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# Marginal regeneration-induced drainage of surface bubbles 

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#### Abstract

The prediction of the lifetime of surface bubbles necessitates a better understanding of the thinning dynamics of the bubble cap. In 1959, Mysels et al. [Soap Films: Studies of Their Thinning and a Bibliography (Pergamon, New York, 1959)], proposed that marginal regeneration, i.e., the rise of patches thinner than the film should be taken into account to describe the film drainage. Nevertheless, an accurate description of these buoyant patches and of their dynamics as well as a quantification of their contribution to the thinning dynamics is still lacking. In this paper, we visualize the patches, and show that their rising velocities and sizes are in good agreement with models respectively based on the balance of gravitational and surface viscous forces and on a Rayleigh-Taylor-like instability. Our results suggest that, in an environment saturated in humidity, the drainage induced by their dynamics correctly describes the film drainage at the apex of the bubble within the experimental error bars. We conclude that the film thinning of soap bubbles is indeed controlled, to a large extent, by marginal regeneration in the absence of evaporation.


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## I. INTRODUCTION

What is the lifetime of a surface soap bubble? This question contributes to the fascination that bubbles exert on people whatever their age [1,2], and the answer is crucial to understand exchanges between liquid baths and their environment. This concerns various domains such as the sparkling beverages industry for the dispersion of flavors [3], climate models for the exchange between oceans and atmosphere [4,5], or dispersion models for pollutants above swimming pools [6]. Despite this wide range of applications, the question of the bubble stability remains largely open. This is directly linked to the global thinning dynamics of the bubble cap, which requires one to take into account two contributions: the evaporation and the liquid flow within the film (drainage).

The effect of evaporation has been dismissed in most experimental studies concerning bubbles’ lifetime and film thinning dynamics, and in most of them the atmospheric humidity is measured $a$ posteriori rather than controlled. It is only recently that this parameter has been properly controlled and incorporated in the models [6-8].

The liquid drainage between the interfaces is dictated by a balance between capillary suction from the thin film to the meniscus, gravity for $\mathrm{Bo} \geqslant 10$ [8], and viscous dissipation. The capillary suction is controlled by the shape of the bubble, more specifically by the curvature gradient at the bottom of the film, and is controlled at the macroscopic scale by the balance between the buoyancy force and the surface tension. On the other hand, the viscous dissipation is set by the ability of the gas-liquid interfaces to oppose a resistance to the flow of the liquid. In the case of bare bubbles, the

[^0]

FIG. 1. Photograph of a surface bubble with a radius of curvature of $1.13 \mathrm{~cm}(\mathrm{Bo}=25)$ illuminated in white light for a TTAB concentration of 0.5 cmc ; credits: Serge Guichard.
flow is extensional and the velocity is therefore limited by the viscous dissipation induced by the velocity gradients along the flow. If the liquid is viscous enough, the process is slow enough and can be observed more easily, leading to exponential decay of the film thickness at the apex [9-11]. In the case of low viscosity, the rupture of bare bubbles is extremely fast [7].

In practice, however, aqueous liquids always feature surface active impurities [12] and surface tension gradients emerge upon the penetration of bubbles through the interface and subsequent stretching of the surface. These gradients allow the interfaces to carry the film weight [13] and to oppose some resistance to the liquid flow, therefore leading to more stable systems. If this resistance is high enough the velocity profile is expected to lead to a Poiseuille-flow profile within the film. However, in the most common situation of standard surfactants neither the plug-flow nor the Poiseuille-flow profiles allow description of the experiments [14,15].

In the case of flat films, another scenario, deduced from the observation of the whole film dynamics and of thickness heterogeneity in the presence of surfactants, has been proposed by Mysels et al. [16] and relies on the so-called marginal regeneration. This phenomenon is linked to the appearance of thin patches near the borders, in the vicinity of the meniscus (Fig. 1). The associated drainage mechanism assumes that exchanges between thick patches, which enter the meniscus, and thin patches, which are extracted out of it, regulate the global thinning of the film. Gros et al. [17] proposed naming this phenomenon sliding puzzle dynamics since it necessitates a conservation of the surface area.

