

Elastocaloric effect: Impact of heat transfer on strain-induced crystallization kinetics of natural rubber

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1	Elastocaloric effect: Impact of heat transfer on strain-induced
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14	Abstract:
15	When natural rubber is rapidly loaded and unloaded there occurs a variation of its temperature
16	called the elastocaloric effect. The objective of this work was to determine whether this
17	temperature variation could be responsible for a delay in strain-induced crystallization (SIC)
18	kinetics and stress relaxation. To this end, the SIC kinetics of cross-linked natural rubber
19	samples with different thicknesses was studied at constant elongation after adiabatic stretching
20	using thermal, mechanical and in-situ WAXS characterizations. The coupling of these
21	techniques revealed that, at a fixed elongation λ (between 5 and 6), the crystallization kinetics
22	and stress relaxation were faster in the thinner sample (with a short heat exchange time
23	constant), thus providing evidence that heat transfer affected the SIC kinetics and should be
24	considered when interpreting experimental results.

<u>Keywords</u>: Natural rubber, Strain-induced crystallization, Crystallization kinetics, Latent heat,
 Infrared camera.

1. Introduction

The elastocaloric effect (eC) in elastomers can be used as an alternative cooling 32 technology that has the potential to be cheap, efficient and environmentally friendly.[1–3] This 33 effect is known as the change in temperature of a material when subjected to cyclic mechanical 34 solicitation. It has been observed in different elastomers such as Natural Rubber (NR)[4–7], 35 blends using recycled Natural Rubber[8], Polyurethanes [9,10], Silicone, Styrene-36 37 Butadiene[11] and poly(styrene-bethylene-co-butylene-b-styrene) (SEBS)[12]. In the following study, we focus on NR which has a large temperature variation up to $\Delta T=12^{\circ}C$ and good fatigue 38 resistance[3]. The origin of its eC effect is Strain-Induced Crystallization (SIC) and entropic 39 40 elasticity. [7,8,11] Since the SIC is not an instantaneous phenomenon [13–15], its kinetics will necessarily have an impact on the choice of the operating frequency of the elastocaloric device, 41 hence the need to study it. Among the first investigations carried out on the subject, one can 42 43 cite that of Mitchell and Meier [16] who showed, using thermal measurements, that the crystallization of NR started less than 50 ms after the adiabatic deformation. More recently, this 44 45 result was confirmed by Candau et al [17] and Albouy et al [18] based on *in-situ* WAXS 46 measurements. The same technique was employed by several authors to demonstrate that at constant elongation, the crystallization kinetics could last several tens of seconds, [13–15,19– 47 21] and this observation has been explained by mechanisms based on polymer chains diffusion, 48 49 crystal nucleation and stress relaxation [13–15].

These results suggest that in order to maximize the phase transition at the origin of the 50 51 elastocaloric effect, it would be preferable to perform long-period cycles (at least one hundred seconds). However, from an elastocaloric point of view, lowering the frequency would limit 52 53 the power involved, which is why it would seem relevant to increase the frequency as much as 54 possible. However, in this case, the material would partially crystallize and the heat that can be 55 exchanged during the cycle between the system and the surroundings would be limited. In 56 addition, the average temperature of the sample at high frequency can increase considerably 57 due to self-heating (because of the viscoelasticity of the material) [17] and might reach 50°C at 70Hz. According to the literature [7,10], with such an increase in temperature, the crystalline 58 fraction developed at a given elongation would decrease considerably $\left(\frac{d\chi_c}{d\tau} = -0.5\%/^\circ C\right)$ [19] 59 thus restraining the eC effect. 60

61 Crystallization kinetics is also temperature-dependent since it is controlled by the 62 nucleation rate [15,23,24] which in turn is affected by the energy barrier that must be crossed

to create nuclei. In fact, when NR is stretched adiabatically at high elongations, crystallization 63 is favored by the high elongations but the temperature rise induced by this phase transition (up 64 to 12°C at λ =6) [4,25] is likely to hinder the nucleation process as long as the generated heat 65 has not been totally evacuated to the external environment. For a sample with an initial 66 thickness equal to 1 mm that is stretched adiabatically at λ =6, the time required to reach thermal 67 equilibrium with the air is of the order of a few tens of seconds [26,27]. This also corresponds 68 to the duration of the fast relaxation induced by crystallization [28], and thus the following 69 70 question arises: to what extent does heat transfer have an impact on the strain-induced 71 crystallization kinetics?

