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# Restoring and tailoring very high dimensional spatial entanglement of a biphoton state transmitted through a scattering medium

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We report experimental results where a momentum entangled biphoton state with a Schmidt number of a few thousand is retrieved and manipulated when only one photon of the pair is transmitted through a thin scattering medium. For this purpose, the transmission matrix of the complex medium is first measured with a phase-shifting interferometry measurement method using a spatial light modulator (SLM) illuminated with a laser source. From this matrix, different phase masks are calculated and addressed on the SLM to spatially control the focusing of the laser through the complex medium. These same masks are used to manipulate the phase of the biphoton wave function transmitted by the thin diffuser in order to restore and control in the same way the momentum correlations between the far-field images of twin beams issued from strongly spatial-multi-mode spontaneous parametric down conversion.

## I. INTRODUCTION

The control of light propagation through complex media such as multimode optical fibers, atmospheric turbulence or biological media is a major challenge for the development of protocols and systems for information processing, communication and imaging using the quantum or the classical properties of light [1]. Besides, the manipulation of high dimensional quantum states allows a significant increase of the information that can be transmitted and processed. In this context, it is of great interest to be able to transmit high-dimensional quantum states through complex media while preserving and manipulating their dimensionality.

Although it is easy to produce spatially entangled photon pairs with giant dimensionality [2], the entanglement is strongly degraded by the propagation in a complex medium [3, 4]. Several approaches have been proposed and experimentally demonstrated to counteract the effects of this environment on the transmission and propagation of quantum states. All these methods are based on the use of adaptive optics and wavefront shaping either of the pump beam [5, 6] or of the phase front of the biphoton wave function [7]. In these works, type-I entangled photons are inseparable and therefore transmitted through the same complex medium, unlike in most practical applications. Another approach consists in using type-II entangled photons to process and detect separately the photons of a pair. In that case two methods can be considered. First, in [8] Valencia et al. demonstrated the transmission of a 7-dimensional entangled state through a short commercial multi-mode fibre where unscrambling of entanglement is obtained by manipulating only the photon that does not enter the fibre.

Here we demonstrate the second method consisting in the manipulation of the photon propagating through the complex medium. Contrary to [8], where the transmission matrix (TM) of the complex medium is measured using the entangled state itself, we use as in [7] a laser source for this measurement and the design of phase masks that are applied to manipulate focusing of this laser through the complex medium. Then, we show that the same masks allow restoring and controlling the high dimensional biphoton state transmitted through the ground glass diffuser. Instead of point detectors measuring temporal coincidences between spatially entangled photons [5, 6, 8], single-photon sensitive cameras are used, allowing the detection of all photons of the images and the measurement of momentum spatial coincidences on the whole set of photons without any prior selection of the photons in time and space coincidence.

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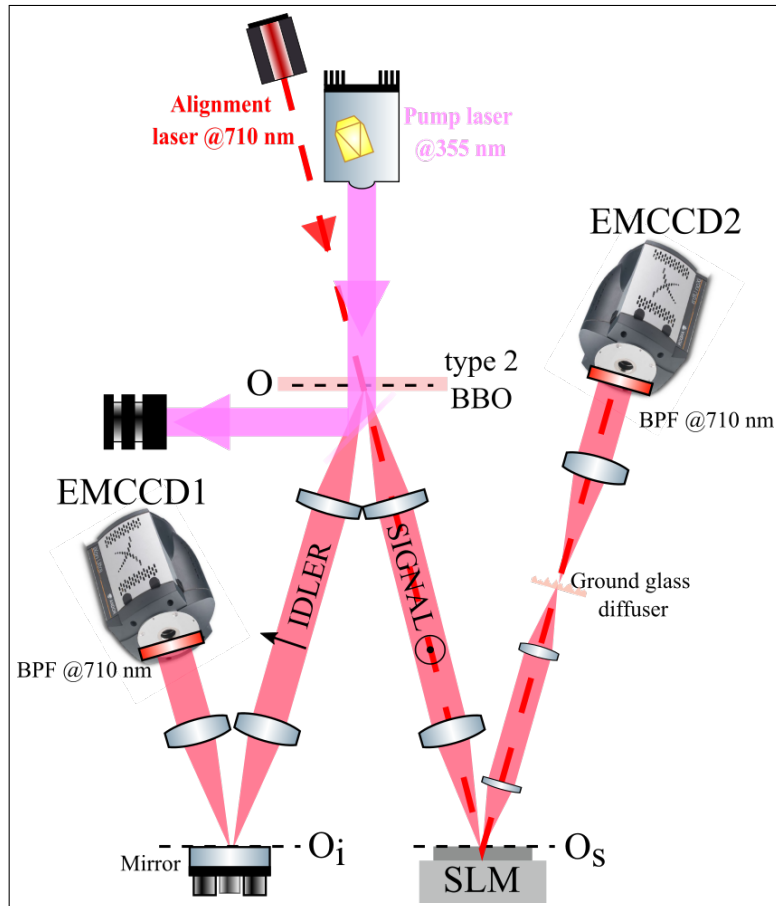


