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# Numerical investigation of salt-frost damage of pervious concrete at the scale of a few aggregates

<sup>3</sup> Iliass Tahiri<sup>*a*</sup>, Patrick Dangla<sup>*a*,\*</sup>, Matthieu Vandamme<sup>*a*</sup> and Quoc Huy Vu<sup>*b*</sup>

<sup>4</sup> <sup>a</sup>Navier, Ecole des Ponts, Univ Gustave Eiffel, CNRS, Marne-la-Vallée, France

<sup>b</sup>Holcim Innovation Center, 95 rue du Montmurier, F-38070 Saint Quentin Fallavier, France

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#### ABSTRACT

Keywords:	In this study, we aim to gair
Frost attacks	to frost attacks in the preser
Frost damage	model on system geometries
Freeze-thaw cycles	gates: 1) one aggregate coate
Pervious concrete	of cement paste, and 3) two
Numerical modeling	simulations indicate that the
	Furthermore, we observe sig
	We undertake a thorough pa
	tions, initial conditions, and
	freeze-thaw cycles. The inst
	hanced freeze-thaw durabilit

a this study, we aim to gain insight into the damage mechanisms of pervious concrete subject of fost attacks in the presence of salt. We perform numerical simulations using a poroelastic odel on system geometries representing pervious concrete at the scale of one or a few aggreates: 1) one aggregate coated with cement paste, 2) one aggregated coated with a cracked layer of cement paste, and 3) two aggregates coated and bonded with cement paste. The numerical mulations indicate that the damage is more likely to occur at the contact between aggregates. Therefore, we observe significant shear stress at the vicinity of the paste/aggregate interface. We undertake a thorough parametric study to evaluate the impact of various boundary condions, initial conditions, and materials parameters on the stresses generated during one or several eeze-thaw cycles. The insights can provide guidelines to design pervious concretes with enanced freeze-thaw durability.

# 22 1. Introduction

Pervious concrete is a cement-based material with a high volume of inter-granular pores: its intergranular porosity 23 varies between 11 % to 35 % [1] and its permeability varies between 0.1 and 2 cm/s [2]. Pervious concrete is made 24 25 of single-sized aggregates coated and bonded by a small layer of cement paste. The thickness of the paste coating the aggregates depends on various parameters such as paste rheology, aggregate size, and volume of paste [3]. Xie 26 et al. [3] report thickness of cement paste between 0.2 and 0.6 mm. Pervious concrete has substantial benefits, for 27 instance, allowing water to drain easily from the surface to the soil to avoid floods. Still, it is subject to durability 28 challenges such as low resistance to freeze-thaw cycles and clogging. In fact, in cold regions, freeze-thaw cycles 29 30 damage rapidly pervious concrete structures. Studies have shown that in saturated conditions and the presence of deicing salts, pervious concrete undergoes only a few cycles of freeze-thaw before partial or total damage [4]. The 31 durability of different pervious concrete pavements in service in a wet, hard-freeze region is investigated in [5] using 32 microscopic observations. The authors suspect that freeze-thaw attacks cause the observed damage. This damage 33 manifests as cracks in the aggregates, cement paste, and interfacial transition zone (ITZ). This limit to the use of 34 pervious concrete in cold climate regions pushed various researchers to tackle the problem of freeze-thaw durability 35 of pervious concrete [6–9]. 36

Freeze-thaw observed in cementitious materials has been studied for several decades by both experimental and theoretical approaches. There are two prominent families of damage mechanisms for cementitious materials subjected to frost attacks: internal damage and salt scaling [10].

On the one hand, internal damage occurs in the concrete bulk, when ice forms first in capillary pores. Ice formation 40 induces a volume increase of 9% compared to liquid water. Therefore, water pressurization occurs in the smaller (and 41 still unfrozen) pores due to additional volume induced by ice formation in the largest pores. According to the hydraulic 42 pressure theory, the pressure that drives the flux away from freezing regions (pressurized zones) is the cause of damage 43 from internal frost. Mechanically, if the tensile strength of the paste is inferior to the hydraulic pressure, damage 44 occurs. This theory explains the role of air voids in reducing the hydraulic pressure as unfrozen water can flow toward 45 the air voids. However, it does not take into account the presence of salt. To tackle this, Powers [11] proposed the 46 osmotic pressure theory. The theory postulates that when the ice starts to form in a porous medium saturated with a 47 saline solution, the salt concentration of the remaining solution increases. The difference in salt concentration between 48

\*Corresponding author patrick.dangla@univ-eiffel.fr (P. Dangla) ORCID(s): the zone of high concentration and other surrounding saturated zones with lower concentrations will result in water diffusion from low to high concentration zones. Therefore, the fluid pressure will rise in the zone of high concentration and induce tensile stress in the cement matrix. Valenza and Scherer [12] reported that this induced stress surpasses concrete tensile strength only if the difference in salt concentration reaches approximately 14 %. Therefore, the authors concluded that the osmotic pressure would never reach damaging levels for concrete since the fluid flow will rapidly dissipate the rising pressure.

On the other hand, salt scaling consists of the debonding of small flakes at the surface of cementitious materials 55 upon freezing a saline solution on the surface. The maximum damage occurs with a concentration of solute of about 56 3 wt% [13, 14]. The existence of this pessimum has been proved experimentally by various studies. According to the 57 glue-spall theory [12], as the freezing occurs, ice and concrete contract at different rates (as the coefficient of thermal 58 expansion of ice is five times larger than that of concrete). The ice cracks around brine pockets to form ice islands. 59 When the salt concentration of the solution is low, the formed ice is strong enough not to crack, whereas, when its 60 salt concentration is high, the formed ice is too weak to propagate cracking into the concrete. Other mechanisms are 61 proposed to explain salt scaling, such as damage caused by the pressure of brine forced from the outer ice layer into 62 the concrete Yener [15]. 63

Various studies use the poroelastic approach to model frost attack of cement-based materials [16–18]. According 64 to Coussy [19], the following mechanisms can explain the deformation of a material under freezing: 1) density change 65 when ice forms, which results in a rise of pore pressure, 2) pressure associated with interfacial energy between the 66 various constituents, 3) pressure associated to the transfer of water due to ice crystallization, 4) the cryosuction process, and finally, 5) the thermomechanical coupling between the various constituents (solid matrix and the pressurized pores). 68 Various conditions such as full or partial saturation, air voids, and salt can impact the freezing behavior. Eriksson et al. 60 [20] developed a model of freezing behavior of partially saturated air-entrained concrete. However, this model does 70 not take into account the presence of salt in the solution. To overcome this limitation, they developed another model, 71 which considers the presence of salt in the solution, as well as the freeze-thaw hysteresis in a partially saturated air-72 entrained concrete [21]. In the work of Rhardane et al. [22], the developed model considers the presence of salt, the 73 saturation degree, and the osmotic pressure to assess the freeze-thaw damage mechanisms of cementitious materials 74 at the cement paste microscale. Finally, at the scale of aggregates coated with cement paste, Rahman and Grasley [18] 75 developed a model to investigate the impact of freeze-thaw cycles in saturated conditions on one aggregate coated with 76 cement paste. 77

In this study, we investigate the behavior of pervious concrete under freeze-thaw solicitations, which is a topic 78 of societal interest, as those materials, which make it possible to alleviate soil impermeabilization, are sensitive to 79 freeze-thaw damage. Our goal is to simulate the impact of freeze-thaw cycles on an individual aggregate coated 80 with cement paste and two aggregates coated and bonded with cement paste. We work on these systems to provide 81 information on the mechanisms of freeze-thaw damage at the local scale of the cement coating, the aggregates, and 82 the paste/aggregate interface. Moreover, since the permeability of pervious concrete is high (because the macrovoids 83 pore structure is interconnected), it is likely that no hydraulic pressure develops in the macrovoids during freezing, 84 which is an additional reason to focus on the scale of a few aggregates. We utilize numerical simulations based on a 85 poromechanical model, which considers relevant processes for freezing porous solids. These processes are hydraulic 86 pressure, cryosuction, salt diffusion, and brine pockets at the material's surface. The combined equations describing 87 the complex phenomena in a porous material are solved using the finite element method in three dimensions at the scale 88 of two aggregates coated and bonded with cement paste. To the best of our knowledge, our work is the first application 89 of poromechanical freeze-thaw modeling to pervious concrete at the relevant scale of a few aggregates coated with 90 cement paste.

