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Eric Fantuzzi, Sandro Heuke, Simon Labouesse, Dominykas Gudavičius,

Randy Bartels, Anne Sentenac, Hervé Rigneault

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- Wide-field coherent anti-Stokes Raman
- scattering microscopy using random
- illuminations (CARS-RIM)
- ERIC M. FANTUZZI^{1,†}, SANDRO HEUKE^{1,†}, SIMON LABOUESSE², DOMINYKAS GUDAVIČIUS^{3,4}, RANDY BARTELS^{5,6,7}, ANNE
- SENTENAC^{1,*} AND HERVÉ RIGNEAULT^{1,*}
- ¹Aix Marseille Univ, CNRS, Centrale Marseille, Turing Center for Living Systems, Institut Fresnel, 7
- Marseille, France. 8
- ²Toulouse Université, CNRS, Centre de Biologie Intégrative, Toulouse, France
- ³Light Conversion, Keramiku st. 2B, LT-10233 Vilnius, Lithuania 10
- ⁴Cardiff University, School of Physics and Astronomy, The Parade, Cardiff CF24 3AA, United Kingdom. 11
- ⁵Colorado State University, Fort Collins, USA. 12
- ⁶Morgridge Institute for Research, Madison, WI USA USA. 13
- ⁷Department of Biomedical Engineering, University of Wisconsin, Madison Madison, WI USA. 14
- [†]Contributed equally. 15
- ^{*}Corresponding authors: anne.sentenac@fresnel.fr, herve.rigneault@fresnel.fr 16

Coherent Raman microscopy is the method of choice for label-free, real-Abstract: 17 time characterization of the chemical composition in biomedical samples. The common 18 implementation relies on scanning two tightly focused laser beams across the sample, which 19 20 frequently leads to sample damage and proves slow over large fields of view. The few existing wide-field techniques for their part, feature a reduced lateral resolution and do 21 not provide axial sectioning. To solve these practical limitations, we developed a robust 22 wide-field nonlinear microscope that combines Random Illumination Microscopy (RIM) 23 with coherent anti-Stokes Raman scattering (CARS) and sum frequency generation (SFG) 24 contrasts. Based on a comprehensive theoretical study, CARS-RIM provides super-resolved 25 reconstructions and optical sectioning of the sample from the second-order statistics of 26 multiple images obtained under different speckled illuminations. We experimentally show 27 that multimodal CARS-RIM and SFG-RIM achieve wide-field nonlinear imaging with a 28 3 micron axial sectioning capability and a 300 nm transverse resolution, while effectively 29 reducing the peak intensity at the sample compared to conventional point scanning CARS. 30 We exemplify the label free, highly contrasted, chemical imaging potential of CARS-RIM 31 and SFG-RIM wide-field microscopy in 2D, as well as 3D, for a variety of samples such as 32 beads, unstained human breast tissue, and a mixture of chemical compounds. 33

1. Introduction 34

Tissue and cell imaging heavily relies on the use of chemical markers, fluorescent probes or dyes, 35 to reveal different chemical species like DNA, proteins, or lipids. These staining techniques 36 are time consuming, may cause unwanted perturbations of the samples and are not adapted to 37 situations where markers cannot be used such as in some medical applications. Conversely, 38 label free microscopy techniques, such as coherent anti-Stokes Raman scattering (CARS), offer 39 chemical sensitivity, intrinsic 3D sampling, and real-time imaging within a limited field of view. 40 CARS is a spectroscopic technique based on a nonlinear four-wave mixing process that is sensitive 41 to the vibrational levels of chemical bonds [1]. In point scanning CARS microscopy [2], the 42 sample is illuminated by two high power laser beams (the pump and the Stokes) that are scanned 43 across the sample to produce an image from the CARS scattered power. Molecular-specific image 44 structure is obtained when the pump and Stokes frequency difference matches the frequency of 45 vibration of a given molecule. At this condition, the nonlinear light-matter interaction becomes 46

resonant within the targeted chemical bond and results in a surge of coherent radiation at a 47 third frequency (the anti-Stokes light) [3]. Because CARS detects molecular signatures without 48 requiring the introduction of labels, it has been extensively used for imaging of biochemical 49 constituents in a variety of samples ranging from material science to biology and medicine [4]. 50 CARS microscopy implemented with focused NIR beams provides good penetration in water, 51 high lateral resolution (\sim 300 nm) [2], and optical sectioning of \sim few microns. This explains 52 its growing success for chemical imaging of fixed or living biological samples [5–7] and more 53 recently for histological applications [8]. 54

In practice, CARS imaging is performed by scanning the sample with the superposition of 55 tightly focused pump and Stokes beams and the anti-Stokes light is collected with a light sensitive 56 detector, such as a photomultiplier tube. Signal is collected from each focus point in the sample 57 for long enough dwell time to reach a useful image quality. Speeding up the scanning process, to 58 cover large regions or for *in vivo* studies, requires the diminution of the detector integration time 59 per focus point and therefore leads to the inevitable increase of the laser powers to compensate 60 for the loss of anti-Stokes signal. Working at few images per second over few hundred microns 61 field of view requires tens to hundreds of milliwatts focused onto diffraction limited spots [5]. 62 These power levels are often above the photo-induced sample damage threshold [9], which limits 63 the illumination power and drastically restricts the scope of applications of rapid point scanning 64 CARS imaging. 65