FIG. 1: Experimental setup.

## II. EXPERIMENTS

Fig. 1 shows the experimental setup. Strongly spatially multi-mode twin beams (i.e. a high-dimensional biphoton state) are generated in a non-colinear type-II geometry using spontaneous parametric down conversion (SPDC) in a 0.8 mm long  $\beta$ -barium borate ( $\beta$ -BBO) crystal pumped at 355 nm. The pump pulses are provided by a passively Q-switched Nd:YAG laser (330 ps FWHM, i.e. full width at half maximum, pulse duration, 27 mW mean power and 1 kHz repetition rate). Because of the non-colinear interaction, the SPDC twin beams are separated and propagate through two different telescope systems imaging the near-field  $O$  of the crystal in planes  $O_s$  and  $O_i$  for the signal and idler channels. For the signal, which is vertically polarized, the image plane  $O_s$  is first conjugated with the SLM (Hamamatsu LCOS-SLM X10468-07). Then, the SLM plane is imaged on a ground glass diffuser (i.e. the thin scattering medium of 1 mm thickness, 3  $\mu\text{m}$  roughness and 125  $\mu\text{m}$  average waviness profiles [4]) with a second telescope system. All telescope systems have a magnification of -1. Finally, in order to measure momentum correlations, far-field (FF) images of the two SPDC beams are formed with  $2f$  imaging systems on two separate Electron Multiplying Charge Coupled Devices (EMCCD, ANDOR iXon Ultra 897), used in photon-counting regime [9]. Before detection, the photons pairs emitted around the degeneracy are selected by band-pass filters (BPF) centered at 710 nm (3 nm FWHM).

First, momentum correlations are measured between FF images of twin SPDC beams without the thin diffuser and the SLM turned off. In the signal and idler images (figures 2a and 2b), the mean number of photon is adjusted to about 0.15 photon/pixel in order to optimize the efficiency of EMCCDs operating in photon-counting regime [9]. Fig. 2c shows the highly contrasted normalised momentum correlation peak which is obtained by averaging the measurements on a set of 500 twin images. The standard deviations (in spatial frequency unit) of the narrow correlation peak along both axes are  $\sigma_{\nu_x} = 0.89 \pm 0.03 \text{ mm}^{-1}$  and  $\sigma_{\nu_y} = 0.80 \pm 0.03 \text{ mm}^{-1}$  and its integral, corresponding to the detection rate of photons by pairs [10], is about 23%. From this rate, which is in a good agreement with the quantum efficiency of the whole imaging systems [11], we can estimate at more than 4000 the number of photons detected by pairs in a single acquisition of twin images.

