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A numerical model of thermoacoustic heat pumping inside a compact cavity

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Abstract – This paper presents a numerical study of thermoacoustic heat pumping along a stack of solid plates placed inside a compact cavity submitted to an oscillating flow. Velocity and pressure fields are controlled by two acoustic sources: a main “pressure” source monitoring the fluid compression and expansion phases, and a secondary “velocity” source generating the oscillating fluid motion. Numerical simulations are performed with an “in-house” code solving Navier–Stokes equations under a Low Mach number approximation in a two-dimensional geometry. In the linear regime, thermoacoustic heat pumping is correctly described with this model for different sets of parameters such as thermo-physical properties of the stack plates, amplitude of pressure oscillation or of the velocity source, phase shift between both sources. Numerical results on the normalized temperature difference established between the ends of stack plates are in excellent agreement with analytical estimates and experimental results published in the literature. Several configurations corresponding to different thermal conditions applied on the outside wall and an inside separation plate are then considered. If the separation plate is adiabatic, temperature varies linearly along the stack, recovering classical linear theory’s results. If the separation plate is thermally conductive, the model, providing detailed description of local heat and mass transfer, shows that the temperature field becomes fully two-dimensional and thermoacoustic heat pumping is less efficient. The model is well adapted to explore the influence of local heat transfer constraints on the heat pump efficiency and thus well suited for detailed analyses of more complex mechanisms such as buoyancy effects.

Keywords: Thermoacoustics, Low Mach number, Compact cavity, Numerical simulation, Thermoacoustic heat pump

1 Introduction

Thermoacoustic effect is a phenomenon of heat transport driven by acoustic oscillations. It occurs in the gas oscillating in the vicinity of a conducting solid, within viscous and thermal boundary layers. Thermoacoustic devices are used to generate either heat pumping for refrigerating purposes or mechanical work for engine operating purposes. The energy conversion takes place in a thermoacoustic core consisting of a stack of solid plates or a porous medium made of mesh grids or another geometry, placed between two heat exchangers. The thermoacoustic core is usually placed inside a closed resonator in which the gas is working at the fundamental resonant frequency associated with the geometry of the resonator [1–3].

Thermoacoustic engines and refrigerators are interesting for industrial applications because they are an ecological alternative of classical thermal machines, since they have very few moving parts, use inert gas and are simple to build.

They are however less competitive because of a much lower efficiency, which is limited by acoustics. For more than 30 years, different configurations have been studied for various types of resonators and thermoacoustic cores and coupling methods between engines and refrigerators. A wide variety of thermoacoustic devices were constructed in order to improve the overall performance for each application: cryogenics [4], air conditioning [5], domestic refrigeration, solar powered thermoacoustic engines [6], electric energy generators [7], waste heat recovery systems [8].

In the last 20 years efforts have focused on reducing the dimensions of the systems, especially for applications in cooling microelectronic components [9]. The present study deals with thermoacoustic refrigerating systems. When reducing the size of a device with a classical configuration, the resonance working frequency is significantly increased, and it is difficult to construct thermoacoustic cores well adapted to high frequencies, so that the resulting systems have limited performances [10]. A different design based

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1 on a co-axial travelling wave refrigerator [11] allowed to
2 reduce the resonator's length and to obtain a more compact
3 device with better performances than previously developed
4 standing-wave refrigerators (COP equal to 25% of the
5 Carnot COP, representing improvement by a factor of
6 two). Smith et al. [12] developed a more compact travel-
7 ling-wave system in which the resonator is replaced by a
8 hybrid acoustic-mechanical system.

9 Another solution was to eliminate completely the res-
10 onator and create the acoustic field needed in the thermoac-
11 oustic core with two acoustic sources inside a non resonant
12 compact cavity [13–15] (i.e. the cavity size is much smaller
13 than the wavelength associated to the frequency of the
14 acoustic sources). The main driver acts as a pressure source
15 and the second source is a loud-speaker acting as a velocity
16 source. The thermoacoustic core is a regenerator (mesh of
17 stainless steel screens) or a stack of solid plates placed
18 between heat exchangers. The overall geometry is coaxial
19 with a peripheral channel allowing a feedback flow. There-
20 fore the fluid can oscillate in this closed cavity in a similar
21 way as in a travelling wave system. The acoustic sources
22 are working at the same frequency and their amplitudes
23 and phases are tuned independently. The device can be
24 directly optimized by controlling the magnitude and phase
25 shift of acoustic sources.

26 Following this idea a compact thermoacoustic refrigera-
27 tor prototype for automobile air conditioning applications
28 was designed and built recently [16]. The prototype was
29 designed using the numerical code DeltaEC [17], based on
30 the linear theory of thermoacoustics (Rott's linear theory
31 [18, 19], later extended by Swift [2], Arnott et al. [20]).
32 The numerical implementation is based upon a lumped
33 element approximation, each element being a part of the
34 system: stack, heat exchanger, duct, etc. For each element,
35 the geometry of the transverse section and the characteris-
36 tics of the solid are accounted for through mean values over
37 the element section, in the quasi-one dimensional set of
38 equations, written in the frequency domain. The code
39 provides an estimate of one-dimensional distributions of
40 pressure, velocity and temperature, for a given system
41 working in the periodic regime. Until now, this approach
42 has been widely used to design thermoacoustic devices,
43 despite observed discrepancies on the thermal quantities
44 [16, 21]. These could be associated with nonlinear phenom-
45 ena such as streaming [22], end effects or natural convection
46 [23, 24], known to be responsible for reducing the efficiency
47 of thermoacoustic systems. Those phenomena are partially
48 taken into account or simply neglected in the context of
49 the linear thermoacoustic theory. Previous CFD studies of
50 thermoacoustic standing wave refrigerator have been based
51 upon a fully viscous, conductive, and compressible solu-
52 tion [25] for high frequencies (20 KHz), simulating devices
53 of extremely small size (on the order of millimeters).
54 Although promising, this approach would lead to extremely
55 large simulations for the present application (cavity size on
56 the order of ten centimeters, and low frequency of 50 Hz).
57 Simulations based on the linearized Navier–Stokes
58 equations (LNSE) are commonly used to implement

multidimensional acoustic simulations, in which a back-
ground flow interacts with and modifies an acoustic field
[26]. This approach could be interesting but is restricted
to the linear regime.

