Wellenhof et al., 2008), based on Equation 1,

$$sTEC = \frac{1}{40.308} \frac{f_1^2 f_2^2}{f_1^2 - f_2^2} (L_1 \lambda_1 - L_2 \lambda_2 + const + nL), \quad (1)$$

where $f_1=1575.42$ MHz and $f_2=1227.60$ MHz are the carrier-wave frequencies, $\lambda_1 = c/f_1$ and $\lambda_2 = c/f_2$ are the corresponding wavelengths in meters, c is the speed of light, L_1 and L_2 are the carrier phases, $const$ is the unknown initial phase ambiguity, and nL is the error in determining the phase path. The TEC is measured in TECU units (TECU) with 1 TECU = $10^{16} el/m^2$. The exactitude of TEC estimation from phase measurements is about 0.01–0.02 TECU (Coster et al., 2013).

The vTEC is derived from sTEC using the following conversion Equation 2, (Klobuchar, 1987).

$$vTEC = sTEC \cdot \cos \left[\arcsin \left(\frac{r_e}{r_e + H_{\text{ION}}} \cos \theta \right) \right], \quad (2)$$

106 where r_e is the Earth's radius, H_{ION} is the altitude of the ionospheric thin layer
107 and θ is the satellite elevation angle.

108 2.2 V_{SISM} estimation from seismometers

109 To obtain the vertical velocity (V_{SISM}) associated with the ground vibration from
110 the seismometers, we employ the Python library: `obspyDMT`. `ObspyDMT` is an open-
111 source toolbox for querying, retrieving, processing, and managing seismological data sets
112 (Hosseini & Sigloch, 2017). The library downloads the data in count format, estimates
113 the ground vibration, and minimizes the instrumental response contributions associated
114 with the frequency response, amplifier, analog and digital filters, and digitization. We
115 used a bandpass filter on the seismograms before deconvolution, with a tuple defining
116 the four corner frequencies (0.02, 0.12, 10, 20) (Hosseini & Sigloch, 2017).

117 In the present study, V_{SISM} corresponds to the seismic station CO03 for the Illapel
118 earthquake, PSGCX for the Iquique earthquake, and KSN for the Sanriku-Oki earthquake
119 (Figure 1). To match the TEC sampling rate and to achieve identical spectral conditions
120 between the two datasets, we reduce the seismic data sampling rate from 0.05 seconds
121 to 15 seconds. The IRIS network (http://ds.iris.edu/wilber3/find_event) and Na-
122 tional Research Institute for Earth Science and Disaster Resilience (NIED)-F-net ([https://](https://www.fnet.bosai.go.jp/)
123 www.fnet.bosai.go.jp/) administer the seismic data.

124 3 Methodology

125 In contrast to previous studies that rely on the onset time of an earthquake, here
126 we suggest to use the seismic peak time of the V_{SISM} for the estimation of the ionoquake
127 detection time ($t_{\text{detection}}$). The seismic peak time represents the time of the maximum
128 seismic oscillations rather than the beginning time of the oscillations. We note, however,
129 that the identification of the oscillation peak in the time series is comparatively unam-
130 biguous. The analysis subjects the V_{SISM} and TEC data to the spectral analysis pro-
131 cedure with identical spectral conditions, namely, the equal data length of 2 hours and
132 a sampling rate of 15 seconds. Then, we examine the spectrogram in a frequency range
133 of 0.13 mHz-33 mHz, and, for each frequency, we search for new oscillations in TEC start-
134 ing from the corresponding peak onset time of V_{SISM} and in the vicinity of the epicen-
135 ter.

136 We test two independent criteria to identify the peak time. In TEST-1, the peak
137 time corresponds to the time of the first peak in the V_{SISM} and TEC oscillation. In TEST-
138 2, the peak time corresponds to the time of the maximum in the V_{SISM} and TEC oscil-
139 lations, i.e., corresponds to the time of the maximum amplitude. The peaks and the max-
140 ima are estimated by using the Python module "find-peaks". If the peak time of V_{SISM}
141 and ionoquake are t_{SISM} and t_{TEC} respectively, then the ionoquake detection time can
142 be defined as follows:

$$t_{\text{detection}} = t_{\text{TEC}} - t_{\text{SISM}} \quad (3)$$

143 Since both t_{SISM} and t_{TEC} suffer identical time shift from spectral analysis, the iono-
144 quake detection time $t_{\text{detection}}$ remains unaffected by the time shift.

4 Results and Discussion

We first apply our methodology to the 2015 Illapel earthquake case. The time series of the seismic V_{SISM} and the ionospheric TEC data are shown in Figure 2. The seismic data are from the seismic station CO03, which is the closest to the epicenter, and TEC data corresponds to the SIP of Line-Of-Sight between the GPS station LSCH and G12 satellite (Figure 1). The SIP of the trajectory of PRN 12 passes over the seismic fault region and remains close to the epicenter (Figure 1). Figure 3 demonstrates the results of TEST-1 and TEST-2 in the left and right panels, respectively. We note the following characteristics:

- panels (A1, B1) reveal that the peak time of V_{SISM} depends on the frequency and occurs between 22:54 UT and 23:03 UT,
- panels (A2, B2) reveal that the peak time of ionoquakes also depends on the frequency,
- panels (A3, B3) reveal that the ionoquake detection time ranges between 250-550 seconds from the peak time of V_{SISM} , depending on the frequency and testing criteria,
- In both TEST-1 and TEST-2, the detection time of ionoquakes predominantly ranges between 250-400 seconds for the frequency range of 2-10 mHz,

Since both TEST-1 and TEST-2 confirm the ionoquake detection time range of 250-400 seconds, it can be considered as the valid ionoquake detection time in this frequency range, invariant of the criteria.

To validate the methodology of the detection time estimation, we apply it to the other SIP from various GPS stations within ± 400 km CO03-SIP distance that detected ionoquakes, and we further examine the relationship between the detection time and the CO03-SIP distance. Figure 4(A, B) demonstrates the relationship for the frequency of 3.7 mHz and a frequency range of 3.2-10 mHz, respectively. We note the expected increase of the detection time with the distance. According to Figure 4(B), the minimum detection time is about 200 seconds at the distance of about -125 km, corresponding to the CO03-SIP distance of LSCH-G12. Since detection time prolongs symmetrically across the minimum ionoquake detection time location, the analysis identifies this detection as the "earliest ionoquake". Noticeably, it is located very close to the epicenter and fault region (denoted as red star and purple square in Figure 4). Therefore, our methodology not only estimates the detection time vs. distance characteristics but also, locates the earliest ionoquake close to the epicenter, based on the minimum detection time of the ionoquake.

In supplementary Figure S1, we present time snapshots of the TEC map during -300-1400 seconds where 0 seconds correspond to the peak onset time of V_{SISM} at the frequency of 3.7 mHz. We note that the TEC response becomes noticeable approximately 240-300 seconds after the earthquake onset, in confirmation of findings in Figures 3-4.

4.1 Possible subjectivities of the new methodology and their impacts on the ionoquake detection time

4.1.1 Seismic station Vs. Epicenter

Figure 4 shows the ionoquake detection time estimated with reference to a particular seismic station: CO03, instead of the epicenter location. In order to examine any possible subjectivity arising from the location of a seismic station, we carry out the ionoquake detection time estimation for various seismic stations (Figure S2). We note that the ionoquake detection time remains within 250-400 seconds near the epicenter, inde-

pendently on a choice of a seismic station. Therefore, the results of the present methodology are not subjective to a choice of seismic station.

4.2 Detection altitude for rapid ionoquakes

Figure 4(A, B) reveals the potential of the present methodology to identify the epicentral distance of the earliest ionoquake close to the epicenter. However, the location of CID/ionoquakes depends on the altitude (H_{ION}) of the thin ionospheric layer that is assumed to be $H_{\text{ION}}=300$ km in Figure 4(A, B). Consequently, the horizontal distribution of ionoquakes will also depend on H_{ION} . To have an unambiguous ionoquake detection time, we examine the horizontal distribution of ionoquake detection time with varying $H_{\text{ION}}=200, 250, 300,$ and 350 km (Figure 5). Interestingly, in Figure 5(C), for $H_{\text{ION}}=300$ km, the epicenter and the locations of minimum detection time are the closest. Therefore, the altitude region around 300 km is the most favorable altitude for the detection of the ionoquakes.

4.2.1 Onset time of an earthquake Vs. Peak onset time of V_{SISM}

In previous studies, the onset time of an earthquake was used as a reference for the seismic source time (Astafyeva et al., 2011, 2013; Astafyeva & Shults, 2019; Thomas et al., 2018). However, strictly speaking, the earthquake onset time does not represent the source time. The theory considers the co-seismic crustal uplift to be the source of CID. Consequently, it is the time of the co-seismic uplift that should be taken as the source time. However, seismic ruptures take time to propagate and cause crustal uplifts. For large earthquakes that are characterized by large-dimension faults, the delay between the earthquake onset and the maximum uplift can reach up to 3 minutes. For smaller events, the delay of 10 to 20 seconds is usually observed. While this time is the most correct to use, it cannot be calculated rapidly and without numerical modeling of seismic faults. Besides, different seismological and seismo-geodetic techniques provide different solutions.