To reduce the photo-toxicity, the excitation power can be dispersed over a large area of the 66 sample and then image the anti-Stokes light onto a camera. In this wide-field scheme, the 67 necessary long integration time is compensated by the simultaneous acquisition of the signal 68 on the multiple camera pixels. Several wide-field CARS microscopes were developed in which 69 the sample was illuminated by collimated pump and Stokes laser beams, either in a collinear or 70 folded-box geometry [10–13]. These schemes, however, introduced new difficulties. First, the 71 collimated illuminations at the sample plane lead to focused beams at the objective back-focal 72 plane, a situation that is likely to damage the optics when using high-peak laser power - see Fig. 1a. 73 Second, wide-field CARS does not provide the optical sectioning and transverse resolution of 74 point scanning CARS. 75

In this context, speckled illuminations, obtained by scattering coherent light with a diffuser, 76 seem ideally suited for replacing the collimated beams in a wide-field imaging configuration. 77 Speckles can be viewed as a multitude of randomly placed focused spots that probe the sample 78 in parallel, and that are suitable for achieving high resolution due to their wide spread in 79 spatial-frequency space. As the beam intensity is simultaneously spread across a large area in 80 both the spatial and spatial frequency domains, the power of the laser beams can be increased 81 without damaging the sample or the optics -a necessity for scaling the field of view. In this 82 work, we developed a wide-field CARS microscope that combines speckled illuminations with 83 the principles of random illumination microscopy (RIM) for precise computation of the sample 84 density. We show that random illumination CARS microscopy (CARS-RIM) achieves molecular 85 specificity with axial and transverse resolutions comparable to that of scanning-CARS, but 86 obtained in a wide-field configuration with reduced illumination peak intensity. 87

88 2. Theory of CARS-RIM

RIM was initially developed as a super-resolved wide-field fluorescence imaging technique in
which multiple images of a fluorescent sample are recorded under different random speckled
illuminations. A super-resolved image of the sample is recovered numerically from the variance
of the speckled images using a variance matching procedure based on the knowledge of the
speckle auto-correlation. It was shown that the RIM image processing doubles the transverse
resolution and provides an axial resolution comparable to that of an ideal confocal fluorescence
microscope [14–16]. The RIM concept was developed for incoherent imaging systems in which

the intensity recorded by the camera can be modeled as the sum of the intensities emitted by each 96 point-source of the sample. In particular, when the speckled illuminations are changed, the bright 97 spots corresponding to in-focus object planes show larger signal variations than the larger blurred 98 spots coming from out-of-focus object planes, Fig. 1c. However, CARS is a coherent scattering 99 process. The recorded image is a complex interference pattern of the fields radiated by all the 100 nonlinear induced CARS dipoles and there is no distinction between the out and in-focus sources, 101 Fig. 1b. Transferring the principles of RIM to coherent nonlinear microscopy is, therefore, not 102 straightforward. 103



Fig. 1. Challenges in nonlinear wide-field microscopy: a) a high power plane-wave illumination (in green) easily damages the objective lens while a wide-field speckled illumination (in blue) avoids focusing at any plane. b) In coherent imaging, interference between the coherent radiation arising from scatterers placed at different object planes (orange and purple) leads to a pronounced signal variation in the image camera plane. In incoherent imaging, the intensities stemming from the different sources are summed. The light coming from out of focus sources forms blurred spots at the camera plane and contributes less to the overall image variance. c) Optical sectioning in incoherent imaging using the variance of speckled images: when illuminated with varying speckle intensities, the image from in-focus scatterers (orange) leads to a larger frame to frame intensity variation (large standard deviation) than that of out of focus scatterers (purple).

In the following, we show how it is possible to take advantage of the independence between 104 the random speckled pump and Stokes beams involved in the CARS process to generate a 105 "quasi-incoherent" CARS emission. The idea is to vary rapidly the pump speckle while the Stokes 106 speckle is kept static such that each CARS active speckle grain, generated by the superposition 107 of pump and Stokes speckle grains, acquire a randomly and rapidly varying phase (due to the 108 rapidly changing pump speckle). If the resulting CARS speckle grain phase variation is fast 109 compared to the camera integration time, one expects the recorded CARS radiation to have some 110 similarity with the light stemming from incoherent sources. More precisely, the phase of two 111 CARS scatterers is fully random as soon as they are displaced from each other by more than 112 the square of the speckle pump grain. This combination was proposed more then ten years 113 ago by Heinrich et al [17] but in absence of theoretical grounds and of satisfactory results, 114 the approach was abandoned. In this work, we developed the theory of CARS imaging under 115 speckled illuminations. In brief, we modeled the CARS image obtained under fixed pump and 116 Stokes illuminations and derived its expression when the pump speckles are varied during the 117 camera integration time. Then, we studied the conditions under which this expression resembles 118 the fluorescence image model. 119

