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# Analysis of experimental spectra of phosphine in the Tetradecad range near 2.3 µm using *ab initio* calculations

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#### **Abstract**

Due to its major interest for the chemistry of planetary atmospheres and exobiology, accurate spectroscopy data of phosphine are required for the search of signatures of this molecule in astronomical observations. In this work, high resolution infrared laboratory spectra of phosphine were analyzed for the first time in the full Tetradecad region (3769 -4763 cm<sup>-1</sup>) involving 26 rotationally resolved bands. Overall, 3242 lines were assigned in spectra previously recorded by Fourier transform spectroscopy at temperatures 200 K and 296 K, using a combined theoretical model based on ab initio calculations. The total nuclear motion Hamiltonian of PH3 including ab initio potential energy surface, was reduced to an effective Hamiltonian using the high-order contact transformation method adapted to vibrational polyads of the AB<sub>3</sub> symmetric top molecules, followed by empirical optimization of the parameters. At this step, the experimental line positions were reproduced with a standard deviation of 0.0026 cm<sup>-1</sup> that provided unambiguous identification of observed transitions. The effective dipole transition moments of the bands were obtained by fitting to the intensities obtained from variational calculations using the ab initio dipole moment surface. The assigned lines were used to newly determine 1609 experimental vibrationrotational levels up to  $J_{\text{max}}$ = 18 with energy in the range 3896-6037 cm<sup>-1</sup> that represents significant extension towards higher energies compared to previous works. Transitions for all 26 sublevels of the Tetradecad were identified but with noticeably fewer transitions for fourfold excited bands because of their weaker intensity. At the final step, pressure-broadened half widths were attached to each transition and a composite line list adopting ab initio intensities and empirical line positions corrected to the accuracy of about 0.001 cm<sup>-1</sup> for strong and medium transitions was validated against experimental spectra available in the literature.

#### 1. Introduction

Phosphine is a molecule of major interest for planetary atmospheres and exobiology. The search of its spectral signature in the microwave and infrared ranges has recently regained a strong attention in astronomical observation [1] [2] [3] [4] [5] [6] [7] [8] [9] [10] [11] [12]. It was found that phosphine is spectroscopically active and present in atmospheres of carbon stars [1] whereas some observed spectral features might be attributed to PH<sub>3</sub> also in brown dwarfs [2]. It was recently claimed [4] that PH<sub>3</sub> could represent a potential biosignature gas on anoxic (oxygen lacking) rocky planets or exoplanets. This is because on Earth, phosphine is associated with anaerobic ecosystems [4] [13] [14]. A particular role of phosphorus-bearing species in chemistry and biology was an incentive to find phosphine in the Venus atmosphere [4] [5] [6] [7] [8] [9] [10] [11] where an observation of PH<sub>3</sub> spectral signatures has become a controversial issue [7] [8] [9] [10] [11]. A surprising observation of phosphine in Venus using both the James Clerk Maxwell Telescope (JCMT) and the Atacama Large Millimeter Array (ALMA) facilities [4] [5] is yet to be confirmed [6] [7] [8] as no known process in the consensus model of atmosphere or geology could explain the presence of parts per billion PH<sub>3</sub> in Venus clouds [15]. Other hypotheses of phosphine anomalies as an extraordinary volcanism [16] [17] [18] or the biological explanation [4] [15] by analogy with biological production of PH3 on Earth are under discussion. "If the presence of PH3 in Venus' atmosphere is confirmed, it is highly likely to be the result of a process not previously considered plausible for Venusian conditions" [19]. Small concentrations (a few ppm) of phosphine occur in the atmospheres of Jupiter and Saturn [20] [21] [22] [23] [24]. In fact, PH<sub>3</sub> is expected to be well-mixed between the altitudes, yet the measurements for Saturn (e.g. at 0.5 bar sampled in the 10 µm range by Cassini/CIRS and at 2 - 3 bars in the 4.5 µm range by Cassini/VIMS) indicate a puzzling increase in their bulk abundance with altitude [25] As there are no known sources of PH<sub>3</sub> in the altitude range [26], such a finding is difficult to explain through atmospheric chemistry alone.

It seems to become a consensus in astrophysics, that other PH<sub>3</sub> spectral features should be sought [4], consequently an extension of accurate laboratory spectroscopy data of phosphine would be beneficial for further investigations in complementary spectral ranges. Note that recently developed methods using cross-correlation interpretation [27] [28] of astronomical observations require accurate high-resolution spectral data. Since the strongest bands (e.g. 4450 – 4650 cm<sup>-1</sup>) corresponding to so called Tetradecad rovibrational upper states are located in the 2.2  $\mu$ m region in the atmospheric window of the K band and they are fairly away from the strongest CH<sub>4</sub> bands (e.g.  $v_1+v_4$  and  $v_3+v_4$ ), the PH<sub>3</sub> Tetradecad bands

would be a good complementary region of interest for ground-based observations as well. These bands have not been assigned in laboratory experimental spectra because of the complexity in the rotationally resolved patterns. Corresponding line parameters are not yet available either in HITRAN [29], [30] GEISA [31] spectroscopic databases or *via* Virtual Atomic and Molecular Data Center (VAMDC) portal [32].