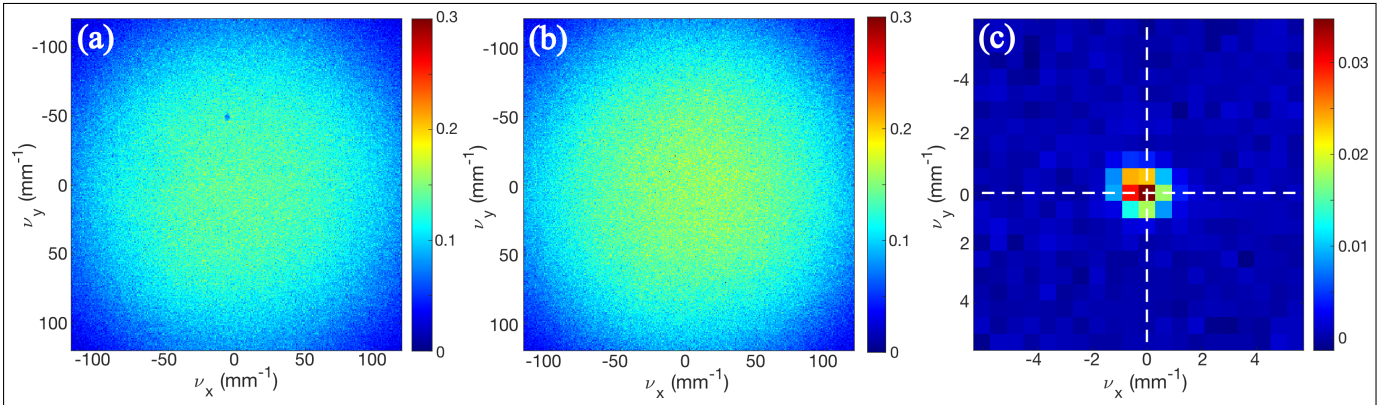


FIG. 2: Spatial distribution of the mean number of photon per pixel in far-field images of the (a) idler and (b) signal SPDC beams. (c) Normalised momentum correlation peak obtained by averaging measurements on a set of 500 twin images.

Even if the biphoton wavefunction is naturally a doubly continuous variable both in momentum and position domains, its Schmidt decomposition is always discrete [12]. Working in the monochromatic limit, we assume that the biphoton spatial state is Gaussian : the biphoton amplitude in momentum domain is defined by the transverse momentum profile of the Gaussian pump beam and Gaussian approximation of the phase-matching condition [12]. In that case, we can estimate the SPDC mode number, which is identical to the Schmidt number [12–14], as follows:

$$K = \frac{A_{pump}\Omega_{SPDC}}{\lambda_{SPDC}^2}, \quad (1)$$

where  $A_{pump}$  is the near-field (NF) area of the pump beam (i.e. the area of the NF SPDC beam) and  $\Omega_{SPDC}$  the FF solid angle of SPDC (i.e.  $\Omega_{SPDC}/\lambda_{SPDC}^2$  corresponds to the area of the SPDC beam given in spatial frequency units). From the FF and NF images of SPDC (Fig. 2a and Fig. 3b), we measure the standard deviations ( $\sigma_{\nu_x}^{SPDC} = 38.8 \pm 0.1$  mm<sup>-1</sup>,  $\sigma_{\nu_y}^{SPDC} = 37.0 \pm 0.1$  mm<sup>-1</sup>) and ( $\sigma_x^{SPDC} = 0.707 \pm 0.002$  mm,  $\sigma_y^{SPDC} = 0.796 \pm 0.002$  mm) in the momentum and position domains, respectively. It leads to an estimated Schmidt number  $K = \pi^2 \sigma_x^{SPDC} \sigma_y^{SPDC} \sigma_{\nu_x}^{SPDC} \sigma_{\nu_y}^{SPDC} \simeq 8000$ . On the other hand, the narrowness of the correlation peak (Fig. 2c) also demonstrates the high dimensionality of the biphoton state and the accuracy of its measurement. From the standard deviation of the momentum correlation peak we have also estimated the Schmidt number by dividing the area of the FF SPDC beam by the area of the correlation peak  $N = (\sigma_{\nu_x}^{SPDC} \sigma_{\nu_y}^{SPDC}) / (\sigma_x \sigma_y) \simeq 2000$  which is smaller than  $K \simeq 8000$  calculated previously, but in the same order of magnitude. This discrepancy can be easily explained by geometric aberrations and residual defocusing of the telescope systems that increase the uncertainties on the measurement of the joint momentum probability and, consequently, the standard deviation of the correlation peak. Although the Schmidt number estimated with Eq. 1 is probably overestimated because the pump beam is not perfectly Fourier transform, we can claim that a biphoton state with a Schmidt number of a few thousand is involved in this experiment.

A laser used for alignment (Fig. 1) is also used in these experiments as a coherent light source to measure the TM of the complex medium using the phase-shifting interferometry measurement method proposed in [15, 16]. Fig. 3 shows the NF image of the signal channel where the crystal, the SLM and the thin diffuser planes are conjugated through the telescope systems (Fig. 1). Fig. 3a is obtained when the crystal is illuminated with the alignment laser and when a phase mask is addressed on the SLM. Fig. 3b corresponds to the NF image of the signal SPDC beam. In both figures the white dotted circle denotes the circular mount of the BBO crystal, the green dotted square denotes the  $256 \times 256$  pixels phase mask addressed on the SLM and the red dotted ellipse denotes the NF location and the size of the SPDC beam with respect to the phase mask.