We consider a transmission microscope similar to the one presented schematically in Figs. 2a and 3. The sample is defined by its nonlinear susceptibility $\chi_{aS}^{(3)}$ and is illuminated by two co-propagating, fully developed, pump and Stokes speckled fields, E_p and E_S passing through condensers with numerical apertures NA_S and NA_p. For simplification, the susceptibility tensor and the excitation fields are assumed to be scalar. The pump and Stokes fields are modeled as random complex variables of zero mean and known correlation functions which depend on the numerical aperture of the illumination condenser objectives [18], $C_{p,S}(\mathbf{r_1} - \mathbf{r_2}) = \langle E_{p,S}(\mathbf{r_1})E_{p,S}^*(\mathbf{r_2})\rangle$, where $\langle \cdot \rangle$ stands for the averaging over different realizations of the speckles. The CARS emitted field, E_{aS} , is collected in the forward direction, through an objective of numerical aperture NA_{aS} and a tube lens, onto a camera. The CARS intensity, I_{aS} , at the pixel **R** of the image plane reads [19],

$$I_{aS}(\mathbf{R}) = |E_{aS}|^2(\mathbf{R}) = \left| \iiint G_{aS}(\mathbf{R}, \mathbf{r}) \chi_{aS}^{(3)}(\mathbf{r}) E_p^2(\mathbf{r}) E_S^*(\mathbf{r}) d\mathbf{r} \right|^2,$$
(1)

where $G_{aS}(\mathbf{R}, \mathbf{r})$ is the anti-Stokes Green function that describes propagation of the anti-Stokes field, with wavelength λ_{aS} , that is radiated from a point source located at \mathbf{r} in the sample and propagates to a point \mathbf{R} in the image plane. Note that the Fourier supports of G_{aS} , E_p and E_S are all caps of sphere defined by their radius $1/\lambda_{aS,S,p}$, with their projection onto the transverse (x, y) plane disks of radius NA_{aS,S,p}/ $\lambda_{aS,S,p}$. Also, the Fourier supports of C_p and C_S are the same as that of E_p and E_S (see the supplemental information 1 part 1).

As the pump and Stokes speckled beams are formed independently, by choosing a suitably long camera integration time, it is possible to record the average of I_{aS} over many realizations of the pump speckled field, while the Stokes field is kept constant. The intensity averaged over the pump speckles (denoted as $\langle \cdot \rangle_p$) reads,

$$\langle I_{aS} \rangle_{p} (\mathbf{R}) =$$

$$\iiint G_{aS}(\mathbf{R}, \mathbf{r}_{1}) \chi_{aS}^{(3)}(\mathbf{r}_{1}) E_{S}^{*}(\mathbf{r}_{1}) G_{aS}^{*}(\mathbf{R}, \mathbf{r}_{2}) \chi_{aS}^{(3)*}(\mathbf{r}_{2}) \langle E_{p}^{2}(\mathbf{r}_{1}) E_{p}^{2*}(\mathbf{r}_{2}) \rangle E_{S}(\mathbf{r}_{2}) d\mathbf{r}_{1} d\mathbf{r}_{2},$$
(2)

where a^* stands for the conjugate of a and $\langle E_p^2(\mathbf{r}_1)E_p^{2*}(\mathbf{r}_2)\rangle$, the characteristic function of the pump speckle grain, is equal to $2C_p^2(\mathbf{r}_1 - \mathbf{r}_2)$ [18]. Hereafter, the pump averaged image $\langle I_{aS}\rangle_p$ will be called a speckle-CARS image. It corresponds to the image that is recorded on the camera when the Stokes speckled illumination is static and the pump speckles vary rapidly during the integration time.

If the sample is made of isolated point-like scatterers that are separated by more than the width of C_p^2 , Eq. (2) can be simplified to,

$$\langle I_{aS} \rangle_{\mathbf{p}} \left(\mathbf{R} \right) = I_{aS}(\mathbf{R}) = 2I_p^2 \iiint |G_{aS}|^2 (\mathbf{R}, \mathbf{r}) |\chi_{aS}^{(3)}|^2 (\mathbf{r}) |E_S|^2 (\mathbf{r}) d\mathbf{r}.$$
(3)

Equation (3) corresponds to the model of a fluorescence image obtained under a speckled 148 illumination which is used in RIM [14, 16], $g_{as} = |G_{as}|^2$ is the standard fluorescence point 149 spread function at emission wavelength λ_{aS} , $|E_S|^2$ is the speckle intensity for each static Stokes 150 speckle illumination, and $|\chi_{aS}^{(3)}|^2$ is analogous to the fluorescence density. This result can be 151 understood by noting that each CARS point-scatterer is tagged by the uncorrelated random 152 phases of the pump field so that, when averaging over many pump speckled illuminations, the 153 field emitted by each CARS source add in intensity on the camera in the same way as that of 154 fluorophores. Yet, this result implicitly requires the sample to be sparse. Interestingly, and less 155 restrictively, we show in the supplementary information 1 part 1 that the same fluorescence-like 156 model can be obtained if $\chi_{aS}^{(3)}$ varies slowly in space over the width of C_p^2 . In this case, g_{aS} is slightly different and accounts for the coherent radiation of the CARS sources over the pump 157 158 speckle excitation grains. 159

