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SPOT: Secure and Privacy-preserving prOximiTy protocol for e-healthcare systems

SOUHA MASMOUDI^{1,2}, NESRINE KAANICHE^{1,2}, AND MARYLINE LAURENT^{1,2}

¹SAMOVAR, Telecom SudParis, Institut Polytechnique de Paris, Evry, France
²Member of the Chair Values and Policies of Personal Information, Institut Mines-Telecom, Paris, France

Corresponding author: Souha Masmoudi (e-mail: souha.masmoudi@telecom-sudparis.eu).

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ABSTRACT This paper introduces SPOT, a Secure and Privacy-preserving prOximity based protocol for e-healthcare systems. It relies on a distributed proxy-based approach to preserve users' privacy and a semi-trusted computing server to ensure data consistency and integrity. The proposed protocol ensures a balance between security, privacy and scalability. As far as we know, in terms of security, SPOT is the first one to prevent malicious users from colluding and generating false positives. In terms of privacy, SPOT supports both anonymity of users being in proximity of infected people and unlinkability of contact information issued by the same user. A concrete construction based on structure-preserving signatures and NIWI proofs is proposed and a detailed security and privacy analysis proves that SPOT is secure under standard assumptions. In terms of scalability, SPOT's procedures and algorithms are implemented to show its efficiency and practical usability with acceptable computation and communication overhead.

INDEX TERMS Anonymity, e-healthcare, NIWI proofs, Privacy, Structure-preserving signature, Unlinkability.

I. INTRODUCTION

The recent health crisis has led governments to apply different tracing solutions to control the contamination chain among the population. These solutions are aimed at sharing valuable data while preserving users' privacy. However, there are still privacy threats and robustness challenges as long as users are required to disclose and share correct sensitive and personal information with different third parties with various levels of trust.

Most of the solutions rely on the Bluetooth technology, namely Bluetooth Low Energy (BLE), to exchange contact information, thanks to its efficiency in active communications [17]. Among these governmental solutions, the TraceTogether application [11] has been launched by Singapore. TraceTogether enables to collect, via the Bluetooth technology, temporary IDs (generated by a central trusted server) of users in close proximity. Collected IDs are stored in an encrypted form using the server's public key, at users' devices, and in case of infection, they are shared with the server. The COVIDSafe application [6] from the Australian government is another Bluetooth-based solution. It also logs infection is detected. The server is required to alert users at risk without revealing the identity of the infected user. Both TraceTogether and COVIDSafe applications are set upon a centralized architecture. Many other applications like Stop COVID-19 (Croatia) [3], CA Notify (California) [1] rely on the Google and Apple Exposure Notification (GAEN) service [5], which is set upon a decentralized architecture. Although contact tracing applications have helped governments to alleviate the widespread of the pandemic by automating the manual contact tracing done by health authorities, they raise critical privacy concerns, namely users tracking and identification [15].

encrypted users' contact information, and share them once an

Academic solutions have been also proposed to support both centralized [13] and decentralized [7], [8], [14], [16], [18] architectures. However, each architecture has his merits and limits in terms of security and privacy. Indeed, using centralized solutions, users guarantee the reception of correct alerts as long as the generation of users' contact tokens and the verification in case of infection are performed by a centralized server. This guarantee is compensated with threats to users' privacy, i.e., users are exposed to tracking and identification of their contact lists. Decentralized solutions have been proposed to mitigate these privacy threats. Users are responsible for generating their contact tokens in order to ensure their privacy and anonymity, but, they are not prevented from forging contact information, which results in high level of false alerts. To get the best of both architectures, hybrid architecture based solutions [9], [12] have been proposed. However, security and privacy requirements, like the correctness of contact information and the anonymity of contacted users, are not yet handled and ensured together.

In this paper, we present SPOT, a novel hybrid Secure and Privacy-preserving prOximity-based protocol for e-healthcare systems. It combines a decentralized proxy front-end architecture, ensuring both users' anonymity and contact information integrity, and a centralized back-end computing server, guaranteeing a real time verification of contact information integrity. SPOT assumes that two users in close proximity rely on their Ephemeral Bluetooth IDentifiers (EBID) to compute a common contact message. This message is relayed to a central server through a group of proxies. With the help of the computing server and relying on a proof-based group signature, SPOT prevents users from forging their contact lists. The signed contact messages are given to the user to be locally stored. In case of a detected infection, the user consents to share his contact list, i.e., a set of signed contact messages, with the health authority. This latter checks the correctness of the received list and shared it back with all the involved users, if the verification holds. The contributions of this paper are summarized as follows:

- we design a proximity protocol for e-health services that prevents the injection of false positives, i.e., alert users to be at risk when they are not. SPOT enforces the verification of the correctness and the integrity of users' contact information by health authorities, thanks to the support of both a computing server and a group of proxies.
- we guarantee strong privacy properties namely the anonymity of users being in contact with infected people, and the unlinkability of users' transactions when relying on random EBIDs that can neither be linked to each other nor be linked to their issuer.
- we propose a concrete construction of the SPOT protocol relying on a structure-preserving signature scheme [4] that supports securely signing group's elements, i.e., contacts' information. This signature scheme is coupled with Groth-Sahai Non-Interactive Witness-Indistinguishable (NIWI) proof [10] in order to ensure integrity of proxies' keys. Indeed, NIWI proofs guarantee the anonymity of proxies while the health authority is still able to verify that proxies are trustful by verifying the validity of their keys without having access to them.
- we evaluate the performances of SPOT through the full implementation of different procedures and algorithms. The conducted experiments have shown acceptable

computation times proving the efficiency and practical usability of the proposed solution.

This paper is organized as follows. Section II introduces and compares most closely-related proximity tracing algorithms and solutions to SPOT. Section III gives an overview of SPOT. After introducing the underlying building blocks in Section IV The concrete construction of the proposed SPOT protocol is presented in Section V. Section VI and Section VII provide security and privacy properties and a detailed discussion of SPOT's conducted experiments, before concluding in Section VIII.

II. RELATED WORK

Recently, several industrial and research contact tracing solutions have been proposed for e-health applications [17], [19]. These solutions aim at ensuring security properties, namely **anti-replay** mitigating the multi-submission of the same contact information , and **unforgeability** preventing malicious entities¹ from threatening data integrity. Privacy properties have been significantly addressed, including the **anonymity** of end-users and the **unlinkability** between their different transactions (i.e., a formal definition of security and privacy requirements is given in Section III-D).

Indeed, researchers from Inria, France, and Fraunhofer, Germany proposed Robert [13], a contact tracing protocol that relies on a centralized architecture, where a central server delivers pseudonyms to users. Each user collects pseudonyms of users in close proximity and shares them with the server when being infected. In such centralized solution, users are sure that they receive correct alerts (i.e., collected pseudonyms are neither replayed nor falsified by malicious entities), however, their privacy is threatened as long as the server is able to identify users' contacts and to track them. In [7], Troncoso et al. introduced the Decentralized Privacy-Preserving Proximity Tracing (DP-3T) solution which is one of the most popular contact-tracing protocols. DP-3T has been proved to mitigate the privacy threats of centralized solutions as there is no need for a central entity which collects users' contact information with the risk of tracking them. However, it does not prevent relay and replay attacks and gives no mean to verify the correctness of contact information. Thus, users are exposed to false alerts from malicious entities either by creating falsified information or replaying information of previous sessions. Afterwards, Castelluccia et al. proposed Desire [9], a proximity tracing protocol that leverages the advantages of the centralized and decentralized solutions. However, some security and privacy issues have not been considered in this solution. First malicious users are able to collude and merge their contact lists, which leads to false positive injection attacks. Second, the server requested to compute the exposure status and risk, is able to link users' requests, and to deanonymize them. Two very similar proposals called PACTs are also introduced. The east coast PACT [18] and the west

¹Malicious entities involve either a single malicious adversary or colluding adversaries.

coast PACT [8] are very close to DP-3T. The two solutions rely on random pseudonyms derived from a private seed, that are broadcasted to users in proximity via Bluetooth. The pseudonyms are generated using cryptographic pseudorandom generators and pseudorandom functions. Apart from the nonresistance against replay attacks, these two proposals give no mean to check the correctness of the contact information before being broadcasted. Pietrzak [16] proposed a decentralized contact-tracing solution to mitigate replay attacks against DP-3T. However, privacy concerns are raised, namely tracking users, as geo-location and time of contacts are shared within the Bluetooth message. In [12], Hoepman proposed two tracing protocols, the first one relies on an interactive session between two users in proximity to register contact information. If the interaction fails, the contact is not registered. Thus, the second protocol comes to mitigate this risk of failure and relies on an authority that relays information between users. In both protocols, the identities of users who have been in contact with an infected person, are revealed to a central entity, which contradicts the defined anonymity requirement. Liu et al. [14] use zero-knowledge proofs and group signatures in order to preserve users' privacy for their proposed tracing protocol. Zero-knowledge proofs are generated by users over the contact information they collected. Indeed, users prove the contacts to their doctors without revealing the information. Afterwards, doctors, being members of a group, sign the proofs and publish them in a public board. Then, relying on their secrets, users can check if they were in contact with infected people. As such, no entity can identify the contacts of an infected user. However, based on a long interactive protocol between two devices, the collection of contacts' information may result in a failed interaction, thus causing the non-registration of the contact. Furthermore, the authors only consider honest but curious adversaries, which leads to possible false alerts due to malicious colluding users. It is also worth noticing that, unlike SPOT and other related work [7], [9], [16], [14] assume that all the computations (handshake, zero-knowledge, verification) are performed by the user's device, which leads to device's battery depletion. A new contact tracing strategy based on online social networking is proposed in [20] but does not provide privacy guarantees. Table 1 provides a comparative summary between SPOT and related works in terms of architecture settings and properties. As shown, SPOT is the only solution which supports strong security and privacy requirements.

III. SPOT OVERVIEW

This section first presents the involved entities and gives an overview of SPOT. Then, it details the system model with its procedures and algorithms and defines the threat model through formal security games.

A. ENTITIES

- The user (U) represents the entity that owns the device where the proximity-tracing application is installed. During the Generation phase, U broadcasts his EBID (Ephemeral Bluetooth IDentifier), collects the EBIDs of other users in proximity, and computes a common contact message shared between each two users being in contact. U wants to receive alerts if he was in contact with confirmed cases.
- The Health Authority (*HA*) is responsible for issuing users' identifiers during the Sys_Init phase, and for checking the correctness of the contact messages provided by an infected user during the Verification phase.
- The Server (S) is responsible for anonymously collecting and storing users' contact messages relayed by proxies during the Generation phase². S performs a real-time verification of the received contacts during the Generation phase, in order to help \mathcal{HA} to verify the correctness and integrity of the contact messages.
- The Proxy (\mathcal{P}) is considered as a member of a group of proxies managed by the group manager (\mathcal{GM})³. Proxies form an intermediate layer by relaying the common contact messages of users to \mathcal{S} in order to ensure the anonymity of involved users towards the server during the Generation phase. Proxies also play an important role in ensuring data integrity and user geolocation privacy thanks to group signatures.

B. OVERVIEW

SPOT is set upon an hybrid architecture that leverages the best of the centralized and decentralized settings in proximitytracing protocols. It relies on a proxy-based solution to preserve users' privacy (i.e., users remain anonymous towards the server, thus preventing users' tracking) and is based on a semi-trusted computing server to ensure data consistency and integrity (i.e., users are ensured that the received alerts are correct). The architecture of the proposed protocol is depicted in Figure 1. SPOT involves three main phases: Sys_Init, Generation and Verification presented hereafter.

The Sys_Init phase consists of initializing the whole system. It relies on seven algorithms, referred to as Set_params, HA_keygen, S_keygen, Setup_ProxyGr_{GM} and Join_ProxyGr_{\mathcal{P}/GM}, Set_UserID_{$\mathcal{H}\mathcal{A}$} and Userkeygen_{\mathcal{U}}. During the Sys_Init phase, a trusted authority⁴ generates the system public parameters published to all involved entities and the pair of keys of both $\mathcal{H}\mathcal{A}$ and \mathcal{S} , relying on Set_params,

⁴For ease of presentation, the trusted authority is neither presented in Figure 1 nor in the system's model entities.