In the first instance, the TM of the thin scattering medium is measured between a region of interest (ROI) of  $256 \times 256$  pixels in the SLM plane (Fig. 3a) and a ROI of  $100 \times 100$  pixels (corresponding to an area of  $60 \times 60$  mm<sup>-2</sup> in spatial frequency unit) in the FF plane imaged on the EMCCD1 that contains the entire speckle pattern observed when the alignment laser is transmitted through the ground glass diffuser (Fig. 4e). We emphasize at this point that the ROI of  $100 \times 100$  pixels defined on EMCCD1 corresponds to an area which is much smaller than the whole etendue of the SPDC beams (Fig. 2a).

Following the method proposed in [16], we display a basis of orthogonal patterns (i.e. Hadamard matrices) on the SLM and we measure the output field using phase-shifting holography. To optimize the size of the TM, the pixels of the SLM are binned  $4 \times 4$  in order to address the SLM with phase masks of  $64 \times 64$  macropixels fitting the size of the

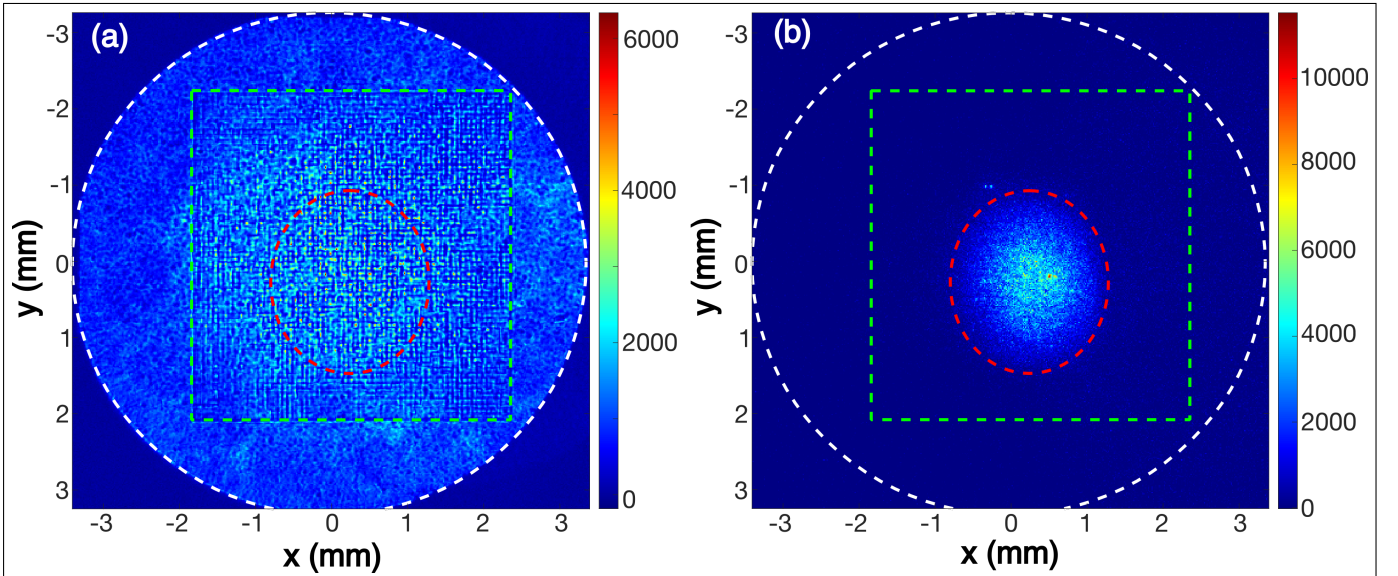


FIG. 3: Near-field images graded in grayscale of the signal channel where the image planes of the crystal, the SLM and the ground glass diffuser are conjugated, (a) when the crystal is illuminated with the alignment laser, (b) when SPDC is emitted from the crystal. Dotted white circles, green squares and red ellipses denote the sizes and positions of the crystal circular mount, the phase mask addressed on the SLM and the SPDC beam, respectively.