In this work, the crystallization of an industrial crosslinked NR was characterized by in-72 73 situ Wide-angle X-ray Scattering (WAXS) and Infra-Red (IR) thermography at different elongations in order to study the correlation between the duration of the crystallization process 74 75 and the time needed to exchange the generated heat with the surroundings. We prepared crosslinked NR samples with different thicknesses (between 0.13 mm and 1.15 mm) but 76 77 identical intrinsic properties, so that only their form factor varied and thus also their heat exchange time constant τ (a parameter characterizing the heat exchange between the sample 78 and its surroundings [29]). In order to maximize the potential influence of the increase in 79 temperature during the test on the crystallization, samples were stretched under adiabatic 80 conditions. Finally, the impact of heat transfer on the crystallization kinetics was discussed. 81

82

2. Experimental setup

83

2.1 Materials and specimen geometry

Two types of unfilled crosslinked natural rubber samples were studied in this work. The 84 85 first one, denoted NR_{1.53}, was purchased from Xinyinte Rubber Products Co., Ltd., China and the second, named NR_{1.46}, was prepared in the laboratory using the recipe detailed in Table 1. 86 87 The densities of the elastically active chains (EAC) of these materials were estimated from the swelling ratio in toluene and from the Flory-Rehner equation [30] and were found to be 88 1.53×10^{-4} mol. cm⁻³ and 1.46×10^{-4} mol. cm⁻³, respectively. This EAC density was 89 high enough to avoid undesirable phenomena (inverse yield, stable crystals at room temperature 90 after retraction[31–33], ...) and close to the optimal EAC density that would allow a maximum 91 92 crystallization rate [34].

- Table 1: Chemical composition of the studied material in phr (parts per hundred, i.e., g per 100g
- 95 of rubber)

Components	NR _{1.46}
NR	100
6PPD*	3
SA**	2
ZnO	1.5
CBS***	1.9
Sulfur	1.2

96 *N-(1,3-dimethylbutyl)-N'-phenyl-p-phenylenediamine), **Stearic acid, *** N-cyclohexyl-2 97 benzothiazole sulfenamide.

Regarding the geometry of the samples, the original length was 40 mm with an initial distance
between the jaws of 20 mm, and a width of 20 mm. The thickness of NR_{1.53} was 0.63 mm, and
those of NR_{1.46} were 0.19 mm and 1.15 mm.

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2.2 Mechanical measurements

The tensile testing machine was similar to the one used by Yoshida et al. [35]. It is a single axis robot RSDG212 (MISUMI Corporation, Japan) with an analog force sensor XFTC300-200N (Measurement Specialties, France). The displacement was measured via a Laser optical displacement sensor ILD1420-200 (micro-epsilon, France). The signals recovered from both sensors were simultaneously recorded via an oscilloscope.

