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Oort cloud (exo)planets

Sean N. Raymond ¹ ★ Andre Izidoro ² and Nathan A. Kaib^{4,5}

- ¹Laboratoire d'Astrophysique de Bordeaux, CNRS and Université de Bordeaux, Allée Geoffroy St. Hilaire, F-33165 Pessac, France
- ²Department of Physics and Astronomy, Rice University, 6100 Main MS-550, Houston, TX 77005, USA
- ³Department of Earth, Environmental and Planetary Sciences, Rice University, MS 126, Houston, TX 77005, USA
- ⁴HL Dodge Department of Physics and Astronomy, University of Oklahoma, Norman, OK 73019, USA

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ABSTRACT

Dynamical instabilities among giant planets are thought to be nearly ubiquitous and culminate in the ejection of one or more planets into interstellar space. Here, we perform N-body simulations of dynamical instabilities while accounting for torques from the galactic tidal field. We find that a fraction of planets that would otherwise have been ejected are instead trapped on very wide orbits analogous to those of Oort cloud comets. The fraction of ejected planets that are trapped ranges from 1 to $10 \, \mathrm{per}$ cent, depending on the initial planetary mass distribution. The local galactic density has a modest effect on the trapping efficiency and the orbital radii of trapped planets. The majority of Oort cloud planets survive for Gyr time-scales. Taking into account the demographics of exoplanets, we estimate that one in every 200– $3000 \, \mathrm{stars}$ could host an Oort cloud planet. This value is likely an overestimate, as we do not account for instabilities that take place at early enough times to be affected by their host stars' birth cluster or planet stripping from passing stars. If the Solar system's dynamical instability happened after birth cluster dissolution, there is a ~ 7 per cent chance that an ice giant was captured in the Sun's Oort cloud.

Key words: Oort Cloud – planets and satellites: detection – planets and satellites: dynamical evolution and stability.

1 INTRODUCTION

* E-mail: rayray.sean@gmail.com

The 'planet-planet scattering' model is the leading hypothesis to explain the broad eccentricity distribution of giant exoplanets (Butler et al. 2006; Udry et al. 2007). The model proposes that systems of gas giants undergo dynamical instabilities that frequently eject planets into interstellar space; the eccentric orbits of surviving planets are scars from these violent events (Rasio & Ford 1996; Weidenschilling & Marzari 1996; Lin & Ida 1997; Adams & Laughlin 2003; Chatterjee et al. 2008; Jurić & Tremaine 2008; Raymond, Armitage & Gorelick 2010). This model can also explain other observed features of giant exoplanet systems, such as their dynamical spacing and secular architectures (e.g. Raymond et al. 2009; Timpe et al. 2013; Bitsch & Izidoro 2023).

The Solar system is also thought to have undergone a dynamical instability early in its history, albeit a relatively mild one (Tsiganis et al. 2005; Morbidelli et al. 2007). There is abundant (circumstantial) evidence to support this, from the distributions of small body populations and the giant planets' orbital architectures (see Nesvorný 2018). During the instability, one or two extra ice giants may have been ejected (Batygin, Brown & Betts 2012; Nesvorný & Morbidelli 2012).

Previous work on dynamical instabilities has rarely taken into account the external Galactic environment. Stars are born in clusters (e.g. Adams 2010) and after clusters disperse stars remain in loose dynamical contact with other stars while orbiting within the Galaxy's gravitational field (Oort 1950). It is vital to account for

the Galactic tidal field (specifically the component that results from the density gradient perpendicular to the Galactic disc) to model the origin and dynamics of Oort cloud comets, a fraction of which is trapped on wide orbits due to torques from the Galactic tide or from passing stars (Heisler & Tremaine 1986; Duncan, Quinn & Tremaine 1987; Wiegert & Tremaine 1999; Kaib & Quinn 2008). These external factors also affect the fates of scattered planets.

Here, we show that many planets that would have been considered 'ejected' in previous work are actually trapped on Oort cloud-like orbits with orbital radii of tens of thousands of au. We quantify the importance of the Galactic tidal field and estimate the frequency of Oort cloud exoplanets.

