

Iron coordination in liquid FeAl_2O_4

James Drewitt, Adrian Barnes, Sandro Jahn, Richard Brooker, Louis Hennet, Daniel Neuville, Henry Fischer

▶ To cite this version:

James Drewitt, Adrian Barnes, Sandro Jahn, Richard Brooker, Louis Hennet, et al.. Iron coordination in liquid FeAl_2O_4. Philosophical Transactions of the Royal Society A: Mathematical, Physical and Engineering Sciences, 2023, 381 (2258), 10.1098/rsta.2022.0351. hal-04189043

HAL Id: hal-04189043 https://hal.science/hal-04189043

Submitted on 29 Aug 2023

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.



Distributed under a Creative Commons Attribution 4.0 International License

PHILOSOPHICAL TRANSACTIONS A

royalsocietypublishing.org/journal/rsta

Research



Cite this article: Drewitt JWE, Barnes AC, Jahn S, Brooker RA, Hennet L, Neuville DR, Fischer HE. 2023 Iron coordination in liquid FeAl₂O₄. *Phil. Trans. R. Soc. A* **381**: 20220351. https://doi.org/10.1098/rsta.2022.0351

Received: 31 January 2023 Accepted: 5 April 2023

One contribution of 13 to a theme issue 'Exploring the length scales, timescales and chemistry of challenging materials (Part 1)'.

Subject Areas:

atomic and molecular physics

Keywords:

high temperature, liquid structure, neutron diffraction, molecular dynamics, levitation, iron coordination

Author for correspondence:

James W. E. Drewitt e-mail: james.drewitt@bristol.ac.uk

tion in liquid ²School of Earth S **81**: 20220351. Building, Queens

liquid FeAl₂O₄ James W. E. Drewitt^{1,2}, Adrian C. Barnes¹,

Iron coordination in

Sandro Jahn³, Richard A. Brooker², Louis Hennet^{4,5}, Daniel R. Neuville⁶ and Henry E. Fischer⁷

¹School of Physics, University of Bristol, H H Wills Physics Laboratory, Tyndall Avenue, Bristol BS8 1TL, UK ²School of Earth Sciences, University of Bristol, Wills Memorial Building, Queens Road, Bristol BS8 1RJ, UK ³Institute of Geology and Mineralogy, University of Cologne, Zuelpicher Strasse 49b, Cologne 50674, Germany ⁴Interfaces, Confinement, Matériaux et Nanostructures (ICMN), CNRS, Université d'Orléans, Orléans Cedex 2 45071, France ⁵Conditions Extrêmes et Matériaux: Haute Température et Irradiation (CEMHTI), CNRS, Université d'Orléans, Orléans Cedex 2 45071, France ⁶Géomatériaux, Institut de Physique du Globe de Paris (IPGP), CNRS, Institut de physique du globe de Paris, Université de Paris Cité, 1 rue Jussieu, Paris 75005, France ⁷Institut Laue-Langevin, 71 Avenue des Martyrs, CS 20156, Grenoble Cedex 9 38042, France

JWED, 0000-0002-3510-4155; ACB, 0000-0002-4324-4641;
 SJ, 0000-0002-2137-8833; RAB, 0000-0003-4931-9912;
 LH, 0000-0002-2992-4800; DRN, 0000-0002-8487-5001;
 HEF, 0000-0002-1204-0750

The structure of aerodynamically levitated liquid FeAl₂O₄ was measured by neutron diffraction with isotope substitution (NDIS). Classical and *ab initio* molecular dynamics simulations were performed and their results were found to be in close agreement with each other and the NDIS data. The results reveal that molten FeAl₂O₄ may be considered as an ionic liquid without any preference for particular short-range structural motifs.

This article is part of the theme issue 'Exploring the length scales, timescales and chemistry of challenging materials (Part 1)'.

© 2023 The Authors. Published by the Royal Society under the terms of the Creative Commons Attribution License http://creativecommons.org/licenses/ by/4.0/, which permits unrestricted use, provided the original author and source are credited.

THE ROYAL SOCIETY PUBLISHING

1. Introduction

As one of the most abundant elements on Earth, iron is a major constituent of natural magmas. The ability of iron to exist in different valence states can play a crucial role in altering the physical properties, such as viscosity, density and melting point, of the geological melts that control geochemical processes in the Earth's deep interior [1-3]. Due to its important geological role, extensive experimental and simulation studies have been conducted to understand how iron is incorporated in the structure of oxide liquids and glasses (see reviews [4-8] and references therein). However, despite this extensive body of research, the local coordination of Fe by oxygen in these melts remains uncertain. Traditionally, particularly for silicate systems, comparisons are made with mineral structures. Strong fourfold (tetrahedral) or sixfold (octahedral) structural motifs are assumed for the liquid, with the former dominantly associated with Fe³⁺ taking a similar role to fourfold coordinated Al³⁺, and the latter mainly associated with Fe²⁺. However, XANES studies on silicate melts suggest an average of fivefold coordination for a wide range of Fe^{2+}/Fe^{3+} ratios [2,9–11], only moving towards fourfold at the highest Fe^{3+} contents. The dominance of the fivefold average over a considerable range of Fe^{2+}/Fe^{3+} ratios could result from all Fe being fivefold coordinated (as seen in some minerals) or a near constant mix of fourfold and sixfold coordination, with or without fivefold units [9]. However, although X-ray absorption and Mössbauer spectroscopy are the most widely employed techniques to determine iron coordination in geological glasses and melts [4], their reliance on indirect interpretation of spectra based on crystalline calibration data is a major limitation. Comparison between mineral analogues and melt structures is unreliable for compositions outside of the calibrated silicate range and risky even for simple iron oxides [12]. By contrast, diffraction techniques offer direct measurement of the local structure in liquids and glasses and are hence a valuable but underutilized tool in this field [12-14].