Following the RIM approach, CARS-RIM requires the recording of multiple speckle-CARS images for different Stokes speckled illuminations. A first estimate of the sample, hereafter called

average-CARS, can be obtained by simply averaging these speckle-CARS images. Note that the 162 averaging can be implemented experimentally by simultaneously varying both the Stokes and 163 pump speckles during the camera integration time. Recalling that $\langle |E_S|^2 \rangle$, is constant throughout 164 the field of view, average-CARS $\langle \langle I_{aS} \rangle_{p} \rangle_{s}$, is similar to the image provided by a fluorescence 165 microscope using homogeneous illumination. The average-CARS image follows the model 166 of incoherent wide-field imaging, which is proportional to the sample density (here $|\chi_{\alpha s}^{(3)}|^2$) 167 convolved with g_{aS} . Because of the missing cone of the Fourier support of g_{aS} , average-CARS 168 does not provide optical sectioning. Yet, its resolution is expected to be better than that of 169 widefield 'coherent' microscopes using collimated laser beams (assimilated to plane waves). 170 Indeed, in coherent imaging, the image, given by the square of Eq. (1), is related to the sample 171 convolved with G_{aS} which has a significantly larger footprint than $g_{aS} = |G_{aS}|^2$ and explains 172 the poor lateral resolution of the existing widefield CARS microscopes. 173

In the RIM technique, the sample is not reconstructed from the average of the speckled images but from their variance [16]. In CARS-RIM, the variance of the speckle-CARS images reads,

$$\mathcal{V}[(I_{aS})](\mathbf{R}) = \iiint g_{aS}(\mathbf{R}, \mathbf{r}_1) |\chi_{aS}^{(3)}(\mathbf{r}_1)|^2 g_{aS}(\mathbf{R}, \mathbf{r}_2) |\chi_{aS}^{(3)}(\mathbf{r}_2)|^2 g_S(\mathbf{r}_1 - \mathbf{r}_2) d\mathbf{r}_1 d\mathbf{r}_2,$$
(4)

where $g_s = |C_S|^2$ is the autocorrelation of the Stokes speckle intensity. Since \mathcal{V} depends quadratically on $|\chi_{aS}^{(3)}|^2$, recovering the sample from the speckle-CARS image variance is a non-trivial operation. CARS-RIM uses an iterative reconstruction algorithm, algoRIM, that estimates $|\chi_{aS}^{(3)}|^2$ so as to minimize the distance between the empirical variance and its model, Eq. (4). AlgoRIM requires the knowledge of g_{aS} and g_S and is based on a fast calculation of Eq. (4), which is detailed in the supplementary information 1 part 2. In theory, algoRIM is able to recover the sample spatial frequencies over the Fourier support of g_{aS}^2 , which corresponds to the resolution of an ideal confocal fluorescence microscope [15].

To begin RIM iterative inversion procedure, the initial estimate of the sample is set as 184 the empirical standard deviation of the recorded speckle-CARS images. This simple data 185 processing, named DSI-CARS, in reference to the Dynamic Speckle Illumination approach (DSI) 186 in fluorescence microscopy [20] generally yields a better starting point than the average-CARS 187 image. The optical sectioning arises in DSI because at the camera imaging plane the incoherent 188 CARS speckle grains are in focus and the intensity for each camera pixel varies a lot for different 189 speckle illuminations. On the contrary for out of focus camera imaging plane, the blurred CARS 190 speckle grains generate poor camera pixel intensity variations for different speckle illuminations. 191 Indeed, we observed that DSI-CARS provided optical sectioning, as illustrated in Fig. 1c and in 192 the supplemental information 1 part 3. 193

194 3. Results

The axial and transverse resolutions of CARS-RIM reconstructions were first studied on synthetic 195 data obtained with a CARS microscope simulator [19]. In Fig. 2b, a simulated sample is 196 considered that is composed of an axially thin, homogeneous layer featuring a uniform transverse 197 spatial density of $|\chi_{aS}^{(3)}|^2$. CARS-RIM and average-CARS reconstructions were obtained for 198 different axial positions of the layer with respect to the detection focal plane, yielding a z-profile 199 of the sample. As expected, the average-CARS profile is a constant whereas the CARS-RIM 200 profile peaks when the thin layer is in focus. CARS-RIM axial resolution, given by the full 20 width at half maximum (FWHM) of the latter was about $\approx 1.6 \mu m$, which is close to that of a 202 confocal fluorescence microscope $1.4\lambda_{aS}/NA^2 = 1.78\mu m$ [21]. Note that in this particular case, 203 RIM iterative processing did not improve the z-profile given by the initial estimate, DSI-CARS, 204 because the full axial resolution gain had already been achieved. 205

²⁰⁶ The transverse resolution of CARS-RIM is studied in Fig. 2c. We considered a thin inhomoge-

²⁰⁷ neous layer in which the scatterer concentration formed a star-like pattern in the transverse plane.

208 CARS-RIM and average-CARS images were compared to the image provided by a coherent

²⁰⁹ widefied CARS microscope using Stokes and pump collimated beam illumination (plane waves)

²¹⁰ propagating along the optical axis. As expected, we observe a significant improvement of the

resolution from coherent CARS to average-CARS and from average-CARS to CARS-RIM.