The literature on these striking patches (Fig. 1) remains surprisingly scarce [12,17-24]. To explain their presence, Mysels et al. proposed the existence of a marginal pinch or dimple due to a difference of capillary pressure between the film and the meniscus [16]. A theoretical model predicting the pinching dynamics in flat films has been proposed by Aradian et al. [20] but has never been verified experimentally.

The patches come from the destabilization of the marginal pinch [19]. Two different scenarios are available in the literature, which rely either on a Benard-Marangoni-like instability due to the presence of surface tension gradients [12,21,22,25] or on a Rayleigh-Taylor-like instability driven by gravity [26]. A similar gravity-driven scenario can also be observed in slightly different experiments, in which a thick film is created above a thinner one [27]. In both scenarios, the unstable nature of the pinching triggers the extraction of patches that still have a thickness comparable to that of the main film [12,17]. This has been confirmed by Nierstrasz and Frens, who performed experimental measurements of the patch thickness on planar vertical films by interferometry and found a value of 0.8 for the ratio between the patches' thickness and that of the rest of the film. This is comparable to the upper limit found for this ratio in the model of Gros et al. [17] equal to 0.7. a result on the


FIG. 2. (a) Sketch of the experimental setup with the notations used. (b) Example of an experimental image centered on the bottom of the bubble on which we can measure the characteristic size of the patches $\ell_{0}(\mathrm{~m})$ and the number of patches per unit area $n_{0}\left(\mathrm{~m}^{-2}\right)$.
order of the averaged film thickness (the patch thickness is found to be equal to 0.8 times the film thickness) [21], which is comparable to the upper limit found in the model of Gros et al. [17], equal to 0.7 .

The question of the quantitative and precise contribution of the marginal regeneration to the film drainage also remains largely open. Following the proposition by Mysels et al. [16], Seiwert et al. [24] proposed that, in planar vertical films, the rise of thin patches which replace the thick ones is the main mechanism responsible for drainage. Lhuissier et al. [12] proposed a second scenario to link the bubble cap drainage to marginal regeneration with a drainage limited by the liquid flow through the pinch. This model leads to a prediction, which has been proven to describe well the experimental data $[6,8]$. Our main result, which we will discuss in the following, is that both scenarios hold, which is probably due to a coupling through the pinch thickness.

The purpose of this article is to explore in detail the question of the contribution of the sliding puzzle dynamics to bubble drainage. To tackle this problem, we first observe and characterize marginal regeneration patches. We then perform a comparison between direct thinning measurements at the apex of the bubble cap and a model allowing us to derive the contribution of the marginal regeneration to drainage. As mentioned earlier, this necessitates suppressing the influence of evaporation on thinning and thus controlling the atmospheric humidity. Our conclusion is that the sliding puzzle dynamics is a sufficient ingredient to explain the film drainage in the absence of evaporation.

## II. PATCHES VISUALIZATION AND CHARACTERIZATION

The study is conducted on bubbles stabilized by an aqueous surfactant solution made with recrystallized TTAB (tetradecyl trimethylammonium bromide, purchased from Sigma-Aldrich) at a concentration of 0.5 cmc (critical micelle concentration, equal to $3.6 \mathrm{mmol}^{-1}$ ) and ultrapure water (resistivity $=18.2 \mathrm{M} \Omega \mathrm{cm}$ ). The TTAB recrystallization [28] ensures a good reproducibility of the data. The bubbles are generated by injecting air below the surface, through a vertical Teflon beveled needle (outer diameter $=0.56 \mathrm{~mm}$ ). The flow rate of the injected air is controlled by a syringe pump and fixed at $\mathrm{Q}=15 \mathrm{ml} \mathrm{min}^{-1}$ ([Fig. 2(a)]. The bubble size is controlled by the injection time and the radius $R$ of the emerged spherical cap is between 9 and 13 mm . The temperature is between $20^{\circ} \mathrm{C}$ and $23^{\circ} \mathrm{C}$. In our study, $\gamma=50 \mathrm{mN} \mathrm{m}^{-1}$ and $\rho=1000 \mathrm{~kg} \mathrm{~m}^{-3}$ so that the Bond number $\mathrm{Bo}=\rho g R^{2} / \gamma$, which controls the shape adopted by the bubble at the interface [29], is always larger than 5 . The entire setup is enclosed in a box, in which the humidity is controlled with a humidity regulator developed by Boulogne [30]. In these conditions, we observe systematically some marginal regeneration after a few tens of seconds.