In this paper, we have employed the method of neutron diffraction with isotope substitution (NDIS) to measure directly the Fe–O coordination environment of aerodynamically levitated liquid FeAl₂O₄ at 2200 K. The NDIS data are analysed in combination with classical and *ab initio* molecular dynamics simulations to obtain an accurate atomic-scale model of the liquid structure.

2. Theory

Downloaded from https://royalsocietypublishing.org/ on 29 August 2023

The coherent scattering intensity of liquid ${\rm FeAl_2O_4}$ measured by neutron diffraction is represented by the total structure factor

$$F(Q) = \sum_{\alpha}^{3} \sum_{\beta}^{3} c_{\alpha} c_{\beta} b_{\alpha} b_{\beta} [S_{\alpha\beta}(Q) - 1], \qquad (2.1)$$

where *c* and *b* denote the atomic fraction and coherent neutron scattering length of chemical element α or β , $S_{\alpha\beta}(Q)$ is a Faber & Ziman [15] partial structure factor, and *Q* is magnitude of the elastic scattering vector. In this study, two FeAl₂O₄ samples were prepared that were identical in every respect except for their isotopic composition, containing either ⁵⁴Fe or ^{nat}Fe (i.e. Fe in its natural isotopic abundance). Due to the contrast in neutron scattering lengths ($b_{nat} = 0.945(2)$ fm cf. $b_{54} = 0.42(1)$ fm [16]) all $S_{\alpha\beta}(Q)$ functions involving Fe receive different weightings leading to observably different total structure factors ^{nat}F(Q) and ⁵⁴F(Q) measured for the two samples.

All correlations not involving Fe are identical in both measurements and can be eliminated in the difference function

$$\Delta F_{\rm Fe}(Q) \equiv {}^{\rm nat}F(Q) - {}^{54}F(Q)$$

= $2c_{\rm Fe}(b_{\rm nat} - b_{54}) \Big(c_{\rm O}b_{\rm O}[S_{\rm FeO}(Q) - 1] + c_{\rm Al}b_{\rm Al}[S_{\rm FeAl}(Q) - 1] \Big)$
+ $c_{\rm Fe}^2 (b_{\rm nat}^2 - b_{54}^2) [S_{\rm FeFe}(Q) - 1].$ (2.2)

$$\Delta F_{\mu}(Q) \equiv \frac{b_{\text{nat}}^{54} F(Q) - b_{54}^{\text{nat}} F(Q)}{b_{\text{nat}} - b_{54}}$$

= $2c_{\text{AI}}c_{\text{O}}b_{\text{AI}}b_{\text{O}}[S_{\text{AIO}}(Q) - 1] + c_{\text{AI}}^{2}b_{\text{AI}}^{2}[S_{\text{AIAI}}(Q) - 1]$
+ $c_{\text{O}}^{2}b_{\text{O}}^{2}[S_{\text{OO}}(Q) - 1] - c_{\text{Fe}}^{2}b_{\text{nat}}b_{54}[S_{\text{FeFe}}(Q)].$ (2.3)

The total pair distribution function G(r) provides a measure of the variation in atom–atom pair density as a function of distance r in real-space, and is determined by the Fourier transformation

(

$$G(r) = \frac{1}{2\pi^2 r\rho} \int_0^\infty Q[F(Q)] \sin(Qr) \, \mathrm{d}Q$$
$$= \sum_{\alpha=1}^n \sum_{\beta=1}^n c_\alpha c_\beta b_\alpha b_\beta [g_{\alpha\beta}(r) - 1], \qquad (2.4)$$

where $g_{\alpha\beta}(r)$ is a partial pair distribution function. The mean coordination number, \bar{n}_{α}^{β} , gives the average number of β atoms in a spherical coordination shell of radius $r_1 \le r \le r_2$ centred on an atom of type α and is obtained by integrating over a peak in real-space arising from a specific $g_{\alpha\beta}(r)$ function, according to

$$\bar{n}_{\alpha}^{\beta} = 4\pi\rho c_{\beta} \int_{r_1}^{r_2} g_{\alpha\beta}(r) r^2 \,\mathrm{d}r.$$
(2.5)

It is important to recognize that the coordination number is not precisely defined. In general, peaks in G(r) overlap so that the contribution from neighbouring peaks cannot be unambiguously separated. Similarly, the coordination number is a statistical quantity that is an average so that it does not need to be an integer. Hence, we do not need to and it is not helpful to discuss atomic coordination in liquids in terms of strict and clearly coordinated structural motifs (tetrahedra, octahedra, etc.).

The real-space difference functions, denoted $\Delta G_{\text{Fe}}(r)$ and $\Delta G_{\mu}(r)$, are obtained by Fourier transforming the corresponding reciprocal-space functions in equations (2.2) and (2.3), respectively, and are defined by replacing the $S_{\alpha\beta}(Q)$ functions in $\Delta F_{\text{Fe}}(Q)$ and $\Delta F_{\mu}(Q)$ with their corresponding real-space partials $g_{\alpha\beta}(r)$.