Fig. 2. CARS-RIM *in silico*: a) Schematic representation of the CARS-RIM microscope using a diffuser to generate the pump speckles and a spatial light modulator (SLM) to generate the Stokes speckles. The sample is imaged on the camera sensor in transmission. b) Study of the axial resolution of CARS-RIM with a single homogeneous thin layer that is scanned along the z optical axis. Speckled images are recorded for different positions z_c of the layer with respect to the focal plane ($z_c = 0$). Average-CARS yields a constant intensity profile as a function of z_c whereas CARS-RIM profile peaks when the layer is in focus. c) Study of the transverse resolution. Images of a thin layer featuring star-like inhomogeneous nonlinear scatterer density placed in-focus for different wide-field CARS imaging modalities (i) plane wave illumination, (ii) average-CARS, which is superior to plane-wave CARS.

The analysis of the experimental performance of CARS-RIM was conducted on a home-made wide-field transmission microscope. A high-peak-power laser with a repetition rate of 515 kHz was used as the Stokes beam to drive the CARS four-wave-mixing process. The laser also pumped an optical parametric amplifier (OPA) to generate the color-tunable pump beam - see Fig. 3. The



Fig. 3. Experimental setup: - 1 High peak-power laser, 2 optical parametric amplifier (OPA), 3 fast spinning diffuser, 4 spatial light modulator (SLM), 5 excitation and collections optics with the sample in between, 6 CMOS camera. Right top corner: stack of speckle-CARS images for different Stokes speckled illuminations and their CARS-RIM reconstruction. The lower part of the figure shows from left to right: a pump speckle; a Stokes speckle; CARS raw image of an olive oil thin film obtained with a static pump and static Stokes speckle illuminations at 2850 cm⁻¹ CH₂ symmetric stretching vibration; speckle-CARS image obtained by averaging the CARS raw images over a large number of pump speckles (keeping the Stokes speckles static); average-CARS image obtained by averaging the CARS raw images over a large number of pump *and* Stokes speckles.

Stokes speckled patterns were generated by a Spatial Light Modulator (SLM), while the pump 216 speckles were formed through a rapidly spinning diffuser. Both the pump and Stokes beams 217 passed through the same condenser to illuminate the sample. The anti-Stokes light was detected 218 through a high-NA objective and was recorded with a camera placed at the image plane of a 4f 219 imaging system. The speckle-CARS images were obtained by keeping the Stokes speckled beam 220 static while averaging over the continuously varying pump speckles. The Stokes patterns were 221 changed with the SLM every 50 ms (20 Hz). Supplementary video 1 shows raw live CARS (and 222 SFG) images recorded by the camera with spinning pump speckle and 20Hz updating Stokes 223 speckle. Note that this video is intended to exemplify the data acquisition to perform CARS-RIM 224 (that require static Stokes speckle). Depending on the sample, the average-CARS or CARS-RIM 225 images were reconstructed using 600 to 2000 CARS speckle images. 226

The axial resolution of CARS-RIM was studied using a thin film of olive oil sandwiched 227 between two cover slips. The 3D image was obtained by translating the sample in steps of 1 µm 228 along the axial direction. As expected, CARS-RIM was able to localize the oil film contrary to 229 average-CARS, see Fig. 4a. The axial resolution of the reconstructed image stack, estimated from 230 its spatial frequency cut-off along the axial spatial frequency direction, was approximately 3 µm. 231 CARS-RIM 3D imaging was also tested on 30 µm diameter silica beads immersed in oil, see 232 Fig. 4b and the supplementary video 2. The CARS-RIM images at different depths, Fig. 4b (left) 233 are significantly crispier than that obtained with average-CARS. A set of CARS-RIM images 234 taken by translating the sample along the optical axis was processed to recover the 3D shape of 235 the spheres, Fig. 4b (right). 236



Fig. 4. Comparison between average-CARS, DSI-CARS, and CARS-RIM reconstructions of different samples represented schematically in the rightmost column. a) Average-CARS and CARS-RIM z-profiles of an approximately 5 μ m thick sheet of olive oil sandwiched between 2 cover slips. The spatial frequency cut-off of the profile was found to be ~ 1/3 μ m⁻¹, yielding an axial resolution of about 3 microns. b) 30 μ m diameter glass beads in olive oil imaged with CARS contrast at 2850 cm⁻¹ for two different depths (left) and CARS-RIM 3D reconstruction (right). The bead is clearly visible. c) Multi-lamellar vesicles imaged with CARS at 2850 cm⁻¹. d) Collagen tissue imaged with sum-frequency generation (SFG) contrast. In all cases, the CARS-RIM and SFG-RIM reconstructions are better resolved and better contrasted than average-CARS or DSI-CARS. The transverse resolution, was about 300 nm for the RIM images while an estimate of 650 nm was obtained for the average-CARS and -SFG images. In b), c) and d) are presented the average-CARS (or SFG) images, the standard deviation of the speckled images (DSI) and the RIM images. Average power in each beams ~250 mW. The white scale bar is 20 μ m.