2 SIMULATIONS

2.1 Code and initial conditions

Our simulations capture the dynamics of unstable planetary systems while taking into account the Galactic tidal field. We modified the MERCURY integrator (Chambers 1999) to include the galactic tide, using the same methodology as previous studies (Heisler & Tremaine 1986; Wiegert & Tremaine 1999; Levison, Dones & Duncan 2001; Kaib & Quinn 2008). The calculation is done in Cartesian galactic coordinates $(\tilde{x}, \tilde{y}, \tilde{z})$, where \tilde{x} points away from the Galactic centre, \tilde{y} points in the direction of Galactic rotation, and \tilde{z} points toward the Galactic South Pole. The resulting force can be expressed as

$$F_{\text{tide}} = (A - B)(3A + B)\tilde{x}\hat{x} - (A - B)^2 \tilde{y}\hat{y}$$
$$- (4\pi G\rho_0 - 2 * (B^2 - A^2))\tilde{z}\hat{z}, \tag{1}$$

⁵Planetary Science Institute, 1700 E. Fort Lowell, Suite 106, Tucson, AZ 85719, USA

where $A=14.82\,\mathrm{km\,s^{-1}\,kpc^{-1}}$ and $B=12.37\,\mathrm{km\,s^{-1}\,kpc^{-1}}$ are Oort's constants, and ρ_0 is the local Galactic density which we set to $0.15\,\mathrm{M}_\odot$ pc⁻³ for our fiducial set of simulations (following Tremaine 1993), and test the effect of varying ρ_0 in Section 2.4. We assumed a constant angle of 60.2° between the ecliptic and Galactic planes, following Kaib & Quinn (2008). The galactic distribution of inclinations should be uniform in $\cos(i)$, such that the Solar system value is almost exactly the median. The galactic torque scales as $\sin(i)^2$, so systems with larger inclinations will experience modestly stronger torquing. In practice, the galactic torque will affect all systems to some degree, even those in which the planets' initial plane is aligned with the galactic disc, because planet–planet scattering itself generates significant mutual inclinations (e.g. Chatterjee et al. 2008; Jurić & Tremaine 2008).

We performed four sets of simulations with different planet masses, chosen because previous work demonstrated that they are compatible with the known giant exoplanet population (Raymond et al. 2008, 2009, 2010, 2011, 2012). The mass distributions are as follows:

- (i) The *mixed1* set: Each system contains three planets with masses drawn from a $dN/dM \propto M^{-1.1}$ distribution (Butler et al. 2006; Udry et al. 2007) between one Saturn mass and three Jupiter masses.
- (ii) The *mixed2* set: Each system started with four planets drawn from a $dN/dM \propto M^{-1.1}$ distribution between $10\,{\rm M}_\oplus$ and $3\,M_{\rm Jup}$.
- (iii) The *equal-mass* set: Three equal-mass planets of one Saturn mass, one Jupiter mass, and four Jupiter masses.
- (iv) The 'Solar system-like' set mimics the Solar system's giant planet instability. Each simulation started with Jupiter, Saturn, and three ice giants (assuming one was ejected; see Nesvorný & Morbidelli 2012) and an outer disc containing 270 planetesimal particles (that interacted gravitationally with the planets but not with each other) totalling $20\,M_\oplus$.

Our systems were designed to be immediately unstable but start from a plausible orbital configuration. For the mixed1, mixed2, and equal-mass sets, the innermost planet was placed at 5 au. The orbital semimajor axis of each subsequent planet was randomly chosen to correspond to the location of the 3:4, 3:5, 2:3, or 1:2 with its inner neighbour (although other orbital angles were not chosen to favour resonance). The orbital eccentricities of the inner and outer planets were randomly chosen below 0.01, but the eccentricity of the middle planet (or, for the mixed2 set, either the second or third planet) was chosen that at periastron it crossed the orbit of the inner planet, ensuring an immediate dynamical instability. For the Solar systemlike set, the giant planets were placed in a multiresonant configuration that represents a plausibly pre-instability configuration (Nesvorný & Morbidelli 2012; Pierens et al. 2014; Clement et al. 2021) with Jupiter at 5.35 au, Saturn in 2:3 resonance at 7.496 au, an additional 15 M_⊕ ice giant in 2:3 resonance with Saturn at 9.9 au, Uranus in 1:2 resonance with the extra ice giant at 15.7 au, and Neptune in 2:3 resonance with Uranus at 20.5 au. Unlike the other sets of simulations, the planets started on near-circular orbits. The starting inclinations of all planets were randomly chosen between zero and 1°.