3. Methods

Downloaded from https://royalsocietypublishing.org/ on 29 August 2023

(a) Sample preparation

Polycrystalline FeO was synthesized by oxidizing pure Fe (Alfa Aesar, powder, spherical, $<10 \,\mu$ m, 99.9%) or ⁵⁴Fe (Pennywood chemicals, foil, 99.91% enrichment) in a gas-mixing vertical tube furnace at the University of Bristol petrology laboratory, using a CO/CO₂ mixture to control the oxygen fugacity (fO_2). The samples were heated in Al₂O₃ crucibles at 1173 K for approximately 48 h at an fO_2 of 10^{-14} bar. The samples were re-ground in an agate pestle and mortar periodically every 12 h during heat treatment to ensure sample homogeneity. The unit cell parameter for the synthesized ^{nat}FeO sample was measured using a Bruker D8 X-ray powder diffractometer giving a = 4.2892 Å, corresponding to Fe_{0.961}O stoichiometry [17].

The ^{nat}FeAl₂O₄ and ⁵⁴FeAl₂O₄ samples were prepared by mixing the synthesized FeO or ⁵⁴FeO with dried Al₂O₃ (Alfa Aesar, 99.995%) powder in the appropriate proportions in an agate pestle and mortar to achieve a powder grain size of $\leq 30 \,\mu$ m. The powder mixtures were heated for 2 h in Pt capsules at 1773 K at an fO_2 of $10^{-9.5}$ bar. To ensure there was no Fe loss to the Pt capsules, they were pre-saturated using Fe (Alfa Aesar, 99.9%) or ⁵⁴Fe (AERE, Harwell) powders at 1273 K at an f_{O_2} of $10^{-7.6}$ bar to form a Fe–Pt alloy skin on the interior of the Pt capsule [18]. Polycrystalline samples appeared dark green, as expected for Hercynite (Fe²⁺Al₂O₄). A mass of approximately 400 mg per sample was recovered cleanly from the Pt capsule. In preparation for

(b) Neutron diffraction experiment

The neutron diffraction measurements were performed using the D4c neutron diffractometer [19] at the Institut Laue-Langevin research reactor in Grenoble, France. The experiment [20] was performed using a monochromatic beam of neutrons of wavelength 0.4961(1) Å and the aerodynamic levitation and CO₂ laser-heating apparatus developed by Hennet et al. [21]. To reduce background scattering from the sample environment, the 9 mm horizontal and 48 mm vertical incident beam was collimated vertically using two neutron absorbing ¹⁰B₄C panels with 4mm separation, positioned close to the sample position. The upper section of the conical levitation nozzle was machined from vanadium which has an almost entirely incoherent neutron scattering cross-section [16]. Prior to the liquid diffraction measurements, the instrument sample chamber was evacuated to $\lesssim 10^{-4}$ mbar and filled to atmospheric pressure with the levitation gas (Ar + 5 ppm O_2) to prevent oxidation of the sample or reduction to metallic Fe and to ensure a reproducible atmosphere for reliable background correction. The $\leq 3 \text{ mm}$ diameter levitated samples were melted using two 125 W CO2 lasers (Synrad 60-1) of wavelength 10.6 μ m incident from above the sample at 20° to the vertical axis and heated to a constant temperature of 2200(30) K, as measured by an optical pyrometer placed within the instrument sample chamber operating at a wavelength of 0.85 µm. Heating from two angles, combined with the continuous rotation of the levitated sample, reduced the temperature inhomogeneity due to cooling from the levitation gas to approximately 50K at 2200K on the lower portion of the sample, which is obstructed from the incident neutron beam by the ¹⁰B₄C collimator [21]. During the measurements, the measured temperatures remained very stable within ± 20 K. Neutron diffraction patterns of the levitated ^{nat}FeAl₂O₄ and ⁵⁴FeAl₂O₄ liquids were recorded for 5h, with the full detector range scanned at intervals of 15-30 min. Crystallization events occasionally occurred in both samples upon which the experiments were paused to re-melt the sample before continuing the measurements. For each set of measurements, successive diffraction patterns for every full detector scan were compared and any measurements found to be inconsistent within the statistical noise were rejected. Two background diffraction measurements of the empty levitation apparatus were made, one inside the Argon-filled sample chamber with a continuous flow of levitation gas and one in the evacuated chamber. An additional measurement of a 5 mm diameter solid vanadium sphere, placed on top of the levitation nozzle within the evacuated diffraction chamber with a volume above the nozzle similar to the levitated sample volume illuminated by neutrons, was conducted for the purpose of normalization [22].

Before corrections the background scattering data from the levitation nozzle under vacuum were subtracted from the sample and the nozzle (with the levitation gas present) data. Corrections for the levitation gas ('empty container'), self attenuation and Plazcek corrections for the samples and vanadium were applied [22]. Due to the small size of the sample, the attenuation corrections are small (less than 5% with little angular dependence) and any multiple scattering is negligible. A final, small, normalization correction (due to uncertainties in the scattering volume of the sample and vanadium sphere) was made to the data to ensure consistency with the known scattering lengths of the sample.

In addition to the nuclear scattering from the atomic nuclei there is also a contribution from the paramagnetic scattering of the electrons on the Fe²⁺ ions that manifests itself as a Q dependent scattering contribution in the data. This contribution is unchanged in the two isotopically different samples and cancels in the first order difference. However, for the total structure factors and $\Delta F_{\mu}(Q)$ it appears as an unwanted slope in the data that gives unphysical contributions in G(r) at small r. For the case of Fe²⁺ the orbital angular momentum (L) contribution to this scattering

is small and we have taken the total angular momentum as $J \sim S$ [23] so that the magnetic crosssection may be taken as [24]

$$\frac{\mathrm{d}\sigma}{\mathrm{d}\Omega} \simeq 4c_M(\gamma r_e)^2 < j_0 >^2 (Q), \tag{3.1}$$

where

$$\langle j_0(Q) \rangle^2 = 0.0263 \exp(-34.9597Q^2) + 0.3668 \exp(-15.9435Q^2) + 0.6188 \exp(-5.5935Q^2) - 0.0119,$$
 (3.2)

where the coefficients have been taken from the International Table for Crystallography [25]. All analysis of the scattering data was made after this contribution had been removed.