Our approach suggests using the peak onset time of V_{SISM} that is calculated from seismic stations. The main advantage of our method is the independence on the seismological models, and also in the fact that it allows to calculate the CID arrivals very rapidly, i.e. potentially it can be used in near-real-time.

According to the USGS solutions, the Illapel earthquake onset time is 22:54:32 UT, and the maximum uplift occurred at 22:55:22 UT on the north-east from the epicenter. The peak onset time of V_{SISM} varies between 22:54 and 23:03 UT (Figure 3(A1, B1)), i.e., it is delayed between 32 seconds and 9 minutes from the USGS onset time, and 87 seconds to nearly 10 min from the seismic uplift time.

To examine the effects of the delay and other subjectivities arising from the usage of the seismic peak onset time rather than the earthquake onset time and the uplift time, we carry out the ionoquake detection time estimation with the following conventional definitions:

$$t_{1\text{detection}} = t_{\text{TEC}} - 22 : 54 : 32, \quad t_{2\text{detection}} = t_{\text{TEC}} - 22 : 55 : 25 \quad (4)$$

Here, t_{TEC} is the peak onset time of ionoquake is the same as defined for TEST-1 in Equation (3). The $t_{2\text{detection}}$ in Equation (4) the maximum uplift time. Figure 4(C, D) shows the results for the $t_{1\text{detection}}$ and $t_{2\text{detection}}$. One can see that within 50 to 200 km epicentral distance, both the $t_{1\text{detection}}$ and $t_{2\text{detection}}$ are less than 400 seconds.

Moreover, we note that in Equation (4), the t_{TEC} corresponds to the first peak of ionoquake, and it is subtracted from the earthquake onset time of 22:54:32. However,

237 in this scenario, the onset time of an ionoquake is more correct than the time of the first
 238 peak of ionoquake. This will however decrease the $t_{\text{detection}}$. For instance, at a frequency
 239 of 4.3 mHz, the onset time of the ionoquake will occur about 116 seconds earlier than
 240 the time of the peak of the ionoquake. Therefore, in Figure 4(C, D), the appropriate iono-
 241 quake detection time will shift by -116 seconds at the frequency of 4.3 mHz. Consequently,
 242 in the vicinity of the epicenter the ionoquake detection time can be around 300 seconds,
 243 which might seem too short knowing that the "nominal" propagation of CID is about
 244 7-10 minutes. Such a short timing could be related to low elevation angles during the
 245 detection of ionoquakes, that will lead to lower and much lower altitudes of detection,
 246 or higher vertical and horizontal propagation speeds because of transformation of acous-
 247 tic waves into shock-acoustic waves due to non-linear effects. Below we discuss all these
 248 possible explanations.

249 4.3 Propagation speed and acoustic wave energetics

250 Relative to the location of the minimum detection time, the averaged propagation
 251 speed of the ionoquakes can be estimated as follows:

$$v = \frac{d - d_{\text{generation}}}{t - t_{\text{generation}}} \implies v1 = \frac{d - d_0}{t - t_0} \quad \text{or} \quad v2 = \frac{d - d_{eq}}{t - t_{eq}} \quad (5)$$

252 where (d, t) are the coordinates of the ionoquake in Figure 4(B), $(d_{\text{generation}}, t_{\text{generation}})$
 253 are the coordinates of the ionoquake at the time of generation, (d_0, t_0) are the coordi-
 254 nates of the ionoquake corresponding to the minimum detection time in Figure 4(B), and
 255 (d_{eq}, t_{eq}) are the location of the epicenter and the onset time of the earthquake. The speed
 256 $v1$ sets the upper limit for the actual speed since the ionoquakes are possibly generated
 257 either at the minimum detection time or slightly earlier. The speed $v2$ sets the lower limit
 258 for the actual speed since ionoquakes are certainly generated after the onset time of earth-
 259 quake t_{eq} . Therefore, the actual speed resides in between the lower $v2$ and upper $v1$ lim-
 260 its. Figure S3 shows the distribution of $v1$ and $v2$ as a function of ionoquake detection
 261 time and CO03-SIP distance. We note that they are in the range of 0.25-1.5 km/s such
 262 that the early detected ionoquakes have predominantly large speeds. For instance, rapid
 263 ionoquakes with a detection time of 250-400 seconds predominantly propagate faster than
 264 0.75 km/s which is the acoustic speed range in the upper atmosphere. Previous stud-
 265 ies have found that acoustic-gravity waves resulting from ground vibration can efficiently
 266 couple with the ionosphere and give rise to the ionoquakes (Rolland et al., 2013; Sanchez
 267 et al., 2022). If a wave responsible for coupling propagates faster than 0.75 km/s, it ar-
 268 rives at 180 km or higher altitude in 250-400 seconds. Therefore, the detection time and
 269 propagation speed of rapid ionoquakes suggest the altitude of detection of rapid iono-
 270 quakes to be above 180 km altitude, i.e., in the upper atmosphere where acoustic speed
 271 is faster than 0.75 km/s. Therefore, the methodology of ionoquake detection time esti-
 272 mation and their propagation speed estimation validate each other. Moreover, it is cor-
 273 rect to say that the majority of rapid ionoquakes originate in the altitude range between
 274 180 km and $H_{\text{ION}}=300$ km. Interestingly, simulation study by Chum et al. (2016) for
 275 the Illapel earthquake finds significant air particle disturbance in the altitude range of
 276 170-250 km, raising the possibility of the majority of ionoquakes to be in this altitude
 277 range, as found in the present study. Also, the simulation study by Kherani et al. (2012)
 278 demonstrated the acoustic-gravity wave with a vertical phase speed of more than 600
 279 m/s to give rise to the coseismic TEC disturbances within (300) 360 seconds at the height
 280 of 180 (250) km.

281 The lower limit $v2$ distribution in Figure S3 also attains the lowest of about 0.25
 282 km/s for the early detected ionoquakes in the vicinity of the epicenter. This is due to
 283 the instantaneous generation ($t_{\text{generation}} = t_{eq}$) assumption in (5) which is not quite re-
 284 alistic. For the large earthquake of the 2011 Japan tsunami, the simulation of the Seismo-
 285 Atmosphere-Ionosphere (SAI) coupling revealed that the ionoquake can be developed
 286 within 360 seconds from the earthquake onset due to the fast-propagating Acoustic-Gravity

287 wave energetics (Kherani et al., 2012). Therefore, the definition $v1$ in (5) and the cor-
 288 responding distribution in Figure S3(A) represent a realistic scenario. Moreover, in the
 289 present study, the ionoquake detection time of 250-400 seconds can be associated with
 290 the SAI coupling mechanism energized by the acoustic-gravity wave.

291 4.4 Ionoquake detection time during the Mw8.2 Iquique earthquake of 292 01 April, 2014

293 Figures 6-7 show our results for the Iquique earthquake of 01 April 2014. The temporal-
 294 spectral characteristics of V_{SISM} and TEC data in Figure 6(A1-A2) and the estimation
 295 of $t_{\text{detection}}$ in Figure 6(A3) reveal the detection of ionoquakes starting from 430 seconds
 296 after the peak onset time of V_{SISM} for the frequency range of 2 mHz-10 mHz. The con-
 297 ventional detection time $t1_{\text{detection}}$, represented by yellow circles in Figure 6(A3) is in
 298 between 600-700 seconds which suffers from the time shift effects, as discussed in sec-
 299 tion 4.1.1. The relationship between $t_{\text{detection}}$ and seismic-SIP distance in Figure 7 shows
 300 the two-direction propagating ionoquakes with the earliest ionoquake location near the
 301 epicenter for $H_{\text{ION}}=200$ km. We note the detection of several rapid ionoquakes in 400-
 302 430 seconds within 200 km seismic-SIP distance, i.e., within about 250 km epicentral dis-
 303 tance. The detection of rapid ionoquakes in the case of the Iquique earthquake is slightly
 304 delayed, in comparison to the much earlier detection (lower than 400 seconds) in the case
 305 of the Illapel earthquake. This suggests that not all strong earthquakes produce rapid-
 306 ionoquakes detectable within 400 seconds from the peak onset time of the ground vibra-
 307 tion.