In the following section, we derive the poromechanical model necessary to simulate freeze-thaw in porous materi-92 als. We present the details of the simulations and the adopted geometry in Sections 2.2 and 2.3, respectively. Section 93 2.4 details the initial conditions, boundary conditions, and the properties used for the simulations. Regarding, bound-94 ary conditions, we propose a method for modeling brine pockets with different levels of connectivity. Section 3.1 95 presents the results obtained on an individual aggregate coated with cement paste and discusses the impact of various 96 parameters (i.e., the effect of salt, the effect of time and the number of freeze-thaw cycles, the effect of boundary con-97 ditions, the effect of materials properties, and the influence of a crack in the cement paste). Section 3.2 presents the 98 results of simulations on the system of two aggregates coated and bonded with cement paste. We discuss the zones 99 where damage is most likely to occur in Section 3.3, before concluding. To do so, we concatenate the poromechanical 100 model for freeze-thaw with adequate failure criteria for bulk phases (i.e., cement paste and aggregates) and for the 101

<sup>102</sup> paste/aggregate interface.

## 103 2. Model

This section describes the main equations of the model used to simulate freeze-thaw cycles of aggregates surrounded with cement paste and immersed in a salt solution. The section also provides the necessary inputs to conduct the simulations of frost attacks. Later in the manuscript, we discuss the effect of the number of freeze-thaw cycles (see Section 3.1.2), the impact of initial conditions (see Section 3.1.3), and the impact of boundary conditions (see Section 3.1.4) on the system response to freeze-thaw.

#### **109 2.1.** Poroelastic model

We can use the poromechanical approach to describe the phenomena that occur in cement-based materials. This approach gives access to saturation and stresses during the process of freezing in concrete, for instance. Two phases coexist when freezing saturated porous solids: liquid water (which contains dissolved salt) and ice crystals. We define  $\phi_J$  as the Lagrangian porosity. The fact that this porosity is Lagrangian means that, by definition,  $\phi_J = V_J/V_0$ , where  $V_J$  is the actual volume occupied by phase J and  $V_0$  is the volume of the porous solid in the reference state. The partial Lagrangian porosity  $\phi_J$  can be expressed as [23]:

$$\phi_J = \phi_0 S_J + \varphi_J \tag{1}$$

where  $\phi_0$  is the initial porosity,  $S_J$  is the Lagrangian saturation of the phase J. Eq. 1 states that this volume can vary because of two reasons: 1) because  $S_J$  varies, or because  $\varphi_J$  varies. Those two terms represent two different physical processes. The term  $\phi_0 S_J$  takes into account variations of porosity occupied by phase J due to displacement of the meniscus separating phase J from the other phases. The term  $\varphi_J$  takes into account variations of porosity occupied by phase J due to deformation of the pore volume currently occupied by the phase J.

During the freezing of saturated cement-based material, the saturation of each phase is the fraction of pore volume occupied by the various phases. In this work, we consider that the material is saturated with water initially. At any time during the freezing process, the total Lagrangian porosity  $\phi$  is the sum of the partial Lagrangian porosities  $\phi_L$ and  $\phi_C$ . In addition the liquid and ice the saturations verify the following equation:

$$S_L + S_C = 1 \tag{2}$$

In the followings we will neglect the deformation of pores,  $\varphi_I$ , in the conservation of mass for water and salt.

In any representative elementary volume, the total mass change is due to liquid solution transport between pores. The total mass is the mass of water and salt in liquid and solid states. We express the conservation of total mass by [24]:

$$\frac{\partial m_{total}}{\partial t} = -\nabla \cdot \mathbf{w}_{\mathbf{L}} \tag{3}$$

where  $m_{total}$  is the total mass content and  $\mathbf{w}_{\mathbf{L}}$  is the total mass flow vector.

The total mass content  $m_{total}$  is given by:

$$m_{total} = (\rho_L S_L + \rho_C S_C)\phi_0 \tag{4}$$

where  $\rho_L$  and  $\rho_C$  are the liquid water and ice density, respectively.

We express the conservation of salt mass by [24]:

$$\frac{\partial m_{salt}}{\partial t} = -\nabla \cdot \mathbf{w}_{salt} \tag{5}$$

where  $m_{salt}$  is the mass of salt and  $w_{salt}$  is the mass flow vector of salt.

The mass of salt  $m_{salt}$  is given by:

$$m_{salt} = \rho_{salt} S_L \phi_0 \tag{6}$$

where  $\rho_{salt}$  is the mass salt concentration in the pore solution.

The liquid transport through the porous medium due to a pressure gradient can be modeled with Darcy's law [25]:

$$\mathbf{w}_{\mathbf{L}} = -\rho_L k_{rl} \frac{k_{int}}{\mu_L} \nabla p_L \tag{7}$$

where  $k_{rl} = k_{rl}(S_L)$  is the relative permeability,  $k_{int}$  is the intrinsic permeability,  $\mu_L = \mu_L(T)$  is the viscosity of the liquid phase, here considered to depend on temperature T only and  $p_L$  the liquid pore pressure.

The mass flow vector  $\mathbf{w}_{salt}$  of salt is:

$$\mathbf{w}_{\text{salt}} = M_{salt} \frac{c_s}{\rho_L} \mathbf{w}_L + \mathbf{j}_{\text{salt}}$$
(8)

where  $M_{salt}$  is the molar mass of salt,  $\rho_{salt} = M_{salt}c_s$  is the mass salt concentration in the pore solution,  $c_s$  is the molar salt concentration, and **j**<sub>salt</sub> is the diffusive salt flux.

The salt transport through the porous media can be modeled with Fick's law [25]:

$$\mathbf{j}_{\text{salt}} = -M_{salt}\phi S_L \tau D_{salt} \nabla (c_s) \tag{9}$$

where  $\tau = \tau(\phi_0, S_I)$  is the tortuosity coefficient,  $D_{salt}$  is the molecular diffusion coefficient of salt in water.

The density  $\rho_J$ , of the phase J depends on the pressure  $p_J$ , temperature T, and salt concentration  $\rho_{salt}$ . They are given by [17]:

$$\rho_C = \rho_C^0 \left[ 1 - \alpha_C (T - T_m) + \frac{p_C - p_m}{K_C} \right]$$
(10)

$$\rho_L = \rho_L^0 \left[ 1 - \alpha_L (T - T_m) + \frac{p_L - p_m}{K_L} - \rho_{salt} \tilde{V}_{salt} \right]$$
(11)

where  $\rho_J^0$  is the density of phase J in the reference state (namely at atmospheric pressure  $p_m = 101.325$  kPa and at melting temperature  $T_m = 0$  °C),  $\alpha_J$  its coefficient of thermal expansion,  $K_J$  its bulk modulus, and  $\tilde{V}_{salt}$  is the relative partial specific volume of salt (in m<sup>3</sup>.kg<sup>-1</sup>). We summarize the value of liquid and ice crystals parameters in Table 1. The relative partial specific volume  $\tilde{V}_{salt}$  of salt is calculated using the following equation:

$$\tilde{V}_{salt} = \frac{V_{\text{NaCl}}}{M_{\text{NaCl}}} - \frac{V_{\text{H}_2\text{O}}}{M_{\text{H}_2\text{O}}}$$
(12)

where  $V_{\text{NaCl}}$  and  $V_{\text{H}_2\text{O}}$  are the partial molar volumes of salt and liquid water, respectively, and where  $M_{\text{NaCl}}$  and  $M_{\text{H}_2\text{O}}$ are their molar mass, respectively.

The conservation of heat in a porous material under freezing can be modeled by the following equation reported in Zeng et al. [16]:

$$\frac{\partial s}{\partial t} = -\nabla \cdot s_L \mathbf{w}_L - \frac{1}{T} \nabla \cdot \mathbf{q}$$
(13)

where  $s = s_{sol} + (\rho_L s_L S_L + \rho_C s_C S_C) \phi_0$  is the total entropy, and  $s_{sol}$  is the entropy of the solid skeleton.

Parameter	Value	Unit	Significance	Source
KL	1.8	GPa	Bulk modulus of liquid water	[17]
$\overline{K_C}$	7.8	GPa	Bulk modulus of ice crystals	[17]
$C_L$	4180	$J.kg^{-1}.K^{-1}$	Heat capacity of liquid water	[26]
$C_{C}$	2000	$J.kg^{-1}.K^{-1}$	Heat capacity of ice crystals	[26]
$\lambda_L$	0.6	$W.m^{-1}.K^{-1}$	Thermal conductivity of liquid water	[26]
$\lambda_C$	2.2	$W.m^{-1}.K^{-1}$	Thermal conductivity of ice crystals	[26]
$\alpha_L(T)$	$68.7 \cdot 10^{-6} + 13.877 \cdot 10^{-6} (T - T_m)$	$K^{-1}$	Coefficient of thermal expansion of liquid water	[27]
$\alpha_{C}$	$155 \cdot 10^{-6}$	$K^{-1}$	Coefficient of thermal expansion of ice crystals	[17]
V <sub>NaCl</sub>	$16.6 \cdot 10^{-6}$	m <sup>3</sup> .mol <sup>-1</sup>	Partial molar volume of salt	[28]
$V_{\rm H_2O}$	$18.0 \cdot 10^{-6}$	m <sup>3</sup> .mol <sup>-1</sup>	Partial molar volume of liquid water	[29]
$\tilde{M_{\rm H_2O}}$	$18.0 \cdot 10^{-3}$	$kg^{-1}.mol^{-1}$	Molar mass of water	
M <sub>NaCl</sub>	$58.4 \cdot 10^{-3}$	$kg^{-1}.mol^{-1}$	Molar mass of salt	
$\rho_I^0$	1000.0	kg.m <sup>-3</sup>	density of liquid in the reference state	
$\rho_C^{\tilde{0}}$	917.0	kg.m <sup>-3</sup>	density of ice in the reference state	
S <sub>m</sub>	23.54	$J.mol^{-1}.K^{-1}$	Entropy of fusion of ice	

#### Table 1

Liquid water and ice crystals inputs for the simulations.