(c) Classical molecular dynamics

Molecular dynamics (MD) simulations of liquid FeAl₂O₄ were carried out using DLPOLY (v.3.17) [26]. Morse potentials for Fe²⁺, Al³⁺ and O²⁻ ions were taken from the paper of Pedone *et al.* [27]. The simulations were carried out with 9996 atoms (1428 Fe, 2856 Al and 5712 O) giving the same stoichiometry as the samples. The simulation cubic box size was of length 49.83 Å corresponding to an atomic number density of 0.0808 Å⁻³. The simulation was run at 2500 K using a Berendsen *NVT* thermostat using 1 fs steps and was run for a total of 50 000 steps (50 ps) with 500 equilibration steps (0.5 ps) at the start.

The final MD configuration was used as the input configuration for a Reverse Monte Carlo (RMCPROFILE [28]) refinement of the structure to the measured diffraction data. The total structure factors ^{nat}F(Q) and ⁵⁴F(Q) measured for the two isotopic samples and the difference functions $\Delta F_{\text{Fe}}(Q)$ and $\Delta F_{\mu}(Q)$ were included in the refinement. The refinement was run with approximately 350 000 moves generated after which the structure factors for the refined configuration had converged with the experimental data. No significant differences were observed between the MD and RMC refined data, demonstrating strong consistency between the classical MD model and the neutron diffraction measurements.

(d) Ab initio molecular dynamics

Ab initio molecular dynamics (AIMD) simulations were performed using the Quickstep module of the CP2K code [29]. The particle interactions were treated in the frame of density functional theory with a mixed Gaussian and planewave approach [30]. A multi-grid with five levels was employed for real-space integration with a planewave cut-off of 800 Ry for the finest level and a relative cut-off for Gaussian mapping of 70 Ry. As basis sets, we chose the MOLOPT split valence double-zeta valence plus polarization parameters [31] supplied by CP2K. For computational efficiency, we employed Goedecker-Teter-Hutter pseudopotentials [32]. As the exchange-correlation functional, the generalized gradient approximation (GGA) according to Perdew et al. (PBE) [33] was used. Due to unpaired spins in the d-orbitals of Fe, the electronic structure calculations were done in spin-polarized mode. We performed simulations without and with Hubbard-U correction [34], the latter to account for the strong correlations between Fe delectrons. While the resulting structure model from standard GGA was already in good agreement with the experiments, including +U did have a minor effect on the Fe–O and Fe–Fe correlations and a slight improvement in the overall agreement with the NDIS data. Here, we chose the same U - J parameter of 2.5 eV as in a previous study of Fe-bearing oxide melt [35]. In the following, only results of the GGA + U simulations are presented. The periodic simulation box contained 112 atoms, i.e. 16 formula units of FeAl₂O₄. Initial structures were adopted from earlier AIMD simulations of CaAl₂O₄ melts [36]. The cubic box length was set to 11.15 Å, and simulations were performed in the canonical ensemble at constant volume and temperature with a particle density of 0.0808 Å⁻³. The temperature of 2200 K was controlled by the canonical sampling through velocity rescaling method [37] using a time constant of 0.1 ps. The AIMD time step was set to 1 fs. After initial equilibration, structural properties were derived from a 20 ps production run.



Figure 1. (*a*) Total structure factors ^{nat}F(Q) and ⁵⁴F(Q) and difference functions (*b*) $\Delta F_{Fe}(Q)$ and (*c*) $\Delta F_{\mu}(Q)$ of aerodynamically levitated liquid FeAl₂O₄ at 2200 K as measured using the D4C neutron diffractometer (blue) shown together with the corresponding functions computed from the MD (black) or AIMD (red) simulation trajectories. (Online version in colour.)



Figure 2. (*a*) Total pair distribution functions ^{nat}G(r) and ⁵⁴G(r) and difference functions (*b*) $\Delta G_{Fe}(r)$ and (*c*) $\Delta G_{\mu\nu}(r)$ for aerodynamically levitated liquid FeAl₂O₄ at 2200 K as determined by Fourier transforming the corresponding reciprocal-space functions in figure 1 (blue), shown together with the corresponding functions computed from the MD (black) or AIMD (red) simulation trajectories. (Online version in colour.)