Figure 1 depicts the four main actors involved in SPOT with their interactions according to the different phases. Four actors are defined as follows:

²The Server can be distributed by considering one or several servers per geographical area, each server participating in locally storing part of users' contact messages databases. All the parts are then collected on offline in a centralized server. Thus, for ease of presentation, we consider only one server.

³Proxies are distributed over several geographical areas. We assume that a load-balancing is established between at least two proxies in the same geographical area to ensure the system availability in case of failure or overload. More precisely, proxies in a same geographical area are separated into two subsets - a primary and a secondary - and two users in a contact interaction must contact proxies belonging to different subsets in order to prevent a proxy from gaining too much knowledge about users' interactions.

| | | SPOT | [14] | [12] | [7] | [18] [8] | [13] | [9] | [16] |
|--------------|-----------------------------|--------------|----------------|----------------|--------------|--------------|--------------|--------------|--------------|
| Architecture | Centralized | - | - | - | - | - | \checkmark | - | - |
| | Decentralized | - | \checkmark | - | \checkmark | \checkmark | - | - | \checkmark |
| | Semi-centralized | \checkmark | - | \checkmark | - | - | - | \checkmark | - |
| Properties | Unforgeability ^a | \checkmark | √ ^b | √ ^b | X | X | N.A. | X | X |
| | Anti-replay | \checkmark | \checkmark | \checkmark | X | × | \checkmark | \checkmark | \checkmark |
| | Unlinkability | \checkmark | N.A. | X | \checkmark | \checkmark | X | \checkmark | X |
| | Anonymity | \checkmark | \checkmark | X | X | × | X | \checkmark | X |

TABLE 1: Comparison between SPOT and related works

NOTE: N.A. is the abbreviation for Not Applicable; a indicates that the unforgeability implies the integrity of users' contact information and the prevention of false positives injection; ^a indicates that unforgeability is partially satisfied while not considering malicious colluding entities.

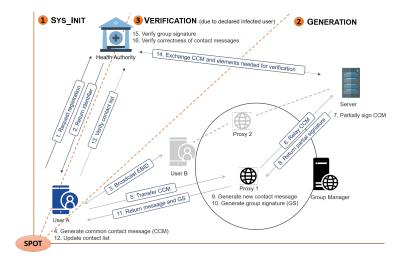


FIGURE 1: Overview of the SPOT protocol

HA_keygen and S_keygen algorithms. During this phase, the group manager defines the group of proxies. It generates the group signature parameters using the Setup_ProxyGr_{GM} algorithm and it interacts with each group member to derive the associated keys relying on the Join_ProxyGr_{P/GM} algorithm. The Health Authority is also involved in this phase to register a user when installing the proximity-tracing application. \mathcal{HA} generates a specific secret value $t_{\mathcal{U}}$ (only known by \mathcal{HA}) and a unique identifier $ID_{\mathcal{U}}$ for each user (\mathcal{U}), using the Set_UserID_{$\mathcal{H}\mathcal{A}$} algorithm. Finally, \mathcal{U} uses his identifier to generate his pair of keys relying on the UserkeygenU algorithm. The user's identifier $ID_{\mathcal{U}}$, secret value $t_{\mathcal{U}}$ and public key are stored in a database DB_{USER} owned by \mathcal{HA} . We note that the trusted authority, the group manager and proxies are involved only once in the Sys_Init phase, while the health authority must intervene every time a user wants to register.

The Generation phase occurs when two users \mathcal{U}_A and \mathcal{U}_B are in contact. It represents the process of generating contact messages and contact lists for users. Three main entities participate in this phase relying on three different algorithms, referred to as Set_CCM $_{\mathcal{U}}$, S_PSign $_{\mathcal{S}}$ and P_Sign $_{\mathcal{P}}$. At first, \mathcal{U}_A and \mathcal{U}_B execute the Set_CCM_{\mathcal{U}} algorithm to generate a common contact message relying on their random EBIDs (denoted by D_A^e and D_B^e) for an epoch e^5 . \mathcal{U}_A and \mathcal{U}_B choose

4

two different proxies to relay their common contact message to the server. For this purpose, they compare their EBIDs, i.e., if $D_A^e > D_B^e$, \mathcal{U}_A chooses the first proxy and \mathcal{U}_B selects the second one, and vice versa. Each of the two proxies relays the common contact message to the server. S checks if the two copies are similar. If so, S executes the S_PSign_S algorithm to partially sign the common contact message, thus proving that the contact message correctly reached the server. Afterwards, given back only a correct message, each proxy executes the $P_Sign_{\mathcal{P}}$ algorithm. Indeed, each proxy extends the message, given by S, with the corresponding user's identifier and it signs the resulting message on behalf of the group. He, finally, sends back the message and the corresponding group signature to the user and closes the communication session, while removing all the exchanged and generated contact information. The user adds the group signature, along with the common contact message, the date, time and duration of contact, in his contact list $CL_{\mathcal{U}}$. Note that each contact information is stored for Δ days.

The Verification phase is run by the health authority to check the correctness of a contact list $CL_{\mathcal{U}}$ provided by \mathcal{U} during a period of time t. To this end, \mathcal{HA} performs three successive verifications relying on two main algorithms, referred to as Sig_Verify_{$\mathcal{H}\mathcal{A}$} and CCM_Verify_{$\mathcal{H}\mathcal{A}$}. (i) $\mathcal{H}\mathcal{A}$

⁵An epoch e denotes a period of time in which the Bluetooth identifier (EBID) remains unchanged.

checks if, in his DB_{USER} database, \mathcal{U} is infected⁶. (ii) \mathcal{HA} checks the validity of the group signatures relying on the Sig_Verify_{\mathcal{HA}} algorithm, w.r.t. the messages contained in the contact list $CL_{\mathcal{U}}$. (iii) \mathcal{HA} verifies that the contact messages have been correctly generated and have successfully reached S, using the CCM_Verify_{\mathcal{HA}} algorithm.

It is worth mentioning that if one of the verifications given above fails, the contact message is rejected. Otherwise, \mathcal{HA} collects all verified messages of all infected users in a set S_{CCM} that she signs. Note that for each period of time t, \mathcal{HA} removes users' contact lists after verifications. S_{CCM} and the corresponding signature are sent to the server that shares them with all users. To compute the risk score, each user compares the set S_{CCM} with his contact list, taking into account the number of infected users being contacted and the contact duration.

For ease of presentation, the different notations used in this paper are depicted in Table 2.

| Notation | Description | | | | |
|--------------------|---|--|--|--|--|
| U | User | | | | |
| \mathcal{HA} | Health Authority | | | | |
| S | Server | | | | |
| \mathcal{P} | Proxy | | | | |
| \mathcal{GM} | Group Manager | | | | |
| \mathcal{TA} | Trusted Authority | | | | |
| $ID_{\mathcal{U}}$ | An identifier of a user \mathcal{U} | | | | |
| $t_{\mathcal{U}}$ | A secret value associated to \mathcal{U} | | | | |
| DB_{USER} | The users' database at \mathcal{HA} | | | | |
| \mathtt{D}^e | An ephemeral Bluetooth Identifier during an epoch e | | | | |
| $CL_{\mathcal{U}}$ | A user's contact list | | | | |
| λ | A security parameter | | | | |
| pp | The system's public parameters | | | | |
| sk | A private key | | | | |
| pk | A public key | | | | |
| \mathtt{vk}_g | The group public parameters | | | | |
| CCM | A common contact message | | | | |
| (PS, PS') | A partial signature | | | | |
| σ | A signature | | | | |
| М | A message derived from PS and $ID_{\mathcal{U}}$ | | | | |
| π | A NIWI proof | | | | |
| S_{CCM} | A set of verified CMMs of infected users | | | | |
| - | | | | | |

C. SYSTEM MODEL

Based on the three phases, Figure 2 presents the chronological sequence of twelve PPT algorithms, defined below. For ease of presentation, we consider only one user and one proxy in the sequence diagram. For the Generation phase, we suppose that two users have been in contact and exchanged their EBIDs. The Verification phase occurs only if the user receives a negative analysis' result.

- Sys_Init phase:
 - $\mathsf{Set_params}(\lambda) \to pp \mathsf{run}$ by a trusted authority. Given

the security parameter λ , this algorithm generates the system public parameters pp that will be considered as a default input for all the following algorithms.

 $K_{kygen}() \rightarrow (sk_j, pk_j)$ – performed by a trusted authority. It returns the pair of keys (sk_j, pk_j) of j where $j = \{HA, S\}.$

Setup_ProxyGr_{*GM*}() \rightarrow (sk_g, vk_g) – this algorithm is performed by the group manager to set up the group signature. It returns the proxies' group verification key vk_g represented as (pk_g, Σ_{NIWI}), where pk_g is the public key of the group manager and Σ_{NIWI} is the Common Reference String CRS of a NIWI proof [10]. The Setup_ProxyGr_{*GM*} algorithm also outputs the secret key sk_g that is privately stored by *GM*.

Join_ProxyGr_{\mathcal{P}/\mathcal{GM}}(sk_g) \rightarrow (sk_p, pk_p, σ_p) – this algorithm is performed through an interactive session between the proxy and the group manager. It takes as input the secret key sk_g, and outputs the pair of keys (sk_p, pk_p) of \mathcal{P} belonging to the group (i.e., \mathcal{P} is responsible for generating his pair of keys), and a signature σ_p over \mathcal{P} 's public key pk_p (i.e., σ_p is generated by \mathcal{GM}).

Set_UserID_{\mathcal{HA}}() \rightarrow ($t_{\mathcal{U}}$, ID_{\mathcal{U}}) – this algorithm is run by \mathcal{HA} and returns a secret value $t_{\mathcal{U}}$ specific for \mathcal{U} and the identifier ID_{\mathcal{U}} of \mathcal{U} .

$$\begin{split} & \mathsf{Userkeygen}_{\mathsf{U}}(\mathtt{ID}_{\mathcal{U}}) \to (\mathtt{sk}_{\mathcal{U}},\mathtt{pk}_{\mathcal{U}}) - \mathsf{performed} \ \mathsf{by} \ \mathcal{U} \ \mathsf{to} \\ & \mathsf{set} \ \mathsf{his} \ \mathsf{pair} \ \mathsf{of} \ \mathsf{keys} \ (\mathtt{sk}_{\mathcal{U}},\mathtt{pk}_{\mathcal{U}}) \ \mathsf{relying} \ \mathsf{on} \ \mathsf{the} \ \mathsf{identifier} \\ & \mathsf{ID}_{\mathcal{U}}. \end{split}$$

· Generation phase:

Set_CCM_U(D_A^e, D_B^e) \rightarrow CCM_{AB}^e – run by each of two users \mathcal{U}_A and \mathcal{U}_B being in contact during an epoch e. Given two Bluetooth identifiers D_A^e and D_B^e , this algorithm generates a common contact message CCM_{AB}^e, S_PSign_S(CCM_{AB}^e, sk_S) \rightarrow (PS^e_{AB}, PS'_{AB}) – run by S. Given a common contact message CCM_{AB}^e sent by \mathcal{U}_A and \mathcal{U}_B through two different proxies \mathcal{P}_1 and \mathcal{P}_2 , this algorithm outputs the couple (PS^e_{AB}, PS'^e_{AB}) that is stored with CCM^e_{AB} at S, for Δ days. Note that only PS^e_{AB} is given back to \mathcal{P}_1 and \mathcal{P}_2 to prove that CCM^e_{AB} has been successfully received and verified by S (i.e., a real contact took place), while PS'^e_{AB} is kept secret at S and is sent only to $\mathcal{H}\mathcal{A}$ to check the correctness of a contact message provided by a infected user.