Each simulation was integrated for 100–200 Myr using a modified version of MERCURY's hybrid integrator (Chambers 1999). We increased the size of the central (solar mass) star to 0.4 au because tests showed that our chosen time-step of 10 d accurately resolves approaches as close as this without accumulating errors in energy (see appendix A in Raymond et al. 2011). A planet was considered ejected if it reached the Sun's 'tidal radius' of 170 000 au, which scales

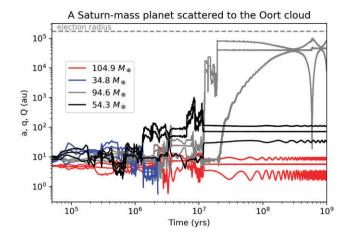


Figure 1. An example simulation from the *mixed2* set in which a roughly Saturn-mass planet was trapped on a very wide orbit. Each planet's semimajor axis a, perihelion distance q, and aphelion distance Q are shown. The dashed line shows the ejection radius at 170 000 au.

with the Galactic density and therefore the strength of the Galactic tide (Tremaine 1993; Wyatt et al. 2017, see Section 2.4).

2.2 An example simulation

Fig. 1 shows a planet being trapped in its star's Oort cloud. This system (from the *mixed2* set) started with four planets, with masses - in order of increasing orbital distance - of 104.9, 34.8, 94.6, and $54.3 \,\mathrm{M}_{\oplus}$. The dynamical instability led to close encounters between the planets, scattering each other to higher eccentricities such that the lowest mass planet collides with the central star at $t \sim 2.3$ Myr. At $\sim \! 10 \, \text{Myr}$, the $94.6 \, M_{\oplus}$ planet was repeatedly scattered by the more massive inner planet to a semimajor axis of ~40 000 au. During the same phase of instability, the 54.3 M_{\oplus} was scattered out to an orbital radius close to 100 au. Over a span of \sim 100 Myr, the Galactic tide acted to decrease the $94.6\,M_{\oplus}$ planet's orbital eccentricity, lifting its periastron distance and decoupling it from perturbations from the other planets. At the end of the simulation, the three surviving planets had semimajor axes of 5.6, 71, and 39 153 au, eccentricities of 0.62, 0.53, and 0.27, and inclinations with respect to their starting plane of 65.7° , 8.6° , and 71.7° , respectively. The two inner planets continued to undergo Lidov-Kozai-like oscillations in eccentricity and inclination on time-scales of a few tens of Myr, but the outer planet was mostly decoupled.

2.3 Results from the ensemble of simulations

Fig. 2 shows the final orbital distribution of the planets in all of our fiducial sets of simulations. Each set shows the same general pattern with three key features. First, planets inside $10-20\,\mathrm{au}$ have a broad distribution of orbital eccentricities. These are the survivors of planet–planet scattering that provide analogues to the observed giant exoplanets and our simulations adequately reproduce the observed eccentricity distribution (Raymond et al. 2010). Secondly, there is a long tail of scattered planets that extends from the inner region out to ever-larger semimajor axes, with eccentricities that asymptotically approach unity. These are the planets that are in the process of being ejected, as they continue to undergo close approaches when they cross the orbits of other planets at periastron. Thirdly, there is a tail of planets with semimajor axes larger than $\sim 10^4\,\mathrm{au}$ with eccentricities below 1. These are Oort cloud planets; they followed

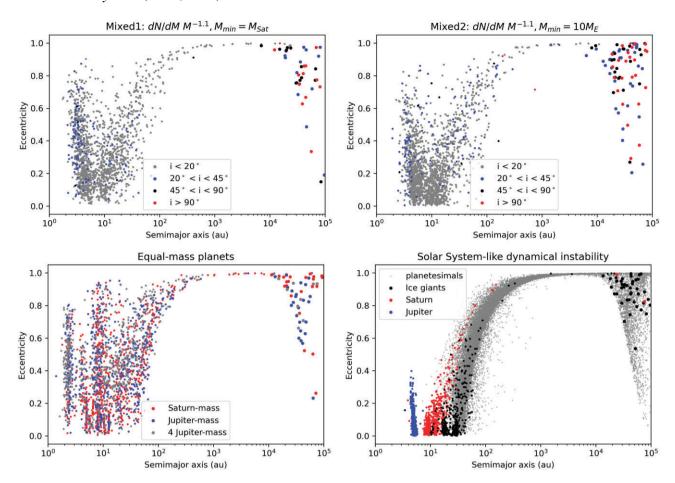


Figure 2. Final distributions of the planets' orbits in our fiducial sets of simulations. In the mixed1 and mixed2 sets (top panels), the colour corresponds to the final inclination of each planet's orbit with respect to the starting plane. In the 'equal-mass' planets set (bottom left), the colour corresponds to the planet mass; note that in each simulation all three planets were the same mass. In the 'Solar system-like' set, the colour corresponds to the planet and the small grey dots represent planetesimal particles. In all panels, Oort cloud planets particles are larger.

the ejection track with eccentricities approaching 1, but torques from the Galactic tide decreased their eccentricities sufficiently to lift their periastron distances outside of the realm of surviving planets (as in the simulation from Fig. 1). This is analogous to how the Sun's Oort cloud was populated (Heisler & Tremaine 1986; Duncan et al. 1987; Fernández 1997; Brasser & Morbidelli 2013; Dones et al. 2015).