SPDC NF spatial modes. Given the pixel size of ROIs defined on the SLM and EMCCD1, the size of the TM to be measured is  $100^2 \times 64^2$ . The impact of the number of pixels addressed on the SLM has of course consequences on the correction quality of the aberrations introduced by the ground glass diffuser. The increase in the number of pixels certainly improves the resolution of the transmission matrix but it significantly increases the number of patterns to address on the SLM and therefore the acquisition time for the measurement of the TM. Conversely, reducing the number of pixels addressed on the SLM significantly reduces the acquisition time but at the expense of the resolution of the transmission matrix and therefore the quality of the recovery of momentum correlations. By matching the size of the macropixels on the SLM to the size of the SPDC NF spatial modes, we propose the best compromise.

Once the TM has been measured, different phase masks are calculated in order to retrieve and manipulate the FF focusing of the laser beam through the thin diffuser. To that end, we compute from the TM the masks that perform a phase conjugation operation [16], i.e. that put in phase all the contributions from the SLM macropixels at a single or multiple localized targets in the camera plane. In Fig. 4 we show the experimental results. The first row corresponds to the different phase masks (in radians) addressed on the SLM and the second row gives the corresponding FF image (in grayscale) of the laser intensity. We emphasize here that the alignment laser is not used in single-photon regime. The first column corresponds to the results obtained when no phase mask is addressed. In that case, the laser FF image exhibits a broad speckle pattern due to the ground glass diffuser (Fig. 4e). Figures 4b and 4c show the phase masks designed to target the FF focusing of the alignment laser at the center and at the coordinates  $(\nu_x = +3 \text{ mm}^{-1}, \nu_y = -3 \text{ mm}^{-1})$  of the  $100 \times 100$  pixels ROI on EMCCD1 (figures 4f and 4g). The last phase mask (Fig. 4d) is designed to focus the laser through the scattering medium in two spots (Fig. 4h). The third row shows the normalised momentum correlation patterns between the entangled photons obtained when the same phase masks are successively addressed on the SLM. Like in [4], a low-contrast two-photon speckle pattern is observed (Fig. 4i) when one photon of the biphoton state is transmitted through the thin diffuser and when the SLM is switched off. When one of the phase masks is addressed, the narrow momentum correlation peak is retrieved at the same location targeted with the alignment laser (figures 4j to 4l). We emphasize that the phase masks used to manipulate the momentum entanglement of the biphoton state are calculated from the TM measured with the alignment laser to target its focusing. Moreover, since the TM is measured between an area on the SLM ( $256 \times 256$  pixels) larger than the NF SPDC beam (Fig. 3b), and an area on EMCCD1 ( $100 \times 100$  pixels) much smaller than the FF signal SPDC beam (Fig. 2b), the momentum correlations are calculated on the whole transverse section of the FF SPDC twin beams. All momentum correlation patterns are obtained by averaging the measurements on 500 pairs of twin images. In figures 4j and 4k the standard deviations of the correlation peaks are about  $1.0 \pm 0.1 \text{ mm}^{-1}$  along the  $x$  and  $y$  axes, which is very close to the result obtain without scattering medium (Fig. 2c). In [17] we have demonstrated that a pure phase object, even random, (i.e. a ground glass plate) lying in the NF or in the FF of a biphoton state does not change the respective position or momentum correlation distributions. Consequently, because



in our experiment the SLM and the scattering medium are conjugated with the NF of the SPDC signal beam, we can assume that entanglement in position of the biphoton state is not affected by the pure random phase of the ground glass plate and the pure phase addressed on the SLM and that high-dimensional momentum entanglement of the biphoton state is retrieved with a good accuracy and a good signal-to-noise ratio. We point out that detection rate of photons by pairs falls down to 5% because of additional losses induced by the transmission through the ground glass plate and by the low numerical aperture of the imaging system which does not allow efficient collection of the high diffraction orders produced by the small SLM pixels. Finally, with the phase mask depicted in Fig. 4d, we obtained two narrow correlation peaks (Fig. 4l) with amplitudes half of the correlation peak amplitude in Fig. 4i.