 $\begin{array}{lll} \mathsf{P}_\mathsf{Sign}_{\mathcal{P}}(\mathsf{vk}_g,\mathsf{sk}_p,\mathsf{pk}_p,\sigma_p,\mathsf{ID}_{\mathcal{U}_A},\mathsf{PS}^e_{AB}) &\to (\mathsf{M}^e_{AB},\sigma_m,\pi)^7 - \mathsf{performed} \text{ by the proxy } \mathcal{P} \ (\mathcal{P}_1 \ \text{or} \ \mathcal{P}_2). \\ \text{This algorithm takes as input the proxies' group public parameters } \mathsf{vk}_g, \text{ the pair of keys } (\mathsf{sk}_p,\mathsf{pk}_p) \ \text{of} \ \mathcal{P}, \text{ the signature } \sigma_p \ \text{over} \ \mathcal{P}'s \text{ public key, the identifier } \mathsf{ID}_{\mathcal{U}_A} \ \text{of} user \ \mathcal{U}_A \ \text{and the message } \mathsf{P}^e_{AB}. \ \text{It returns a signature } \sigma_m \ \text{over a new message } \mathsf{M}^e_{AB} \ \text{and a group signature } \mathsf{represented by a NIWI proof } \pi \ \text{over the two signatures } \sigma_p \ \text{and } \sigma_m. \ \text{The couple} \ (\mathsf{M}^e_{AB},\pi) \ \text{is sent to user } \ \mathcal{U}_A \ \text{to be stored with the contact message } \mathsf{CCM}^e_{AB} \ \text{in his contact} \end{array}$

⁶We suppose that the health status of a user is updated when being tested. Indeed, to be tested, \mathcal{U} has to provide an encrypted form of his identifier $ID_{\mathcal{U}}$ (i.e., $ID_{\mathcal{U}}$ is encrypted meaning the \mathcal{HA} public key). Afterwards, the analysis' result is sent with the encrypted identifier to \mathcal{HA} , that extracts the identifier and updates the user's health status in the DB_{USER} database.

⁷In this algorithm, we only consider user U_A with ID_{U_A} . The same operations are performed for user U_B with ID_{U_B} .

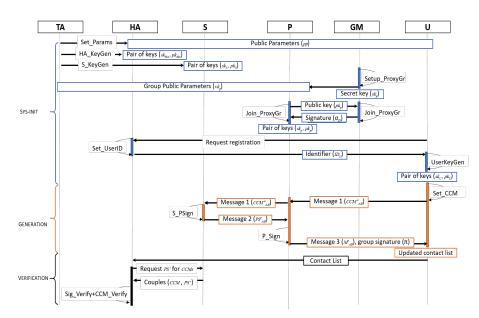


FIGURE 2: Workflow of the SPOT protocol

list. Note that each input of the contact list is stored for Δ days.

• Verification phase:

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Sig_Verify_{HA}(vk_g, M^e_{AB}, π) \rightarrow b – performed by HA. Given the public parameters vk_g, a message M^e_{AB} from the contact list of an infected user, and the corresponding NIWI proof π , the Sig_Verify_{HA} algorithm returns a bit $b \in \{0, 1\}$ stating whether the proof is valid. CCM_Verify_{HA}(M^e_{AB}, PS'^e_{AB}, pk_S, t_{UA}) \rightarrow b – run by HA. This algorithm takes as input the message M^e_{AB}, the message PS'^e_{AB} requested from S, the server's public key pk_S and the secret value t_{UA}, and outputs a bit $b \in \{0, 1\}$, i.e., CCM^e_{AB} is correctly generated or not.

D. THREAT MODEL

In this section, we first present the adversaries considered in SPOT, and then, the formal definitions of the different security and privacy properties.

- A malicious user (U): this adversary attempts to inject false contact messages or contact messages of other users in his contact list. He may also collude with corrupted proxies or malicious users.
- A honest but curious health authority (*HA*): given a valid group signature, *HA* tries to identify the signer (i.e., proxy) of a particular message, hence for identifying the appropriate geographical area and for tracking the user's movements. She may also attempt to link two signatures issued by the same group member. A curious *HA* may also try to identify, from a contact list of a particular user, the list of users he had been in contact with.
- A honest but curious server (S): he attempts to link several common contact messages generated by the same user, to trace users' movements.

• A malicious proxy (\mathcal{P}): this adversary, either colluding with a malicious user or with *n* other proxies, attempts to forge the partial signature of the server and to generate a valid signature over a false contact message.

Both malicious users and malicious proxies are considered against security properties, i.e., unforgeability, anti-replay, while the curious health authority and server are considered against privacy requirements, i.e., unlinkability and anonymity. The different adversaries are involved in different phases. Note that the **anti-replay** property which aims at mitigating the multi-submission of the same contact information is not formally presented below, but is informally discussed in Section VI. The following properties are defined w.r.t the corresponding phases and the involved adversaries.

Remark 1. We do not deeply analyze the case of a malicious \mathcal{GM} although our scheme is resistant against this adversary. Indeed, proxies are responsible for generating their key pair and only their public keys are shared with \mathcal{GM} . Thus, unless holding a proxy's secret key, \mathcal{GM} is not able to generate a valid signature on behalf of \mathcal{P} thanks to the unforgeability of the signature scheme.

1) Unforgeability

The unforgeability property ensures the security of SPOT for the different phases. It states that a malicious user is not able to forge his contact list (i.e., forging either the group signature or the server's partial signature when colluding with a malicious proxy)⁸. Formally, this is defined in a game Exp_A^{unforg} where an adversary A, playing the role of a corrupted proxy colluding with a malicious user, has access to

⁸We assume that (i) malicious user refers to either a single user or colluding users, and (ii) the group signature scheme used in SPOT is unforgeable as proven in [4], thus in the security model and analysis, we will only consider the unforgeability of the server's partial signature.

a S_PSign oracle. We note that, for each session i, \mathcal{A} only gets PS^{*i*} from the S_PSign oracle, while PS'^{*i*} is kept secret from the adversary. Then, given a valid message PS' that cannot be obtained by combining either a part of or all messages PS^{*i*}, \mathcal{A} succeeds if it outputs a valid message PS* to be signed using P_Sign, such that the CCM_Verify verification holds.

Definition 1. Unforgeability – We say that SPOT satisfies the unforgeability property, if for every *PPT* adversary \mathcal{A} , there exists a negligible function κ such that: $Pr[\mathbf{E}xp_{\mathcal{A}}^{unforg}(1^{\lambda}) = 1] \leq \kappa(\lambda)$, where $\mathbf{E}xp_{\mathcal{A}}^{unforg}$ is given below.

$$\begin{split} & Exp_{\mathcal{A}}^{unforg}(\lambda) \\ & pp \gets \mathsf{Set_params}(\lambda) \end{split}$$
 $(\mathtt{sk}_{\mathcal{H}\mathcal{A}}, \mathtt{pk}_{\mathcal{H}\mathcal{A}}) \leftarrow \mathsf{HA}_{\mathsf{keygen}}(pp)$ $(\mathtt{sk}_{\mathcal{S}}, \mathtt{pk}_{\mathcal{S}}) \leftarrow \mathsf{S}_{\mathsf{keygen}}(pp)$ $(\mathtt{sk}_{q}, \mathtt{vk}_{q}) \leftarrow \mathsf{Setup}_\mathsf{Proxy}\mathsf{Gr}(pp)$ $(\mathtt{sk}_p, \mathtt{pk}_p, \sigma_p) \leftarrow \mathsf{Join}_\mathsf{Proxy}\mathsf{Gr}(pp, \mathtt{sk}_q)$ $ID_{\mathcal{U}} \leftarrow Set_UserID(pp)$ $(\mathtt{sk}_{\mathcal{U}}, \mathtt{pk}_{\mathcal{U}}) \leftarrow \mathsf{Userkeygen}(pp, \mathtt{ID}_{\mathcal{U}})$ $CCM \leftarrow Set_CCM(D_1, D_2)$ $(PS, PS') \leftarrow \{S_PSign(CCM, sk_S)\}$ $\mathcal{O} \leftarrow \{\mathsf{S}_\mathsf{PSign}(\cdot, \mathtt{sk}_{\mathcal{S}})\}$ $\mathtt{PS}^* \leftarrow \mathcal{A}^{\mathcal{O}}(\mathtt{vk_g}, \mathtt{sk_p}, \mathtt{pk_p}, \sigma_p, ID_{\mathcal{U}}, pp, \mathtt{PS'})$ letting CCM and PS^i denote the queries and answers to and from oracle S_PSign $(\mathbb{M}^*, \sigma^*, \pi^*) \leftarrow \mathsf{P}_{\mathsf{Sign}}(\mathsf{vk}_q, \mathsf{sk}_p, \mathsf{pk}_n, \sigma_p, ID_{\mathcal{U}}, \mathsf{PS}^*)$ If CCM_Verify(M^* , PS'^* , pk_S , t_U) = 1 return 1 Else return 0

2) Unlinkability

The unlinkability property can be divided into two subproperties. The first one constitutes the *group-signature unlinkability* stating that a curious health authority is not able to link two or several group signatures issued by the same proxy during the Verification phase. The second sub-property *multi-CCM unlinkability* ensures that a curious server is not able to link two or several common contact messages to the same user during the Generation phase ⁹.

We note that the *multi-CCM unlinkability* property will be informally discussed in Section VI. In this section, we only focus on the *group-signature unlinkability*. Formally, this property is defined in a game $\mathbb{E}xp_{\mathcal{A}}^{unlink}$ where an adversary \mathcal{A} acting as a curious $\mathcal{H}\mathcal{A}$ has access to a P_Sign oracle. The adversary may query this oracle on the same message PS^{*} and on a tuple (($\mathfrak{sk}_{p_j}, \mathfrak{pk}_{p_j}, \sigma_{p_j}$), where $j \in \{0, 1\}$ (i.e., the tuple belongs either to proxy \mathcal{P}_0 or proxy \mathcal{P}_1). A left-or-right oracle LoRSig is initialized with a secret random bit b and returns to \mathcal{A} P_Sign on message PS^{*} and respectively on tuples $(\mathbf{sk}_{p_0}, \mathbf{pk}_{p_0}, \sigma_{p_0})$ and $(\mathbf{sk}_{p_b}, \mathbf{pk}_{p_b}, \sigma_{p_b})$. The adversary wins the game if he successfully predicts the bit *b* (i.e., the guessing probability should be greater than $\frac{1}{2}$).

Definition 2. Unlinkability – We say that SPOT satisfies the unlinkability property, if for every *PPT* adversary \mathcal{A} , there exists a negligible function κ such that: $Pr[\mathbf{E}xp_{\mathcal{A}}^{unlink}(\lambda) = 1] = \frac{1}{2} \pm \kappa(\lambda)$, where $\mathbf{E}xp_{\mathcal{A}}^{unlink}$ is defined below.

 $Exp_{A}^{unlink}(\lambda)$ $pp \leftarrow \mathsf{Set_params}(\lambda)$ $(\mathtt{sk}_{\mathcal{H}\mathcal{A}}, \mathtt{pk}_{\mathcal{H}\mathcal{A}}) \leftarrow \mathsf{HA}_{\mathsf{keygen}}(pp)$ $(\mathtt{sk}_{\mathcal{S}}, \mathtt{pk}_{\mathcal{S}}) \leftarrow \mathsf{S}_{\mathsf{keygen}}(pp)$ $(\mathtt{sk}_q, \mathtt{vk}_q) \leftarrow \mathsf{Setup_ProxyGr}(pp)$ $(\mathtt{sk}_{p_i}, \mathtt{pk}_{p_i}, \sigma_{p_i}) \leftarrow \mathsf{Join}_\mathsf{ProxyGr} (pp, \mathtt{sk}_q), i \in$ $\{0,1\}$ $\mathtt{ID}_{\mathcal{U}} \leftarrow \mathsf{Set_UserID}(pp)$ $(\mathtt{sk}_{\mathcal{U}}, \mathtt{pk}_{\mathcal{U}}) \gets \mathsf{Userkeygen}(pp, \mathtt{ID}_{\mathcal{U}})$ $m^* \leftarrow \mathsf{Set} \ \mathsf{CCM}(\mathsf{D}_1,\mathsf{D}_2)$ $(PS^*, PS'^*) \leftarrow S_PSign(m^*, sk_S)$ $b \leftarrow \{0, 1\}$ $\mathcal{O} \leftarrow \{\mathsf{P}_\mathsf{Sign}(\cdot,\mathsf{sk}_{p_j},\mathsf{pk}_{p_j},\sigma_{p_j},\cdot,\cdot), \mathsf{LoRSig}(\cdot,\cdot,b)\}$ $b' \leftarrow \mathcal{A}^{\mathcal{O}} (\mathsf{sk}_{\mathcal{H}\mathcal{A}}, \mathsf{pk}_{\mathcal{H}\mathcal{A}}, \mathsf{vk}_{g}, \mathsf{pk}_{p_0}, \mathsf{pk}_{p_1}, pp, \mathsf{PS}^*)$ If b = b'return 1 Else return 0