In this work, high resolution infrared laboratory spectra of phosphine recorded several decades ago at the National Solar Observatory on Kitt Peak in Arizona could be analyzed for the first time in the full Tetradecad region 3769 - 4763 cm<sup>-1</sup> involving 26 rotationally resolved bands using a theoretical model assisted with on *ab initio* calculations. The goal of the present work is to obtain an accurate theoretical modelling of these laboratory spectra in this range, to extent the knowledge of rovibrational levels towards higher energies and of line intensities for the corresponding transitions. In practical terms, we aim to provide an accurate and reliable line list for atmospheric remote sensing applications in the 2.3 µm region.

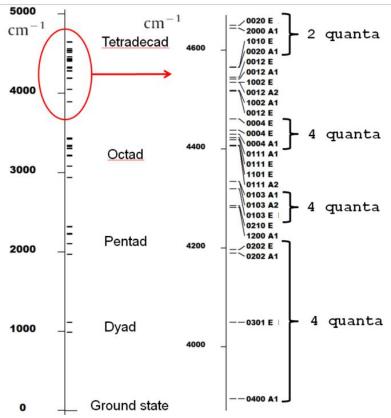
#### 2. Theoretical background and an overview of previous works

Phosphine (PH<sub>3</sub>) is a semi-rigid symmetric top molecule having four vibrational modes: two stretching non-degenerate modes  $v_1(A_1)$  and  $v_3(A_1)$  with frequency 2326.82 and 2321.14 cm<sup>-1</sup>, respectively, and the two doubly degenerate bending modes,  $v_2(E)$  and  $v_4(E)$  with a frequency of 1118.31 cm<sup>-1</sup>. Normal mode frequencies of PH<sub>3</sub> exhibit an approximate relation of stretching and bending frequencies,  $\omega_1 \approx \omega_3 \approx 2\omega_2 \approx 2\omega_4$ , resulting in vibrational levels being grouped into polyads. The vibrational energy levels with the same polyad number,  $P = 2V_1 + V_2 + 2V_3 + V_4$ , calculated from the four principal vibrational quantum numbers  $V_i$  fall within the same energy range. The first polyads including ground vibrational state (GS), Dyad, Pentad, Octad and Tetradecad are presented on **Fig. 1**. In this work, we study the phosphine absorption spectra belonging to the Tetradecad band system that correspond to  $(P=0) \rightarrow (P=4)$  bands.

Up to now, the four lower polyads up to the Octad (P=3) have been studied quite well and were included in the HITRAN [33] [29] and GEISA [31] databases. The HITRAN2020 database [33] includes a set of 104759 lines in the 0 - 3659.2657 cm<sup>-1</sup> range. Several bands in the PH<sub>3</sub> Octad were previously assigned [34] [35] [36] and theoretically modelled using an effective Hamiltonian and effective dipole transition moments. Recently, line positions and intensities of the Pentad bands (1500-2650 cm<sup>-1</sup>) have also been revised [37]. In addition, theoretical studies [38] [39] [40] [41] have provided variational predictions of transitions obtained from *ab initio* potential energy surfaces (PES) and dipole moment surfaces (DMS)

[42] [43] [40]. Sousa-Silva et al. [44] applied the DMS of Ref. [43] to rotation-vibrational calculations of PH<sub>3</sub> spectra at T=296 K [44] and at 1500 K [45] using the TROVE program [46]. Rey et al. [47] have calculated a theoretical list of lines at room temperature included in TheoReTS database and information system using the *ab initio* PES and DMS of Nikitin et al. [39] [40].

Formally, the definition of the phosphine polyads is similar to that of the methane polyads, though the resonance coupling interactions and the intensity distribution among the bands differ. The Tetradecad of phosphine consists of 14 vibrational bands divided into 26 vibrational sublevels, while in the case of methane there are 60 vibrational sublevels. Another difference is the localization of all two-quanta stretching vibration states at the top of the Tetradecad near 4600 cm<sup>-1</sup> above all three- and four-quanta vibration states (see **Fig. 1**) whereas the top of the methane Tetradecad is occupied by four-quanta states [48]. In the Tetradecad range, detailed analyses and theoretical modeling of high-resolution spectra of strongly coupled bands using purely empirical spectroscopic models become a complicated and tedious task. In case of methane, a full analysis of the Tetradecad bands has taken about fifteen years [49].