107 In order to avoid residual elongation due to Mullin's effect [36] and to ensure reproducibility of thermomechanical properties, the material was subjected to cyclic strain 108 (between $\lambda = 1$ and $\lambda = 6.8$) ten times. The initial length was then adjusted in order for the 109 sample to be taut. The samples were tested at least 5 minutes after this procedure, and the same 110 waiting time was applied between each test at room temperature (i.e. T=22°C). It was indeed 111 checked that 5 min was enough for the materials to show the same mechanical response as a 112 material having rested during 30 min (cf. supporting information Fig.S1; note that 5 minutes 113 would be likely insufficient in the case of a filled elastomer). The distance between the jaws 114 was taken as the initial length l_0 and the elongation was defined as $\lambda = \frac{l(t)}{l_0}$. 115

2.3 Thermal measurements

118 While stretching the material, an infrared camera, Optris PI450 (Optris, Germany) with 119 a 29° optic simultaneously recorded the temperature variation of its surface. The frequency 120 chosen to acquire the signal was f=80 Hz and the surface of measurement was about 15 121 mm². This surface was chosen to be in the center of the material in the stretched state to 122 minimize the effect of the edges (both mechanically and thermally). A second area was used to 123 measure the temperature in the center of the material at λ =1. (see Supporting Information 124 Fig.S.2)

During the test, there were three possibilities for the sample to evacuate thermal energy: 125 thermal radiation, heat conduction with a clamping system, and convection. The former was 126 127 neglected since the temperature variation between the sample and the environment remained small (up to 13K at most). The second was also neglected since the thermal conductivity of NR 128 is small (~0.146 W.m⁻¹.K⁻¹) [37], and also because the jaws were covered with strips of natural 129 rubber acting as thermal insulators. An emissivity of 0.95 was used during our experiments 130 [38], in accordance with a comparison between direct measurements using a thermocouple and 131 132 the information retrieved by the IR measurements. Convection was considered to be the most important mechanism of heat exchange. 133

134

2.4 In-situ WAXS measurements

The *in-situ* WAXS measurements were carried out on the D2AM beam-line of the European Synchrotron Radiation Facility (ESRF). The X-ray wavelength was 1.54 Å. The irradiation area was about $150*150 \ \mu m^2$. The acquisition times were fixed at 500 ms for the part of the study dedicated to the characterization of the crystallization right after deformation, and this time was then extended to 5 s to study the evolution of the crystallinity index during 200 s after adiabatic stretching. Each pattern was integrated as a function of the scattering angle (20), cleaned of air scattering, and then normalized by sample thickness and transmission.

In this study, the evolution of the crystallinity was followed via the intensity of the (200) plane's reflection after the deconvolution of the curve $I=f(2\theta)$ (denoted I_{200} and proportional to the crystallinity index as shown in Supporting Information, Fig.S3). This intensity will be called crystallinity index since it does not correspond to the real value of crystallinity.

147 **3. Results and discussion**

The impact of heat transfer on strain induced crystallization kinetics is expected to be 148 maximal when sample is stretched adiabatically. Therefore, to determine the adiabatic and 149 isothermal deformation domains, NR_{1.53} sample was deformed at different strain rates ranging 150 from 0.005 s⁻¹ to 16 s⁻¹ between λ =1 and λ =7. The maximum temperature variation measured 151 after discharge $1\Delta T_2$ are plotted in Fig. 1 as a function of the strain rate (d λ /dt). The results 152 suggest that at high rates of deformation $(d\lambda/dt > 8 \text{ s}^{-1})$ the temperature change is almost 153 constant ($\approx 13^{\circ}$ C) (adiabatic domain). Once this strain rate is lowered, the sample exchanges 154 heat with the external environment, therefore the values of $1\Delta T_2$ gradually decrease until 155 reaching 0°C at $d\lambda/dt = 0.005$ s⁻¹ indicating entry into the isothermal domain. 156



157

Fig. 1: Temperature variation measured after retraction (ΔT_2) at different strain rates between 0.005 s⁻¹ and 16 s⁻¹ for NR_{1.53}

160

161 The NR_{1.53} sample was stretched under adiabatic conditions at a strain rate of 16 s⁻¹, 162 from $\lambda = 1$ to $\lambda_{max} = \{4.5; 5; 5.5; 6; 6.5\}$ and then maintained at constant elongation for 200 s 163 before returning to $\lambda = 1$ as shown in Fig. 2-a. The step of the mechanical program which occurs 164 at constant elongation will be called holding step. The corresponding temperature change 165 profiles are given in Fig. 2-b and the stress-elongation curves are plotted in Supporting 166 Information, Fig.S4.