 $\begin{array}{l} \mathsf{LoRSig}\;(\mathsf{vk}_g,\,((\mathsf{sk}_{p_0},\,\mathsf{pk}_{p_0},\,\sigma_{p_0}),\,(\mathsf{sk}_{p_1},\,\mathsf{pk}_{p_1},\,\sigma_{p_1})),\\ \mathsf{ID}_{\mathcal{U}},\,\mathsf{PS}^*,b)\\ (\mathsf{M}^*,\sigma^*,\pi^*) \leftarrow \mathsf{P}_\mathsf{Sign}(\mathsf{vk}_g,\,\mathsf{sk}_{p_0},\,\mathsf{pk}_{p_0},\,\sigma_{p_0},\,\mathsf{ID}_{\mathcal{U}}\,,\\ \mathsf{PS}^*)\\ (\mathsf{M}^*,\sigma^*_b,\pi^*_b) \leftarrow \mathsf{P}_\mathsf{Sign}(\mathsf{vk}_g,\,\mathsf{sk}_{p_b},\,\mathsf{pk}_{p_b},\,\sigma_{p_b},\,\mathsf{ID}_{\mathcal{U}}\,,\\ \mathsf{PS}^*)\\ \mathsf{return}\;((\mathsf{M}^*,\pi^*),(\mathsf{M}^*,\pi^*_b)) \end{array}$

3) Anonymity

This property guarantees that no entity is able to identify users involved in a contact list (i.e., the owner and the contacted users), during the Verification phase, and is described through the game $\mathbf{E}xp_{\mathcal{A}}^{anon}$. The anonymity property implies that even if \mathcal{HA} knows that a contact list belongs to a user (\mathcal{U}), \mathcal{HA} is not able to identify users being in contact with \mathcal{U}^{10} . This should hold even if an efficient adversary, playing the role of the curious health authority, is given access to Set_CCM, S_PSign, P_Sign oracles. A can learn contact messages and signatures associated to the selected users' identifiers. A also gets access to a left-or-right oracle LoRCU which is initialized with a secret random bit $b \in \{0, 1\}$. A may query this oracle on $ID_{\mathcal{U}_0}$ and $ID_{\mathcal{U}_1}$ referred to as the identifiers of respectively user \mathcal{U}_0 and user \mathcal{U}_1 . Observe that user \mathcal{U}_A is involved in all queries. $D^*_{\mathcal{U}_A}$ and $D^*_{\mathcal{U}_b}$, respectively belonging to user \mathcal{U}_A and user \mathcal{U}_b , are randomly selected in order to execute the LoRCU oracle. To win the proposed anonymity game, the adversary

⁹The collusion between the health authority and the server does not pose additional and plausible threats to the different procedures of the whole framework. Indeed, during the GENERATION phase, contact messages are anonymous to the server (and a possible colluding health authority); during the VERIFICATION phase, the health authority knows the true identity of the confirmed cases with their contact information; as such, a collusion between the server and the authority does not bring extra knowledge.

¹⁰We assume that the probability of two confirmed users being in contact and submitting their respective contact lists to \mathcal{HA} at the same period, is low.

should predict the bit b (i.e., which one of users U_0 and U_1 is involved in the contact with user \mathcal{U}_A) with a probability greater than $\frac{1}{2}$.

Definition 3. Anonymity – We say that SPOT fulfills the anonymity requirement, if for every PPT adversary A, there exists a negligible function κ such that: $Pr[\mathbf{E}xp_{\mathcal{A}}^{anon}(1^{\lambda}) =$ 1] = $\frac{1}{2} \pm \kappa(\lambda)$, where $\mathbf{E} x p_{\mathcal{A}}^{anon}$ is defined as follows.

 $Exp_{\mathcal{A}}^{anon}(\lambda)$ $pp \leftarrow \mathsf{Set_params}(\lambda)$ $(\mathtt{sk}_{\mathcal{H}\mathcal{A}}, \mathtt{pk}_{\mathcal{H}\mathcal{A}}) \leftarrow \mathsf{HA}_{\mathsf{keygen}}(pp)$ $(\mathtt{sk}_{\mathcal{S}}, \mathtt{pk}_{\mathcal{S}}) \leftarrow \mathsf{S}_\mathsf{keygen}(pp)$ $(\mathtt{sk}_a, \mathtt{vk}_a) \leftarrow \mathsf{Setup}_\mathsf{Proxy}\mathsf{Gr}(pp)$ $(\mathtt{sk}_p, \mathtt{pk}_p, \sigma_p) \gets \mathsf{Join_ProxyGr}(pp, \mathtt{sk}_g)$ $ID_{\mathcal{U}_A} \leftarrow Set_UserID(pp)$ $(\mathtt{sk}_{\mathcal{U}_A}, \mathtt{pk}_{\mathcal{U}_A}) \leftarrow \mathsf{Userkeygen}(pp, \mathtt{ID}_{\mathcal{U}_A})$ $ID_{\mathcal{U}_i} \leftarrow Set_UserID(pp), i \in \{0..N\}$ $(\mathsf{sk}_{\mathcal{U}_i}, \mathsf{pk}_{\mathcal{U}_i}) \leftarrow \mathsf{Userkeygen}(pp, \mathsf{ID}_{\mathcal{U}_i}), i \in \{0..N\}$ $b \leftarrow \{0,1\}$ $\mathcal{O} \leftarrow \{ \mathsf{Set} \ \mathsf{CCM}(\cdot, \cdot), \mathsf{S} \ \mathsf{PSign}(\cdot, \mathsf{sk}_{\mathcal{S}}), \mathsf{P} \ \mathsf{Sign}(\cdot, \mathsf{sk}_{n}) \}$ $\sigma_{p}, \sigma_{p}, \cdot, \cdot$, LoRCU(\cdot, \cdot, b, \cdot) $b' \leftarrow \mathcal{A}^{\mathcal{O}} (\mathsf{sk}_{\mathcal{H}\mathcal{A}}, \mathsf{pk}_{\mathcal{H}\mathcal{A}}, pp, \mathsf{ID}_{\mathcal{U}_A}, \{\mathsf{ID}_{\mathcal{U}_i}\}_{i=0}^N)$ If b = b'return 1 Else return 0

LoRCU $(D^*_{\mathcal{U}_A}, D^*_{\mathcal{U}_b}, b, vk_g, sk_S, sk_p, pk_p, \sigma_p, ID_{\mathcal{U}_A},$ $ID_{\mathcal{U}_h})$ $\mathsf{CCM}_b^* \leftarrow \mathsf{Set}_\mathsf{CCM}_{\mathcal{U}_A} (\mathsf{D}_{\mathcal{U}_A}^*, \mathsf{D}_{\mathcal{U}_b}^*)$ $(\mathsf{PS}_b^*, \mathsf{PS'}_b^*) \leftarrow \mathsf{S}_\mathsf{PSign} (\mathsf{CCM}_b^*, \mathsf{sk}_S)$ $(\texttt{M}^*_b, \sigma^*_b, \pi^*_b) \leftarrow \mathsf{P}_{\mathsf{Sign}}(\texttt{vk}_g, \texttt{sk}_p, \texttt{pk}_p, \sigma_p, \texttt{ID}_{\mathcal{U}_A},$ PS_{h}^{*}) return ($\mathsf{CCM}_b^*, \mathsf{M}_b^*, \pi_b^*$)

IV. BUILDING BLOCKS

After introducing bilinear maps and security standard assumptions in Section IV-A, the section next presents structurepreserving signatures [4] with their different variants as main building blocks of the SPOT protocol. Sections IV-B and IV-C describe respectively constant-size signatures and signatures on mixed-group messages that are instantiated in Appendix IV-D to build a group signature scheme on group element messages.

A. MATHEMATICAL BACKGROUND AND CRYPTOGRAPHIC ASSUMPTIONS

Hereafter, we define bilinear maps and we present the computational indistinguishability property and the CDH assumption.

1) Bilinear Maps

Let $\mathbb{G}_1 = \langle g_1 \rangle$ and $\mathbb{G}_2 = \langle g_2 \rangle$ be two cyclic groups of order n so there exists a bilinear map $e : \mathbb{G}_1 \times \mathbb{G}_2 \to \mathbb{G}_3$ that satisfies the following properties: (i) bilinearity for all $g_1 \in \mathbb{G}_1, g_2 \in$ \mathbb{G}_2 , (ii) non-degeneracy: $e(g_1, g_2) \neq 1$ and (iii) $e(g_1, g_2)$ is efficiently computable for any $g_1 \in \mathbb{G}_1$ and $g_2 \in \mathbb{G}_2$.

2) Computational Witness-Indistinguishability

The Computational Witness-Indistinguishability property is defined as follows: Let $L \in \mathcal{NP}$ be a language and let $(\mathcal{P}, \mathcal{V})$ be an interactive proof system for L. We say that $(\mathcal{P}, \mathcal{V})$ is witness-indistinguishable (WI) if for every PPT algorithm \mathcal{V}^* and every two sequences $\{w_x^1\}_{x \in L}$ and $\{w_x^2\}_{x \in L}$ such that w_x^1 and w_x^2 are both witnesses for x, the following ensembles are computationally indistinguishable, where z is an auxiliary input to \mathcal{V}^* :

- 1) { $\langle \mathcal{P}(w_x^1), \mathcal{V}^* \rangle(x)$ }_{x \in L, z \in \{0,1\}^*} 2) { $\langle \mathcal{P}(w_x^2), \mathcal{V}^* \rangle(x)$ }_{x \in L, z \in \{0,1\}^*}
- 3) Computational Diffie Hellman Assumption (CDH)

The CDH assumption is defined as follows: Let \mathbb{G} be a group of prime order n, and g is a generator of \mathbb{G} . The CDH problem is defined as: Given the tuple of elements (q, q^x, q^y) , where $\{x, y\} \leftarrow \mathbb{Z}_n$, there is no efficient algorithm \mathcal{A}_{CDH} that can compute g^{xy} .

B. STRUCTURE-PRESERVING CONSTANT-SIZE SIGNATURE

Structure-preserving constant-size signature was defined by Abe et al. [4] as the main scheme of structure-preserving signatures used to sign a message $\vec{m} = (m_1, ..., m_k) \in$ \mathbb{G}_2^k , considering an asymmetric bilinear group $(n, \mathbb{G}_1, \mathbb{G}_2, \mathbb{G}_2)$ $\mathbb{G}_3, g_1, g_2, e$). A constant-size signature scheme CSIG [4] relies on the following three PPT algorithms (CSIG.Key, CSIG.Sign, CSIG.Verify):

CSIG.Key (1^{λ}) : This algorithm takes as input the security parameter (1^{λ}) and outputs the pair of public and secret keys (sk, pk) of the signer. It chooses two random generators $g_r, h_u \leftarrow \mathbb{G}_1^*$ and random values $\gamma_i, \delta_i \leftarrow \mathbb{Z}_n^*$ and computes $g_i = g_r^{\gamma_i}$ and $h_i = h_u^{\delta_i}$, for i = 1, ..., k. It then selects $\gamma_z, \delta_z \leftarrow \mathbb{Z}_n^*$ and computes $g_z = g_r^{\gamma_z}$ and $h_z = h_u^{\delta_z}$. It also chooses $\alpha, \beta \leftarrow \mathbb{Z}_n^*$ and sets the couples (g_r, g_2^{α}) and (h_u, g_2^{β}) . The public key is set as $\mathbf{pk} = (g_z, h_z, g_r, h_u, g_2^{\alpha}, g_2^{\beta}, \{g_i, h_i\}_{i=1}^k) \text{ and the secret key}$ is set as $\mathbf{sk} = (\mathbf{pk}, \alpha, \beta, \gamma_z, \delta_z, \{\gamma_i, \delta_i\}_{i=1}^k).$

CSIG.Sign(sk, \vec{m}): This algorithm generates a signature σ over a message \vec{m} using the secret key sk. That is, the signer randomly selects $\zeta, \rho, \tau, \varphi, \omega \leftarrow \mathbb{Z}_n^*$ and computes

$$z = g_2^{\zeta}, r = g_2^{\alpha - \rho \tau - \gamma_z \zeta} \prod_{i=1}^k m_i^{-\gamma_i}, s = g_r^{\rho}, t = g_2^{\tau},$$
$$u = g_2^{\beta - \varphi \omega - \delta_z \zeta} \prod_{i=1}^k m_i^{-\delta_i}, v = h_u^{\varphi}, w = g_2^{\omega}$$

The signature is set as $\sigma = (z, r, s, t, u, v, w)$.