63 In the present work a numerical simulation of the flow
64 and heat transfer in a compact simplified thermoacoustic
65 heat pump is proposed. It consists in solving Navier–Stokes
66 equations under a low Mach number approximation (using
67 the numerical solver SUNFLUIDH [27]). The low Mach
68 number approximation has already been used to describe
69 a thermoacoustic stack refrigerator in the years 1998–1999
70 [28, 29] and later by [30]. The simulation of the oscillation
71 flow and the heat pumping effect was performed in a region
72 restricted between two stack plates with boundary condi-
73 tions that meant to represent the acoustic resonator. More
74 recently, the same approach was used to simulate idealized
75 thermoacoustic engines, by coupling a numerical model of
76 nonlinear flow and heat exchange inside the stack with
77 linear acoustics in the resonator and a variable load
78 [31, 32]. In the present study the low Mach number
79 approach can be applied to describe finely the entire device
80 since the frequency of the acoustic sources is such that the
81 associated wavelength is much greater than the cavity size.
82 As a consequence, pressure oscillations can be considered as
83 spatially uniform in a first approximation. This model is
84 capable of simulating non-linear hydrodynamics interac-
85 tions with lower numerical cost than CFD simulations.

86 The main objective of this work is to show the relevance
87 and interest of such an approach for the simulation of
88 heat pumping in compact cavities. For the sake of simplic-
89 ity a 2D geometry of the cavity is considered. The simula-
90 tions provide a fine description of the flow fields and heat
91 transfer inside the cavity allowing to account for their
92 two-dimensional features and to analyse their effect on
93 thermoacoustic heat pumping. Moreover, we point out that
94 thermoacoustic effects can be correctly represented by
95 coupling two mechanisms: a compression-relaxation cycle
96 and an oscillating fluid motion. The former is related to a
97 homogeneous thermodynamic pressure component whose
98 time variation is governed by a first source acting as an
99 “acoustic driver”. The latter is sustained by a second source,
100 the “oscillating fluid generator” that imposes a sinusoidal
101 time-variation of the flow rate. This point of view is quite
102 different from the linear theory of thermoacoustics where
103 the main role of acoustic propagation and local pressure
104 gradients is emphasized. Part of this work was presented
105 during the CFA 2022 [33]. The paper is organized as
106 follows: After a short presentation of the low Mach number
107 approach coupled with specific boundary conditions model-
108 ing both acoustic sources, and of numerical methods, a
109 reference simulation setup is described (geometry, thermo-
110 physical properties, . . .). In the result section, thermoacous-
111 tic heat pumping is first analyzed for different key param-
112 eters such as the stack thermal conductivity, the flow
113 velocity magnitude, the drive ratio, the relative phase
114 between pressure oscillations and particle velocity oscilla-
115 tions. Numerical results are compared with analytical esti-
116 mates and experimental results presented by Poignand

et al. [13, 15]. Several configurations corresponding to different thermal conditions applied on the outside wall and the separation plate are then considered and their impact on thermoacoustic heat pumping is discussed.

2 Numerical models

2.1 Governing equations in the low Mach number approach

For a perfect gas, the flow dynamics is commonly described by the compressible, viscous, and heat-conductive Navier–Stokes equations, namely the conservation laws of mass, momentum, energy and the ideal state equation:

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{V}) = 0, \quad (1)$$

$$\rho \left(\frac{\partial \mathbf{V}}{\partial t} + \mathbf{V} \cdot \nabla \mathbf{V} \right) = -\nabla P + \nabla \cdot \boldsymbol{\tau} + \mathbf{f}_{\mathbf{V}}, \quad (2)$$

$$\rho c_p \left(\frac{\partial T}{\partial t} + \mathbf{V} \cdot \nabla T \right) = \nabla \cdot \kappa \nabla T + \frac{dP}{dt} + \Phi, \quad (3)$$

$$P = \rho \frac{R}{\mathcal{M}} T, \quad (4)$$

where ρ stands for the density, \mathbf{V} for the velocity field, $\mathbf{f}_{\mathbf{V}}$ for the volume forces (i.e. gravity force) and $\boldsymbol{\tau}$ for the stress tensor, which is defined as $\boldsymbol{\tau} = \mu(\nabla \mathbf{V} + {}^T(\nabla \mathbf{V}) - (\frac{2}{3} \nabla \cdot \mathbf{V}) \mathbb{1})$, with μ the dynamic viscosity. In the energy equation, T represents the temperature, c_p the specific heat at constant pressure, κ the thermal conductivity and $\Phi = \boldsymbol{\tau} : \nabla \mathbf{V}$ the viscous dissipation rate. In the state equation, R is the universal gas constant ($R = 8.314 \text{ J.K}^{-1}.\text{kg}^{-1}$) and \mathcal{M} the molar mass of the gas. The viscous dissipation rate is often negligible compared to the other terms for low speed flows and this was checked in the present study. It will therefore no longer be considered here.

Solving the fully compressible Navier–Stokes equations can be too time consuming since it requires a numerical time step very small in order to verify an acoustic Courant–Friedrichs–Lewy condition, based on the speed of sound as velocity scale.

As already mentioned in introduction, the dimensions of the prototype under study are much smaller than the wavelength associated with the oscillation frequency of the two sources, i.e. the Helmholtz number He defined as the ratio of a reference length scale L of the cavity to the wavelength λ_0 is small. Acoustic wave propagation can therefore be neglected and the whole prototype considered as acoustically compact. Navier–Stokes equations can then be simplified using asymptotic expansions in powers of Mach number ($M = \frac{V_0}{c_0}$) yielding the so-called low Mach number model that filters acoustic waves, following the approach proposed in [34, 35]. As a result, the pressure P is split into two terms : the first order thermodynamic pressure

component P_{th} and a much smaller dynamic pressure component P_{dyn} of order $\mathcal{O}(M^2)$. The first term P_{th} is homogeneous in space, depends only on time and is related to the global time-variation of the thermodynamic state of the system during an expansion/relaxation cycle. The second term, which depends on both space and time, represents the small variations of pressure that directly acts on the flow dynamics. The Navier–Stokes equations are rewritten as:

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{V}) = 0, \quad (5)$$

$$\rho \left(\frac{\partial \mathbf{V}}{\partial t} + \mathbf{V} \cdot \nabla \mathbf{V} \right) = -\nabla P_{\text{dyn}} + \nabla \cdot \boldsymbol{\tau}, \quad (6)$$

$$\rho c_p \left(\frac{\partial T}{\partial t} + \mathbf{V} \cdot \nabla T \right) = \nabla \cdot \kappa \nabla T + \frac{dP_{\text{th}}}{dt}, \quad (7)$$

$$P_{\text{th}} = \rho \frac{R}{\mathcal{M}} T. \quad (8)$$

The low Mach number model allows to finely describe flow dynamics and heat transfer for compact thermoacoustic configurations, while being less time-consuming than a fully compressible model. In this study, the buoyancy effect is not considered ($\mathbf{f}_{\mathbf{V}} = 0$). This point will be discussed in Section 4. Since the pressure is split into two components an added equation is required to close the system. The relation yielding P_{dyn} is described in the following Section 2.2. The relation for P_{th} is obtained by integrating over the whole domain the state Equation (8), yielding:

$$P_{\text{th}} = \frac{R}{\mathcal{M}} \frac{\int_{\Omega} \rho d\Omega}{\int_{\Omega} \frac{1}{T} d\Omega}, \quad (9)$$

taking into account that the entire mass of fluid is known at any time in the domain Ω .