**Fig. 1.** Vibrational levels of the  $PH_3$  polyads (left side) and the vibrational sublevels of a part of Tetradecad (right side) corresponding to rovibrational bands analyzed in this work. The right hand side panel displays the principal vibration quantum numbers  $(V_1V_2V_3V_4)$ , symmetry types of vibration sublevels. The symmetry types correspond to irreducible representations of the  $C_{3v}$  point group.

With the advent of accurate electronic structure calculations approaching the spectroscopic accuracy, this process can be efficiently assisted by first-principle predictions of rovibrational energy levels, line intensities and the interaction parameters of the polyad models. In the present work, we use a combined approach based on *ab initio* calculations with a subsequent empirical optimization.

To this end, we use the contact transformation (CT) method that permitted deriving initial effective Hamiltonians from an ab initio PES as described in [50], [51], [48], [52]. Another complementary method using numerical transformation of the Hamiltonian matrix with the application to PH<sub>3</sub> was suggested in [53]. In this work, we have built a CT effective Hamiltonian ( $H^{eff}$ ) from the PES of Ref. [39] using a multi-step procedure. First, the full nuclear motion Hamiltonian of phosphine was reduced to an effective Hamiltonian using high-order CT method [48], [52] that included resonance coupling intra-polyad terms predicted from the ab initio PES. After that, this was expressed in the Irreducible Tensor Operators (ITO) formalism [54] [55] for a full account of symmetry properties for AB<sub>3</sub>-type molecules, following the procedure described in [56]. At this step, the technique of the transformation is similar to that for methane previously considered in [57]. Typical accuracy of direct calculations of low-J lines was within one wavenumber or even better, which allowed assigning a large part of the ro-vibrational patterns in the observed spectra. We proceeded then by a fine tuning of some  $H^{eff}$  parameters, for which the variations were statistically well determined during the empirical optimization of the model. Since then, the number of assigned lines was iteratively increased whereas the RMS deviation for line positions dropped down to 0.002 - 0.003 cm<sup>-1</sup>. This new CT-based effective Hamiltonian required less than half number of adjustable parameters with better predictive properties in comparison to purely empirical models [36].

The line intensities were computed in two steps.

First, variational calculations for line strengths were produced using our *ab initio* DMS of Ref. [40] in the normal-mode Eckart frame ITO representation according to the techniques described in [47]. This provided integrated intensities that agree with empirical values to about 2% for the Dyad and to 5-10% for the Pentad and Octad as discussed in [40]. A similar level of accuracy is achieved for strong lines. In cases of accidental resonances between nearby rovibrational states, the wavefunctions could be extremely sensitive to small errors in *ab initio* energy level calculations. Such small errors in energies may have a significant impact on the mixing coefficients of the wavefunction basis set expansions and thus produce erratic values in line strengths for the weaker transitions. This issue of "sensitive" (or

"unstable") line intensities in variational *ab initio* calculations is well-known for triatomic molecules [58] [59] and for larger molecules like methane [60]. A possible way to get rid of these erratic intensities of sensitive lines is a combined *ab initio*/effective model as discussed in [48], [52] for the methane polyads. Since the eigenvalues of the empirically optimized CT-based effective Hamiltonian match precisely experimental energy levels, the mixing of the basis set wavefunctions is also improved in the case of accidental resonances.

At the second step, we fit effective dipole transition moments of the bands to a subset of stable (non-perturbed by resonances) *ab initio* intensities produced by variational calculations and compute the entire set of transitions using the symmetry adapted MIRS code [61]. A comparison with experiment generally shows an improved agreement between theoretically simulated and experimental spectra.

#### 3 Positions and Intensities Analysis in the Tetradecad Range

Since the 80's a number of FTS spectra of phosphine was recorded at the Kitt Peak National US Observatory spectra in the range 1579-5700 cm<sup>-1</sup> (see Table 1 of Butler et al. [34] and Table 1 of Ref. [36]). These spectra (including several low temperature scans at 210 K) were used to study the Octad region near 3 µm [62], but as illustrated on Fig. 2, strong Tetradecad bands are also clearly visible near 2.2 µm region. In the present work, an experimental list was retrieved from the room temperature Kitt Peak spectrum with reference number 840801R002 recorded with a spectral resolution of 0.0115 cm<sup>-1</sup>. Line parameters of about 2000 lines with intensity above 5×10<sup>-24</sup> cm/molecule were retrieved using a multiline fitting program assuming a Voigt profile as line shape. As reliable values of the pressure and pathlength could not be obtained from the Kitt Peak archives files, absolute intensity values were obtained by scaling the fitted line areas. The scaling factor was obtained using the area of a ten of lines in the octad region measured in the same spectrum near 3400 cm<sup>-1</sup> for which absolute intensity values are provided in the HITRAN database [30]. In Fig. 2, the overview of the experimental stick spectrum is compared to the calculated spectrum. Note that the lines which appear to have experimental intensities largely overestimated compared to the calculated spectrum, are unresolved doublets which were considered as single line in the line profile fit.