The specific entropy  $s_J$  of each phase depends on its pressure  $p_J$ , its heat capacity  $C_J$ , its thermal expansion coefficient  $\alpha_J$ , and the temperature T [17] [30]:

$$s_{L} = s_{L}^{0} + C_{L} \ln \frac{T}{T_{m}} - \frac{\alpha_{L}}{\rho_{L}^{0}} (p_{L} - p_{m})$$
(14)

$$s_C = s_C^0 + C_C \ln \frac{T}{T_m} - \frac{\alpha_C}{\rho_C^0} (p_C - p_m) - s_m / M_{\rm H_2O}$$
(15)

where the reference specific entropy  $s_J^0$  is defined as the specific entropy of phase J at temperature  $T_m$  and pressure  $p_m$ . The entropy  $s_{sol}$  of the solid skeleton is given by:

$$s_{sol} = C_s \ln \frac{T}{T_m} \tag{16}$$

where  $C_s$  is the specific heat capacity of the solid skeleton.

Fourier's law governs heat conduction. This law relates the rate of heat transfer to the gradient of temperature in the material [24]:

$$\mathbf{q} = -\lambda \nabla T \tag{17}$$

where **q** is the heat flow vector,  $\lambda = \lambda(\lambda_{sol}, \lambda_L, \lambda_C, S_L, \phi_0)$  is the thermal conductivity of the porous material, which takes into account the thermal conductivity of the various phases:  $\lambda_{sol}$  for the solid phase,  $\lambda_C$  for the ice crystals, and  $\lambda_L$  for the liquid water.

Hashin and Shtrikman [31] proposed a model to estimate the thermal conductivity of isotropic composite materials:

$$\lambda = \lambda_s + \frac{\phi_0}{\frac{1 - \phi_0}{3\lambda_s} + \frac{1}{S_L \lambda_L + (1 - S_L) \lambda_C - \lambda_s}}$$
(18)

<sup>165</sup> The equation of mechanical equilibrium in absence of body forces is [24]:

$$\boldsymbol{\nabla} \cdot \boldsymbol{\sigma} = \boldsymbol{0} \tag{19}$$

The constitutive equations for a linear isotropic thermoporoelastic material with a porosity filled by liquid and ice phases can be expressed as [24]:

$$\boldsymbol{\sigma} = \left(K - \frac{2}{3}G\right)\boldsymbol{\epsilon}\mathbf{I} + 2G\boldsymbol{\epsilon} - \left[b_C p_C + b_L p_L + 3\alpha K \left(T - T_m\right)\right]\mathbf{I}$$
(20)

where **I** is the second-order identity tensor,  $b_L$  and  $b_C$  denote the liquid and ice Biot coefficients, respectively,  $\epsilon$  is the strain tensor,  $\epsilon = tr(\epsilon)$  is the volume strain,  $\sigma$  is the stress tensor,  $\alpha$  is the coefficient of thermal expansion of the dry porous solid, *K* is the drained bulk modulus of the porous solid.

The linearized strain tensor  $\epsilon$  is defined by:

$$\boldsymbol{\epsilon} = \frac{1}{2} \left( \nabla \mathbf{u} + \nabla^{\mathsf{T}} \mathbf{u} \right) \tag{21}$$

where **u** is the displacement vector.

The local thermodynamic equilibrium of liquid water and ice (i.e., the equality of their chemical potentials) yields the Thomson equation:

$$p_{C} = p_{m} + \frac{1}{V_{C}} \left[ V_{\text{H}_{2}\text{O}}(p_{L} - p_{m}) - s_{m}(T - T_{m}) + R_{g}T \ln(a_{w}(c_{s}, T)) \right]$$
(22)

where  $p_C$  is the ice pressure,  $V_C$  is the ice molar volume,  $R_g$  is the ideal gas constant,  $s_m$  is the entropy of fusion of ice,  $c_s$  is the salt concentration, and  $a_w(c_s, T)$  is the water activity. The water activity is calculated as function of temperature and salt concentration using the model developed by Lin and Lee [32, 33].

To link the macroscopic poroelastic properties to the elastic properties of the skeleton and saturation, we use the following equations [23]:

$$b = b_L + b_C \tag{23}$$

$$b_J = bS_J \tag{24}$$

During freezing, there exists a threshold size such that all pores with an entry radius smaller than this threshold 180 are filled with liquid phase and all pores with an entry radius larger than this threshold are filled with ice. During 181 thaving, this threshold size is such that all pores with a size smaller than this threshold are filled with liquid phase and 182 all pores with a size larger than this threshold are filled with ice. For poromechanical calculations, rather than in how 183 this threshold size varies during the solicitation (see Figure 1 for a few cases), we are interested in how the saturation 184  $S_L$  varies during the solicitation. How this liquid saturation evolves is related to the capillary pressure through the Van 185 Genuchten relation. The Van Genuchten model provides a retention curve that relates the liquid saturation  $S_L$  with the 186 capillary pressure  $(p_C - p_L)$  [34]: 187

$$S_L = \left[1 + \left(\frac{p_C - p_L}{n}\right)^{\frac{1}{1-m}}\right]^{-m}$$
(25)

where *n* and *m* are constants related to the pore structure of the porous solid.

<sup>189</sup> Upon freezing, blockage of the pore by ice reduces the permeability of the material. We relate the permeability to <sup>190</sup> the retention curve with the Mualem model [35]:



**Figure 1:** Threshold size of interest during freeze-thaw problems. All pores with an entry radius (respectively a radius) smaller than this threshold remain full of liquid phase during freezing (respectively thawing). All other pores are filled with ice.

$$k_{rl} = \sqrt{S_L} \left( 1 - \left( 1 - S_L^{1/m} \right)^m \right)^2$$
(26)

The combination of the previous equations is solved using the 3D finite element method (FEM) in the numerical solver BIL [36]. We generate the geometry and mesh with the meshing software GMSH [37]. We summarize the primary and the secondary variables in Table 2. The equations solved are Eqs. 3 to 11, 13 to 17, 19 to 22, and 25. One can check that there are as many scalar unknowns (i.e., 39) as scalar equations.

## **195** 2.2. Simulations rationale

The goal of the model is to numerically simulate the effect of freeze-thaw cycles on pervious concrete at the scale of one or a few aggregates covered by cement paste. Studying a unique aggregate coated with cement paste allows us to quantify the interactions between aggregate and cement paste in pervious concrete. In particular, we also aim to study the impact of a crack in the cement layer. Studying a system of two aggregates coated and bonded with cement paste allows us to quantify what happens at the junction between two aggregates.

The simulations are performed for various boundary and initial conditions to gain insights on the extent of the influence of these entry conditions, which are difficult to quantify experimentally. We also investigate the influence of cement paste and aggregate properties on the response to freeze-thaw cycles.

## 204 2.3. Geometry

For our numerical simulations, we consider three model systems: 1) a spherical aggregate of diameter 8 mm coated with a cement paste of thickness 300 μm, 2) a spherical aggregate of diameter 8 mm coated with a cement paste of thickness 300 μm in the presence of a crack, 3) two spherical aggregates of diameter 8 mm coated and bonded with a cement paste of thickness 300 μm.

Figure 2 presents the geometries and the mesh considered for this study. Due to the symmetry of the problems, we model the individual aggregate coated with intact cement paste as a one-dimensional system. For the aggregate coated with a cracked layer of cement paste, we model only half a sphere and perform two-dimensional axisymmetric

Modeling	salt-frost	damage	of	pervious	concrete
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State variable	Significance	Number of scalar unknowns	Type of variable
Т	Temperature	1	Primary
C <sub>s</sub>	Salt concentration	1	Primary
$p_L$	Liquid pressure	1	Primary
u	Displacement vector	3	Primary
m	Total mass of solution per unit volume	1	Secondary
w <sub>L</sub>	Mass flow vector of solution	3	Secondary
m <sub>salt</sub>	Mass of salt per unit volume	1	Secondary
w <sub>salt</sub>	Mass flow vector of salt	3	Secondary
<b>j</b> <sub>salt</sub>	Diffusive salt flux vector	3	Secondary
$s_L$	Entropy of liquid	1	Secondary
$s_{C}$	Entropy of ice	1	Secondary
s <sub>sol</sub>	Entropy of solid	1	Secondary
q	Heat flow vector	3	Secondary
σ	Stress tensor	6	Secondary
$p_C$	Pressure in ice	1	Secondary
$S_L$	Lagrangian saturation in liquid water	1	Secondary
$ ho_L$	Density of solution	1	Secondary
$\rho_C$	Density of ice crystal	1	Secondary
$\epsilon$	Strain tensor	6	Secondary

#### Table 2

Primary and secondary variables of the model.

simulations (see Figure 2-a). For the two bonded aggregates, we model a quarter of the geometry, again performingtwo-dimensional axisymmetric simulations (see Figure 2-b).