In the solid parts of the stack, the following heat equation is solved, denoting with the subscript s the thermo-physical properties of the stack plates:

$$\rho_s c_{ps} \frac{\partial T}{\partial t} = \nabla \cdot \kappa_s \nabla T. \quad (10)$$

Continuity of heat flux is applied at fluid-solid interfaces. The main steps of the algorithm are outlined in the next section.

2.2 Numerical methods

The governing equations are solved following a finite difference approach of second order in time and space. Convective/advective fluxes and conductive/viscous terms are discretized with a second order scheme on a staggered grid. The time scheme is based on a Crank–Nicholson method where the diffusive terms are implicit in order to

1 increase the numerical stability of the method with respect
 2 to the time step, which is based on the CFL criterion only.
 3 The dynamic pressure component is solved by means of an
 4 incremental projection method commonly used for the
 5 simulation of incompressible flows [36] and adapted for the
 6 low-Mach number approach. For that, the divergence-free
 7 constraint is replaced by the mass conservation constraint
 8 by using Equation (5). The projection method also allows
 9 to update the velocity field estimated from the momentum
 10 Equation (6) in such a way that mass conservation is satisfied.
 11 More information can be found in [37], for example. To
 12 sum up, this leads to a Poisson's equation of the form:
 13

$$\nabla^2 \cdot \Psi = \frac{\nabla \cdot \left(\rho^{n+1} \mathbf{V}^* - \frac{\partial \rho^{n+1}}{\partial t} \right)}{\Delta t}, \quad (11)$$

16 where $\Psi = P_{\text{dyn}}^{n+1} - P_{\text{dyn}}^n$ is the time increment of pressure,
 17 the index n denotes the time iteration, \mathbf{V}^* is the velocity
 18 field estimated from the momentum Equation (6), ρ the
 19 mass density obtained from the state Equation (8), $\frac{\partial \rho}{\partial t}$
 20 its time derivative and Δt the numerical time step. In
 21 order to satisfy the mass conservation Equation (5), the
 22 velocity field is updated as:
 23

$$\mathbf{V}^{n+1} = \mathbf{V}^* - \frac{\Delta t}{\rho^{n+1}} \nabla \Psi. \quad (12)$$

25 The main steps of the algorithm used for the time advance-
 26 ment of physical quantities can be summarized as:
 27

- 28 1. Solve Equation (10) to update the temperature field.
- 29 2. Use the state equation in both forms (9) and (8) to
 30 obtain the thermodynamic pressure component P_{th}
 31 and the density ρ respectively/in that order. The
 32 entire mass of fluid in the domain is known at each
 33 time step from initial and boundary conditions (see
 34 Sect. 2.3.2 below).
- 35 3. Solve Equation (6) to estimate the velocity field \mathbf{V}^*
 36 (which does not satisfy mass conservation).
- 37 4. Use the projection method to compute the dynamic
 38 pressure component P_{dyn} and correct the velocity field
 39 in order to satisfy mass conservation.
 40

42 2.3 Boundary conditions

43 2.3.1 Wall boundary conditions

44 Wall boundary conditions considered in this numerical
 45 study are classical. The usual impermeability and no-slip
 46 conditions ($\mathbf{V} = 0$ on the solid walls) are used for the veloc-
 47 ity. Since velocity values are fixed, the projection method
 48 naturally imposes a zero normal derivative for the dynamic
 49 pressure component P_{dyn} . Several cases are considered
 50 about heat transfer. Either walls are adiabatic, which
 51 implies to impose a zero normal derivative for temperature,
 52 or wall temperature is imposed and set to a constant value
 53 T_w . For thermally conductive solids, continuity of tempera-
 54 ture and heat flux at the solid–fluid interface is ensured in
 55 the model, since the enthalpy equation naturally reduces
 56 to the heat equation within the solid.

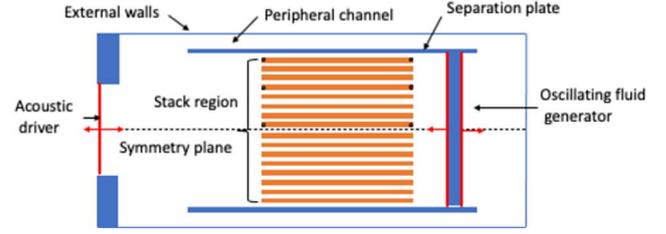


Figure 1. Sketch of the 2D TACOT configuration. The computational domain is restricted to the upper part above the symmetry plane. Circle tags show probe locations used for recording time series of temperature.

2.3.2 Modeling the acoustic sources

57 The experimental technology used to monitor the
 58 governing pressure variation and oscillating fluid motion
 59 consists in various acoustic sources, like pistons and loud-
 60 speaker membranes. These complex elements are difficult
 61 to model in a CFD code. This would require specific meth-
 62 ods managing moving objects in a fluid, like ALE or
 63 immersed body methods, as well as a finer mesh refinement
 64 in the zones of interest. As a consequence, numerical simu-
 65 lations would be particularly complex and time consuming.
 66 To overcome this difficulty, we have opted to model the
 67 acoustic sources by using oscillating flowrate inlets (see
 68 Fig. 1). For each acoustic source, the boundary conditions
 69 are defined as:
 70

$$Q_m(i) = \rho_0 U_i S_i \sin(2\pi f_0 t - \phi_i), \quad (13)$$

71 where $Q_m(i)$ is the mass flow rate at each inlet i with an
 72 amplitude $\rho_0 U_i S_i$ (reference values of fluid density, veloc-
 73 ity and surface of the inlet i) and a time variation defined
 74 from the oscillation frequency of the device f_0 and the
 75 phase ϕ_i . This formulation ensures mass conservation over
 76 each thermoacoustic cycle and allows us to know the mass
 77 of fluid at any time. For others quantities (temperature,
 78 density, dynamic pressure component) a zero normal
 79 derivative is imposed.
 80

81 For sake of clarity the inlets are reported in red color in
 82 the sketch of the computational domain (see Fig. 1). The
 83 oscillating fluid generator (OFG) is constructed as two
 84 back-to-back inlets which have the same parameters ρ_0 ,
 85 U_{OFG} , S_{OFG} , ϕ_{OFG} . The OFG model therefore produces a
 86 zero mass balance at any time and plays a role in the
 87 fluid motion only. The acoustic driver (AD), which governs
 88 the the compression/relaxation cycle through the varia-
 89 tion of pressure, is modeled as a single inlet whose
 90 parameters are ρ_0 , U_{AD} , S_{AD} , ϕ_{AD} . By considering the phase
 91 of the acoustic driver as a reference ($\phi_{\text{AD}} = 0$) and the
 92 quadratic phase delay between the time variation of pres-
 93 sure and the acoustic driver velocity, the usual phase
 94 shift between velocity and pressure can be expressed as
 95 $\Phi_u - \Phi_p = \frac{\pi}{2} - \phi_{\text{OFG}} \pm m \cdot \pi$ (where m is an integer).
 96

97 The drive ratio (i.e. the ratio between the amplitude of
 98 pressure oscillation and the mean pressure) and the velocity
 99 scale in the stack are directly related to the flow rates of the
 100 acoustic driver and the oscillating fluid generator.
 101

Table 1. Geometrical features of the thermoacoustic device defined in the top half-domain.