The resolution gain of CARS-RIM was further explored with samples showing more pronounced 237 transverse spatial structure, such as multilamellar vesicles and human connective tissues, as 238 shown in Fig.4c,d. Note that in Fig.4d, the CARS-RIM technique was applied to sum-frequency 239 generation (SFG), this SFG contrast highlights the distribution of collagen in the sample. In the 240 SFG case, the optical filter behind the collection objective lens is changed to detect the light at a 241 frequency given by the sum of the pump and Stokes beam frequencies. The transverse resolution 242 of CARS-RIM and SFG-RIM images in Fig. 4c,d were estimated with image cross sections (data 243 not shown), to be 300 nm, while the resolution of average-CARS and average-SFG was estimated 244 at about 650 nm. As expected there is a two-fold improvement of the resolution between average 245 and RIM images. 246

The capability to excite both the CARS and SFG contrasts using the same experiment allowed 247 us to acquire multi-modal images with both of these modalities. Fig. 5a shows a mosaic image 248 of a 20 µm thick human breast tissue section covering the connective tissue and the epithelial 249 layer down to the stratum corneum. For each image tile in the figure, 2000 speckle-CARS and 250 speckle-SFG images were acquired sequentially. Clearly, CARS-RIM and SFG-RIM images 251 exhibited better optical sectioning and transverse resolution than average-CARS and average-SFG. 252 Lastly, in Fig. 5b, we show that the resolution gain of CARS-RIM is compatible with 253 spectroscopic applications. We imaged a mixture of a powder of polypropylene (PP) and 60 µm 254 diameter polystyrene beads (PS) that were suspended in deuterated water (D_2O). Speckle-CARS 255 images were acquired at the Raman resonance frequencies 2400 cm⁻¹, 2850 cm⁻¹ and 3050 cm⁻¹ 256 matching the stretching vibrations of D_2O , the methylene groups (-CH₂-) within PP and the 257 aromatic rings (=C-H) within PS, respectively. The CARS-RIM images nicely distinguished the 258 different chemical bonds. 259

260 4. Discussion

Wide-field nonlinear microscopy is still in its infancy, but the advent of high power lasers 261 oscillators and optical parametric amplifiers makes it a promising technique for imaging large 262 samples with molecular specificity at high acquisition rates. Up to now, the few attempts to 263 develop wide-field nonlinear imaging were plagued by plane wave illumination schemes leading 264 to (i) low spatial resolution, (ii) the lack of optical sectioning, and (iii) experimental difficulties 265 due to harmful beam focusing at the fragile back-focal plane of objective lenses. CARS-RIM 266 and SFG-RIM have broken free of these limitations. Using speckled illuminations followed by 267 statistical reconstruction, they provide images with (i) optical z sectioning and (ii) enhanced spatial 268 resolution as compared to plane-wave non-linear imaging. In the supplementary information 269 section 4 we show that for the same average power, a speckle wide-field illumination (with 270 independent pump and Stokes speckles) generates ~ 2 times more CARS signal than a plane-wave 271 illumination for thin samples. This is because the CARS signal generation in bright speckle 272 grains overcompensates for dark speckle grains due to the cubic dependency of the CARS signal 273 on the excitation fields. In addition, the speckle illumination scheme is harmless to the condenser 274 and objective lenses and is extremely resilient to beam misalignment and optical or specimen 275 aberrations. This is in sharp contrast with point scanning nonlinear microscopy that requires 276 delicate beam alignment, spatial beam superposition and low-aberration numerical condenser 277 objectives to activate the CARS and SFG contrasts. Furthermore, CARS-RIM reconstruction 278 algorithm needs only the spatial frequency support of the condenser to estimate the sample. 279 rather than the full complex pupil, including aberrations, that is required for widefield harmonic 280 optical tomography or ptychography [19, 22]. 281

²⁸² CARS-RIM microscopy is based on a theoretical analysis showing that averaging the CARS ²⁸³ signal over the pump speckles while keeping the Stokes speckled beam static can yield a ²⁸⁴ speckle-CARS image similar to that obtained in Random Illumination fluorescence Microscopy ²⁸⁵ (RIM), with $|\chi_{aS}^3|^2$ standing for the fluorescence density and the Stokes intensity standing for



Fig. 5. a) Multimodal imaging of connective tissue of a 20 μ m thick human skin sample. The CARS-RIM and SFG-RIM images (right column) are compared to average-CARS and average-SFG images. The composite image corresponds to the superposition of SFG and CARS signal. b) Spectroscopic CARS-RIM images of polystyrene beads in a suspension of polypropylene powder diluted in deuterated water. The CARS signal is detected at Raman resonances 2400cm⁻¹, 2850cm⁻¹ and 3050cm⁻¹ matching the stretching vibrations of deuterated water (D₂O), the methylene (-CH₂-) group within polypropylene (PP) and the aromatic =C-H breathing vibration of polystyrene (PS), respectively. Average power in each beams ~250 mW.