We use a Cartesian system of coordinates. Axes Ox and Oy are in the simulated plane, with Oy aligned with the axis of symmetry. The origin of the coordinate system is at the center of the aggregate. We will refer to the x-direction and the y-direction as horizontal and vertical directions, respectively.



**Figure 2:** Modeled systems: (a) spherical aggregate coated with a cracked layer of cement paste, (b) two spherical aggregates coated and bonded with cement paste. The plane y = 0.0041 m is a plane of symmetry for this latter system.



Figure 3: Temperature cycle and resulting salt concentration imposed at the boundary in the case of interconnected brine pockets.

# 217 2.4. Initial and boundary conditions

#### 218 2.4.1. Initial conditions

We consider that both the aggregate and the cement paste are initially saturated with pure liquid water at a pressure  $p_L$  equal to the atmospheric pressure  $p_{atm}$ , i.e.:

$$p_L(t=0) = p_{atm} \tag{27}$$

In Section 3.1.3, we will discuss the impact of this initial condition by considering that the samples are initially filled with a salt solution as if the salt present in the solution around the samples had time to diffuse throughout the medium before the start of the freeze-thaw cycles. In terms of temperature, for all systems, we consider that the initial temperature is homogeneous and equal to 10 °C.

## 223 2.4.2. Mechanical boundary conditions

For all systems, on the axis of symmetry x = 0, we prevent any horizontal displacement. The outer surface of the cement paste is free of stress. For the systems with one aggregate, we prevent vertical displacement of the bottom extremity of the system. For the system with two aggregates bonded by the cement paste, the top horizontal surface is a plane of symmetry. On this plane of symmetry, we impose no vertical displacement and no friction in the horizontal direction. Furthermore, the bottom extremity of the sphere is free.

## 229 2.4.3. Thermal boundary conditions

Starting from +10 °C, each freeze-thaw cycle, lasting 24 hours, consists in: 1) decreasing the temperature at a rate of -5 °C/h for 6 hours, down to a minimum temperature of -20 °C; 2) maintaining the sample at -20 °C for 4 hours; 3) increasing the temperature at a rate of +7.5 °C/h for 4 hours, back up to +10 °C; 4) maintaining the sample at +10 °C for 10 hours. We impose the temperature cycle on the outer boundary of the systems. The thermal cycle considered is displayed in Figure 3.

## 235 2.4.4. Hydraulic boundary conditions

<sup>236</sup> We consider a null flux condition in the horizontal direction on the axis of symmetry of all systems.

When the temperature at boundaries is positive, the outer surface of the specimens is in contact with the salt solution at pressure  $p_L = p_{atm}$  and concentration  $c_s = 520$  mol/L corresponding to  $\approx 3\%$  of the weight of water.

Parameter	Symbol	Unit	Value for cement paste	Source	Value for aggregate	Source
Porosity	$\phi_0$	-	0.3	[50]	0.04	[24]
Intrinsic permeability	$k_{int}$	m <sup>2</sup>	$1.10^{-21}$	[42]	$1 \cdot 10^{-20}$	[47]
Young modulus	E	GPa	25	[38]	60	[44]
Poisson coefficient	ν	-	0.22	[50]	0.3	[45]
Biot coefficient	b	-	0.55	[50]	0.6	[24]
Thermal expansion of solid matrix	$\alpha_s$	$10^{-6} \text{ K}^{-1}$	17	[39]	2.2	49
Thermal conductivity of solid matrix	$\lambda_s$	$W.m^{-1}.K^{-1}$	0.53	[43]	2.8	48
Volumetric heat capacity of solid	$C_s$	$J.m^{-3}.K^{-1}$	$1.47 \cdot 10^{6}$	[51]	$1.9 \cdot 10^{6}$	45
Van Genuchten parameter	т	-	0.42	[16]	0.42	16
Van Genuchten parameter	n	MPa	16.28	[52]	16.28	52
Friction angle	$\theta$	۰	35	[53]	35	[44]

#### Table 3

Materials inputs for the simulations.

When freezing occurs, a mixture of ice and brine pockets surrounds the sample. At all instants, we consider that liquid water and ice outside the cement paste are in thermodynamic equilibrium (i.e., their chemical potentials are equal). Therefore, the Thomson equation (22) remains valid to relate the pressure of the solution in the pockets with the ice pressure. We consider interconnected brine pockets: the liquid pressure in these brine pockets and the ice pressure remain equal to the atmospheric pressure. Consequently, the Thomson equation (22) reduces to:

$$(T - T_m)S_m - R_g T \ln(a_w(c_s, T)) = 0$$
(28)

which imposes a relationship between the temperature T and the concentration  $c_s(T)$  on the system's boundaries. This relationship is displayed in Figure 3.

We observe in Figure 3 that the hypothesis that both ice and the brine pockets remain at atmospheric pressure implies that, upon freezing, the lower the temperature, the higher the concentration of salt in the brine pockets (i.e., on the boundaries of the system). This hypothesis also entails that no ice forms in the pores in the vicinity of the samples' surface because of the rise in salt concentration which lowers the melting temperature of the brine pocket.

In Section 3.1.4, we will assess the impact of this boundary condition by considering that the brine pockets are disconnected and that their pressure may differ from the atmospheric pressure.

## **252** 2.5. Properties of aggregates, cement paste, and their interface

In the simulations, we focus on modeling a standard cement paste and a standard limestone aggregate. For cement 253 paste, Young's modulus varies from 30 MPa for a water-to-cement ratio w/c of 0.35 to 15 GPa for a water-to-cement 254 ratio of 0.6 [38]. The Poisson ratio is assumed equal to 0.2. The coefficient of thermal dilatation  $\alpha_s$  of the solid skeleton 255 varies from  $13 \cdot 10^{-6}$  K<sup>-1</sup> to  $20 \cdot 10^{-6}$  K<sup>-1</sup> [39–41]. The permeability of cement highly depends on its water-to-cement 256 ratio and age. Cui and Cahyadi [42] report a permeability of  $2.66 \cdot 10^{-22}$  m<sup>2</sup> for a cement paste with a water-to-cement 257 ratio of 0.3 at 7 days of age and a permeability smaller than  $2.69 \cdot 10^{-23} \text{ m}^2$  at 210 days of age. For a cement paste 258 with a cement-to-water ratio of 0.4, the permeability at 7 days of age is  $8.11 \cdot 10^{-21}$  m<sup>2</sup> and  $1.22 \cdot 10^{-22}$  m<sup>2</sup> at 210 days 259 of age. Heat conductivity of cement paste is 0.53 W.m<sup>-1</sup>.K<sup>-1</sup> for cement without silica fume and 0.33 W.m<sup>-1</sup>.K<sup>-1</sup> for 260 cement paste with silica fume as reported in Xu and Chung [43]. 261

For limestone rocks, the static Young modulus ranges between 18 GPa and 66 GPa [44]. Poisson ratio for limestones 262 vary from 0.11 to 0.45 [45]. Iscan et al. [46] report values of limestone water permeability that range from  $1.67 \cdot 10^{-14}$ 263  $m^2$  to 2.27  $\cdot 10^{-14}$  m. Porosities reported in this study range from 12 % to 18 %. Selvadurai and Głowacki [47] report 264 for Cobourg limestones values of porosity of 1.5 %  $\pm$  0.2 %. This same study reports values of permeability in the 265 range of  $7 \cdot 10^{-18}$  m<sup>2</sup> to  $2.7 \cdot 10^{-20}$  m<sup>2</sup>. Thermal conductivity is reported to be 2.29-2.78 kcal.m<sup>-1</sup>.h<sup>-1</sup>.°C<sup>-1</sup> [48]. The 266 coefficient of thermal expansion  $\alpha_s$  for pure limestone, basalt, granite and gneiss is reported to vary between 0.7 and 267 2.5.10<sup>-6</sup> °C<sup>-1</sup> [49]. For the volumetric heat capacity, Aurangzeb et al. [45] report values ranging from  $1.6 \cdot 10^6$  to 268 2.2 · 10<sup>6</sup> J.m<sup>-3</sup>.K<sup>-1</sup>. For limestone, Biot coefficient is reported to vary from 0.34 to 0.88 and porosity from 4 to 29 % 269 [24]. 270

Failure models are necessary to investigate the failure of the cement paste, the aggregate and the interface. Gu et al. [54] found that paste/aggregate interface failure can be modeled by a Mohr-Coulomb failure criterion, which can be described by the following equation:

$$|\tau| = c + \left(\sigma_{rr} + S_L p_L + S_C p_C\right) \tan(\theta) \tag{29}$$

where  $\tau = \sigma_{r\theta}$  is shear stress acting on the interface,  $\sigma_{rr} + S_L p_L + S_C p_C$  is the effective stress acting normal to the interface (We assume that all irreversible deformations occur at constant volume of the solid matrix, from which the effective stress that intervenes in the failure criterion is the Terzaghi effective stress (extended to partially saturated porous solid) [25].) and where *c* and  $\theta$  are the cohesion and friction angle of the interface, respectively.