Q7 Domain size	$1.42 \cdot 10^{-1} \text{ m} \times 2.80 \cdot 10^{-2} \text{ m}$
Stack plate size	$5.00 \cdot 10^{-2} \text{ m} \times 1.28 \cdot 10^{-3} \text{ m}$
Distance between plates	$1.28 \cdot 10^{-3} \text{ m}$
Stack area height	$2.11 \cdot 10^{-2} \text{ m}$
Distance AD-OFG	$1.16 \cdot 10^{-1} \text{ m}$
Distance AD-stack	$5.40 \cdot 10^{-2} \text{ m}$
AD height	$1.54 \cdot 10^{-2} \text{ m}$
OFG height	$2.11 \cdot 10^{-2} \text{ m}$
Pheripheral channel height	$5.60 \cdot 10^{-3} \text{ m}$

3 Numerical configurations

3.1 Description of the thermoacoustic device

In this section, we describe the 2D configuration used in our numerical simulations (in the context of this study, we consider that any phenomenon associated with the third direction can be neglected). It includes the main components of compact thermoacoustic refrigerators designed in laboratory experiments [14, 16]: an acoustic driver (AD) controlling the compression and relaxation cycle, an oscillating fluid generator (OFG), a peripheral channel (PC) allowing circulating fluid and a stack of 16 solid plates along which is created the temperature gradient (see Fig. 1). The geometry is cartesian and the computational domain is restricted to the upper part of the device by assuming symmetry of the flow behavior with respect to the median-plane. The main geometrical features of the device are summarized in Table 1.

The physical properties of the stack plates are chosen to be representative of materials commonly used in thermoacoustic devices. The mass density is fixed at $\rho_s = 2000 \text{ kg.m}^{-3}$, and the thermal conductivity is set to $\kappa_s = 0.2 \text{ W.m}^{-1}.\text{K}^{-1}$ (except in Section 4.1.1 where different values of κ_s are considered). The specific heat capacity is however set to an artificially small value ($c_{ps} = 10 \text{ J.K}^{-1}.\text{kg}^{-1}$). The objective is to shorten the transition time before reaching a converged time-average state of flow and heat transfer, and thus reduce the CPU time. The value of c_{ps} has a negligible impact on the final temperature gradient in the stack as will also be shown in Section 4.1.1.

The fluid is a gas mixture composed of 30% argon and 70% helium as in the TACOT experiments [16]. This choice is made in order to verify the ability of the numerical model to supply a high temperature gradient of the same order of magnitude as those obtained with experimental prototypes [16]. The perfect gas state law is considered with constant physical properties. The specific heat capacity, thermal conductivity and dynamic viscosity are set to $c_p = 1404.97 \text{ J.K}^{-1}.\text{kg}^{-1}$, $\kappa = 8.56 \cdot 10^{-2} \text{ W.m}^{-1}.\text{K}^{-1}$ and $\mu = 2.11 \cdot 10^{-5} \text{ kg.m}^{-1}.\text{s}^{-1}$ respectively.

The frequency of both the acoustic driver and the oscillating fluid generator is fixed at $f_0 = 50 \text{ Hz}$. By considering a reference temperature of $T_0 = 298 \text{ K}$ and mass density of $\rho_0 = 0.597 \text{ kg.m}^{-3}$ (corresponding pressure $P_0 = 10^5 \text{ Pa}$),

the thicknesses of the dynamic and thermal boundary layers along the stack plates are estimated to be $\delta_v = 4.75 \cdot 10^{-4} \text{ m}$ and $\delta_\kappa = 8.07 \cdot 10^{-4} \text{ m}$ respectively.

The value of the resulting temperature difference along the stack plate and therefore of the heat pump efficiency is potentially dependent upon constraints on local heat transfer within the cavity. Several configurations corresponding to different thermal boundary conditions applied on the outside wall and the separation plate are thus considered:

- Case 1: All solid walls are adiabatic (except for the stack plates). This configuration corresponds to an ideal situation with no heat transfer through external walls or the separation plate between the stack region and the peripheral channel (locations are shown on the sketch of the device, Fig. 1).
- Case 2: All external walls are at fixed temperature T_w and the separation plate between the stack region and the peripheral channel is adiabatic. It is also a simplified configuration corresponding to isothermal outer walls, but it allows for heat loss to the ambient surroundings. In real situations there is also convective heat transfer with the surroundings and a fine determination of the overall heat loss would require complex numerical simulations which is beyond the scope of this study. The wall temperature T_w is arbitrarily set to 285 K.
- Case 3: All external walls are at fixed temperature $T_w = 285 \text{ K}$ and the separation plate between the stack region and the peripheral channel is conductive. For the sake of simplicity, the values of heat capacity and mass density are the same as for the stack. The thermal conductivity is set to either $\kappa_1 = 0.25 \text{ W.m}^{-1}.\text{K}^{-1}$ (case 3a : moderate conductivity specific to ceramics [15]) or $\kappa_2 = 14 \text{ W.m}^{-1}.\text{K}^{-1}$ (case 3b: large conductivity specific to stainless steel [16]) accounting for the variability of materials used in thermoacoustic devices.

3.2 Numerical parameters

The computational domain is discretized according to a cartesian grid 384×320 in the longitudinal (x) and the normal (y) directions respectively (with respect to the stack plates orientation). In the normal direction, the cell size distribution is regular over the stack area. There are 16 cells across the plate thickness as well as across the fluid interspace between plates, the resulting cell size being $\Delta y = 8 \cdot 10^{-5} \text{ m}$. This ensures a correct spatial resolution of the boundary layers.

In the longitudinal direction, the cell size varies following a specific distribution law so that the minimum values are positioned nearby the stack ends ($\Delta x_{\min} = 2.5 \cdot 10^{-4} \text{ m}$).

