Supplementary Information

Chemical composition of lithiated nitrodonickelates Li_{3-xy}Ni_xN: evidence of the intermediate valence of nickel ions from ion beam analysis and *ab-initio* calculations.

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S.I. 1: schematic representation of the various LiNiN structural models evaluated in this work.



Figure S1 : schematic representation of the various LiNiN structural models evaluated in this work.

S.I. 2: Cell parameters and Enthalpy of formation for LiNiN ca	lculated in
several prototypes.	

	Cell parameters (Å)		Enthalpy of formation
	а	С	(kJ.mol ⁻¹ .at ⁻¹)
LiNiN (<i>P-6m2</i>)	3.637	3.415	-7.50
LiNiN (<i>P-62m</i>)	7.268 (3.634*2)	3.415	-7.49
LiNiN (<i>P6₃/mmc</i>)	3.632	6.828 (3.41*2)	-7.64
LiNiN (P42/mmc)	3.368	7.557	17.1

S.I.3: Bond Valence Sum analysis of Li_{3-xy}Ni_xN solid solution phases.

The Bond Valence Sum analysis is an empirical method which linked the lengths of bonds formed by an ion to its oxidation state [1]. A fraction of valence is attribute to each bond according to:

$$v.b. = e^{\left(\frac{R_0 - R}{b}\right)} \tag{S1}$$

Were *v*. *b*. is the valence bond fraction, *R* is the bond length, and R_0 and *b* are tabulated values determined. The sum of all the *v*. *b*. attributed to each bond formed by the ion should be close to the expected valence. In this work, we used the tabulated values determined by Gagné recently for nitrides [2]. Thus, R_0 and *B* are 1.611 Å and 0.457 for Ni²⁺-N³⁻ bonds (parameters for lower nickel valence are not available) and for Li⁺-N³⁻ bonds, R_0 and *B* are 1.713 Å and 0.312 respectively. The next figure shows the bond valence evolution versus the bond length for Ni²⁺-N³⁻ and Li⁺-N³⁻ bonds (red curve and black curve respectively). In the 2-fold coordination of the 1b site, a Ni valence greater than 1 (v.b. > 0.5 to 1) is expected to lead to shorter bond lengths than Li⁺.



Figure S2: bond valence vs bond length for $Ni^{2+}-N^{3-}$ (red curve) and $Li^{+}-N^{3-}$ (black curve) bonds.

The c parameter is directly related to these bond lengths: increasing the Ni content leads to a contraction of the cell parameter. According to the BVS method, in 2-fold coordination, the v.b. should be 0.5 for Li⁺ and v.b. 0.75 for Ni^{1.5+}. Thus, the *c* parameter evolution with Ni content might follow the expression:

 $c = 2[(1 - x_{Ni})(1.713 - 0.312ln 0.5) + x_{Ni}(1.611 - 0.457ln 0.75)] = 3.858 - 0.373x_{Ni}$ (S2) Conversely, the *a* parameter increases with increasing Ni content is related to the three Li-N bonds into the P/6mmm Li₃N type structure. The fractional occupation by Li ions of the 2c site is $(1-0.25x_{Ni})$ for a Ni^{1.5+} valence, i.e., $0.5x_{Ni}$ vacancies created in the site of multiplicity 2. According to the crystal structure, the *a* parameter might follow the expression:

$$a = 2\cos\left(\frac{\pi}{6}\right) \times d_{Li-N} = 2\cos\left(\frac{\pi}{6}\right) \times \left(1.713 - 0.312\ln\left((1 - 0.25x_{Ni})/3\right)\right)$$
(S3)

These expected evolutions are plotted in the following figure. Using this empirical approximation, overall evolutions are respected. Main weakness of this reflection lies with the reliability of the tabulated parameters and to the assumption of localized bonds within the structure (i.e., ionic structure), which is completely the case here.



Figure S3: cell parameters evolution expected using Bond Valence approach with Gagné parameters [2].



S.I.4: Phonon dispersion curves for LiNiN within the 4 structures evaluated.

Figure S4: Phonon diagram for LiNiN in the P-6m2 prototype



Figure S5: Phonon diagram for LiNiN in the P-62m prototype



Figure S6: Phonon diagram for LiNiN in the P6₃/mmc prototype



Figure S7: Phonon diagram for LiNiN in the P4₂/mmc prototype





Figure S8: electronic density of states of Li₃N



Figure S9: electronic density of states of Li_{2.76}Ni_{0.16}N



Figure S10: electronic density of states of Li_{2.5}Ni_{0.33}N



Figure S11: electronic density of states of Li_{2.25}Ni_{0.50}N



Figure S12: electronic density of states of Li₂Ni_{0.67}N

References:

[2] Gagné, O.C.; On the crystal chemistry of inorganic nitrides: crystal-chemical parameters, bonding behavior, and opportunities in the exploration of their compositional space, *Chem. Sci.* 2021,**12**, 4599-4622

^[1] Brown, I.D.; Recent developments in the methods and applications of the Bond Valence model, *Chem. Rev.* 2009, 109, 6858–6919