FIG. 3. (a) Rising velocity of the patches $V^{+}$as a function of time $t$. The Bond number is ranging from 15 to 35 , which corresponds to bubbles with a spherical cap radius between 9 and 13 mm . Error bars correspond to the standard deviation measured by averaging over ten patches. (b) Rising velocity of the patches $V^{+}$as a function of the film thickness $h$. The error for $h$ is taken to be 50 nm (the choice of this value has no noticeable impact on the errors calculated for $\eta_{s}$ and $V_{d}$; see next figures).

To characterize the patches' size and dynamics, we perform direct visualization. We illuminate uniformly the bubbles with a white light panel above the tank containing the solution and a diffusing "tunnel" of tracing paper placed around the bubble [Fig. 2(a)]. A monochromatic camera (Basler acA3800-14um) at the entrance of the "tunnel" allows us to record the images, at a fram rate of 10 images per second. The bubble size and the contact angle $\alpha$ between the bath surface and the bubble cap just above the meniscus are defined in Fig. 2 and are measured for each bubble in the images. The angle $\alpha$ varies between $55^{\circ}$ and $65^{\circ}$, in good agreement with Teixeira et al. [31]. The characteristic size of the patches $\ell_{0}$, their number per unit area $n_{0}$, and their rising velocity $V^{+}$are extracted from the images using the ImageJ software [Fig. 2(b)]. These measurements are performed in the vicinity of the meniscus to avoid distortions due to the inclination of the surface. The contrast is unfortunately too poor and too variable for an automatic detection, thus the patches' size is measured by superimposing a circle on the image and by extracting its radius; $n_{0}$ is counted by hand in a box of approximately $1700 \times 200$ pixels $^{2}$ and $V^{+}$is estimated by averaging the displacement around a given time for at least five successive frames. To carry out these measurements, averages were taken to ensure the robustness of the values: for a given time, the size of the patches, their rising velocity, and their average number per unit area were measured ten times. We also measured the film thickness $h$ at the apex of the bubbles using a white light spectrometer $[8,14]$. The spectra obtained are semiautomatically processed making use of Python code using the library Oospectro [32].

As shown in Fig. 3(a), the mean values of $V^{+}$decrease as a function of the age $t$ of the bubbles since their generation, whatever the bubble sizes (Bo between 15 and 35 at $50 \%$ humidity and Bo $=25$ at $100 \%$ humidity). The rising velocity $V^{+}$at a given time is furthermore expected to depend essentially on the film thickness $h$, itself very dependent on the relative humidity RH after a few tens of seconds. This is illustrated in Fig. 3(b), which shows that plotting $V^{+}$versus $h$ allows one to reasonably rescale the data. The corresponding sizes $\ell_{0}$ of the patches are reported in Fig. 4(a) as a function of the film thickness $h$. Their values show a wide dispersion. Nevertheless, the averaged values tend to grow with the film thickness.

The obtained values of $V^{+}$can be compared to the model proposed by Seiwert et al. [24] for planar films. Here, this model, based on a force balance and on surface conservation, is adapted to the geometry of surface bubbles.


FIG. 4. (a) Evolution of the characteristic size of the patches $\ell_{0}(\mu \mathrm{~m})$ as a function of the film thickness $h$ $(\mathrm{nm})$ for 387 measurements performed on all systems. The orange circles correspond to direct measurements. The blue triangles correspond to the average values of $\ell_{0}$ over an interval of 50 nm for $h$. The green curve represent an adjustment of Eq. (4) with $\delta=36 \mu \mathrm{~m}$. Vertical error bars correspond to the standard deviation measured. (b) Surface shear viscosity $\eta_{s}$ as a function of time $t$. The solid line corresponds to the mean value measured for the surface shear viscosity: $\eta_{s}=(2.0 \pm 0.1) \times 10^{-8} \mathrm{~Pa} \mathrm{~m} \mathrm{~s}$. The error bars take into account errors in the measured parameters and are calculated using the error propagation formula.