For the cement paste and aggregate, we consider a Drucker-Prager failure criterion, which can be expressed by the following equation:

$$f\left(\sigma_{eff}, \sigma_{VM}\right) = B\sigma_{eff} + \sigma_{VM} + A \tag{30}$$

where  $\sigma_{eff} = \sigma_m + S_L p_L + S_C p_C$  is the effective mean stress,  $\sigma_m = \frac{1}{3}tr(\sigma)$  is the mean stress, and  $\sigma_{VM}$  is the Von Mises stress (i.e., the second invariant of the deviatoric stress). The parameters *A* and *B* are called Drucker-Prager parameters. These parameters can be related to the friction angle  $\theta$  and the cohesion *c* of the material [55]. Drucker-Prager parameters can be calculated by the following equations:

$$A = \frac{6c\cos(\theta)}{\sqrt{3}(3\pm\sin(\theta))} \tag{31}$$

$$B = \frac{2\sin(\theta)}{\sqrt{3}(3\pm\sin(\theta))}$$
(32)

For limestone rocks, the friction angle is reported to vary between  $34.5^{\circ}$  and  $45^{\circ}$ . The cohesion is reported to be 23.5 MPa [44]. For the cement paste, the friction angle is reported to vary between  $25^{\circ}$  to  $65^{\circ}$  [53]. For the interface, Gu et al. [54] showed that the friction angle does not depend on the aggregate roughness. The friction angle found in this study is  $35^{\circ}$ , which is similar to values reported in Taylor and Broms [56]. The cohesion of the interface varies from 0.81 MPa to 7.31 MPa, according to this study. These values depend on the nature of the aggregate and its surface roughness. In this study, we consider that the friction angle for both the aggregate and the cement paste is equal to  $35^{\circ}$ .

We use the properties summarized in Table 3 for the aggregate and the cement paste for our simulations.

## **3.** Results and discussion

291

#### **3.1. Individual coated aggregate**

This section first presents the effect of 1 freeze-thaw cycle on an aggregate coated with cement paste. Later in the manuscript, in Section 3.1.2, we discuss the impact of the number of freeze-thaw cycles. We also study the effect of various inputs and situations related to the initial and boundary conditions.

Simulations show that temperature varies almost homogeneously in the system: indeed, at all times, the temperature everywhere differs at maximum by 0.01 °C from the temperature imposed on the edges.

#### 299 3.1.1. Qualitative description of the response to 1 freeze-thaw cycle

Figure 4 and Figure 5 provide the spatial distribution and temporal evolution of liquid saturation, liquid pore 300 pressure, salt concentration, and ice pore pressure in the cement paste and the aggregate during one freeze-thaw cycle. 301 Ice starts to form inside the larger pores upon freezing (i.e., when  $T < T_m$ ). First, positive fluid pressure builds up 302 due to the rapid volume increase imposed by ice formation (because of the difference in density between crystals and 303 liquid water). At this stage, liquid water does not have enough time to escape the pores. While the freezing phase 304 continues from 2 h to 6 h, a depression and over-pressure of the liquid is observed in Figure 5a. Ice continues to form 305 in pores, and the liquid continues to flow to dissipate the pressure. However, with continuous ice formation, the relative 306 permeability becomes lower and lower, which increases the time needed for the pore liquid pressure to dissipate. When 307

the ice blocks the pore, liquid finds it more difficult to travel through the material, and therefore the pressure rises until 308 becoming positive. This competition between ice formation, permeability, and liquid pressure dissipation explains the 309 decrease and increase of liquid pressure for the time intervals [2 h, 3 h] and [3 h, 5 h], respectively. Over the phase 310 where the temperature is constant (during which T = 253.15 K = -20 °C), no additional ice is formed in the material, 311 as can be observed in Figure 5b. The liquid water pressure slowly dissipates when water moves from frozen pores to 312 the outside. At the end of this phase, 10 h into the freeze-thaw cycle, the pore pressure did not have the time to dissipate 313 completely by reaching the atmospheric pressure. At the beginning of the thawing phase, the ice starts melting and, 314 since the molar volume of liquid water is smaller than that of ice, the liquid pore pressure decreases. Concurrently, the 315 permeability increases. 316



Figure 4: Spacial distribution of (a) liquid pressure, (b) liquid saturation, (c) salt concentration, and (d) ice pressure at various temperatures for an individual aggregate coated with cement paste.

At the boundary, the brine pockets with an increasing salt concentration lower the freezing point. Thus, there is no 317 formation of ice in the pores at the vicinity of the outer surface. Figure 5 presents the variation of liquid pressure, liquid 318 saturation, salt concentration, and ice pressure at the center of the aggregate (i.e., r = 0.05 mm), at a position r = 2 mm 319 from the center of the aggregate, at the interface in both the cement paste and the aggregate, and at the outer boundary 320 (i.e., r = 4.3 mm). Note that when the ice saturation is equal to zero (liquid saturation equal to 1) the ice pressure, 321 resulting from the Eq. 22, is fictitious and therefore not physical. This case is that of the negative values in Figs. 4d 322 and 5d. We observe the minimal ice saturation in the cement paste, while the ice saturation is larger at the center of 323 the aggregates than closer to the outer surface. With time, the salt diffusion process in the cement paste increases the 324 liquid saturation in the zones reached by salt. The salt concentration at the boundary decreases when the temperature 325 increases back (i.e., upon thawing). Salt near the surface starts migrating outside and inside the sample, where less 326 salt is present. At the end of the first cycle, not all the salt that penetrated the sample during freezing diffused outside. 327



**Figure 5:** Evolution over time for various points of (a) liquid pressure, (b) liquid saturation, (c) salt concentration and, (d) ice pressure in the individual aggregate coated with cement paste.

We will shed more light on these observations in Section 3.1.2.

Mechanically, liquid pressure variations, thermal behavior of the various phases, and boundary conditions control the stresses (and, consequently, the deformations). Figure 6 shows the resulting distribution of Von Mises (Figure 6a) and effective mean stress (Figure 6b) at various temperatures during the freeze-thaw cycle. High shear stress is observed in the cement paste, reaching a maximum at the paste/aggregate interface. The effective mean stress curve shows that high stresses prevail in the cement paste and the aggregate. Concerning effective mean stress, the highest stresses are observed in the aggregate when reaching the minimal temperature of -20 °C.

## 335 3.1.2. Effect of time and of number of freeze-thaw cycles

Through the freeze-thaw cycles, we observe (Figure 7) that there is an accumulation of salt in pores. Upon freezing, salt penetrates the system, but not all salt flows back outside upon thawing. Therefore, the melting temperature decreases in the zone with larger salt content, implying lesser ice. This mechanism repeats itself, freeze-thaw cycle after freeze-thaw cycle, resulting in less ice formation in zones with high salt concentrations. Therefore, more salt in the pores after a larger number of freeze-thaw cycles helps lower the ice saturation in the pores. Furthermore, Figure 7 shows that the maximal Von Mises stress decreases with an increasing number of freeze-thaw cycles. This decrease is because less ice crystallizes in regions with higher salt concentrations.

In actual materials, once the damage initiates, we know that some material properties differ from the initial ones.



Figure 6: Spacial distribution of (a) Von Mises stress and (b) effective mean stress at various time steps for individual aggregate coated with cement paste.

For example, initiation of cracks in the cement matrix will result in a more permeable material with less mechanical resistance [57]. Thus, lower stresses can still result in a progression of damage over the cycles after damage initiation. With our present poroelastic model, we do not capture such damage. Damage laws should be incorporated into the modeling approach to better model the effect of repeated cycles on the evolution of stress distributions.