The inclinations of surviving planets at Jupiter- to Saturn-like distances tend to have modest inclinations, typically below 20° but with a tail extending up to $\sim 45^{\circ}$ (see top two panels in Fig. 2). Planets scattered out to very wide orbits on the pathway to ejection tend to maintain similar, modest inclinations. However, planets captured into their stars' Oort clouds have very broad inclination distributions, with a large fraction of planets on retrograde orbits. This is, again, similar to the case of Oort cloud comets, whose inclinations are isotropically distributed with respect to the ecliptic (e.g. Dones et al. 2015).

We define Oort cloud planets in our simulations as those with semimajor axes larger than 10³ au and periastron distances larger than 10^2 au. Our simulations show a trend toward a higher rate of planets trapped in the Oort cloud for lower mass planetary systems. Among simulations with equal-mass planets there was a rough mass trend, with the most massive planets producing fewer Oort cloud planets: planets were trapped in the Oort cloud in 4.6 per cent, 4.8 per cent, and 1.8 per cent of simulations with Saturn-mass, Jupiter-mass, and four Jupiter-mass planets, respectively. This trend is likely due to the fact that higher mass planets undergo a smaller number of (stronger) gravitational encounters before ejection (Raymond et al. 2010), thus producing a random walk in orbital energy with larger steps than for lower mass planets. The fraction of simulations that produced a planet in the Oort cloud was 4 per cent for the mixed1 set and 8.1 per cent for the *mixed2* simulations.

The most efficient population of the Oort cloud appears to happen when lower mass (~Neptune-mass) planets are scattered by Saturnto Jupiter-mass planets. This outcome is consistent with previous models of Oort cloud formation that varied the masses of the Sun's planets (Lewis, Quinn & Kaib 2013) and also with trapping of scattered planets in cluster environments (Izidoro et al. 2023). Solar system-like instabilities produced the highest overall rate of Oort cloud planets, with 9 per cent of simulations trapping a planet in the Oort cloud. This includes two systems in which Saturn was scattered by Jupiter and ended up trapped in the Oort cloud. Such an outcome is not consistent with Solar system's dynamical evolution. If we restrict ourselves to systems that are broadly consistent with the Solar system's present-day architecture (by requiring a final eccentricity lower than 0.1 for Jupiter), an ice giant was trapped in the Oort cloud in 7 per cent of simulations.

Oort cloud planets tend to be lower in mass than their surviving counterparts. When dynamical instabilities take place in systems with mixed planet masses, lower mass planets are more commonly ejected - and when they survive, they tend to have higher eccentricities (Jurić & Tremaine 2008; Raymond et al. 2010). The median mass

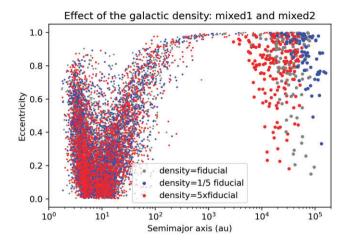


Figure 3. Final distribution of wide-orbit planets in the *mixed1* and *mixed2* sets of simulations, including those with higher or lower galactic densities. It is clear that a higher galactic density correlates with trapping scattered planets on closer orbits.

of surviving planets interior to 10 au in the *mixed1* set is $1.76\,M_{\rm J}$, but the median mass of Oort cloud planets in those simulations is $0.63\,M_{\rm J}$. In the *mixed2* set this difference is even more striking, as the median mass of surviving inner planets is $0.9\,M_{\rm J}$ but the median mass of Oort cloud planets is $0.092\,M_{\rm J}\approx 30\,M_{\oplus}$. Given that the exoplanet occurrence rate increases sharply for lower mass planets, including past the snow line (Suzuki et al. 2016), we expect the population of Oort cloud planets to be dominated by low-mass planets. We return to this issue in Section 3.1.