First, the authors propose that the driving force is gravity, since the lower thickness of the patches acts as two-dimensional (2D) buoyancy [33]. This driving force is balanced by the viscous dissipation due to the surface shear viscosity $\eta_{\mathrm{s}}$. The shear is due to the difference between $V^{+}$and $V^{-}$, the respective velocities of the rising and descending patches. For surface bubbles [Fig. 2(a)], this force balanceis

$$
\begin{equation*}
2 \eta_{\mathrm{s}} \frac{\left(V^{+}-V^{-}\right)}{\ell_{0}^{2}} \sim \rho g \sin \alpha\left(h-h_{\mathrm{p}}\right) \tag{1}
\end{equation*}
$$

where $h_{\mathrm{p}}$ is the thickness of the patches. The factor 2 accounts for the two sheared interfaces on both sides of the film.

Second, $V^{-}$can be related to $V^{+}$assuming surface conservation: the surface of rising thin patches exactly compensates the surface of the thick descending patches. In the bubble geometry, the total rising surface $d S^{+}$crossing a reference horizontal line at the top of the meniscus during a time interval $d t$ is $d S^{+}=V^{+} d t \times \pi n_{0} \ell_{0}^{2} \times 2 \pi r_{0}$, where $r_{0}$ is the radius of the bubble on this line. This rising surface must be exactly compensated by the surface of descending liquid $d S^{-}=V^{-} d t \times$ $\left(1-\pi n_{0} \ell_{0}^{2}\right) \times 2 \pi r_{0}$, which leads to a prediction for the drainage velocity of the liquid:

$$
\begin{equation*}
V^{-}=V^{+} \frac{\pi n_{0} \ell_{0}^{2}}{1-\pi n_{0} \ell_{0}^{2}} \tag{2}
\end{equation*}
$$

Combining the force balance from Eq. (1) with Eq. (2) and assuming $\left(h-h_{p}\right) \simeq 0.2 h$ [21], we get

$$
\begin{equation*}
\eta_{s} \sim \frac{\rho g h \ell_{0}^{2} \sin \alpha}{10 V^{+}\left(\frac{1-2 \pi n_{0} \ell_{0}^{2}}{1-\pi n_{0} \ell_{0}^{2}}\right)} . \tag{3}
\end{equation*}
$$

The values of $\eta_{\mathrm{s}}$ deduced from Eq. (3) and from our measurements of $h, V^{+}, \alpha, n_{0}$, and $\ell_{0}$ are represented in Fig. 4(b). They feature a constant behavior with a surface shear viscosity around $\eta_{s} \simeq$ $2.0 \times 10^{-8} \mathrm{~Pa} \mathrm{~m} \mathrm{~s}$, whatever the size of the bubbles or the relative humidity, which confirms the reliability of this approach. The values of surface shear viscosities in surfactant-based systems are
controversial. Zell et al. could not measure it and concluded that it must be smaller than $10^{-8} \mathrm{~Pa} \mathrm{~m} \mathrm{~s}$. Other, mostly indirect measurements proposed values in the range of $10^{-6}-10^{-8} \mathrm{~Pa} \mathrm{~m} \mathrm{~s}[34,35]$. Our values thus point to the lower limit of the indirect measurements and are slightly higher than the maximum value inferred by Zell et al. Note that here the bulk viscosity is neglected compared to the surface shear viscosity $\left(\eta h \sim 10^{-9} \mathrm{~Pa} \mathrm{~m} \mathrm{~s}\right.$, with $\eta$ the bulk viscosity that is approximately that of water and $h$ the film thickness).