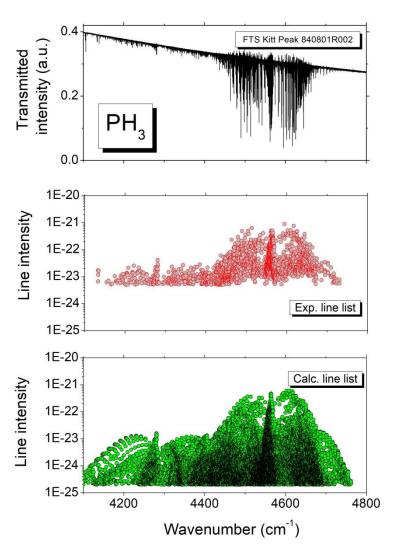


Figure 2
Upper panel: The room temperature phosphine spectrum near 2.2  $\mu$ m, recorded using the Kitt Peak FTS at 0.0115 cm<sup>-1</sup> resolution (Ref. 840801R002),

Middle panel: Experimental line list retrieved from the above FTS spectrum,

Lower panel: Tetradecad line list calculated in this work.

In the case of unresolved doublets, the experimental intensity values appear much larger than calculated.

Contrary to the first four PH<sub>3</sub> polyads, which have been well modeled [35] [34] [62], previous identification of Tetradecad energy levels is very sparse. To our knowledge, it is limited to a few upper states of the  $4v_2$ - $v_2$  hot band transitions that fall in the Octad range. Maki et al. [63] reported 84 transitions for the  $4v_2$ - $v_2$  hot band, later Butler et al. [34] extended the number of the assignments to 125.

The modeling of the positions of the phosphine Tetradecad was noticeably simpler than that of the methane Tetradecad because of the smaller number of vibrational degrees of freedom. In addition, phosphorus has only one stable isotope, <sup>31</sup>P, while natural methane

contains  $\sim 1\%$  of  $^{13}$ CH<sub>4</sub>. Together with the predictions using *ab initio* based calculations, this simplified the identification of the PH<sub>3</sub> spectra.

As discussed in the previous section, the cold Tetradecad bands were analyzed using an effective Hamiltonian constructed from the *ab initio* PES [39] by applying high-order contact transformations (CT) [48], [52] with a subsequent empirical optimization. First, the parameters specific to the lower polyads including the Octad [62] were slightly adjusted to line positions in the 1000-3600 cm<sup>-1</sup> range. This generally led to calculated low-J line positions of the Tetradecad bands down to an uncertainty of about 0.1 - 0.2 cm<sup>-1</sup>, except for few outliers. Together with information on line intensities predicted from our *ab initio* DMS [40] using variational calculations [47], [53], this permitted assigning iteratively 3242 new PH<sub>3</sub> lines up to J= 18. The RMS of the (obs.-calc.) deviation for these line positions in the range 3896-4763 cm<sup>-1</sup> has quite rapidly converged to 0.0026 cm<sup>-1</sup> after a fine tuning of a subset of H<sup>eff</sup> parameters, whereas more than a half of parameters were held fixed to the values derived from the *ab initio* PES *via* the CT-method.

As mentioned in [36] [62] for PH<sub>3</sub> Octad, an accurate measurements and fitting of intensities is a complex and laborious task, because of many blended lines in the crowded spectra and because the partial pressure of this unstable molecule degraded in the cell during observations. The accuracy of empirically fitted intensities in the Dyad and Octad ranges has been evaluated as about 10-12%. Comparison of simulated theoretical spectra using *ab initio* intensities with the experimental ones showed a similar or even better agreement in their absorption coefficients, at least for strong and medium lines.

Therefore, we employed in this work a combined approach, in which the parameters of the effective dipole transitions moments (EDTM) of the Tetradecad bands were determined from *ab initio* line intensities computed by variational method [40], [47], [53]. As explained in Section 2, we used for the EDTM fit a subset of "stable" line intensities that are not strongly perturbed by sharp accidental resonances. The full set of line intensities was computed using this EDTM and accurate rovibrational eigenfunctions of the empirically optimized  $H^{eff}$ . The resulting calculated line list made it possible to identify transitions for all 24 vibrational bands in the observed spectra. The fit statistics are shown in Table 1. Overall, a sufficient number of assignments was obtained in the studied range, except for the weakest bands  $3v_2+v_4$ ,  $2v_2+2v_4$ ,  $v_2+3v_4$  corresponding to four excited vibrational quanta. The EDTM parameters for the weak bands (all fourfold excited and some threefold excited vibrations) were fixed at zero since their absorption appeared to be mostly due to resonance intensity transfers from stronger bands. Note that the intensity distribution is quite different from that

of methane Tetradecad: the  $2v_3$  (E) band of phosphine is weak, while for methane the  $2v_3$  (E) and  $2v_3$  (F<sub>2</sub>) bands are the strongest bands.