2.4 Effect of the local Galactic density

The local Galactic density is a central key factor controlling the capture of planets in the Oort cloud. A star's tidal radius $R_{\rm tide}$ – beyond which an object is no longer bound to its star – can be written as (Tremaine 1993; Wyatt et al. 2017)

$$R_{\rm tide} \approx 1.7 \times 10^5 \, {\rm au} \, \left(\frac{M_{\star}}{\rm M_{\odot}}\right)^{1/3} \rho_0^{-1/3},$$
 (2)

where M_{\star} is the stellar mass. We performed 1000 additional simulations of the *mixed1* and *mixed2* sets, varying the local Galactic density ρ_0 by a factor of 5 and 1/5. This corresponds to a radial shift of 1.6 scale lengths (the radial scale length of the Galaxy is debated, with estimates ranging from 1 to 5 kpc; see Amôres, Robin & Reylé 2017, and references therein). For an increase in ρ_0 by a factor of 5, $R_{\rm tide} = 99\,400$ au and for a decrease in ρ_0 by a factor of 5, $R_{\rm tide} \approx 290\,000$ au. We set these values as ejection radii in running additional simulations, while simultaneously increasing the strength of the galactic torque acting on the planets (see equation 1).

For a higher Galactic density, planets are trapped on closer orbits and at a higher rate than for lower Galactic densities. Fig. 3 shows the outcome of our planet–planet scattering simulations for different values of ρ_0 . For ρ_0 of 1/5, 1, and 5 times the fiducial value, the median orbital radius of Oort cloud planets were 60 700, 34 300, and 18 700 au, respectively. A planet was trapped in the Oort cloud in 4.2 per cent of simulations with $\rho_0=\rho_{\rm fid}$, 6.1 per cent of simulations with $\rho_0=\rho_{\rm fid}$, and 8.5 per cent of simulations with $\rho_0=5\rho_{\rm fid}$. These values include both the *mixed1* and *mixed2* sets of simulations; the single highest trapping efficiency was for the *mixed2* set with $\rho_0=5\rho_{\rm fid}$, in which 9.8 per cent of simulations produced an Oort cloud planet.

These trends are a consequence of the Galactic tide. For a higher local Galactic density, the Galactic tidal force can influence planets' orbits closer to their host stars and therefore lift their perihelia and trap them on smaller orbital radii. While the tidal radius is smaller for a high Galactic density, the stronger tidal force traps a larger fraction of planets than in lower Galactic density. However, while we do not model their long-term evolution, we suspect that planets formed in higher Galactic densities may be shorter lived because they will undergo faster periastron cycling and be subjected to stronger stellar encounters. This would go in the direction of balancing the long-term frequencies of Oort cloud planets across the Galaxy.

3 DISCUSSION

3.1 Comparison with previous work

Portegies Zwart (2021) simulated the scattering of planetesimals and planets orbiting stars with a range of masses on different orbits within the Galaxy and with corresponding temporal variations of the tidal radius. Their planetary systems were similar to our equal-mass sets of simulations, as they included planets with near-equal masses (with an 'oligarchic' layout), although their systems were at 10-100 au. Portegies Zwart (2021) found a typical capture rate of Oort cloud planets of \sim 2 per cent. While this is lower than that in most of our sets of simulations, it is a decent match to the set with equal-mass planets of $4\,M_{\rm J}$, which is close to the median planet mass in Portegies Zwart (2021). We interpret this as confirmation that our results are broadly realistic despite our simplified implementation of a fixed tidal radius.

3.2 Long-term survival and dynamics of Oort cloud planets

The population of Oort cloud planets only declines very slowly in time. Our fiducial runs simulated the main phase of capture of planets within the Oort cloud, but not their long-term survival. We addressed this question in two steps. We first ran all mixed1 and mixed2 simulations to 500 Myr. The mixed1 set contained 40 Oort cloud planets at 100 Myr; it lost 11 (27.5 per cent) of its Oort cloud planets between 100 and 500 Myr, but gained 10 new ones. The mixed2 set contained 81 Oort cloud planets at 200 Myr; it lost 13 (16 per cent) between 200 and 500 Myr, but gained 8 new ones. Next, we selected all of the mixed1 and mixed2 simulations with Oort cloud planets at 500 Myr and ran them out to 1 Gyr. Combining both sets, 81 out of 114 Oort cloud planets (71 per cent) survived. This is an underestimate because these simulations did not allow for the capture of planets in the process of being ejected (from what Portegies Zwart 2021 calls the 'Oort cloud conveyor belt').