Fig. 2: a) Mechanical loading conditions: the NR_{1.53} sample with a thickness of 0.63 mm was stretched to different maximal elongations λ_{max} between 4.5 and 6.5 at $\lambda = 16 \, \text{s}^{-1}$; b) Corresponding temperature changes profiles ($\Delta T=T_{\text{measured}}-T_{\text{room}}$); c) Adiabatic temperature variations after loading (ΔT_1) and unloading ($|\Delta T_2|$) (blue and orange dots, respectively) as well as the entropic contribution $\Delta T_{\text{entropic}}$ (grey dashed line)

Firstly, while stretching the sample, a positive temperature variation ΔT_1 was measured. It resulted from the entropic elasticity and the strain-induced crystallization (SIC) [6,16]. A negative temperature variation ΔT_2 was observed when the sample was unloaded after heat exchange and its absolute value increased with the elongation. This cooling effect was due to the melting of crystallites and to entropic elasticity recovery [6].

The second observation was related to the kinetics of heat exchange. For each elongation, the area under the peak ΔT_2 presented in Fig. 2.b was much wider than the one under the peak ΔT_1 . Indeed, when the sample was stretched, its thickness decreased and its exchange surface became larger [26] wherefore the convective heat flow φ increased as well. The small thickness of the sample also helped reduce the thermal gradient within the thickness of the rubber films. The Biot number remained below 0.1 in all the experiments (Bi=hL/k, where h is surface heat exchange coefficient ~12W.m⁻².K⁻¹, L is the thickness of the samples which is inferior to 1.15 mm for each experiments, and k is the thermal conductivity of natural rubber ~0.15 W.m⁻¹K⁻¹). Therefore, the temperature of the NR film may be considered as uniform, and the heat flow φ across the external rubber surfaces may be linked directly to convection via the difference in temperature with the ambient temperature ΔT :

190
$$\varphi(t) = h \times S(\lambda) \times \Delta T(t) = \frac{\rho \times C_m \times V}{\tau(\lambda)} \times \Delta T(t)$$
(1)

Here, $S(\lambda)$ is the external surface of the sample, ρ the density, C_m the heat capacity, Vthe volume and τ (λ) = $\frac{\tau (\lambda = 1)}{\sqrt{\lambda}}$ the heat exchange time constant at a certain elongation λ [29]. In turn, τ ($\lambda = 1$) is the time needed for the sample to absorb 63% of the heat from the surroundings to reach the ambient temperature at $\lambda=1$. This value was directly determined from the second part of the temperature profile by analogy with the time constant of a first-order system, and was found to be (52±5) s for NR_{1.53} and (92±6) s for NR_{1.46}.

197 Fig. 2.c includes the total temperature changes measured after stretching ΔT_1 and 198 retraction $|\Delta T_2|$ as well as the contribution of entropic elasticity ΔT_{elast} which is assumed to be 199 proportional to the volumetric work given to the sample during adiabatic loading (W_{loading}), as 200 mentioned by Mitchell et al [16]:

201
$$\Delta T_{elast} = \frac{W_{loading}}{\rho \times C_m}$$
(2)