**Table 1** Summary for the analyses of the Tetradecad PH<sub>3</sub> bands: line positions and intensity fit statistics.

Band	Band origin This Work	Band center [39]	Integrated Intensity (cmolecule)	#Positio	RMS	STD	$J_{min}$	$J_{max}$	#Intens	RMS
$2v_1$ (A1)	4644.6633	4646.50 <sup>a</sup>	2.8e-21	116	2.6	1.3	0	17	39	0.20
$v_1 + 2v_2$ (A1)	4282.4629	4283.96	1.1e-21	210	2.0	1.0	0	14	10	0.00
$v_1 + v_2 + v_4 (E)$	4407.7498	4408.36 <sup>b</sup>	9.5e-22	124	2.5	1.2	0	12	4	0.01
$v_1 + v_3$ (E)	4565.8215	4566.98	5.8e-20	765	2.4	1.2	0	18	103	0.11
$v_1 + 2 v_2$ (E)	4535.1834	4535.52	5.8e-21	203	2.5	1.2	1	15	33	0.10
$v_1 + 2 v_4$ (A1)	4518.5996	4516.94	3.0e-21	167	2.3	1.1	1	16	26	0.04
$4v_2$ (A1)	3896.0154	3895.75	9.7e-23	52	2.6	1.3	0	10	0	
$3v_2 + v_4$ (E)	4050.3521	4050.08	1.4e-23	3	6.3	3.1	4	8	0	
$2v_2+v_3$ (E)	4285.7254	4285.37	9.9e-22	338	2.0	1.0	0	14	0	
$2v_2+2v_4$ (E)	4197.0825	4196.57	1.7e-23	1	7.5	3.7	14	14	0	
$2v_2+2v_4$ (A1)	4189.7643	4189.36	4.7e-24	3	9.1	4.5	4	5	0	
$v_2 + v_3 + v_4 (A1)$	4423.1429	4422.59	1.4e-21	2	5.5	2.7	4	7	0	
$v_2 + v_3 + v_4 (A2)$	4406.4911	4406.08	3.6e-22	41	3.0	1.5	2	11	5	0.02
$v_2 + v_3 + v_4(E)$	4419.2725	$4419.50^{b}$	1.6e-22	179	2.9	1.4	1	12	17	0.05
$v_2 + 3 v_4$ (A1)	4335.0982	4334.15	1.4e-22	1	6.2	3.1	10	10	0	
$v_2 + 3 v_4$ (A2)	4334.5040	4333.65	2.4e-23	1	2.9	1.4	9	9	0	
$v_2 + 3 v_4$ (E)	4320.0009	4319.29	1.7e-23	12	4.6	2.3	1	10	0	
$2v_3$ (E)	4650.6412	4650.50	6.1e-22	10	6.7	3.3	5	11	0	
$2v_3$ (A1)	4565.5474	4566.86 <sup>a</sup>	1.9e-20	373	2.4	1.2	0	18	68	0.12
$v_3 + 2v_4$ (A1)	4541.5262	4541.11	5.3e-21	157	2.3	1.1	2	15	21	0.13
$v_3 + 2 v_4$ (E)	4517.4739	4516.94	5.3e-21	209	2.9	1.4	1	15	22	0.05
$v_3 + 2 v_4$ (A2)	4535.1144	4534.13	1.4e-21	44	2.9	1.4	3	13	7	0.04
$v_3 + 2 v_4$ (E)	4545.3069	4544.58	4.2e-21	179	2.9	1.4	1	16	45	0.12
$4v_4$ (E)	4461.4004	4459.91	5.0e-22	33	2.6	1.3	7	12	0	
$4v_4$ (E)	4438.0193	4436.82	1.3e-21	13	4.6	2.3	7	17	0	
$4v_4$ (A1)	4430.3124	4429.20	3.4e-22	6	6.2	3.1	3	9	0	
All			1.13e-19	3242	2.6	1.4			400	

#### Notes

The symmetry type of the upper vibration state is given in parentheses. RMS for line positions is given in units [0.001 cm<sup>-1</sup>]; STD is dimensionless weighted standard deviation; RMS for line intensities is in %. <sup>a,b</sup> the corresponding upper vibrational states are strongly mixed. Integrated intensity corresponds to the sum of calculated line intensities of a band up to cut-off of  $2\times10^{-25}$  cm/molecule.