CSIG.Verify(pk, \vec{m}, σ): This algorithm checks the validity of the signature σ on the message m relying on the signer's public key pk. It outputs 1 if the signature is valid and 0 otherwise. The verifier checks if the following equations hold:

$$A = e(g_z, z)e(g_r, r)e(s, t)\prod_{i=1}^{k} e(g_i, m_i)$$
(1)

$$B = e(h_z, z)e(h_u, u)e(v, w)\prod_{i=1}^{k} e(h_i, m_i)$$
(2)

where $A = e(g_r, g_2^{\alpha})$ and $B = e(h_u, g_2^{\beta})$

C. STRUCTURE-PRESERVING SIGNATURE ON MIXED-GROUP MESSAGES

A structure-preserving signature on mixed-group messages XSIG [4] represents a signature scheme where the message space is a mixture of the two groups \mathbb{G}_1 and \mathbb{G}_2 . We consider two constant-size signature schemes CSIG1 and CSIG2. CSIG2 is the same scheme as in Section IV-B where the message space is $\mathbb{G}_2^{k_2}$, while CSIG1 is a 'dual' scheme obtained by exchanging \mathbb{G}_1 and \mathbb{G}_2 in the same scheme, where the message space is $\mathbb{G}_1^{k_1}$. The message space for the XSIG is then $\mathbb{G}_1^{k_1} \times \mathbb{G}_2^{k_2}$. Let (\vec{m}, \vec{m}) be a message in $\mathbb{G}_1^{k_1} \times \mathbb{G}_2^{k_2}$. For a vector $\vec{m} \in \mathbb{G}_1^{k_1}$ and a single element $s \in \mathbb{G}_1$, let $\vec{m} || s$ denote a vector in $\mathbb{G}_1^{k_1+1}$ obtained by appending s to the end of \vec{m} .

A mixed-group messages signature scheme XSIG relies on the following three PPT algorithms (XSIG.Key, XSIG.Sign, XSIG.Verify):

XSIG.Sign(sk, (\vec{m}, \vec{m})): This algorithm runs $\sigma_2 = (z, r, s, t, u, v, w) \leftarrow \text{CSIG2.Si-gn}(\text{sk}_2, \vec{m})$ and $\sigma_1 = (z', r', s', t', u', v', w') \leftarrow \text{CSIG1.Sign}(\text{sk}_1, \vec{m} || s)$, and outputs $\sigma = (\sigma_1, \sigma_2)$.

XSIG.Verify(pk, $(\vec{m}, \vec{m}), (\sigma_1, \sigma_2)$): This algorithm takes $s \in \mathbb{G}_1$ from σ_2 , runs $b_2 = \mathsf{CSIG2.Verify}(\mathsf{pk}_2, \vec{m}, \sigma_2)$ and $b_1 = \mathsf{CSIG1.Verify}(\mathsf{pk}_1, \vec{m} || s, \sigma_1)$. If $b_1 = b_2 = 1$, the algorithm outputs 1, otherwise it outputs 0.

D. GROUP SIGNATURES DRAWN FROM STRUCTURE-PRESERVING SIGNATURES

We present hereafter an instantiation of a group signature scheme that allows to sign a group element message relying on a constant-size signature scheme CSIG, a mixed-group messages signature scheme XSIG and a witness indistinguishable proof of knowledge system NIWI [10] (cf. Appendix).

A group signature scheme GSIG relies on the four following algorithms (GSIG.Setup, GSIG.Join, GSIG.Sign, GSIG.Verify):

GSIG.Setup : represents the setup algorithm. It runs XSIG.Key algorithm that generates the key pair (sk_g, pk_g) of the group manager and sets up a CRS Σ_{NIWI} for the NIWI proof. The group verification key is set as $vk_g = (pk_g, \Sigma_{NIWI})$,

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while the certification secret key sk_g is privately stored by the group manager.

GSIG.Join: represents the join algorithm. It is composed of two steps. In the first one, the group member generates his key-pair (sk_p, pk_p) while running the CSIG.Key algorithm. Only the public key pk_p is sent to the group manager. This latter generates a signature σ_p over pk_p , using the XSIG.Sign algorithm, and sends it to the group member.

GSIG.Sign: represents the signing algorithm run by a group member on a message $m \in \mathbb{G}_2$. The group member generates, over the message m, a signature $\sigma_m \leftarrow \text{CSIG.Sign}(\mathfrak{sk}_p, m)$ and a non-interactive witness indistinguishable proof of knowledge $\pi \leftarrow \text{NIWI.Proof}(\Sigma_{\text{NIWI}}, pub, wit)$ that proves $1 = \text{XSIG.Verify}(pk_g, pk_p, \sigma_p)$ and $1 = \text{CSIG.Verify}(pk_p, m, \sigma_m)$ with respect to the witness $wit = (pk_p, \sigma_p, \sigma_m)$ and the public information $pub = (pk_g, m)$. The signing algorithm outputs the group signature π .

GSIG.Verify: represents the group signature verification algorithm run by a verifier. It takes (vk_g, m, π) as input and verifies the correctness of the NIWI proof π w.r.t. $pub = (pk_g, m)$ and the CRS Σ_{NIWI} .

V. SPOT ALGORITHMS

This section gives a concrete construction of the different phases and algorithms of SPOT, introduced in Section III-A. SPOT relies on the different variants of structure-preserving signatures represented in Appendix IV.

A. SYS_INIT PHASE

- Set_params a trusted authority sets an asymmetric bilinear group (n, 𝔅₁, 𝔅₂, 𝔅₃, g₁, g₂, e) relying on the security parameter λ, where 𝔅₁ and 𝔅₂ are two cyclic groups of prime order n, g₁ and g₂ are generators of respectively 𝔅₁ and 𝔅₂ and e is a bilinear map such that e : 𝔅₁ × 𝔅₂ → 𝔅₃. The trusted authority also considers a cryptographic hash function H : {0,1}* → ℤ_n. The output of the Set_params algorithm represents the system global parameters that are known by all the system entities. The tuple (n, 𝔅₁, 𝔅₂, 𝔅₃, g₁, g₂, e, H) is denoted by pp, and is considered as a default input of all algorithms.
- HA_keygen a trusted authority takes as input the public parameters *pp*, selects a random *x* ∈ Z^{*}_n and generates the pair of secret and public keys (sk_{HA}, pk_{HA}) of the health authority as follows:

sl

$$\mathbf{x}_{\mathcal{H}\mathcal{A}} = x$$
 ; $\mathbf{pk}_{\mathcal{H}\mathcal{A}} = g_2^x$

 S_keygen – a trusted authority generates the pair of secret and public keys (sk_S, pk_S) of the server as given below, relying on the system public parameters *pp* and two selected randoms *y*₁, *y*₂ ∈ Z^{*}_n.

 $\mathsf{sk}_{\mathcal{S}} = (y_1, y_2)$; $\mathsf{pk}_{\mathcal{S}} = (Y_1, Y_2) = (g_2^{y_1}, g_2^{y_2})$

- Setup_ProxyGr_{GM} GM sets up the group of proxies by generating a group public key vk_g and a certification secret key sk_g as shown in Algorithm 1.
- Join_ProxyGr_{P/GM} P first generates his pair of keys (sk_p, pk_p) w.r.t. the CSIG.Key algorithm (cf. Section

IV-B). Afterwards, \mathcal{GM} generates a signature σ_p over the public key pk_p w.r.t. the XSIG.Sign algorithm (cf. Section IV-C). The Join_ProxyGr_{P/GM} algorithm is detailed in Algorithm 2.

Algorithm 1 Setup_ProxyGr_{GM} algorithm

- 1: **Input:** the system public parameters *pp*
- 2: **Output:** the public parameters vk_a of the proxies' group and the secret key sk_g
- 3: // The next iterations are executed to generate the pair of keys of \mathcal{GM}
- 4: pick at random $g_{r1}, h_{u1} \leftarrow \mathbb{G}_1^*, g_{r2}, h_{u2} \leftarrow \mathbb{G}_2^*$
- 5: for i = 1 to 2 do pick at random $\gamma_{1i}, \delta_{1i} \leftarrow \mathbb{Z}_n^*$ compute $g_{1i} \leftarrow g_{r1}^{\gamma_{1i}}, h_{1i} \leftarrow h_{u1}^{\delta_{1i}}$
- 6: end for
- 7: for j = 1 to 7 do pick at random $\gamma_{2j}, \delta_{2j} \leftarrow \mathbb{Z}_n^*$ compute $g_{2i} \leftarrow g_{r2}^{\gamma_{2j}}$ and $h_{2j} \leftarrow h_{u2}^{\delta_{2j}}$
- 8: end for
- 9: pick at random $\gamma_{1z}, \delta_{1z}, \gamma_{2z}, \delta_{2z} \leftarrow \mathbb{Z}_n^*$; 10: compute $g_{1z} \leftarrow g_{r1}^{\gamma_{1z}}, h_{1z} \leftarrow h_{u1}^{\delta_{1z}}, g_{2z} \leftarrow g_{r2}^{\gamma_{2z}}$ and $h_{2z} \leftarrow h_{u2}^{\delta_{2z}}$;
- 11: pick at random $\alpha_1, \alpha_2, \beta_1, \beta_2 \leftarrow \mathbb{Z}_n^*$;
- 12: $\mathbf{pk}_1 \leftarrow (g_{2z}, h_{2z}, g_{2r}, h_{2u}, g_1^{\alpha_2}, g_1^{\beta_2}, \{g_{2j}, h_{2j}\}_{j=1}^7)$ and $\mathbf{sk}_1 \leftarrow (\mathbf{pk}_1, \alpha_2, \beta_2, \gamma_{2z}, \delta_{2z}, \{\gamma_{2j}, \delta_{2j}\}_{j=1}^7);$
- 14: set $pk_q \leftarrow (pk_1, pk_2)$ and $sk_q \leftarrow (sk_1, sk_2)$;
- 15: // The next iterations are executed to generate the CRS Σ_{NIWI}
- 16: pick at random $r, s \leftarrow \mathbb{Z}_n^*$ and set $\mathcal{U} = rg_1$ and $\mathcal{V} = sg_2$
- 17: set $\Sigma_{\text{NIWI}} = (\mathbb{G}_1, \mathbb{G}_2, \mathbb{G}_3, e, \iota_1, p_1, \iota_2, p_2, \iota_3, \mathcal{U}, \mathcal{V});$
- 18: $\mathsf{vk}_g \leftarrow (\mathsf{pk}_q, \Sigma_{\mathsf{NIWI}});$
- 19: **return** $(\mathbf{sk}_q, \mathbf{vk}_q)$
- Set_UserID_{$\mathcal{H}\mathcal{A}$} every time, a user (\mathcal{U}) installs the application and wants to register, \mathcal{HA} picks a secret $t_{\mathcal{U}} \in \mathbb{Z}_n^*$ and sets the user's identifier $ID_{\mathcal{U}}$ as

$$\mathtt{ID}_\mathcal{U} = h_\mathcal{U} = g_2^{t_\mathcal{U}}$$

• Userkeygen \mathcal{U} – After receiving his identifier ID \mathcal{U} , a user generates his pair of secret and private keys $(sk_{\mathcal{U}}, pk_{\mathcal{U}})$. Indeed, \mathcal{U} randomly selects $q_{\mathcal{U}} \in \mathbb{Z}_n^*$ and sets $(\mathtt{sk}_{\mathcal{U}}, \mathtt{pk}_{\mathcal{U}})$ as

$$\mathtt{sk}_{\mathcal{U}} = q_{\mathcal{U}}$$
 ; $\mathtt{pk}_{\mathcal{U}} = h_{\mathcal{U}}^{q_{\mathcal{U}}}$