The time step is fixed at $\Delta t = 2 \cdot 10^{-5} \text{ s}$. This choice ensures that the CFL criterion is satisfied (maximum value is about 0.5) and each period of the thermoacoustic cycle is exactly described with 1000 time steps. Initially the fluid is at rest. Initial conditions for pressure and temperature are set to $P_0 = 10^5 \text{ Pa}$ and $T_0 = 298 \text{ K}$ and the mass density is equal to $\rho_0 = 0.597 \text{ kg.m}^{-3}$.

4 Numerical results

The numerical results presented below are obtained for physical configurations adapted from experiments [14, 16] so that the operating mode mainly corresponds to the linear regime. The working gas and frequency were chosen to be the same as in the TACOT prototype [16] in order to obtain a thermoacoustic heat pumping effect large enough for industrial applications. However, the mean thermodynamic pressure was set to atmospheric pressure in order to keep boundary layers large enough to be discretized without excessive numerical cost. Here the ratio between the half-distance between plates and the thermal boundary layer thickness is equal to 0.8 which means that the stack is neither quasi-adiabatic nor quasi-isothermal, but in between.

Numerical simulations are then compared with analytical results obtained from linear theory [13] for various sets of parameters as well as with experimental measurements of Poignand et al. [15], with either a quasi-adiabatic stack (Exp. 1) or a quasi-isothermal regenerator (Exp. 2). Equations for the linear theory are solved with parameter values presented in Section 3.1, in order to describe the ideal case 1. The main input parameters characterizing the different simulations are the drive ratio, the stack velocity scale and the phase shift between the acoustic driver and the oscillating fluid generator. The drive ratio is the commonly used parameter to characterize the acoustic operating regime. It is defined with respect to the thermodynamic pressure component as:

$$Dr = \frac{P_{th}^{\max} - P_{th}^{\min}}{P_{th}^{\max} + P_{th}^{\min}}.$$

In the present study, the drive ratio is small enough ($Dr < 2.5\%$) so that Rott's linear theory should give the correct value for the temperature difference between stack ends (ΔT). The stack velocity scale u_s is commonly defined as the mean velocity amplitude over the stack channels. It can be simply estimated as $u_s = \frac{U_{OFG}}{R_b}$ (the density variation in space being neglected as a first approximation), where U_{OFG} is the velocity amplitude of the OFG, and R_b is the stack porosity (ratio between the fluid part and entire stack volumes).

In the following sections, results obtained on the three configurations presented in Section 3.1 are detailed. These results mainly focus on the mean value of ΔT computed from time series recorded at locations reported in Figure 1. This quantity is normalized in order to compare numerical results with experimental measurements whose operating regimes are not the same as those used for computations. Temperature fields are also presented to point out how thermoacoustic heat pumping can be influenced by the previously described thermal configurations. In order to smooth the time variations related to each thermoacoustic cycle, all physical variables are averaged over 100 oscillation cycles. Time series show the evolution of the averaged quantities. Simulations are run until convergence is obtained for

the mean value of ΔT (or quasi-convergence, see discussion in Sect. 4.2).

4.1 Parametric analysis of thermoacoustic heat pumping

In this section, the sensitivity of the thermoacoustic heat pumping effect, given by ΔT , with respect to some input parameters (driver ratio, stack-velocity scale, ...) is shown. The main objective is to validate the model in the linear regime by comparison with experimental measurements and analytical results obtained from the linear theory. Results corresponding to the configuration case 1 only were already described in CFA 2022 [33]. In the following discussion the reference operating conditions correspond to a drive ratio equal to $Dr = 0.0236$, a velocity scale in the stack on the order of $u_s = 0.5 \text{ m.s}^{-1}$ ($U_{OFG} = 0.25 \text{ m.s}^{-1}$ and $R_b = 0.5$), and the mass flow rates associated with the AD and OFG sources are adjusted in such a way that the phase shift between the velocity and the pressure in the stack is equal to $\Phi_u - \Phi_p = 5\pi/6$, as explained in the end of Section 2.3.2. These reference values were chosen in order to obtain a significant thermoacoustic effect for all configuration cases. All other input parameters are described in Section 3. The sensitivity to each parameter is analysed separately.

4.1.1 Influence of stack thermo-physical properties

Results shown in this paragraph were obtained for the configuration case 1. The considered thermo-physical properties are the heat capacity $\rho_s c_{ps}$ and the thermal conductivity κ , since the heat flux is essentially determined by these parameters. The time evolution of the temperature difference ΔT is plotted in Figure 2 for several values of the stack plates specific heat capacity c_{ps} (the actual parameter should be $\rho_s c_{ps}$ but it is obvious that considering only the variation of c_{ps} is sufficient, ρ_s being fixed). There is a transient phase before reaching an asymptotic regime giving $\Delta T \simeq 51.5 \text{ K}$, which, as expected, is longer as the value of the heat capacity is larger (see Fig. 2). The low sensitivity of ΔT in the asymptotic regime to the heat capacity of the stack allows us to consider a small value in order to reduce drastically the computation time and justifies our choice to set $c_{ps} = 10 \text{ J.K}^{-1}.\text{kg}^{-1}$. Similar observations were made for the other configurations (cases 2 and 3). Therefore the same value of c_{ps} was kept for all simulations.

Figure 3 shows the value of ΔT between stack ends for six values of the thermal conductivity κ_s of the solid stack plates (case 1). The solid line shows the corresponding prediction of the linear theory of thermoacoustics. The agreement is excellent. As expected, when κ_s is very large, ΔT becomes negligible because of enhanced heat conduction in the solid: thermoacoustic heat pumping becomes ineffective. For $\kappa_s = 0$ (adiabatic stack) the thermoacoustic effect is canceled, as predicted by Swift [1]. Note that for very small (non-zero) values of κ_s the numerical prediction departs for the linear theory, suggesting that the evolution

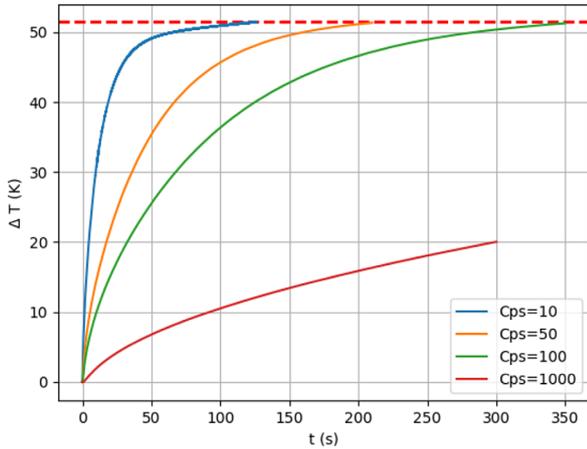


Figure 2. Mean temperature difference ΔT between stack ends computed by numerical simulation for several values of c_{ps} , configuration case 1.