These three temperature variations increase from $\Delta T_1 = 1.3$ °C, $|\Delta T_2| = 2.2$ °C and $\Delta T_{elast} = 1.3$ °C 202 at λ =4 to $\Delta T_1 = 11.7^{\circ}$ C, $|\Delta T_2| = 13.3^{\circ}$ C and $\Delta T_{elast} = 3.8^{\circ}$ C at λ =6.5. This difference between 203 the temperature variation values after loading and unloading reflects the fact that during 204 retraction, the number of crystallites that melt is greater than that created just after stretching. 205 This result comes from the existence of kinetics of crystallization which is responsible for the 206 207 increase of the crystallinity index $\chi(t)$ during the holding step. The previous thermal measurements made it possible to describe the crystallinity index as a function of time using an 208 209 equation similar to the one proposed by Plagge. [39] The main difference is that we fix the term which multiplies $(T(t) - T_{room}(t)) * \sqrt{\lambda(t)}$ (equ3) and do not consider it as an adjustable 210 parameter. In the work of Plagge et al. the adjustment is done in order to assure that crystallinity 211 is null at $\lambda = 1$. 212

213
$$\chi(t) = \int_{t_0}^{t} \frac{C_m}{\tau(\lambda) * \Delta h_f} (T(t) - T_{room}(t)) dt + \frac{C_m}{\Delta h_f} (T(t) - T_{\lambda_f}) + \frac{C_m}{\Delta h_f} (\Delta T_{\lambda_f} - \frac{W_{loading}}{\rho \times C_m})$$
(3)

Here, t_0 is the moment when the maximal elongation λ_{max} is reached, $\rho = 910 \text{ kg/m}^3$ the density

[40], $C_m = 1900 \text{ J/(kg.K)}$ the heat capacity [16], $\tau(\lambda)$ the heat exchange time constant, T the measured temperature, T_{room} the room temperature, T_{λ_f} the temperature reached just after elongation and $\Delta h_f = 64 \text{ J/g}$ the melting enthalpy [4].

All the results obtained via equation (3) during the holding steps at different elongations are presented in Fig. 3.a. Firstly, for each test, the index of crystallinity increases with elongation and tends to stabilize to a maximum (χ_{max}) when the temperature no longer changes after a specific time that depends on the maximal elongation λ_{max} . The lowest χ_{max} (8% for λ_{max} =4.5) is reached after 100 s and the highest one (24% at $\lambda_{max} = 6.5$) after 70 s. These durations coincide with the time needed to evacuate all the heat generated after loading (5 τ : indicated in Fig. 3.a by black stars).

225 To verify that this slowdown of kinetics is not dependent on the employed method used, the evolution of the crystallization was characterized by WAXS using a synchrotron source. 226 227 The intensity I_{200} diffracted by the (200) plane was followed during the holding step at different 228 maximal elongations between 5 and 6.5. It was not possible to do the same for λ_{max} =4.5 because the low level of crystallinity reached, made detection too difficult with this technique. The time 229 at which the acquisition started was however increased at 1 s after the deformation (instead of 230 0.1 s for the thermal acquisition), because of the minimum acquisition time of the X-ray patterns 231 (around 500 ms). 232



233

Fig. 3: Evolution of (a) the crystallinity index determined using eq (3) and (b) the intensity of (200) planes diffraction measured via WAXS in NR_{1.53} during the holding steps at different elongations as a function of time after fast stretching at $\dot{\lambda} = 13 \ s^{-1}$ (5 τ corresponds to $\frac{5*\tau (\lambda=1)}{\sqrt{\lambda}}$)

As can be seen in Fig. 3.b, the intensity I_{200} evolves significantly during tens of seconds (black stars added on each curve of the same figure) and then slower after. This duration also corresponds to the time needed to evacuate the heat generated after adiabatic stretching (as presented on Fig 2.b). These results therefore suggest the existence of a link between the crystallization kinetics and the heat exchange which will be studied in more detail in the next experiment.

NR_{1.46} samples with two thicknesses (0.19 mm and 1.15 mm) were prepared in order to vary 244 the characteristic heat exchange time constant $\tau(\lambda)$. It decreases from (92±6) s to (20±3) s 245 when the thickness is reduced from 1.15 mm to 0.19 mm (Figure S.5). Subsequently, two main 246 physical quantities were used to study the evolution of crystallinity during the holding step: 247 248 stress and I₂₀₀ intensity. Fig.4 shows these quantities for NR_{1.46}, at constant elongation λ =6. It clearly evidences that stress relaxation occurs faster for the thin sample for times lower than 249 250 70s and with the same kinetics for times longer. Regarding the I₂₀₀ intensity, it increases faster 251 for the thin sample during the first 70s.