Fig. 3 gives an example of experimental spectra and line assignments using the SpectraPlot program [64]. The two uppermost panels show the FTS spectra at 200 K and at room temperature [34], middle panel shows calculated spectra at 296 K with assignments in MIRS [61] format. The third and fourth panels shows the experimental list at 296 K and the calculated list at 296 K, respectively. Fig. 4 gives an example of experimental spectra and line assignments in the range of  $4v_2$ , which is presented in the same format as in Fig. 3 but with no

third panel. Traces of lines due to water (broadened by atmospheric air pressure) are noticeable at the right-hand side of **Fig .4**.

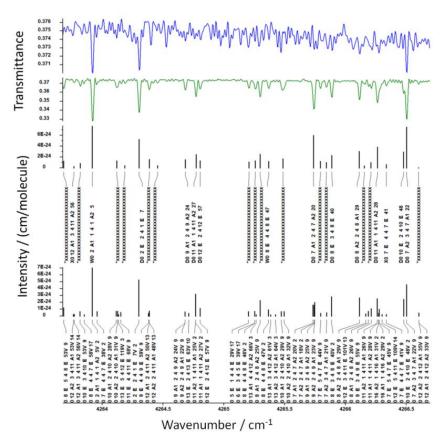
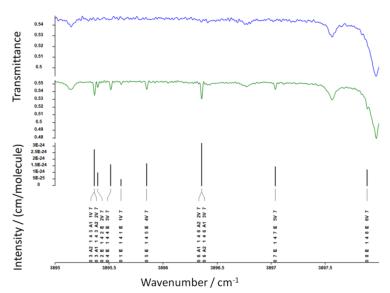


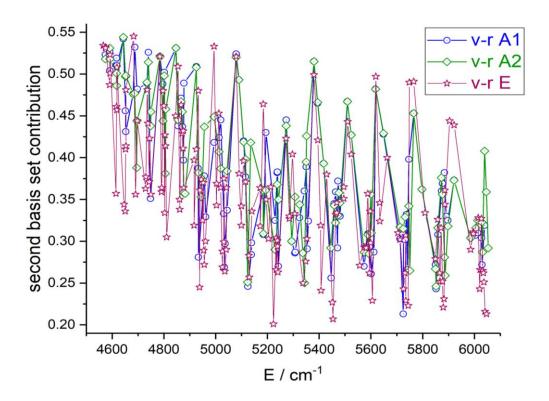
Fig. 3. Example of the PH<sub>3</sub> quantum assignment process using SpectraPlot program interface [64]. The upper panels show the FTS spectrum at 200 K (blue) and the second panel at room temperature [34] (green, 16.4 m optical path length). The third panel shows the sticks corresponding to the experimental line list at 296 K with assignments in MIRS [61] format. The fourth panel shows the sticks of our calculated lines at 296 K.



**Fig. 4.** Example of the  $4v_2$  band quantum assignment. The upper panels show the FTS spectrum: the first panel at 200 K (blue) and the second panel at room temperature [34] (green, 16.4 m optical path length). The third panel shows the sticks of our calculated lines at 296 K.

### 3. Vibration-rotation levels and resonance interactions among the Tetradecad states

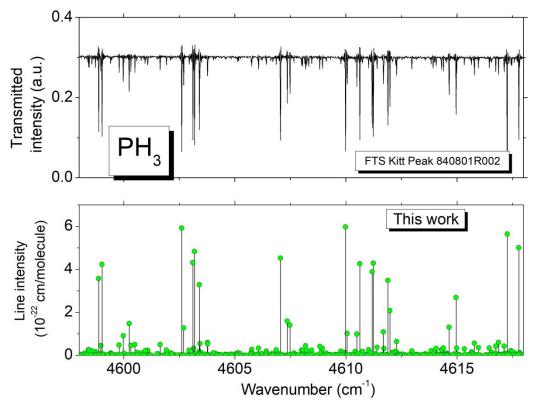
The assigned lines were used to determine new 1609 experimental vibration-rotational levels up to  $J_{\text{max}}$ = 18 with energy in the range 3896-6037 cm<sup>-1</sup> that represents a significant extension towards higher energies compared to previous works. In total, the set of empirically determined levels includes 313, 462, and 834 levels of  $A_1$ ,  $A_2$  and E rovibrational symmetry types, respectively. The experimental energies per vibrational sublevels are provided as a Supplementary Material file which includes the ro-vibrational assignment and three major contributions of the basis set function for each state. The assignment is given according to the first major coefficient of the expansion of the final wavefunctions in the rotation-vibration basis set. In some cases, the second and the third expansion coefficients have values comparable with the first one. This results from the quite strong and irregular couplings due to resonance interactions within the Tetradecad. An example of the variation of the absolute value of the second coefficient in the wavefunction expansion is plotted in **Fig. 5** between  $V_1V_2V_3V_4$  ( $\Gamma_v$ ) = 1010 (E) and 0020 (E) sublevels *versus* energy.