308 4.5 Ionoquake detection time during the Mw7.4 Sanriku-Oki earthquake 309 of March 9, 2011

310 We applied our newly developed method to seismic and TEC data around the epi-
 311 central area of the Sanriku-oki earthquake (Figures 8-9). The temporal-spectral char-
 312 acteristics of V_{SISM} and TEC data in Figure 8(A1-A2) and the estimation of $t_{\text{detection}}$
 313 in Figure 8(A3) reveal the detection of ionoquakes between 240-400 seconds for the fre-
 314 quency range of 2.5 mHz-10 mHz. The conventional detection time $t1_{\text{detection}} = t_{\text{TEC}} -$
 315 $02 : 45 : 20$, represented by yellow circles in Figure 8(A3) also below 400 seconds for
 316 frequencies below 5 mHz. Figure 9 reveals the detection of rapid ionoquakes, as close as
 317 100 km of the epicentral distance. The relationship between the $t_{\text{detection}}$ and the seismic-
 318 SIP distance shows two-direction propagating ionoquakes from the epicentral region for
 319 $H_{\text{ION}}=150$ km-180 km.

320 Previously, Thomas et al. (2018) and Astafyeva and Shults (2019) reported the de-
 321 tection of the first ionoquakes at 430 seconds and 470-480 seconds respectively at the
 322 altitudes 150 km and 180-190 km, respectively. Our methodology applied for the same
 323 LOS as in Thomas et al. (2018) and Astafyeva and Shults (2019) shows quite similar re-
 324 sults: The conventional detection time $t1_{\text{detection}}$, represented by yellow-circles in Fig-
 325 ure S4(A3-B3) is 430-520 seconds. However, based on the $t_{\text{detection}}$, the earliest ionoquakes
 326 are detected at about 320 to 460 seconds, as shown by the gray circles in Figure S4(A3-
 327 B3). Moreover, $H_{\text{ION}}=150$ km-180 km of the present methodology confirms the altitude
 328 of the earliest ionoquakes reported in the previous studies of Thomas et al. (2018) and
 329 Astafyeva and Shults (2019). Therefore, our methodology estimates the true earliest ar-
 330 rivals of the ionoquakes/CID, in addition to the altitude of detection.

331 Supplementary Figure S5(A) shows the results for conventional detection time $t1_{\text{detection}}$
 332 in the same format as Figure 9(B). For comparison, Figure 9(B) is re-drawn as Figure
 333 S5(B). The conventional method detects the earliest ionoquakes 350-400 seconds after
 334 the earthquake onset time though they are few compared to the number of earliest iono-
 335 quakes detected from the newly developed method in Figure S5(B). Therefore, both con-
 336 ventional and the newly developed methods detect the earliest ionoquakes in less than

337 400 seconds from the earthquake onset time and from the time of the peak seismic up-
 338 lift.

339 **5 Rapid Ionoquakes from Seismo-Atmosphere-Ionosphere Coupling**

340 Past simulation studies (e.g., Kherani et al. (2012, 2016)) have found that the SAI
 341 coupling energized by the Acoustic-Gravity waves (AGWs) generates rapid ionoquakes
 342 in the upper thermosphere within 360 seconds from the earthquake onset. The rapid iono-
 343 quakes of the present study are likely to be associated with this coupling mechanism. How-
 344 ever, the simulation study of Kherani et al. (2016) was for the case of a tsunami. For an
 345 earthquake, no simulation study is available to support the early arrival within 360 sec-
 346 onds from the mainshock onset of the present study. The simulation study of Chum et
 347 al. (2016) for the Illapel earthquake demonstrates the onset time of air particle distur-
 348 bances only 530 seconds after the earthquake at 800 km epicentral distance. Consequently,
 349 in the vicinity of the epicenter, the disturbance should be detected several hundreds of
 350 seconds earlier.

351 We examine this possibility by solving the governing equations of the ground uplift-
 352 Acoustic-Gravity wave-Ionospheric disturbances coupling mechanism, presented by Kherani
 353 et al. (2012) for the Tohoku-Oki event and later employed by Sanchez et al. (2022) for
 354 the Ridgecrest earthquake. In Figures 10-11, we demonstrate the simulation results for
 355 the Illapel earthquake. We note in Figure 10 that the observed and simulated waveforms
 356 of ionoquakes are fairly good in agreement. Moreover, in Figure 11, observed and sim-
 357 ulated ionoquake detection times are in the same time range of 260-400 seconds. There-
 358 fore, the physical mechanism responsible for the rapid ionoquakes Seismo-Atmosphere-
 359 Ionosphere coupling dynamics energized by the Acoustic-Gravity waves.

360 The supplementary Figure S6 demonstrates the vertical propagation of simulated
 361 acoustic-gravity waves above the epicenter. We note that from the ground uplift, numer-
 362 ous waves with wavefronts of different slopes i.e., of different phase speeds are launched
 363 into the atmosphere. This is owing to the numerous scale heights and duct sizes present
 364 in the atmosphere, that allow numerous wavelengths at a given frequency to be sustained
 365 in the atmosphere. We note that the waves with significant amplitudes of about 10-20
 366 m/s arrive at 160 km altitude at 22.975 hours from the mainshock onset time of 22.91
 367 hours i.e., the waves arrive in about 240 seconds from the onset. These waves have wave-
 368 lengths comparable to the size of the longest atmospheric duct of about 150 km and at
 369 the acoustic frequencies, they propagate with a phase speed of about 600 m/s or more.
 370 Therefore, in the rapid development of ionoquakes, the long wavelength AGWs partic-
 371 ipate, as also found by Kherani et al. (2012). We note in Figure S6 that though the
 372 phase speed is about 600 m/s or more, the amplitude of the wave i.e., the fluid oscilla-
 373 tion is about 10-20 m/s, much slower than the average atmospheric sound speed. There-
 374 fore, such a fast propagating wave is not a shock acoustic wave, the wave which is char-
 375 acterized by a phase speed slower than the average atmospheric sound speed and an am-
 376 plitude comparable to the thermospheric sound speed (Zettergren et al., 2017).

377 **6 Summary**

378 We report early detections of co-seismic ionospheric disturbances (or ionoquakes)
 379 associated with the 2015 Illapel, the 2014 Iquique, and the 2011 Sanriku-Oki earthquakes.
 380 Using Total-Electron-Content (TEC) and seismic measurements, the study compares iono-
 381 quakes from our new and previous methods. The new method relies on applying the same
 382 data processing procedures to the seismic and TEC data, and on estimating the time of
 383 the peak of the seismic and TEC vibrations to obtain the ionoquake detection time. The
 384 advantage of our method is its independence from the seismological models. The method
 385 produces the expected prolongation in ionoquake detection time with increasing distance
 386 from the epicenter. Moreover, the method allows locating the earliest detected ionoquakes

387 which turns out to be near the epicenter. The localization is more accurate for the thin
 388 ionospheric layer centered around an altitude of 300 km for the Illapel, 200 km for the
 389 Iquique, and 150-180 km altitude for the Sanriku-Oki earthquakes. The new method also
 390 finds spectral and propagation characteristics of the earliest ionoquakes predominantly
 391 in the acoustic range. A comparative study with the conventional ionoquake detection
 392 time method highlights a new result that the detection time of earliest ionoquakes is within
 393 400 seconds from the earthquake onset time and from the time of peak seismic uplift,
 394 for the Illapel and Sanriku-Oki earthquakes. For the Iquique earthquake, the new method
 395 detects the ionoquakes as early as 430 seconds from the time of the peak seismic uplift.
 396 Based on numerical simulation of the Seismo-Atmosphere-Ionosphere (SAI) coupling mech-
 397 anism, the study associates the rapid ionoquakes with the SAI coupling energized by the
 398 acoustic-gravity waves.

399 **Open research statement**

400 The GNSS data for the earthquakes in Chile are available at the UNAVCO web-
 401 service (<https://www.unavco.org/data/gps-gnss/data-access-methods/gnss-data-access-notebook/gnss-data-access-notebook.html>) and CSN (<http://gps.csn.uchile.cl/>). The GNSS data for the 2011 Sanriku earthquake are available from the
 403 GeoSpatial Authority of Japan (GSI, terras.go.jp) via http://datahouse1.gsi.go.jp/terras/terras_english.html). The seismic data can be downloaded from the IRIS (http://ds.iris.edu/wilber3/find_event)
 406