252

Fig. 4: a) Stress (σ) and b) Intensity I₂₀₀ of X-ray Diffraction during the holding step at λ =6 as a function of the time for two sample thicknesses: 0.19 mm and 1.15 mm of NR_{1.46} after fast stretching at $\dot{\lambda} = 13 \ s^{-1}$

It is difficult to compare stress and I_{200} intensity directly since the stress decreased whereas the intensity increased. Consequently, their variations were compared using two indices.

The first index was calculated via equation (4) and is presented in Fig. 5. It is based on the stress relaxation, and related to the SIC as shown by Flory [41]:

260

261
$$\frac{\Delta\sigma(t)}{\Delta\sigma_{max}} = \frac{\sigma(t) - \sigma_{min}}{\sigma_{max(1s \ after \ stretching)} - \sigma_{min}}$$
(4)

were σ_{max} is the maximum stress 1s after loading and σ_{min} is the stress reached at the end of the holding step.

From 1s to 70 s after deformation, a large difference is found between the stress curves (continuous lines) of thick (1.15 mm) and thin (0.19 mm) samples. This trend was also observed on the same specimen with other thicknesses (0.13 mm and 0.34 mm) and on another material

(NR_{1.53}) (see supporting information, Fig.S6). The results show that the thicker samples relax 267 more slowly, likely due to slower crystallization kinetics. The largest relative difference (40%) 268 is observed at about 8 s after deformation. Beyond 70 s, all curves merge indicating that both 269 270 samples have the same crystallization behaviors when the heat exchange ends. However, the stress does not appear to be stabilized at the end of the time interval studied, probably because 271 272 the crystallization continues to evolve very slowly over a longer duration than the one of our study or because of viscoelastic effects [9,17]. This points at the fact that stress relaxation is not 273 completely driven by the heat exchange, and that it may also be related to the relaxation of the 274 275 amorphous phase which decreases the local elongation and delays the SIC [15].

The relative evolution of the stress relaxation was then compared to that of the intensity of the peak 200 (square symbols) calculated via equation (5):

278
$$\frac{\Delta I_{200}(t)}{\Delta I_{200_{\text{max}}}} = \frac{I_{max} - I(t)}{I_{max} - I_{\min(1s \ after \ stretching)}}$$
(5)

The results of this comparison displayed in Fig. 5 show a good correlation between the evolution of the stress relaxation and the intensity for both thicknesses. The modelling of stress relaxation using a modified model of Flory supports also these results (Fig.S.7). Furthermore, they confirm that the crystallization kinetics is faster in the thinner sample. This suggests that the heat generated by SIC and entropic elasticity, could significantly delay the crystallization kinetics of the thicker sample.



Fig. 5: Stress relaxation (solid lines) and intensity variation (squares) during the holding step (after rapid stretching $\dot{\lambda} = 13 \ s^{-1}$) for the thicknesses 0.19 mm (blue) and 1.15 mm (yellow) at three final elongations: (a) $\lambda=5$, (b) $\lambda=5.5$ and (c) $\lambda=6$.