the speckled illumination [16]. The fluorescence-like model is valid for slowly varying samples 286 or dispersed point-scatterers. It requires the Stokes speckle grains to be much larger than the 287 pump grains (which is the case if the pump speckles are generated through an objective with a 288 numerical aperture close to unity). CARS-RIM statistical data processing consists in forming 289 the variance of multiple (600 to 2000) statistically independent speckle-CARS images obtained 290 under different random Stokes speckled patterns. It is shown that the variance is a complex 291 quadratic functional of $|\chi^3_{aS}|^2$, which depends on the Stokes speckle auto-correlation and the 292 anti-Stokes point spread function. These two functions are usually well-known and can be 293 computed or measured experimentally. The sample is then estimated iteratively by minimizing 294 the distance between the experimental variance and the variance model. It was demonstrated 295 that such data processing yields reconstructions that are linear to the sample with transverse resolution and optical sectioning comparable to that of a confocal microscope [14,15]. In practice, 297 CARS-RIM provided sample reconstructions with a resolution estimated to 3 µm axially and 0.3 298 um laterally, Fig. (4). These results place CARS-RIM spatial resolution at the level of scanning 299 CARS microscopy [2] with the advantage of a robust set-up requiring minimal control over the 300 co-propagating pump and Stokes speckled beams. 301

In our experimental implementation, the field of view was about $80 \times 80 \ \mu\text{m}^2$ and the temporal 302 resolution of CARS-RIM (using several hundred to thousands of speckled images) was about a 303 few tens of seconds, this is two orders of magnitude slower than state-of-the-art scanning CARS. 304 Yet, there is clear room for improvement. Faster SLMs and cameras could reduce the acquisition 305 time per speckled image to 1ms (instead of the present 50 ms). In addition, one could reduce 306 the number of speckle images per reconstruction to 50 at the cost of some granular artifacts in 307 the reconstruction due to the residual inhomogeneity of the illumination on average [16]. Using 308 complementary speckles [23] could help reduce these artifacts by forming a uniform illumination 309 with only few speckles. We expect that combining kHz SLMs and cameras as well as fast signal 310 processing would yield CARS-RIM images at a few frames per second. 311

Furthermore, we showed in the supplementary information section 4, that with our laser 312 average power and repetition rate, widefield CARS-RIM requires theoretically ~ 4 times lower 313 peak intensity density on the sample as compared to point scanning CARS (for equal total 314 CARS signal and equal acquisition time) leading to fewer toxic multi-photon absorption events. 315 Interestingly, we show that it is possible to adjust the laser parameters (average power and 316 repetition rate) of wide-field CARS to perform faster image acquisition than in point scanning 317 (for equal peak-intensity density), or to diminish the peak-intensity density (and the heating) for 318 an equal image acquisition time than in point scanning (see supplementary information sections 4 319 and 5). This versatility is not possible in point scanning CARS where the acquisition time and the 320 peak-intensity density (and its induced phototoxicity) cannot be dissociated. Finally, whereas only 321 1/3 of the pump and Stokes speckle grains overlap with pump and Stokes independent speckles, 322 we show that this leads to ~ 2 times more CARS signal than using plane wave illumination (see 323 supplementary information section 4). 324

CARS-RIM principle works for any two-color nonlinear process. In this work, it was applied 325 to CARS and non-degenerate three-wave mixing (SFG) imaging. Still, it could also be readily 326 extended to four-wave mixing processes such as non-degenerate third harmonic generation. We 327 obtained multimodal images of human skin samples where collagen (SFG signal), nuclei and 328 borders of epithelial cells (CARS signal) were clearly distinguished, Fig. (5)a. We believe these 329 multi-modal images could be diagnostically relevant [24, 25] and useful for medical applications. 330 In another experiment, the spectroscopic ability of CARS-RIM combined with its confocal axial 331 resolution permitted to distinguish beads embedded in a powder suspension, Fig. (5b), paving 332 the way towards three-dimensional spectroscopic analysis of materials in a wide-field scheme. 333 Implemented with the spectral focusing scheme [26,27] CARS-RIM could address a narrower 334 vibrational band and generate hyper-spectral images with reduced non-resonant background 335

contribution [28] enabling its potential for *in vivo* applications in biology and medical sciences.

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341 Author contributions

E.M.F prepared the samples and performed the experiments. S.H. conceived the idea, assisted the experiments and performed the numerical calculations. S. L. developed the RIM reconstruction algorithm, algoRIM. D.G. assisted the experiments and installed the laser source. A.S. conceived the idea and derived the analytical description of CARS-RIM with the help of R.B. H.R. conceived and supervised the project. S.H. A.S. H.R. R.B wrote the manuscript. All authors discussed the results and commented on the manuscript.

348 Competing financial interests

³⁴⁹ The authors declare no conflict of interest.