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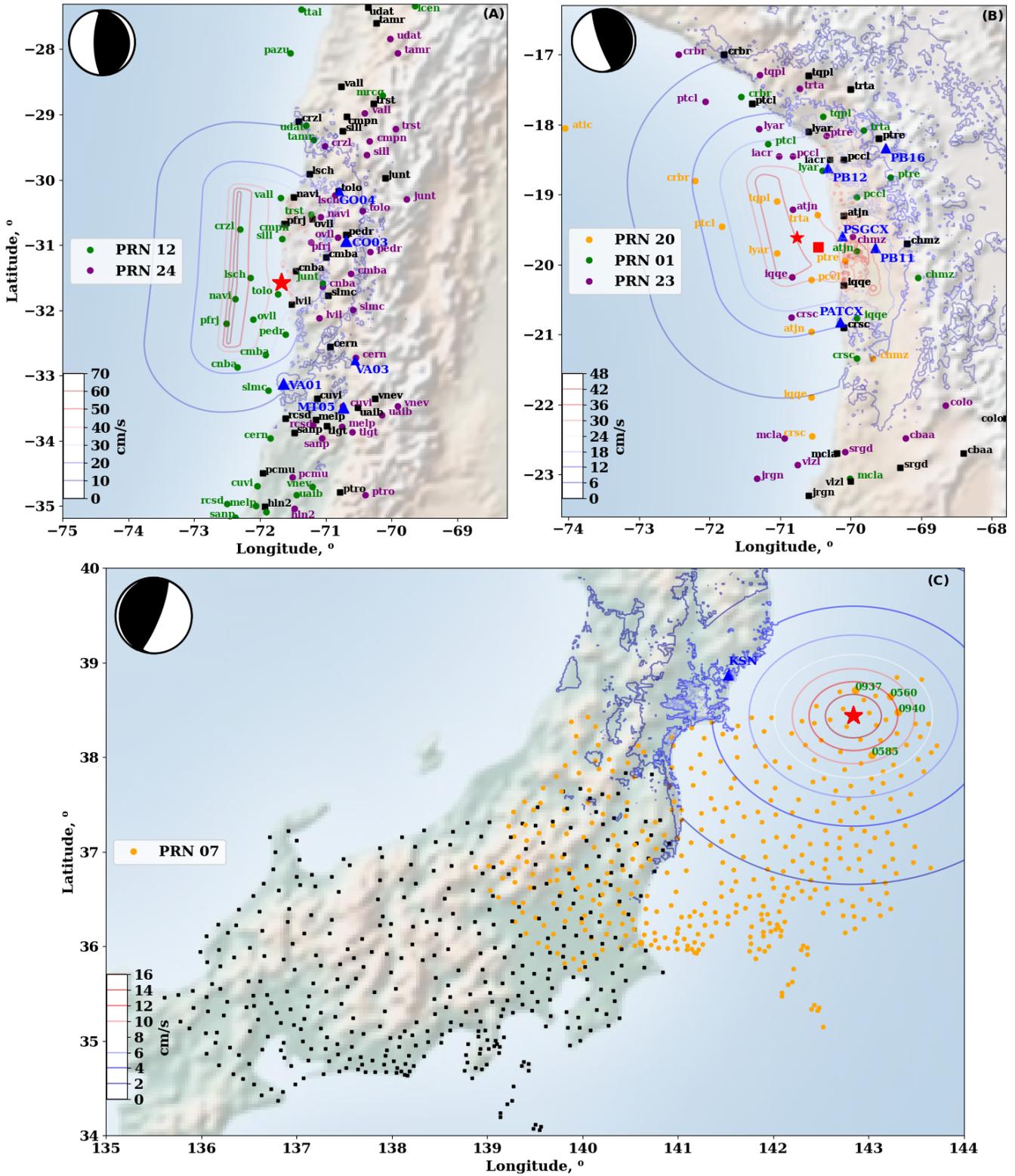


Figure 1. Locations of the 2015 Illapel (A), the 2014 Iquique (B) and the 2011 Sanriku-oki (C) earthquakes. The epicenter of the earthquakes is represented by a red star and the blue triangles show the location of the seismic stations used in this study. The dots of different colors represent the SIPs at the time when the ionoquake occurred, each color corresponds to a particular PRN. The black squares depict the location of the GNSS stations. The colored contours represent the PGVs (Peak-Ground-Velocity) for each of the earthquakes. Beach ball shows the Global Centroid Moment Tensor

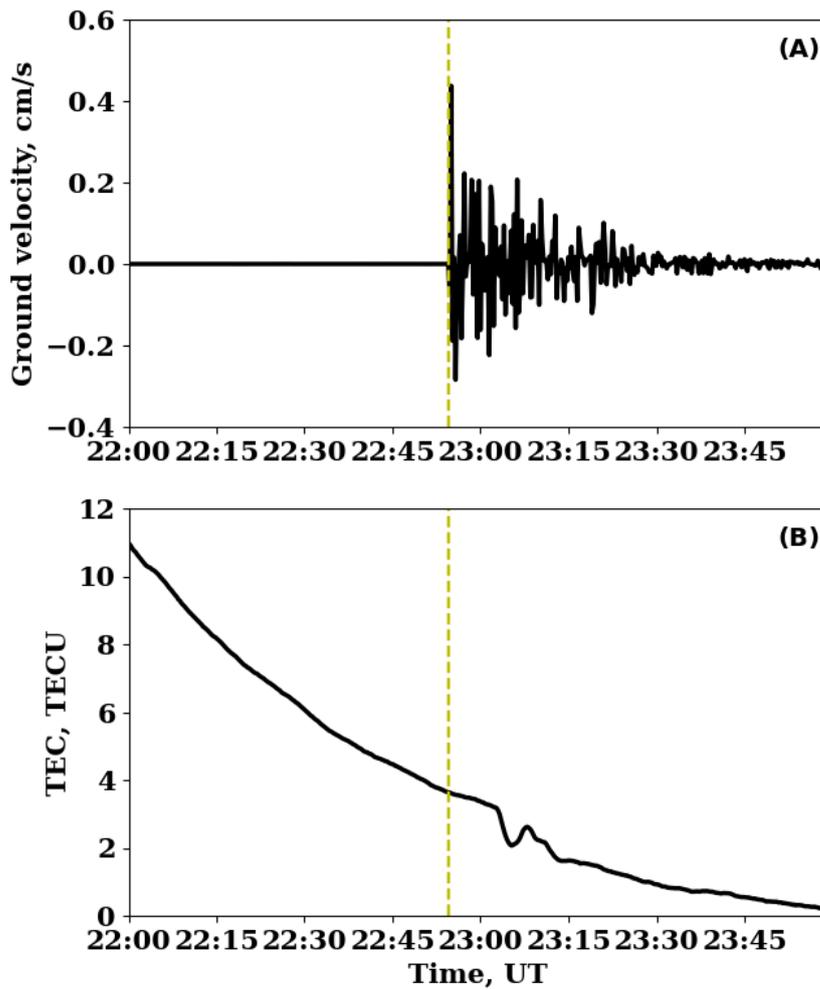


Figure 2. The 2015 Illapel earthquake: Vertical ground velocity recorded by seismic station CO03 (A), TEC time series recorded by the GNSS satellite PRN G12 and the LSCH ground receiver (B). Both the V_{SISM} and TEC time series have a resolution of 15 seconds.