**Figure 5.** An example of the irregular behavior of the wavefunction coupling coefficients (absolute value of the second coefficient in the expansion in the basis set functions) between rovibrational states of  $V_1V_2V_3V_4$  ( $\Gamma_v$ ) = 1010 (E) and 0020 (E) sublevel versus rovibrational energy (upper panel) and the upper J value (lower pane): see the Supplementary Materials for more detailed information. Blue curve corresponds to A1-type, green curve to A2-type and red curve to E-type vibration-rotation levels.

#### 4. Combined line list for line positions and intensities

The line list for the Tetradecad transitions was constructed in two steps. First, the line positions and line intensities were computed using empirically optimized  $H^{eff}$  and the dipole transition moments of all bands fitted to "stable" *ab initio* intensities with the MIRS code [61]. The intensity cut-off was fixed to  $2\times10^{-25}$  cm/molecule. At this step, the RMS (obs.-calc.) deviation of the line position fit was 0.0026 cm<sup>-1</sup> for 3242 transitions. The average intensity uncertainty for strong lines is estimated as 5% by comparison of the simulated and observed spectra. At the second step, for all identified transitions, the calculated positions were replaced by the experimental ones. In addition, the positions of unassigned calculated transitions reaching determined upper state levels  $E_{upper}$  were replaced by ( $E_{upper} - E_{lower}$ ). This makes the line position accuracy to be about 0.001 cm<sup>-1</sup> or better for the most of strong and medium lines in the final list. The calculated list at 296 K including the assignments from the present work is provided as Supplementary Material. A typical example of agreement for line positions and intensities and experimental Kitt Peak spectrum in a blown up scale is given in Fig. 6.



**Figure 6.** An example of an agreement for line positions and intensities between our line list and a room temperature Kitt Peak spectrum (Ref. 840801R002).

A sample of the list is given in **Table 2**; this includes the rovibrational quantum assignments (the assignment notation is described in the notes of Table 3 of ref. [62]) and the lower state energies.

**Table 2.** An excerpt of Electronic Supplementary data: spectroscopic line parameters of PH<sub>3</sub> at 296 K with assignment in the 3769-4763 cm<sup>-1</sup> region.

Iso* v(cm <sup>-1</sup> ) <sup>a</sup>	-1\a	Int. (296 K) <sup>b</sup>	1£ 1 1337 C	air HW <sup>d</sup>	$E_{low}$	f	Rotational as	Vibr.	
	cm/molec.	self HW <sup>c</sup>	air HW "	cm <sup>-1</sup> e	$n^{J}$	Upper state	Lower state	stateh	
281	4349.03464	2.276E-25	0.072	0.104	386.6223	.61	4 8 7 E 112	0 9 5 E 3	0111A1
281	4349.15310	3.794E-25	0.063	0.094	787.7732	.57	4 14 6 A1 41	0 13 6 A2 3	1200A1
281	4349.15646	3.800E-25	0.063	0.094	787.7732	.57	4 14 6 A2 39	0 13 6 A1 3	1200A1
281	4349.16780	5.379E-25	0.068	0.098	566.8762	.59	4 12 7 A1 35	0 11 6 A2 2	0210E
281	4349.16786	5.379E-25	0.068	0.098	566.8762	.59	4 12 7 A2 33	0 11 6 A1 2	0210E
281	4349.22787	2.576E-24	0.053	0.091	628.0441	.58	4 11 10 E 135	0 12 11 E 1	0111E
281	4349.36179	4.439E-24	0.080	0.112	184.6638	.64	4 5 1 E 58	0 6 2 E 3	1101E
281	4349.42990	2.472E-24	0.077	0.102	294.0276	.62	4 9 8 E 45	0 8 7 E 2	0210E
281	4349.64044	3.834E-25	0.067	0.104	580.8453	.59	4 10 3 A1 77	0 11 3 A2 3	0004A1
281	4349.73405	5.822E-25	0.084	0.112	128.6891	.65	4 4 4 A2 19	0 5 3 A1 1	0111E
281	4349.73412	5.823E-25	0.084	0.112	128.6890	.65	4 4 4 A1 22	0 5 3 A2 1	0111E
281	4349.75651	2.068E-25	0.059	0.091	911.2002	.56	4 15 6 A2 45	0 14 6 A1 3	1200A1
281	4349.75904	2.074E-25	0.059	0.091	911.2002	.56	4 15 6 A1 43	0 14 6 A2 3	1200A1

#### Notes:

## 5. Insertion of pressure-broadened half widths and validation tests under atmospheric conditions

Devi et al. [37] reported that no significant vibrational dependence of the self-widths was observed between the Pentad  $(2v_4, v_1, v_3)$  and Dyad  $(v_2, v_4)$  regions for the transitions having identical rotational quantum numbers. Thus, we have introduced self- and N<sub>2</sub>-broadened half-widths in this Tetradecad region following the same procedure as in the Octad region [62]. Briefly, for self-widths, we have borrowed the self-width values measured for the  $v_3$  band by Devi et al. [37], by matching their quantum identifiers  $(J, K, \Delta J, \text{ and } \Delta K)$ . For the transitions having no match in their quantum assignments, their median values over K are adopted for the given J. For N<sub>2</sub>-broadening, we have adopted the measurements of Bouanich et al. [65] in the Dyad region. Either case, for the transitions with  $J \ge 18$ , a default value of 0.05 and 0.08 cm<sup>-1</sup>/atm was assumed, respectively. For the temperature dependence exponents