In our long-term simulations, Oort cloud planets were lost mainly because the same torquing that decreases the eccentricities of wide-orbit planets (to trap them in the Oort cloud) acts to make their eccentricities increase again, bringing them back into dynamical contact with the inner planetary system (as for wide binary stars; Kaib, Raymond & Duncan 2013). This happened to the Oort cloud planet from Fig. 1 after $\sim\!600\,\mathrm{Myr}$; while the planet's orbit remained within the Oort cloud, it received a visible energy kick and corresponding bump in its semimajor axis. The time-scale for this torquing depends mainly on the planet's orbital radius and inclination, and is typically between 0.1 and several Gyr. This second- (or third-) generation scattering can lead to the planet's ejection. In nature, this torquing is unlikely to be as easily repeated as in our simulations, as the phases

of scattered planets can be randomized (e.g. by passing stars and the radial component of the galactic torque) such that torques do not exactly reverse the planet's eccentricity evolution. Of course, passing stars can strip loosely bound Oort cloud planets (e.g. Matese & Whitman 1992) and transform them into free-floating planets like the ones observed via microlensing (Mróz et al. 2017) and direct imaging (Miret-Roig et al. 2022).

3.3 Frequency of Oort cloud planets

To estimate the fraction of stars that may host Oort cloud planets requires two quantities: the occurrence rate of gas giants and the Oort cloud trapping efficiency.

Radial velocity and microlensing surveys find that \sim 10-20 per cent of Sun-like stars host gas giants (e.g Mayor et al. 2011; Clanton & Gaudi 2016; Suzuki et al. 2016), most located at 1-3 au or beyond (Mayor et al. 2011; Fernandes et al. 2019; Lagrange et al. 2023). The occurrence rate of gas giants increases with stellar metallicity (Fischer & Valenti 2005), especially among systems showing strong signs of planet-planet interaction (Dawson & Murray-Clay 2013). The occurrence rate also increases as a strong function of the stellar mass (Johnson et al. 2007).

The trapping frequencies for our different sets of simulations ranged from 1 to 10 per cent. The simulations that most naturally reproduce the exoplanet eccentricity distribution - the mixed1 and mixed2 sets - trapped planets in the Oort cloud in 4-8 per cent of simulations, although matching the observed mass-eccentricity correlation also requires a contribution from equal-mass systems (Raymond et al. 2010), which had trapping efficiencies of 1–5 per cent.

Given the uncertainties in occurrence rates, we assume that 1-10 per cent of all stars host gas giants integrated over all spectral types. Giant planet systems have a mixture of orbital architectures, and our results suggest that roughly 5 per cent of unstable systems will trap a planet in the Oort cloud for the Sun's local density. To match the observed eccentricity distribution, 75-95 per cent of all giant planet systems must be the survivors of instability (Jurić & Tremaine 2008; Raymond et al. 2010). Put together, this implies an Oort cloud planet frequency between 3.75×10^{-4} and 4.75×10^{-3} . This amounts to one Oort cloud planet for every \sim 210–2700 stars. This value only applies to planets within the mass range of our simulations. In real systems, planetary embryos and lower mass planets are frequently ejected, and may outnumber the ejected planets by an order of magnitude or more (Barclay et al. 2017). The rate of Oort cloud Mars-mass or Earth-mass planets may thus be far higher than estimated above.

Our simulations apply to instabilities that take place after the dispersal of the stellar birth cluster, a few to 10 Myr after the start of star and planet formation (e.g. Adams 2010). Instabilities during the cluster phase can trap planets on orbits with radii of hundreds to thousands of au (Izidoro et al. 2023) but the high local density makes it impossible to reach 10^{4-5} au simply because those lie beyond the tidal radius (see equation 2; Tremaine 1993; Wyatt et al. 2017). While the timing of giant planet instabilities is hard to constrain directly, the existence of a rich population of free-floating planets in the upper Scorpius star-forming association hints that many instabilities may indeed happen early (Miret-Roig et al. 2022). Our calculation may therefore overestimate the true abundance of Oort cloud planets. None the less, there is circumstantial evidence that some systems undergo late dynamical instabilities - such as the abundant dust produced in the 1 Gyr-old η Corvi system (e.g. Lisse et al. 2012) – so it appears unavoidable that Oort cloud planets do exist.

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DATA AVAILABILITY

All simulations and analysis code in this paper will be made available upon reasonable request.

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