#### 348 3.1.3. Role of salt

This section investigates the impact of initial saturation with a solution of NaCl at a concentration of 0, 100, 200, 349 520 mol.m<sup>-3</sup>. We assume that salt has diffused through the whole cement paste before the freeze-thaw cycles. This 350 hypothesis is reasonable because the cement paste thickness in pervious concrete is small (i.e., from 100 µm to 2 351 mm). We consider that the freezing of the sample occurs in an outside salt solution with an initial concentration of 352 520 mol.m<sup>-3</sup>. When the temperature becomes smaller than the solution's freezing point, some of the liquid water in 363 the porosity turns into ice. When a given amount of pure liquid water freezes, its volume increases by +9 %. In the 354 presence of salt in the solution, increasing the concentration decreases the solution's freezing point. Upon freezing 355 the salt solution, dissolved salt diffuses toward the still unfrozen part of the solution and the ice crystals formed are 356 crystals of pure water. As shown in Figure 8, at -20 °C, the ice saturation decreases with an increasing initial salt 357 concentration. Experimental data corroborate such observation: at a given temperature, in various porous media, the 358 amount of unfrozen water determined by the NMR technique increases with an increasing solute concentration (may 350 it be NaCl, KCl, MgCl<sub>2</sub>) [58]. Upon an increase of salt concentration, less ice crystallizes in the pores, and therefore 360 the pore pressures applied to the solid skeleton decrease. Said otherwise, the maximal magnitude of stresses in the 361 cement paste and the aggregate decreases with an increasing salt concentration. Thus, the present poroelastic model 362 predicts that the presence of salt in the pore fluid has a protecting effect against internal damage. 363

Figure 8 presents the Von Mises stress for three initial salt concentrations. The Von Mises stress in this configuration decreases with increasing initial salt concentration. One beneficial aspect of using deicing salt is that it lowers the ice melting temperature. Yuan Jie et al. [59] report that the volume variation during freezing of sodium chloride solution decreases with increasing salt concentrations. However, salt also presents negative effects, such as increasing the degree of saturation due to the concentration differences, potential osmotic pressures due to salt concentration gradient, and salt crystallization in the material's pores.

Experimentally, the presence of salt solution causes maximal damage for an intermediate salt concentration. This pessimum is at a salt concentration of  $\approx 3$  % by weight for various types of salts [13, 14, 60, 61]. According to Yuan Jie et al. [59], the pessimum concentration is due to the competition between positive and negative aspects of NaCl on the freezing behavior, while Valenza and Scherer [12], with the glue-spall theory, rather attribute this pessimum to the impact of salt on the mechanical properties of the ice formed at the surface of the porous solid. In any case, the proposed model does not capture this pessimum, which shows that properly modeling this pessimum requires more physical ingredients (e.g., glue-spall) than those present in the model.

We think that the glue spall will occur in the inter-granular porosity. The ice that forms within these macrovoids



**Figure 7:** Evolution over 10 freeze-thaw cycles of (a) liquid pressure, (b) liquid saturation, (c) salt concentration and (d) Von Mises stress for the individual aggregate coated with cement paste.

will attach to the cement coating. Then, because of the difference in thermal expansion and of the presence of brine
pockets, the ice will stress the cement, which will lead to failure. Since the ITZ in pervious concrete is near the
macrovoid surface, glue spall by the ice could induce significant stresses at the paste/aggregate interface.

Given the small thickness of the cement paste coated layer (which is on the order of a few hundred microns), it is very likely that, after immersion under water, the cement paste becomes saturated very quickly. Consequently, we judge unlikely the fact that including partial saturation into the model would make it possible to capture the salt pessimum. We also judge it unlikely because we do not see *a priori* why partial saturation would make salt more detrimental than in a fully saturated case.

## 386 3.1.4. Effect of boundary conditions on modeling

In the previous sections, we considered that the brine pockets at the boundary are connected so that the salt concentration increases when the temperature decreases (see Figure 3). In other words, since the liquid pressure at the boundary is at atmospheric pressure, the process of cryosuction is not active at the boundary due to the connectivity of the brine pockets. Eriksson et al. [21] considered two extreme cases: an open boundary to simulate fully connected brine pockets and a closed boundary to simulate fully isolated brine pockets. A novelty of our study is that we model and study various connectivity levels. In the present section, to activate the cryosuction at the boundary, we consider that the brine pockets are isolated and relax the hypothesis that the liquid phase is at atmospheric pressure.

We note  $p_L^{lowbound}$  the liquid pressure obtained at the system boundary when assuming that ice around the brine pockets is at atmospheric pressure and that Thomson equation (22) is verified.  $p_L^{lowbound}$  is, therefore, the liquid pressure when the cryosuction is maximum. In such a case, the depression of the liquid at the boundary is equal to  $p_L^{lowbound} - p_{atm}$ . In the present section, we consider that only a fraction X of this depression applies, and therefore that the liquid



**Figure 8:** (a) Liquid pressure, (b) liquid saturation, (c) salt concentration, (d) ice pressure, (e) Von Mises stress, and (f) effective mean stress for various initial conditions at t = 6 h corresponding to the beginning of the -20 °C plateau for individual aggregate coated with cement paste.

<sup>398</sup> pressure  $p_L$  at the boundary verifies:

$$p_L - p_{atm} = X \left( p_L^{lowbound} - p_{atm} \right) \tag{33}$$

399

The non-connectivity of the brine pockets increases with the magnitude of X. We consider three different fractions.



Figure 9: Liquid pressure  $p_L$  applied at the boundary for various brine pockets connectivities.

Each fraction is related to the degree of connectivity of the brine pockets at the system boundary. When X is equal to 0, we ensure  $p_L = p_{atm}$ , which means that the brine pockets are totally connected and that there is no cryosuction at the boundaries, like in the simulations performed in Sections 3.1.1, 3.1.2 and 3.1.3. In the case X = 1, the cryosuction is fully active at the boundary and  $p_L = p_L^{lowbound}$ . Figure 9 represents the liquid pressure at the boundary for X = 0.2, X = 0.5, and X = 0.9. We then use the calculated liquid pressure to solve Equation (22) to obtain the salt concentration at the boundary.

Figure 10 presents the liquid saturation, liquid pressure, salt concentration and Von Mises stress for different brine 406 connectivities ranging from fully connected brine pockets (i.e., X = 0 and  $p_L = p_{atm}$ ) to partially connected brine 407 pockets (X = 0.2, X = 0.5, X = 0.9) at t = 6 h corresponding to the beginning of the -20 °C plateau. We observe 408 that the less the brine pockets are connected, the lower the salt concentration at the boundary. Therefore, less salt 409 diffuses toward the inside of the material, compared to the case of fully connected brine pockets. We observe low 410 liquid saturation and maximum stresses for the case with a higher non-connectivity degree (i.e., X = 0.9). Also, the 411 connectivity of the brine pockets impacts the localization of the maximal stresses. For X = 0.9, the maximal stress is 412 at the surface of the cement paste, not in the vicinity of the paste/aggregate interface. We find that the maximal shear 413 stress is located at the interface for the case X = 0.5. 414

We conclude that the hydraulic and salt concentration boundary conditions significantly impact the response of the material subject to freeze-thaw cycles in the presence of salt and saturated conditions. We can speculate that various types of boundary conditions can be present at various locations on the concrete surface. Indeed, some zones at the surface can be in contact with brine pockets, while others can be in contact with pure ice. Experimental work is necessary to fully understand the behavior of the frozen solution at the outer surface of the concrete.

## 420 3.1.5. Influence of various material properties on the response to freeze-thaw cycles

In this section, we investigate the impact of various cement paste and aggregate properties. We investigate the impact of porosity, permeability, and coefficient of thermal expansion, for both cement paste and aggregate.

We consider the porosity couples reported in Table 5 to estimate the impact of the porosity of cement paste and aggregates. The other materials parameters are kept unchanged and correspond to the values summarized in Table 3. Figure 11-a presents the resulting Von Mises stress distribution at t = 6 h. We find that the porosity does not impact much the Von Mises stress maximal value.

To estimate the impact of the coefficient of thermal expansion of cement and aggregate, we consider the values



**Figure 10**: (a) Liquid pressure, (b) liquid saturation, (c) salt concentration and (d) Von Mises stress for various boundary conditions at t = 6 h corresponding to the beginning of the -20 °C plateau for individual aggregate coated with cement paste.

reported in Table 4. We find (see Figures 11-c and 11-d) that the higher the difference between the coefficient of thermal
expansion of the cement paste and the aggregate, the higher the maximal stress at the interface. The maximal stress does
not depend on those two coefficients independently but on the mismatch between those two coefficients. The magnitude
of the stresses can double when the coefficients of thermal expansion for paste and aggregate span a realistic range.
Consequently, the cement and aggregate dilation mismatch could explain part of the damage that concrete sustains
when subjected to freeze-thaw cycles. Therefore, it might be essential to lower the mismatch between cement paste
and aggregate coefficient of thermal expansion to improve the freeze-thaw durability of pervious concrete.

From Figures 11-c and 11-d we also observe that, in the absence of thermal mismatch, the maximal stress at the interface would be about five times smaller than the thermal mismatch obtained with the material properties given in Table 3. Consequently, for the pervious concretes here simulated, it appears that stresses are mostly of thermal origin and that poromechanical effects per se are of second order.