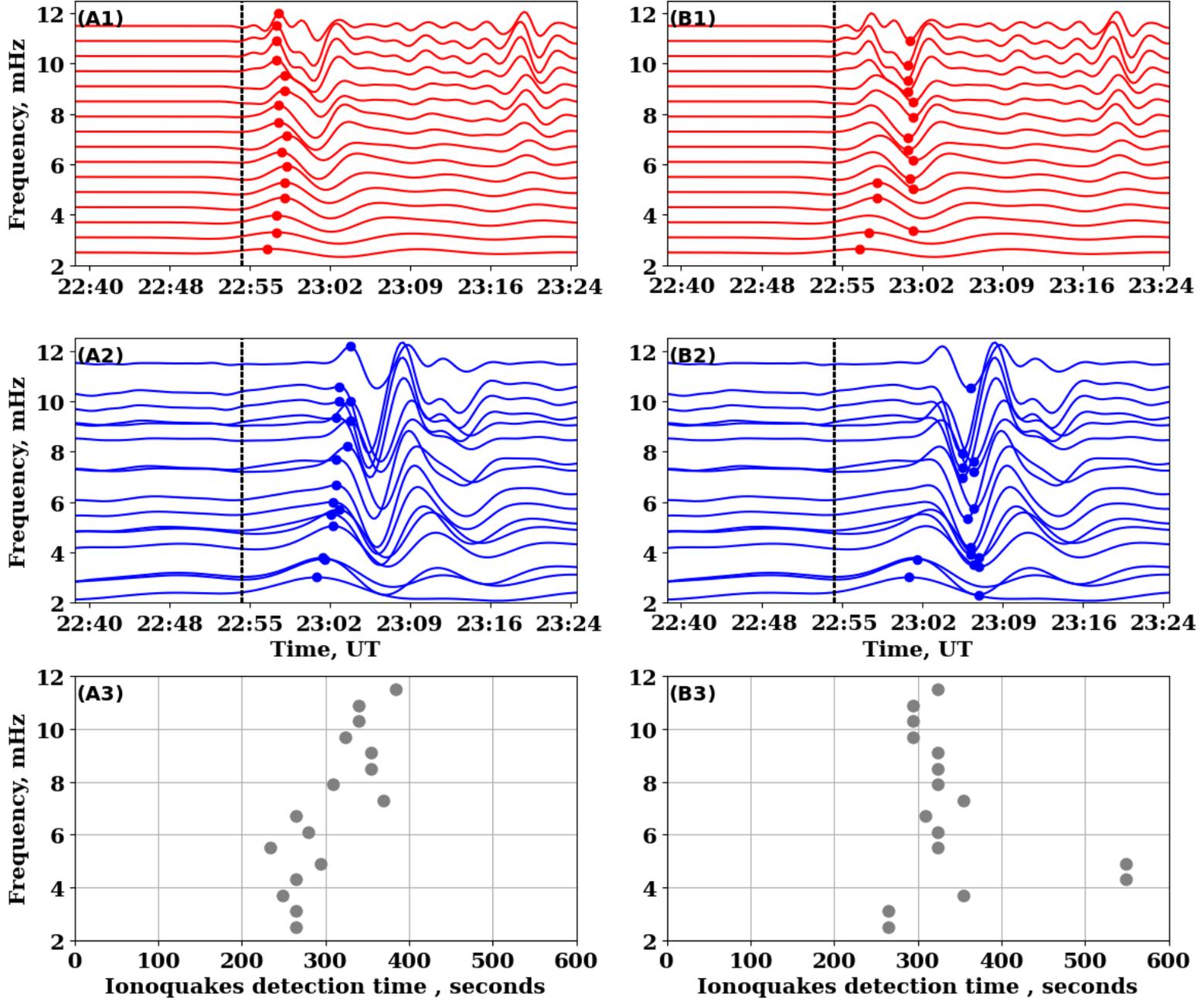


Figure 3. The 2015 Illapel earthquake: Results of TEST-1 (left) and TEST-2 (right). Panels A1-B1 show the V_{SISM} time series recorded by the CO03 seismic station for different frequencies. Panels A2 and B2 show the ΔTEC time series obtained at different frequencies for the LSCH PRN G12 station. The filled circles in (A1,A2) represent the time of the peak in the first seismic oscillation and the first ΔTEC oscillation, respectively. The filled circles in (B1, B2) show the peak in the entire series of seismic and ΔTEC oscillations, respectively. The filled circles in panels (A3, B3) represent the detection time of ionoquakes, $t_{\text{detection}}$, derived from the definition (3).

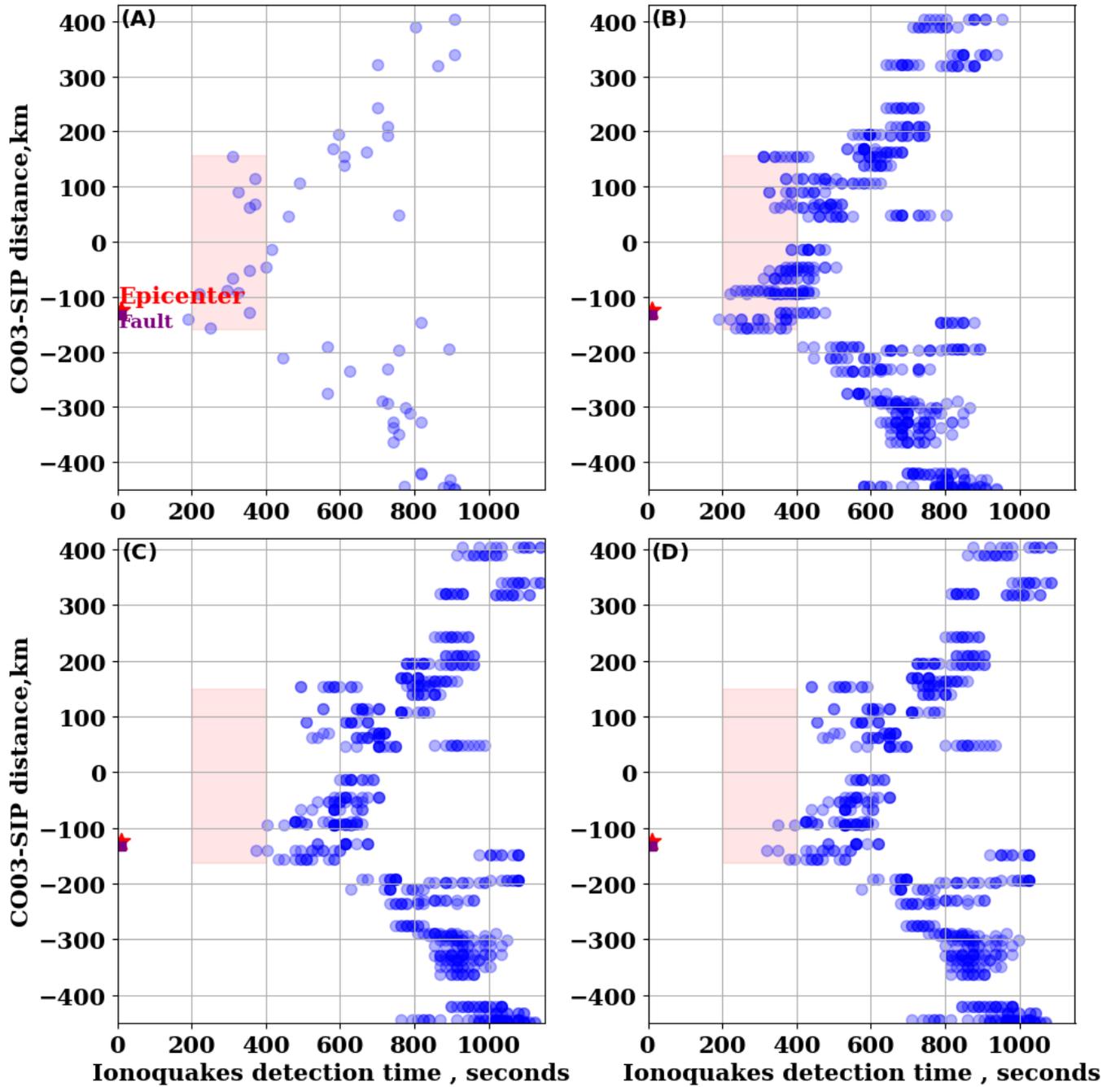


Figure 4. The 2015 Illapel earthquake: Ionoquake detection time vs. distance diagram where distance is in between seismic station (C003) and Sub-Ionospheric-Point (SIP) of Line-of-sight (LOS) of LSCH-G12 pair. Panels (A-B) correspond to the new definition $t_{\text{detection}}$ in (3) for a frequency of 3.7 mHz, and a frequency range 3.2-10 mHz, respectively. Panels (C-D) correspond to the conventional definitions $t_{1\text{detection}}$ and $t_{2\text{detection}}$ in (4), respectively for a frequency range 3.2-10 mHz. The distance of 0 km indicates the location of the CO03 seismic station. In (A-B), $t_{\text{detection}} = 0$ in the x-axis corresponds to the time of peak seismic uplift at each corresponding frequency. In (C-D), $t_{1\text{detection}} = 0$ in the x-axis corresponds to the time of earthquake onset.