function	technique	r _{AlO} (Å)	r _{Fe0} (Å)	r ₀₀ (Å)	$\bar{n}_{ m Al}^{ m 0}$	$\bar{n}_{ m Fe}^0$	r ₂ (Å)
$^{nat}G(r)$	NDIS	1.80(2)		2.89(5)			
^{nat} G(r)	MD	1.77(2)		2.84(5)			
^{nat} G(r)	AIMD	1.85(2)		2.95(5)			
⁵⁴ G(r)	NDIS	1.79(2)		2.81(5)			
⁵⁴ G(r)	MD	1.72(2)		2.83(5)			
⁵⁴ G(r)	AIMD	1.81(2)		2.90(5)			
$\Delta G_{\mu}(r)$	NDIS	1.78(1)		2.77(5)	4.34(5)		2.15(1)
$\Delta G_{\mu}(r)$	MD	1.70(1)		2.82(5)	3.83(5)		2.20(2)
$\Delta G_{\mu}(r)$	AIMD	1.79(1)		2.86(5)	4.16(5)		2.23(1)
$\Delta G_{\rm Fe}(r)$	NDIS		1.93(3)			3.26(5)	2.36(1)
$\Delta G_{\rm Fe}(r)$	MD		2.00(3)			3.40(5)	2.42(5)
$\Delta G_{\rm Fe}(r)$	AIMD		1.98(3)			3.78(5)	2.45(5)
g _{AIO} (r)	MD	1.70(1)			4.25(5)		2.50(1)
g _{AIO} (r)	AIMD	1.79(1)			4.40(5)		2.50(1)
g _{FeO} (r)	MD		2.01(3)			4.95(5)	2.90(1)
g _{FeO} (r)	AIMD		1.98(3)			4.94(5)	2.90(1)
g ₀₀ (r)	MD			2.78(3)			
g ₀₀ (r)	AIMD			2.78(3)			

4. Results

The total structure factors $^{nat}F(Q)$ and $^{54}F(Q)$ of the levitated FeAl₂O₄ liquids at 2200(30) K are shown in figure 1a together with the structure factors computed from the MD and AIMD simulation trajectories. Small discrepancies between the experimental and simulation results are observed in the region of the principal peak in F(Q), which relates to structural ordering on extended length scales [38]. These longer range correlations are not fully captured in the AIMD simulations due to the relatively small periodic simulation box of 112 atoms. A marked improvement in capturing these low-Q features is observed for the larger-scale classical MD simulations. The reciprocal-space difference functions $\Delta F_{\rm Fe}(Q)$ (equation 2.2) and $\Delta F_{\mu}(Q)$ (equation 2.3) are shown in figure 1b,c, respectively. The corresponding real-space functions $^{nat}G(r)$, $^{54}G(r)$, $\Delta G_{Fe}(r)$ and $\Delta G_{\mu}(r)$ are shown in figure 2. Peak bond distances $r_{AlO}(\text{\AA})$, $r_{\rm FeO}$ (Å), $r_{\rm OO}$ (Å) and average coordination numbers $\bar{n}_{\rm Al}^{\rm O}$, $\bar{n}_{\rm Fe}^{\rm O}$ obtained from the experimental and simulated real-space functions are reported in table 1. The NDIS, MD and AIMD results are in good overall agreement within the bounds of uncertainty, although the bond distances r_{AIO} and r_{FeO} determined are slightly more consistent with the experimental difference functions for the AIMD calculations than the classical MD results. In $\Delta G_{\mu}(r)$, all correlations involving Fe and the chemical element $\mu \neq$ Fe are eliminated such that the first peak at 1.78(1)Å arises solely from nearest neighbour Al–O correlations. In $\Delta G_{\rm Fe}(r)$, there is no indication of any residual contribution from Al-O correlations, indicating all correlations not involving Fe are successfully eliminated. This provides a direct measurement of the nearest neighbour Fe–O peak at 1.93(3) Å which cannot be resolved in ${}^{nat}G(r)$ or ${}^{54}G(r)$. Although the $g_{AIO}(r)$ and $g_{FeO}(r)$ are successfully



Figure 3. Faber–Ziman partial structure factors $S_{\alpha\beta}(Q)$ for liquid FeAl₂O₄ at 2200 K computed from the MD (black) or AIMD (red) simulation trajectories. (Online version in colour.)

separated in the $\Delta G_{\mu}(r)$ and $\Delta G_{\text{Fe}}(r)$ difference functions, they are not entirely isolated from other correlations, especially towards higher-*r* where contributions from other atomic pair interactions become more significant. Hence, the first minimum in $\Delta G_{\mu}(r)$ and $\Delta G_{\text{Fe}}(r)$ does not correspond to the first minimum in $g_{\text{AlO}}(r)$ and $g_{\text{FeO}}(r)$, respectively, resulting in an underestimate of the calculated average coordination numbers due to the limited integration range.

The Faber–Ziman partial structure factors $S_{\alpha\beta}(Q)$ and pair distribution functions $g_{\alpha\beta}(r)$ calculated from the atomic configurations generated by the MD and AIMD simulations are shown in figures 3 and 4, respectively. Considering the AIMD results, the first peak in $g_{AIO}(r)$ appears at 1.79(1) Å and gives an average coordination number $\bar{n}_{AI}^{O} = 4.40(5)$ when integrated to the first minimum at 2.50(1) Å. The first peak in $g_{FeO}(r)$ appears at 1.98(3) Å and gives an average coordination number of $\bar{n}_{Fe}^{O} = 4.94(5)$ when integrated to the first minimum at 2.90(1) Å.

5. Discussion

The results from the MD and AIMD simulations show strong similarities and good broad agreement with the NDIS data at both the total and difference function level (figures 1 and 2). The first peak in $g_{AIO}(r)$ at 1.79(1) Å is close to that observed in other aluminate oxide liquids and glasses [39–42]. However, there is a notable asymmetry of the peak on the high *r* side and the first minimum in $g_{AIO}(r)$ does not reach zero. A close analysis of the oxygen coordination around aluminium from the MD and AIMD simulations shows that, unlike most aluminate glasses in



Figure 4. Partial pair distribution functions $g_{\alpha\beta}(r)$ for liquid FeAl₂O₄ at 2200 K computed from the MD (black) or AIMD (red) simulation trajectories. (Online version in colour.)