We investigate the impact of permeability for the various permeabilities reported in Table 6. We find that the lower the cement paste permeability, the higher the maximal Von Mises stress, as observed in Figure 11. A lowpermeability cement paste (i.e., a paste with  $k_{paste} = 10^{-22} \text{ m}^2$ ) exhibits the highest stress at the interface among all our simulations. The stresses at the interface can increase by a factor of 1.5 when the permeability of cement paste decreases from  $1 \cdot 10^{-21} \text{ m}^2$  to  $1 \cdot 10^{-22} \text{ m}^2$ . The high permeability of the cement paste allows fast dissipation of the liquid pore pressure, which dissipates the tensile stresses that might develop. The impact of variations of thermal expansion coefficient and permeability on the stresses is larger than that of the variations of porosity of the cement paste and aggregates.



**Figure 11:** Influence of cement paste and aggregates properties on Von Mises stress (at t = 6 h corresponding to the beginning of the -20 °C plateau) for an individual aggregate coated with cement paste: (a) porosity, (b) permeability, (c) coefficient of thermal expansion and, (d) Von Mises stress at the interface as function of coefficient of thermal expansion mismatch.

Coefficient of thermal expansion $\alpha$	
Aggregate	at the interface (MPa)
$\alpha_{agg} = 2.2 \cdot 10^{-6} \text{ K}^{-1}$	6.04
$\alpha_{agg} = 10 \cdot 10^{-6} \text{ K}^{-1}$	1.16
$\alpha_{agg} = 2.2 \cdot 10^{-6} \text{ K}^{-1}$	1.16
$\alpha_{agg} = 2.2 \cdot 10^{-6} \text{ K}^{-1}$	8.04
$\alpha_{agg} = 2.2 \cdot 10^{-6} \text{ K}^{-1}$	7.02
$\alpha_{agg} = 2.2 \cdot 10^{-6} \text{ K}^{-1}$	3.73
$\alpha_{agg} = 2.2 \cdot 10^{-6} \text{ K}^{-1}$	2.09
	$\begin{array}{c} \text{rmal expansion } \alpha \\ & \text{Aggregate} \\ \hline \alpha_{agg} = 2.2 \cdot 10^{-6} \text{ K}^{-1} \\ \alpha_{agg} = 10 \cdot 10^{-6} \text{ K}^{-1} \\ \alpha_{agg} = 2.2 \cdot 10^{-6} \text{ K}^{-1} \\ \end{array}$

#### Table 4

Coefficients of thermal expansion and resulting maximum stress at the interface for the various parametric simulations.

#### 447 3.1.6. Influence of the presence of a crack

This section explores the response of the same system as the previous one (i.e., one aggregate coated with cement paste) but in the presence of a crack in the cement paste layer. We presented the geometry of the system in Figure 2. In this case, the system's boundary (on which the boundary conditions are applied) is the outside surface of the cement paste, the crack lips, and the exposed aggregate surface. Mechanically, the crack lips are free from mechanical stress. The temperature, salt concentration, and liquid pressure at the boundary are similar to the boundary conditions used in Section 3.1. Figure 12 shows the mean effective stress and the Von Mises stress at the vicinity of the crack. In the aggregate and the cement paste, both stresses are maximal close to the crack tip. We can attribute this high stress to

Poros	ity $\phi$	Maximal Von Mises stress
Cement	Aggregate	at the interface (MPa)
$\phi_{paste} = 0.3$	$\phi_{agg} = 0.04$	4.4
$\phi_{paste} = 0.35$	$\phi_{agg} = 0.04$	4.43
$\dot{\phi}_{paste} = 0.4$	$\phi_{agg} = 0.04$	4.44
$\phi_{naste} = 0.3$	$\phi_{agg} = 0.02$	4.28
$\phi_{paste} = 0.3$	$\phi_{agg} = 0.01$	4.16
$\phi_{paste} = 0.2$	$\phi_{agg} = 0.04$	4.13
$\phi_{paste} = 0.1$	$\phi_{agg} = 0.04$	3.62

#### Table 5

Porosities and resulting maximum stress at the interface for the various parametric simulations.

Permeab	ility $(k)$	Maximal Von Mises stress at
Cement	Aggregate	the interface (MPa)
$k_{paste} = 10^{-21} \text{ m}^2$	$k_{agg} = 10^{-20} \text{ m}^2$	4.4
$k_{paste} = 10^{-22} \text{ m}^2$	$k_{agg} = 10^{-20} \text{ m}^2$	6.22
$k_{paste} = 10^{-23} \text{ m}^2$	$k_{agg} = 10^{-20} \text{ m}^2$	19.7
$k_{paste} = 10^{-19} \text{ m}^2$	$k_{agg} = 10^{-20} \text{ m}^2$	4.2
$k_{paste} = 10^{-16} \text{ m}^2$	$k_{agg} = 10^{-20} \text{ m}^2$	4.2
$k_{paste} = 10^{-21} \text{ m}^2$	$k_{agg} = 10^{-16} \text{ m}^2$	4.3
$k_{paste} = 10^{-21} \text{ m}^2$	$k_{agg} = 10^{-22} \text{ m}^2$	4.3

## Table 6

Permeabilities and resulting maximum stress at the interface for the various parametric simulations.



Figure 12: (a) Displacement, (b) effective mean stress and (c) Von Mises stress at -20  $^{\circ}$ C at 6 h for individual aggregate coated with fractured cement paste.

the noticeable difference between the aggregate and cement paste coefficient of thermal expansion. Upon freezing, the
crack opens because the edges of the two cement lips move in opposite directions due to their contraction, as shown
in Figure 12. The stresses in the aggregate and cement paste far from the crack are the same as in the intact system.



Figure 13: (a) Liquid pressure, (b) liquid saturation, and (c) salt concentration at -20  $^{\circ}$ C at 6 h for two aggregates coated and bonded with cement paste.

## **3.2.** System of two cemented aggregates

This section aims to study a more complex geometry consisting of two aggregates coated and bonded with cement paste. This geometry aims at modeling the behavior of pervious concrete at the level of its constituents by considering the mechanical interaction between the aggregates and the cement that binds and coats them. In this section, we limit the study to the case of connected brine pockets (see Section 3.1.4 for the impact on boundary conditions). We summarize the value of materials parameters in Table 3. Figure 2-b displays the simulated geometry.

## **3.2.1.** Qualitative description of the response to 1 freeze-thaw cycle

405 Simulations show that temperature varies almost homogeneously in the system: indeed, at all times, the temperature 406 everywhere differs at maximum by 0.01 °C from the temperature imposed on the edges.

We focus on the mechanical response of this system to the freeze-thaw solicitation. Figure 13 shows the liquid pressure, liquid saturation, and salt concentration at t = 6 h. Figure 14 shows the Von Mises stress in the system at various times. Around t = 10 h, at which time the temperature reached its minimal value T = -20 °C, the Von Mises stress is maximal at the level of the contact between the two aggregates. The fact that the aggregates block the cement paste deformation due to their different coefficients of thermal expansion could explain the high shear stress in this contact region. Moreover, we also observe significant shear stresses at the interface between aggregates and cement paste, but those shear stresses remain small compared to the stresses developed in the contact region.

Figure 15 displays the effective mean stress  $\sigma_m^{eff} = \sigma_m + S_L p_L + S_C p_C$  in the system at various times in the 474 freezing process. The figure shows that significant tensile stresses prevail at the aggregate center. The fact that the 475 drainage length in the cement paste is larger for water in the contact region than outside the contact region could explain 476 the tensile stresses prevailing in the contact region. The stresses start decreasing after they have reached a maximum 477 value, between 8 h to 10 h after the beginning of the cycle, when the temperature has reached -20  $^{\circ}$ C. The decrease 478 is due to water flowing to the outside boundary, as we observed for one aggregate coated with a cement paste layer. 479 The combined effect of the Von Mises stress and mean effective stress will be discussed later in the paper by using the 480 Drucker-Prager criterion. 481



Figure 14: Von Mises stress for two aggregates coated and bonded with cement paste at -20  $^{\circ}$ C at (a) 6 h, (b) 8 h, and (c) 10 h.

# **3.2.2.** Influence of coefficients of thermal expansion on response to freeze-thaw cycle

In this section, we study the impact of the coefficients of thermal expansion on the behavior of the two aggregates 483 coated and bonded with cement paste. Figure 16 shows that the larger the difference between the coefficient of ther-484 mal expansion of aggregates and cement paste, the larger the stress developed in the contact region between the two 485 aggregates and at the paste/aggregate interface. The stress is maximal for the simulations with the largest mismatch of 486 coefficients of thermal expansion. In Figure 16b we present the stress for a system with equal coefficient of thermal 187 expansion for the cement paste and the aggregates. We notice that the shear stresses are much lower than in the case 488 of mismatch, with maximal shear stresses in the contact region and the aggregate. The trends observed on the system 489 made of two aggregates concerning thermal mismatch are consistent with those observed on the system made of one 490 aggregate and discussed in Section 3.1.5. 491

# **3.3.** Identification of regions where damage is most likely to occur

This section introduces failure criteria to predict whether, upon freezing, the materials are susceptible to get damaged. This approach allows us also to identify the regions where damage is most likely to occur. We consider a Mohr-Coulomb criterion for the interface and a Drucker-Prager criterion for cement paste and the aggregates, as already mentioned in Section 2.5. The parameters for the two criteria are in Table 3.