It is generally admitted that SIC is governed by the successive nucleation of crystallites 289 290 (characterized by their dimensions). Their appearance depends on the spatial heterogeneous 291 distribution of the topological constraints resulting from the successive appearance of the 292 crystals, and from the crosslinks initially existing in the material. [15,42]With the assumption of an initially homogeneous elastomer network, the first crystals to appear induced a decrease 293 of the elongation of the remaining amorphous phase and a release of latent heat; both 294 phenomena delaying the crystallization kinetics. The second assumption is supported by the 295 296 fact that, depending on the type of crosslinking, it has been shown that the network created in 297 natural rubber can be more or less heterogeneous [22,43,44]. With this in mind, Candau et al.[22] proposed a model that assumes the presence of several populations of crystallites, each 298 with a different crystallization temperature/elongation couple depending on the local elastically 299 active chain density. The discretization of the crystallites into different populations was based 300 on the evolution of size of the crystals with elongation. The crystals were supposed to reach 301 their final size instantaneously, and the size of the crystal was supposed to be linked to the local 302

303 EAC. Figure 6 recalls the $T_c(\lambda)$ curves of varying crystallite populations calculated by Candau for a material very similar to the one of the present study (crosslinked with sulfur and with a 304 similar elastically active chain density). On the same curve, we reported the maximum 305 temperature reached during adiabatic strain, for different values of λ_{max} , up to 6.5 (black dotes). 306 One can deduce from this figure that the appearance of the two first populations (green and blue 307 curves) is not inhibited by the generated heat, because their T_c is, for an elongation above 5, 308 higher than the temperature of the sample (black curve). Conversely, for crystallite populations 309 formed by longer chains (low local cross-link density, red curve), the temperature variation 310 311 reached just after elongation is greater than T_c, which means that the generated heat must first be partially removed for these populations to appear. The duration of the crystallization kinetics 312 is thus extended since the nucleation rate is slowed down due to the time required to decrease 313 314 the local temperature (i.e., to lower the energetic barrier of nucleation).



315

Fig. 6: Crystallization temperature as a function of elongation for different crystallite populations: 1st in green dashed lines, 2nd in blue dashed lines and the 3rd in red dashed lines. The curves were reproduced using equation 10 of the reference [22]. The points represent the maximum temperatures reached by our materials just after stretching at different λ .

320 **4.** Conclusion

The majority of the models that describe the crystallization kinetics of NR relate it entirely to the germination, stress relaxation and mobility of the macromolecular chains at a stabilized temperature and do not consider the temperature changes during the cycle. This study highlights the impact of the heat generated by entropic elasticity and crystallization on SIC kinetics and stress relaxation. A difference of at least 10% in the relaxed stress of samples of different thicknesses (200 µm and 1 mm) was observed. It is expected to increase as the difference in thickness of the samples increases. Consequently, the heat exchange time constant
is a parameter that should be considered while modeling SIC and the mechanical behavior of
NR. Furthermore, heat transfer could also be partly at the origin of the kinetics of melting of
NR crystallites mentioned in the work of Samaca Martinez et al.[27]. Further studies would be
needed to confirm it.

In view of being applied to elastocaloric devices[45], these results confirm that a non-332 negligible crystallization occurs during a few tens of seconds during the heat transfer. In 333 addition, the interplay between stress, temperature and the kinetics of the strain-induced 334 crystallization is believed to have a great impact on the mechanical losses of natural rubber and 335 thus on its coefficient of performance (COP), especially in the case of non-uniform temperature 336 337 as for regenerative elastocaloric devices (typically when using a liquid as a heat transfer fluid leading to a Biot number above 1). Further work is however necessary to evaluate the impact 338 339 of non-homogenous crystallization and temperature on the mechanical behavior. It also leads to questions about the impact of the conductive heat diffusion on the crystallization at 340 microscopic and low time scales [46], since the local temperature variation induced by 341 crystallization can reach $\Delta T = \frac{\Delta H_f}{C_m} = 38^{\circ}C[47].$ 342

Finally, from a more general point of view, the high toughness of natural rubber and its dynamic mechanical response are strongly dependent on its ability to crystallize. Consequently, the increase in heat transfer could accelerate the kinetics of SIC and have a significant influence on its fatigue resistance in a marine environment (with a high convective heat transfer coefficient)[48–50]. The dependence of the SIC kinetics on temperature and heat transfer could also be taken into account when investigating crystallization at the crack tip where heat exchange is very specific.

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