- **B. GENERATION PHASE**
 - Set_CCM $_{\mathcal{U}}$ For each epoch e, \mathcal{U}_A and \mathcal{U}_B generate random EBIDs $D_{\mathcal{U}_A}^e$ and $D_{\mathcal{U}_B}^e$, respectively. \mathcal{U}_A and \mathcal{U}_B exchange their EBIDs and each of them executes the Set_CCM algorithm. \mathcal{U}_A (resp. \mathcal{U}_B) computes $m_{AB}^e =$ $D^e_{\mathcal{U}_A} * D^e_{\mathcal{U}_B}$ and sets the common contact element between \mathcal{U}_A and \mathcal{U}_B as $CCM^e_{AB} = \mathbf{H}(m^e_{AB})$.
 - S_PSign_S After checking that he receives two copies of CCM^e_{AB} , the server picks at random $r_s \leftarrow \mathbb{Z}^*_n$ and, relying on his secret key sk_S , he computes the two messages

 \mathtt{PS}^e_{AB} and $\mathtt{PS'}^e_{AB}$ such that

- $\mathsf{PS}^e_{AB} = \mathsf{CCM}^e_{AB} y_1 r_s + y_2 \quad and \quad \mathsf{PS'}^e_{AB} = \mathsf{CCM}^e_{AB} r_s$
- $P_Sign_{\mathcal{P}}$ We consider that when being requested by a user \mathcal{U}_A , the proxy opens a session and saves the user's identifier $ID_{\mathcal{U}_A}$. This latter is used when executing the P_Sign_P algorithm (c.f. Algorithm 3) to generate a new message M_{AB}^e (Line 4). The proxy then signs M_{AB}^e (Line 6 - Line 8) following the CSIG.Sign algorithm and finally generates a proof π (Line 10 – Line 16) w.r.t. the GSIG.Sign algorithm.

Algorithm 2 Join_ProxyGr_{P/GM} algorithm

- 1: **Input:** the security parameter λ and the secret key of the group manager sk_a
- 2: Output: the pair of keys of a proxy group member (sk_p, pk_p) and the signature σ_p over the public key the public pk_p
- 3: // The next is set by \mathcal{P}
- 4: pick at random $g_r, h_u \leftarrow \mathbb{G}_1^*, \gamma, \delta \leftarrow \mathbb{Z}_n^*$;
- 5: compute $g_{\gamma} \leftarrow g_r^{\gamma}$ and $h_{\delta} \leftarrow h_u^{\delta}$;
- 6: pick at random $\gamma_z, \delta_z \leftarrow \mathbb{Z}_n^*$;
- 7: compute $g_z \leftarrow g_r^{\gamma_z}$ and $h_z \leftarrow h_u^{\delta_z}$;
- 8: pick at random $\alpha, \beta \leftarrow \mathbb{Z}_n^*$;
- 9: set $pk_p = (g_z, h_z, g_r, h_u, g_2^{\alpha}, g_2^{\rho}, g_{\gamma}, h_{\delta})$ and $sk_p =$ $(\mathtt{pk}_{n}, \alpha, \beta, \gamma_{z}, \delta_{z}, \gamma, \delta);$
- 10: // The next is set by \mathcal{GM}
- 11: $\sigma_p \leftarrow \mathsf{XSIG}.\mathsf{Sign}(\mathsf{sk}_q, \mathsf{pk}_p);$
- 12: **return** $(\mathbf{sk}_p, \mathbf{pk}_p, \sigma_p)$

C. VERIFICATION PHASE

- Sig_Verify_{\mathcal{HA}} Given a contact list of user \mathcal{U}_A (a list of tuples (CCM, M, π) such that π can be parsed as $\{(\vec{\mathcal{A}}_i, \vec{\mathcal{B}}_i, \Gamma_i, t_i)\}_{i=1}^N, \{(\vec{\mathcal{C}}_i, \vec{\mathcal{D}}_i, \pi_i, \theta_i)\}_{i=1}^N\}, \mathcal{HA}$ verifies the validity of the group signature of each message, w.r.t. GSIG. Verify algorithm (cf. Appendix IV-D).
- CCM_Verify_{\mathcal{HA}} We consider that \mathcal{HA} requests from \mathcal{S} the message PS' corresponding to a contact message CCM contained in the contact list of user \mathcal{U}_A . The message PS' is taken as input with the message M (corresponding to CCM), the server's public key pk_S and the secret value $t_{\mathcal{U}_A}$ specific to user \mathcal{U}_A , to the CCM_Verify_{HA} algorithm that checks if the equation 3 holds:

$$\mathbf{M} = Y_1^{\ t_{\mathcal{U}_A} \mathbf{PS}'} Y_2^{\ t_{\mathcal{U}_A}} \tag{3}$$

VI. SECURITY AND PRIVACY ANALYSIS

In this section, we prove that SPOT achieves the defined security and privacy requirements with respect to the threat models defined in Section III-D, by relying on the following theorems and lemmas.

Theorem 1 (Unforgeability). If a probabilistic-polynomial time (PPT) adversary \mathcal{A} wins $\mathbf{E}xp_{\mathcal{A}}^{unforg}$, as defined in Section III-D1, with a non-negligible advantage ϵ , then a PPT

Algorithm 3 P_Sign_P algorithm

- Input: the public parameters of the proxies' group vk_g, the secret key sk_p, the signature σ_p over the proxy's public key, the identifier ID_{U_A} of user U_A and the message PS
- 2: **Output:** a message M, the corresponding signature σ_m and a proof π
- 3: // The next is executed by \mathcal{P} to generate M
- 4: compute $M = ID_{\mathcal{U}_A}^{PS}$;
- 5: // The next is executed by \mathcal{P} to sign M
- 6: pick at random $\zeta, \rho, \tau, \varphi, \omega \leftarrow \mathbb{Z}_n^*$;
- $\text{7: run } z = g_2^{\zeta}, r = g_2^{\alpha \rho \tau \gamma_z \zeta} \mathbb{M}^{-\gamma}, s = g_r^{\rho}, t = g_2^{\tau}, u = g_2^{\beta \varphi \omega \delta_z \zeta} \mathbb{M}^{-\delta}, v = h_u^{\varphi}, w = g_2^{\omega};$
- 8: set $\sigma_m = (z, r, s, t, u, v, w)$;
- 9: // The next is set to generate a proof on equations $\{(\vec{\mathcal{A}_{im}}, \vec{\mathcal{B}_{im}}, \Gamma_{im}, t_{im})\}_{i=1}^2$ where $\vec{\mathcal{A}_{im}} = \vec{\mathcal{B}_{im}} = \vec{0}, \Gamma_{im} = \mathcal{MAT}_{3\times 3}(1)$ for $i = 1, 2, t_{1m} = t_{2m} = 1_{\mathbb{G}_3}$
- 10: $\vec{\mathcal{X}}_{1m} = (g_z, g_r, s), \ \vec{\mathcal{X}}_{2m} = (h_z, h_u, v), \ \vec{\mathcal{Y}}_{1m} = (z, g_2^{\alpha \rho \tau \gamma_z \zeta}, t) \text{ and } \vec{\mathcal{Y}}_{2m} = (z, g_2^{\beta \rho \tau \delta_z \zeta}, w);$
- 11: $\pi_m = \{ (\mathcal{C}_{im}, \mathcal{D}_{im}, \pi_{im}, \theta_{im}) \}_{i=1}^2 \leftarrow \mathsf{NIWI}.\mathsf{Proof}(\mathsf{vk}_g, \{ (\mathcal{A}_{im}, \mathcal{B}_{im}, \Gamma_{im}, t_{im}) \}_{i=1}^2, \{ (\mathcal{X}_{im}, \mathcal{Y}_{im}) \}_{i=1}^2 \};$
- 12: // The next is set to generate a proof on equations $\{(\vec{\mathcal{A}}_{ip}, \vec{\mathcal{B}}_{ip}, \Gamma_{ip}, t_{ip})\}_{i=1}^{4}$ where $\vec{\mathcal{A}}_{1p} = (g_1^{\alpha_2}), \vec{\mathcal{A}}_{2p} = (g_1^{\beta_2}), \vec{\mathcal{A}}_{3p} = (g_{1z}, g_{1r}), \vec{\mathcal{A}}_{4p} = (h_{1z}, h_{1u}), \vec{\mathcal{B}}_{1p} = (g_{2z}, g_{2r}), \vec{\mathcal{B}}_{2p} = (h_{2z}, h_{2u}), \vec{\mathcal{B}}_{3p} = (g_2^{\alpha_1}), \vec{\mathcal{B}}_{4p} = (g_2^{\beta_1}), \Gamma_{1p} = (\gamma_{2z}, -1), \Gamma_{2p} = (\delta_{2z}, -1), \Gamma_{3p} = (\gamma_{1z}, -1), \Gamma_{4p} = (\delta_{1z}, -1), t_{1p} = e(g_1^{\alpha_2}, g_{2r}), t_{2p} = e(g_1^{\beta_2}, h_{2u}), t_{3p} = e(g_{1r}, g_2^{\alpha_1})$ and $t_{4p} = e(h_{1u}, g_2^{\beta_1})$
- $\vec{\mathcal{X}}_{1p} = (z_{1}, g_{1}^{\alpha_{2} \rho_{1}\tau_{1} \gamma_{2z}\zeta_{1}}), \quad \vec{\mathcal{X}}_{2p} = (z_{1}, g_{1}^{\beta_{2} \rho_{1}\tau_{1} \delta_{2z}\zeta_{1}}), \quad \vec{\mathcal{X}}_{3p} = (g_{1r}), \quad \vec{\mathcal{X}}_{4p} = (h_{1u}), \quad \vec{\mathcal{Y}}_{1p} = (g_{2r}), \quad \vec{\mathcal{Y}}_{2p} = (h_{2u}), \quad \vec{\mathcal{Y}}_{3p} = (z_{2}, g_{2}^{\alpha_{1} \rho_{2}\tau_{2} \gamma_{1z}\zeta_{2}}), \quad \text{and} \quad \vec{\mathcal{Y}}_{4p} = (z_{2}, g_{2}^{\beta_{1} \rho_{2}\tau_{2} \delta_{1z}\zeta_{2}}); \quad \vec{\mathcal{Y}}_{3p} = (z_{2}, g_{2}^{\beta_{1} \rho_{2}\tau_{2} \delta_{1z}\zeta_{2}});$
- 14: $\pi_p = \{(\vec{\mathcal{C}_{ip}}, \vec{\mathcal{D}_{ip}}, \pi_{ip}, \theta_{ip})\}_{i=1}^4 \leftarrow \mathsf{NIWI}.\mathsf{Proof}(\mathsf{vk}_g, \{(\vec{\mathcal{A}_{ip}}, \vec{\mathcal{B}_{ip}}, \Gamma_{ip}, t_{ip})\}_{i=1}^4, \{(\vec{\mathcal{X}_{ip}}, \vec{\mathcal{Y}_{ip}})\}_{i=1}^4);$
- 15: set $\pi_p = ((\pi_{ip}, \theta_{ip})_{i=1}^4)$;
- 16: set $\pi = (\pi_p, \pi_m)$;
- 17: return (M, σ_m, π)

simulator \mathcal{B} can be constructed to break the CDH assumption with a non-negligible advantage ϵ .

Proof. In this proof, we show that a simulator \mathcal{B} can be constructed with the help of an adversary \mathcal{A} having advantage ϵ against SPOT scheme.