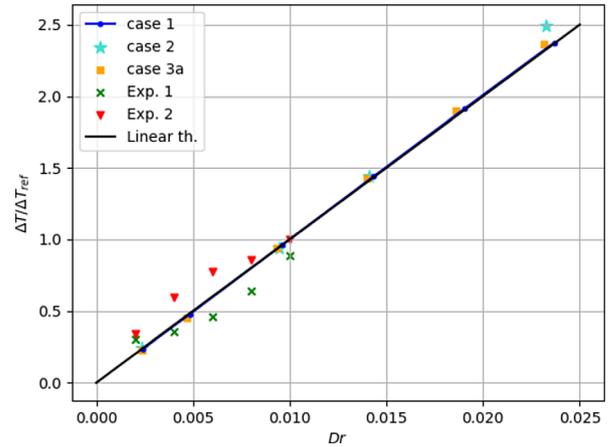


Figure 4. Normalized mean temperature difference $\Delta T/\Delta T_{\text{ref}}$ between stack ends as a function of the Drive ratio Dr . Numerical results (cases 1, 2, 3), linear theory (black solid line), Exp. 1 (green crosses) and Exp. 2 (red triangles) from [15].

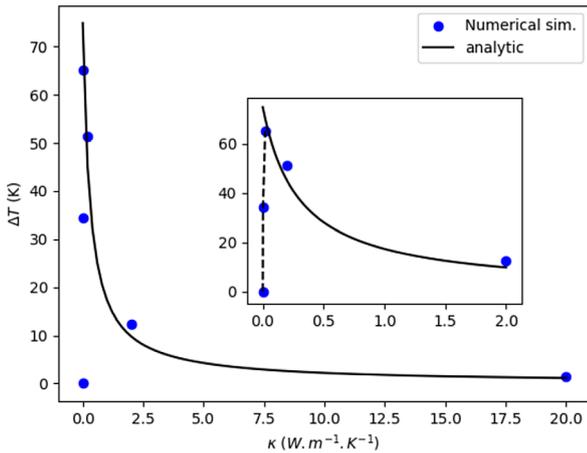


Figure 3. Mean temperature difference ΔT between stack ends for 6 values of κ_s . Numerical results case 1 (blue dots), linear theory (solid line).

1 as $\kappa_s \rightarrow 0$ is sharp but continuous and that there is an
 2 optimum κ_s value for which ΔT is maximum. Again similar
 3 observations were made for the other configurations (cases 2
 4 and 3).

5 4.1.2 Influence of the Drive ratio

6 In this paragraph, the used relative velocities and phase
 7 shift are fixed at their reference values $u_s = 0.5 \text{ m.s}^{-1}$ and
 8 $\phi_u - \phi_p = 5\pi/6$. Figure 4 shows the variation of the
 9 normalized temperature difference along the stack as a
 10 function of the drive ratio for all considered configurations
 11 (cases 1 to 3). Numerical points are plotted as well as the
 12 linear theory prediction and experimental results from
 13 [15]. In order to compare our results with those of Poinand
 14 et al. [15], which are performed in very different physical
 15 conditions, the reference scale ΔT_{ref} used to normalize ΔT
 16 is chosen at $Dr = 0.01$. Both sets of experimental points

(Exp. 1) and (Exp. 2) are shown on the figure, and the
 17 evolutions are consistent with the numerical simulation
 18 results which fall in between as expected, since in the
 19 numerical configuration the stack is neither fully adiabatic
 20 nor isothermal. Very good agreement with the linear
 21 theory is observed (see Fig. 4). We notice the numerical
 22 results are very similar independently from the considered
 23 configuration.
 24

4.1.3 Influence of the stack velocity-scale

25
 26 Another important parameter of the thermoacoustic
 27 heat pumping effect is the characteristic velocity scale
 28 within the stack. The variation of this parameter is
 29 obtained by changing the input velocity U_{OFG} of the oscil-
 30 lating fluid generator. The other relevant parameters, the
 31 drive ratio and the phase shift, are fixed at their respective
 32 reference value ($Dr = 0.0236$ and $\phi_u - \phi_p = 5\pi/6$). In order
 33 to compare numerical, theoretical and experimental results,
 34 the stack velocity scale corresponding to each data set is
 35 normalized with respect to its own optimum value u_{opt}
 36 providing the maximum value of the ΔT in each case.

37 Figure 5 shows the evolution of ΔT between stack ends
 38 as a function of the normalized stack velocity scale
 39 $u_s^* = u_s/u_{\text{opt}}$ for all considered configurations. Again a simi-
 40 lar behavior is observed in numerical or experimental
 41 results and in the linear theory. The value of ΔT result-
 42 ing from the different approaches increases with u_s^* , up to u_s^*
 43 about 0.85, then reaches the same plateau. There are how-
 44 ever some quantitative discrepancies for $u_s^* < 0.6$. While the
 45 experiment 1 fits well with the linear theory, the experiment
 46 2 yields lower values of ΔT . The numerical results present
 47 larger values which are similar for the three considered
 48 cases. The scattering of experiment 2 and numerical results
 49 around the linear theory curve is of the same order and is
 50 more noticeable as u_s^* decreases. However the normalization
 51 allows to obtain analogous behavior for all these physically
 52 very different configurations.

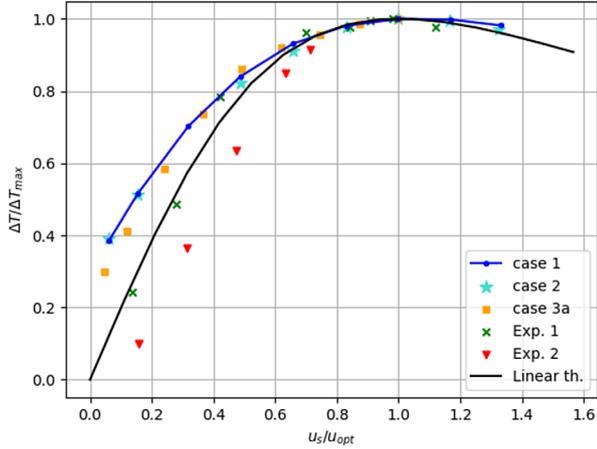


Figure 5. Normalized mean temperature difference $\Delta T/\Delta T_{\max}$ between stack ends as a function of the normalized stack velocity scale u_s/u_{opt} .