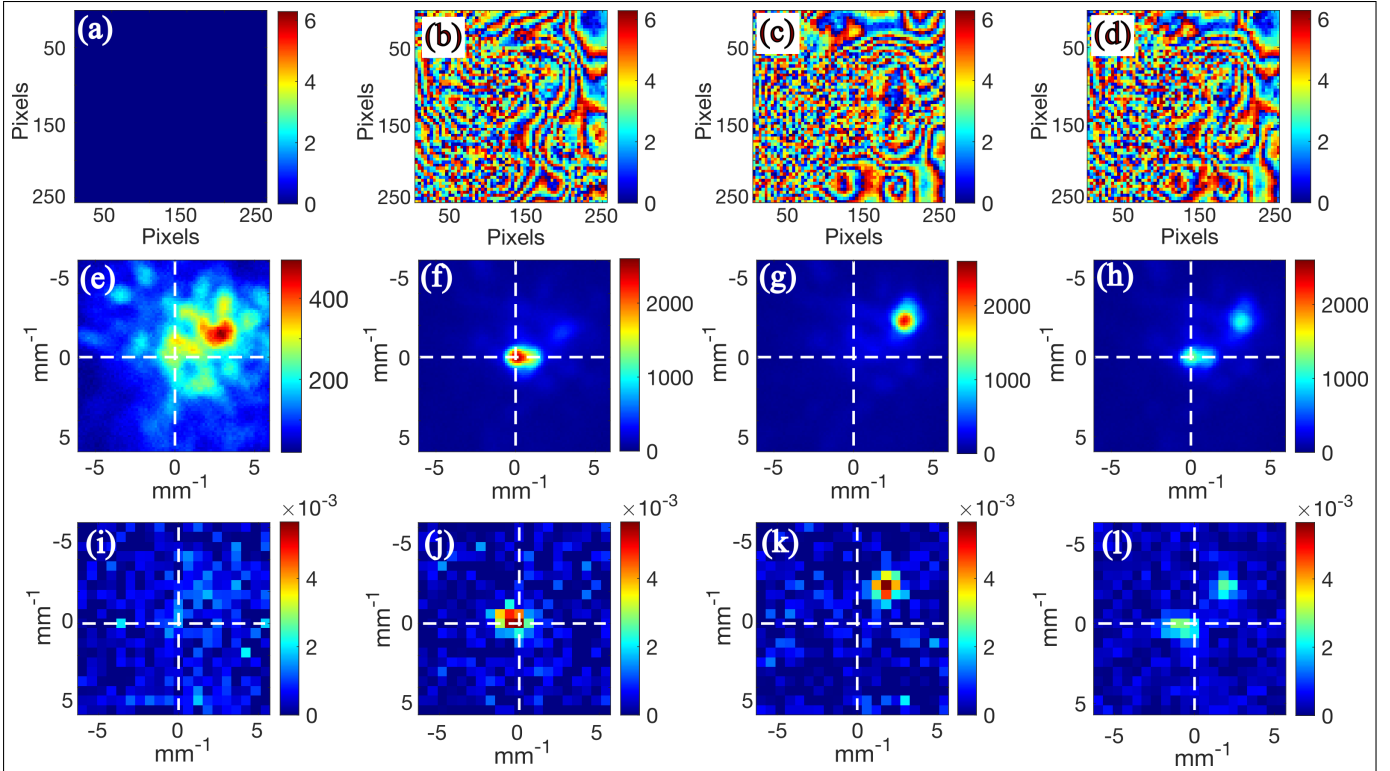


FIG. 4: Experimental results. (b) to (d):  $256 \times 256$  pixels phase masks in radians calculated and addressed on the SLM to control the far-field focusing of the alignment laser through the ground glass diffuser (f to h) and to manipulate in the same way the momentum correlations of the biphoton state (j to l). With the SLM off (a), (e) and (i) show the one-photon and the two-photon speckle patterns observed when the alignment laser or the biphoton state are transmitted through the thin scattering medium, respectively.

### III. CONCLUSION

We have presented a method allowing the manipulation of a spatially very high dimensional biphoton state transmitted through a complex medium when only one photon of the pair is transmitted through it. The unscrambling of a few thousand dimensional entangled quantum state is evidenced by manipulating with a spatial light modulator the only photon that propagates through the medium where the used phase masks have been firstly designed to control and manipulate the focusing of a laser source through the same medium. Although we have used a SLM and the phase-shifting interferometry method with coherent light to measure the TM of the time-stationary thin scattering medium, other methods using faster SLM devices such as a deformable mirror or MEMS-SLM [18] and iterative [6, 19] or genetic [18] feedback algorithms can also be considered, opening the possibility to control in real time the spatial high dimensional entanglement of a quantum state transmitted through a more realistic dynamic complex medium such as turbulent atmosphere or biological tissues.

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## Disclosures

The authors declare no conflicts of interest. The authors state that the article contains no studies involving human or animal participants.

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