The CDH challenger C sends to \mathcal{B} the tuple (g_2, g_2^a, g_2^b) , where $a, b \leftarrow \mathbb{Z}_n^*$ are randomly selected. C asks \mathcal{B} to compute g_2^{ab} . Then, \mathcal{B} sets $g_2^{t_{\mathcal{U}}}$ to g_2^a and $g_2^{y_2}$ to g_2^b . During the challenge phase, \mathcal{B} randomly selects $y_1 \in \mathbb{Z}_n^*$ and sends $g_2^{y_1}$ to \mathcal{A} as part of the server's public key. \mathcal{A} forges the partial signature over the message PS' and generates the message M* with advantage ϵ : M* = ID_{\mathcal{U}}^{PS^*} = g_2^{t_{\mathcal{U}}(PS'y_1+y_2)}. The tuple $(g_2^{t_{\mathcal{U}}}, PS', M^*)$ is sent back to \mathcal{B} . Upon receiving this tuple and knowing y_1 , \mathcal{B} can compute the value of $g_2^{t_{\mathcal{U}}y_2}$ which is the same as g_2^{ab} and can then send the result to the CDH challenger. As such, \mathcal{B} succeeds the forgery against the CDH assumption with advantage ϵ .

Theorem 2 (Unlinkability). Our SPOT system achieves the unlinkability requirement with respect to the *group-signature unlinkability* and *multi-CCM unlinkability* properties.

We prove Theorem 2 through Lemma 3 and Lemma 4 with respect to *group-signature unlinkability* and *multi-CCM unlinkability* properties, respectively.

Lemma 3 (Group-signature unlinkability). SPOT satisfies the group signature unlinkability requirement with respect to the computational witness indistinguishability property of the NIWI proof. *Proof.* In this proof, the objective is to show that the adversary is not able to distinguish group signatures issued by the same proxy. For this purpose, we suppose that, for each session *i*, the adversary receives the message M^* (i.e., the same message M^* is returned by each oracle) and the NIWI proof $\pi^i = (\pi^i_m, \pi^i_p) = ((\pi^i_j, \theta^i_j, \theta^i_{j=1}), (\pi^i_{jp}, \theta^i_{jp})_{j=1}^4)$.

To simplify the proof, we will only consider the NIWI proof π_m^i , as the statements used to generate the proofs π_p^i do not give any information about the proxy generating the proof (i.e., statements do not include the proxy's public key). Thus, for each session *i*, the adversary is given the tuples $(C_{k1}^i, D_{k1}^i, \pi_{k1}^i, \theta_{k1}^i)$ and $(C_{k2}^i, D_{k2}^i, \pi_{k2}^i, \theta_{k2}^i)$ referred to as the group signature generated by a proxy P_k , where $k \in \{0, 1\}$. During the challenge phase, the adversary is also given two group signatures. The first signature is represented by the tuples $(C_{k1}^i, D_{11}^i, \pi_{11}^*, \theta_{11}^*)$ and $(C_{22}^i, D_{22}^i, \pi_{22}^*, \theta_{22}^*)$ generated by a proxy \mathcal{P}_0 , while the second one is represented by the tuples $(C_{b1}^i, D_{b1}^i, \pi_{b1}^*, \theta_{b1}^*)$ and $(C_{b2}^i, D_{b2}^i, \pi_{b2}^*, \theta_{b2}^*)$ and is generated by a proxy \mathcal{P}_b ($b \in \{0, 1\}$).

Let us consider a simulator \mathcal{B} that can be constructed with the help of an adversary \mathcal{A} having advantage ϵ against SPOT scheme. A challenger \mathcal{C} selects two couples of witnesses (X_0, Y_0) and (X_1, Y_1) . \mathcal{C} computes a commitment (C, D)over (X_0, Y_0) , and then selects a bit $b \in \{0, 1\}$ and computes a commitment (C'_b, D'_b) over (X_b, Y_b) . \mathcal{C} asks \mathcal{B} to guess the bit b. Then, \mathcal{B} selects the tuples $(\mathcal{A}, \mathcal{B}, \Gamma, t)$ and $(\mathcal{A}'_b, \mathcal{B}'_b, \Gamma'_b, t'_b)$ and computes the proofs (π, θ) and (π'_b, θ'_b) . \mathcal{B} returns the two proofs to \mathcal{A} . Finally, \mathcal{A} outputs a bit b' that it sends to \mathcal{B} . This latter outputs the same bit b' to its own challenger C. As such, A succeeds in breaking the group-signature unlinkability with advantage ϵ , which is the same as breaking the computational witness-indistinguishability property.

Corollary 3.1. If SPOT satisfies the unlinkability property, then the proxies' group signature (i.e., NIWI proof) fulfills the anonymity requirement stating that it is not possible to identify the proxy that issued a particular group signature.

Lemma 4 (Multi-CCM unlinkability). **SPOT** satisfies the multi-CCM unlinkability requirement with respect to the common contact message structure.

Sketch of proof. Let \mathcal{A} be a successful adversary against the multi-CCM unlinkability property. Assume that \mathcal{A} receives two messages $CCM_1 = \mathbf{H}(D_i * D_j)$ and $CCM_2 = \mathbf{H}(D_i * D_k)$ (with $j \neq k$) meaning that user U_i met U_j and U_k , then \mathcal{A} is not able to link CCM_1 and CCM_2 to the same user \mathcal{U}_i as all EBIDs are randomly generated in each epoch e, and the hashing function \mathbf{H} behaves as a pseudo-random function.

Theorem 5 (Anonymity). SPOT satisfies the anonymity property, in the sense of Definition 3, if and only if, the CCM-unlinkability requirement is fulfilled.

Sketch of proof. We prove that our proximity-based protocol SPOT satisfies the anonymity property using an *absurdum* reasoning. We suppose that an adversary \mathcal{A} can break the anonymity of SPOT, in the sense of Definition 3, by reaching the advantage $Pr[\mathbf{E}xp_{\mathcal{A}}^{anon}(1^{\lambda})=1] \geq \frac{1}{2} \pm \kappa(\lambda)$. \mathcal{A} is given the pair of public-private keys $(pk_{\mathcal{HA}}, sk_{\mathcal{HA}})$ of the health authority, the identifiers $ID_{\mathcal{U}}$ of all users and a contact list of a particular user \mathcal{U}_A , obtained when relying on several sessions. Then, relying on the *left-or-right* LoRCU oracle, A tries to distinguish the user \mathcal{U}_b being in contact with \mathcal{U}_A , better than a flipping coin. That is, given the tuple $(CCM_b^*, M_b^*, \pi_b^*), A$ successfully predicts the identifier ID_{U_b} . Obviously, A tries to identify user \mathcal{U}_b relying on the message CCM_b^* , since both \mathbb{M}_{b}^{*} and π_{b}^{*} are generated based on CCM_{b}^{*} and give no further information about the user \mathcal{U}_b . This refers to link the message CCM_{b}^{*} to its issuer \mathcal{U}_{b} . Thus, if \mathcal{A} succeeds, this means that \mathcal{A} is able to link two or several common contact messages to the same user, which contradicts the multi-CCM unlinkability property previously discussed. As such, we prove that the adversary succeeds $\mathbf{E}xp_{\mathcal{A}}^{anon}(1^{\lambda})$ with a probability Pr = $\frac{1}{2} \pm \kappa(\lambda)$, where $\kappa(\lambda)$ is negligible. Thus, SPOT satisfies anonymity.

Theorem 6 (Anti-replay). SPOT satisfies the anti-replay requirement and supports false positive hindrance, if the proposed scheme is unforgeable.

Sketch of proof. To successfully replay a common contact message generated in an epoch e, in another epoch $e' \neq e$, a malicious user can perform in two ways. (i) The user

reinserts, in his contact list, the tuple (CCM^e, M^e, π^{e}) generated in an epoch e. The reinsertion is performed in an epoch $e' > e + \Delta^{11}$. Afterwards, the contact list is sent to \mathcal{HA} when the user is infected. \mathcal{HA} asks the server to provide the message PS' corresponding to CCM^e . As the server has no entry corresponding to CCM^e in the last Δ days, the second verification performed by \mathcal{HA} does not hold and the tuple is rejected. (ii) We assume that, in an epoch $e' > e + \Delta$, the user is able to replay a message CCM^e with two different proxies and he successfully receives the corresponding message M and the group signature π . Thus, when the user is infected, the health authority validates false positives, but this has no impact on the computation of the risk score, as no user has the same entry in his contact list. As such, we can prove the resistance of SPOT against replay attacks.

VII. PERFORMANCE ANALYSIS

This section introduces SPOT test-bed, discusses the experimental results, presented in Table 3, and demonstrates the usability of the proposed construction for real world scenarios.

A. SPOT TEST-BED

For our experiments, we developed a prototype of the SPOT protocol that implements the three phases Sys_Init, Generation and Verification including the twelve algorithms¹². The tests are made on an Ubuntu 18.04.3 machine - with an Intel Core i7@1.30GHz - 4 cores processor and 8GBmemory. The twelve algorithms were implemented based on JAVA version 11, and the cryptographic library JPBC¹³. We evaluate the computation time of each algorithm relying on two types of bilinear pairings, i.e., type A and type F. The pairing type A is the fastest symmetric pairing type in the JPBC library constructed on the curve $y^2 = x^3 + x$ with an embedding degree equal to 2. The pairing type F is an asymmetric pairing type introduced by Barreto and Naehrig [2]. It has an embedding degree equal to 12. For the two types of pairing, we consider two different levels of security i.e., 112-bits and 128-bits security levels recommended by the US National Institute of Standards and Technology¹⁴ (NIST). Based on the selected cryptographic library and the implementation of Groth-Sahai proofs¹⁵, the SPOT test-bed is built with six main java classes, w.r.t. to the different entities of SPOT, referred to as TrustedAuthority.java, GroupManager.java, Proxy. java, HealthAuthority. java, User. java and Server. java. Each class encompasses the algorithms that are performed by the relevant entity as described in Section III-A. In order to obtain accurate measurements of the computation time, each algorithm is run 100 times. Thus, the computation

13 http://gas.dia.unisa.it/projects/jpbc/

14 http://keylength.com

¹⁵https://github.com/gijsvl/groth-sahai

¹¹It makes no sense to reinsert an element in an epoch $e' < e + \Delta$, as duplicated messages will be deleted either by the server or at the user's end-device.

¹²The source code is available at https://github.com/privteam/SPOT

times represent the mean of the 100 runs while considering a standard deviation of an order 10^{-2} .

B. COMMUNICATION AND COMPUTATION PERFORMANCES OF SPOT

This section first proposes a theoretical analysis of the communication cost. Then, it presents the experimental results of the implementation of SPOT algorithms.

As presented in Table 3, the communication cost is measured according to the size of the elements \mathbb{G}_1 , \mathbb{G}_2 , \mathbb{G}_3 and \mathbb{Z}_n exchanged between entities. Setup_ProxyGr and Join_ProxyGr are the most bandwidth consuming algorithms, however this result must be put into perspective as both algorithms are performed once. Other algorithms have acceptable communication overhead, in particular those performed repeatedly by the user, which proves the efficiency of SPOT.

From Table 3, it is worth noticing that the computation time depends on the selected pairings types and is strongly related to the security level. Some algorithms of the Sys_Init phase are consuming but they are limited to only one execution from a powerful trusted authority. For the Generation phase, the most consuming algorithm is P_Sign which requires 19 seconds (resp. 40 seconds) for pairing type A and 3 seconds (resp. 4 seconds) for pairing type F. The computation time of Set_CCM and S_PSign are negligible, which means that the user and the server are not required to have important computation capacities. Finally, to verify the correctness of a single contact message, the Verification phase requires approximately 7 seconds (resp. 37 seconds) for pairing type F.

It is clear that P_Sign and Sig_Verify are the most consuming algorithms in terms of computation time as they include a large number of exponentiations and pairing functions, however this result must be put into perspective as both the proxy and the health authority are assumed to have advanced hardware features. Table 3 also shows that the Sig_Verify algorithm run with pairing type A is faster than with pairing type F, as this latter requires excessive memory allocation and deallocation. The P_Sign algorithm has an opposite behavior where the execution with pairing type F is faster than pairing type A, which is compliant to the JPBC library benchmark¹⁶ showing that elementary functions of multiplication and exponentiation require less computation time for pairing type F.

From Table 3, we can deduce that the algorithms executed at the user's side, have very low computation and communication overhead, which confirms the usability of SPOT, even when being run on a smartphone with low capacities. For both consuming algorithms (P_Sign and Sig_Verify) that are repeatedly run, some performance improvement means are proposed in the next subsection.