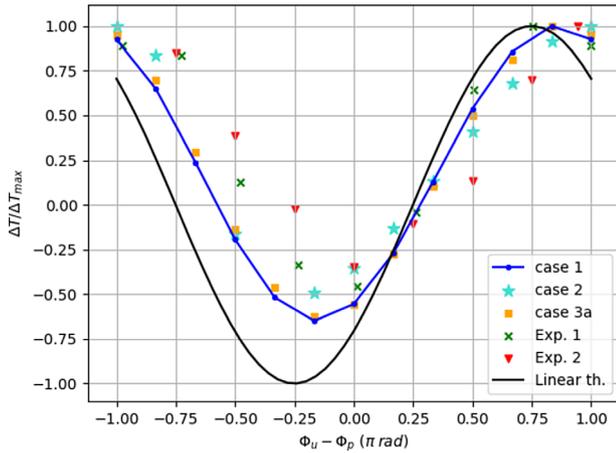


Figure 6. Normalized mean temperature difference $\Delta T/\Delta T_{\max}$ as a function of $\Phi_u - \Phi_p$.

4.1.4 Influence of the phase shift between velocity and pressure.

In this paragraph, the used relative velocities and drive ratio are fixed at their reference values ($u_s = 0.5 \text{ m}\cdot\text{s}^{-1}$, $Dr = 0.0236$). The influence of the phase shift between velocity and pressure is studied and results are plotted in Figure 6 for the three numerical configurations. Here again a similar evolution is observed in numerical simulations, experimental results and the linear theory. In the $[-\pi, 0]$ interval, numerical results are bounded by linear theory and experimental results, while in the $[0, \pi]$ interval all curves are in close agreement. Numerical simulations, for every cases, confirm the experiment results in that the phase shift has a major influence on the thermoacoustic heat pumping effect. Indeed it is possible to control the orientation of heat pumping (and invert ΔT between the stack ends) with the phase shift. The observed asymmetry of the curve (for example on extreme values) is probably correlated to the device geometry with respect to the stack

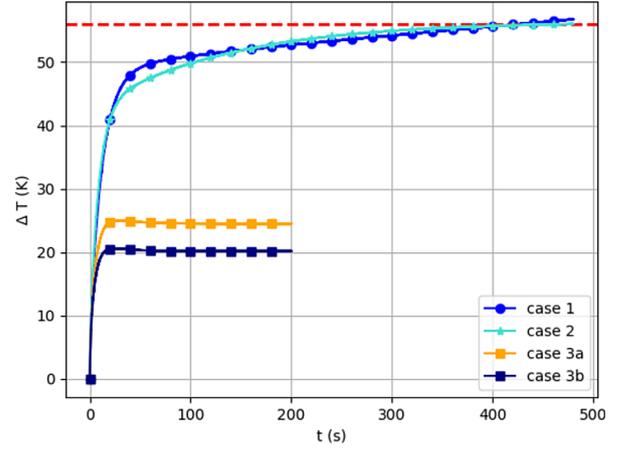


Figure 7. Time evolution of the temperature difference between stack ends for the different configurations.

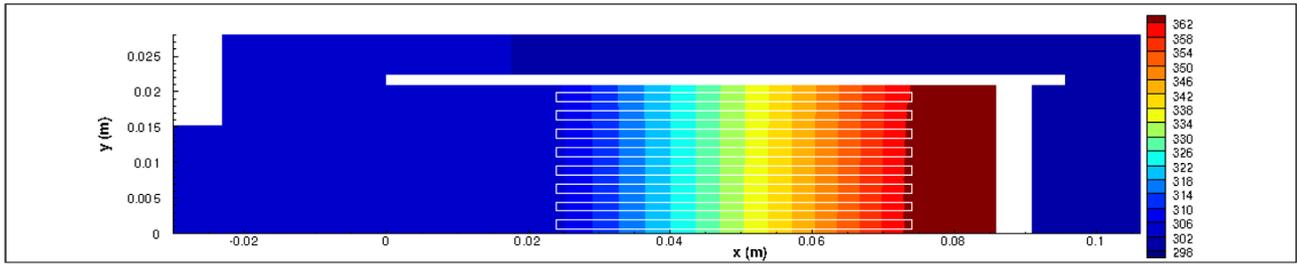
middle cross-section. Note that the model deduced from the linear theory does not predict this asymmetry. It is observed that for all considered configurations, the numerical value of the phase shift Φ leading to the maximum value of ΔT varies between $5\pi/6$ and π which is slightly larger than the value found in the linear model ($3\pi/4$) and close to the experimental results reported in [15].

4.2 Influence of heat transfer constraints (choice of configuration)

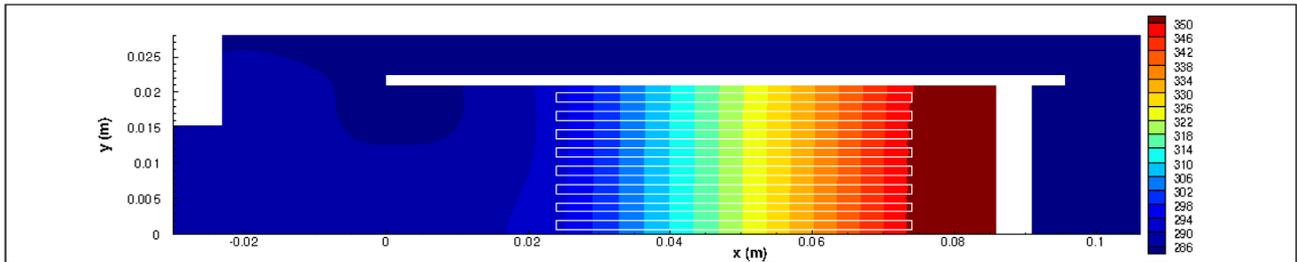
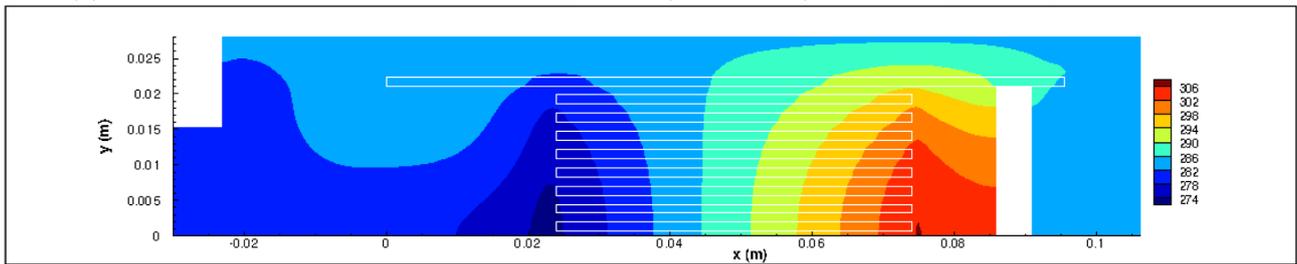
In addition to the very good agreement between the numerical results, experimental measurements and linear theory, we found that the relative variation of the thermoacoustic heat pumping effect with respect to parameters defining the operating regime (drive ratio, stack velocity scale or phase shift) does not depend significantly on the considered configuration (i.e. on the heat transfer constraints). In other words, the normalized temperature difference across the stack plates follows the same scaling laws.