Let us now focus on the destabilization of the pinch, by concentrating on the patches' size. To predict $\ell_{0}$, Shabalina et al. [26] proposed a Rayleigh-Taylor-like description [36], which we will compare to our measurements. In this model, the gravity difference between the pinch [20] and the overlaying thick, heavier film is the motor of the instability. At the frontier between the thin and thick films, the thickness transition has an extension $\delta$ (see [26] for more details), which leads to an extra surface and a subsequent line tension [37]. Among the stabilizing mechanisms proposed, we assume that this line tension is the main stabilizing parameter. Making use of these assumptions leads to the following prediction for the wavelength $\lambda$ of the instability

$$
\begin{equation*}
\lambda(h) \sim \ell_{0}(h)=\left(\frac{\gamma\left(h-h_{p}\right)}{\rho g \delta}\right)^{1 / 2} \tag{4}
\end{equation*}
$$

This prediction is represented against our data in Fig. 4(a) and features a good agreement provided $\delta \sim 36 \mu \mathrm{~m}$, i.e., of the order of the patches' size. This order of magnitude is in agreement with the observation that a few interference fringes can be seen inside a patch. This is slightly visible in Fig. 1 but much more convincing in Fig. 6 of Lhuissier et al. [12]. In their thicker films, Shabalina et al. [26] also measure a transition length $\delta$ around $100 \mu \mathrm{~m}$. This length scale is also in agreement with that measured in another article by Seiwert et al. [38]. Finally, the underlying mechanism which fixes the transition length $\delta$ is still unknown, but our measurement gives an order of magnitude in line with other observations in the literature.

Note that this representation assumes that the film thickness within the bubble cap, away from the pinched zone, features negligible variations. This is coherent with the constant hole opening velocity reported in different works [6,14]-even on metric bubbles [39]-that make use of the roughly homogeneous thickness to retrieve the film thickness from the so-called Taylor-Culick velocity [40].

In addition, the dependency $\ell_{0} \propto h^{1 / 2}$, also found upon matching the curvature of the spherical cap to that of the pinch by Howell [11] and Lhuissier et al. [12], is recovered. This supports the hypothesis of a gravity-driven instability, in good agreement with the qualitative observation that the marginal regeneration can no longer be observed for a bubble suspended under a wet solid plate.

## III. DRAINAGE DUE TO MARGINAL REGENERATION

Finally, we now compare the drainage induced by the sliding puzzle dynamics to direct measurements of the film thinning rate measured by spectrometry, as mentioned in the preceding section. The time evolution of $h$ is plotted in Fig. 5(a).

As expected, the variation of the thickness $h$ along time is in good agreement with the model presented in previous works (not shown; see Refs. [6,8,12]). The data plotted obtained at an atmospheric humidity of $50 \%$ are actually extracted from Miguet et al. [8].

From these curves, we can deduce the thinning rate of the film at the top of the bubble cap at different times by locally making a power law or a second-order adjustment respectively in a saturated environment or in the presence of evaporation. Their derivative gives the value of $d h / d t$ [see the fitting in Fig. 5(a) at time $t=45$ or 130 s for example]. The model of Lhuissier et al. [12] and its extensions [7,8] provide a good scaling for these data but the most appropriate quantifications of $h$ and $d h / d t$ are given by these local fits. The corresponding equation given in the caption of Fig. 5(a) is indicative. Note that the reason why the range of thinning rates is limited for the $100 \%$ humidity experiment is that the thinning is slower because of the lack of evaporation. In principle, it could be possible to reach faster thinning rates at very short time. Nevertheless, the patches are not well developed at the beginning of the experiment and it is impossible to extract reliable


FIG. 5. (a) Time evolution of the film thickness $h$ at the bubble apex for different bubble sizes and humidities. The dashed and dotted black lines correspond respectively to second-order and power law adjustment of the film thickness $h$ as a function of time $t$ around the instant $t=45 \mathrm{~s}$ for $\mathrm{Bo}=35$ obtained at RH $=50 \%$ and $t=130$ s for bubbles with $\mathrm{Bo}=25$ obtained at $\mathrm{RH}=100 \%$. (b) Thinning rate $V_{d}$ predicted by the model as a function of the measured thinning rate $d h / d t$. The black line corresponds to a line of equation $y=x$. The black dashed line corresponds to the equation $y=-11.1+x$. The error bars take into account errors in the measured parameters and are calculated using the error propagation formula.
measurements. Finally, the thinning rate $V_{d}$ due to the marginal regeneration is linked to $V^{-}$by the mass conservation so that $V_{d} \sim \frac{V^{-h}}{R}$.