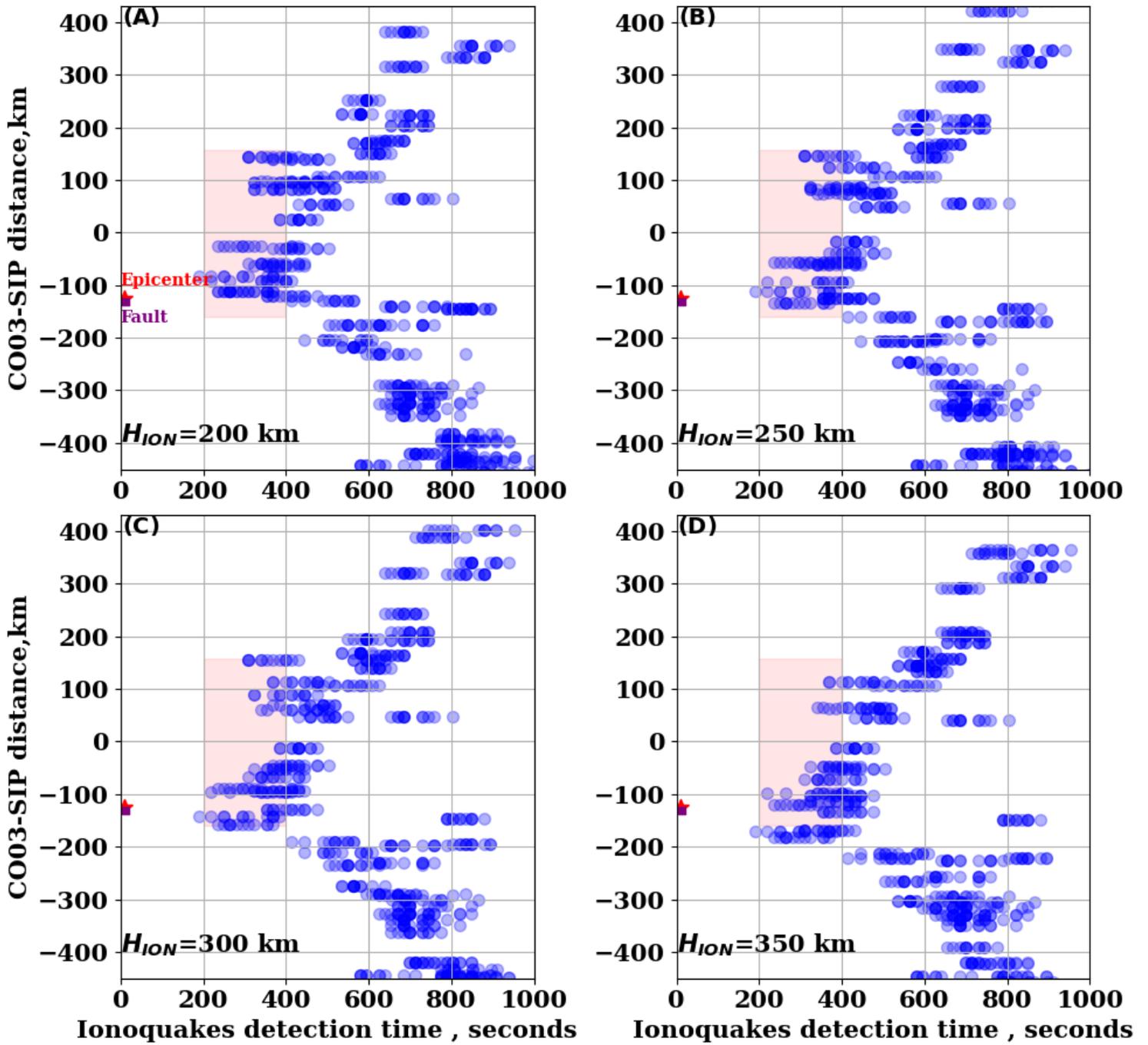


Figure 5. The 2015 Illapel earthquake: $t_{\text{detection}}$ - distance diagram where distance is in between the seismic station (C003) and SIPs of LOSs of numerous GPS receiver-satellite pairs. The frequency range is 3.2-10 mHz. Four panels correspond to four values of altitude of detection (H_{ION}). The distance of 0 km indicates the location of the CO03 seismic station. $t_{\text{detection}} = 0$ in the x-axis corresponds to the time of peak seismic uplift at each corresponding frequency.

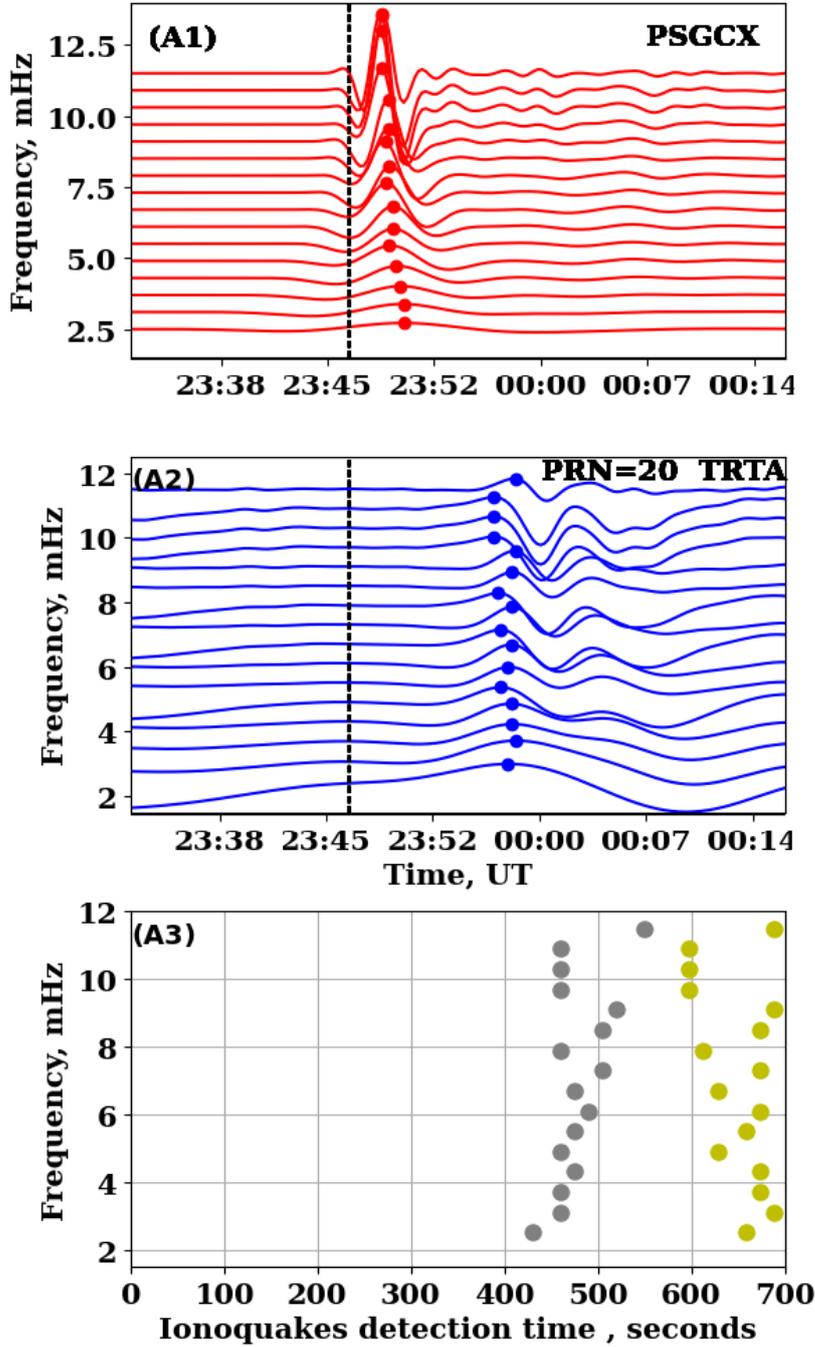


Figure 6. The 2014 Iquique earthquake with TEST-1. Panel A1 shows the V_{SISM} time series recorded by the PSGCX seismic station for different frequencies. Panel A2 shows the ΔTEC time series obtained at different frequencies for the TRTA PRN G20 station. In (A1-A2), the filled circles represent the time of the peak in the first seismic oscillation and the first ΔTEC oscillation, respectively. In panel A3, filled circles in grey and yellow correspond to the new definition, $t_{detection}$ in (3), and the conventional definition, $t_{detection} = t_{TEC} - 23:46:47$, respectively.