We now analyse how the heat loss through external walls and the thermal conductivity of the separation plate act on the magnitude of the thermoacoustic heat pumping effect. We use the reference operating conditions described in Section 4.1 for the three considered configurations. Figure 7 describes the time evolution of ΔT for these different cases.

In both configurations for which the separation plate is adiabatic (cases 1 and 2), the established values of ΔT are close to each other. Moreover, the mean temperature fields for these two cases present very similar spatial distributions over the computational domain (see Figs. 8a and 8b). The temperature distribution is unidirectional and quasi linear along the plates in the stack region with same gradient value while it is rather uniform in other parts of the device. From this observation we can deduce that the established time-average heat flux transported by the flow along the peripheral channel is relatively small and the adiabatic separation plate is sufficient to ensure an efficient thermal insulation of the stack region, thereby strongly reducing



(a) Case 1 : External walls and separation plate are adiabatic

(b) Case 2 : External walls are at a fixed temperature ($T_w = 285 \text{ K}$) while the separation plate is adiabatic(c) Case 3a : External walls are at a fixed temperature ($T_w = 285 \text{ K}$) while the separation plate is thermally conductive ($\kappa = 0.25 \text{ W.m}^{-1}.\text{K}^{-1}$)**Figure 8.** Mean temperature field over the computational domain for cases 1, 2 and 3a.

1 the impact of the heat loss on the thermoacoustic heat
 2 pumping efficiency. Only the global temperature level is
 3 larger in the adiabatic external walls configuration (since
 4 no heat loss is permitted) than that obtained for fixed
 5 temperature outer walls, with heat losses in the latter con-
 6 figuration occurring mainly during the transient stage.

7 Note that the adiabatic external wall configuration
 8 (case 1) induces a small but continuous variation of ΔT over
 9 a long time range. As a consequence, perfectly converged
 10 state of the system (in the sense of time average quantities)
 11 cannot be obtained especially for operating regime close to
 12 optimal conditions. This can be explained by the fact that
 13 the adiabatic conditions coupled with the mechanism of
 14 expansion–compression of the gas cannot maintain the
 15 same thermodynamic state of the fluid from one thermoac-
 16 oustic cycle to another. In other words, ensuring time-aver-
 17 age equilibrium between the enthalpy variation of the fluid
 18 over a thermoacoustic cycle and the heat exchange with the
 19 stack over any thermoacoustic cycle is very difficult. This
 20 small shortcoming however does not affect our results if
 21 the simulation takes place over a limited time (for example,
 22 400 s in configuration case 1, see Fig. 7).

23 What about the absolute magnitude of the temperature
 24 difference established between stack ends? The established

value of ΔT obtained numerically in case 2 is $\Delta T \simeq 56 \text{ K}$.
 Rott's linear theory developed in [13] yields $\Delta T_{\text{lin}} = 49 \text{ K}$
 with the numerical input data set (case 2), in accordance
 with our numerical result.

We now examine the influence of the thermal conductiv-
 ity of the separation plate, by comparing results obtained in
 cases 2, 3a and 3b. As expected, the larger the thermal
 conductivity of the plate, the smaller the thermoacoustic
 heat pumping efficiency, as shown in Figure 7. ΔT is
 reduced by a factor of about 2–2.5 between the adiabatic
 case (case 2) and both thermally conductive cases (3a and
 3b). Moreover, the time required to reach a converged state
 is drastically shorter in cases 3a and 3b. When the separa-
 tion plate is thermally conductive, a significant heat flux
 contribution appears in the normal direction which enables
 heat loss through the peripheral channel and the external
 walls and reduces the magnitude of the mean temperature
 gradient along the stack plates. As a consequence, the
 temperature distribution over the computational domain
 is drastically modified. When the separation plate is adia-
 batic, it is organized following a linear distribution along
 the plates inside the stack plates and a quasi-uniform
 distribution elsewhere (as seen in Fig. 8b). When the separa-
 tion plate is thermally conductive, the temperature field

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1 presents a 2D pattern resulting from heat flux contributions
2 along each direction (see Fig. 8c).

3 If we consider devices with larger span, the vertical
4 distribution of the temperature field in the stack region
5 could trigger buoyancy effects and in turn strongly modify
6 the thermoacoustic heat pumping effect along the stack. As
7 a consequence, thermal insulation of the stack region
8 appears to be a key point in the device optimization, mini-
9 mizing the vertical mean temperature gradient.

10 These observations constitute a significant added con-
11 tribution of numerical simulations compared with linear
12 theory and experiments.

13 5 Conclusion

14 A numerical model based on a Low Mach number
15 approximation was designed to simulate the thermoacoustic
16 heat pumping effect inside a compact cavity consisting of an
17 acoustic driver, an oscillating fluid generator and a stack of
18 solid plates. In this fluid mechanics approach, the physical
19 coupling between the oscillating fluid and homogeneous
20 compression-relaxation cycles results in thermoacoustic heat
21 pumping along the stack plates with no account of acoustic
22 propagation. The main characteristics of thermoacoustics
23 are recovered: the normalized temperature difference as a
24 function of a wide range of operating conditions is in very
25 good agreement with the linear theory predictions and
26 experimental measurements, at least in the linear regime.

27 The model was used to explore a wide range of input
28 parameters in the linear regime for several numerical config-
29 urations, and results were compared with the linear theory
30 as well as experimental measurements. The main results
31 are: Firstly, the normalized temperature difference between
32 stack plate ends follows a scaling law with respect to the
33 main parameters used to determine the operating condi-
34 tions (drive ratio, stack velocity scale or phase shift) inde-
35 pendently from the configuration.

36 Secondly, the influence of heat loss through external
37 walls and of insulation characteristics of the stack region
38 (through the separation plate) is studied. It is shown that
39 the latter has a prevailing effect on the resulting thermo-
40 acoustic heat pumping efficiency, since the temperature dis-
41 tribution inside the stack is no longer unidirectional when
42 the thermal conduction properties of the separation plate
43 become significant. This leads naturally to investigate the
44 relevance of gravity effects when the temperature field
45 inside the stack region becomes multidimensional, especially
46 for compact cavities with larger spans in which buoyancy
47 could arise. The present model is very well adapted for such
48 a study which is the object of our work in progress. In addi-
49 tion the model is also well adapted to explore other nonlin-
50 ear effects, which can be associated for example with jet
51 flow instabilities around stack ends.

52 Conflict of interest

53 Q2 Author declared no conflict of interests.

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