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419 Methods

420 4.1. Numerical Simulations

All the simulations of the CARS-RIM experiments were performed by calculating Eq. (1) and 421 using the image formation technique described in [19]. For simplicity, we approximated the 422 anti-Stokes susceptibility tensor by $\chi_{aS}^{(3)} \approx \chi_{aS,1111}^{(3)}$, implying that we only considered x-polarized light in excitation and detection. The pump and Stokes speckled beams were generated using 423 424 two independent masks placed at a conjugated image plane with random phases which were 425 uniformly distributed in $[0,2\pi]$ and random amplitude in [0,1]. Each wide-field speckle-CARS 426 image was obtained through the averaging over 800 distinct pump speckle patterns for one fixed 427 Stokes pattern. Then, 400 speckle-CARS images were generated for 400 different Stokes speckle 428 patterns. The numerical aperture (NA) of the excitation and detection objectives were set to 0.9 429 and the Stokes, pump and antiStokes wavelengths to 1030nm, 800nm and 654nm, matching our 430 experimental conditions. 431

432

433 4.2. CARS-RIM reconstruction procedure

434 All the CARS-RIM super-resolved images were obtained with the reconstruction code algoRIM

which is accessible at https://github.com/teamRIM/tutoRIM. The different steps of the recon-

- 436 struction procedures are detailed in the supplementary information 1 part 2. AlgoRIM requires
- 437 the knowledge of diffraction-limited g_{aS} and g_S with the experimental parameters NA_S , λ_S and

 438 NA_{aS}. The tuning of Tikhonov parameters required by algoRIM for dealing with the signal to 439 noise ratio of the speckled images was performed manually.

440 4.3. Experimental setup

The CARS-RIM setup is shown schematically in Fig. 3. The output of a Yb-based amplified 441 solid-state laser (Light Conversion, PHAROS; 150 fs, 20 W, 515 kHz, 1030 nm) is split into 2 442 parts. Part 1 serves as the Stokes beam to drive the CARS four-wave mixing process. The second 443 part is coupled into an optical parametric amplifier (OPA; Light Conversion, ORPHEUS-HP) 444 whose emission at 650 - 900 nm is used as the pump beam for the CARS generation. The 445 pump beam goes through the outer edge of a 2" diameter fast-spinning (\approx 5Hz) optical diffuser 446 (Thorlabs, DG20-220). The Stokes beam is centered onto a spatial light modulator (SLM, BNS, 447 HSPDM256-700-900) and recombined as well as temporally superimposed with the pump pulses 448 using a dichroic mirror (Thorlabs, DMSP900L) and a mechanical delay stage. The illuminated 449 spots at the diffuser and SLM are imaged by a 10x telescope (Thorlabs LA1509-B-ML; Nikon, 450 MBL71105, effective NA 0.9 under water immersion) onto the sample. The power at the sample 451 was approximately 250mW per color dispersed over a field of view larger than 80um. To obtain 452 3D images, the sample is moved along the optical axis using a motorized translation stage (PI. M-110.12S). Speckle CARS radiation is collected in forward direction by a 40x objective lens 454 (Nikon, PLAN, NA = 1.15, immersion: water), separated from the excitation wavelength by 455 dielectric filters (Thorlabs, FESH0700) and imaged by a second tube lens (Thorlabs, AC254-200-456 B-ML) onto a CMOS camera (Hamamatsu, ORCA-fusion, C14440). A Matlab-based control 457 software is used to switch between random phase-mask pattern of the SLM which is synchronized 458 to the trigger of the camera's readout. 459

460 4.4. Sample preparation

Preparation of the glass beads in oil: glass beads (diameter 30µm, ThermoFisher) were deposited
on a standard glass object older (thickness 1mm) and a droplet of oil (IMMOIL-F30CC, Olympus)
was added. The sample was sealed using a standard coverslip (thickness 170µm) but no spacer
was used to avoid floating of the beads along the direction of gravity.

Preparation of the lipid vesicles: The multilamellar vesicles were prepared following the instructions outlined in [29]. Briefly, the lipids (dissolved organic carbon (DOC), Avanti Polar 466 Lipids) are dissolved in chloroform within a beaker creating a 10mM solution. The organic 467 solvent is slowly evaporate using a stream of dry nitrogen. The resulting layer of lipids at the 468 bottom of the beaker is suspended in cyclohexane. Dry ice is added to freeze the mixture of lipids and cyclohexane. The solidified mixture is placed under high vacuum to remove the 470 cyclohexane. Multilamellar vesicles are obtained by dissolving the remnant lipids in an aqueous 471 buffer (Phosphate Buffered Saline, Sigma-Aldrich) for 30-60 minutes at room temperature. 472 Preparation of the multi-component sample: polystyrene beads (diameter 60 µm, Fluka Analyti-473

and polypropylene (PP, Sigma-Aldrich) powder were mixed and placed on a glass object
 holder. To match the refractive index and immobilize the sample, the mixture of powders were
 immersed in a solution of 1% of agarose (thermoscientific, TopVision Agarose) in deuterium

477 oxide (Sigma-Aldrich, deuteration degree min. 99.9%). A 100 μm thick spacer and a standard

⁴⁷⁸ coverslip has been used to seal the sample.

Preparation of the tissue sample: 20 µm thick unstained tissue sections from a surgery of a human
breast were provided by the public bio-bank hospital of La Timone hospital (Marseille, FR). A

481 droplet of de-ionized water was added on top of the tissue matching its refractive index in order to

reduce linear scattering of the sample. To avoid draining of the water and a potential contamina-

tion of the condenser lens, the tissue sample was sealed using a 100 µm thick spacer and a cover slip.

484

485 Data Availability

⁴⁸⁶ The data that support the findings of this study are available from the corresponding authors upon

487 request.