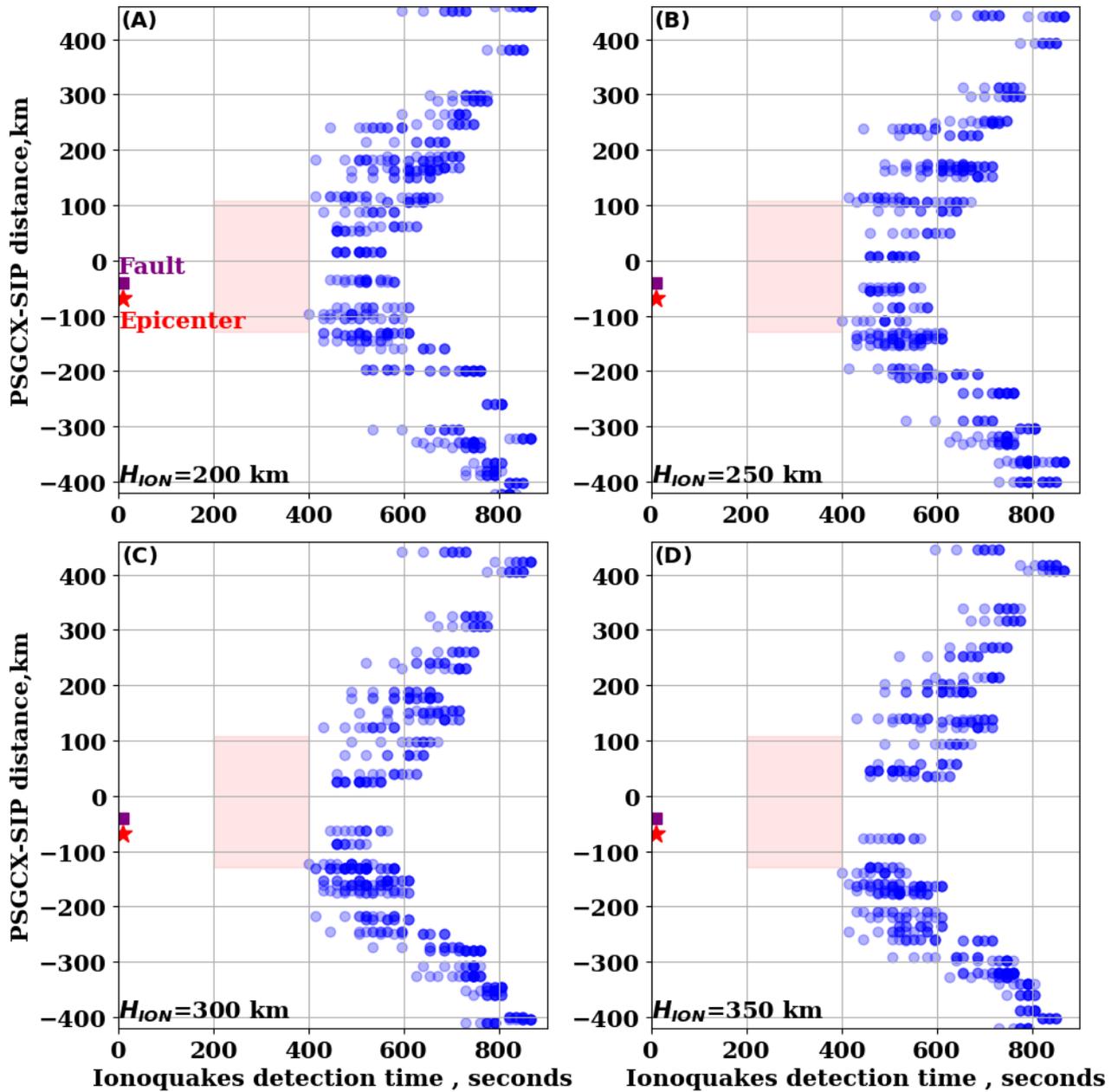


Figure 7. The 2014 Iquique earthquake: $t_{\text{detection}}$ - distance diagram where distance is in between the seismic station (PSGCX) and SIPs of LOSs of numerous GPS receiver-satellite pairs. The frequency range is 3.2-10 mHz. Four panels correspond to four values of altitude of detection (H_{ION}). The distance of 0 km indicates the location of the PSGCX seismic station. $t_{\text{detection}} = 0$ in the x-axis corresponds to the time of peak seismic uplift at each corresponding frequency.

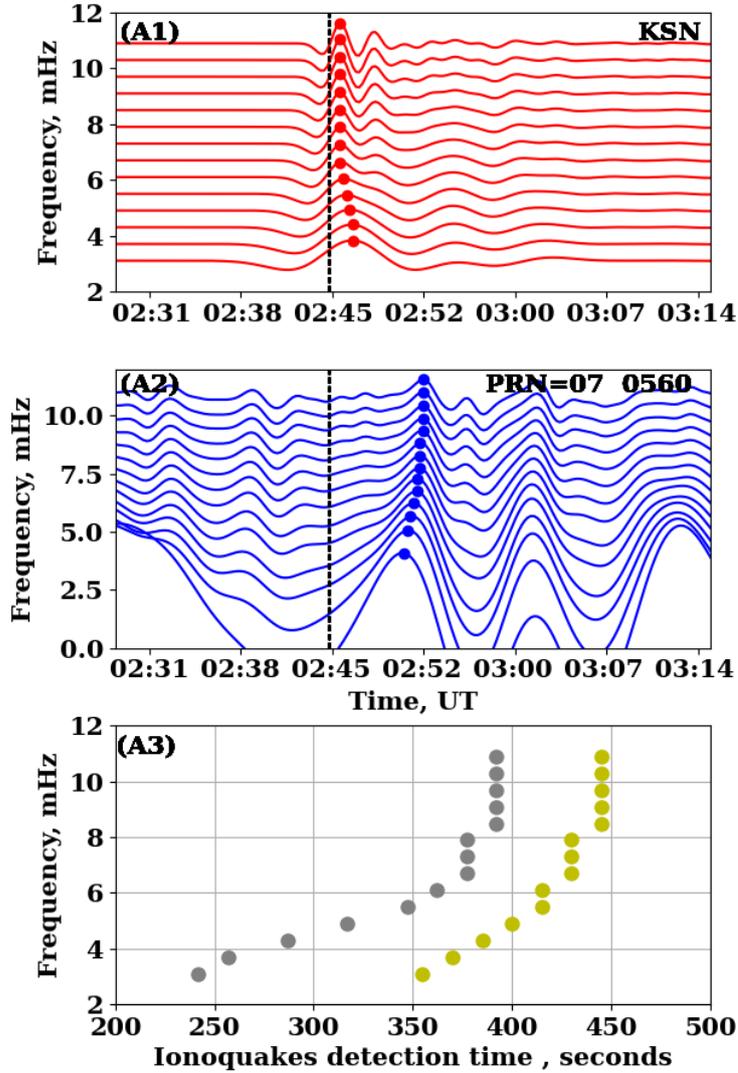


Figure 8. The 2011 Sanriku-Oki earthquake with TEST-1. Panel A1 shows the V_{SISM} time series recorded by the KSN seismic station for different frequencies. Panel A2 shows the ΔTEC time series obtained at different frequencies for the 0560 PRN G07 station. In (A1-A2), the filled circles represent the time of the peak in the first seismic oscillation and the first ΔTEC oscillation, respectively. In panel A3, filled circles in grey and yellow correspond to the new definition, $t_{\text{detection}}$ in (3), and the conventional definition, $t_{1_{\text{detection}}} = t_{\text{TEC}} - 02 : 45 : 20$, respectively.

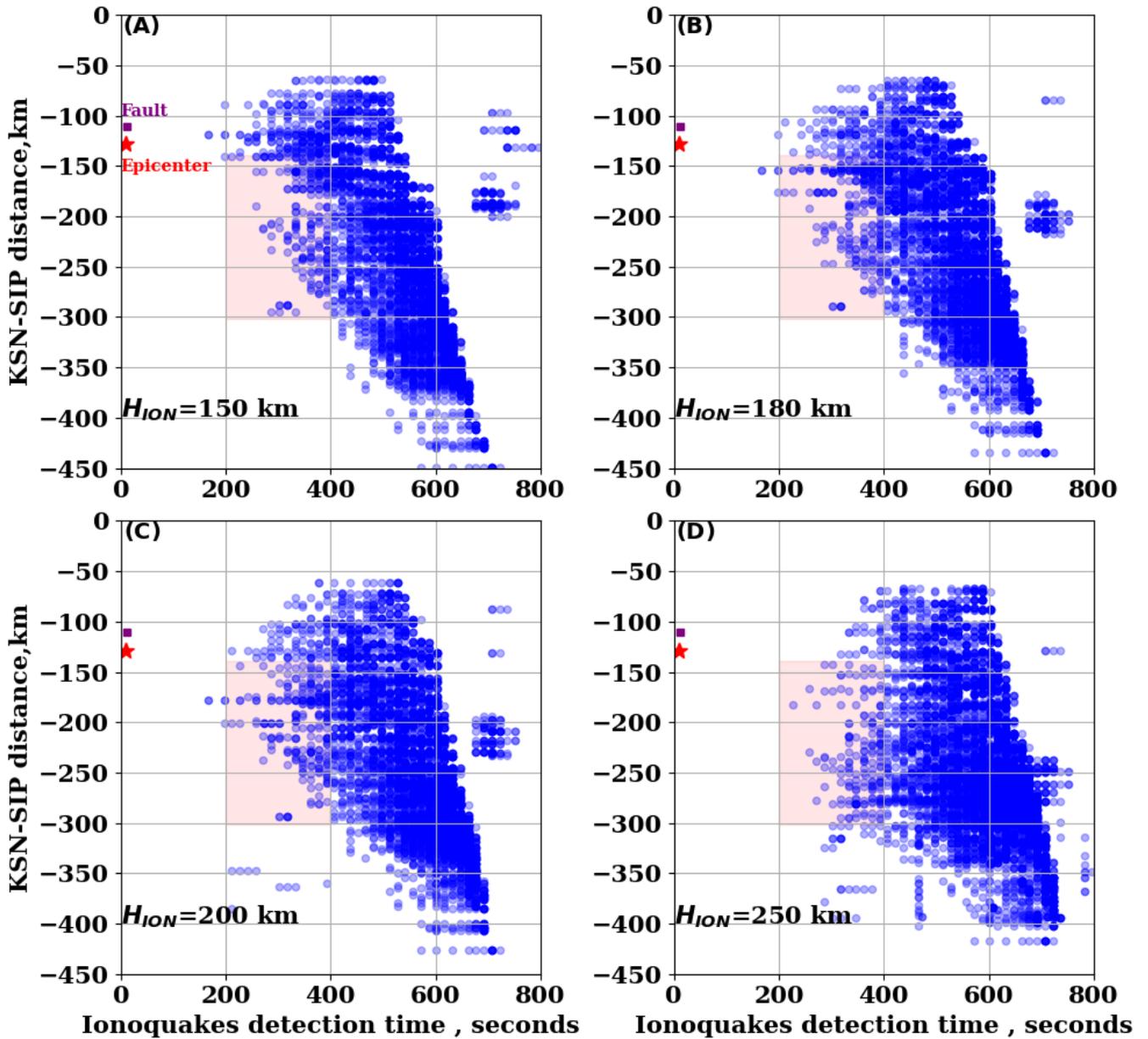


Figure 9. The 2011 Sanriku-Oki earthquake: $t_{\text{detection}}$ - distance diagram where distance is in between the seismic station (KSN) and SIPs of LOSs of numerous GPS receiver-satellite pairs. The frequency range is 3.2-10 mHz. Four panels correspond to four values of altitude of detection (H_{ION}). The distance of 0 km indicates the location of the KSN seismic station. $t_{\text{detection}} = 0$ in the x-axis corresponds to the time of peak seismic uplift at each corresponding frequency.