<sup>\*</sup> Molecule and Isotopologue number in the HITRAN notation, i.e. 281 for <sup>31</sup>PH<sub>3</sub>

<sup>&</sup>lt;sup>a</sup> calculated line positions

<sup>&</sup>lt;sup>b</sup> calculated line intensity at 296 K

<sup>&</sup>lt;sup>c</sup> Self-broadening coefficient in cm<sup>-1</sup>/atm (See Sec.3 for details)

<sup>&</sup>lt;sup>d</sup> Air-broadening coefficient in cm<sup>-1</sup>/atm (See Sec.3 for details)

<sup>&</sup>lt;sup>e</sup> Lower state energy in cm<sup>-1</sup>

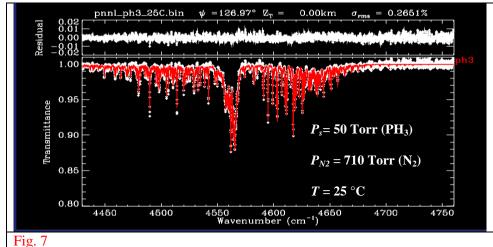
f. temperature dependence exponent of the air-broadening coefficient

<sup>&</sup>lt;sup>8</sup> Lower and upper state rovibrational assignments are given by the vibrational polyad number P, the rotational quantum number J, the rovibrational symmetry type  $C(C_{3v})$  irreducible representation and the ro-vibration ranking index  $\alpha$  [61]

<sup>&</sup>lt;sup>h</sup> Upper vibrational state

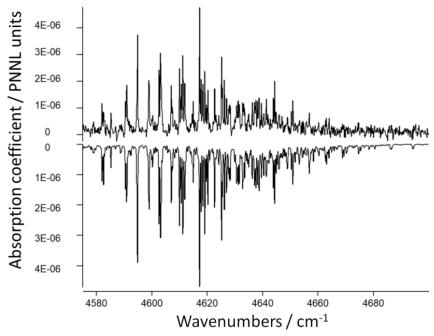
of the  $N_2$ -broadening coefficients, we have assumed a (0.72 - 0.01J) rotational dependence based on the work of [66] as was suggested by Butler et al. [34].

As part of a sanity check of the resulting line list, a synthetic spectrum based on the PNNL cross sections [67] [68] was calculated for 50 Torr of PH<sub>3</sub> diluted in 710 Torr of nitrogen at 25°C and compared with a spectrum generated with our line list. As presented in Fig. 7, the residuals are at the noise level (about 1% of the transmittance) across the spectral region, showing the good quality of the line list from the present work.



Comparison of the PNNL-cross section based spectrum (white) and a synthetic spectrum (red) generated with the current line list, showing their differences less than 1 % in the upper trace.

A more detailed "mirror-type" comparison is presented in **Fig. 8** for the upper part of the Tetradecad. This provides an independent confirmation of the high accuracy of the line list both in terms of line positions, intensities and line widths under atmospheric conditions. The line list can be useful for the next editions of the HITRAN [30] [29] and GEISA [31] databases.



**Fig. 8**Comparison of the PNNL absorption coefficients derived at 25°C [69] (upper pane) with the calculated values (lower pane) based on this work in the 4575-4700 cm<sup>-1</sup> region.

#### 6. Concluding remarks

So far, only global variational lists of ExoMol [45] and TheoReTS [47] lines have been available in the Tetradecad range of phosphine spectrum. The accuracy of line positions in such calculations is limited mainly by the accuracy of the PESs supporting vibration-rotation levels and also by the convergence of the variational methods linked to necessary truncation of infinite-dimensional Hamiltonian matrices. The first analysis of high resolution experimental phosphine spectra using combined ( $ab\ initio/H^{eff}$ ) model carried out in this work has permitted improving the accuracy of line positions by two or three orders of magnitude for the cold bands in the Tetradecad range.

A good agreement of *ab initio* intensities both with high-resolution Kitt Peak and medium resolution PNNL spectra provides a validation of the dipole moment surface [40], which was used in the calculations. The set of new 1609 Tetradecad levels deduced from experimental spectra extends the knowledge of vibration-rotation states towards higher energies in the range 3896-6037 cm<sup>-1</sup>. This will be useful for future assignments of high-temperature spectra in conditions typical for many astronomical observations.

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