# 497 3.3.1. Interface

Figure 17 displays the quantity  $|\tau| - (\sigma_{rr} + S_L p_L + S_C p_C) \tan(\theta)$ , which is homogeneous to a stress, at the interface. If this quantity is larger than the cohesion of the interface, failure should occur. The zone where damage is likely to occur is the interface close to the contact region between the two aggregates. The interface must have a cohesion larger than 9 MPa to avoid failure for the chosen materials and freezing conditions. This value is very large for paste/aggregate interfaces. Indeed, Jebli et al. [62] report a cohesion of 3 MPa for the paste/aggregate interface.

Using a poromechanical model, Rahman and Grasley [18] showed that high tensile stresses develop at the ITZ because of the mismatch of coefficient of thermal expansion between the aggregate and the matrix. Callan [63] obtained similar results. Cwirzen and Penttala [64] showed experimentally that the ITZ properties govern the damage process under salt-frost attacks of non-air-entrained high-performance concretes. Therefore, enhancing the cement paste durability without enhancing the paste/aggregate interface durability may be insufficient to enhance concrete durability since the interface plays a significant role.



Figure 15: Effective mean stress for two aggregates coated and bonded with cement paste at -20  $^{\circ}$ C at (a) 6 h, (b) 8 h, and (c) 10 h.

# 509 3.3.2. Aggregate and cement paste

We now study damage in the aggregate and the cement paste by considering a Druker-Prager failure model for those two phases. Figure 18 presents the value of the quantity  $B\sigma_m^{eff} + \sigma_{VM}$ , which is homogeneous to a stress, in the aggregates and the coating cement paste, for the system made of two aggregates coated and bonded with cement paste. Failure could occur if this quantity is larger than the considered Drucker-Prager material parameter A, which is related to the cohesion of the material. In other words, to avoid damage in the cement paste, we need to ensure that  $A > B\sigma_m^{eff} + \sigma_{VM}$ . From Figure 18, we conclude that, in the cement paste and the aggregates, failure is the most likely to occur in the contact region between the aggregates.

## 517 3.3.3. Comparison of modeling results with experiments from literature

Experimentally, having a weak paste/aggregate cohesion will result in failure at the level of the interface. In the 518 recent work by Song et al. [65], the authors study the role of the interface transitional zone in pervious concrete 519 during freeze-thaw cycles in the presence of salt. Using SEM analysis, the authors show that the main cause of 520 damage is the interface debonding during the freeze-thaw cycles. Our model provides results in accordance with these 521 observations, as it shows the significant role of the paste/aggregate interface properties. Song et al. [65] also explain 522 that an inconsistency between the deformations of aggregate and cement paste is a critical mechanism of damage. 523 Callan [63] showed that high tensile stress at the ITZ is developed due to the mismatch of coefficient of thermal 524 expansion between the aggregate and the matrix. Our model is also consistent with this observation, as we show that 525 the mismatch in thermal dilation coefficient can lead to significant stresses at the interface. 526



**Figure 16:** Von Mises stress for two aggregates coated and bonded with cement paste at -20 °C (6 h) for various coefficients of thermal expansion. (a) Case 1:  $\alpha_{agg} = 2.2 \cdot 10^{-6} \text{ K}^{-1}$  and  $\alpha_{paste} = 17 \cdot 10^{-6} \text{ K}^{-1}$ . (b) Case 2:  $\alpha_{agg} = 10 \cdot 10^{-6} \text{ K}^{-1}$  and  $\alpha_{paste} = 10 \cdot 10^{-6} \text{ K}^{-1}$ . (c) Case 3:  $\alpha_{agg} = 2.2 \cdot 10^{-6} \text{ K}^{-1}$  and  $\alpha_{paste} = 23 \cdot 10^{-6} \text{ K}^{-1}$ .



**Figure 17:** Quantity  $|\tau| - \sigma_{rr} \tan(\theta)$  at -20 °C at (a) 6 h, (b) 8 h, and (c) 10 h for two aggregates coated and bonded with cement paste.



**Figure 18:** Quantity  $B\sigma_m^{eff} + \sigma_{VM}$  at -20 °C at (a) 6 h, (b) 8 h, and (c) 10 h for two aggregates coated and bonded with cement paste.

# 527 4. Conclusions

We developed a poromechanical model to simulate the freezing of porous solids in saturated conditions and in the presence of dissolved salts. We used this poromechanical approach to gain insight into the damage of pervious concrete at the level of a few aggregates coated and bonded with cement paste. We used the model to calculate the stresses and ice saturation distributions in various systems with various boundary conditions, upon freeze-thaw cycles, in the presence of deicing salts. Based on the various simulations presented earlier in the manuscript, the most important conclusions of this work are:

- Significant tensile effective stresses prevail in the center of the aggregates upon freezing because of the crystallization of significant volume fractions of ice.
- Significant shear stresses develop within the cement paste upon freezing. They reach a maximum value at the paste/aggregate interface and in the contact zone between aggregates.
- These stresses could exceed the strength of cement paste and the aggregates, inducing damage during the repeated freeze-thaw cycles. Such damage is the most likely to occur at the paste/aggregate interface or in the contact zone between two aggregates.
- Salt accumulates in the material over repeated freeze-thaw cycles and therefore makes the shear stresses in the cement paste layer decrease with the number of cycles. We cannot retrieve a salt pessimum with the physical ingredients implemented in the model, although several observed this pessimum experimentally. This inability shows that we must find the physical reason for this salt pessimum elsewhere.
- The shear stresses within the cement paste layer depend significantly on the mismatch between the coefficients of thermal expansion of the cement paste and the aggregate. The magnitude of those stresses can double when those coefficients for cement paste and aggregates span a realistic range. For the pervious concretes here modeled and the conditions considered, thermomechanical effects are more significant than poromechanical effects. Therefore, designing pervious concrete mixtures with a minimized mismatch of coefficient of thermal expansion could prove an efficient way to improve the freeze-thaw durability of pervious concrete.
- The shear stresses within the cement paste layer depend significantly on the cement paste permeability also. Those stresses can increase by a factor of 1.5 when the cement paste permeability decreases from  $1 \cdot 10^{-21}$  m<sup>2</sup> to  $1 \cdot 10^{-22}$  m<sup>2</sup>.
- The porosity of the cement paste has a much smaller impact on the magnitude of stresses generated during freeze-thaw than the coefficient of thermal expansion or the permeability.
- The ice brine mixture, formed at the surface of the cement paste upon freezing, is composed of ice and brine pockets more or less interconnected. The degree of connectivity of such brine pockets significantly impacts the stresses generated in the cement paste. Larger connectivity generates lower stresses than those obtained with a lower degree of connectivity.
- If the layer of cement paste has cracked, significant stresses are generated at the crack during freezing because of the contraction of the two cement lips in opposite directions.
  - Enhancing the cement paste durability without enhancing the durability of the paste/aggregate interface may not be sufficient to improve the concrete durability, as the impact of the paste/aggregate interface on the concrete durability is significant.

The model developed in the present work makes it possible to calculate the stresses in cement-based materials, particularly pervious concrete, under frost attacks. This model can help quantify the stress states under various conditions. It can also orient reflections on materials properties to design concretes that resist better frost attacks in the presence of deicing salt. However, we should improve the model by considering incorporating glue-spall to explain the experimentally observed salt pessimum. Also, to quantitatively assess the impact of repeated freeze-thaw cycles, it is necessary to implement a damage model that considers the decay of the resistance of the aggregates, the cement paste, and their interface. Moreover, including the interfacial transition zone (ITZ) in the simulations could be interesting to

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assess its impact on the system properties and damage patterns. One could employ the model to simulate more realis-572 tic geometries in three dimensions to consider more complex geometries involving more than two aggregates. Since, 573 using finite-elements method would be numerically very costly, we propose to identify the damage mechanism and 574 the evolution of the contact between aggregates using FEM. Then, it is possible to envision coarse-grained methods, 676 such as Discrete Elements Method (DEM), to perform simulation yielding macroscopic properties. Furthermore, such 576 simulations will make it possible to compare our modeling results with experimental data such as strength measure-577 ments (e.g., by uniaxial compression) or stiffness measurements (e.g., by ultrasounds). Such upscaling could be done 578 numerically for instance, by using DEM modeling, in which the contact law between the discrete elements (i.e., the 579 aggregates) would be fitted on the results from our present finite element calculations. 580

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