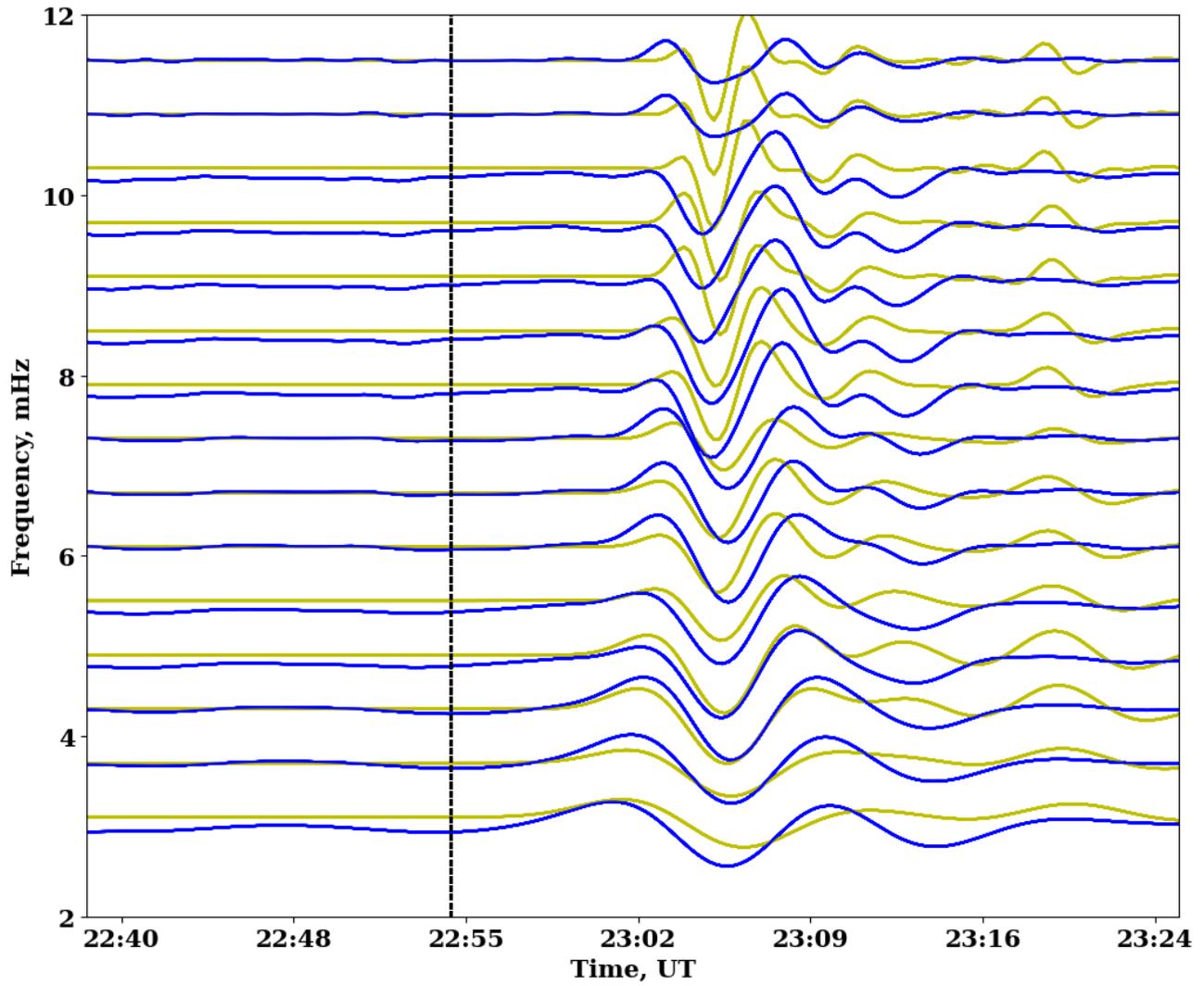


Figure 10. Δ TEC comparison between observation (blue) and simulation (yellow), for the Illapel earthquake.

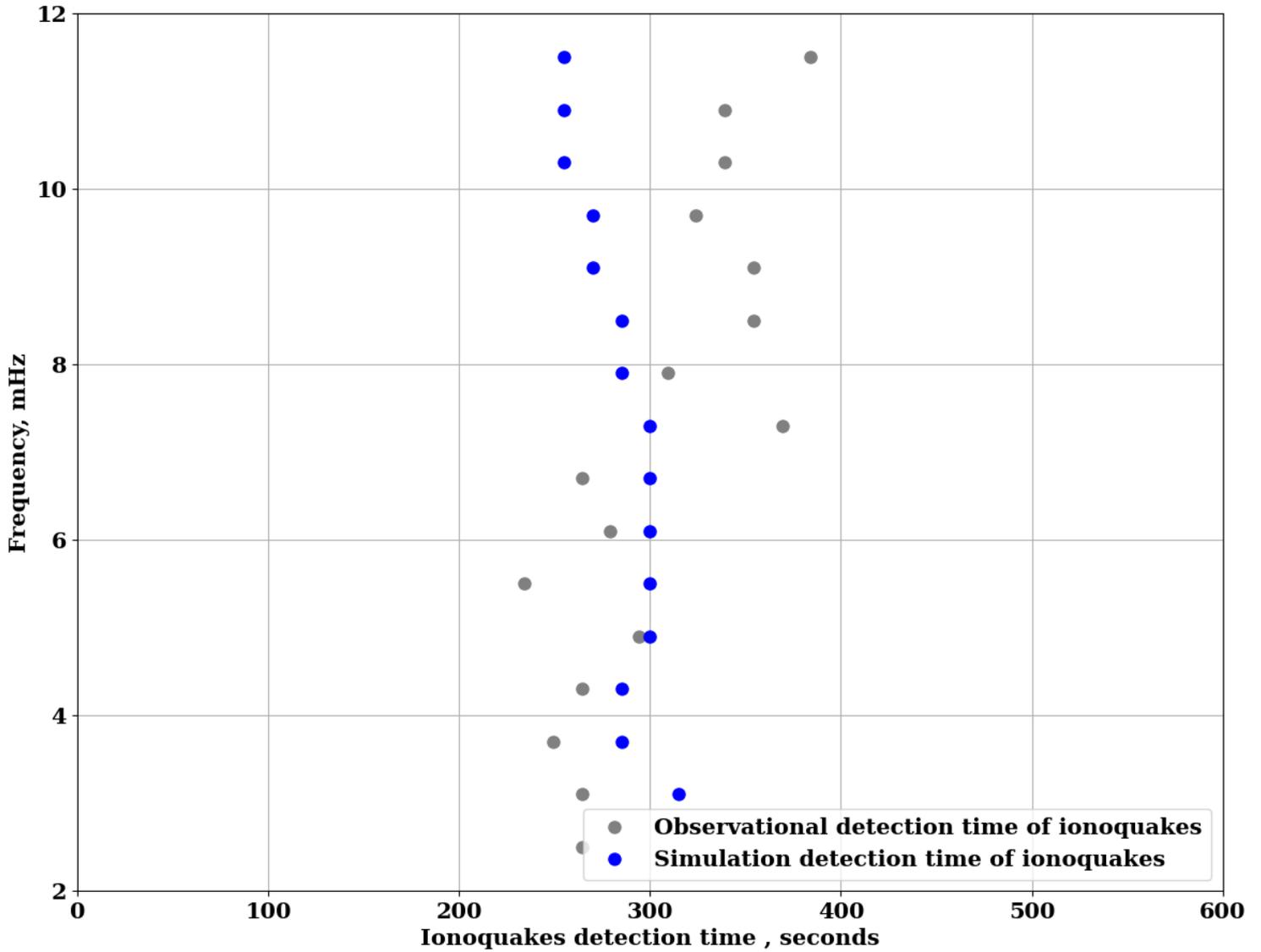


Figure 11. The 2015 Illapel earthquake. Comparison of Ionoquakes detection time between simulation and observation.