C. IMPROVED PERFORMANCES WITH MULTITHREADING AND PREPROCESSING

For both computation consuming algorithms P_Sign and Sig_Verify (see Section VII-B), in an effort to make the computation time as efficient as possible, although they run on powerful SPOT entities, we rely on a two step improvement:

- **Multithreading:** applied to both P_Sign and Sig_Verify algorithms. It enables simultaneous multiple threads execution (e.g., the computation of the different parts of the NIWI proof for the P_Sign algorithm, the computation of either the different verification equations of the NIWI proof, or the two sides of each equation, for the Sig_Verify algorithm).
- **Preprocessing:** applied only to Sig_Verify algorithm. It enables to prepare in advance a value to be later paired several times, like the variables \mathcal{U} and \mathcal{V} which are used as input to pairing functions for each verification equation.

Figure 3 exposes the impacts of one or two combined improvements applied to P_Sign and Sig_Verify. From Figure 3a, we notice that multithreading reduces the computation time for P_Sign of approximately 35%, for the two types of pairing and the two levels of security. For Sig_Verify, Figure 3b shows that multithreading has a greater impact on the computation time (i.e., approximately 40% for pairing type A and 28% for pairing type F) than preprocessing (i.e., approximately 10% for pairing type A and 5% for pairing type F ¹⁷). The two combined improvements ensure a gain of almost 50% for pairing type A and 30% for pairing type F.

VIII. CONCLUSION

In this paper, a novel secure and privacy-preserving proximitybased SPOT protocol for e-healthcare systems is introduced. The objective of SPOT is to help governments and healthcare systems to deal with pandemics by automating the process of contact tracing, with security guarantees against fake contacts injection and privacy preservation for users. Thanks to the underlying network architecture relying on a centralized computing server and decentralized proxies, SPOT enables users to determine whether they were in close proximity with infected people, with no risk of false positive alerts. The strength of the paper is to provide a full concrete construction of SPOT which is proven to be secure and to support several privacy properties under standard assumptions. Another strength of the contribution is a PoC of SPOT including a full implementation of the different algorithms, where practical computation costs measurements demonstrate the feasibility of our proposed protocol.

Further research will consider aggregating the verification of multiple contact messages in an effort to improve verification performances.

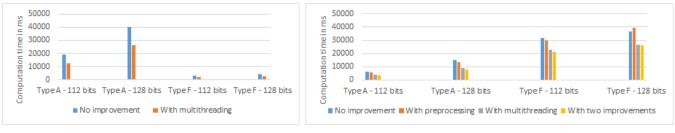
¹⁶http://gas.dia.unisa.it/projects/jpbc/benchmark.html

 $^{^{17}\}mbox{For type F}$ - 128 bits, the preprocessing decreases the performances. This is due to the excessive memory allocation and deallocation required by the pairing type F.

| Algorithm | Entity | Synch/Asynch | Communication cost | Computation time (ms) | | | | |
|-------------------------|----------------------------|--------------|---|-----------------------|------------|------------|------------|--|
| Aigorium | | | Communication cost | A/112-bits | A/128-bits | F/112-bits | F/128-bits | |
| Set_params | \mathcal{TA} | Asynch. | $ \mathbb{Z}_n + \mathbb{G}_1 + \mathbb{G}_2 + \mathbb{G}_3 $ | 874 | 2521 | 1230 | 1364 | |
| HA_Keygen | \mathcal{TA} | Asynch. | $ \mathbb{G}_1 $ | 59 | 123 | 12 | 16 | |
| S_Keygen | \mathcal{TA} | Asynch. | $2 \mathbb{G}_2 $ | 119 | 244 | 24 | 31 | |
| Setup_ProxyGr | \mathcal{GM} | Asynch. | $21(\mathbb{G}_1 + \mathbb{G}_2)$ | 1955 | 4075 | 346 | 451 | |
| Join_ProxyGr | \mathcal{P}/\mathcal{GM} | Synch. | $\mathcal{P}: 8 \mathbb{G}_1 + 2 \mathbb{G}_2 / \mathcal{GM}: 7(\mathbb{G}_1 + \mathbb{G}_2)$ | 2861 | 6014 | 1159 | 1409 | |
| Set_UserID | \mathcal{HA} | Synch. | $ \mathbb{G}_2 $ | 58 | 121 | 12 | 16 | |
| Userkeygen | U | Asynch. | $ \mathbb{G}_2 $ | 117 | 242 | 24 | 31 | |
| Set_CCM | U | Synch. | $ \mathbb{Z}_n $ | 0.1 | 0.1 | 0.1 | 0.1 | |
| S_PSign ^a | S | Synch. | $ \mathbb{Z}_n $ | 0.1 | 0.08 | 0.02 | 0.02 | |
| P_Sign ^a | \mathcal{P} | Synch. | $6 \mathbb{G}_1 +7 \mathbb{G}_2 $ | 19353 | 40371 | 3164 | 4170 | |
| Sig_Verify ^a | \mathcal{HA} | Asynch. | N.A. | 6541 | 15406 | 31637 | 36892 | |
| CCM_Verify ^a | \mathcal{HA} | Asynch. | N.A. | 174 | 360 | 148 | 190 | |

| TABLE 3. Con | putation time and | communication | overhead | of SPOT | algorithms |
|---------------|--------------------|---------------|----------|---------|------------|
| IADLE J. COII | iputation time and | communication | Overneau | U SFOI | algoriumis |

NOTE: Synch./Asynch. indicates whether the algorithm must be run online (i.e., in real time) or offline (i.e., later); ^{*a*} indicates that the algorithm is performed on a single contact message that is generated by the Set_CCM algorithm; $|\mathbb{G}_1|$ (resp. $|\mathbb{G}_2|$, $|\mathbb{G}_3|$ and $|\mathbb{Z}_n|$) indicates the size of an element in \mathbb{G}_1 (resp. \mathbb{G}_2 , \mathbb{G}_3 and \mathbb{Z}_n); N.A. is the abbreviation for Not Applicable.



(a) Influence of multithreading on P_Sign algorithm

(b) Influence of preprocessing or/and multithreading on Sig_Verify algorithm

FIGURE 3: Influence of improvements on P_Sign and Sig_Verify algorithms

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APPENDIX. NON-INTERACTIVE WITNESS INDISTINGUISHABLE PROOF

In this section we represent the Groth-Sahai NIWI proof scheme applied on pairing product equations with an asymmetric bilinear map. Witness-indistinguishability implies that the verifier of a group signature is not able to find the group member that has generated the signature. The NIWI scheme we consider, involves four PPT algorithms (NIWI.Setup, NIWI.CRS, NIWI.Proof, NIWI.Verify):

NIWI.Setup: This algorithm outputs a setup (gk, sk) such that $gk = (n, \mathbb{G}_1, \mathbb{G}_2, \mathbb{G}_3, g_1, g_2, e)$ and sk = (p, q) where n = pq.

NIWI.CRS: This algorithm generates a common reference string CRS. It takes (gk, sk) as inputs and produces CRS = $(\mathbb{G}_1, \mathbb{G}_2, \mathbb{G}_3, e, \iota_1, p_1, \iota_2, p_2, \iota_3, p_3, \mathcal{U}, \mathcal{V})$, where $\mathcal{U} = rg_1$, $\mathcal{V} = sg_2$; $r, s \in \mathbb{Z}_n^*$ and

NIWI.Proof: This algorithm generates a NIWI proof for satisfiability of a set of pairing product equations of the form of

$$\prod_{i=1}^{l} e(\mathcal{A}_i, \mathcal{Y}_i) \prod_{i=1}^{k} e(\mathcal{X}_i, \mathcal{B}_i) \prod_{i=1}^{k} \prod_{j=1}^{l} e(\mathcal{X}_i, \mathcal{Y}_j)^{\gamma_{ij}} = t$$

also written as

$$(\vec{\mathcal{A}} \cdot \vec{\mathcal{Y}})(\vec{\mathcal{X}} \cdot \vec{\mathcal{B}})(\vec{\mathcal{X}} \cdot \Gamma \vec{\mathcal{Y}}) = t$$

It takes as input gk, CRS and a list of pairing product equations $\{(\vec{\mathcal{A}}_i, \vec{\mathcal{B}}_i, \Gamma_i, t_i)\}_{i=1}^N$ and a satisfying witness $\vec{\mathcal{X}} \in \mathbb{G}_1^k, \vec{\mathcal{Y}} \in \mathbb{G}_2^l$. To generate a proof over a pairing product equation, the algorithm, first, picks at random $\mathcal{R} \leftarrow Vec_k(\mathbb{Z}_n)$ and $\mathcal{S} \leftarrow Vec_l(\mathbb{Z}_n)$, commits to all variables as $\vec{\mathcal{C}} := \vec{\mathcal{X}} + \mathcal{RU}$ and $\vec{\mathcal{D}} := \vec{\mathcal{Y}} + \mathcal{SV}$, and computes

$$\pi = \mathcal{R}^{\top} \iota_2(\vec{\mathcal{B}}) + \mathcal{R}^{\top} \Gamma \iota_2(\vec{\mathcal{Y}}) + \mathcal{R}^{\top} \Gamma \mathcal{S} \mathcal{V}$$
$$\theta = \mathcal{S}^{\top} \iota_1(\vec{\mathcal{A}}) + \mathcal{S}^{\top} \Gamma^{\top} \iota_1(\vec{\mathcal{X}})$$

The algorithm outputs the proof (π, θ) .

NIWI.Verify: This algorithm checks if the proof is valid. It takes gk, CRS, $\{(\vec{\mathcal{A}}_i, \vec{\mathcal{B}}_i, \Gamma_i, t_i)\}_{i=1}^N$ and $(\vec{\mathcal{C}}_i, \vec{\mathcal{D}}_i, \{(\pi_i, \theta_i)\}_{i=1}^N)$ as inputs and for each equation, checks the following equation:

$$e(\iota_1(\vec{\mathcal{A}}_i), \vec{\mathcal{D}}_i)e(\vec{\mathcal{C}}_i, \iota_2(\vec{\mathcal{B}}_i))e(\vec{\mathcal{C}}_i, \Gamma_i\vec{\mathcal{D}}_i) = \iota_3(t_i)e(\mathcal{U}, \pi_i)e(\theta_i, \mathcal{V})$$
(4)

The algorithm outputs 1 if the equation holds, else it outputs 0.



SOUHA MASMOUDI is currently a third year PhD candidate, under the supervision of Professor Maryline Laurent at Telecom SudParis, Institut Polytechnique de Paris. She is a member of the chair of Institut Mines-Telecom « Values and Policies of Personal Information ». Her thesis title is « Better management and control over multiple digital identities ». Her research addresses privacy and personal data protection concerns in identity management systems. Souha's research interests

include privacy-enhancing technologies and applied cryptography. She holds a Master degree in Systems and Network Security from Telecom SudParis. She also obtained the title of Expert in Information Systems Security (ESSI) from the National Agency for the Security of Information Systems (ANSSI) of France.



NESRINE KAANICHE, PhD is an Associate Professor in Cybersecurity at Télécom SudParis, Polytechnic Institute of Paris, France and an affialiate member of the interdisciplinary chair Values and Policies of Personal Information of Institute Mines Télécom, France. Previously, she was a lecturer in Cybersecurity at the Department of Computer Science, the University of Sheffield, UK, a Post-Doc researcher at Télécom SudParis, France and an International Fellow at SRI International.

San Francisco, CA, USA. Her major research interests include privacy enhancing technologies and applied cryptography for distributed systems and decentralised architectures, i.e., IoT, fog and clouds



MARYLINE LAURENT, PhD works as a Full Professor, Samovar lab, Télécom SudParis, Institut Polytechnique de Paris, France. She leads the RST department (Telecommunication Networks and services) of Télécom SudParis, and she is cofounder of the chair of Institut Mines-Télécom "Values and Policies of Personal Information". She is representative of France in the technical committee about security and privacy in the International Federation for Information Processing. She is area

editor of Annals of Telecommunication journal and member of the Editorial Board of Blockchain for Good, Frontiers in Blockchain. She is editor of several books including "Digital Identity Management". Her research topics are related to ethic by design, relying on Privacy Enhancing Technologies and applied cryptography, to satisfy both cybersecurity and privacy needs, for Internet of Things, clouds and identity management systems.

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