Downloaded from https://royalsocietypublishing.org/ on 29 August 2023

which aluminium is almost entirely fourfold coordinated by oxygen [40,41,43], there is a large variation in the coordination number around the individual aluminium atoms. Although the results show the predominance (55%) of fourfold coordinated species in the first coordination shell (defined by the first minimum in real-space), it is evident, unlike the case for aluminate glasses [40], that the Al–O structure cannot be considered as an extended network of corner shared AlO₄ tetrahedra but rather a dynamically varying local coordination consistent with a high temperature liquid [44].

The first peak observed in $g_{\text{FeO}}(r)$ at 1.98(3) Å, is consistent with the Fe–O distance associated with Fe²⁺ ions [45]. It is clear from the far from zero value of $g_{\text{FeO}}(r)$ at the first minimum that well defined species of fixed coordination do not exist in the liquid. A close analysis of the oxygen coordination of the iron atoms in the MD and AIMD simulations (figure 5) shows that, even within the first coordination shell there is no coordination preference for oxygen atoms around iron atoms with large numbers of fourfold, fivefold and sixfold coordinated atoms present simultaneously. In the literature, the oxygen coordination around iron is often cited as the origin of many of the properties (viscosity, etc.) of iron-containing liquids. In particular, reference is frequently made to strong fourfold (tetrahedral) or sixfold (octahedral) structural motifs being present in the liquid [5]. In this study, we find no evidence for a dominant and fixed coordination but rather a continuous distribution of local environments. If strong bonding in rigid structural motifs was present we would expect considerable oscillatory structure out to high Q in $\Delta F_{\text{Fe}}(Q)$. This is clearly not observed. The results presented here are consistent with the conclusions of



Figure 5. (*a*) Pair distribution function $g_{Fe0}(r)$ (black) and running coordination number (red) as calculated from the MD (solid curves) and AIMD (dashed curves) simulations. (*b*) Fraction of partial coordination numbers *n*(Fe0) from 0 to 7 as a function of distance. (Online version in colour.)

Alderman *et al.* [14], who similarly found a wide variation in the iron–oxygen coordination in liquid Fe₂SiO₄.

The close similarity between the MD and AIMD simulations and their good agreement with the experimental data supports a conclusion that liquid FeAl₂O₄ may be treated fundamentally as an ionic liquid. The potentials used in the MD simulation are ionic in nature and the simulation consisting of approximately 10 000 atoms in a box size of approximately 50 Å in length is sufficient to obtain a good representation of the medium range ordering of the ions. By contrast, the AIMD simulation, while containing considerably fewer atoms, gives more direct information about the short-range order (bonding) and in particular, it is possible to probe the electron distributions around the atoms as well. An examination of the electron distributions obtained from the AIMD simulation confirms that almost complete charge transfer has taken place between the Fe and Al atoms and the oxygen atoms with a small indication of some polarization of the electron distribution on the O^{2-} ions. It is this almost complete charge transfer that explains the excellent agreement between the MD and AIMD results.

In summary, the close agreement between the experimental data and two independent simulations supports the conclusion that both the AIMD and MD methods give reliable atomistic models of the structure of liquid FeAl₂O₄. Furthermore, it supports the conclusion that this and other aluminate liquids may be considered as fundamentally ionic in nature with no requirement for strong, covalently bonded, structural motifs (i.e. tetrahedra or octahedra) to be present. Indeed, the results show little preference at all for a preferred local structure around the iron ions.

6. Conclusion

In this work, we have demonstrated, through close comparison of computer simulation and detailed structural measurements from neutron diffraction and isotopic substitution, that liquid

Data accessibility. The raw neutron diffraction data are available at: https://doi.org/10.5291/ILL-DATA.6-03-441 [19]. Analysed data are available at the University of Bristol Research data repository, data.bris, at https://doi.org/10.5523/bris.w9d5ypz91ltv2wksargnm510s [46].

Authors' contributions. J.W.E.D.: conceptualization, data curation, formal analysis, funding acquisition, investigation, methodology, project administration, resources, software, validation, visualization, writing—original draft, writing—review and editing; A.C.B.: conceptualization, data curation, formal analysis, funding acquisition, investigation, methodology, resources, software, validation, visualization, writing—original draft, writing—review and editing; S.J.: data curation, formal analysis, investigation, methodology, resources, software, validation, writing—original draft, writing—review and editing; S.J.: data curation, formal analysis, investigation, methodology, resources, software, validation, writing—original draft, writing—review and editing; R.A.B.: investigation, methodology, resources, writing—review and editing; D.R.N.: investigation, methodology, writing—review and editing; H.E.F.: data curation, investigation, resources, writing—review and editing.

All authors gave final approval for publication and agreed to be held accountable for the work performed therein.

Conflict of interest declaration. We declare we have no competing interests.

Funding. This work was supported by the EPSRC (grant no. EP/V001736/1) to A.C.B. and J.W.E.D.

Acknowledgements. Computing time for the AIMD simulations was provided by the Gauss Centre for Supercomputing e.V. to S.J. through the John von Neumann Institute for Computing (NIC) on the JUWELS supercomputer at Jülich Supercomputing Centre (JSC).