In Fig. 5(b), we compare both thinning rates. In the absence of evaporation (at $\mathrm{RH}=100 \%$ ), the measured thinning rates are in excellent agreement. This means that the sliding puzzle dynamics entirely describes the drainage of a bubble over time. Marginal regeneration is therefore the main thinning mechanism in a saturated humidity environment.

For $\mathrm{RH}=50 \%$, the thinning rates measured directly at the top of the bubble cap are more important than the ones attributed to marginal regeneration, which is due to the contribution of evaporation to the thinning of the spherical cap. Adding the evaporation flux to the thinning rate
predicted by the marginal regeneration model should allow recovery of the actual thinning rate. From our measurements in Fig. 5(b), we deduce an evaporation flux of $11 \mathrm{~nm} \mathrm{~s}^{-1}$. This is smaller than but close to the flux calculated taking into account the convective evaporation of the liquid bath [8,41], which is around $35 \mathrm{~nm} \mathrm{~s}^{-1}$.

Note that the main approximation is the use of circles to estimate the area of the patches. The true, elongated, shape of the patches would result in a decreased density of the presence of thin zones along the virtual line where the surface conservation is used to estimate the downward velocity $V^{-}$of the thick zones. This would slightly lower the downward velocity [Eq. (2)] and the corresponding thinning rate $V_{d}$. The second important approximation is that we compare the thinning rate corresponding to the sliding puzzle dynamics to that measured at the apex of the bubble. As mentioned earlier, the underlying assumption that this thinning rate at the apex is representative of that at the foot of the bubble is corroborated by previous works on the drainage of surface bubbles [12] as well as by the constant opening velocity of the hole after puncture.

## IV. CONCLUSION

In conclusion, our data allow direct quantification of the effect of marginal regeneration on the overall drainage of a bubble cap. Our results agree with a drainage model where marginal regeneration explains completely the thinning dynamics of the whole cap in the absence of evaporation.

To some extent, this work can be seen as a confirmation of the assumption of Lhuissier et al. [12] that the drainage through the pinch and the marginal regeneration are coupled and of the same order of magnitude. This is also a counterpart of this model in the sense that our results suggest that both contributions are not of the same order of magnitude but actually equal because the possibility for thick zones to descend is conditioned by the ascension of thin patches, in agreement with the view of Seiwert et al. [24] for foam films. The scenario that we propose is thus the following. The liquid drainage is indeed limited by the pinch thickness. Nevertheless, this liquid flow necessitates a replacement of the thick zones flowing downwards by thinner zones rising upwards to ensure surface conservation. A degree of freedom to ensure the global coherence of the problem is the thickness of the pinch, which impacts both the sliding puzzle dynamics and the limitation of the liquid flow. Capillary suction therefore leads to the pinching of the film, which limits the liquid velocity, while marginal regeneration regulates the thickness of this pinching and allows the sliding puzzle dynamics. Additionally, we showed that the rising dynamics of the patches is well described by the model of Seiwert et al. [24], driven by gravity and limited by surface shear viscosity. The liquid film forming the cap of the bubble can thus be viewed as a two-dimensional fluid with a local density proportional to its thickness. The motions induced by the density differences within the film are limited by surface shear viscous dissipation. The overall thinning of this 2D sheet is conditioned by the 3D Poiseuille flow within the pinch since it induces the thinning of the pinch and eventual detachment of thin patches. Lastly, our data are in good agreement with a gravitydriven instability [26]. We believe that the experimental description proposed in this Letter is a necessary step to describe further the bubble drainage, for example for other surfactants or at larger concentrations.

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