References

Downloaded from https://royalsocietypublishing.org/ on 29 August 2023

- Dingwell DB, Virgo D. 1987 The effect of oxidation state on the viscosity of melts in the system Na₂O-FeO-Fe₂O₃-SiO₂. *Geochim. Cosmochim. Acta* 51, 195–205. (doi:10.1016/ 0016-7037(87)90231-6)
- 2. Wilke M. 2005 Fe in magma—an overview. Ann. Geophys. 48, 509–617. (doi:10.4401/ag-3222)
- Di Genova D, Vasseur J, Hess K-U, Neuville DR, Dingwell DB. 2017 Effect of oxygen fugacity on the glass transition, viscosity and structure of silica- and iron-rich magmatic melts. J. Non-Cryst. Solids 470, 78–85. (doi:10.1016/j.jnoncrysol.2017.05.013)
- Henderson GS, de Groot FMF, Moulton BJA. 2014 X-ray absorption near-edge structure (XANES) spectroscopy. *Rev. Mineral. Geochem.* 78, 75–138. (doi:10.2138/rmg.2014.78.3)
- Mysen B, Richet P. 2019 Chapter 11—Structure of iron silicate glasses and melts. In *Silicate glasses and melts* (eds B Mysen, P Richet), pp. 403–430, 2nd edn. Amsterdam, the Netherlands: Elsevier.
- 6. Losq C, Cicconi MR, Neuville DR. 2021 *Iron in silicate glasses and melts,* pp. 233–253, Ch. 12. Washington DC: American Geophysical Union (AGU).
- Drewitt JWE, Hennet L, Neuville D. 2022 From short to medium range order in glasses and melts by diffraction and Raman spectroscopy. *Rev. Mineral. Geochem.* 87, 55–103. (doi:10.2138/rmg.2022.87.02)
- Jahn S. 2022 Molecular simulations of oxide and silicate melts and glasses. *Rev. Mineral. Geochem.* 87, 193–227. (doi:10.2138/rmg.2022.87.05)
- Wilke M, Partzsch GM, Bernhardt R, Lattard D. 2005 Determination of the iron oxidation state in basaltic glasses using XANES at the K-edge. *Chem. Geol.* 220, 143–161. (doi:10.1016/j.chemgeo.2005.03.004)
- Fiege A, Ruprecht P, Simon AC, Bell AD, Göttlicher J, Newville M, Lanzirotti T, Moore G. 2017 Calibration of Fe XANES for high-precision determination of Fe oxidation state in glasses: comparison of new and existing results obtained at different synchrotron radiation sources. *Am. Mineral.* 102, 369–380. (doi:10.2138/am-2017-5822)

- Alderman OLG *et al.* 2017 Iron *k*-edge X-ray absorption near-edge structure spectroscopy of aerodynamically levitated silicate melts and glasses. *Chem. Geol.* 453, 169–185. (doi:10.1016/ j.chemgeo.2017.01.020)
- Shi C, Alderman OLG, Tamalonis A, Weber R, You J, Benmore CJ. 2020 Redoxstructure dependence of molten iron oxides. *Nat. Commun. Mater.* 1, 80. (doi:10.1038/ s43246-020-00080-4)
- 13. Drewitt JWE, Sanloup C, Bytchkov A, Brassamin S, Hennet L. 2013 Structure of $(Fe_xCa_{1-x}O)_y(SiO_2)_{1-y}$ liquids and glasses from high-energy X-ray diffraction: implications for the structure of natural basaltic magmas. *Phys. Rev. B* **87**, 224201. (doi:10.1103/PhysRevB.87.224201)
- 14. Alderman OLG *et al.* 2017 Local structural variation with oxygen fugacity in Fe₂SiO_{4+x} fayalitic iron silicate melts. *Geochim. Cosmochim. Acta* **203**, 15–36. (doi:10.1016/j.gca.2016.12.038)
- Faber TE, Ziman JM. 1965 A theory of the electrical properties of liquid metals. *Philos. Mag.* 11, 153–173. (doi:10.1080/14786436508211931)
- Sears VF. 1992 Neutron scattering lengths and cross sections. Neutron News 3, 26–37. (doi:10.1080/10448639208218770)
- Jette ER, Foote F. 1933 An X-ray study of the wüstite (FeO) solid solutions. *Philos. Mag.* 1, 29. (doi:10.1063/1.1749215)
- 18. Apted MJ. 1982 Control of loss of iron to platinum capsules and effects on samarium partitioning between garnet and melt. *Am. Mineral.* **67**, 9–10.
- Fischer HE, Cuello GJ, Palleau P, Feltin D, Barnes AC, Basyal YS, Simonson JM. 2002 D4c: a very high precision diffractometer for disordered materials. *Appl. Phys. A: Mater. Sci. Process.* 74, s160–s162. (doi:10.1007/s003390101087)
- Drewitt JWE, Barnes AC, Cormier L, Fischer HE, Hennet L, Kohn S, Walter M. 2019 Neutron diffraction with isotope substitution study of levitated liquid Fe₂SiO₄. Grenoble, France: Institut Laue-Langevin (ILL). (doi:10.5291/ILL-DATA.6-03-441)
- 21. Hennet L *et al.* 2006 Levitation apparatus for neutron diffraction investigations on high temperature liquids. *Rev. Sci. Instrum.* 77, 053903. (doi:10.1063/1.2200756)
- Fischer HE, Barnes AC, Salmon PS. 2005 Neutron and X-ray diffraction studies of liquids and glasses. *Rep. Prog. Phys.* 69, 233–299. (doi:10.1088/0034-4885/69/1/R05)
- 23. Bleaney I, Bleaney BI. 1976 *Electricity and magnetism*, 3rd edn. Oxford, UK: Oxford University Press.
- 24. Balcar E, Lovesey SW. 1989 *Theory of magnetic neutron and photon scattering*. Oxford Series. Oxford, UK: Oxford University Press.
- 25. Wilson AJ (ed.). 1992 International tables for crystallography. Volume C: mathematical, physical and chemical tables, 1st edn. Dordrecht, the Netherlands; Boston, MA; London, UK: Kluwer Academic Publishers for the International Union of Crystallography.
- Todorov IT, Smith W, Trachenko K, Dove MT. 2006 Dl poly 3: new dimensions in molecular dynamics simulations via massive parallelism. J. Mater. Chem. 16, 1911–1918. (doi:10.1039/b517931a)
- Pedone A, Malavasi G, Menziani MC, Cormack AN, Segre U. 2006 A new self-consistent empirical interatomic potential model for oxides, silicates, and silica-based glasses. J. Phys. Chem. B 110, 11780–11795. (doi:10.1021/jp0611018)
- Tucker MG, Keen DA, Dove MT, Goodwin AL, Hui Q. 2007 RMCProfile: reverse monte carlo for polycrystalline materials. *J. Phys.: Condens. Matter* 19, 335218. (doi:10.1088/0953-8984/ 19/33/335218)
- Kühne TD *et al.* 2020 CP2K: an electronic structure and molecular dynamics software package—Quickstep: efficient and accurate electronic structure calculations. *J. Chem. Phys.* 152, 194103. (doi:10.1063/5.0007045)
- VandeVondele J, Krack M, Mohamed F, Parrinello M, Chassaing T, Hutter J. 2005 QUICKSTEP: fast and accurate density functional calculations using a mixed Gaussian and plane waves approach. *Comput. Phys. Commun.* 167, 103–128. (doi:10.1016/j.cpc.2004.12.014)
- VandeVondele J, Hutter J. 2007 Gaussian basis sets for accurate calculations on molecular systems in gas and condensed phases. J. Chem. Phys. 127, 114105. (doi:10.1063/1.2770708)
- 32. Goedecker S, Teter M, Hutter J. 1996 Separable dual-space gaussian pseudopotentials. *Phys. Rev. B* 54, 1703–1710. (doi:10.1103/PhysRevB.54.1703)

13

- Perdew JP, Burke K, Ernzerhof M. 1996 Generalized gradient approximation made simple. *Phys. Rev. Lett.* 77, 3865–3868. (doi:10.1103/PhysRevLett.77.3865)
- 34. Cococcioni M. 2010 Accurate and efficient calculations on strongly correlated minerals with the LDA+*U* method: review and perspectives. *Rev. Mineral. Geochem.* **71**, 147–167. (doi:10.2138/rmg.2010.71.8)
- 35. Holmström E, Stixrude L. 2016 Spin crossover in liquid (Mg, Fe)O at extreme conditions. *Phys. Rev. B* **93**, 195142. (doi:10.1103/PhysRevB.93.195142)
- Drewitt JWE, Jahn S, Sanloup C, de Grouchy C, Garbarino G, Hennet L. 2015 Development of chemical and topological structure in aluminosilicate liquids and glasses at high pressure. *J. Phys.: Condens. Matter* 27, 105103. (doi:10.1088/0953-8984/27/10/105103)
- Bussi G, Donadio D, Parrinello M. 2007 Canonical sampling through velocity rescaling. J. Chem. Phys. 126, 014101. (doi:10.1063/1.2408420)
- 38. Elliott SR. 1995 Second sharp diffraction peak in the structure factor of binary covalent network glasses. *Phys. Rev. B* **51**, 8599–8601. (doi:10.1103/PhysRevB.51.8599)
- Drewitt JWE, Jahn S, Cristiglio V, Bytchkov A, Leydier M, Brassamin S, Fischer HE, Hennet L. 2011 The structure of liquid calcium aluminates as investigated using neutron and high energy X-ray diffraction in combination with molecular dynamics simulation methods. *J. Phys.: Condens. Matter* 23, 155101. (doi:10.1088/0953-8984/23/15/155101)
- Drewitt JWE, Hennet L, Zeidler A, Jahn S, Salmon PS, Neuville DR, Fischer HE. 2012 Structural transformations on vitrification in the fragile glass-forming system CaAl₂O₄. *Phys. Rev. Lett.* **109**, 235501. (doi:10.1103/PhysRevLett.109.235501)
- 41. Skinner LB, Barnes AC, Salmon PS, Fischer HE, Drewitt JWE, Honkimäki V. 2012 Structure and triclustering in Ba-Al-O glass. *Phys. Rev. B* 85, 064201. (doi:10.1103/PhysRevB.85.064201)
- Drewitt JWE, Barnes AC, Jahn S, Kohn SC, Walter MJ, Novikov AN, Neuville DR, Fischer HE, Hennet L. 2017 Structure of liquid tricalcium aluminate. *Phys. Rev. B* 95, 064203. (doi:10.1103/PhysRevB.95.064203)
- Drewitt JWE, Jahn S, Hennet L. 2019 Configurational constraints on glass formation in the liquid calcium aluminate system. J. Stat. Mech: Theory Exp. 2019, 104012. (doi:10.1088/ 1742-5468/ab47fc)
- 44. Skinner LB *et al.* 2013 Joint diffraction and modeling approach to the structure of liquid alumina. *Phys. Rev. B* 87, 024201. (doi:10.1103/PhysRevB.87.024201)
- Henderson CMB, Cressey G, Redfern SAT. 1995 Geological applications of synchrotron radiation. *Radiat. Phys. Chem.* 45, 459–481. (doi:10.1016/0969-806X(95)92799-5)
- Drewitt JWE, Barnes AC. 2023 Data from Drewitt et al RSTA 2023. https://doi.org/10.5523/ bris.w9d5ypz91ltv2wksargnm510s.